

Recent quarkonium results from Belle II

16TH INTERNATIONAL CONFERENCE ON HEAVY QUARKS AND LEPTONS

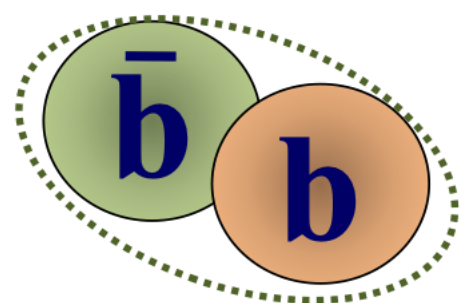
Renu

On the behalf of Belle II Collaboration

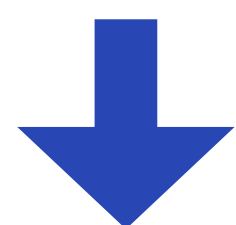
Supported by US DOE funding

28th Nov, 2023 - 2nd Dec, 2023

Bottomonium Scheme

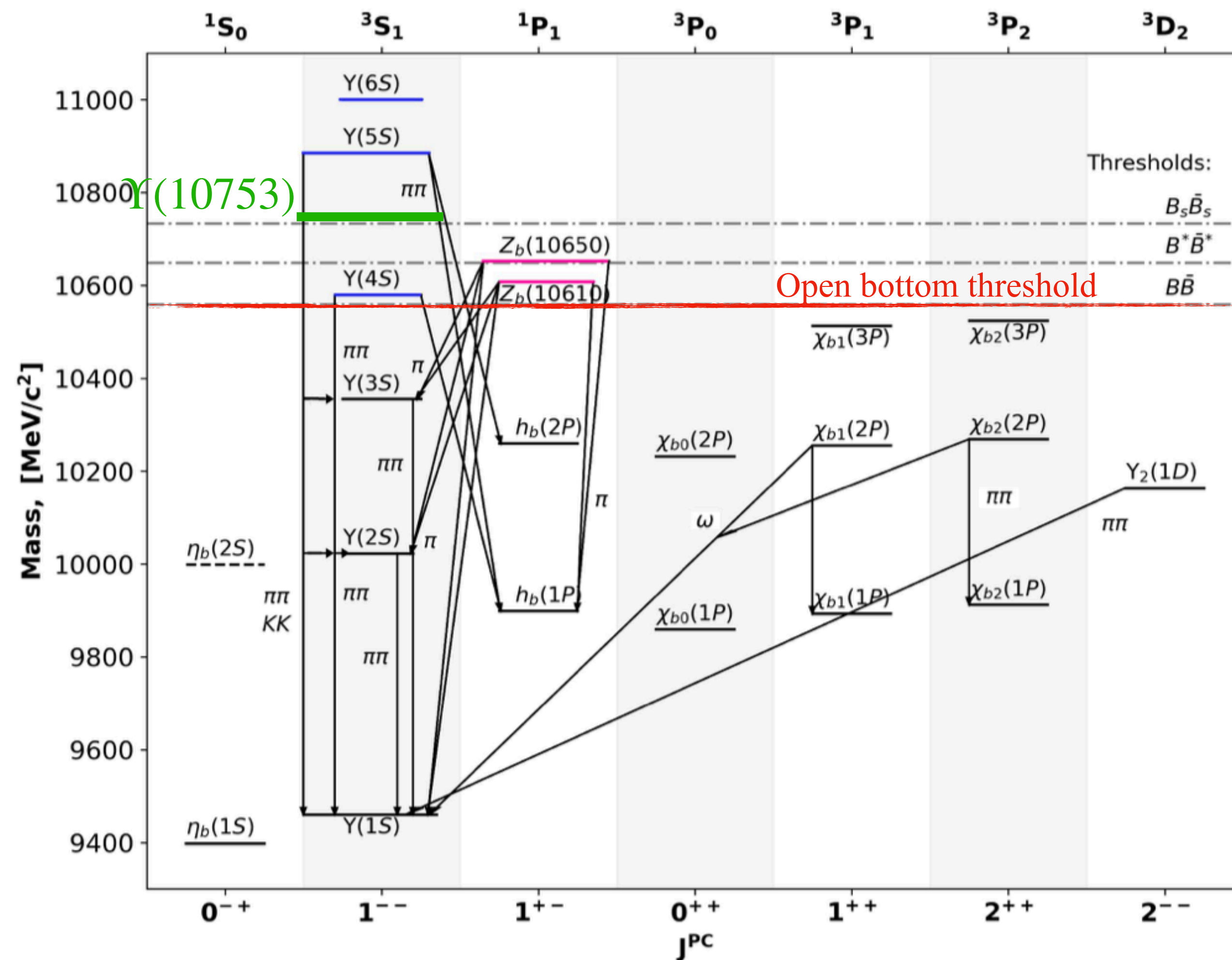


- ▶ Below the $B\bar{B}$ threshold states are well described by potential models.
- ▶ Above $B\bar{B}$ threshold states exhibit unexpected properties:
 - ◆ Hadronic transitions to lower bottomonia are strongly enhanced.
 - ◆ The η transitions are not suppressed compared to $\pi^+\pi^-$ transitions. Strong violation of Heavy Quark Spin Symmetry.



Exotic admixtures: molecule, compact tetraquark, hybrid.

- ▶ $Z_b^+(10610)$ or $Z_b^+(10650)$: observed near the $B^{(*)}\bar{B}^*$ thresholds, properties are consistent with $B^{(*)}\bar{B}^*$ molecules.



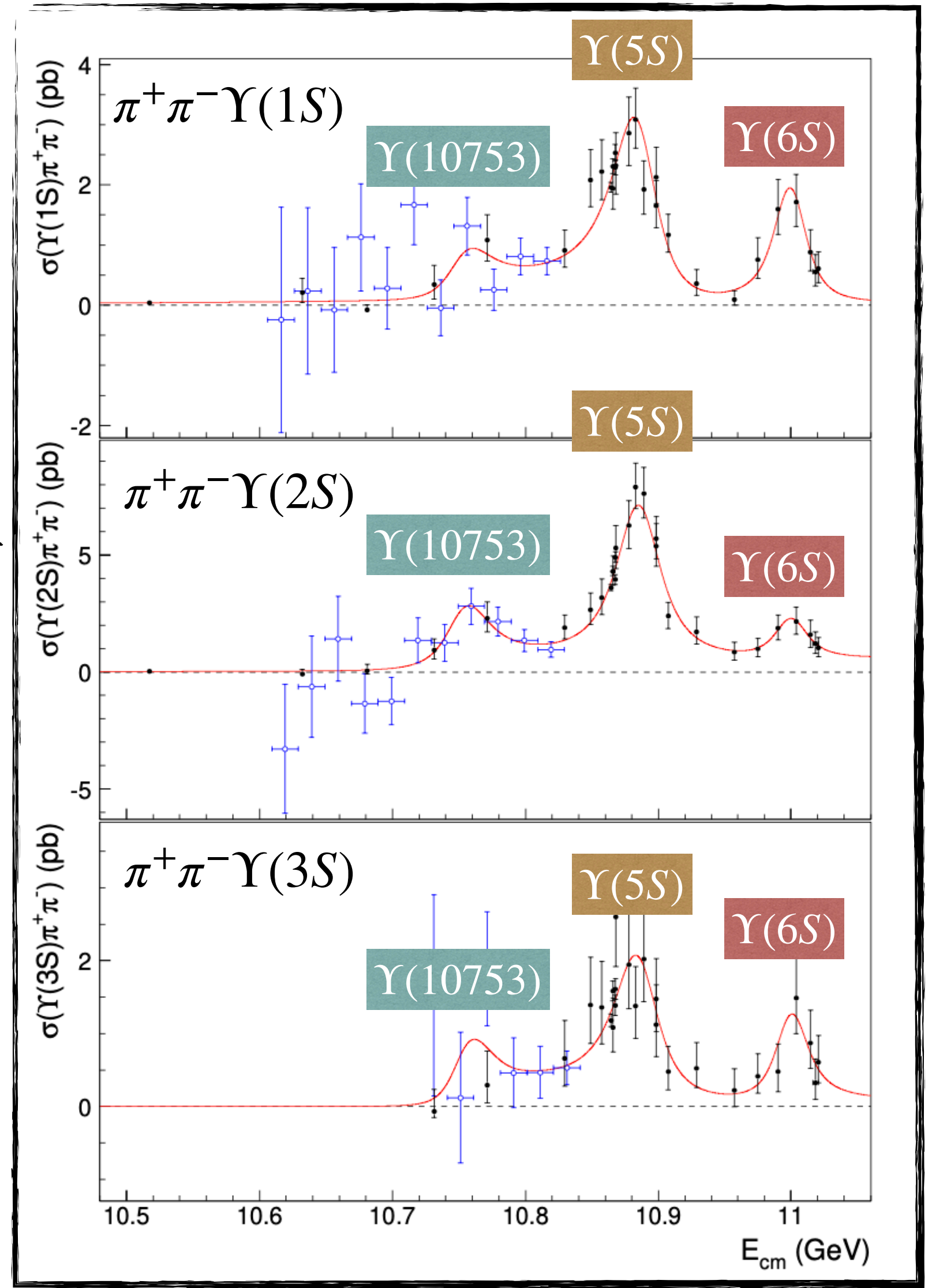
- ▶ Conventional bottomonium (pure $b\bar{b}$ state)
- ▶ Bottomonium like states (mix of $b\bar{b}$ and $B\bar{B}$)
- ▶ Purely exotic states (Z_b)

Discovery of $\Upsilon(10753)$

► $\Upsilon(10753)$ was observed in energy dependence of $e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-$ ($n = 1,2,3$) cross sections by Belle.
 Belle, JHEP 10 (2019) 220

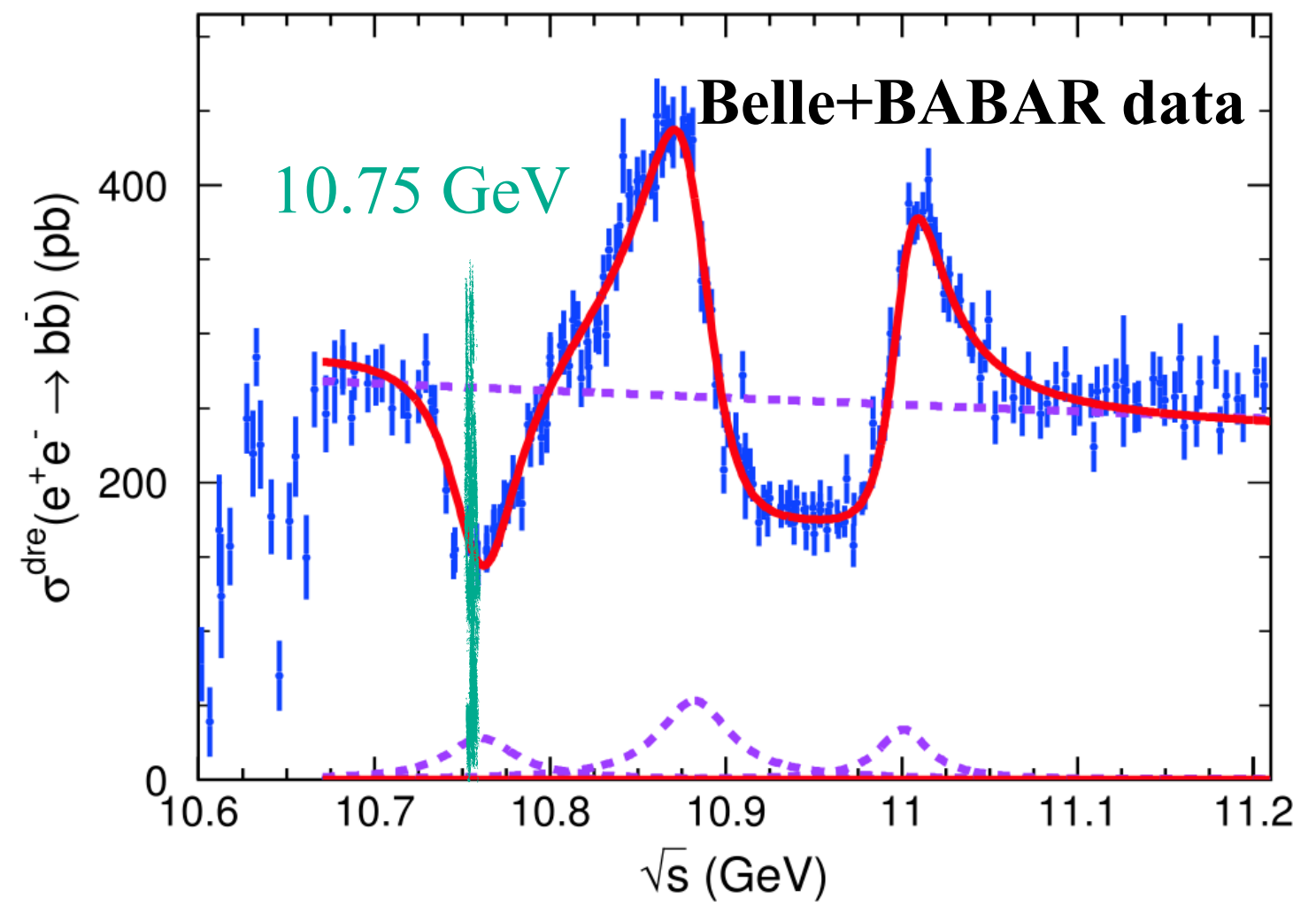
► The global significance is 5.2σ

	$\Upsilon(10860)$	$\Upsilon(11020)$	New structure
M (MeV/c ²)	$10885.3 \pm 1.5^{+2.2}_{-0.9}$	$11000.0^{+4.0}_{-4.5} \ ^{+1.0}_{-1.3}$	$10752.7 \pm 5.9^{+0.7}_{-1.1}$
Γ (MeV)	$36.6^{+4.5}_{-3.9} \ ^{+0.5}_{-1.1}$	$23.8^{+8.0}_{-6.8} \ ^{+0.7}_{-1.8}$	$35.5^{+17.6}_{-11.3} \ ^{+3.9}_{-3.3}$



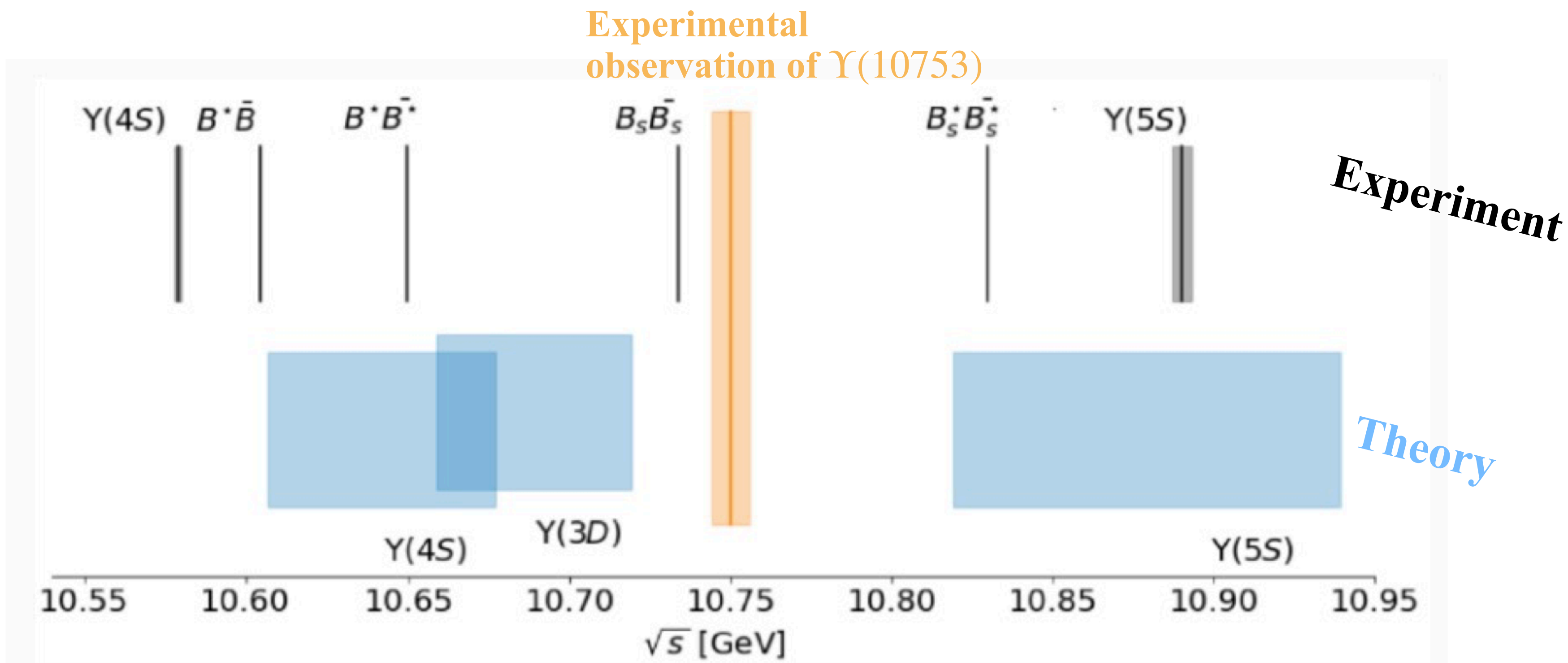
► $e^+e^- \rightarrow b\bar{b}$ cross section in bottomonium energy region based on the Belle and BABAR measurement.

◆ A dip near 10.75 GeV likely caused by interference between BW and smooth component.
 CPC 44, 8, 083001 (2020)



Fit function: 3 BW+smooth component

$\Upsilon(10753)$: theoretical interpretation



Possible interpretations:

► Conventional bottomonium?

Phys. Rev. D 105, 114041 (2022)
Phys. Rev. D 106, 094013 (2022)
Phys. Rev. D 105, 074007 (2022)

► Hybrid state?

Phys. Rept. 873, 1 (2020)
Phys. Rev. D 104, 034019 (2021)

► Tetraquark state?

Phys. Rev. D 103, 074507 (2021)
Phys. Rev. D 107, 094515 (2023)

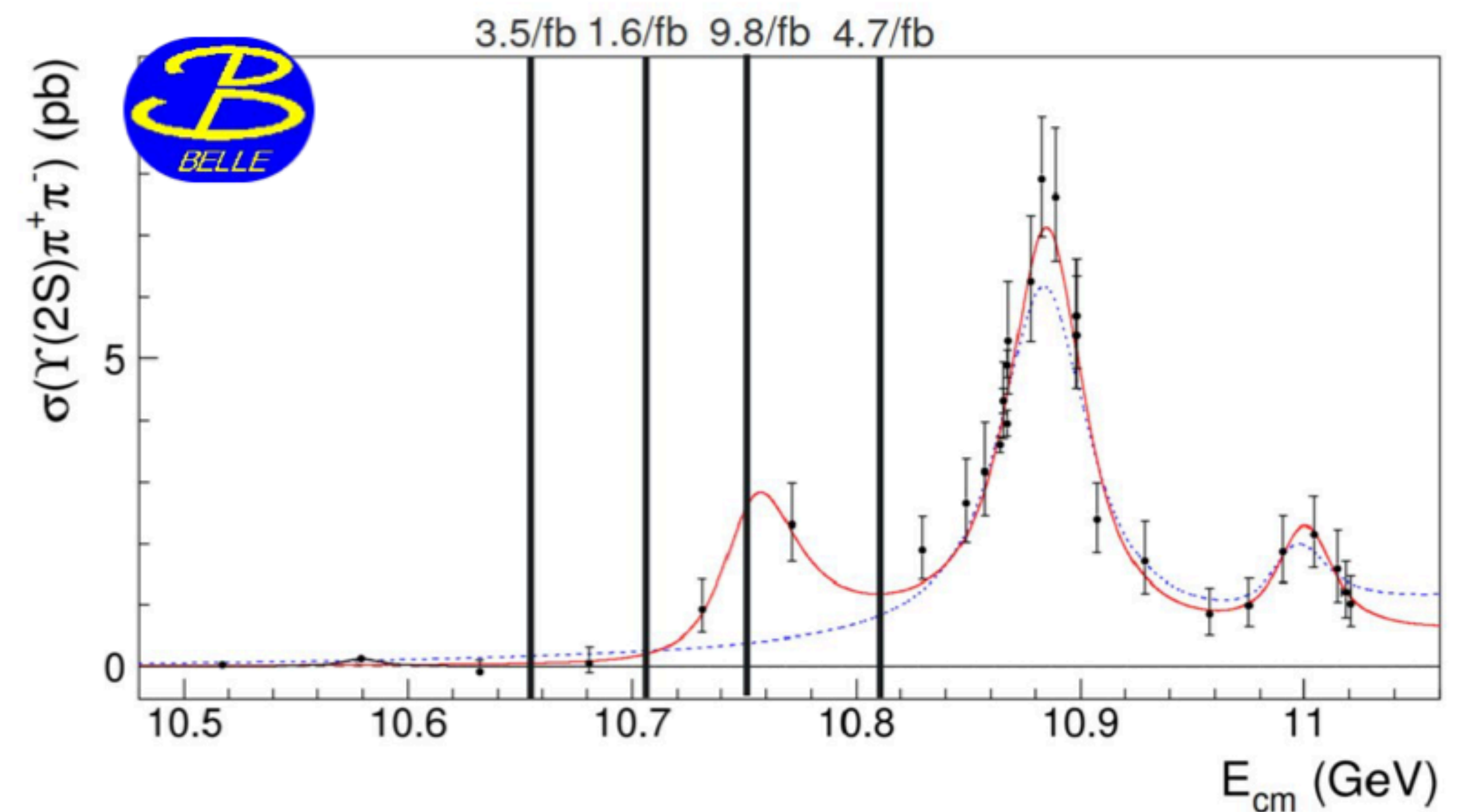
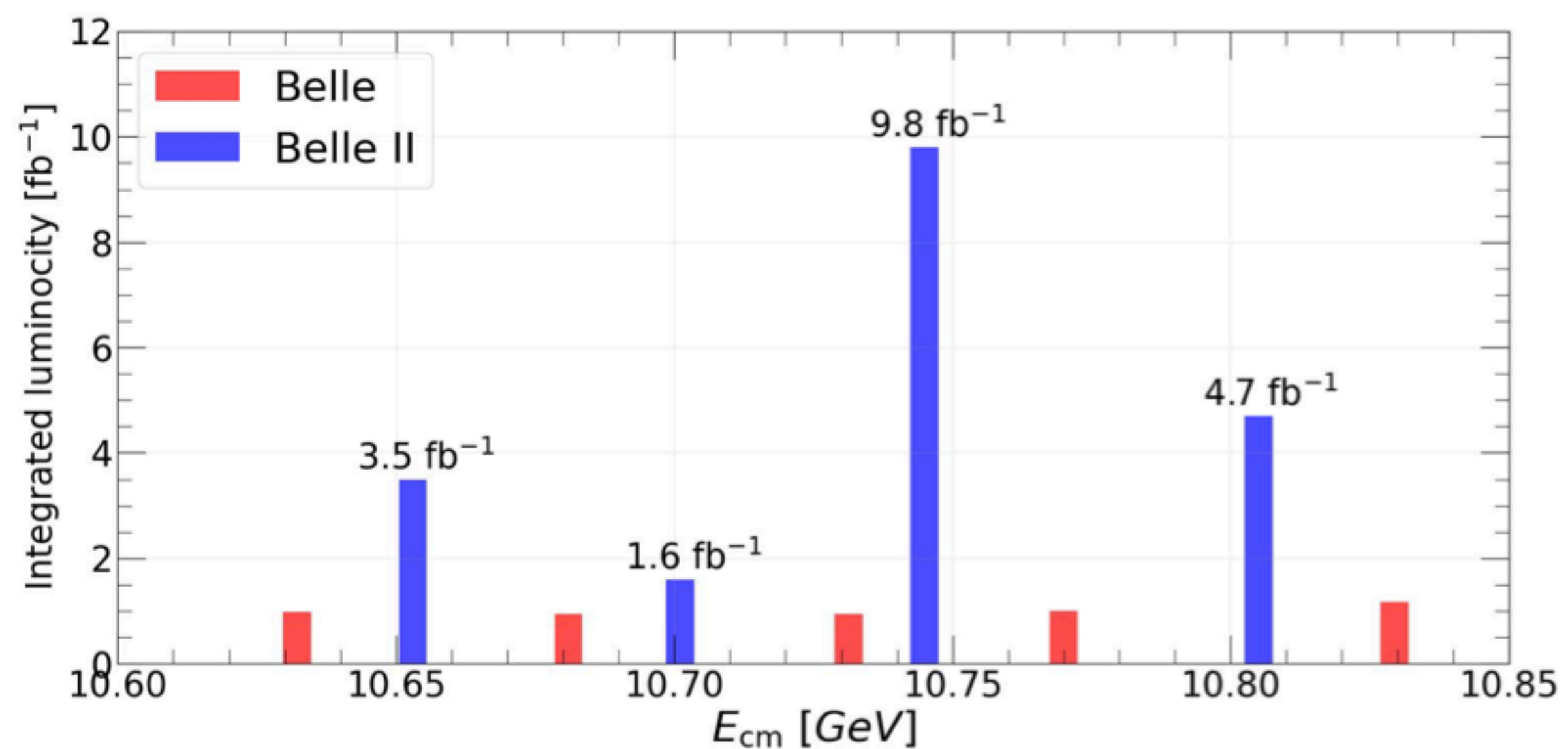
► Hadronic molecule with a small admixture of a bottomonium?

► Mass does not match $\Upsilon(3D)$ theoretical predictions, and D -wave states are not seen in e^+e^- collisions.

► $\Upsilon(4S) - \Upsilon(3D)$ mixing can be enhanced due to hadronic loops.

Unique scan data near $\sqrt{s} = 10.75$ GeV

- ▶ Belle II / SuperKEKB performed an energy scan in November 2021 with a total luminosity of 19 fb^{-1} .
- ▶ **Physics Goals:**
 - ▶ The main goal was to confirm and study the $\Upsilon(10753)$.
 - ▶ Improve the precision of exclusive cross-section below the $\Upsilon(5S)$.



- ▶ Belle II collected data in the gaps between the Belle points.
- ▶ The point with the highest statistics (9.8 fb^{-1}) is near the $\Upsilon(10753)$ peak.

Study of $\Upsilon(10753) \rightarrow (\pi^+ \pi^- \pi^0) \gamma \Upsilon(1S)$

Study of $\Upsilon(10753) \rightarrow (\pi^+\pi^-\pi^0) \gamma \Upsilon(1S)$

► Theory:

◆ Mixed 4S – 3D model suggests $\Upsilon(10753) \rightarrow \chi_{bJ}(1P) \omega$ could be enhanced. [PRD 104, 034036 \(2021\)](#)

► Charmonium sector:

◆ Similar to $\Upsilon(10753)$ in $e^+e^- \rightarrow \pi^+\pi^-\Upsilon(nS)$, $Y(4260)$ was observed in $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ cross section by BESIII.

● Expect similar nature of $\Upsilon(10753)$ and $Y(4260)$.

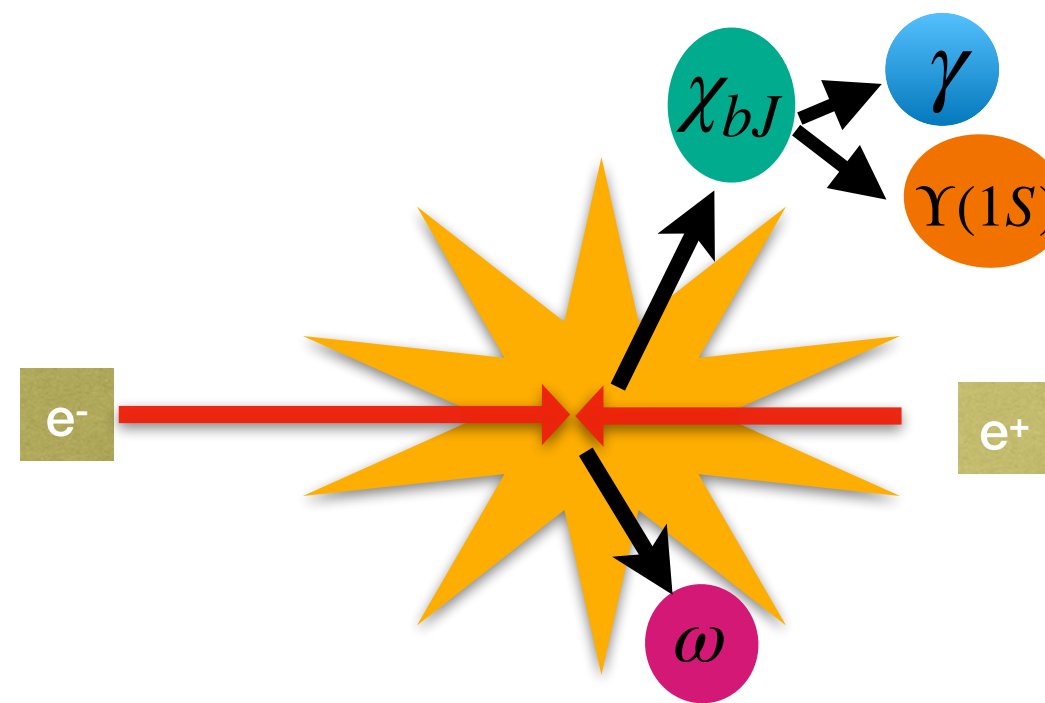
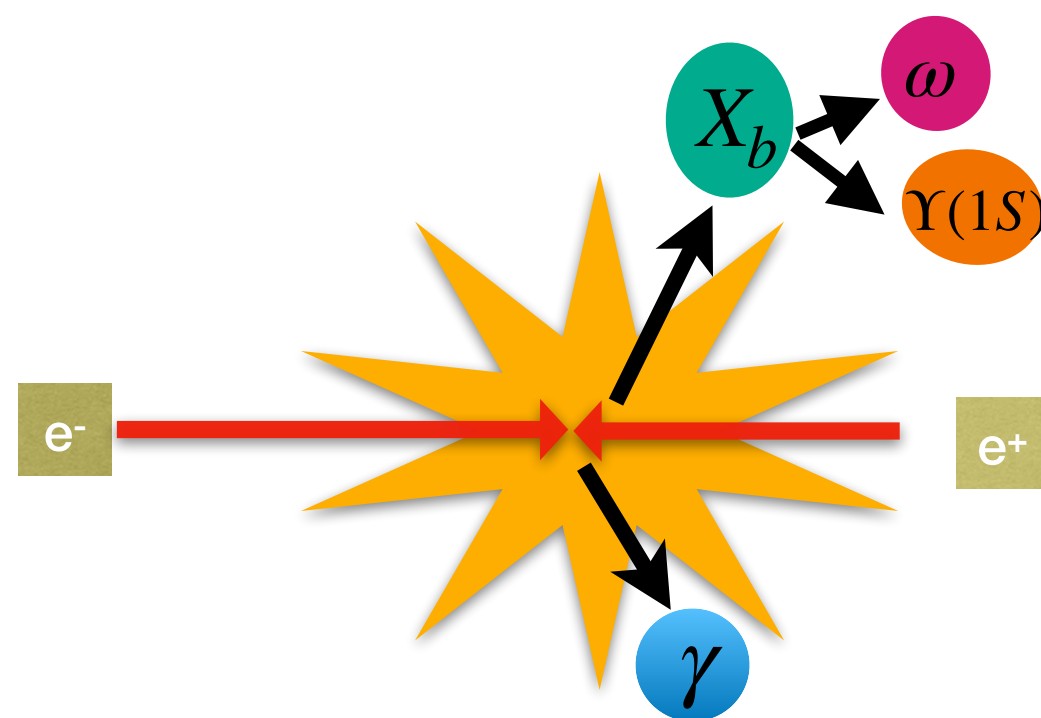
◆ $Y(4260)$ was also observed in $\chi_{c0}(1P) \omega$ and $\gamma X(3872)$ by BESIII.

◆ Inspired by decay modes of $Y(4260)$ charmonium state, we expect

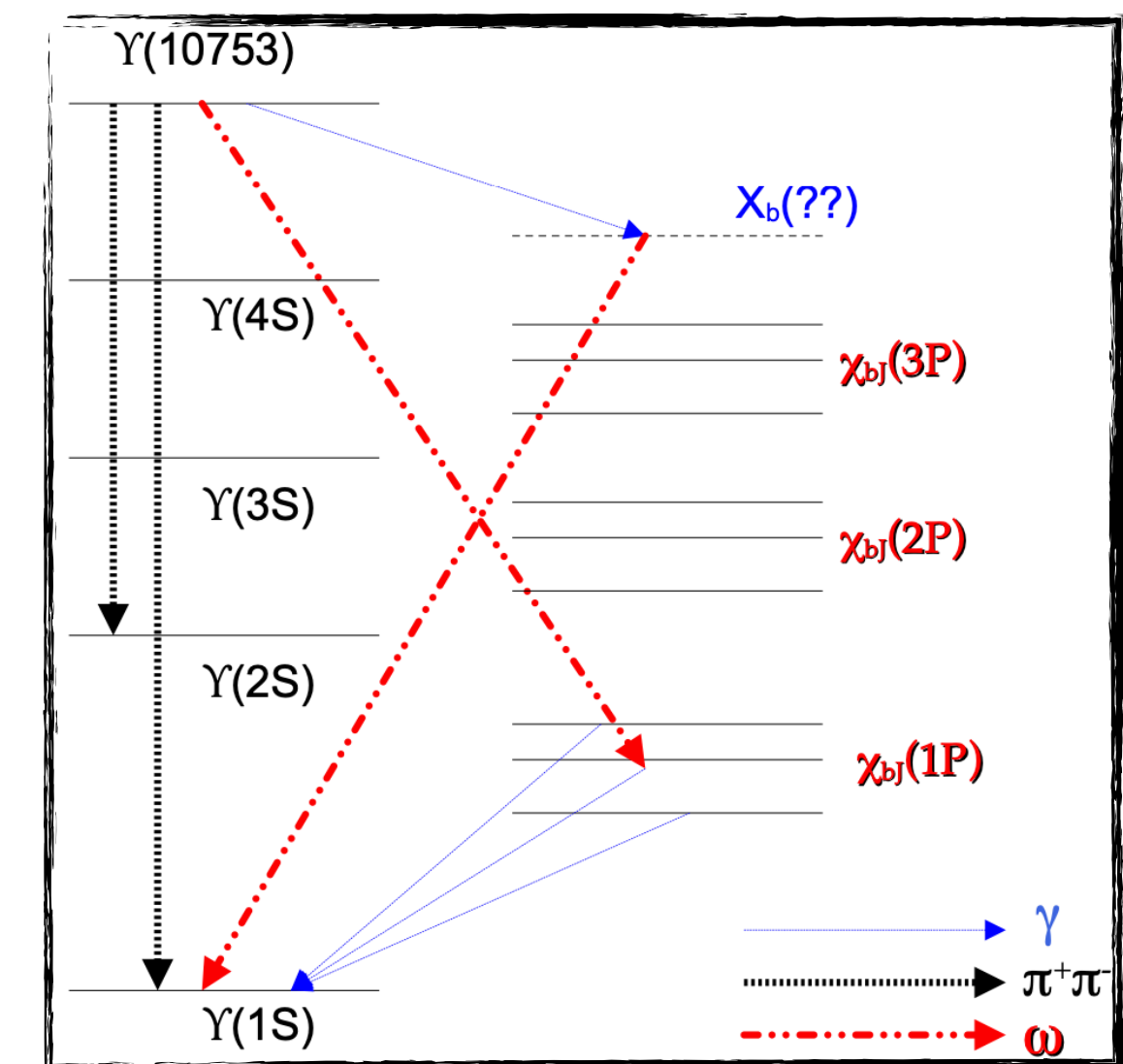
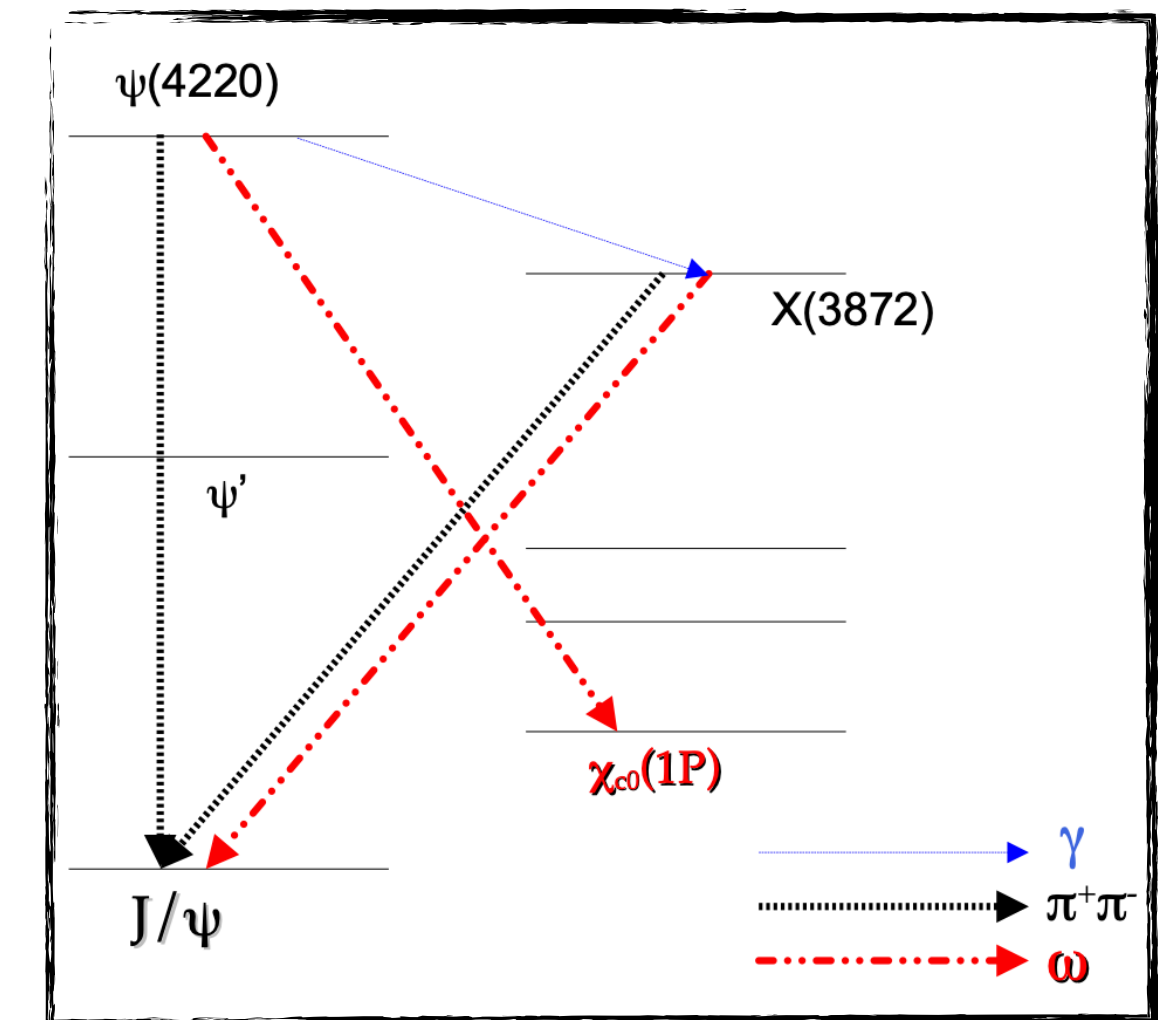
● $\Upsilon(10753) \rightarrow \chi_{bJ}(1P) \omega$

● $\Upsilon(10753) \rightarrow \gamma X_b$

X_b : bottomonium analogue of $X(3872)$



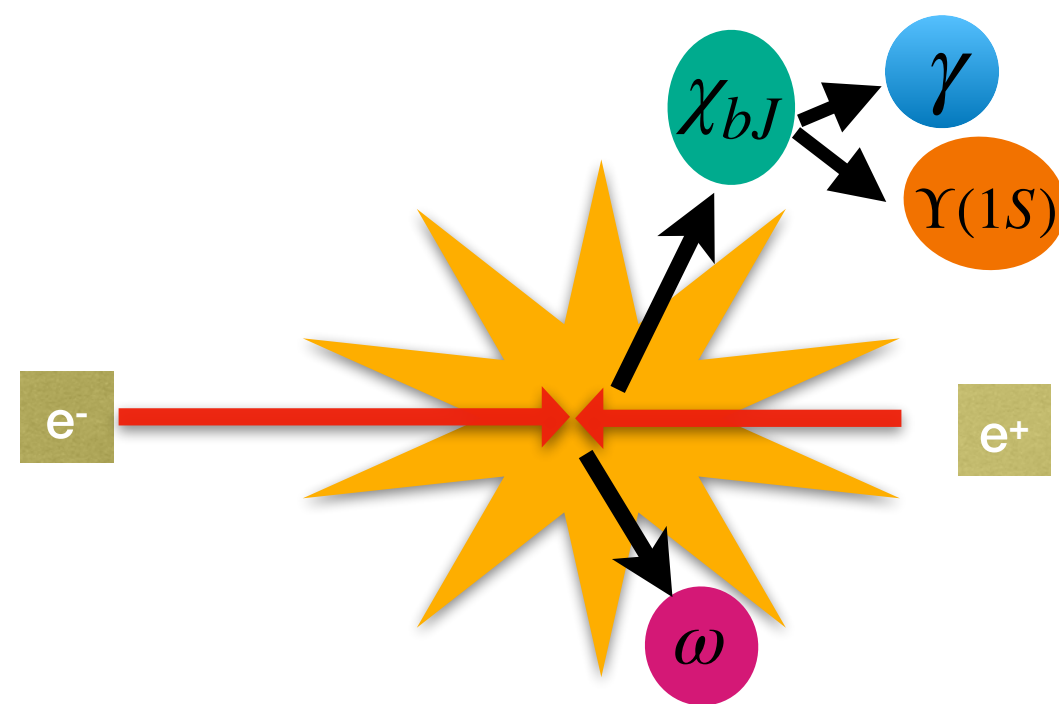
Search in $e^+e^- \rightarrow (\pi^+\pi^-\pi^0) \gamma \Upsilon(1S)$ process



Observation of $\Upsilon(10753) \rightarrow \omega \chi_{bJ}(1P)$

PRL 130, 091902 (2023)

The $e^+e^- \rightarrow \omega \chi_{bJ}(1P)$ ($J = 1,2$) cross sections peak at $\Upsilon(10753)$.



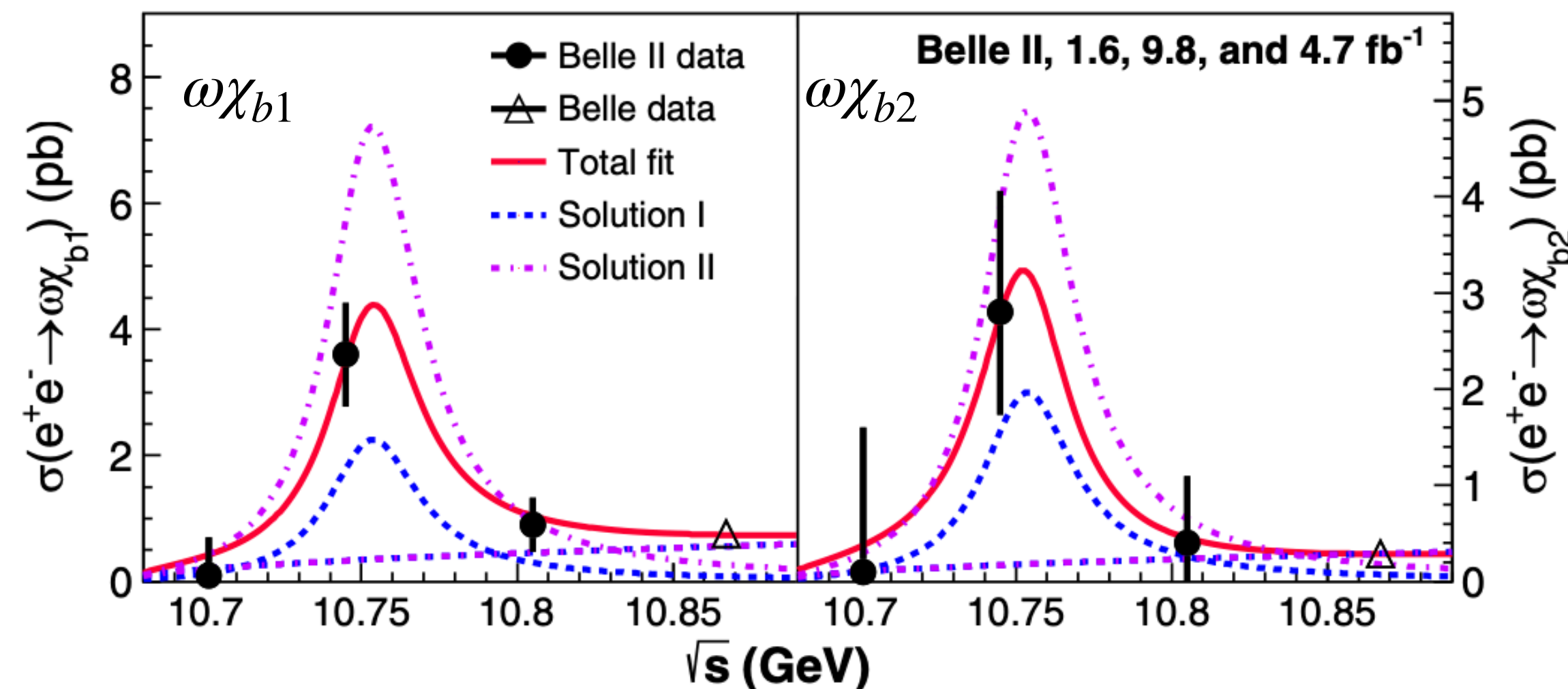
$$\frac{\sigma(e^+e^- \rightarrow \omega\chi_{bJ})}{\sigma(e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-)} \sim \begin{matrix} 1.5 \text{ at } \Upsilon(10753) \text{ GeV} \\ 0.15 \text{ at } \Upsilon(5S) \text{ GeV} \end{matrix}$$

\Rightarrow $\Upsilon(10753)$ and $\Upsilon(5S)$ have different internal structure?

$$\frac{\sigma(e^+e^- \rightarrow \omega\chi_{b1})}{\sigma(e^+e^- \rightarrow \omega\chi_{b2})} = 1.3 \pm 0.6 \text{ at } \sqrt{s} = 10.745 \text{ GeV}$$

Contradicts the expectations for a pure D -wave bottomonium state: **15**

An observation of 1.8σ difference with the prediction for a $S - D$ mixed state: **0.2**



Solution 1: constructive interference

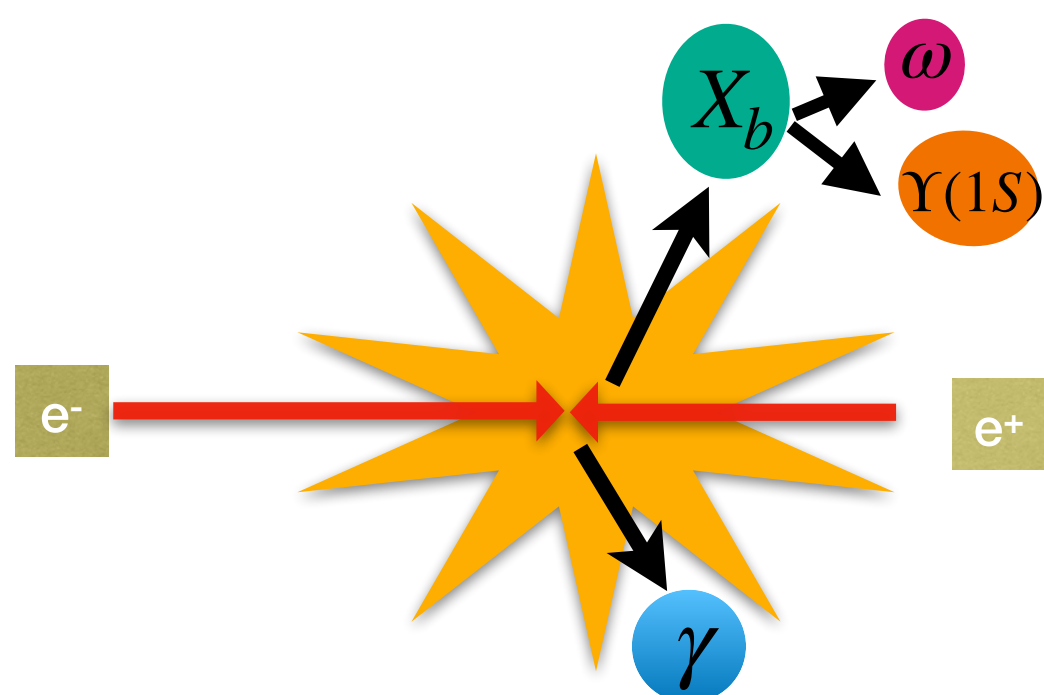
Solution II: destructive interference

Channel	\sqrt{s} (GeV)	N_{sig}	$\sigma_{\text{Born}}^{(\text{UL})}$ (pb)
$\omega\chi_{b1}$	10.745	$68.9^{+13.7}_{-13.5}$	$3.6^{+0.7}_{-0.7} \pm 0.4$
$\omega\chi_{b2}$		$27.6^{+11.6}_{-10.0}$	$2.8^{+1.2}_{-1.0} \pm 0.5$
$\omega\chi_{b1}$	10.805	$15.0^{+6.8}_{-6.2}$	1.6 @90% C.L.
$\omega\chi_{b2}$		$3.3^{+5.3}_{-3.8}$	1.5 @90% C.L.

Search for $\Upsilon(10753) \rightarrow \gamma X_b$

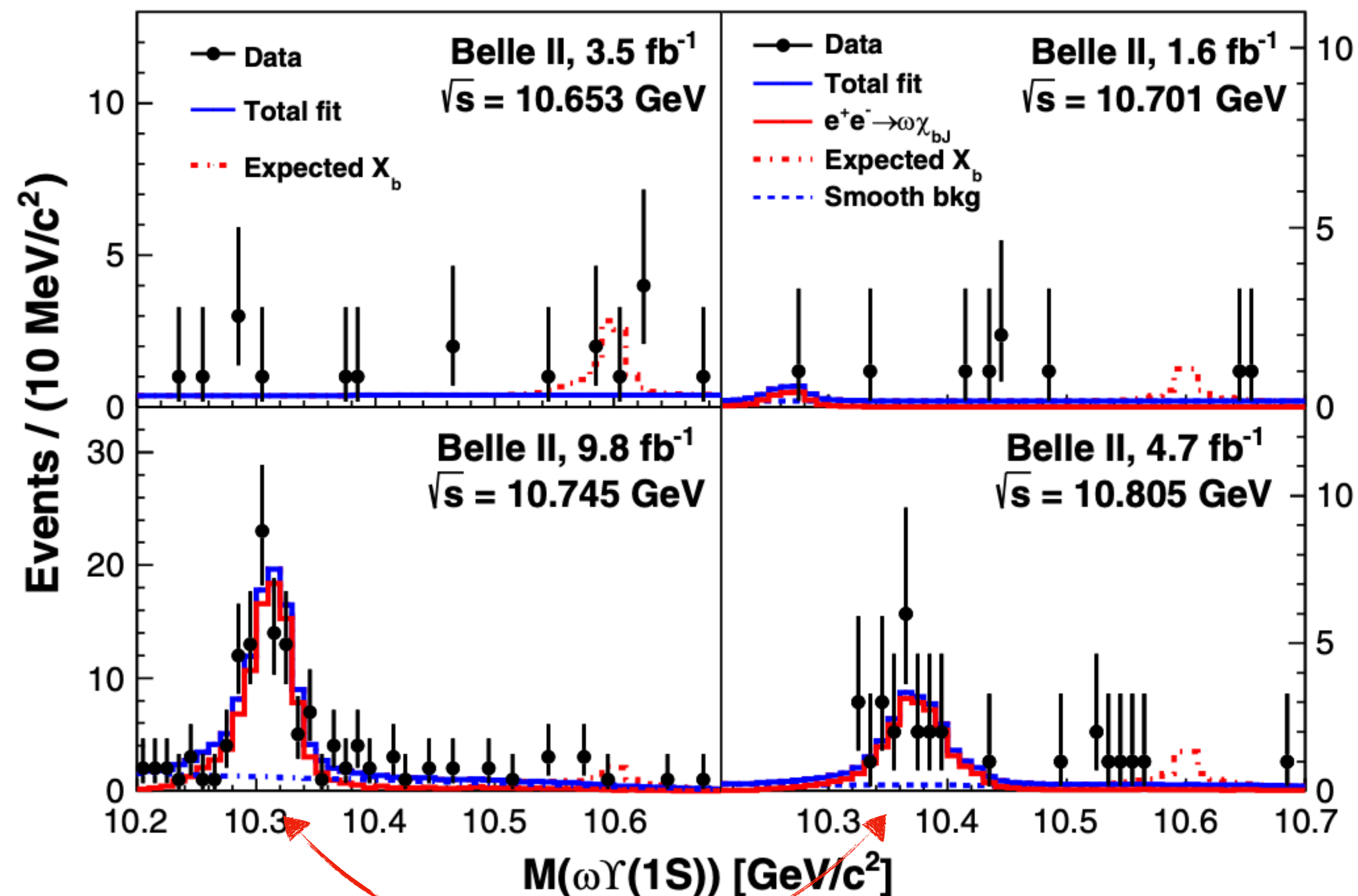
PRL 130, 091902 (2023)

The X_b is posited bottomonium counterpart of X(3872).



- No significant signal of X_b signal is observed.
- Upper limits on cross sections are set for $M(X_b) \in [10.45, 10.65]$ GeV

\sqrt{s} GeV	$\sigma_B(e^+e^- \rightarrow \gamma X_b) \times \mathcal{B}(X_b \rightarrow \omega Y(1S))$
10.653	0.14-0.55
10.701	0.25-0.84
10.745	0.06-0.14
10.805	0.08-0.37



Reflection of $e^+e^- \rightarrow \omega \chi_{bJ}(1P)$

Search for $\Upsilon(10753) \rightarrow \omega\chi_{b0}(1P)/\omega\eta_b(1S)$

Search for $\Upsilon(10753) \rightarrow \omega\chi_{b0}(1P)/\omega\eta_b(1S)$

► Motivation:

◆ $\Upsilon(10753) \rightarrow \eta_b(1S) \omega$

- Theoretically, tetraquark interpretation predicts,
 - a strong enhancement of the decay $\eta_b(1S) \omega$ compared to $\Upsilon\pi^+\pi^-$

$$\frac{\Gamma(\eta_b\omega)}{\Gamma(\Upsilon\pi^+\pi^-)} \sim 30$$

CPC 43 (2019) 12, 123102

◆ $\Upsilon(10753) \rightarrow \chi_{b0}(1S)\omega$

- In charmonium analogy, $Y(4260) \rightarrow \chi_{c0}(1P) \omega$ transition is enhanced compared to $Y(4260) \rightarrow \chi_{c1,c2}(1P) \omega$

- Not observed in full reconstruction analysis of $\Upsilon(10753) \rightarrow \chi_{bJ}(1S) \omega$ due to small branching fraction

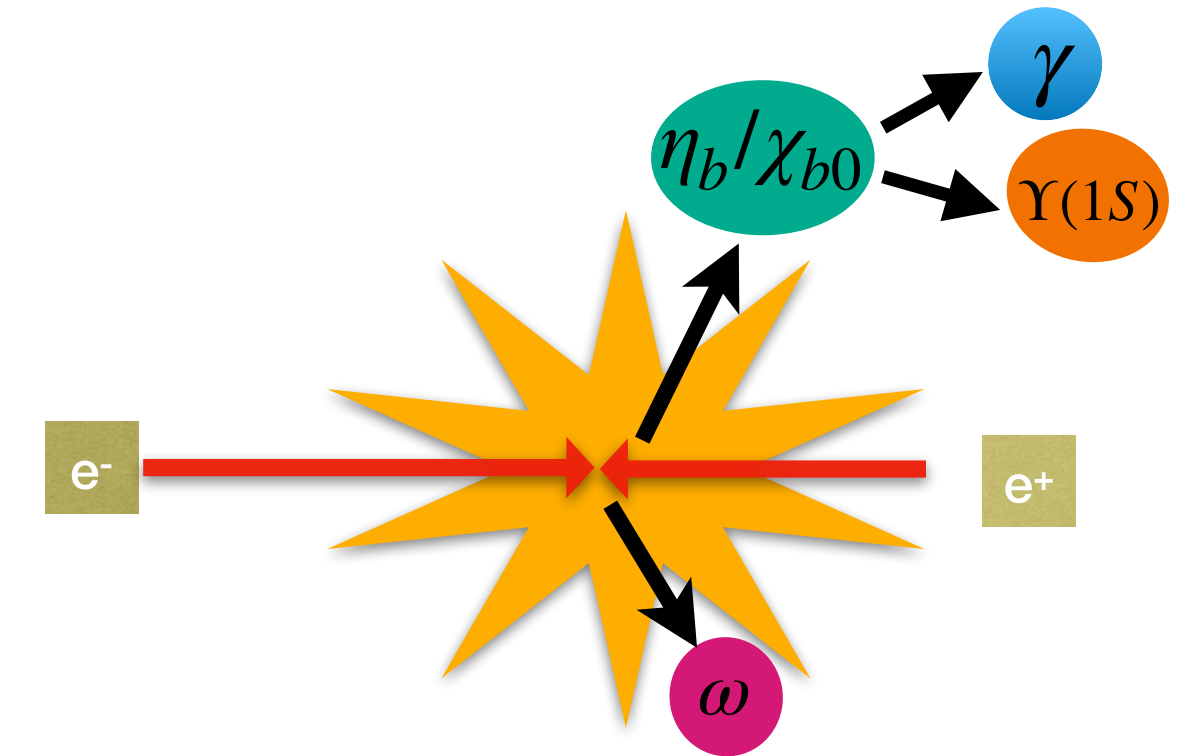
PRD 99, 091103(R) (2019)

► Strategy

◆ Partial reconstruction:

- Reconstructed ω meson in $\pi^+\pi^-\pi^0$ and use the recoil mass of ω as signal variable

$$M_{\text{recoil}}(\pi^+\pi^-\pi^0) = \sqrt{\left(\frac{\sqrt{s} - E^*}{c^2}\right)^2 - \left(\frac{p^*}{c}\right)^2}$$



PRL 130 091902 (2023)

Results

- ▶ No significant $\omega \chi_{b0}(1P)$ and $\omega \eta_b(1S)$ signals are observed.
- ▶ Upper limits at the 90% C.L. on the Born cross section are set.

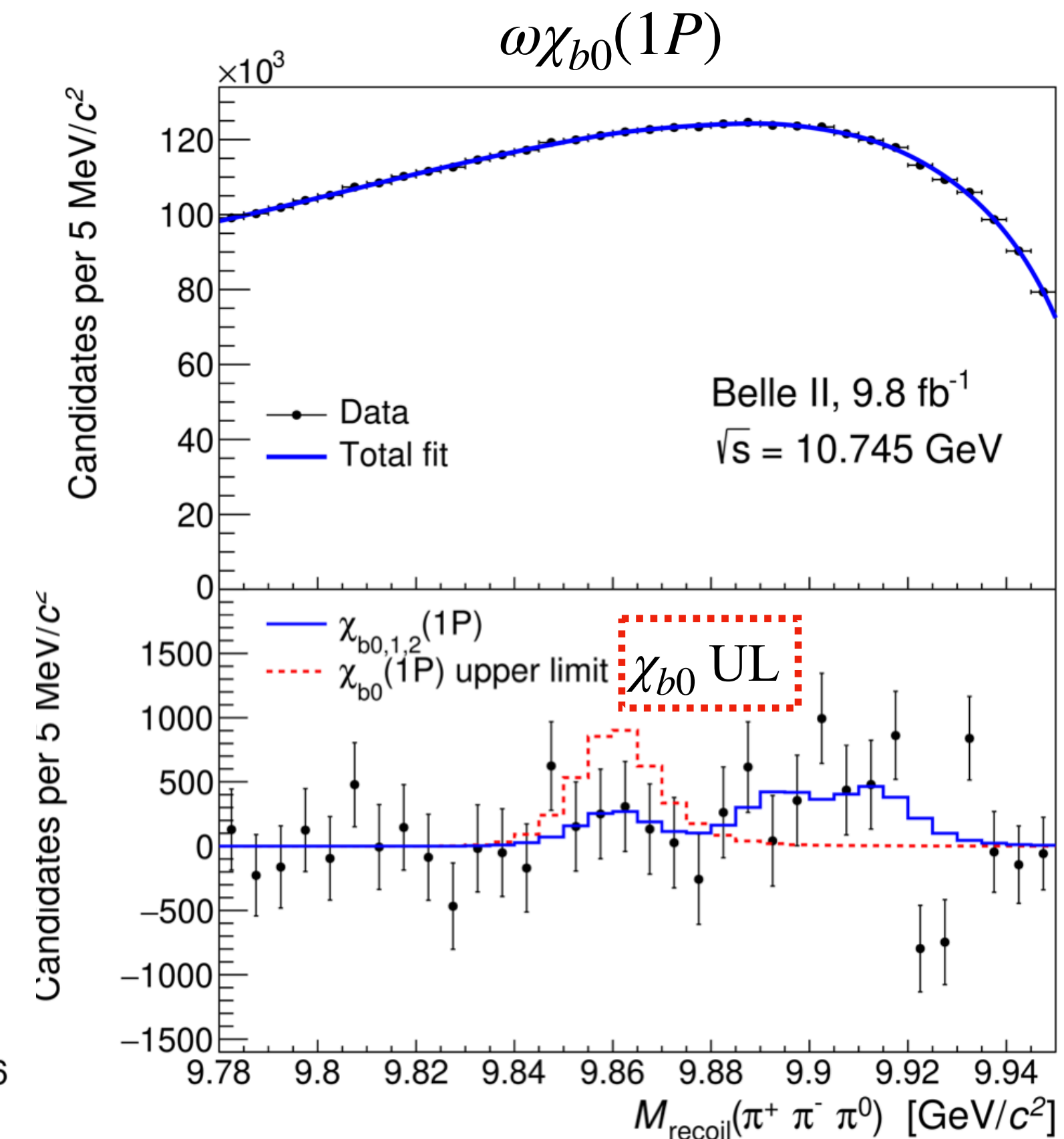
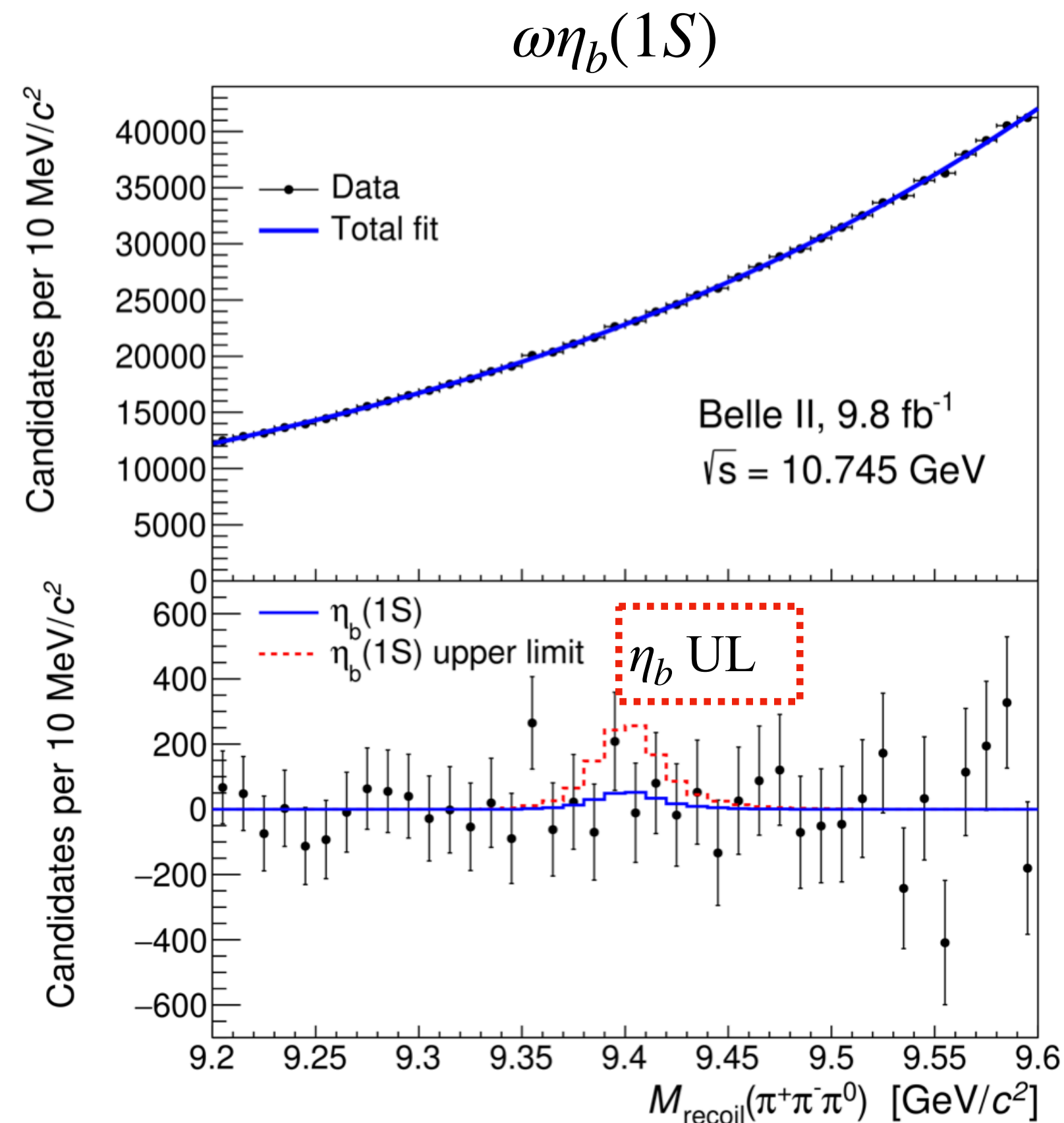
$\omega \rightarrow \pi^+ \pi^- \pi^0$ recoil mass distributions

▶ $\omega \eta_b(1S)$:

- ◆ $\sigma(e^+e^- \rightarrow \eta_b(1S)\omega) < 2.5$ pb
- ◆ c.f $\sigma(e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-) \sim 2.0$ pb
- ◆ Evidence against the tetraquark model predictions. [CPC 43 \(2019\) 12, 123102](#)

▶ $\omega \chi_{b0}(1P)$:

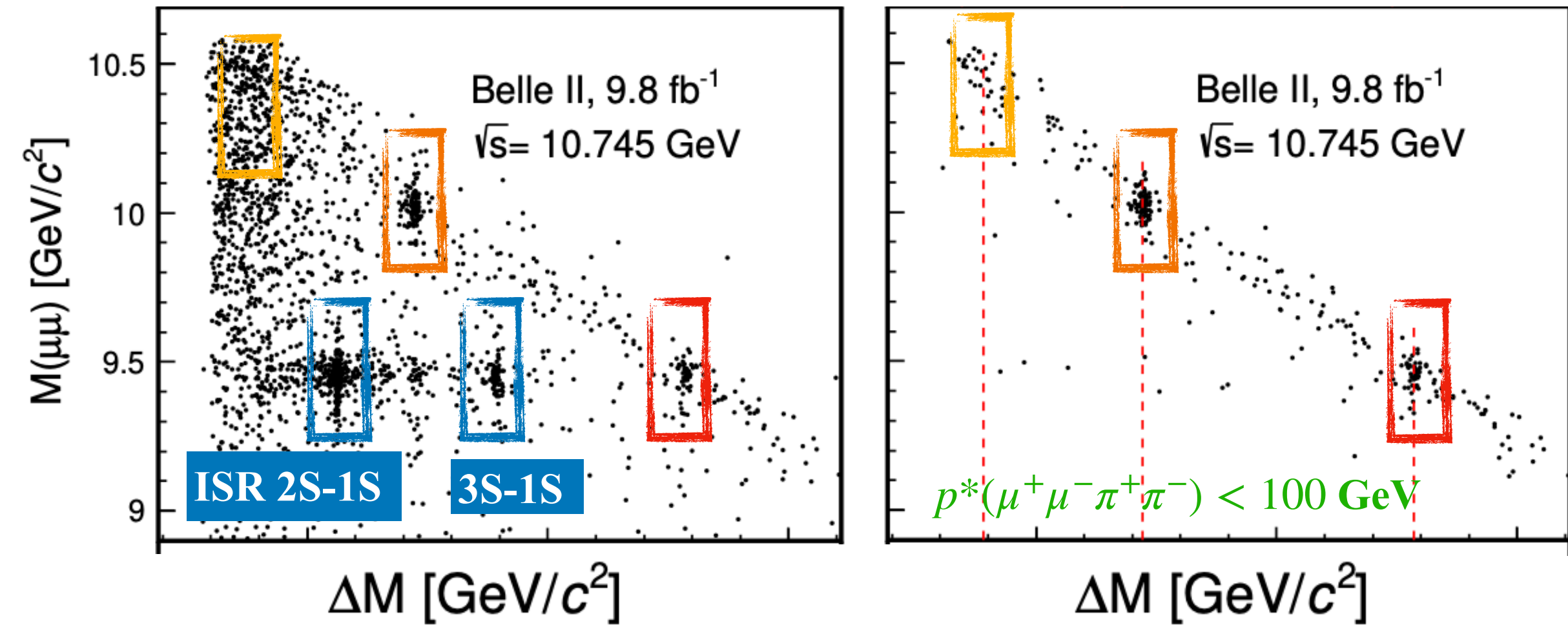
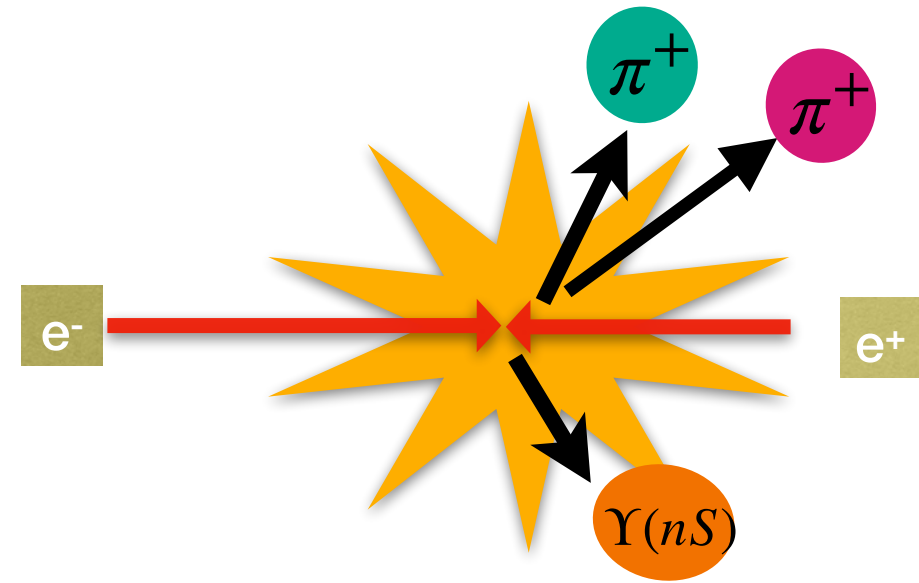
- ◆ $\sigma(e^+e^- \rightarrow \chi_{b0}(1S)\omega) < 8.7$ pb
- ◆ Supports the $S - D$ mixing model [PRD 104 \(2021\), 034036](#)



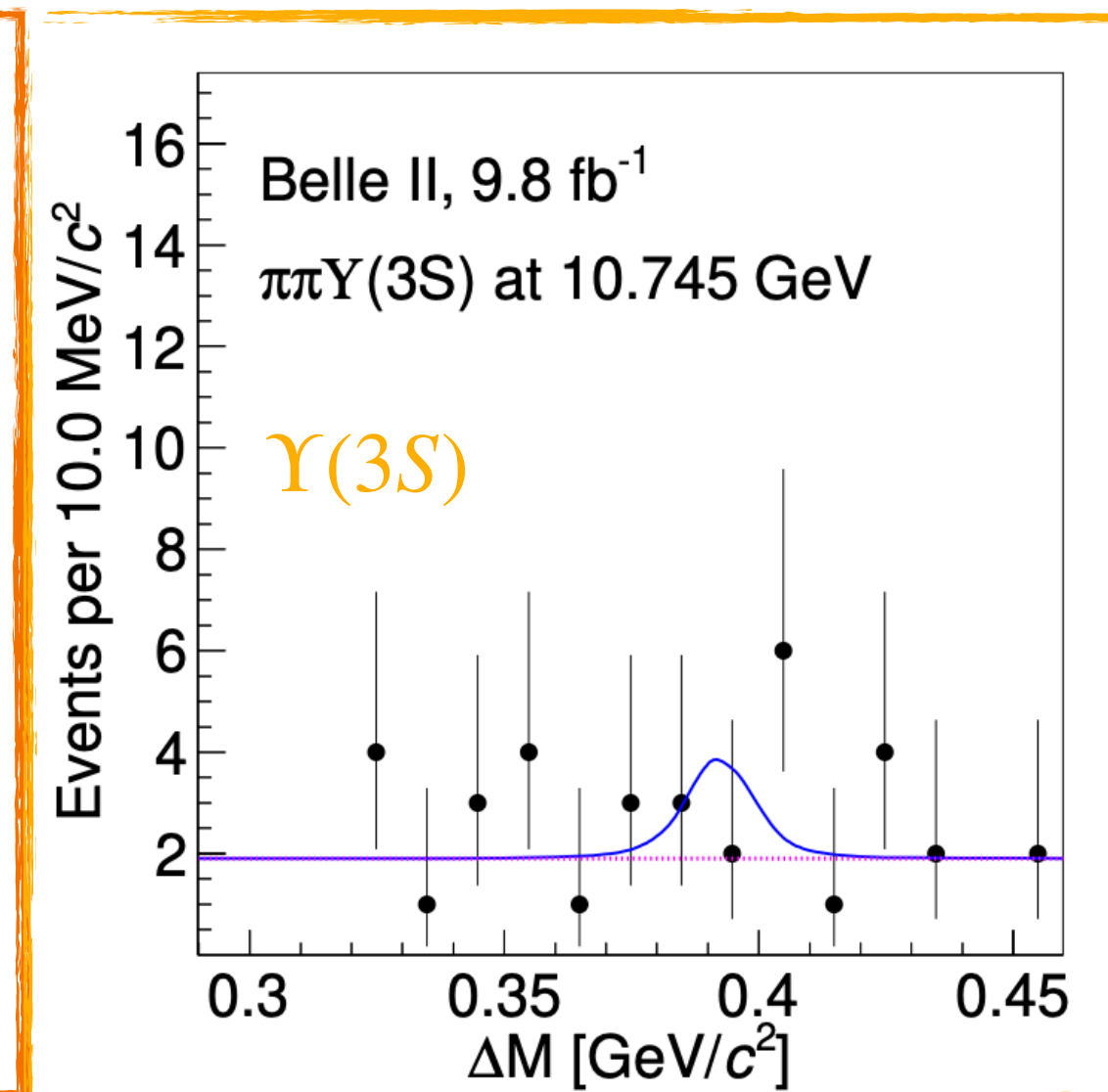
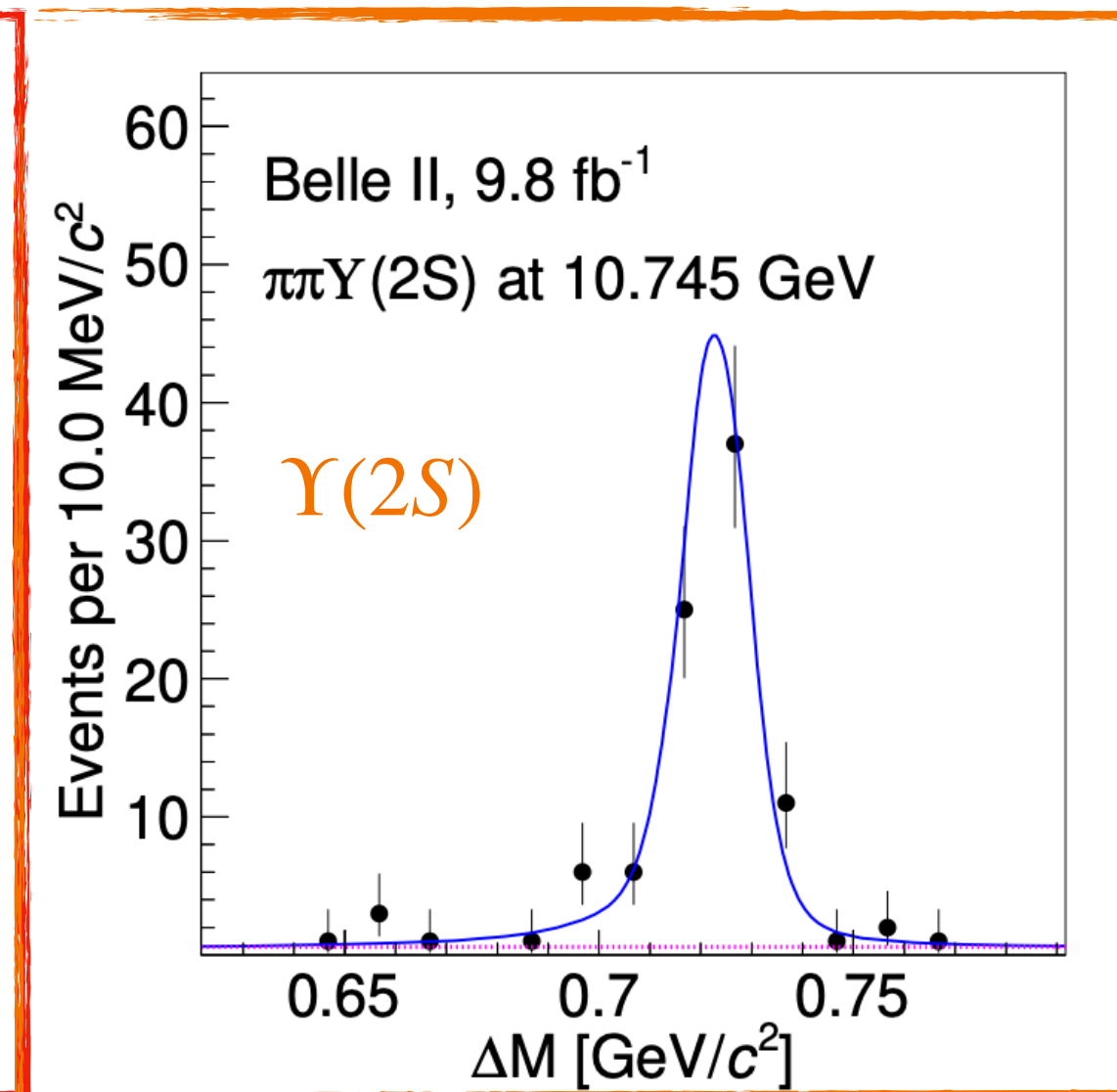
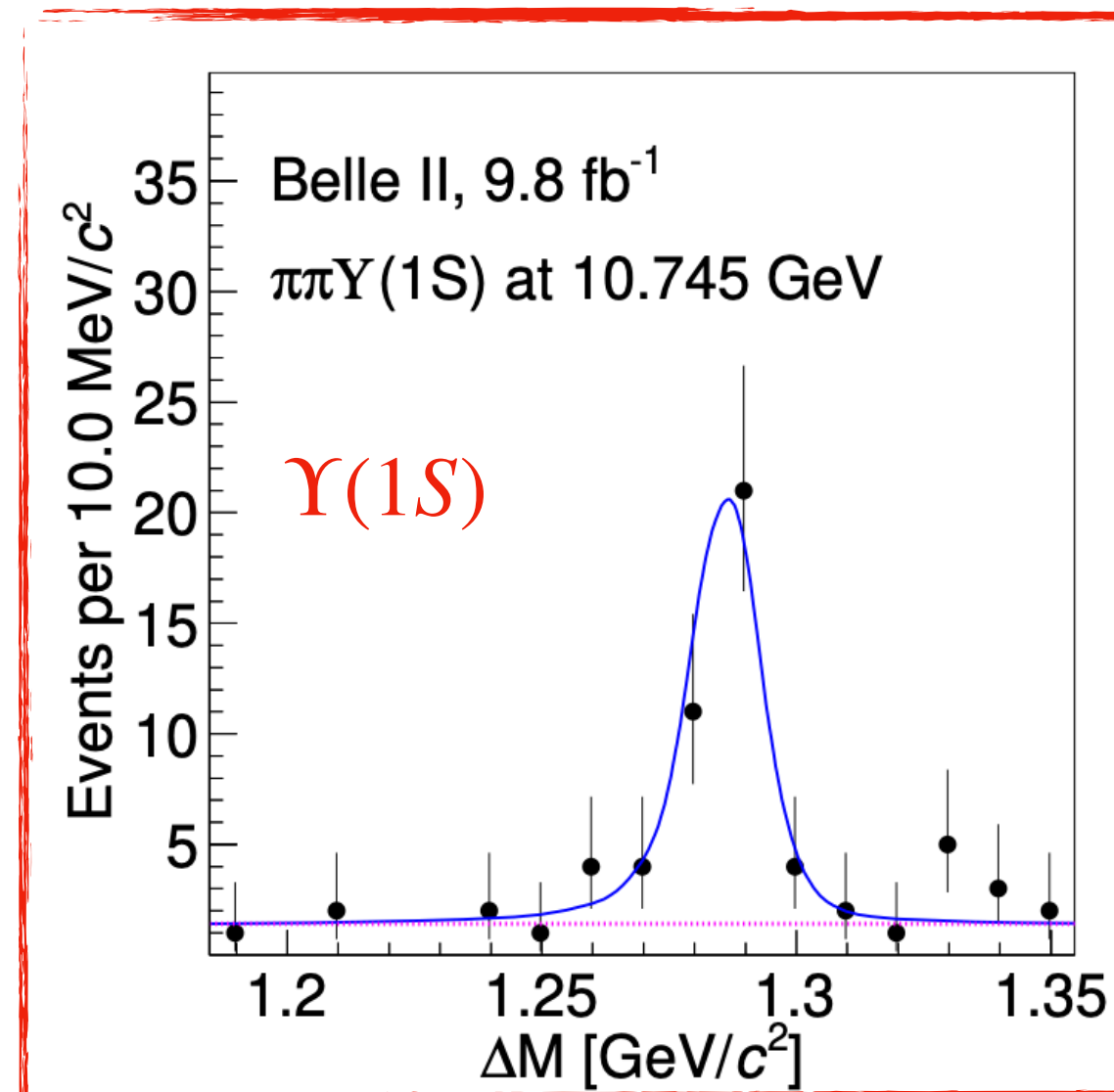
Search for $\Upsilon(10753) \rightarrow \pi^+ \pi^- \Upsilon(nS)$

Search for $\Upsilon(nS) \rightarrow \pi^+\pi^-\Upsilon(nS)$

- Search for $\Upsilon(nS) (\rightarrow \mu^+\mu^-\pi^+\pi^-)$ decay mode.
- $p^*(\mu^+\mu^-\pi^+\pi^-) < 100$ MeV/c to reject ISR.



- Clear signal for $\Upsilon(1S)\pi^+\pi^-$ and $\Upsilon(2S)\pi^+\pi^-$ decay mode.
- No evidence of $\Upsilon(3S)\pi^+\pi^-$

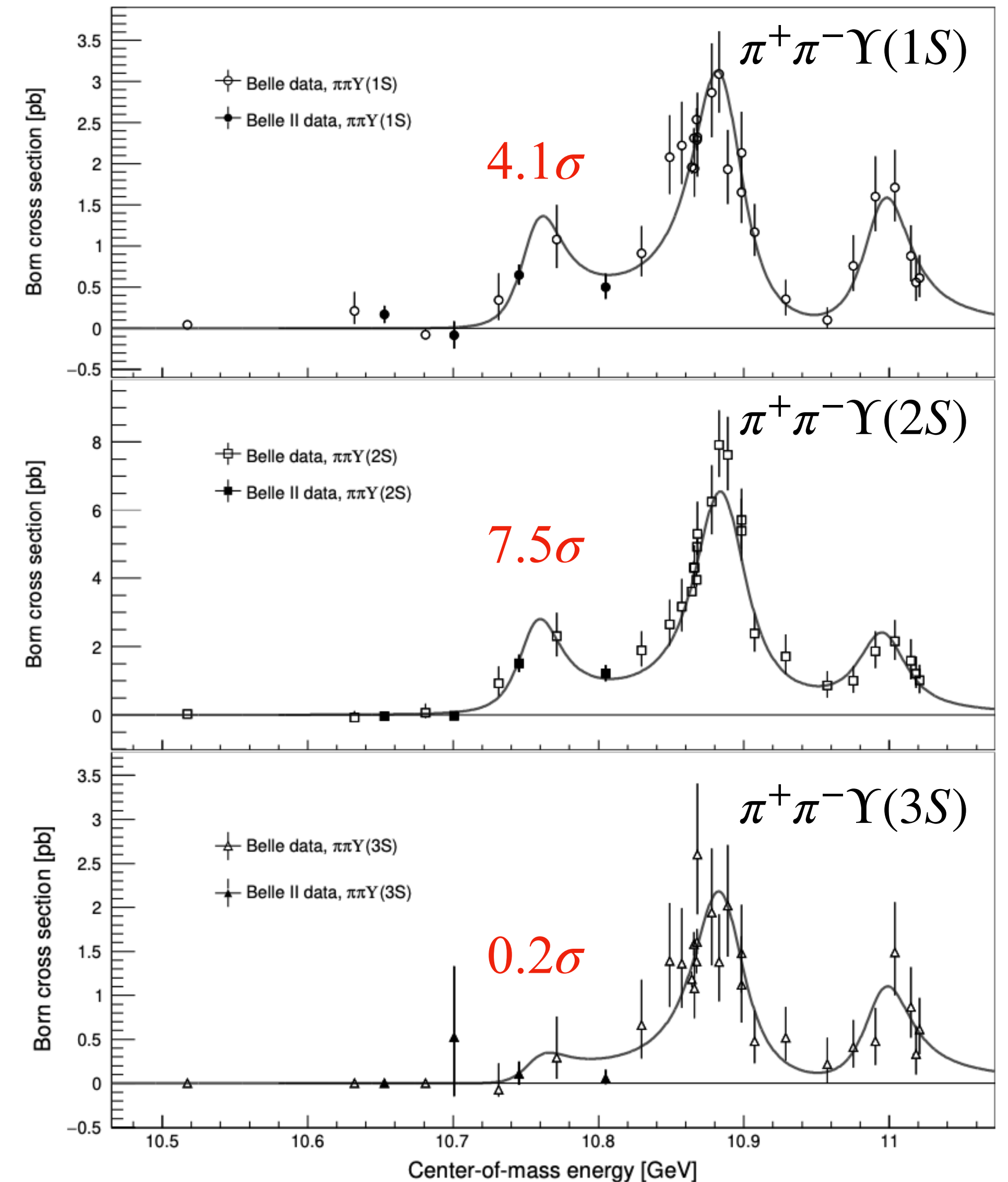


Search for $\Upsilon(10753) \rightarrow \pi^+\pi^-\Upsilon(nS)$

- New measurement **confirms previous Belle result**: cross section is peaking near 10.75 GeV.

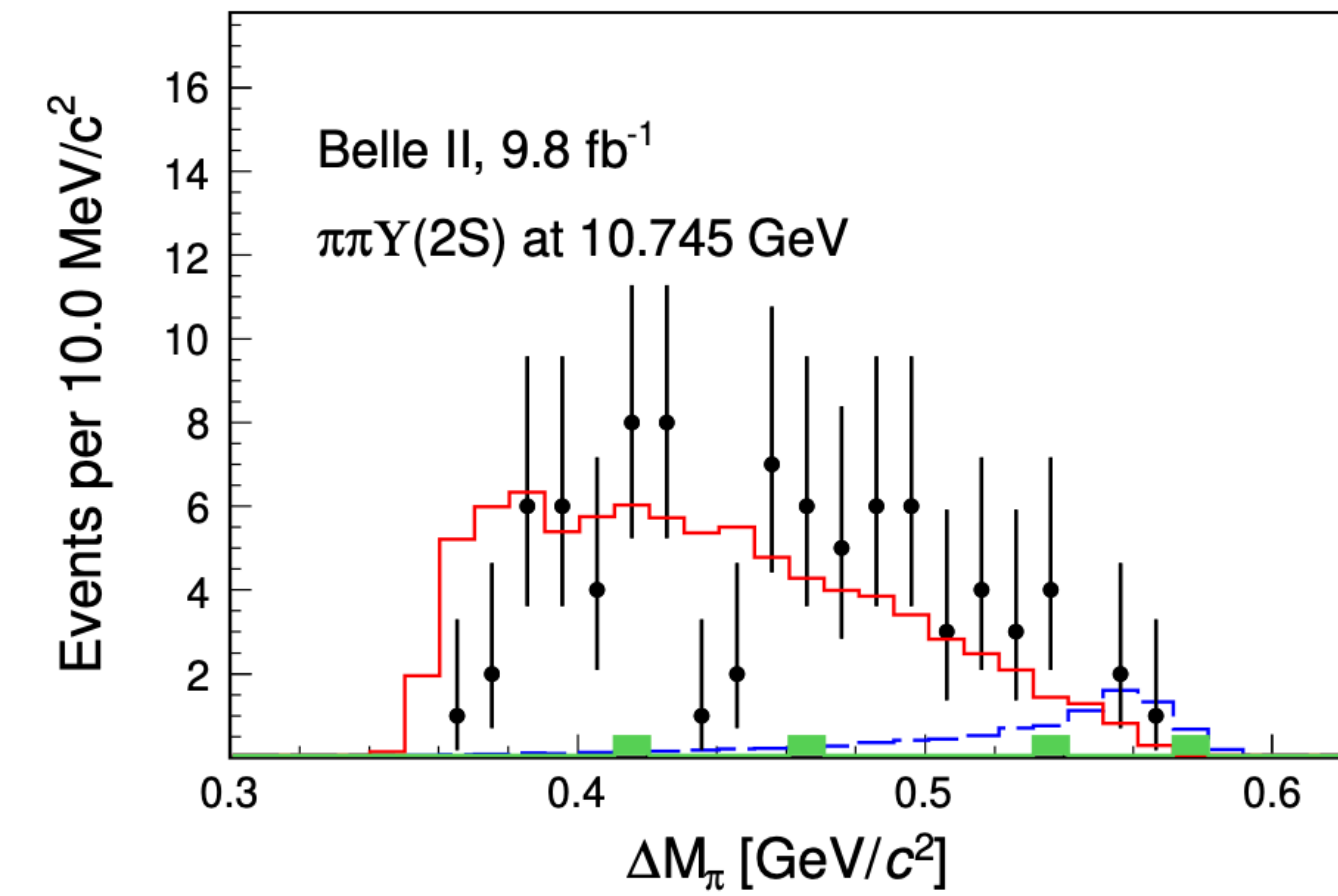
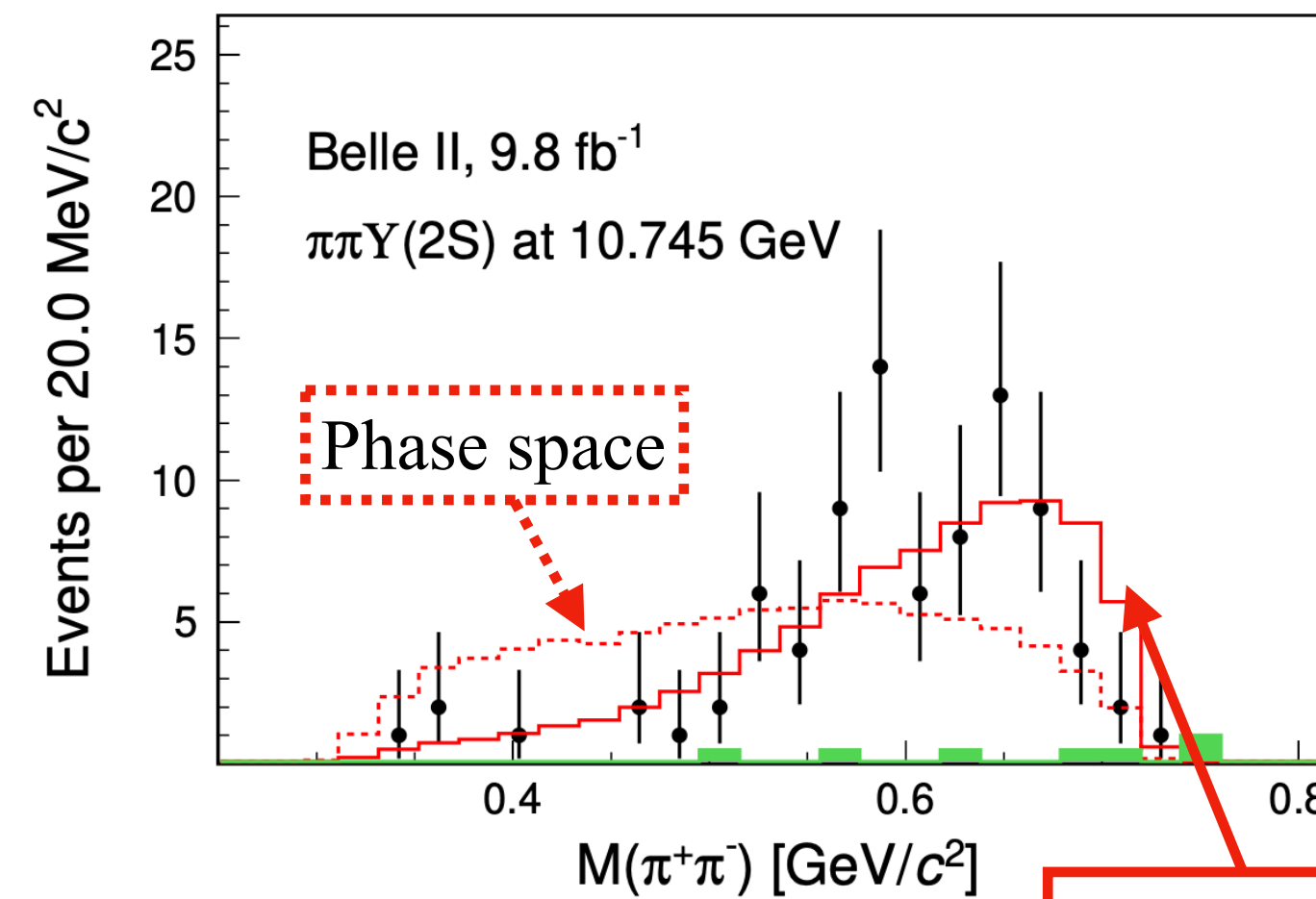
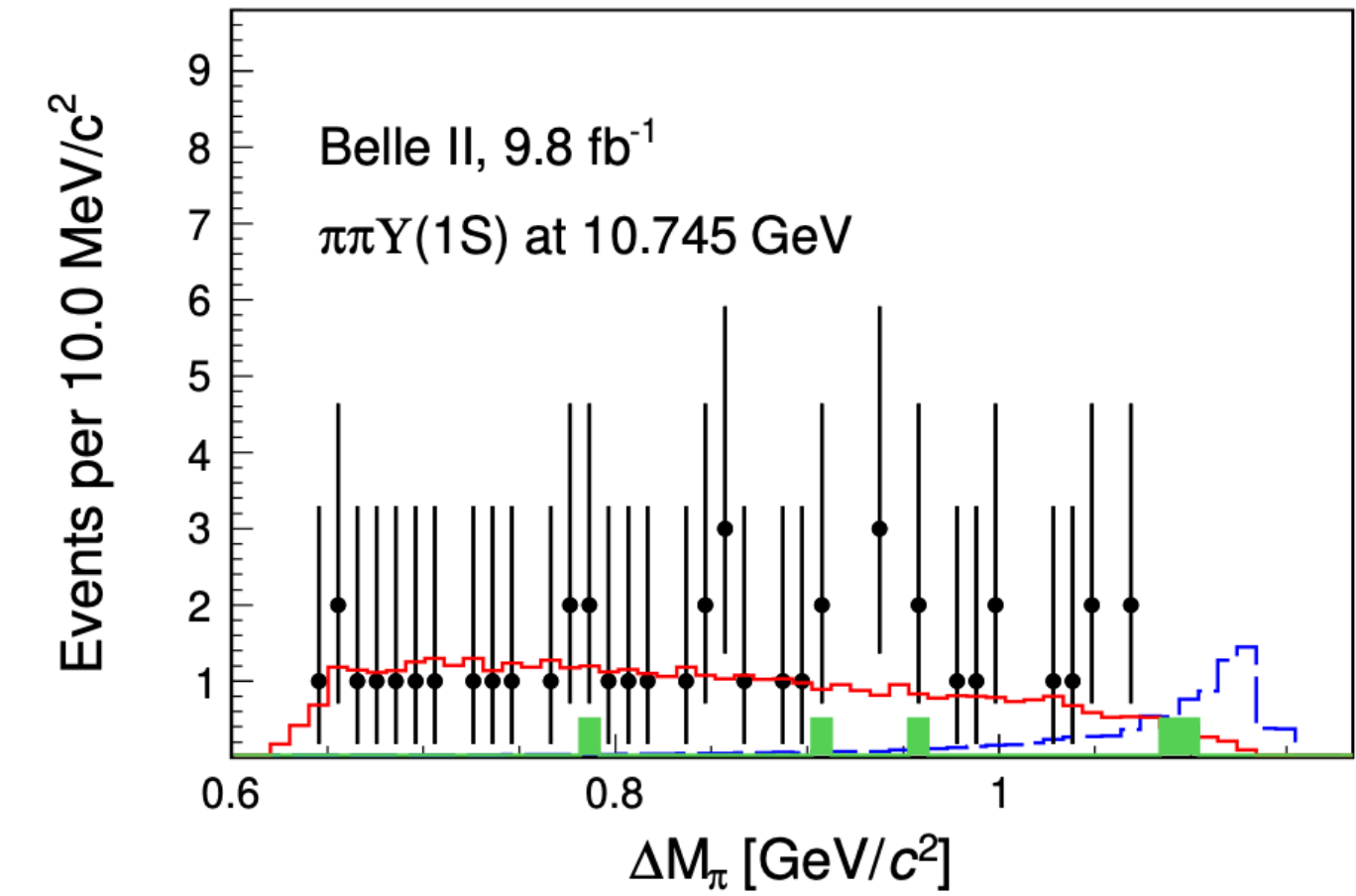
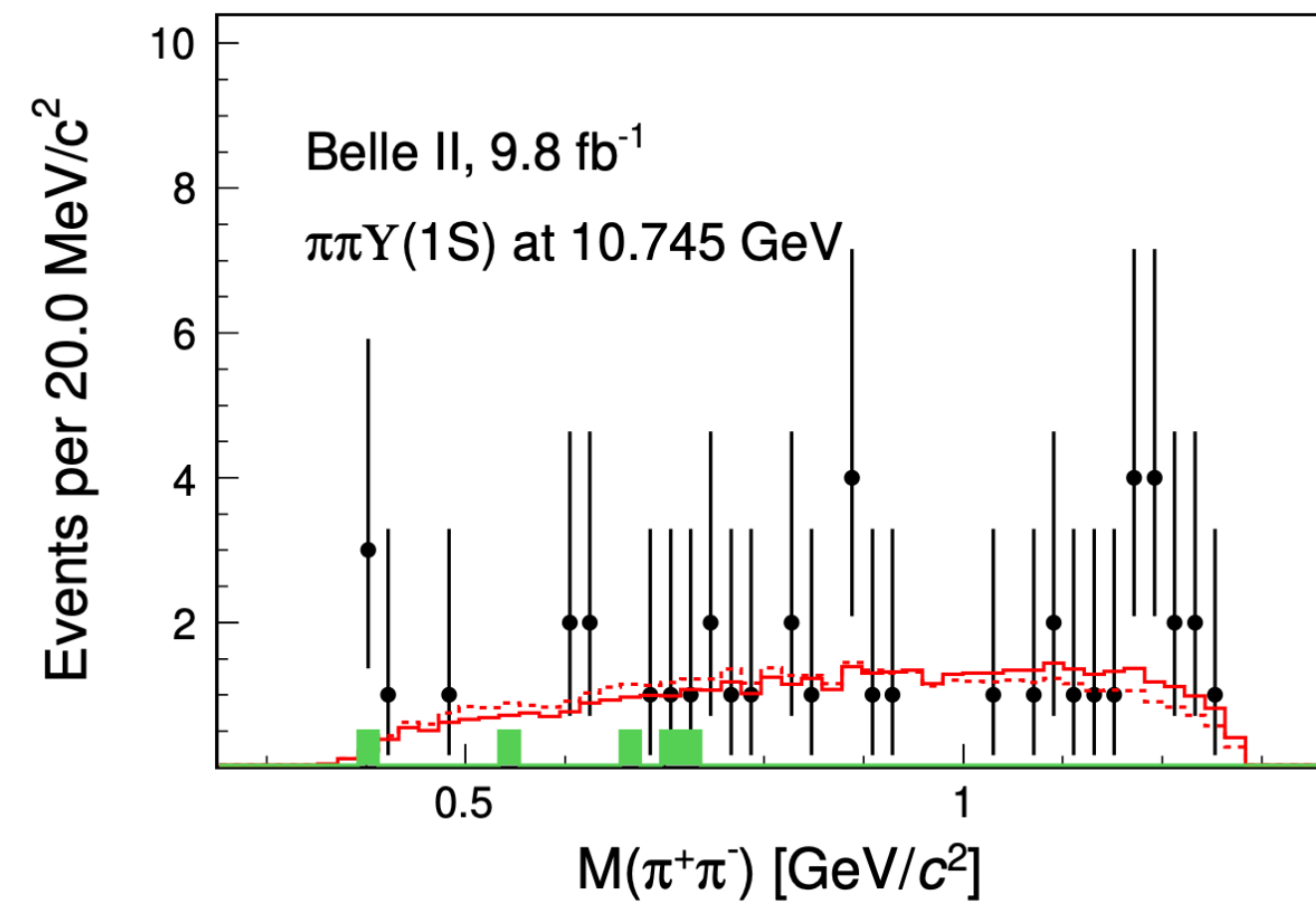
	Belle II	Belle
$M_{\Upsilon(10753)}$	$10756.3 \pm 2.7 \pm 0.6$	$10752.7 \pm 5.9^{+0.7}_{-1.1}$
$\Gamma_{\Upsilon(10753)}$	$29.7 \pm 8.5 \pm 1.1$	$35.5^{+17.6+3.9}_{-11.3-3.3}$

- Results are in consistent with the Belle results.
- Uncertainties are improved by a factor of two from previous Belle results.



Resonant structure in $\Upsilon(10753) \rightarrow \pi^+\pi^-\Upsilon(nS)$

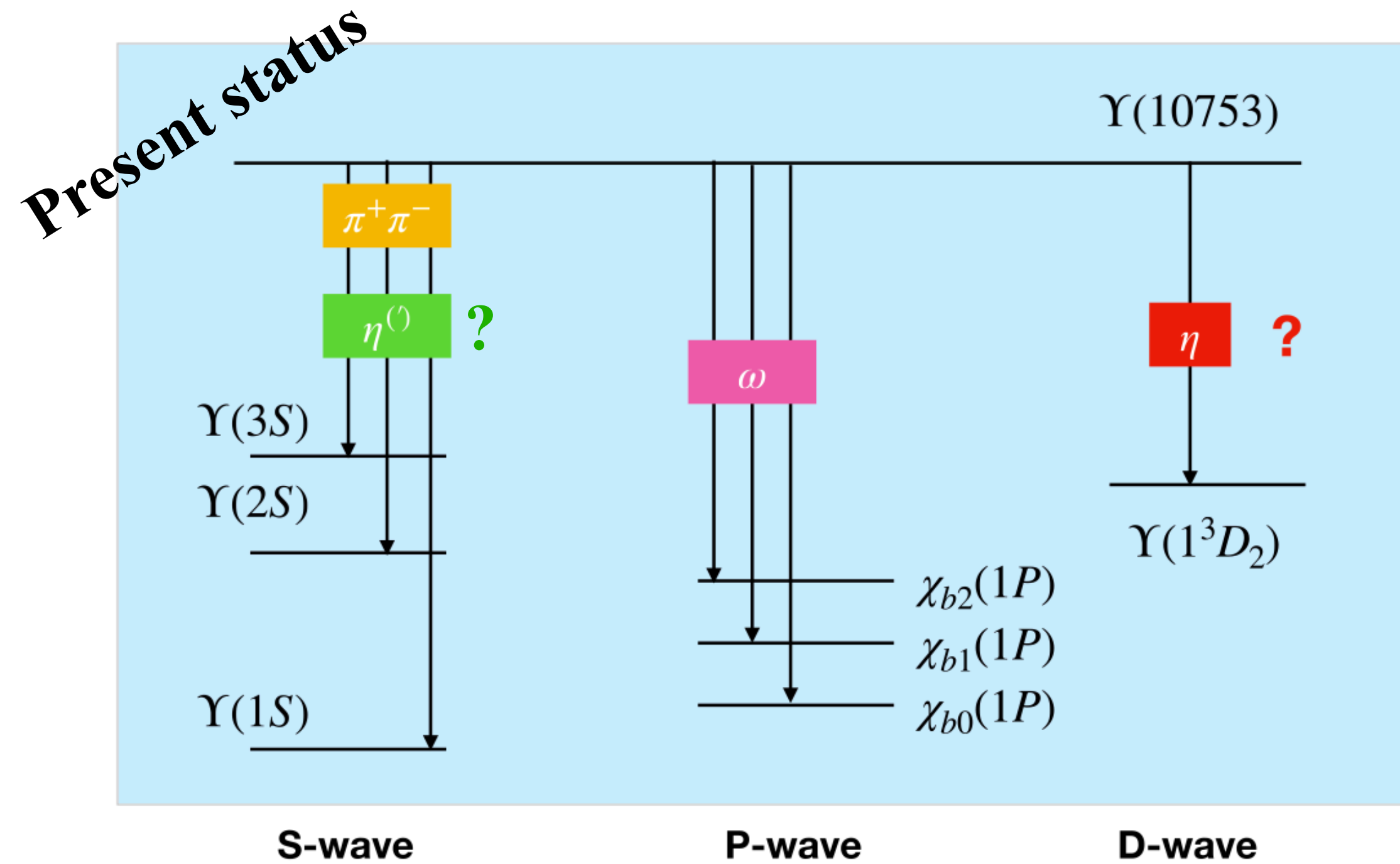
- No signal of intermediate $Z_b^+(10610)$ or $Z_b^+(10650)$ resonances are observed.
- $\pi^+\pi^-\Upsilon(1S)$: $M(\pi^+\pi^-)$ distribution is consistent with phase space.
- $\pi^+\pi^-\Upsilon(2S)$: larger values of $M(\pi^+\pi^-)$ enhanced (similar to $\Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$ process)



CLEO parametrization

Conclusion on $\Upsilon(10753)$

- ▶ New decay modes $\Upsilon(10753) \rightarrow \omega\chi_{b1,2}(1P)$ are observed for the first time.
- ▶ A stringent upper limit is set for the $\Upsilon(10753) \rightarrow \eta_b(1S)\omega$ at $\sqrt{s} = 10.745$ GeV.
- ▶ Improved results for mass and width of $\Upsilon(10753)$ using $\Upsilon(10753) \rightarrow \Upsilon(nS)\pi^+\pi^-$.
- ▶ No signal of intermediate $Z_b^+(10610)$ or $Z_b^+(10650)$ resonances are observed.



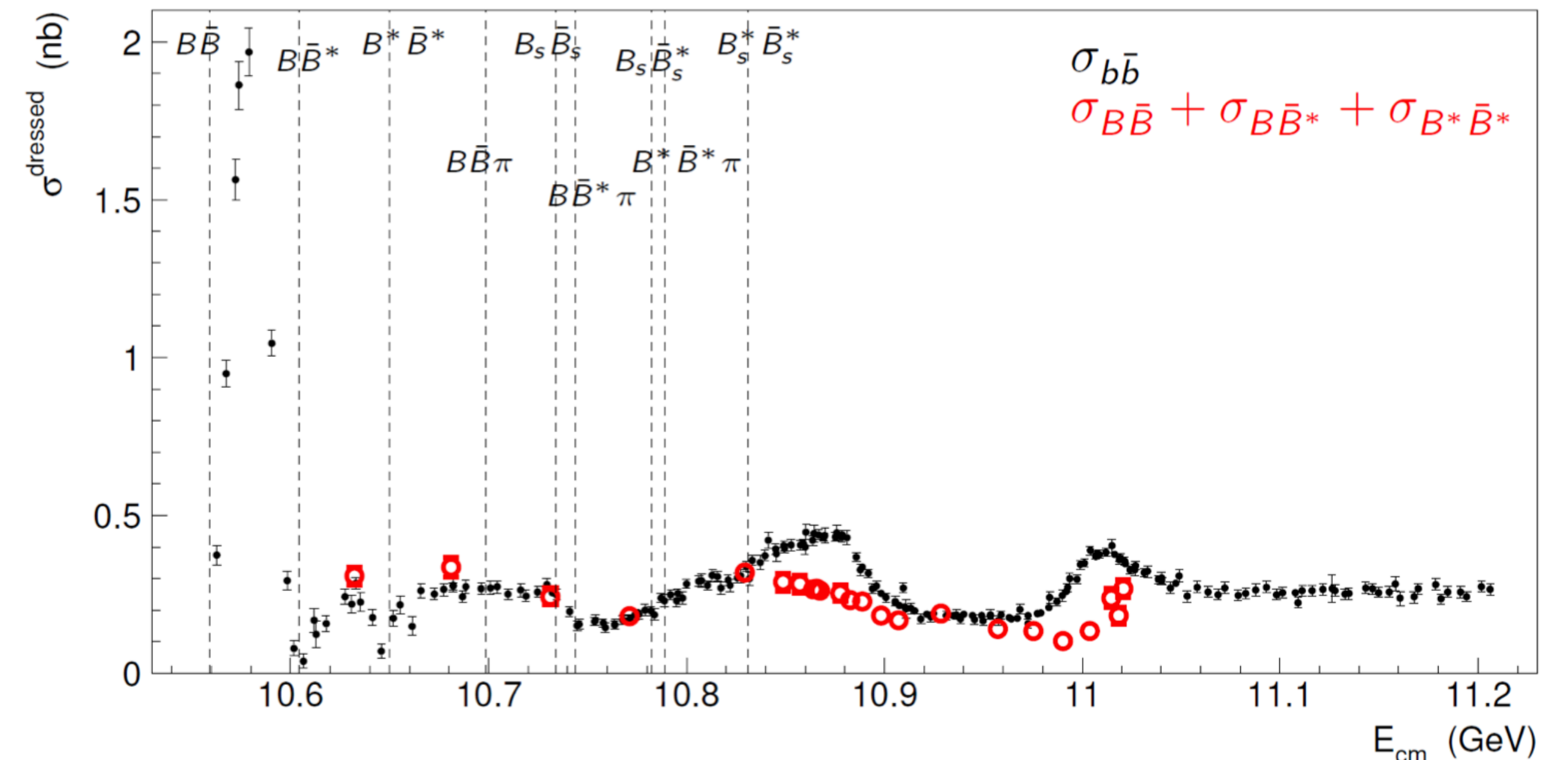
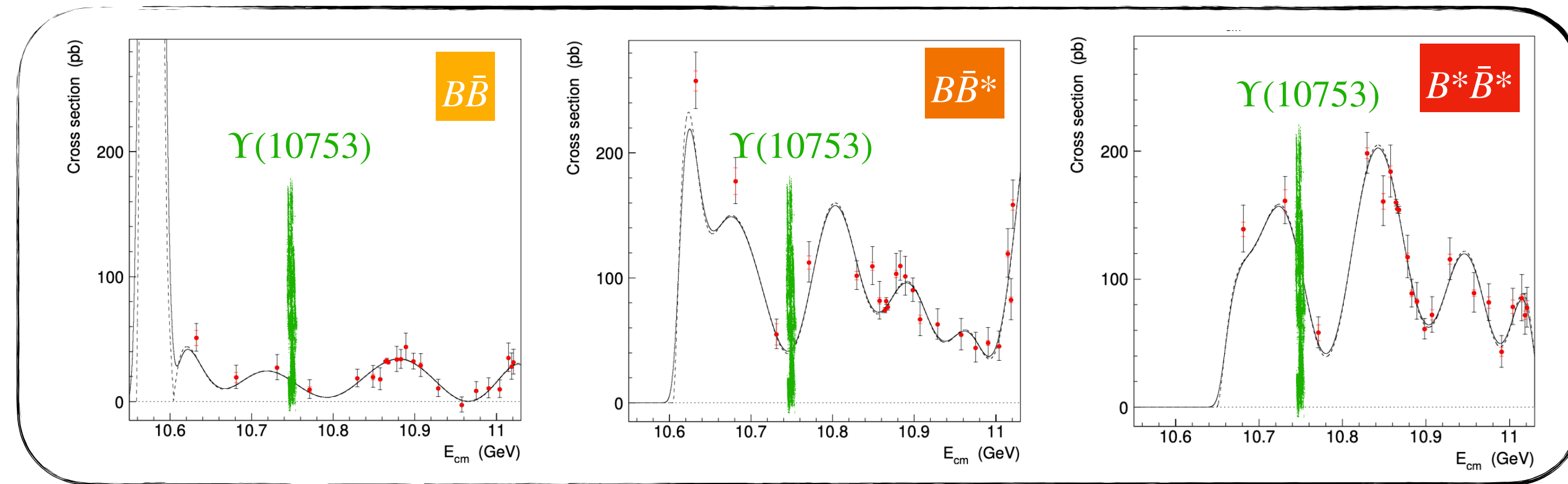
Energy dependence of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

Energy dependence of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

Belle results

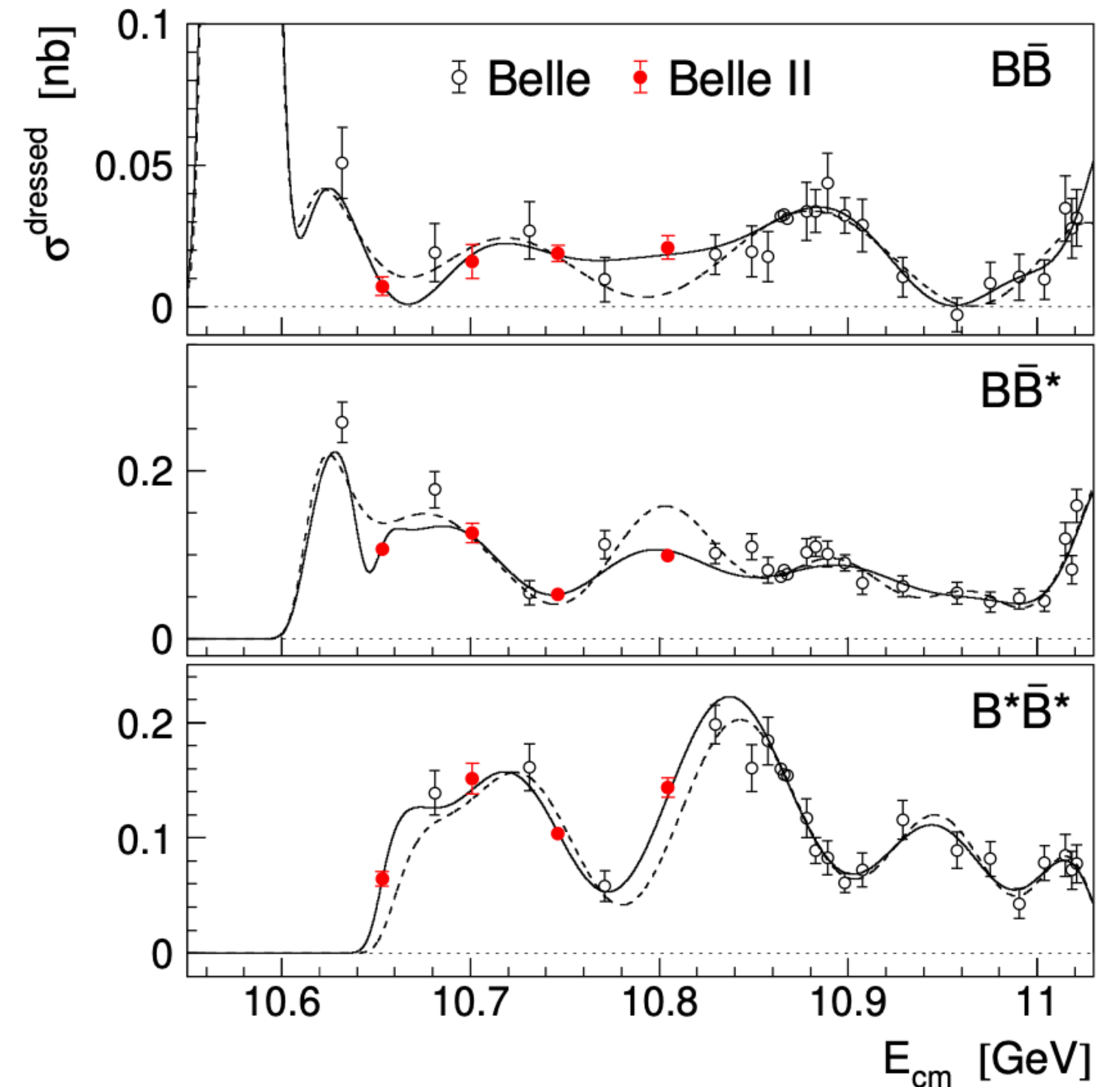
► Motivation:

- ◆ The open flavor final states ($B^{(*)}\bar{B}^{(*)}$) make dominant contribution to $b\bar{b}$ cross-section.
 - Their measurements are critical for understanding the structure of $b\bar{b}$ states.
- ◆ Belle measured the energy dependencies of $\sigma(e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)})$ and observed an oscillatory behavior.
 - Channels $B^{(*)}\bar{B}^{(*)}$ saturate the cross-section below the $B_s^*\bar{B}_s^*$ threshold.
- ◆ The measured cross sections can be used in the coupled channel analysis of all available scan data to extract the parameters of the Υ states.
- ◆ To improve the accuracy below $\Upsilon(5S)$ and understand the nature of $\Upsilon(10753)$, need more data: Belle II



Energy dependence of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

- ▶ The obtained cross sections at four energies are consistent with the Belle results.
- ▶ $\sigma(e^+e^- \rightarrow B^*\bar{B}^*)$ increases rapidly above $B^*\bar{B}^*$ threshold
- ◆ Similar phenomenon was observed near $D^*\bar{D}^*$ threshold.
- ◆ **Possible interpretation: resonance or bound state ($B^*\bar{B}^*$ or $b\bar{b}$) near $B^*\bar{B}^*$ threshold**
- ◆ Inelastic channels [$\pi^+\pi^-\Upsilon(nS)$ and $h_b(1P)\eta$] could also be enhanced

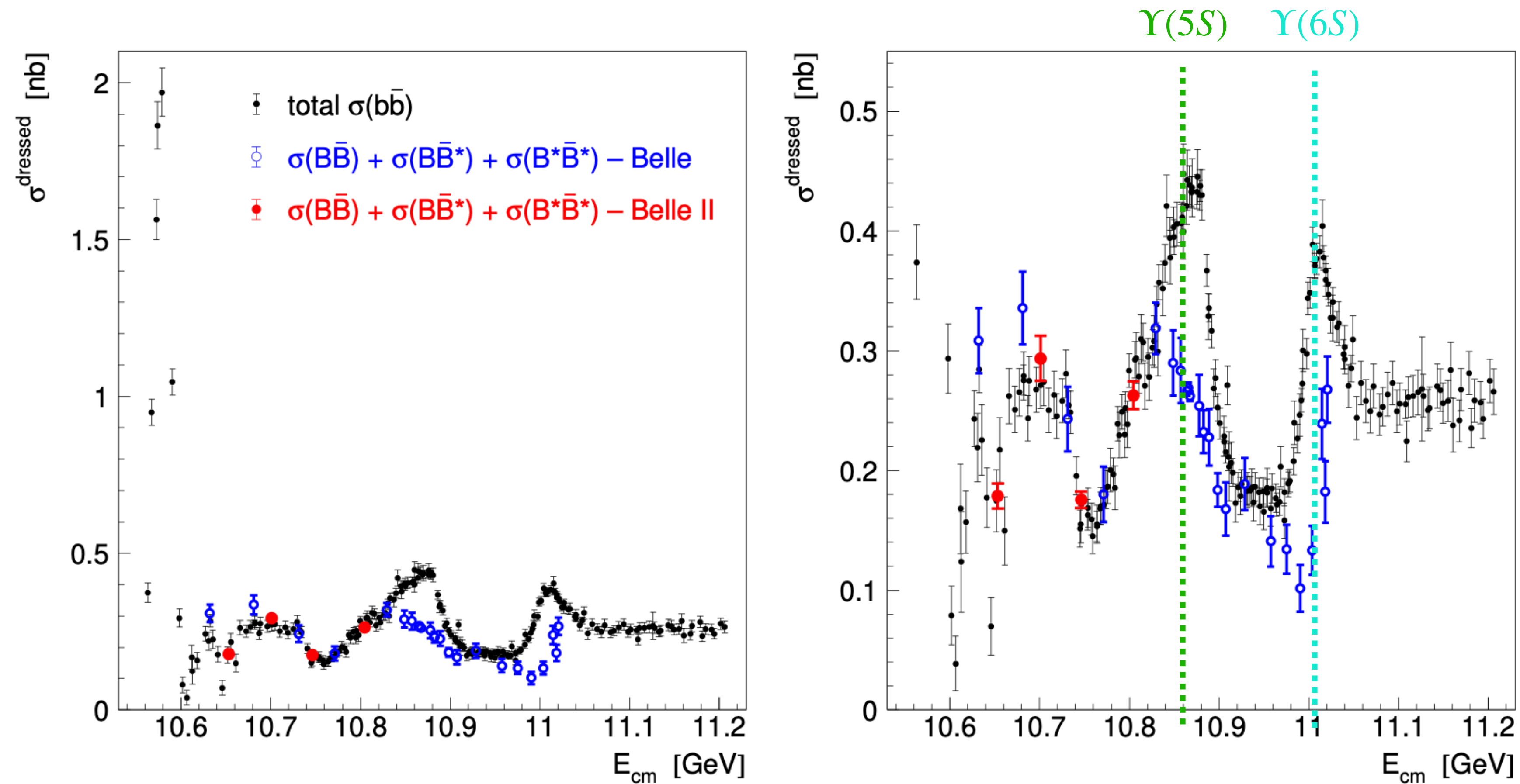


Solid curve – combined Belle + Belle II data fit

Dashed curve – Belle data fit only

Energy dependence of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

Comparison of $\sigma_{b\bar{b}}$ and $\sigma_{B\bar{B}} + \sigma_{B\bar{B}^*} + \sigma_{B^*\bar{B}^*}$



- Agreement with $\sigma_{b\bar{b}}$ below the $B_s^{(*)}\bar{B}_s^{(*)}$ threshold.
- Deviation at high energy is presumably due to $B_s^*\bar{B}_s^*$, multi-body $B^{(*)}\bar{B}^{(*)}\pi(\pi)$, etc.

- ▶ We are at the beginning of a long program of quarkonium physics.
- ▶ The unique scan data near $\sqrt{s} = 10.75$ GeV at Belle II provides an opportunity
 - ▶ To understand the nature of the $\Upsilon(10753)$ energy region,
 - ▶ The quarkonium spectroscopy.





Belle II detector

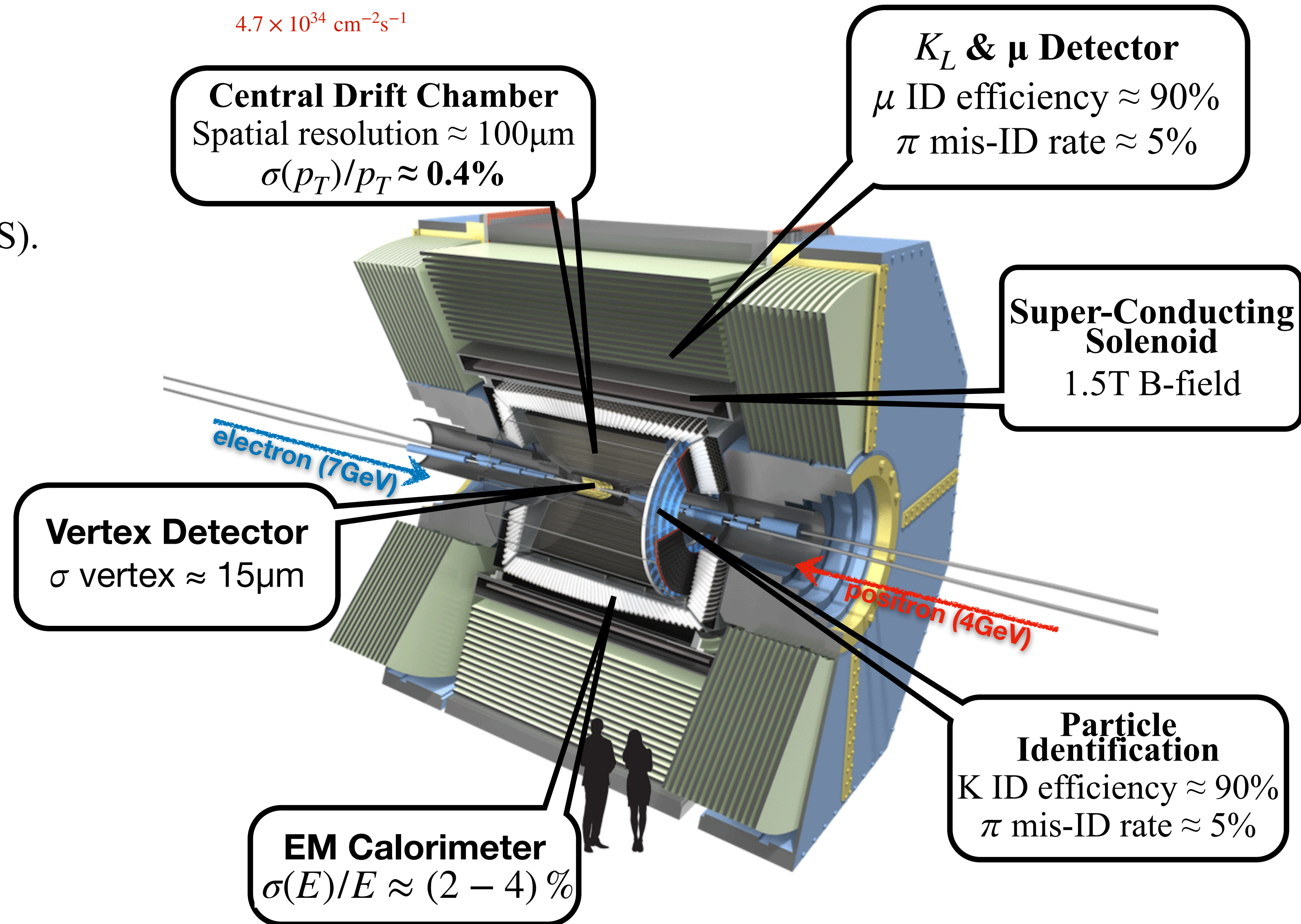
- ▶ Asymmetric e^+e^- collider
- ▶ **Collected data**
 - $\sim 362 \text{ fb}^{-1}$ at Y(4S)
 - 42 fb^{-1} off-resonance, 60 MeV below Y(4S).
 - 19 fb^{-1} energy scan between 10.6 to 10.8 GeV for exotic hadron studies.

Features:

- ▶ Near-hermetic detector
- ▶ Excellent vertexing and tracking
- ▶ High-efficiency detection of neutrals (γ , π^0 , η , η' , ...)
- ▶ Good charged particle reconstruction.

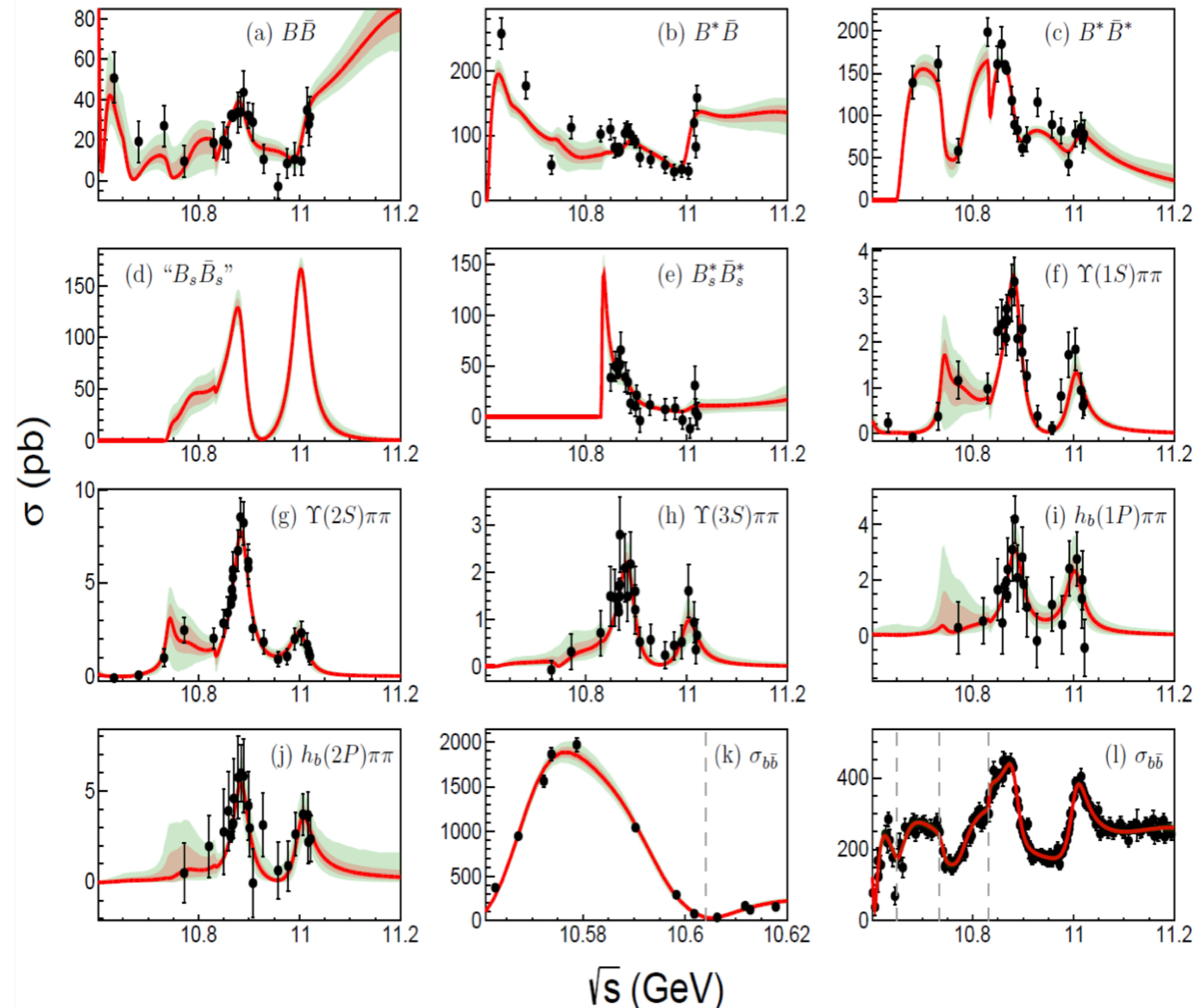
Record-breaking instantaneous luminosity:

$$4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$



Coupled channel analysis

Hüsken, Mitchell, Swanson, PRD 106, 094013 (2022)



All available scan data

K-matrix: scattering via $\Upsilon(4S)$, $\Upsilon(10753)$, $\Upsilon(5S)$, $\Upsilon(6S)$ or non-resonantly.

Results: pole positions, branching fraction, energy dependence of scattering amplitudes.

Accuracy above $\Upsilon(6S)$ and near $\Upsilon(10753)$ is poor.

Energy dependence of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

Decay modes used:

$B^+ \rightarrow$	$B^0 \rightarrow$
$\bar{D}^0\pi^+$	$D^-\pi^+$
$\bar{D}^0\pi^+\pi^+\pi^-$	$D^-\pi^+\pi^+\pi^-$
$\bar{D}^{*0}\pi^+$	$D^{*-}\pi^+$
$\bar{D}^{*0}\pi^+\pi^+\pi^-$	$D^{*-}\pi^+\pi^+\pi^-$
$D_s^+\bar{D}^0$	$D_s^+D^-$
$D_s^{*+}\bar{D}^0$	$D_s^{*+}D^-$
$D_s^+\bar{D}^{*0}$	$D_s^+D^{*-}$
$D_s^{*+}\bar{D}^{*0}$	$D_s^{*+}D^{*-}$
$J/\psi K^+$	$J/\psi K_S$
$J/\psi K_S\pi^+$	$J/\psi K^+\pi^-$
$J/\psi K^+\pi^+\pi^-$	
$D^-\pi^+\pi^+$	$D^{*-}K^+K^-\pi^+$
$D^{*-}\pi^+\pi^+$	

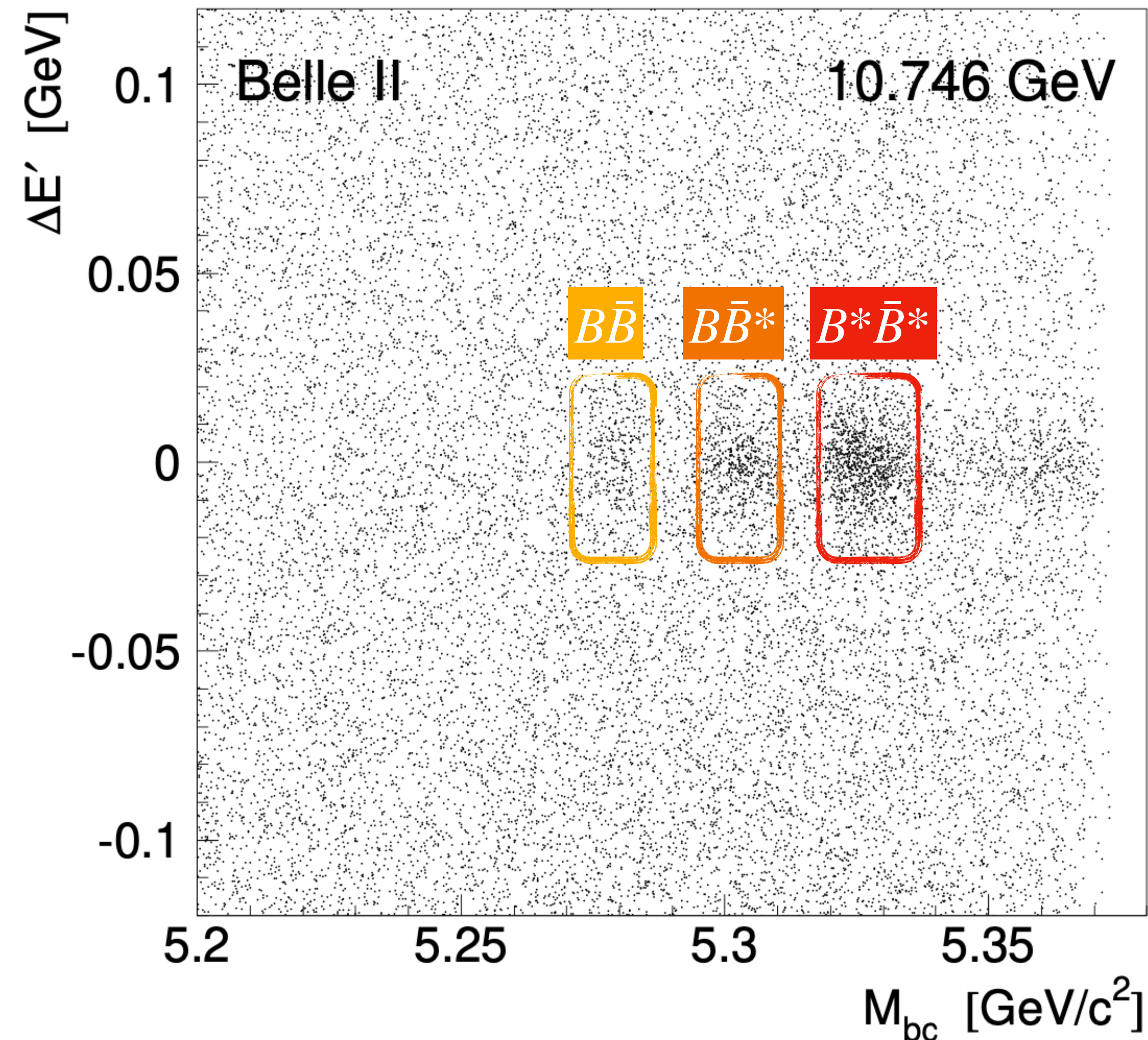
$D^0 \rightarrow$	$D^+ \rightarrow$	$D_s^+ \rightarrow$
$K^-\pi^+$	$K^-\pi^+\pi^+$	$K^+K^-\pi^+$
$K^-\pi^+\pi^0$	$K^-\pi^+\pi^+\pi^0$	K^+K_S
$K^-\pi^+\pi^+\pi^-$	$K_S\pi^+$	$K^+K^-\pi^+\pi^0$
$K_S\pi^+\pi^-$	$K_S\pi^+\pi^0$	$K^+K_S\pi^+\pi^-$
$K_S\pi^+\pi^-\pi^0$	$K_S\pi^+\pi^+\pi^-$	$K^+K_S\pi^+\pi^+$
K^+K^-	$K^+K^-\pi^+$	$K^+K^-\pi^+\pi^+\pi^-$
$K^+K^-K_S$		$K^+\pi^+\pi^-$
		$\pi^+\pi^+\pi^-$

Energy dependence of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

► Method:

- ◆ Reconstruct one B in full hadronic channels.
- ◆ Key variables for analysis are
 - ◆ $M_{bc} = \sqrt{(E_{cm}/2)^2 - p_B^2}$
 - ◆ $\Delta E' = \Delta E - M_{bc} + M_B$, where $\Delta E = E_B - E_{cm}/2$
- ◆ $\Delta E'$ has improved resolution and allows all desired two-body decays to be selected with a common cut
- ◆ Populations of each can be studied by fitting the projections onto the M_{bc} axis for all energies at which data were accumulated
- ◆ $B^* \rightarrow B\gamma$ decays are not reconstructed.

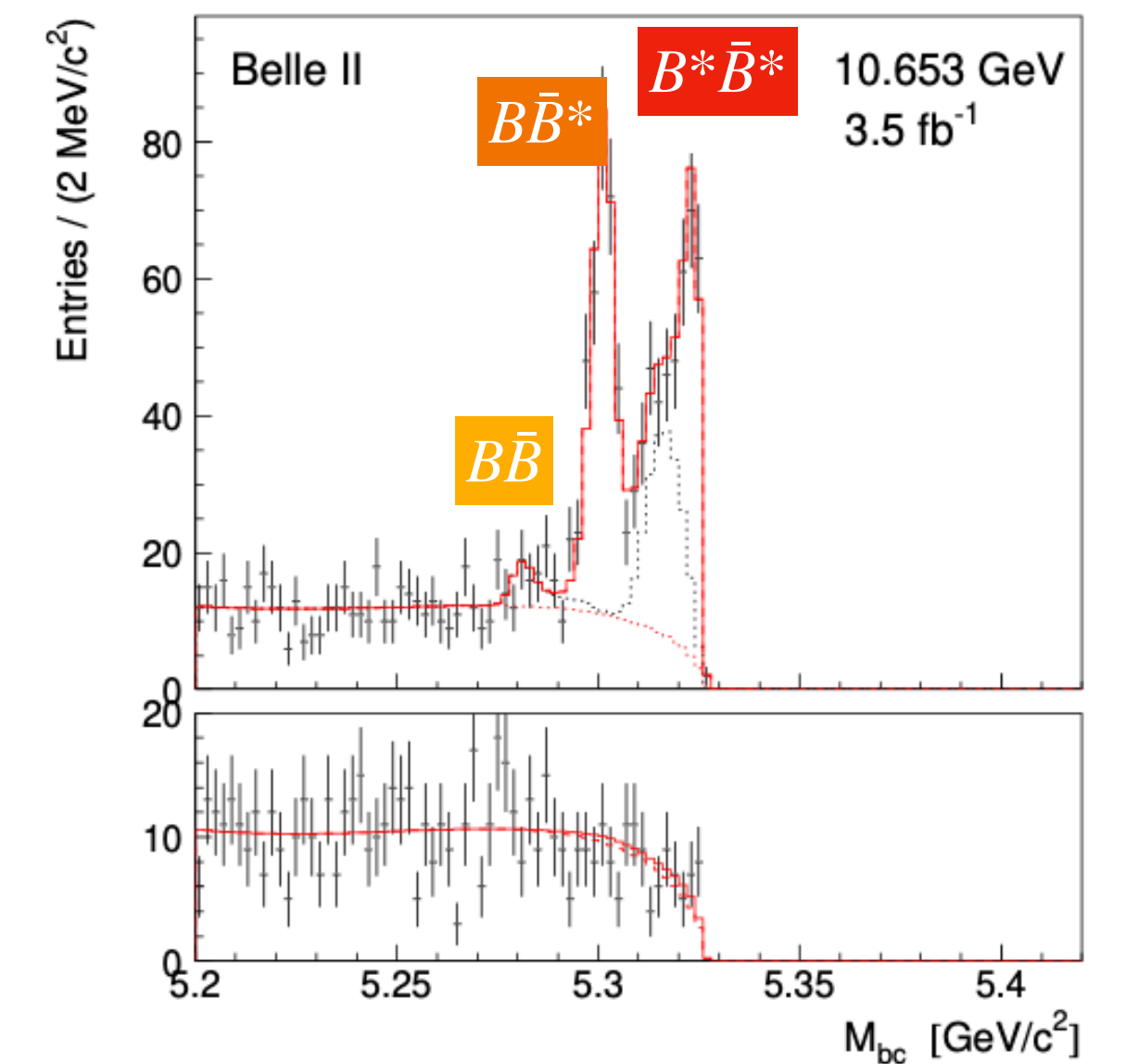
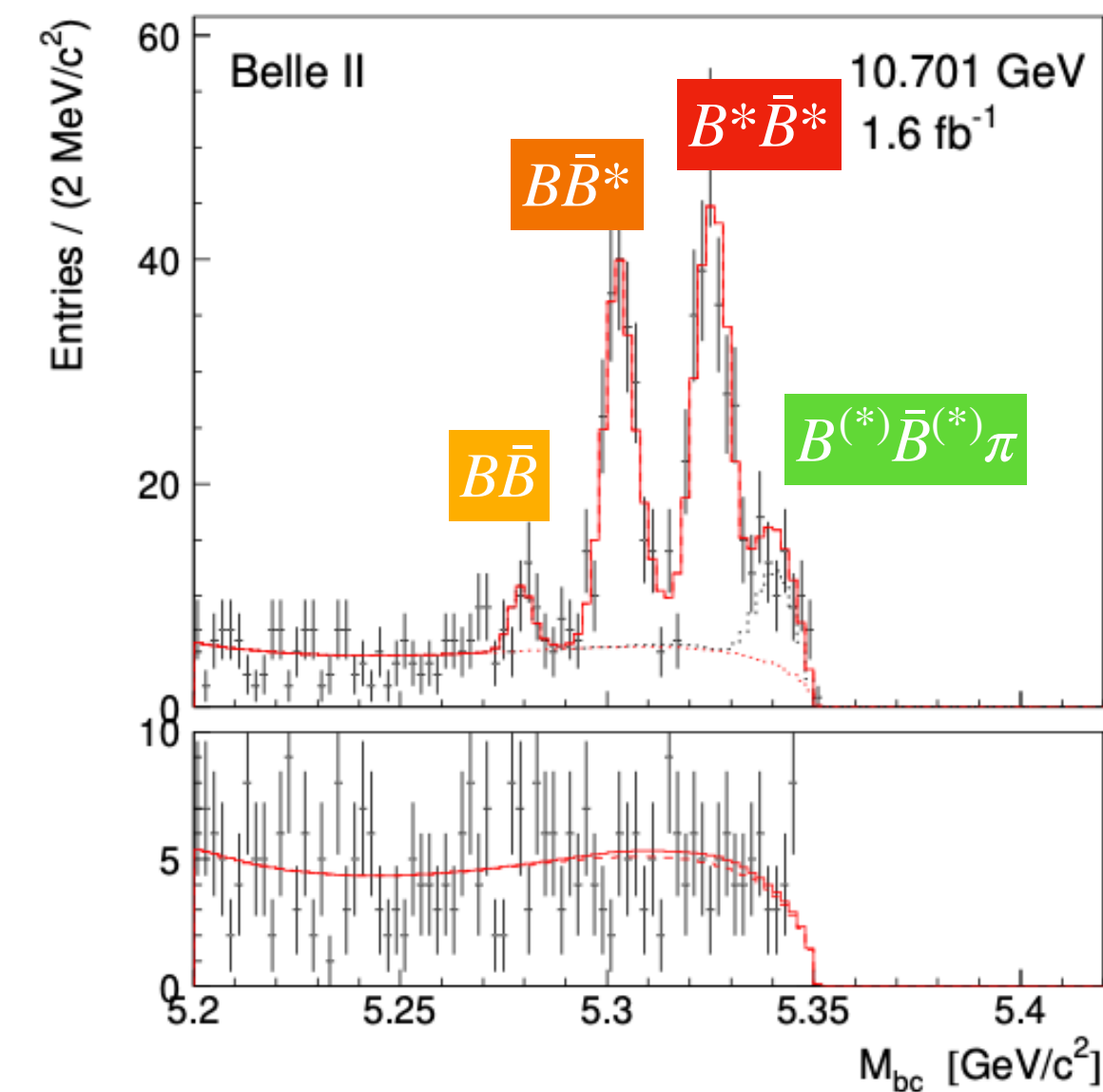
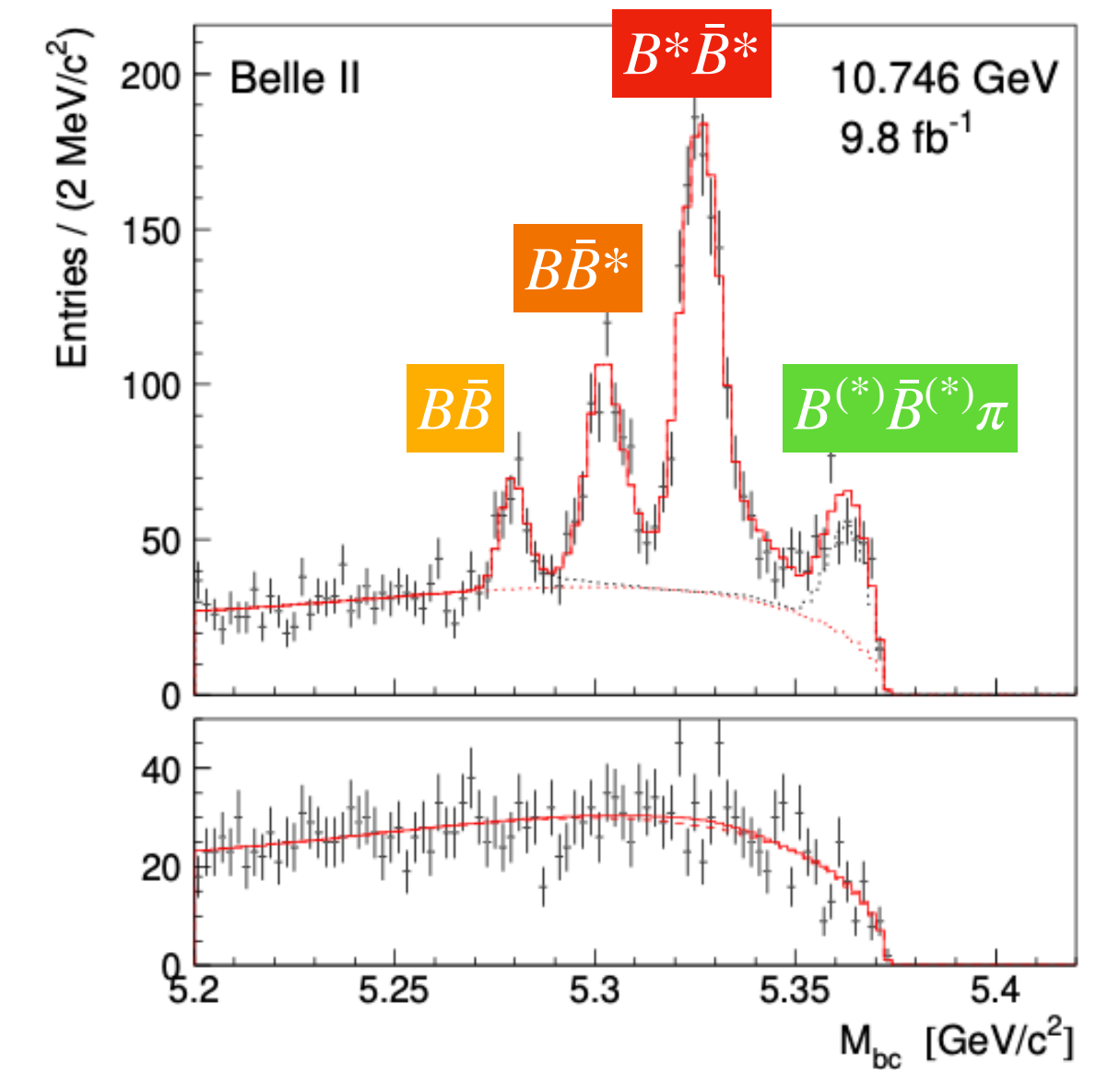
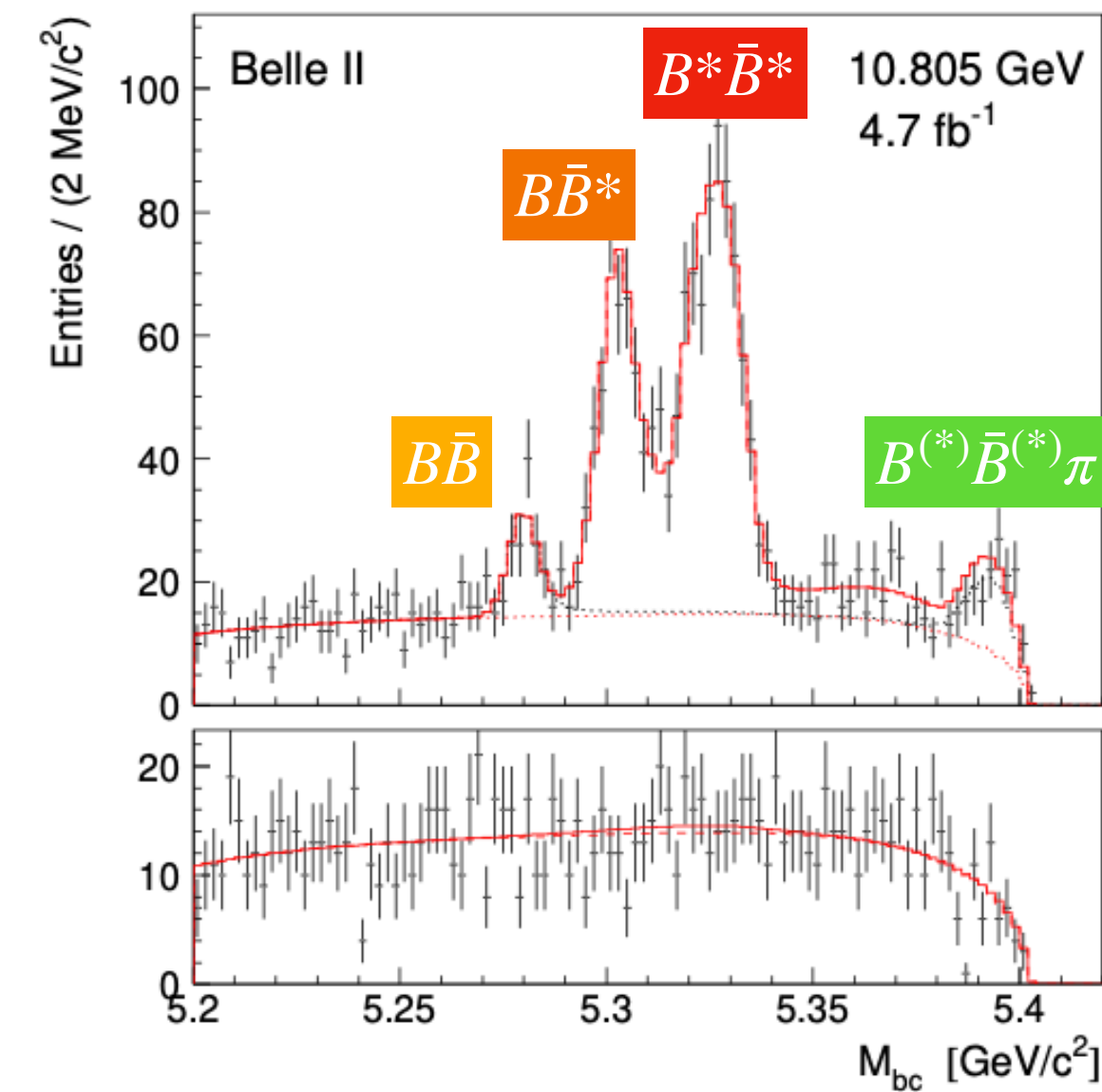
$\Delta E'$ vs M_{bc} at $E_{cm} = 10.746$ GeV



Energy dependence of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

M_{bc} fit at scan energies

- ▶ M_{bc} fit distribution:
- ▶ $\Delta E'$ signal region (upper)
- ▶ $\Delta E'$ side-bands (lower)
- ▶ $e^+e^- \rightarrow B\bar{B}, B\bar{B}^*, B^*\bar{B}^*$ signals at $\sqrt{s} \sim 10.75$ GeV can be clearly observed
- ▶ Contribution of $\Upsilon(4S) \rightarrow B\bar{B}$ production via ISR is visible well (black dotted histograms)
- ▶ At $\sqrt{s} = 10.653$ GeV, the sharp cut of the data at right edge is due to threshold effect



Bottomonium (-like) at Belle II

► Four ways to access bottomonia:

◆ **Direct production** from e^+e^- : $J^{PC} = 1^{--}$: $\Upsilon(nS)$

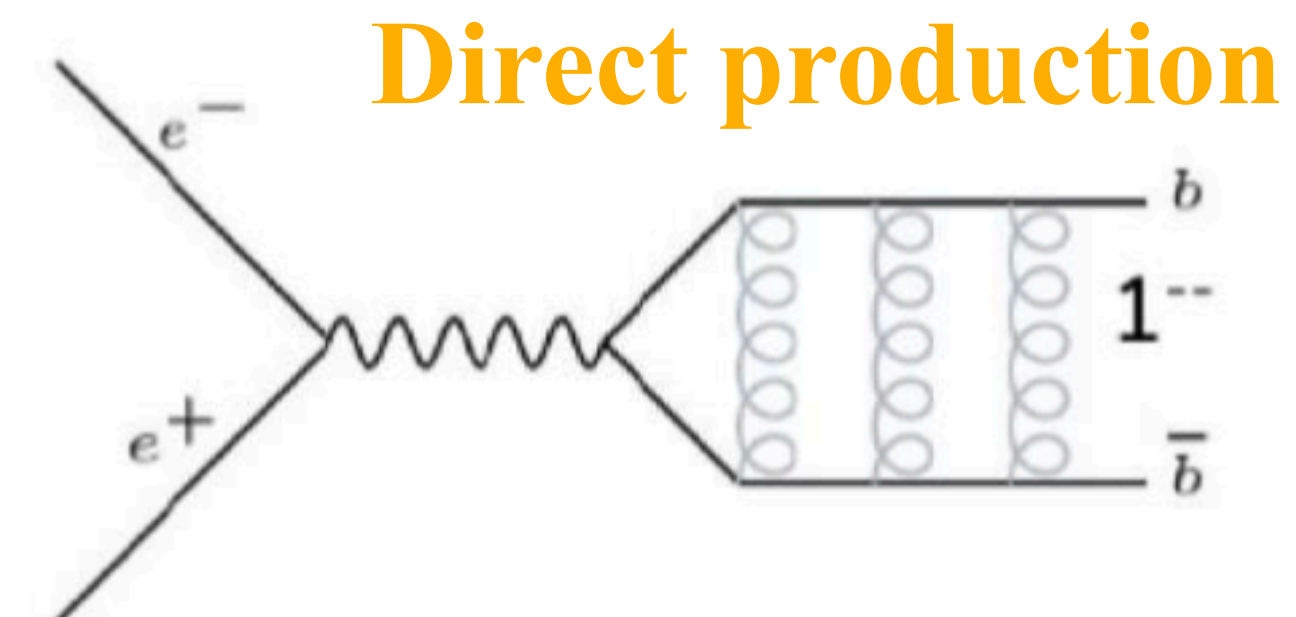
◆ **ISR production**: $J^{PC} = 1^{--}$: $\Upsilon(nS)$

◆ **Hadronic transitions** from $\Upsilon(nS)$ through $\eta, \pi\pi, \dots$

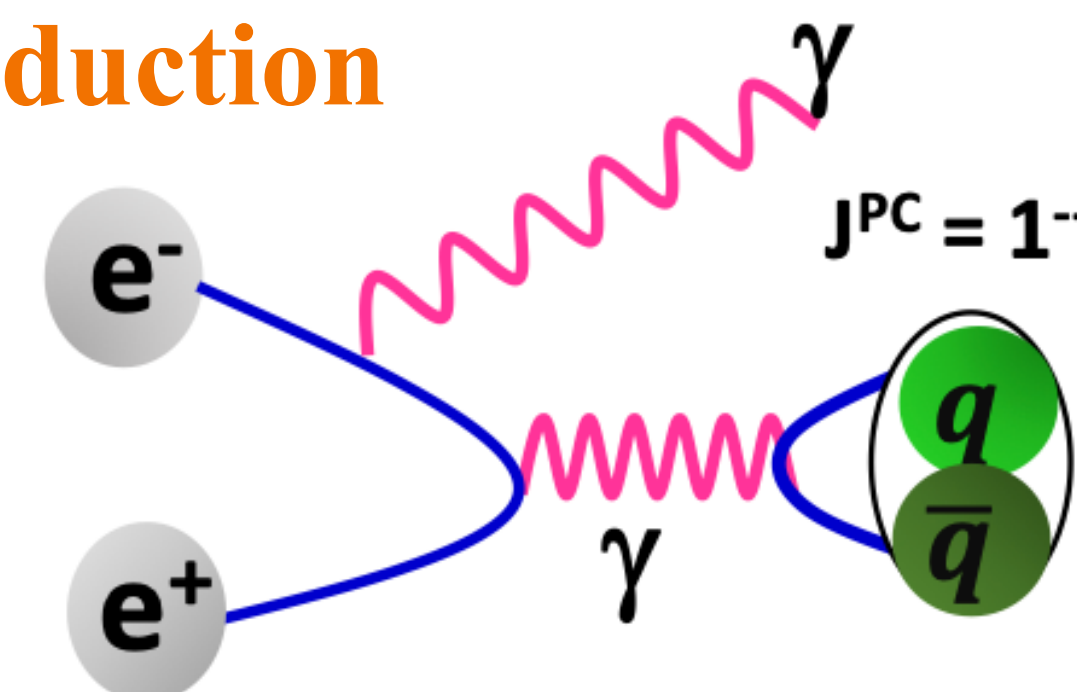
$$J^{PC} = 0^{-+}, 1^{--}, 1^{+-} \dots : \Upsilon(nS), \eta_b(nS), h_b(nS), \dots$$

◆ **Radiative transitions** from $\Upsilon(nS)$

$$J^{PC} = 0^{-+}, 0^{++}, 1^{++}, 2^{++} : \eta_b(nS), \chi_b(nP)$$



ISR production



Hadronic transitions

