

# Searches for Quantum Decoherence at Belle and Belle II

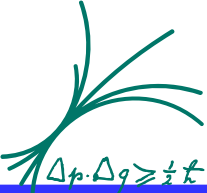


**Entanglement of B-Mesons in  $Y(4s)$  decays  
(Super)KEKB and Belle (II)  
 $B^0$  Oscillations and CP Violation  
Can Bell's Inequality be checked?**

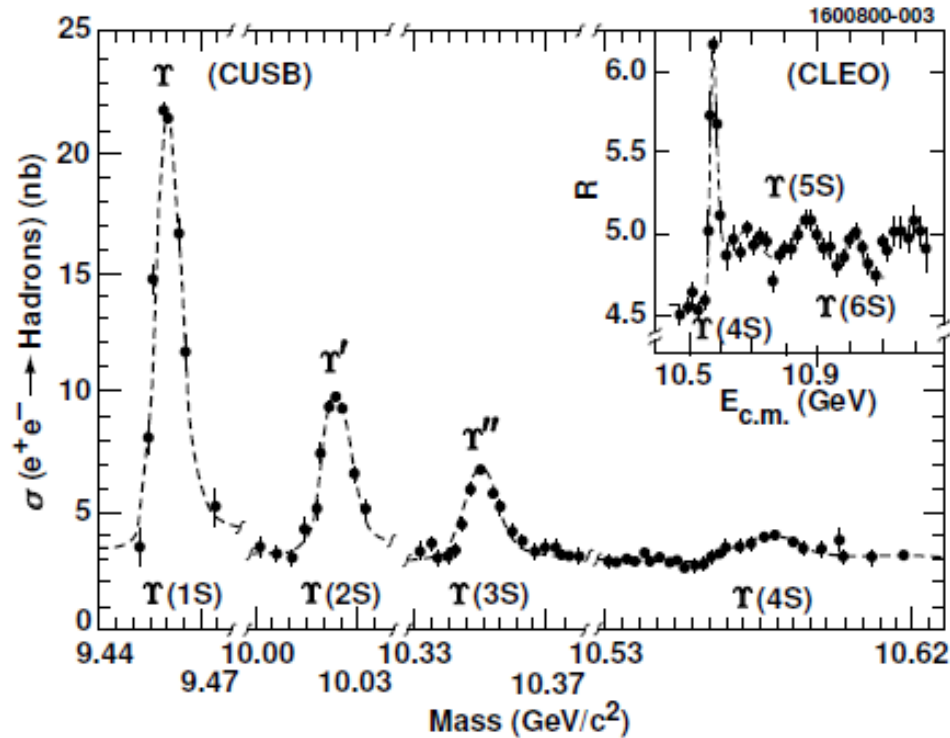
**Hans-Günther Moser  
MPI für Physik  
On behalf of Belle and Belle II**



**Effects of decoherence on time dependent measurements  
Indirect indicators  
Measurement at Belle  
Plans at Belle II  
Conclusions**



# Y(4s)



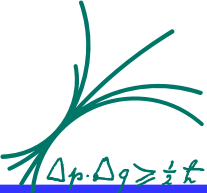
$$e^+ e^- \rightarrow Y(4s) \rightarrow B^0 \bar{B}^0$$

$$m(Y(4s)) = 10.579 (\Gamma=0.0205) \text{ GeV}$$

$$2 \times m(B^0) = 10.558 \text{ GeV}$$

$$\Delta E = 21 \text{ MeV}$$

$$m(B^*) - m(B) = 45.2 \text{ MeV}$$



# Entanglement in $Y(4s)$ decays

$B^0/\bar{B}^0$  from a  $Y(4s)$  decay are supposed to be in an entangled state

$$\Psi = \frac{1}{\sqrt{2}} [ |B^0(p)\rangle |\bar{B}^0(-p)\rangle - |\bar{B}^0(p)\rangle |B^0(-p)\rangle ]$$

If one B decays, the common wave function collapses and the  $B^0/\bar{B}^0$  are in a defined state.

$\gamma\beta c\tau/r(B^0) \sim 5 \times 10^{10} \Rightarrow$  well separated spatially

Our measurements of  $\Delta m_d$  and TDCPV are based on the entanglement (B-tag)

- 1) Can we demonstrate the entanglement (e.g. checking Bell's inequality ?)
- 2) How certain are we that the entanglement is always 100% ?

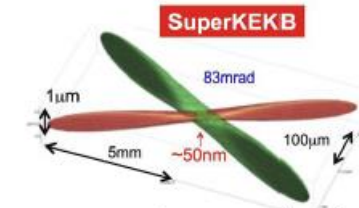
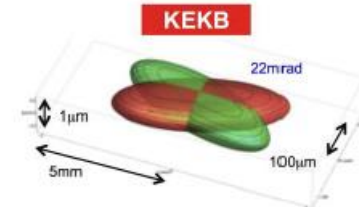
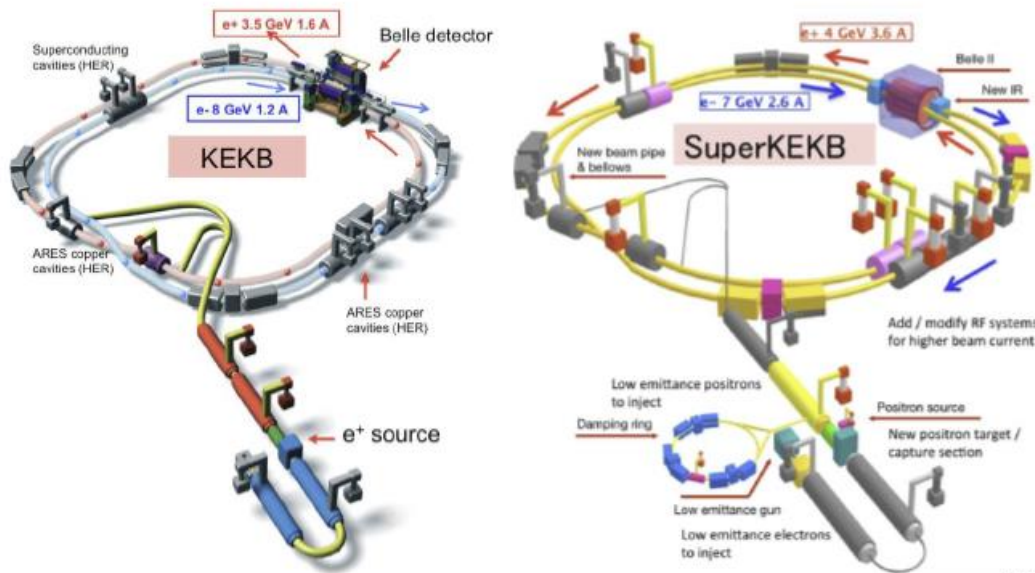
$Y(4s) \rightarrow B^0 \bar{B}^0 \gamma$

decoherence due to interaction with (BSM) background fields

Such effects could lead to systematic errors of our TDCPV measurements



## From KEKB to SuperKEKB



$$\mathcal{L} = \frac{\gamma_{\pm}}{2e r_e} \left( 1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \frac{I_{\pm} \xi_{y\pm}}{\beta_{y\pm}} \left( \frac{R_L}{R_{\xi y}} \right)$$

- moderately increased beam currents
- Squeeze beams @IP by ~1/20

$$\mathcal{L}_{II}^{\text{peak}} \approx 30 \times \mathcal{L}_I^{\text{peak}}$$

$$\int^{\text{goal}} \mathcal{L}_{II} dt = 50 \text{ ab}^{-1} \approx 50 \int \mathcal{L}_I dt$$

3

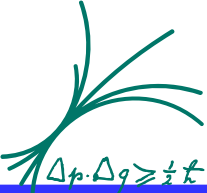
KEKB:  
1999-2010

$$\beta\gamma = 0.42 \quad (8 \text{ GeV}, 3.5 \text{ GeV})$$

	KEKB/Belle	SuperKEKB/Belle II	
		achieved	target
$\mathcal{L}_{\text{peak}}$ [cm <sup>-2</sup> s <sup>-1</sup> ]	2.1×10 <sup>34</sup>	<b>4.7×10<sup>34</sup></b> <b>world record</b>	~6×10 <sup>35</sup>
$\mathcal{L}_{\text{int}}$ [fb <sup>-1</sup> ]	1,004 (711 <sub>Y(4S)</sub> )	<b>424</b> <b>(362<sub>Y(4S)</sub>)</b>	50,000
$N(B\bar{B})_{Y(4S)}$	772×10 <sup>6</sup>	<b>387×10<sup>6</sup></b>	~5×10 <sup>10</sup>

superKEKB:  
2019 - .....

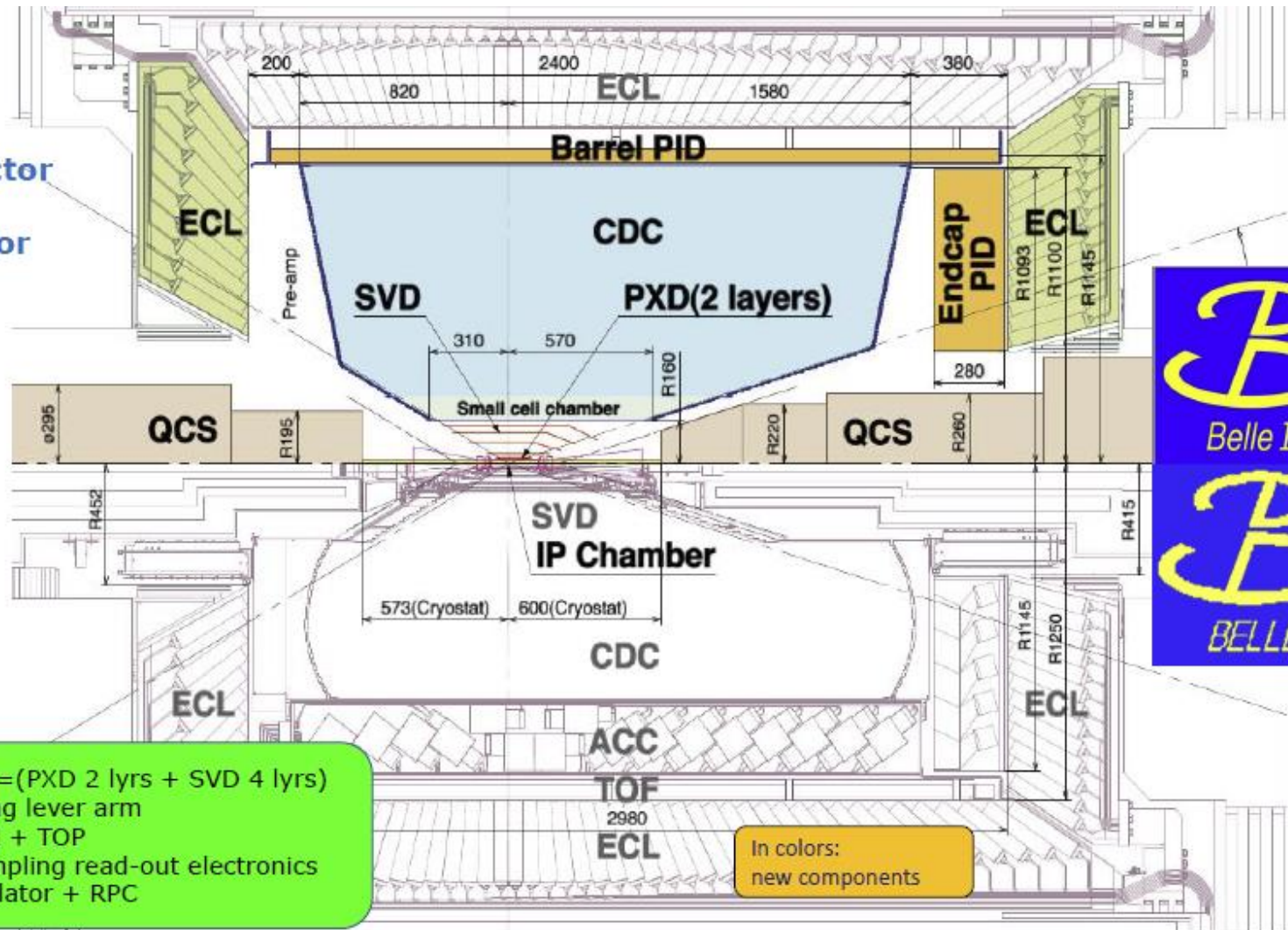
$$\beta\gamma = 0.28 \quad (7 \text{ GeV}, 4 \text{ GeV})$$



# Belle (II)

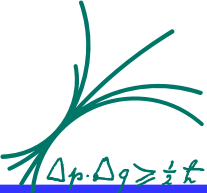


Belle II detector  
Vs.  
Belle detector



SVD: 4 lyrs → VXD=(PXD 2 lyrs + SVD 4 lyrs)  
 CDC: small cell, long lever arm  
 ACC+TOF → ARICH + TOP  
 ECL: waveform sampling read-out electronics  
 KLM: RPC → Scintillator + RPC





# B<sup>0</sup> $\bar{B}^0$ mixing

Due to weak interaction a B<sup>0</sup> can transform into its antiparticle  
Formally this is described by a new (weak) base of B<sub>L</sub><sup>0</sup> and B<sub>H</sub><sup>0</sup>

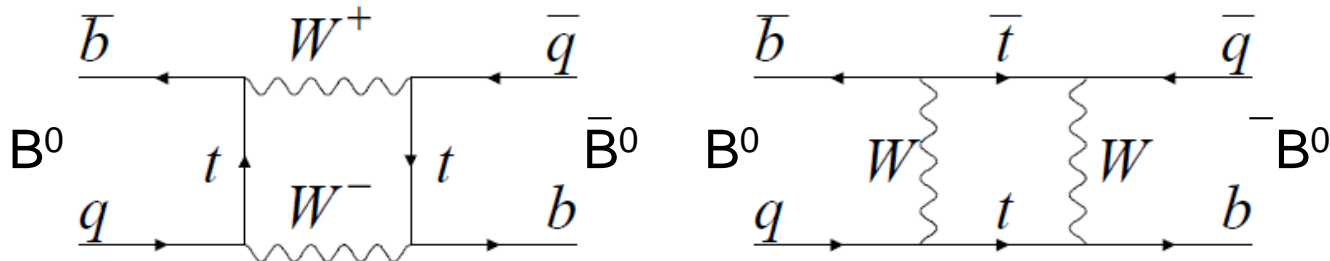
$$|B_{L,H}\rangle = p|B_q^0\rangle \pm q|\bar{B}_q^0\rangle \quad |p/q| = 1 \text{ (CP cons.)}$$

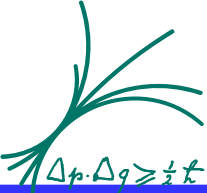
These two states interfere and resulting in time dependent oscillations

$$P(B^0 \rightarrow \bar{B}^0) = \frac{1}{2} \Gamma \exp(-\Gamma t) (1 - \cos(\Delta m t))$$

$$P(B^0 \rightarrow B^0) = \frac{1}{2} \Gamma \exp(-\Gamma t) (1 + \cos(\Delta m t))$$

$\Delta m$ : mass difference of B<sub>H</sub><sup>0</sup> and B<sub>L</sub><sup>0</sup>





# CP violation

Weak interaction is also a source for CP violation

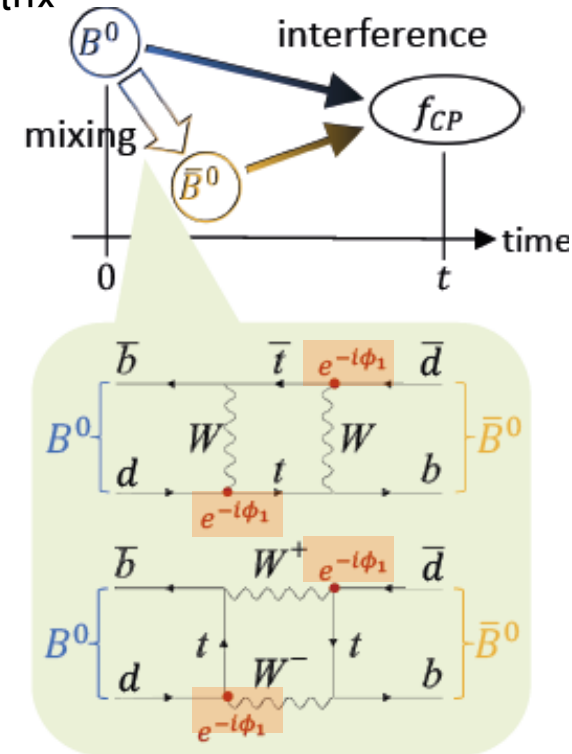
CP violation is a consequence of the complex phase of the CKM matrix

It happens if two (or more) weak amplitudes interfere

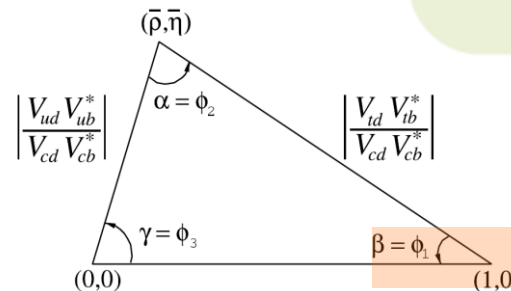
$$\begin{aligned}
 A_f(B^0 \rightarrow f) &= A_1 \exp(i\phi_w) + A_2 \exp(i\phi_s) \\
 A_b(\bar{B}^0 \rightarrow \bar{f}) &= A_1 \exp(-i\phi_w) + A_2 \exp(i\phi_s) \quad \Rightarrow |A_f|^2 \neq |A_b|^2
 \end{aligned}$$

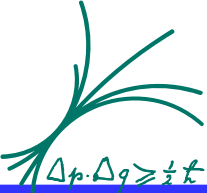
In decays this happens either by interference of different decay amplitudes (tree and penguin)  
 or (more important) by interference of mixing and decay

Precise measurements of CP violation are the primary goals of the Belle and Belle II experiments

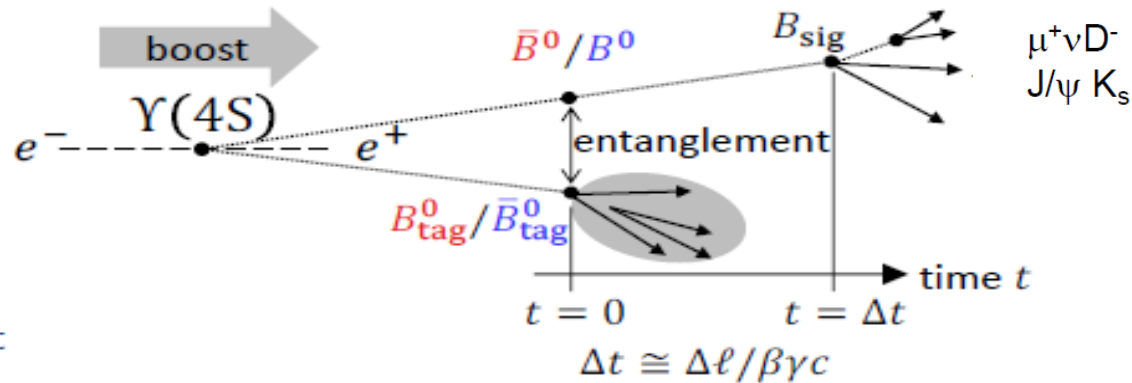


$$V_{CKM} \equiv V_L^u V_L^{d\dagger} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$





# Phenomenology



$Y(4s)$  created at  $t=0$  and decays in  $B^0/\bar{B}^0$

**Tag:** one  $B^0$  decays at  $t_1$  in a way that we know whether it is  $B^0$  or  $\bar{B}^0$  (e.g.  $\mu^+ \nu D^-$ )  
(in practice: use a BDT or NN to determine the decay state)

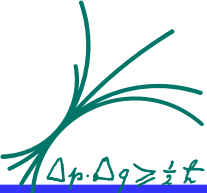
The other  $B^0$  (always in the opposite state because of entanglement) starts oscillating

**Sig:** the other  $B^0$  decays at  $t_2$  in the signal mode we are interested in

oscillation ( $\Delta m$ ) measurement:	$\mu^+ \nu D^-$
CP violation ( $\sin(2\beta)$ ):	$J/\psi K_s$

From the spatial separation and the known boost we determine  $\Delta t = t_2 - t_1$





# Phenomenology

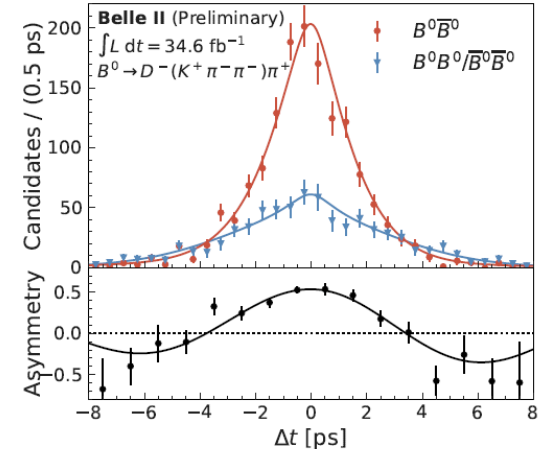


## Oscillations:

$$P(B^0 \rightarrow \bar{B}^0) = \frac{1}{2} \Gamma \exp(-\Gamma \Delta t) (1 - \cos(\Delta m \Delta t))$$

$$A_{osc} = \frac{N(B^0 \rightarrow B^0) - N(B^0 \rightarrow \bar{B}^0)}{N(B^0 \rightarrow B^0) + N(B^0 \rightarrow \bar{B}^0)} = \cos(\Delta m \Delta t)$$

*In reality: take into account mistag, resolution, background*



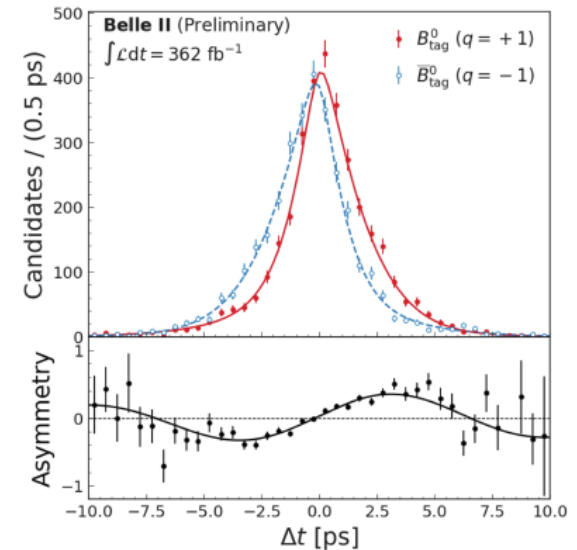
## Mixing induced (or time dependent) CP violation (TDCPV):

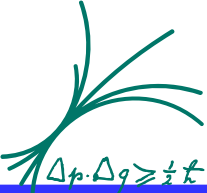
'Golden mode'  $\bar{B}^0(q=+1); B^0(q=-1) \rightarrow J/\psi K_s$

$$P(\Delta t, q) = \frac{1}{4} \Gamma \exp(-\Gamma \Delta t) \{1 + q [S \sin(\Delta m \Delta t) - C \cos(\Delta m \Delta t)]\}$$

For  $J/\psi K_s$   $S = \sin(2\beta)$   $C \sim 0$

$$a_{CP} = \frac{N(\bar{B}^0 \rightarrow f_{CP}) - N(B^0 \rightarrow f_{CP})}{N(\bar{B}^0 \rightarrow f_{CP}) + N(B^0 \rightarrow f_{CP})} = S \sin(\Delta m \Delta t)$$





# Can we check Bell's inequality?

Classical Aspect type correlation experiment  
 A. Aspect et al, Phys. Rev. Lett 49, 1804 (1982)

correlation coeffs in data vs QM  
 optimum relative angles 22.5° and 67.5°

spin-singlet state of photons or particles:  $\frac{1}{\sqrt{2}} [|\uparrow\rangle_1 |\downarrow\rangle_2 - |\downarrow\rangle_1 |\uparrow\rangle_2]$

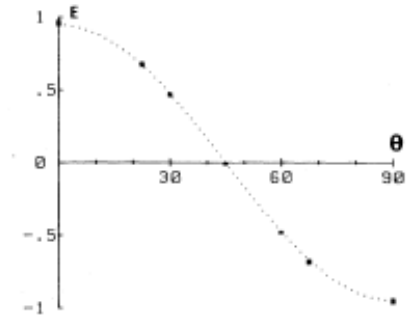
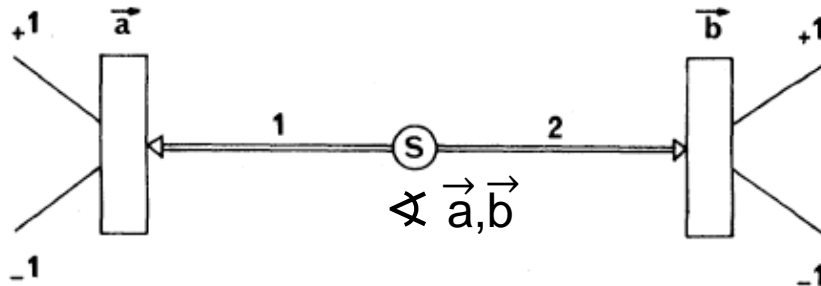


FIG. 3. Correlation of polarizations as a function of the relative angle of the polarimeters. The indicated errors are  $\pm 2$  standard deviations. The dotted curve is not a fit to the data, but quantum mechanical predictions for the actual experiment. For ideal polarizers, the curve would reach the values  $\pm 1$ .

- Bell's Theorem (via Clauser, Horne, Shimony, and Holt):

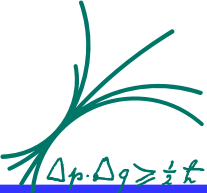
- correlation coeff:  $E(\vec{a}, \vec{b}) = \frac{R_{++}(\vec{a}, \vec{b}) + R_{--}(\vec{a}, \vec{b}) - R_{+-}(\vec{a}, \vec{b}) - R_{-+}(\vec{a}, \vec{b})}{R_{++}(\vec{a}, \vec{b}) + R_{--}(\vec{a}, \vec{b}) + R_{+-}(\vec{a}, \vec{b}) + R_{-+}(\vec{a}, \vec{b})}$

- $S = E(\vec{a}, \vec{b}) - E(\vec{a}, \vec{b}') + E(\vec{a}', \vec{b}) + E(\vec{a}', \vec{b}')$

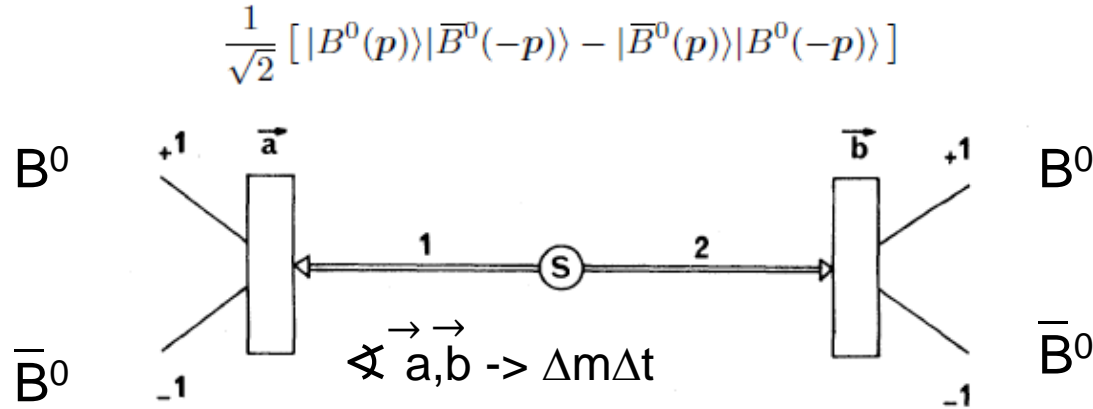
- $|S| \leq 2$  for any local realistic model;  $S_{QM} = \pm 2\sqrt{2}$  for optimal settings

$S = 2.697 \pm 0.015; \text{ cf. } S_{QM} = 2.70 \pm 0.05$

Replace  $\uparrow$  by  $B^0$  and  $\downarrow$  by  $\bar{B}^0$



# Bell's inequality with $B^0\bar{B}^0$



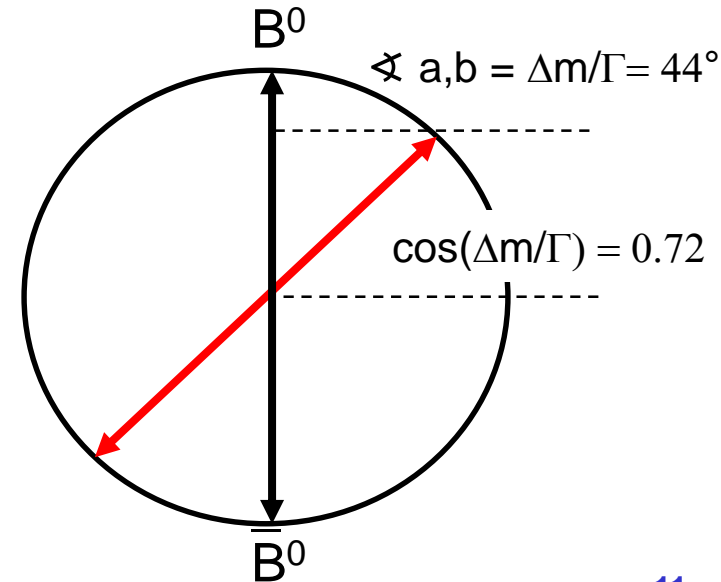
Replace the angle between the polarizers by  $\Delta m \Delta t$

**S = 2.70 (for 22.5 and 67.5°)**

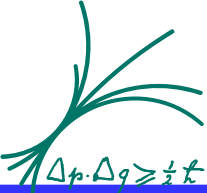
(A. Go & Chung Li, quant-ph/0310192v1 (2003):  
 $S = 2.725 \pm 0.167 \pm 0.092$  (Belle data) )

Non QM test: Assume complete decoherence  
 (both B oscillate independently from  $t=0$ )

**S = 2.61**      **S(decoherent) < 2 for  $\Delta m/\Gamma > 2$**



What's wrong? => high correlation due to short lifetime



# No way for Bell at Belle (II)



Bertlmann, Bramon, Garbarino, Hiesmayr, Phys. Lett. A 332, 355-360 (2004)

crucial parameter  $x_d = \Delta m_d / \Gamma_d$ :  
rate of oscillation relative to decay

Bell test impossible if  $x < 2.0$ :

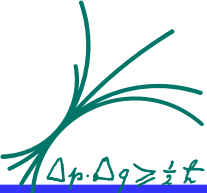
system	$x$
$B^0 / \bar{B}^0$	0.77
$K^0 / \bar{K}^0$	0.95
$D^0 / \bar{D}^0$	$< 0.03$
$B_s^0 / \bar{B}_s^0$	$\sim 26$

Furthermore:

we rely on the random decays of both B  
no (reasonable) way to **actively** determine  $\not\propto a, b \rightarrow \Delta m \Delta t$

A kind of Maxwell's demon could tune hidden parameters ( $t_1, t_2$ , decay type)  
so that QM and Bell's inequality is emulated, despite it's not QM and local.  
No practical way to close this loophole



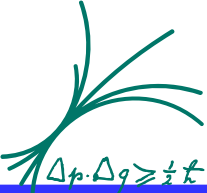


# What's left to be done

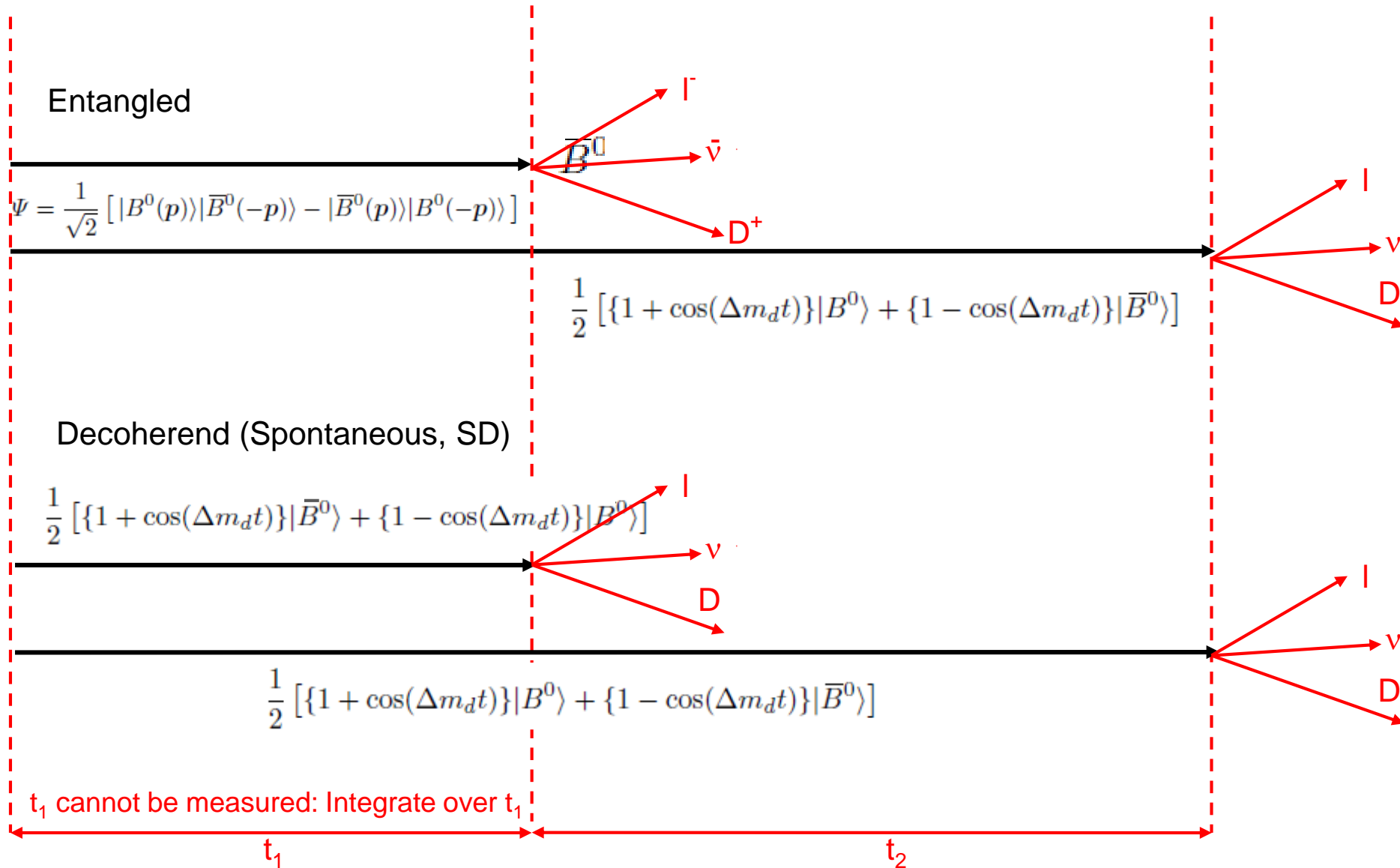


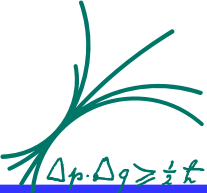
We can still calculate effects of special decoherent or non local models  
Fit (modified) time dependence to data

- Spontaneous decoherence (SD):
  - entanglement is lost at  $t=0$  for a certain fraction of events
  - decoherence fraction  $\zeta$
- Pompili Selleri model (PS) (Eur. Phys. J. C14, 469 (2000)):
  - local realism, which reproduces oscillation phenomenology
- Lindblad type decoherence
  - coherence is gradually lost within a certain decoherence time



# Time dependence if decoherent





# Spontaneous Decoherence

$B^0/\bar{B}^0$  Oscillations: Probability to measure a same sign (SS) event:

a) Full coherence:

$$P(B^0 B^0, \bar{B}^0 \bar{B}^0) = \frac{1}{2} \Gamma \exp(-\Gamma t_2) (1 - \cos \Delta m t_2)$$

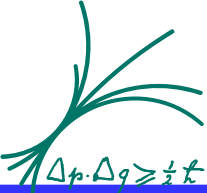
b) Full decoherence (Spontaneous decoherence, SD)

$$P(B^0 B^0, \bar{B}^0 \bar{B}^0) = \frac{1}{2} \Gamma \exp(-\Gamma t_2) \left( 1 - \frac{1}{2} \frac{\Delta m + 2\Gamma^2}{\Gamma^2 + \Delta m^2} \cos \Delta m t_2 + \frac{1}{2} \frac{\Gamma \Delta m}{\Gamma^2 + \Delta m^2} \sin \Delta m t_2 \right)$$

Damping by  $\frac{1}{2} \frac{\Delta m + 2\Gamma^2}{\Gamma^2 + \Delta m^2} \sim 0.81$

Additional SIN-term:  $\frac{1}{2} \frac{\Gamma \Delta m}{\Gamma^2 + \Delta m^2} \sim 0.24$

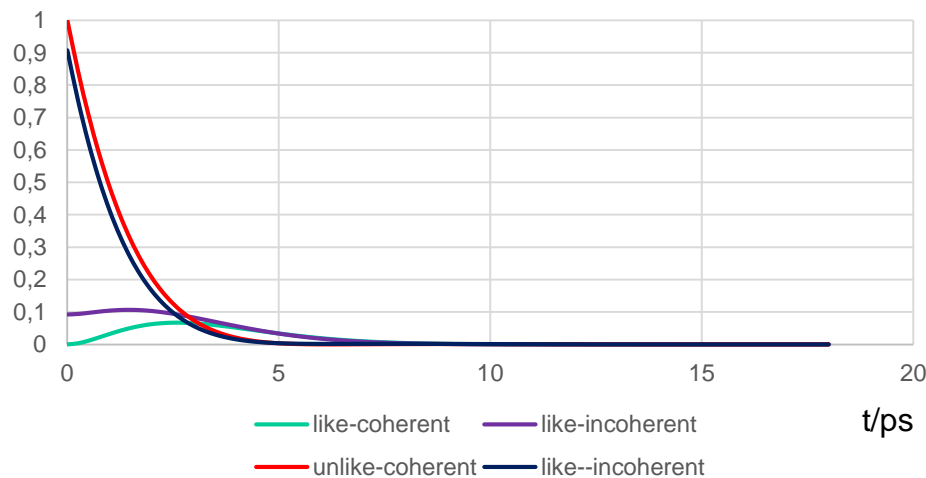
(using PDG averages:  $\Delta m = 0.505 \pm 0.002 \text{ ps}^{-1}$ ,  $\Gamma = 0.658 \pm 0.002 \text{ ps}^{-1}$ )



# Time Dependence (SD)



Like & unlike

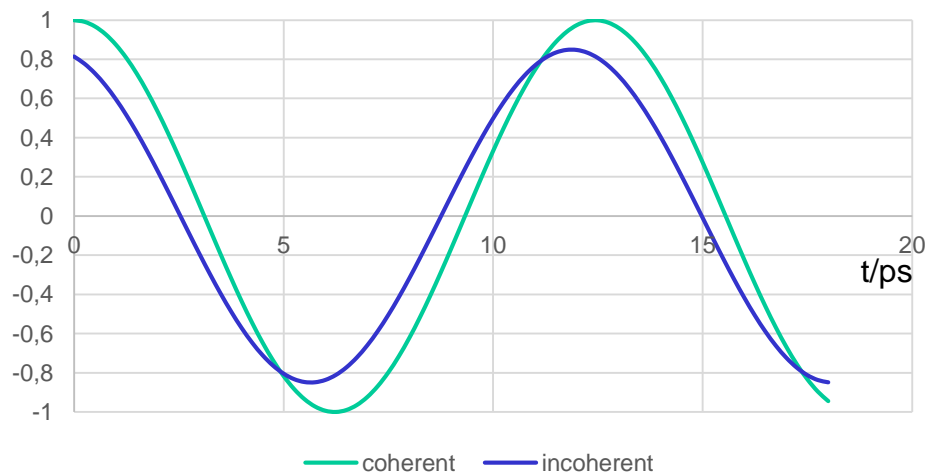


The damping is probably difficult to measure, as it could be interpreted as mistag

The SIN term (or phase shift) should be measurable

Similar damping and phase shifts occur in measurements of TDCPV

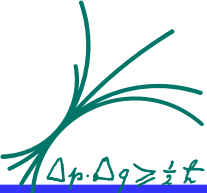
(unlike-like)/all



In principle the damping (if ignored) would lead to a wrong measurement of  $\sin(2\beta)$ , This might be compensated out if the mistag is taken from the oscillation measurement (same damping)

The phase shift would lead to a cross talk between S and C terms





# Indirect Indicator: $\chi$



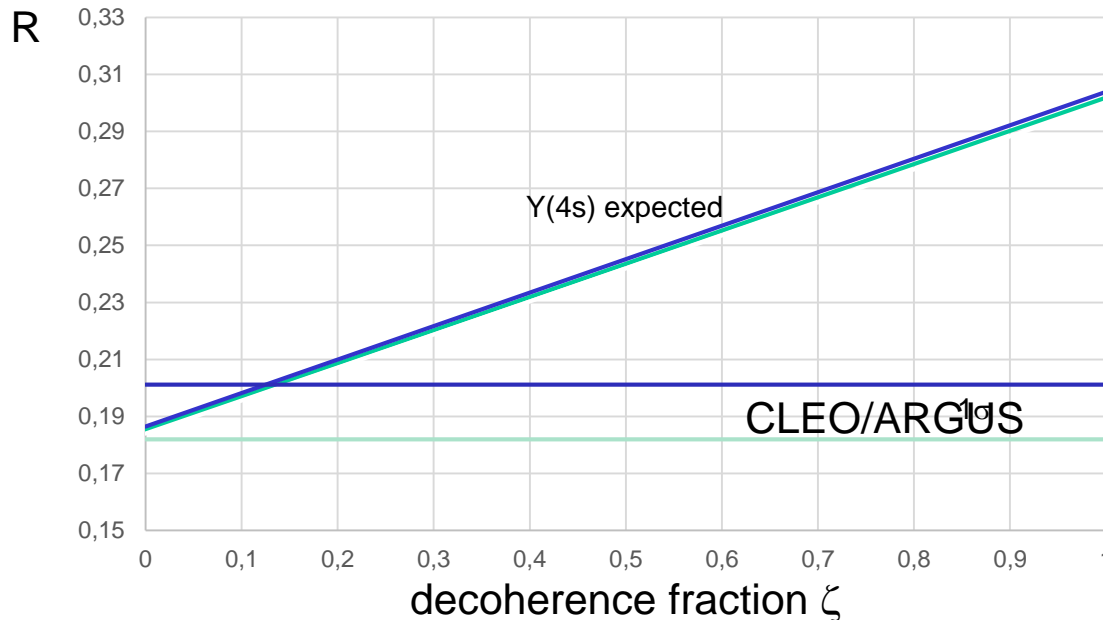
Time integrated oscillations: measure  $\chi = \frac{1}{2} \Delta m^2 / (\Delta m^2 + \Gamma^2)$  using dilepton events

Use  $\Delta m$  from LHCb as reference (no coherence at LHCb!)

Coherence:  $R = (N^{++} + N^{--}) / (N^{++} + N^{--} + N^{+-}) = \chi$

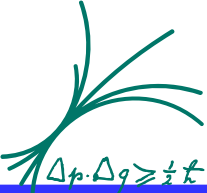
SD:  $R = (N^{++} + N^{--}) / (N^{++} + N^{--} + N^{+-}) = 2(\chi - \chi^2)$

Use  $\chi$  calculated from LHCb's  $\Delta m$  measurement (always decoherent)



Old CLEO/ARGUS measurement of  $R = 0.182 \pm 0.015$  (PDG) still comparable with  $\sim 10\%$  decoherence

Should be able to do much better

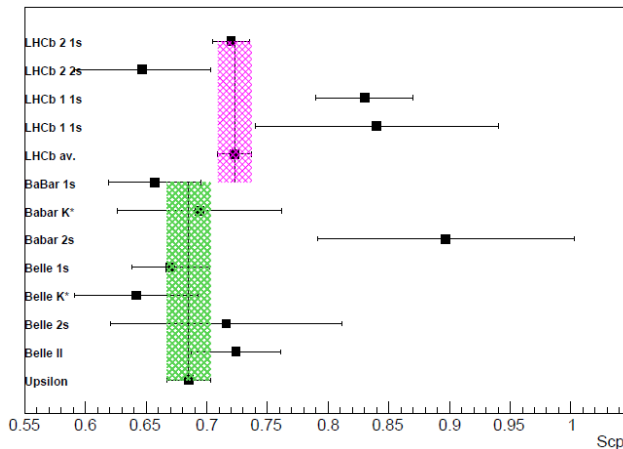


# Indirect Indicators: TDCPV

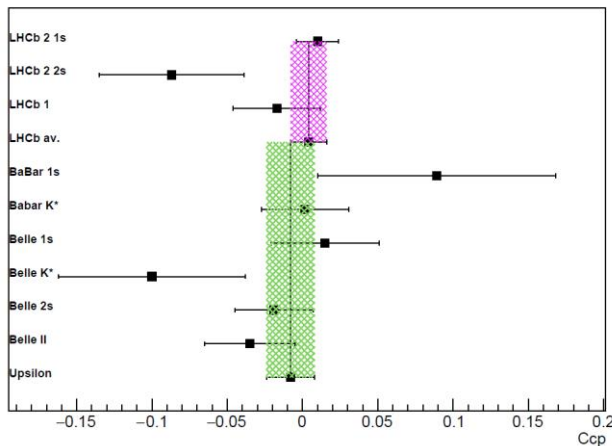


Compare  $S_{CP}$  and  $C_{CP}$  measurements at LHCb (always decoherent) and at  $Y(4s)$

Scp



Ccp



My averages, no correlations!



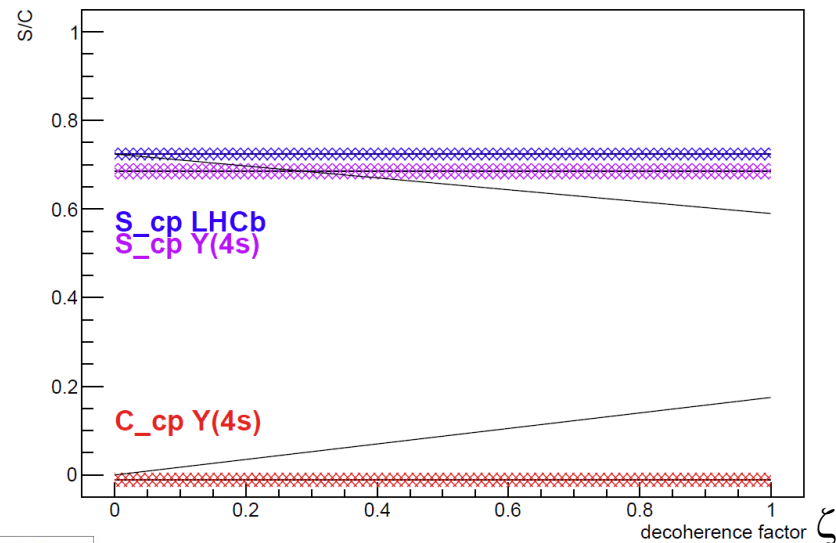
mistag calibration could cancel damping partially!

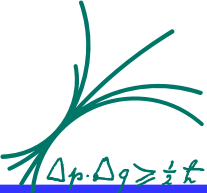
$$(1 + q[S \sin \Delta mt - C \cos \Delta mt])$$

$$\left( 1 + q \left[ \frac{\Delta m \Gamma}{2(\Gamma^2 + \Delta m^2)} C + \frac{\Delta m^2 + 2\Gamma^2}{2(\Gamma^2 + \Delta m^2)} S \right] \sin \Delta mt_2 + q \left[ \frac{\Delta m \Gamma}{2(\Gamma^2 + \Delta m^2)} S - \frac{\Delta m^2 + 2\Gamma^2}{2(\Gamma^2 + \Delta m^2)} C \right] \cos \Delta mt_2 \right)$$

Same damping (0.81) and x-talk factors (0.24) as on slide 3

Compatible with up to 5-20% decoherence, preferred: 10% ( $1.7\sigma$ )





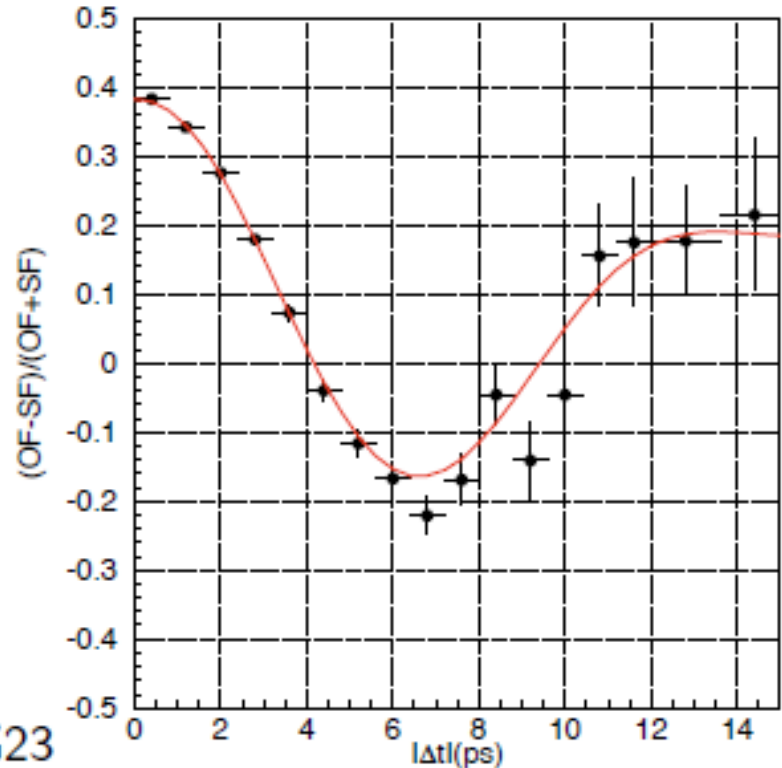
# Belle Analysis



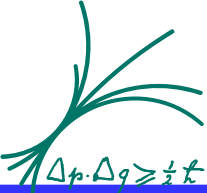
A.Go & Belle, Phys. Rev. Lett 99 (2007) 131802

Belle's most current  $\sin 2\phi_1$ ,  $|\lambda|$ ,  $\tau_B$ ,  $\Delta m_d$  measurement at the time:

- $152 \times 10^6$   $B\bar{B}$  pairs
  - $5 \times$  the discovery dataset
  - $\frac{1}{5} \times$  the eventual dataset
- 5417 CP- and 177368 flavour-eigenstate  $B$ -decay candidates
- sample purities vary 63–98% depending on the decay mode
- multivariate flavour-tagging of the other  $B$  decay;  $\epsilon_{eff} = 28.7\%$
- $\Delta m_d = (0.511 \pm 0.005 \pm 0.006) \text{ ps}^{-1}$   
cf.  $(0.5065 \pm 0.0019) \text{ ps}^{-1}$  PDG23

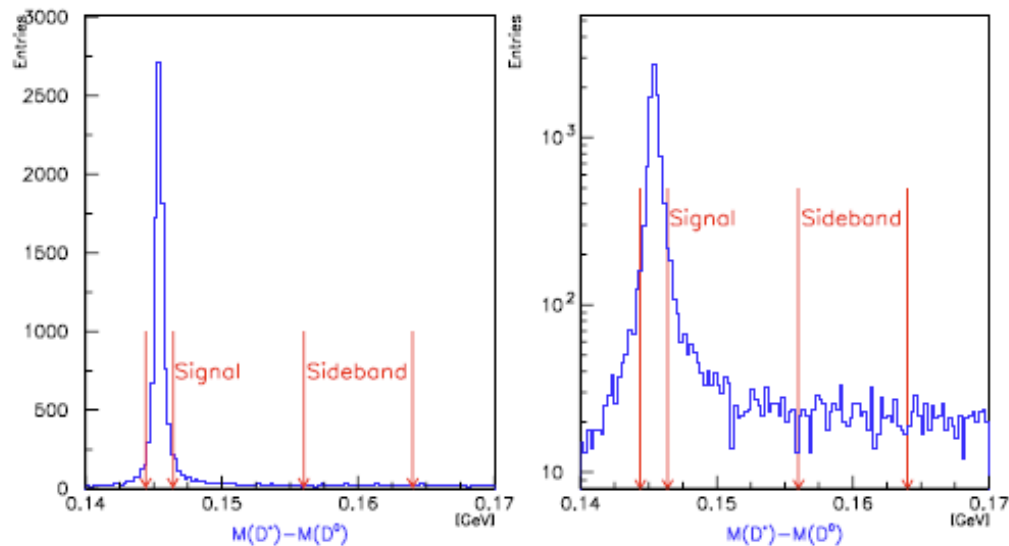


We then adapted this in various ways ...

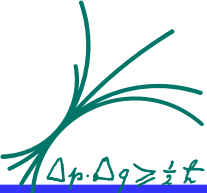


# Event Selection

- restrict 177368 → 84823 flavour eigenstates, choosing only  $B^0 \rightarrow D^{*-} \ell^+ \nu$  where the lepton explicitly determines the  $B$ -flavour
- restrict 84823 → 8565 by choosing only the best flavour tags of the other  $B$ : highest of 7 purity categories; leptons only
- signal relies on  $D^{*-} \rightarrow \bar{D}^0 \pi^-$  tag: energy release  $Q \ll m_\pi \ll m_D$
- estimate background under peak using sideband region:



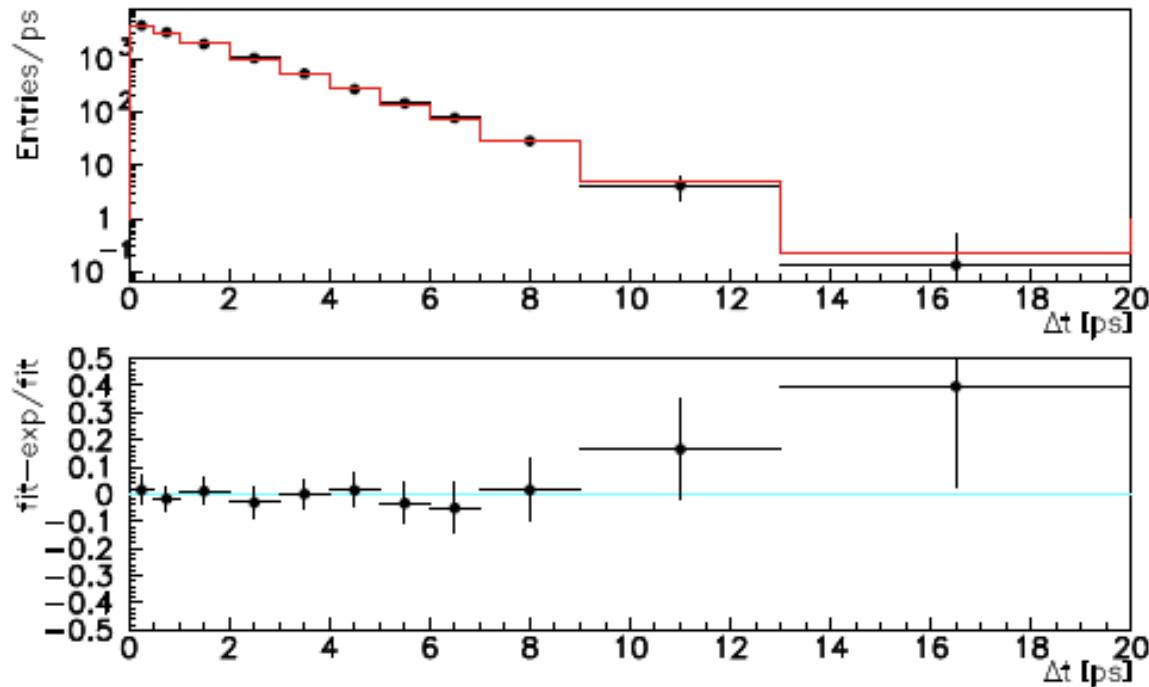




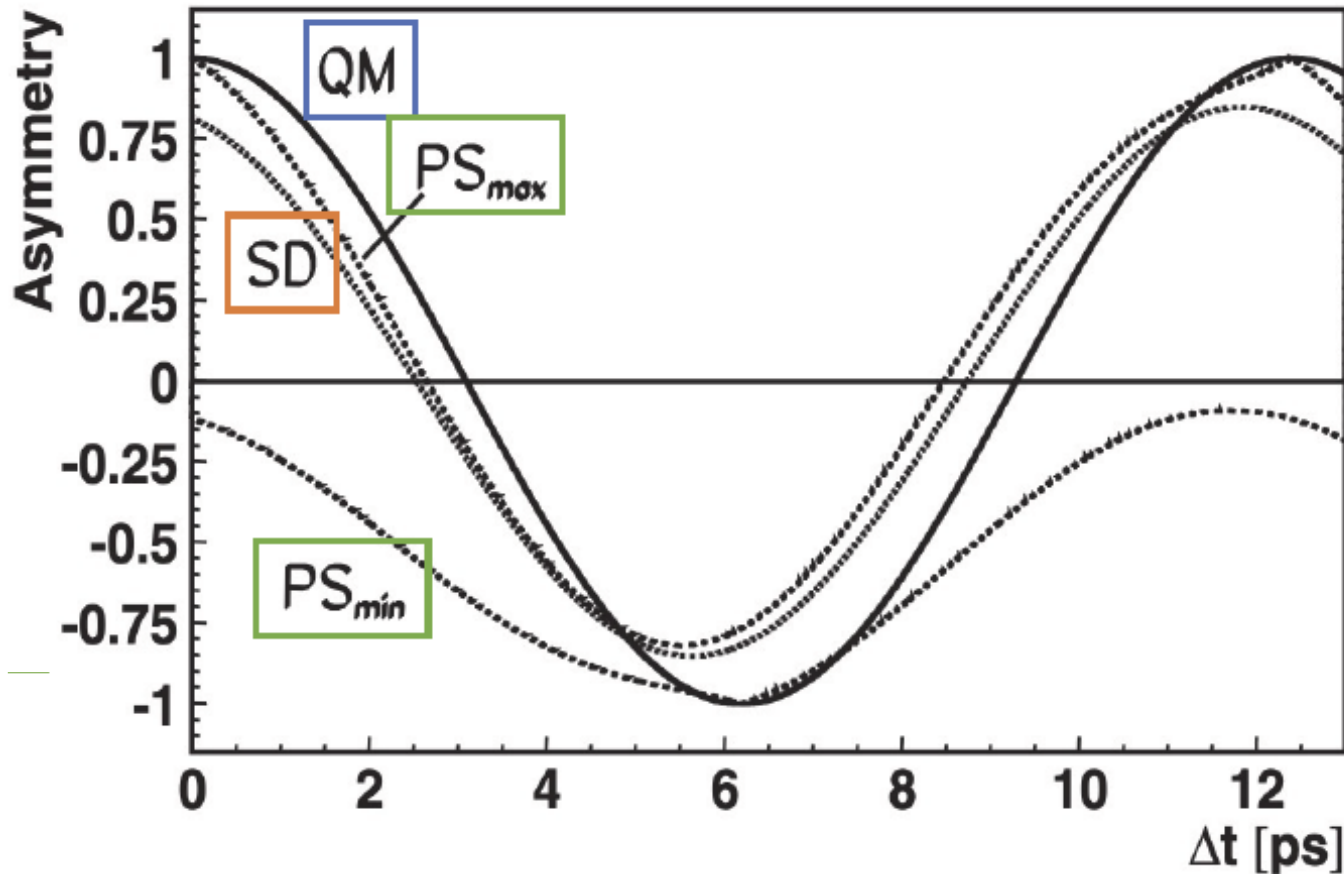
# Check: fit $B^0$ lifetime

- Background subtraction, deconvolution of  $\Delta t$  resolution, mistag.....

... and fitting for the  $B^0$  lifetime:



finds lifetime  $\tau_B^0 = (1.532 \pm 0.017) \text{ ps}$ , with  $\chi^2/n_{dof} = 3/11$   
cf. world average  $(1.530 \pm 0.009) \text{ ps}$  from PDG2006

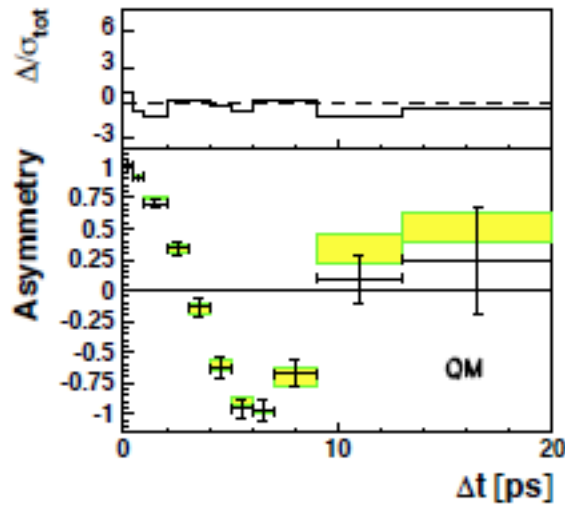


QM: standard quantum mechanical entanglement

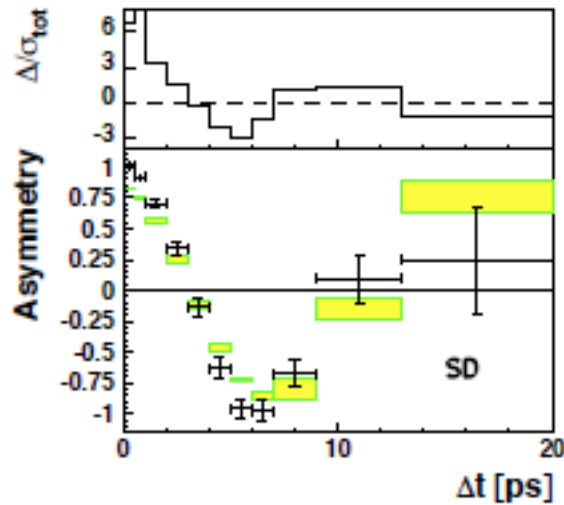
SD: spontaneous decoherence

PM: A. Pompili & F. Selleri, Eur. Phys. J. C14, 469 (2000)

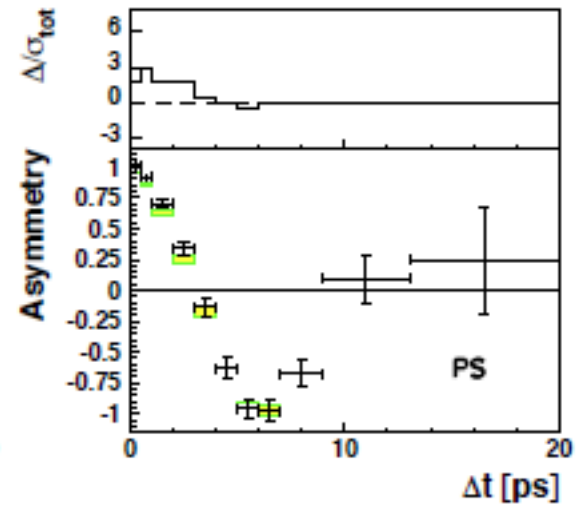
fit: float  $\Delta m_d$  subject to WA-sans-(Belle+BaBar):  $(0.496 \pm 0.014) \text{ ps}^{-1}$



QM fits well  
 $\chi^2/n_{dof} = 5/11$

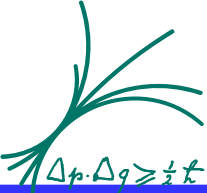


SD disfavoured:  $13\sigma$   
 $\chi^2/n_{dof} = 174/11$



PS disfavoured:  $5.1\sigma$   
 $\chi^2/n_{dof} = 31/11$

- "SD fraction":  $(1 - \zeta_{B^0\bar{B}^0})A_{QM} + \zeta_{B^0\bar{B}^0}A_{SD}$ ,  $\zeta_{B^0\bar{B}^0} = 0.029 \pm 0.057$
- Pompili-Selleri class: QM-like states, stable mass, flavor correlations; QM predictions for *single B-mesons* preserved



# What do we learn?

SD excluded by  $13\sigma$ , but more relevant is the fraction of decoherent events

$$f = (1-\zeta) A_{\text{QM}} + \zeta A_{\text{SD}} \qquad \zeta = 0.029 \pm 0.057$$

**A fraction of ~10% is still possible!**

This could lead to shift of our  $S_{\text{cp}}$  measurements by

$$\Delta S_{\text{cp}} \sim 0.012 \text{ (@ } Y(4s))$$

The total systematic errors of the Belle II  $J/\psi K_S$  analysis is 0.014 !

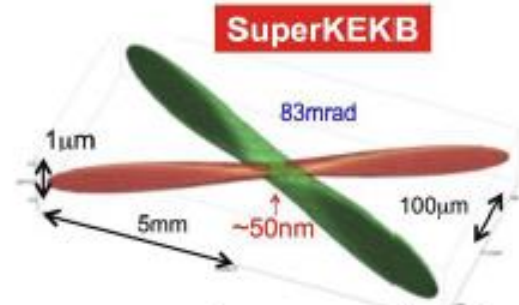
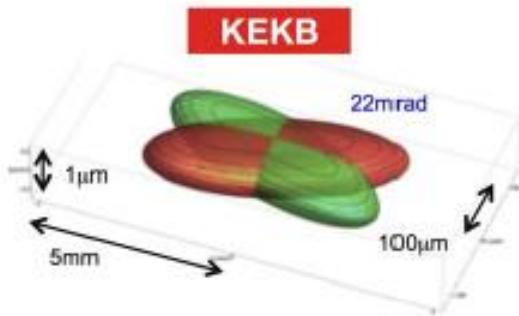
largest single systematic error?

Source	$\sigma(\varepsilon_{\text{tag}})$ [%]	$\sigma(S_{\text{CP}})$	$\sigma(C_{\text{CP}})$
$B^0 \rightarrow D^{(*)-} \pi^+$ sample size	0.43	0.004	0.007
$B^0 \rightarrow J/\psi K_S^0$ sample size		0.035	0.026
Fit model			
Analysis bias	0.02	0.002	0.005
Fixed resolution parameters	0.07	0.004	0.004
$\tau$ & $\Delta m_d$	0.06	0.001	0.000
$\sigma_{\Delta t}$ binning	0.04	0.000	0.000
$\Delta t$ measurement			
Alignment	0.06	0.005	0.003
Beam spot	0.16	0.002	0.002
CMS Energy	0.03	0.000	0.001
Backgrounds			
$B^0 \rightarrow D^{(*)-} \pi^+$ sWeight bias	0.24	0.001	0.001
$B^0 \rightarrow D^{(*)-} \pi^+ \Delta E$ background	0.11	0.001	0.001
Signal $\Delta E$ shape	0.08	0.002	0.000
Tag-side interference	—	0.010	0.007
Total systematic	0.34	0.014	0.012

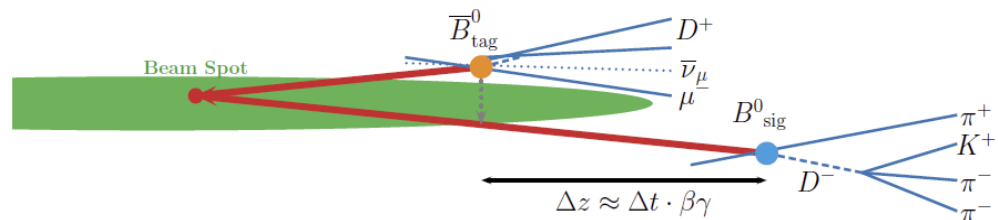
Repeat Belle analysis with higher statistics, more channels, better resolution

$$B^0 \rightarrow D^- \pi^+, D^{*-} \pi^+, D^{*-} \rho^+$$

Make use of better vertex resolution and smaller interaction region:



	KEKB	superKEKB
$\sigma_x$	150 $\mu\text{m}$	10 $\mu\text{m}$
$\sigma_y$	940 nm	50 nm
$\sigma_z, \text{eff}$	7 mm	0.25 mm

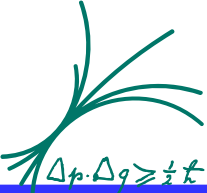


$$\gamma\beta\tau c = 0.125 \text{ mm}$$

Not perfect yet, but some chance to limit  $t_1$

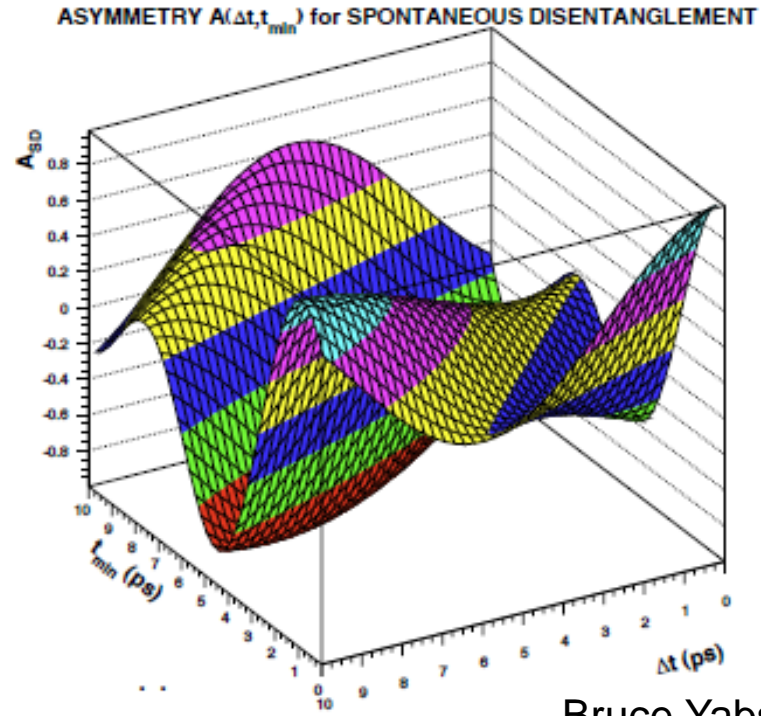
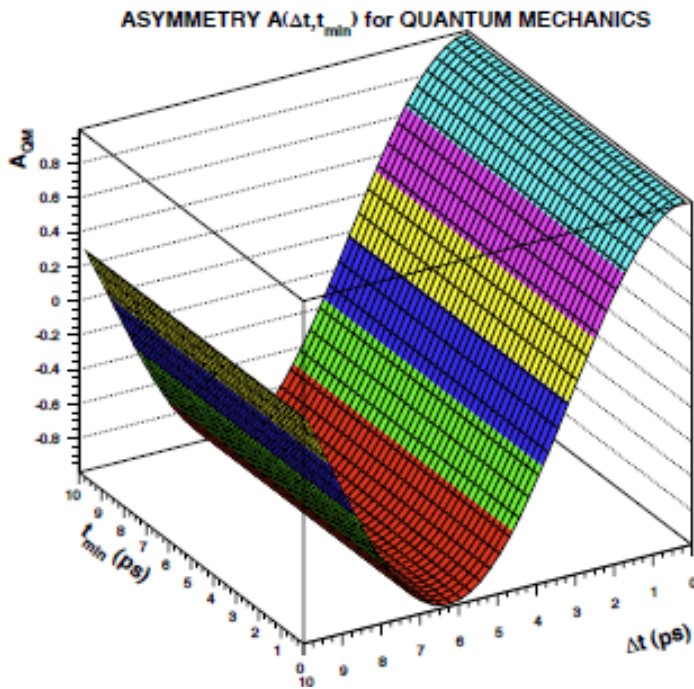
Transverse separation  $\sim 50 \mu\text{m}$

Vertex resolution  $\sigma_{e,s} \sim 20 \mu\text{m}$



# Discrimination Power

Access to  $t_1$  adds a new dimensions and should result higher sensitivity



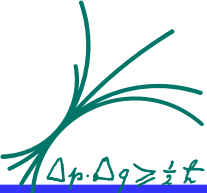
Bruce Yabsley

Entanglement: depends only on  $\Delta t$

Decoherence: depends on  $t_1$  and  $\Delta t$

Setting a lower limit on  $t_1$  could also make a EPR type measurements possible (randomize)





# Conclusions



- ‘Ascent’ style experiments to check Bell’s inequality are not possible with  $Y(4s) \rightarrow B^0 \bar{B}^0$ 
  - no active measurement (random decay of the  $B^0$ ): conspiracy loophole!
  - short  $B^0$  lifetime induces correlations which violate Bell’s inequality even for a local realistic scenario
- QM and alternative models can be tested fitting the time dependence of  $B^0$  oscillations. Belle analysis: alternative scenarios excluded by  $13\sigma$  (SD) and  $5.1\sigma$  (PS)
- A fraction of  $\sim 10\%$  of decoherent events is still compatible with the data
- Possible systematic error to our TDCPV measurements (so far not taken into account!)
- Belle II has the potential to improve on this
- Questions to theory: what mechanisms (SM or BSM) could lead to a loss of coherence?

With contributions from

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Bruce Yabsley (Sidney)  
Fumiaki Otani, Takeo Higuchi (IPMU)