

# Tau physics at Belle and Belle II



European Research Council  
Established by the European Commission



# Outline

- **Belle / Belle II Experiments**
- **Tau physics**
  - Program and Motivation
  - Why at Belle / Belle II ?
  - How to reconstruct tau at Belle / Belle II
- **Standard Model measurements**
- **Lepton Flavor Universality (LFU)**
- **Lepton Flavor Violation (LFV)**
- **Summary and Outlook**

# Belle and Belle II

- General purpose detector with almost  $4\pi$  coverage
- Located at SuperKEKB  
→ asymmetric  $e^+e^-$  collider in Tsukuba Japan

## Belle

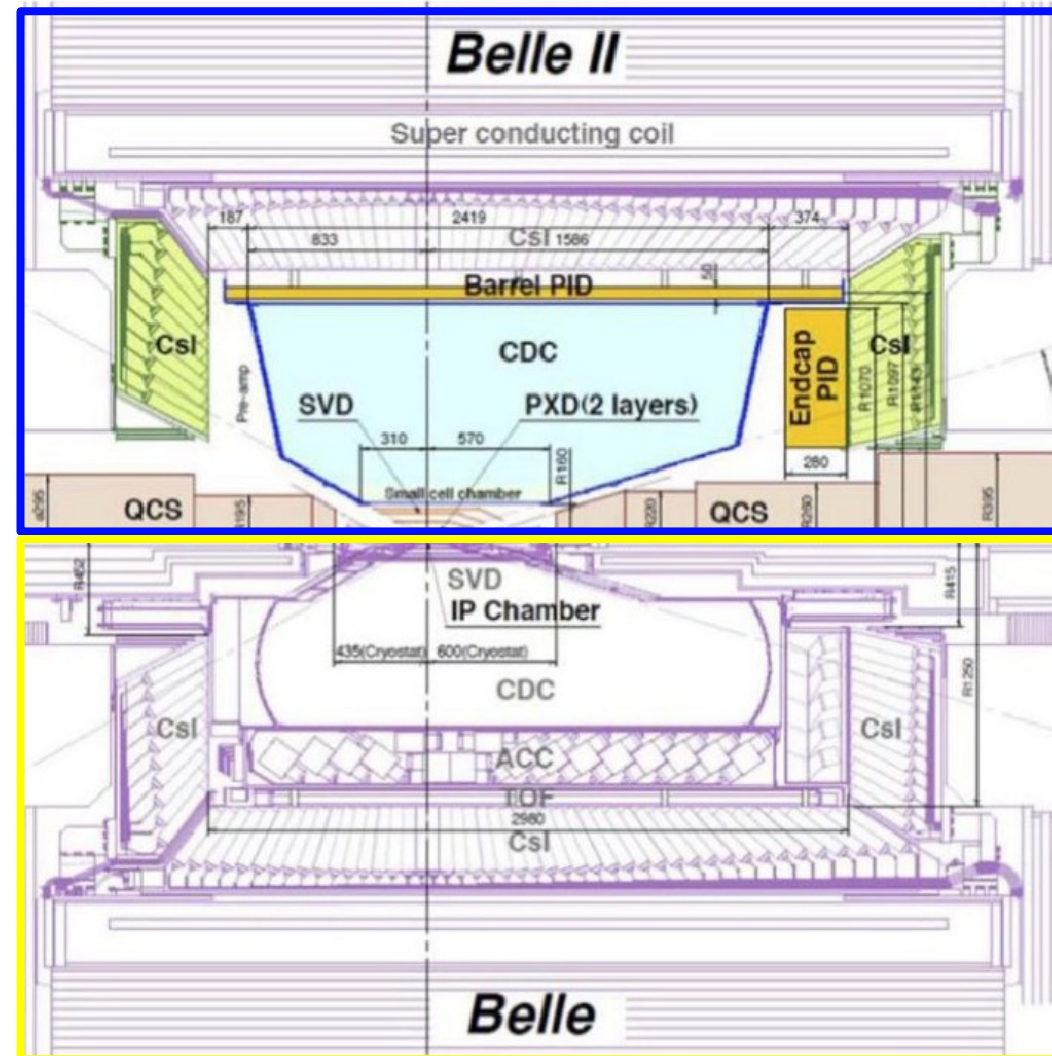
- 1999 – 2010
- 8 GeV electron and 3.5 GeV positron beams
- 980/fb collected

## Belle II (predecessor of Belle)

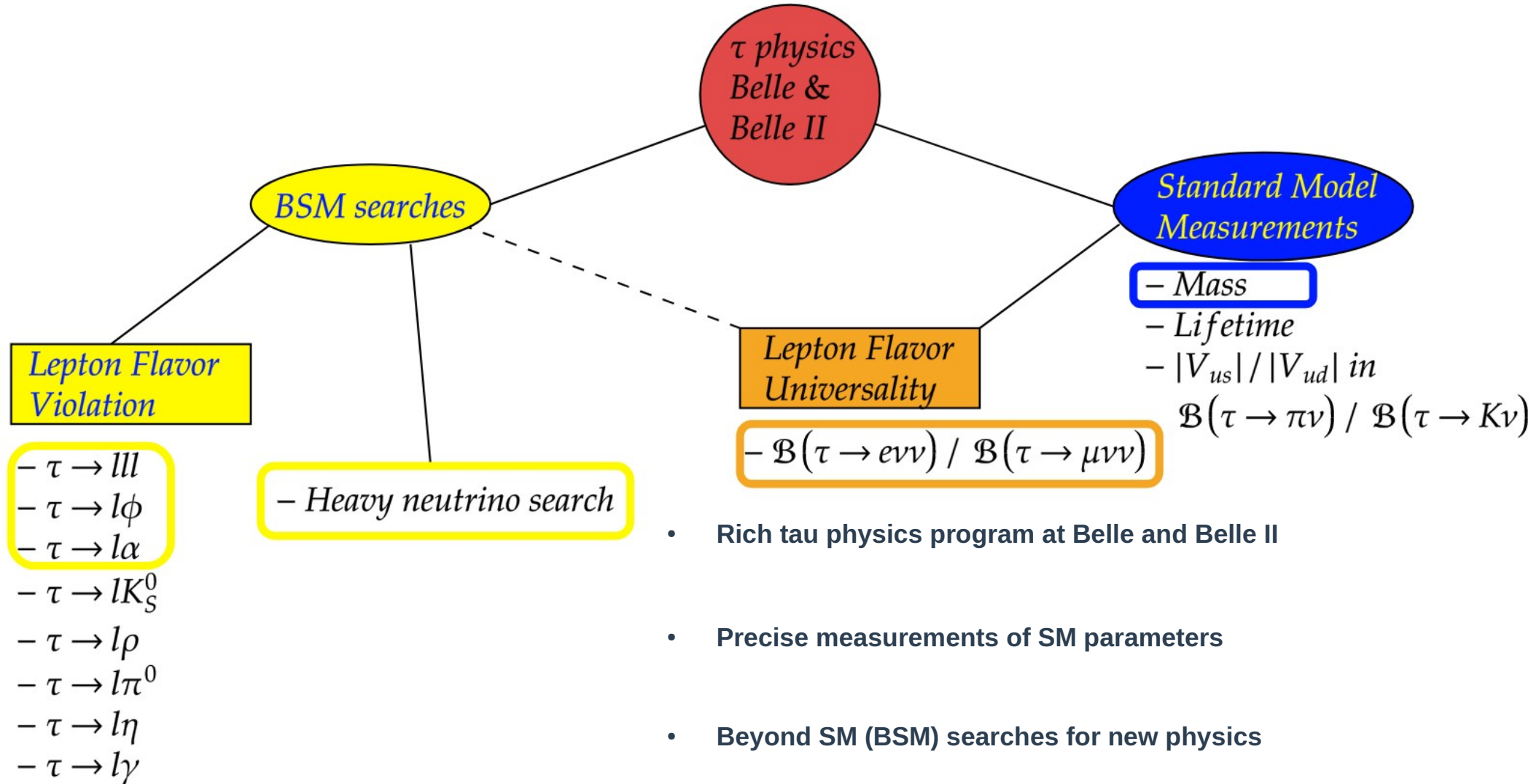
- 2018 - ??
- 7 GeV electron and 4 GeV positron beams
  - Smaller boost → new vertex detector using 2 layers of pixels and 4 layers of strips
- 424/fb up to now → goal : 50/ab

## Detection

- Good efficiency for neutral particles
- Missing energy reconstruction
- Specific low-multiplicity event triggers at Belle II

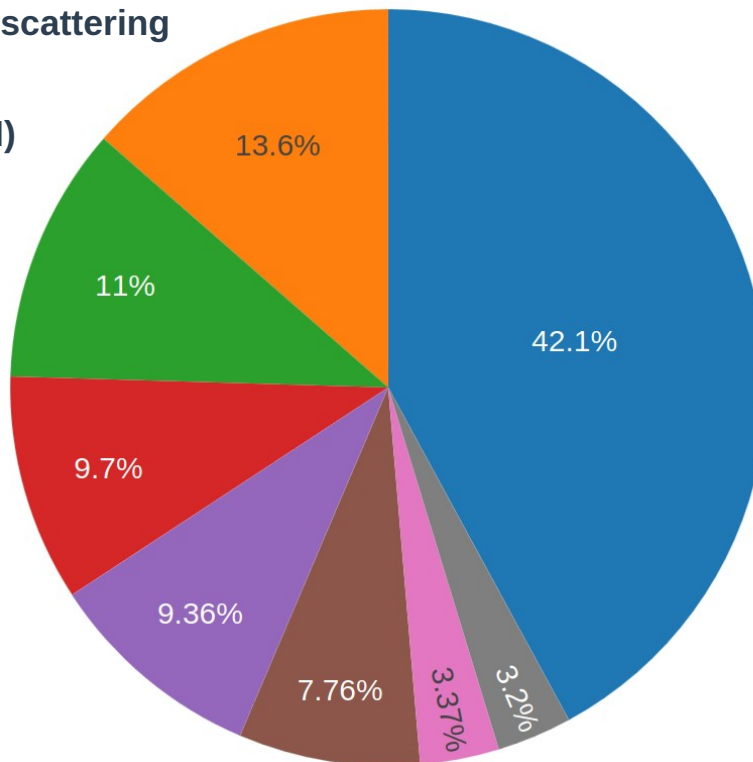


# Tau physics : Program and Motivation

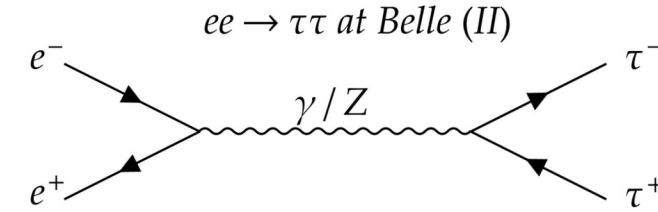
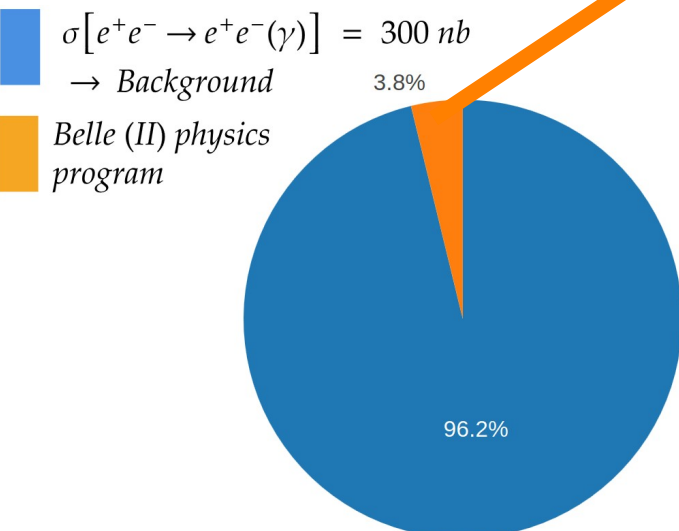


# Tau physics : Why at Belle (II) ?

- 96.2 % of ee collisions do Bhabha scattering  
→ Background
- Remaining 3.8 % compose Belle (II) physics program
  - 9.7 %  $Y(4S) \rightarrow BB$
  - 7.76 % taupair production  
→ 45 billion taupairs @ Belle II
    - High precision studies
    - Rare decay searches



- $\sigma[e^+e^- \rightarrow \gamma\gamma(\gamma)] = 4.99 \text{ nb}$
- $\sigma[e^+e^- \rightarrow uu] = 1.61 \text{ nb}$
- $\sigma[e^+e^- \rightarrow cc] = 1.3 \text{ nb}$
- $\sigma[e^+e^- \rightarrow \mu\mu] = 1.15 \text{ nb}$
- $\sigma[e^+e^- \rightarrow Y(4S)] = 1.11 \text{ nb}$
- $\sigma[e^+e^- \rightarrow \tau\tau] = 0.9 \text{ nb}$
- $\sigma[e^+e^- \rightarrow dd] = 0.4 \text{ nb}$
- $\sigma[e^+e^- \rightarrow ss] = 0.38 \text{ nb}$



- Clean physics environment, known initial state
- Missing energy reconstruction
- Dedicated low multiplicity triggers (not present in Belle)

# Tau physics : How to reconstruct $\tau$ at Belle (II)

- SM  $\tau$  decays are not fully reconstructable due to missing neutrino
- Identify  $\tau^+\tau^-$  events using thrust axis

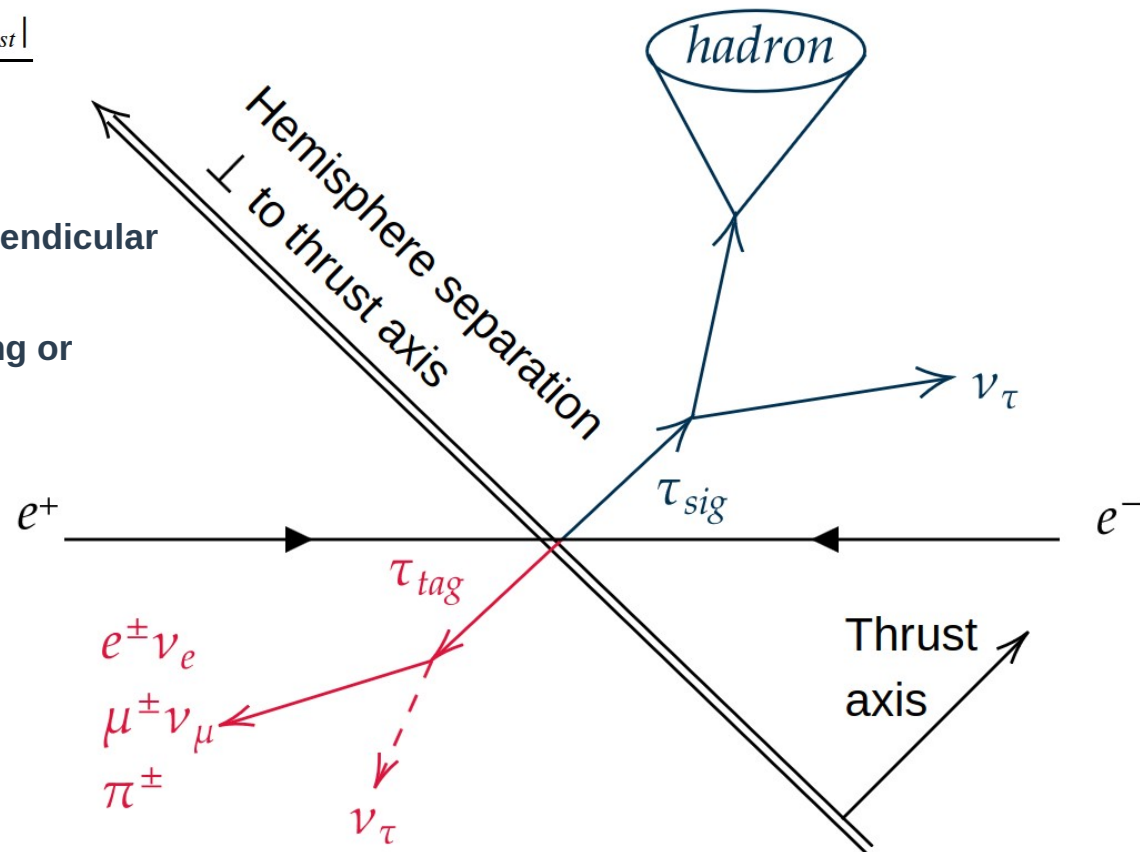
- Maximizes projection of all particle momenta in event

Find  $\vec{n}_{thrust}$  which maximizes 
$$\frac{\sum_i |\vec{p}_i^{CM} \cdot \vec{n}_{thrust}|}{\sum_i |\vec{p}_i^{CM}|}$$

- Define two hemispheres divided by the plane perpendicular to the thrust axis

- Reconstruct tag-side tau in standard model 1-prong or 3-prong decay

- Exclusive  $\rightarrow$  use only 1-prong OR 3-prong events
  - High purity, less efficiency
- Inclusive  $\rightarrow$  do not reconstruct tag-side tau in a specific mode
  - Higher signal efficiency
  - Higher background levels





# SM Measurements : Motivation

- Precision measurement of tau quantities can have significant impact

- First row unitarity of CKM-Matrix (Cabbibo-angle-anomaly)
- $B(\tau \rightarrow K\nu) / B(\tau \rightarrow \pi\nu) \sim |V_{us}| / |V_{ud}|^2$
- Combination with lattice-QCD information gives rise to additional constraints
- Mass of tau is the one with worst precision among leptons

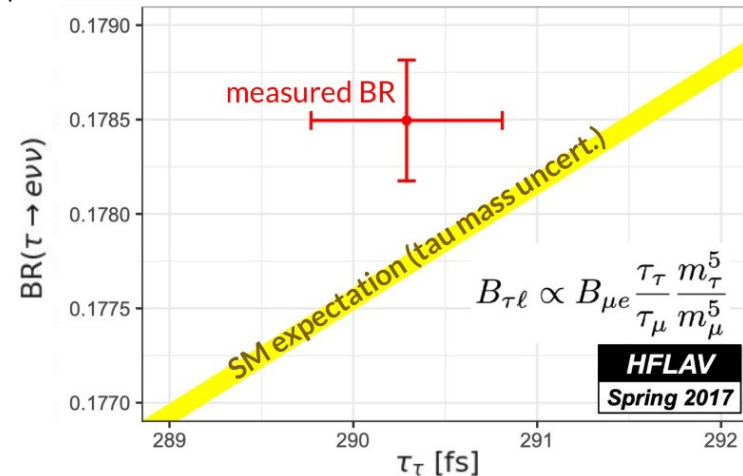
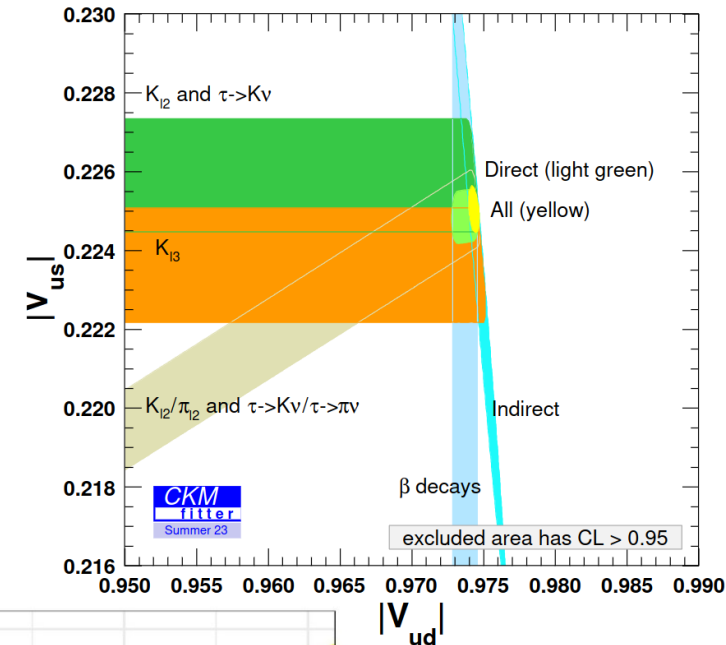
$$m_e = (0.51099895000 \pm 0.00000000015) \text{ MeV}$$

$$m_\mu = (105.6583755 \pm 0.0000023) \text{ MeV}$$

$$m_\tau = (1776.86 \pm 0.12) \text{ MeV}$$

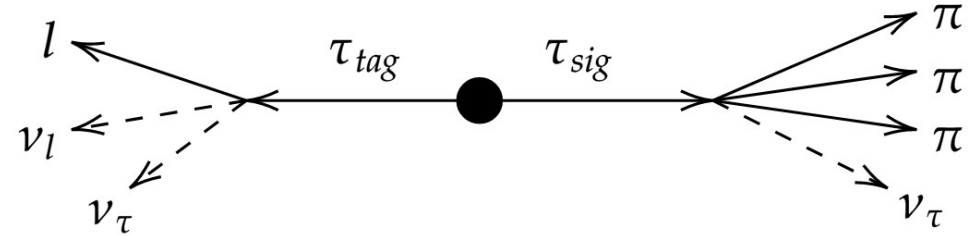
- Lepton Flavor Universality and dipole moments

- All leptons are expected to have same coupling strength to W-Boson in SM
  - Different observations would suggest NP contributions
- Mass and lifetime of  $\tau$  are important inputs to those calculations

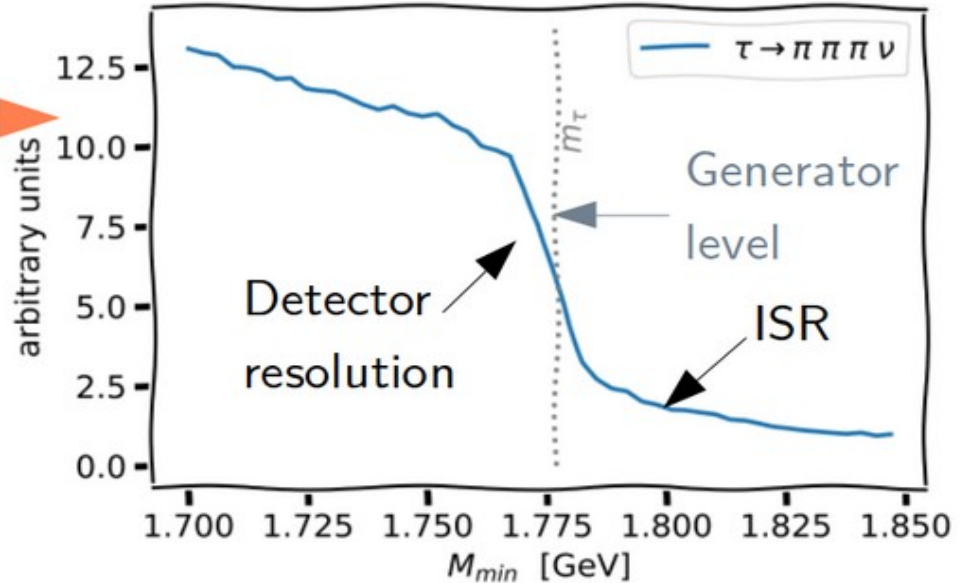
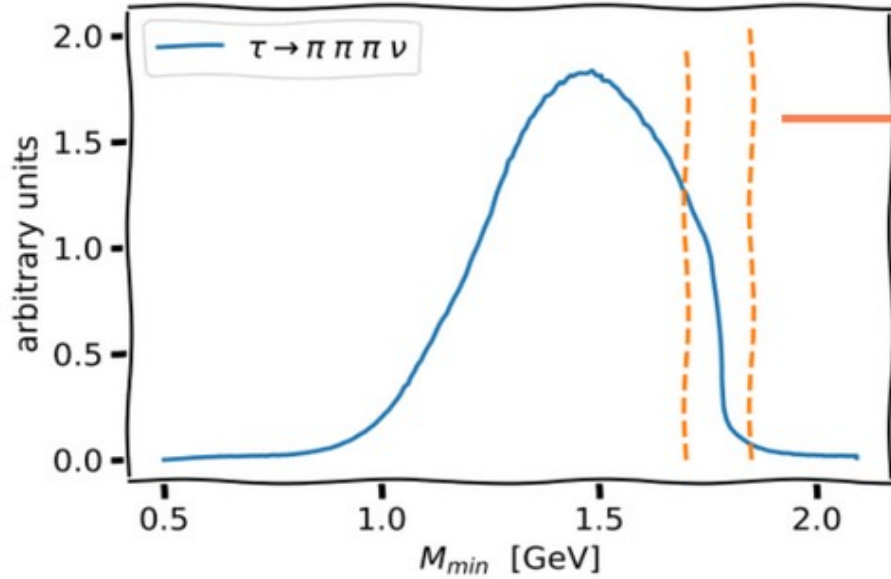


# SM Measurements : $\tau$ Mass – I

- The  $\tau$  mass is a fundamental parameter of the SM
- A precise measurement is an important input to LFU tests
- Belle II uses the Pseudomass method
  - Fit kinematic edge of  $M_{\min}$  distribution in  $\tau \rightarrow 3\pi\nu$  decays with empirical function
  - Smeared edge due to ISR/FSR and detector resolution



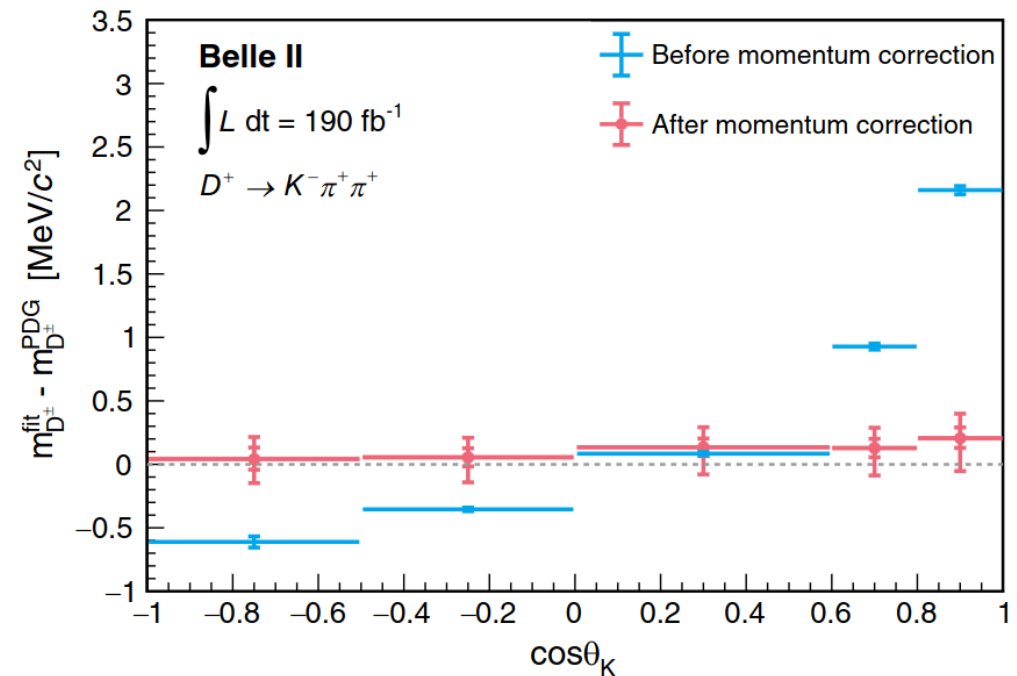
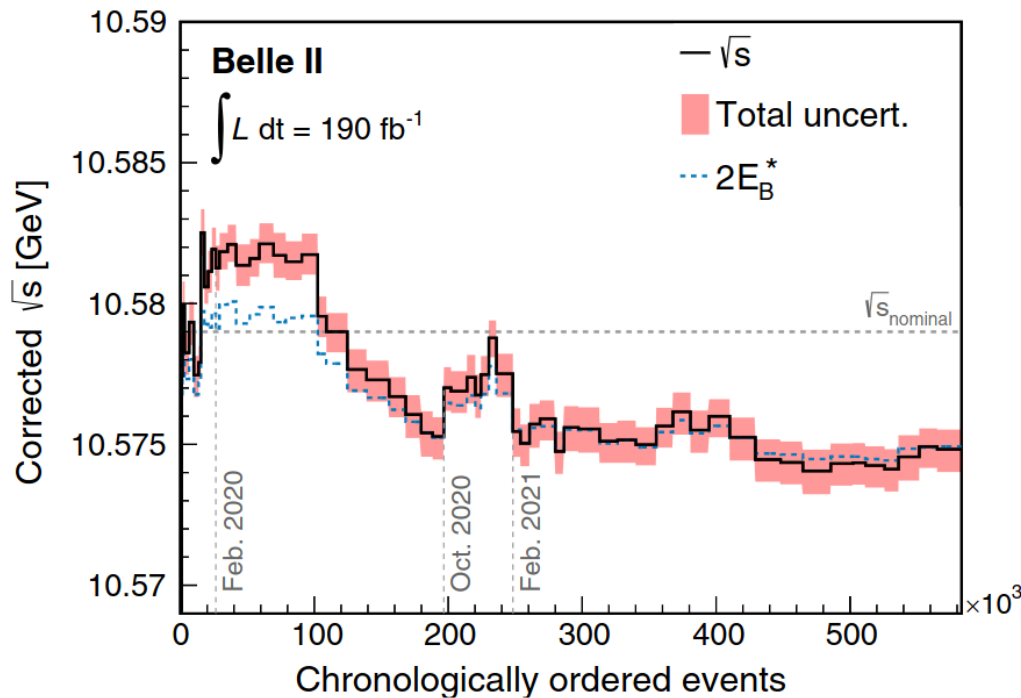
$$M_{\min} = \sqrt{m_{3\pi}^2 + 2(\sqrt{s}/2 - E_{3\pi})(E_{3\pi} - |\vec{p}_{3\pi}|)} \leq m_{\tau}$$





# SM Measurements : $\tau$ Mass – II

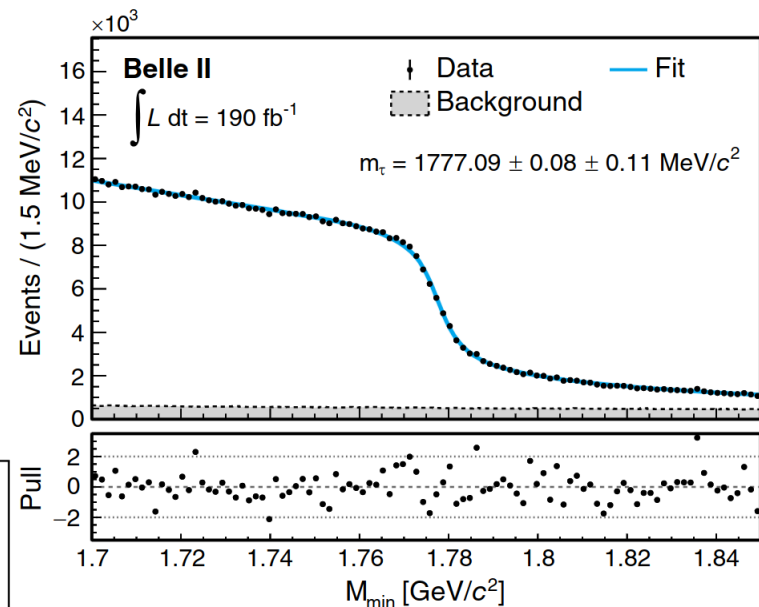
- Beam energy calibration and momentum correction are crucial for this measurement
  - $E_{\text{beam}}$  corrected by hadronic B-Meson decays
  - Momentum correction is done with scale factors for  $\pi$  using  $D^{*+} \rightarrow D^0(\rightarrow K^-\pi^+)\pi^+$ 
    - Originates from imperfect B-field, mismodeling in simulation  $\rightarrow$  bias in mass extraction



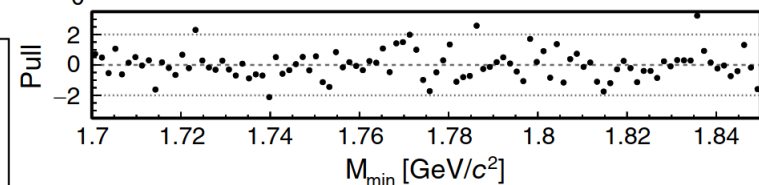
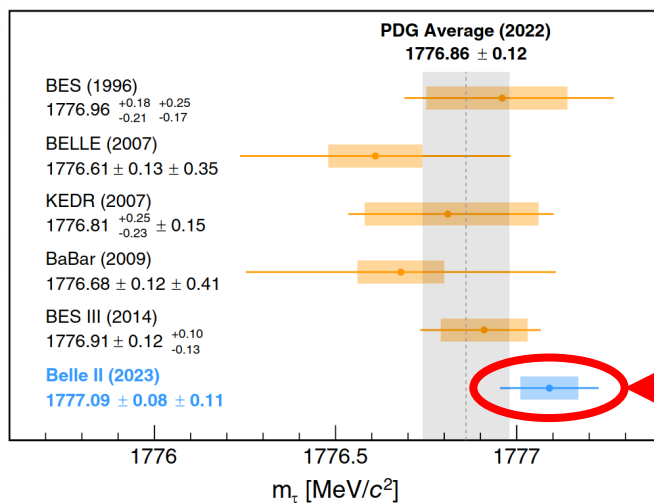
# SM Measurements : $\tau$ Mass – III

- Perform unbinned maximum likelihood fit to the kinematic edge of the mass distribution

$$M_\tau = 1777.09 \pm 0.08 \pm 0.11 \text{ MeV}/c^2$$



$\int \mathcal{L} dt = 190 \text{ fb}^{-1}$   
 $\sim 175 \text{ Million } ee \rightarrow \tau\tau$



World's most precise measurement

Source	Uncertainty (MeV/c <sup>2</sup> )
Knowledge of the colliding beams:	
Beam-energy correction	0.07
Boost vector	< 0.01
Reconstruction of charged particles:	
Charged-particle momentum correction	0.06
Detector misalignment	0.03
Fit model:	
Estimator bias	0.03
Choice of the fit function	0.02
Mass dependence of the bias	< 0.01
Imperfections of the simulation:	
Detector material density	0.03
Modeling of ISR, FSR and $\tau$ decay	0.02
Neutral particle reconstruction efficiency	$\leq 0.01$
Momentum resolution	< 0.01
Tracking efficiency correction	< 0.01
Trigger efficiency	< 0.01
Background processes	< 0.01
Total	0.11

# SM Measurements : LFU – I (NEW)

- SM picture of leptons

- 3 families with different masses and different, separately conserved lepton numbers
- Coupling to W boson is flavor-independent (?)  $\rightarrow g_e = g_\mu = g_\tau$ 
  - lepton universality

- Test LFU (e- $\mu$ ) in tau decays with  $g_e, g_\mu$  being proportional to the leptonic branching fractions

$$\left( \frac{g_\mu}{g_e} \right)_\tau^2 \propto \frac{\mathbf{BR}(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{\mathbf{BR}(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)}$$

$$\int \mathcal{L} dt = 362 \text{ fb}^{-1}$$

$$\sim 334 \text{ Million } ee \rightarrow \tau\tau$$

- LFU is sensitive to new physics if it violates lepton flavor and/or lepton universality in weak charged-currents

- Belle II analysis uses 1-prong decays with one charged hadron and at least one neutral pion on the tag-side

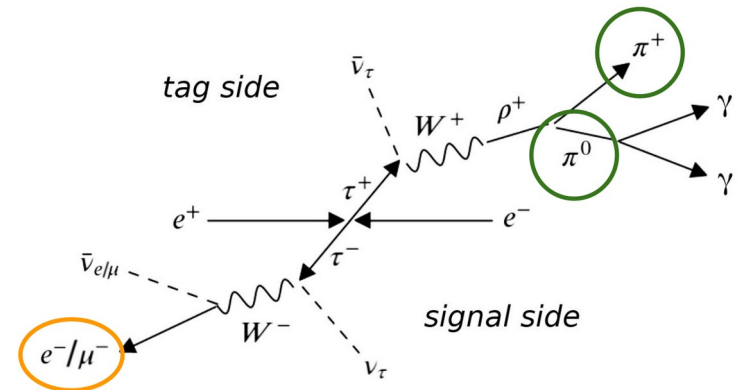
- Large BF  $\sim 35\%$  on tag-side, low backgrounds, high trigger efficiency

- Signal side:

- One particle track with lepton ID requirement

- Tag side:

- One track with  $E_{\text{cluster}} / p < 0.8$
- At least one neutral pion on tag side

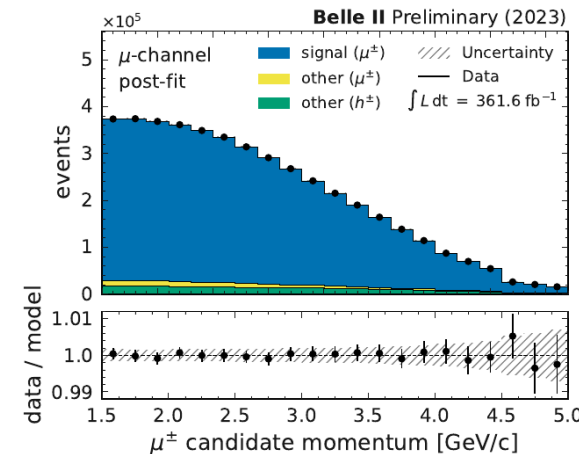
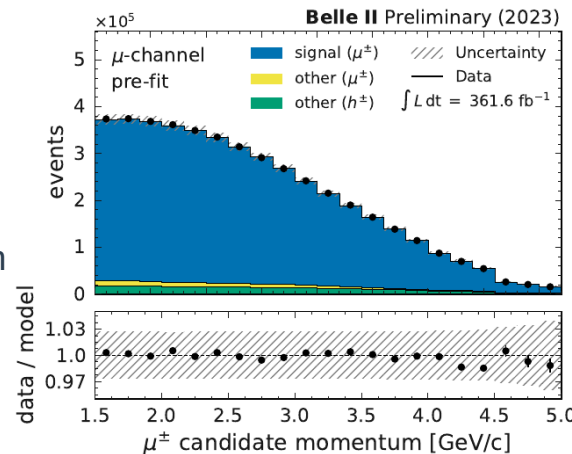
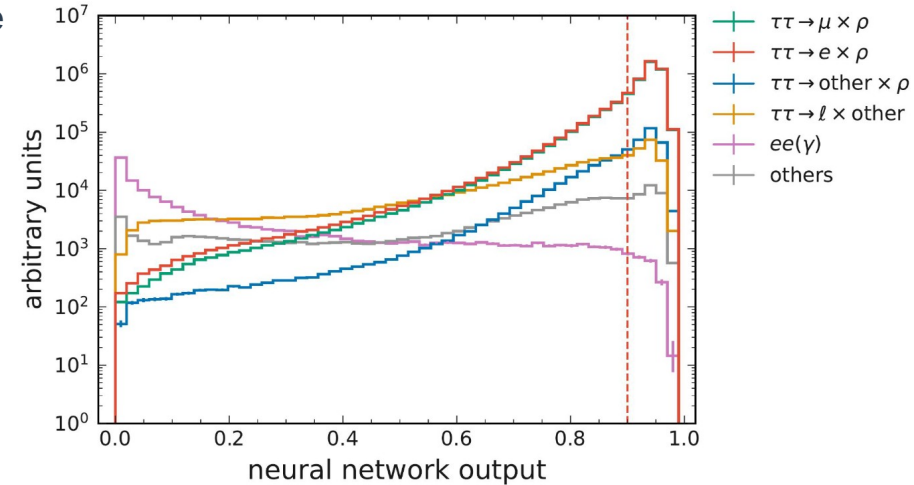


# SM Measurements : LFU – II (NEW)

- Event selection is performed with rectangular cuts + neural network
- 94 % purity with 9.6 % signal efficiency for the combined sample
- Main backgrounds:
  - $ee \rightarrow \tau\tau$  ( $\pi$  faking  $e/\mu$ )  $\sim 3.3$  %
  - $ee \rightarrow \tau\tau$  (wrong tag)  $\sim 2.3$  %
  - $ee \rightarrow ee\tau\tau \sim 0.2\%$
- Extraction of  $R_\mu$

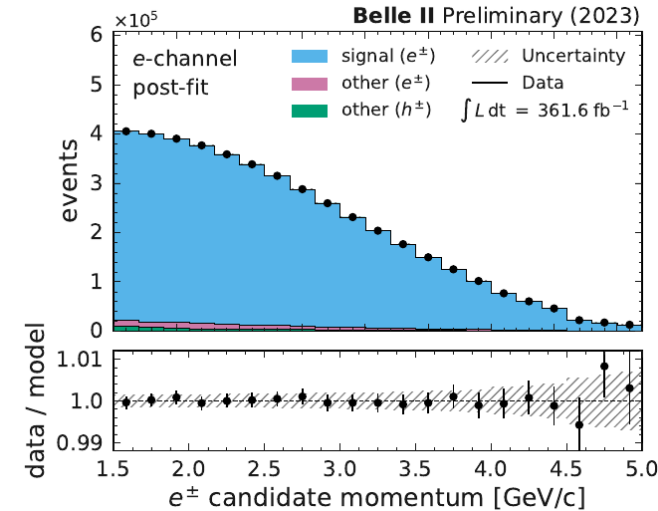
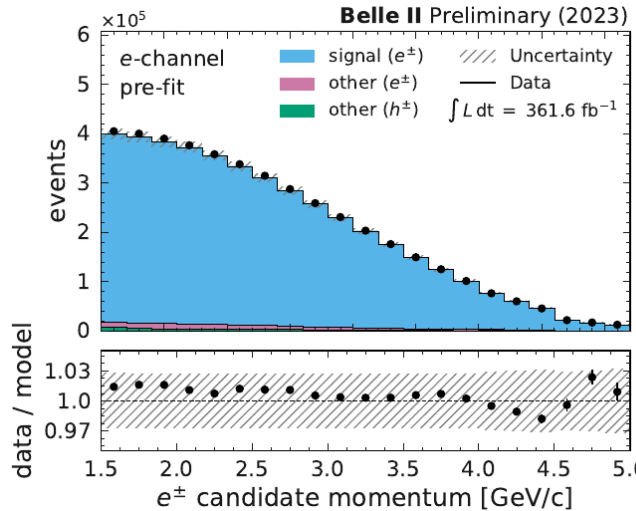
- Binned maximum likelihood template fit with pyhf in lepton momentum [1.5, 5] GeV
- Systematics included with nuisance parameters modifying the templates
- 3 templates for electron and muon channel
  - Signal decays
  - Background with correct signal side lepton
  - Background with misidentified particle on signal side

Belle II Preliminary (2023)



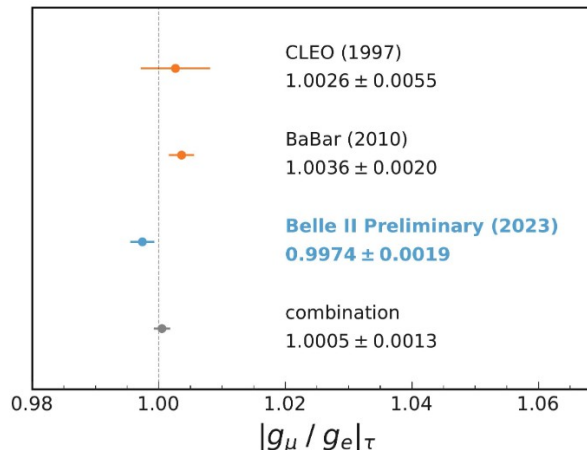
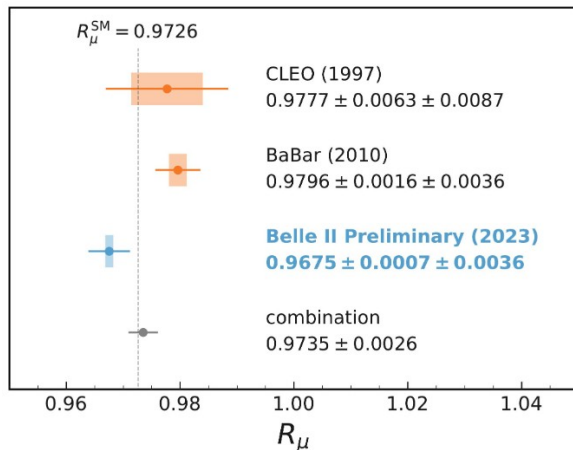
# SM Measurements : LFU – III (NEW)

- Leading systematics
  - Particle identification 0.32%
  - Trigger 0.10%
- Measured  $R = 0.9675 \pm 0.0007 \pm 0.0036$ 
  - Most precise e-mu universality from tau decays in single measurement



$$R_\mu = \frac{\mathcal{B}(\tau^- \rightarrow \nu_\tau \mu^- \bar{\nu}_\mu(\gamma))}{\mathcal{B}(\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e(\gamma))}$$

$$\left(\frac{g_\mu}{g_e}\right)_\tau = \sqrt{R_\mu \frac{f(m_e^2/m_\tau^2)}{f(m_\mu^2/m_\tau^2)}}$$



# BSM : Heavy neutrino search – I

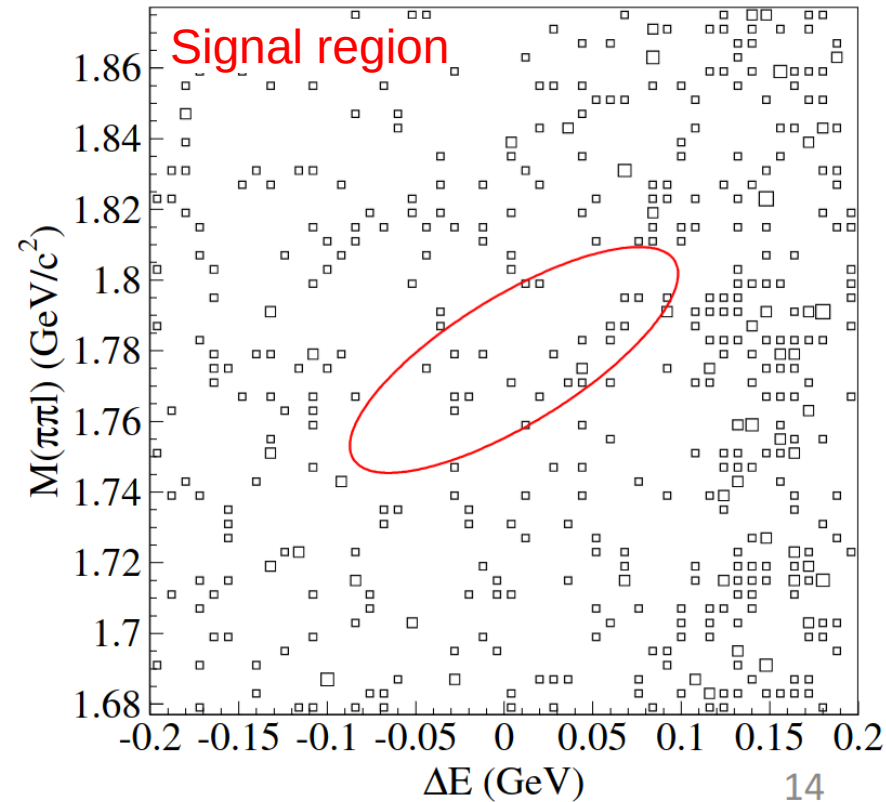
- Neutrino mass is not zero, which needs a mechanism to generate it
  - Including heavy, right-handed neutrinos is an approach to introduce neutrino mass

$$\int \mathcal{L} dt = 980 \text{ fb}^{-1}$$

$$\sim 905 \text{ Million } ee \rightarrow \tau\tau$$

- $\tau^\pm \rightarrow \pi^\pm \nu_h$  **with**  $\nu_h \rightarrow \pi^\pm l^\mp$ 
  - $\nu_h$  long-lived Majorana neutrino,  $l = e/\mu$

Data in M- $\Delta E$  plane

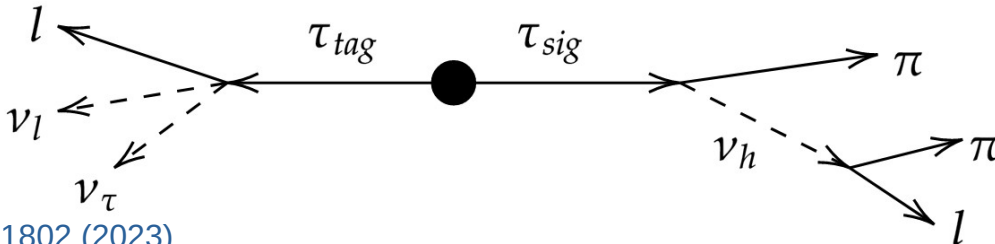


- Signal-side : require two pions and a lepton with common vertex
- Tag-side : 1 or 3-prong tau decay
- Backgrounds originate from  $ee \rightarrow qq, \tau\tau, ll, eell$

- Suppress them with M and  $\Delta E$  cuts

$$\Delta E = (E_{\pi\pi l}^{CM} - \sqrt{s}/2)$$

- Search for signal-like narrow peak





# BSM : Heavy neutrino search – II

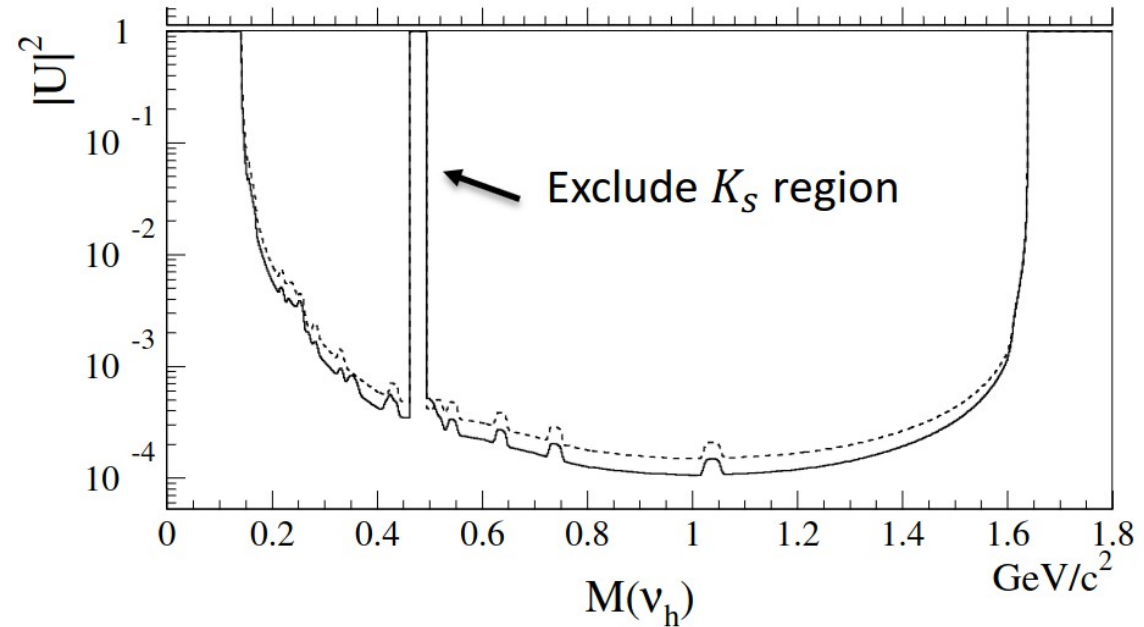
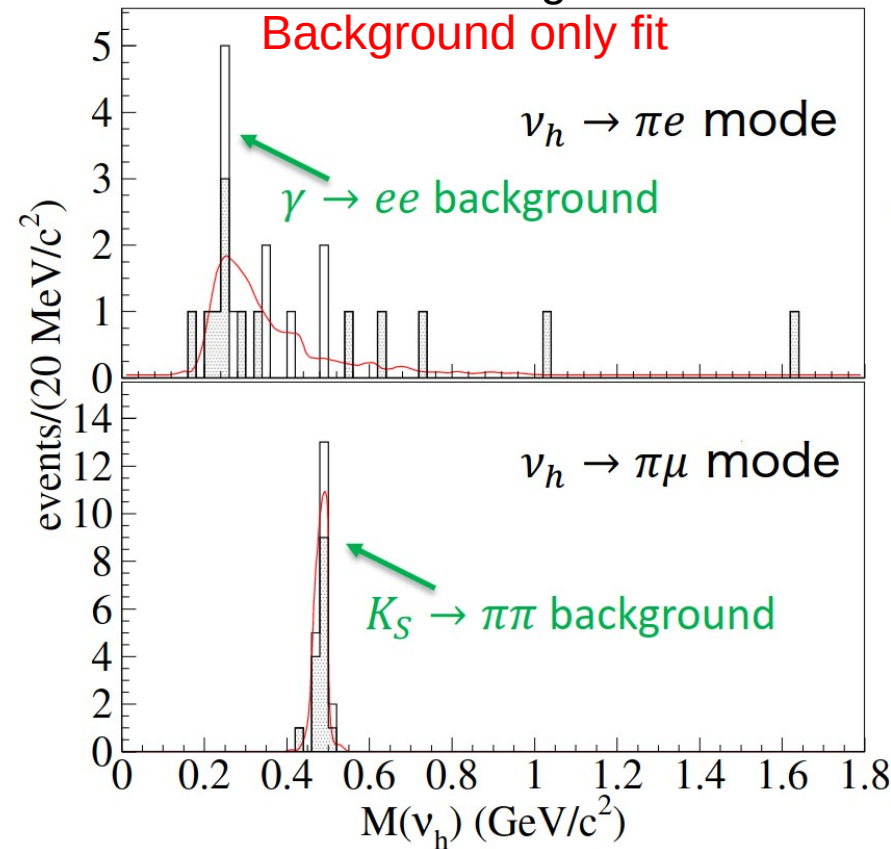
- No narrow signal peak found in  $M(\nu_h \rightarrow \pi l)$  distribution
  - Set upper limit at 95% confidence level

$$\int \mathcal{L} dt = 980 \text{ fb}^{-1}$$

$$\sim 905 \text{ Million } ee \rightarrow \tau\tau$$

Data as histogram

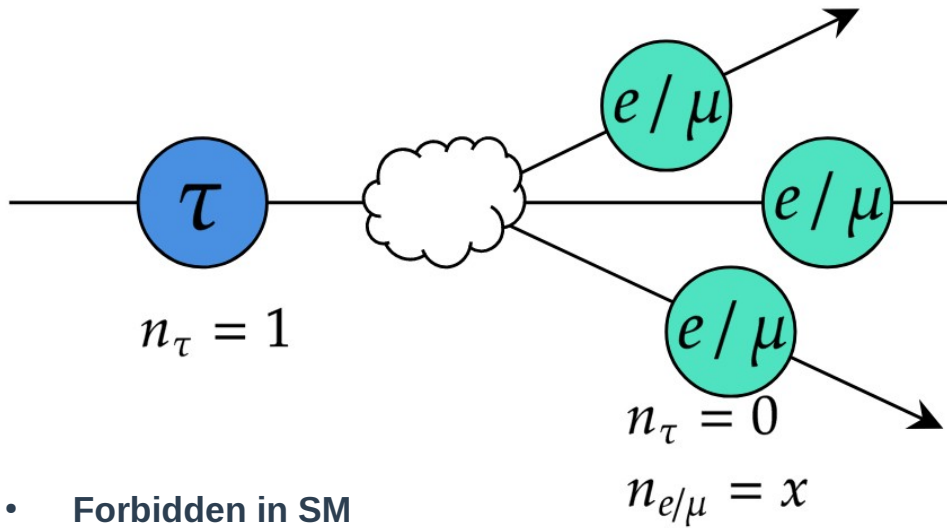
Background only fit



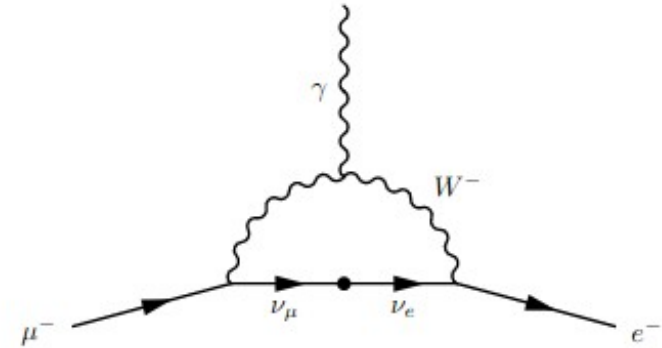
UL on the heavy neutrino mixing set to  
 $0.2 < M(\nu_h) < 1.6 \text{ GeV}/c^2$

# LFV – Motivation

- Lepton Flavor Violation (LFV)

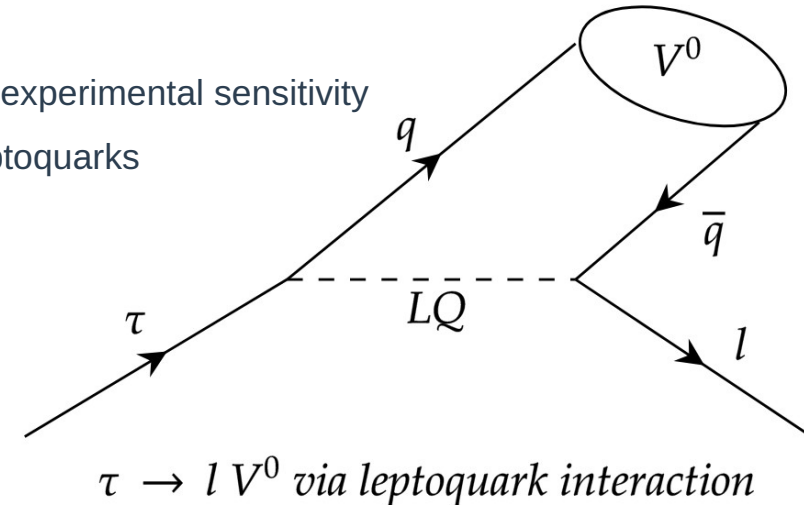


Example: LFV decay  $\mu^- \rightarrow e^- \gamma$  via neutrino oscillations:

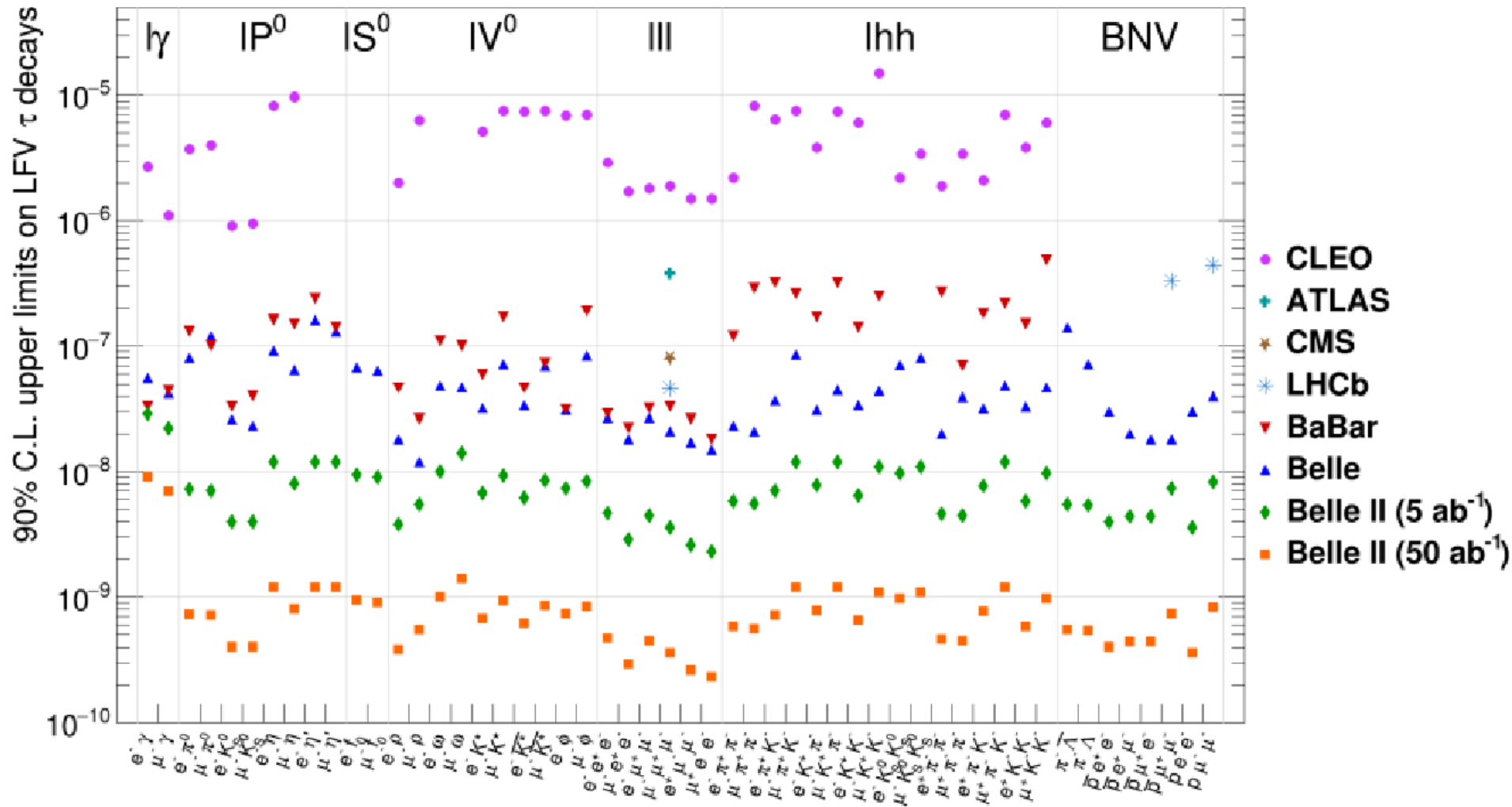


- Forbidden in SM

- Only possible due to neutrino oscillation BR  $\sim O(10^{-50}) \rightarrow$  beyond any experimental sensitivity
- Extensions to the SM (New Physics) predict such decays e.g. via Leptoquarks
  - Can couple to quarks and leptons and so feature LFV decays
- Observation would be new physics



# LFV – Past searches and projections



→ **Belle II is expected to set new upper limits on a wide range of channels**

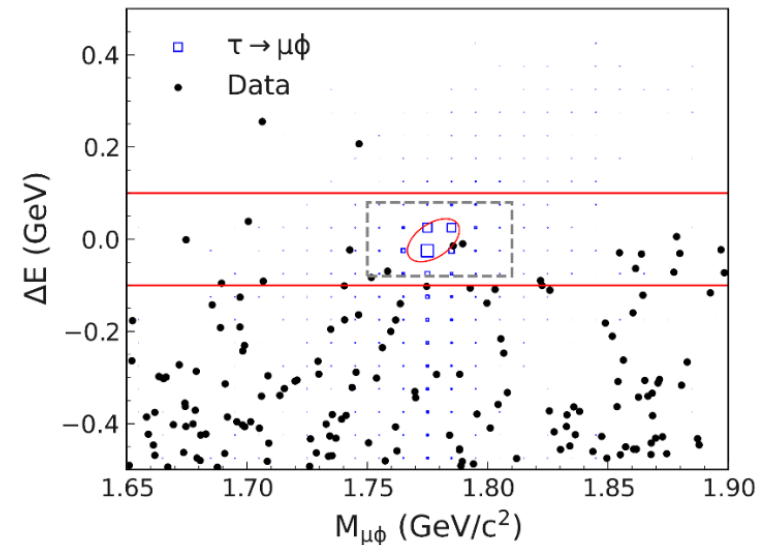
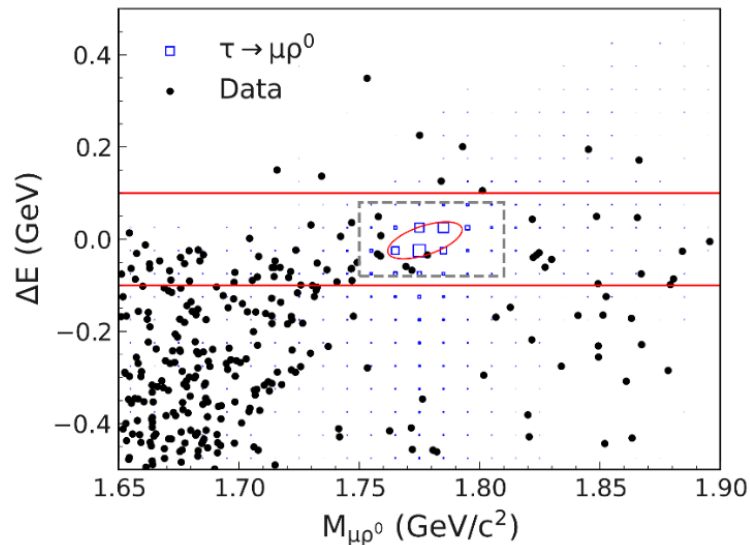
# LFV : $\tau \rightarrow |V^0 - |$

- **Signal side:**
  - Reconstruct lepton and  $V^0 \in [\rho, \phi, \omega, K^*]$
- **Tag side:**
  - Reconstruct 1 or 3-prong tau
- **Backgrounds:**
  - $\tau \rightarrow 3\pi\nu$  and  $ee \rightarrow qq$
  - Suppression with BDT

Source	$\sigma_{\text{syst}}$ (%)
Integrated luminosity	1.4
$ee \rightarrow \tau\tau(\gamma)$ cross section [48]	0.3
$\mathcal{B}(\phi \rightarrow K^+K^-)$ and $\mathcal{B}(\omega \rightarrow \pi^+\pi^-\pi^0)$	1.2 and 0.7
Trigger efficiency	0.2–0.9
Tracking efficiency	$0.35 \times N_{\text{track}}$
Electron identification efficiency	$1.7 \times N_{\text{electron}}$
Muon identification efficiency	$1.8 \times N_{\text{muon}}$
$K^\pm$ and $\pi^\pm$ identification efficiency	1.6 ( $\rho^0$ ), 1.8 ( $\phi$ ) and 1.1 ( $K^{*0}$ and $\bar{K}^{*0}$ )
$\pi^0$ efficiency	$2.2 \times N_{\pi^0}$
Electron veto for hadrons	0.4–1.2
MC statistics	0.3–0.5
Track energy resolution	0.3–1.3
Photon energy resolution	0.0–0.4

$$\int \mathcal{L} dt = 980 \text{ fb}^{-1}$$

$$\sim 905 \text{ Million } ee \rightarrow \tau\tau$$



# LFV : $\tau \rightarrow l V^0 - II$

World leading results

- No significant excess observed  $\rightarrow$  set ULs at 90% CL

Mode	$\varepsilon$ (%)	$N_{BG}$	$\sigma_{syst}$ (%)	$N_{obs}$	$\mathcal{B}_{obs}$ ( $\times 10^{-8}$ )
$\tau^\pm \rightarrow \mu^\pm \rho^0$	7.78	$0.95 \pm 0.20(\text{stat.}) \pm 0.15(\text{syst.})$	4.6	0	$< 1.7$
$\tau^\pm \rightarrow e^\pm \rho^0$	8.49	$0.80 \pm 0.27(\text{stat.}) \pm 0.04(\text{syst.})$	4.4	1	$< 2.2$
$\tau^\pm \rightarrow \mu^\pm \phi$	5.59	$0.47 \pm 0.15(\text{stat.}) \pm 0.05(\text{syst.})$	4.8	0	$< 2.3$ *
$\tau^\pm \rightarrow e^\pm \phi$	6.45	$0.38 \pm 0.21(\text{stat.}) \pm 0.00(\text{syst.})$	4.5	0	$< 2.0$ *
$\tau^\pm \rightarrow \mu^\pm \omega$	3.27	$0.32 \pm 0.23(\text{stat.}) \pm 0.19(\text{syst.})$	4.8	0	$< 3.9$ *
$\tau^\pm \rightarrow e^\pm \omega$	5.41	$0.74 \pm 0.43(\text{stat.}) \pm 0.06(\text{syst.})$	4.5	0	$< 2.4$ *
$\tau^\pm \rightarrow \mu^\pm K^{*0}$	4.52	$0.84 \pm 0.25(\text{stat.}) \pm 0.31(\text{syst.})$	4.3	0	$< 2.9$ *
$\tau^\pm \rightarrow e^\pm K^{*0}$	6.94	$0.54 \pm 0.21(\text{stat.}) \pm 0.16(\text{syst.})$	4.1	0	$< 1.9$ *
$\tau^\pm \rightarrow \mu^\pm \bar{K}^{*0}$	4.58	$0.58 \pm 0.17(\text{stat.}) \pm 0.12(\text{syst.})$	4.3	1	$< 4.3$ *
$\tau^\pm \rightarrow e^\pm \bar{K}^{*0}$	7.45	$0.25 \pm 0.11(\text{stat.}) \pm 0.02(\text{syst.})$	4.1	0	$< 1.7$ *

$$B(\tau \rightarrow e V^0) < (1.7 - 2.4) \times 10^{-8}$$

$$B(\tau \rightarrow \mu V^0) < (1.7 - 4.3) \times 10^{-8}$$

Improvement  $\sim 30\%$  compared to previous results!

# LFV : $\tau \rightarrow l \phi$



- **Untagged inclusive reconstruction: do not reconstruct the tag side into a specific decay**
  - Higher Signal efficiency (~32% improvement), more background, use of rest of event variables

$$\int \mathcal{L} dt = 190 \text{ fb}^{-1}$$

$$\sim 75 \text{ Million } ee \rightarrow \tau\tau$$

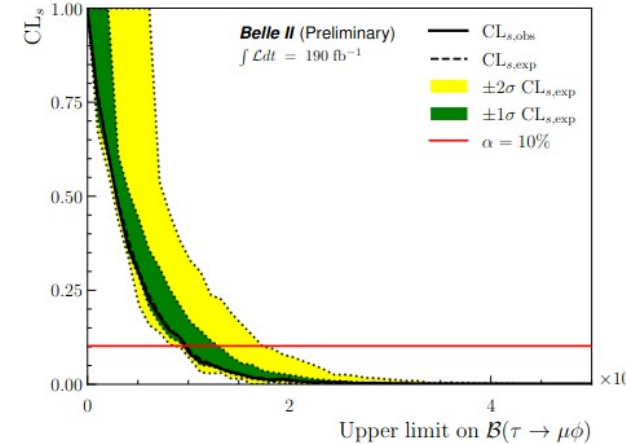
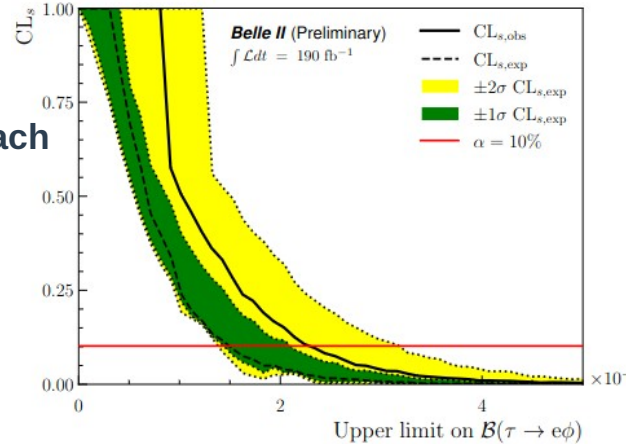
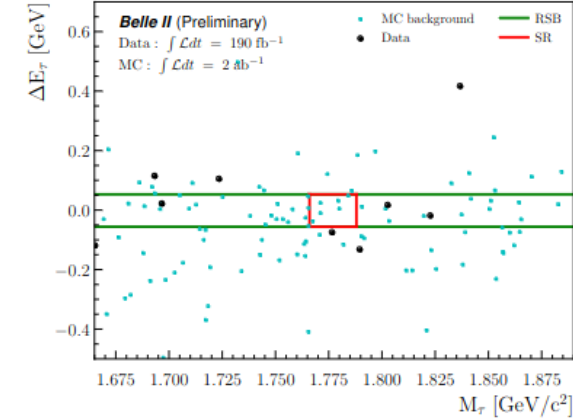
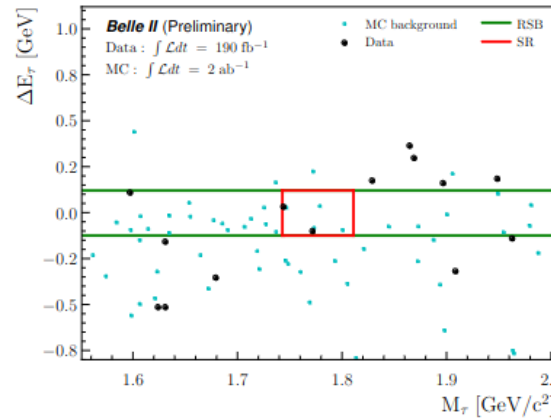
- **Backgrounds reduced with pre selections and a BDT trained against qqbar events**

## Observed UL

- Electron channel :  $1.0 \times 10^{-7}$
- Muon channel :  $6.6 \times 10^{-8}$

- **No improvement to Belle/BaBar**  
→ **Small data set**

- **First, successful untagged strategy approach for tau physics**



Experiment	$\mathcal{B}_{UL}^{90}(e\phi) (\times 10^{-8})$	$\mathcal{B}_{UL}^{90}(\mu\phi) (\times 10^{-8})$
	exp. / obs.	exp / obs.
BaBar	5.0 / 3.1	8.2 / 19
Belle	4.3 / 3.1	4.9 / 8.4

Babar : 451/fb  
Belle : 854/fb

<https://arxiv.org/abs/2305.04759>



# LFV : $\tau \rightarrow l\alpha - l$

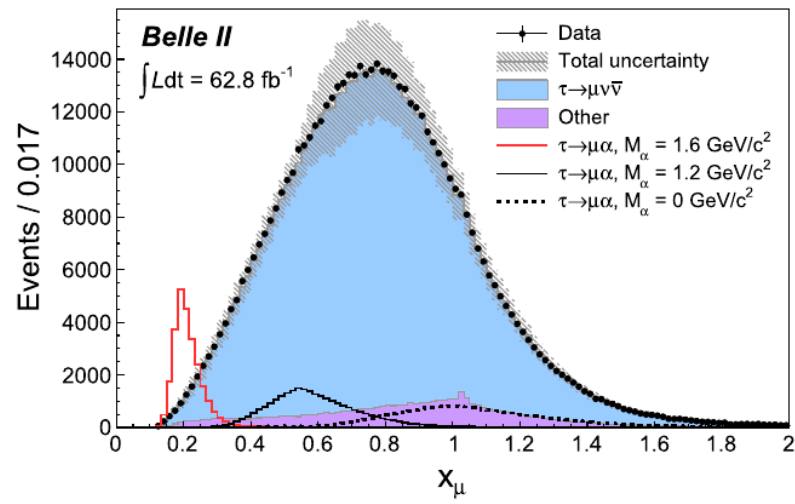
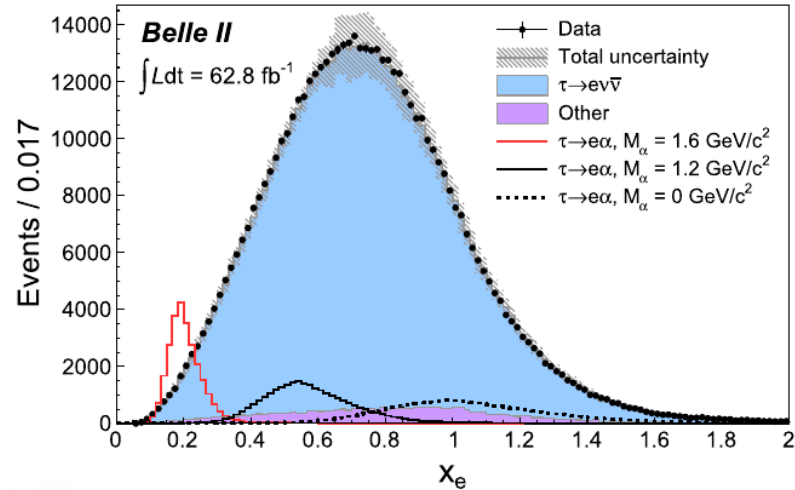
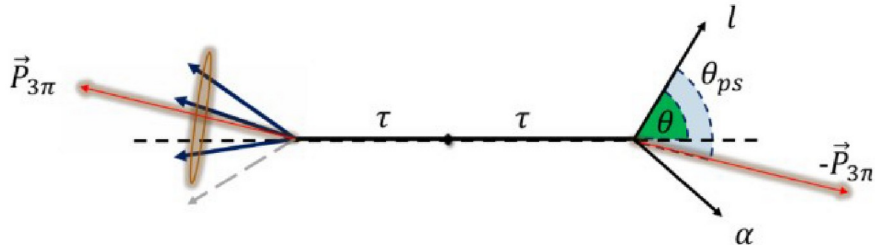
- $\alpha$  is an invisible spin-0 boson
  - Predicted by many models trying to incorporate neutrino-oscillation, muon magnetic moment anomaly or indirect evidence of dark matter in SM

This direct search probes BSM theories with high sensitivity

Previous limits from ARGUS:  $10^{-2}$  to  $10^{-3}$  0.5/fb of data  $\int \mathcal{L} dt = 62.8 \text{ fb}^{-1}$   
 $\sim 57.7$  Million  $ee \rightarrow \tau\tau$

- Tau momentum cannot be determined from the decay particles directly
  - Approximate the energy in CMS as half of the beam energy and its direction opposite to the 3 hadrons on the tag-side pseudo rest frame
  - Search for an excess above the  $\tau \rightarrow l\nu\nu$  normalized lepton energy spectrum with  $E_l^*$  the energy of the charged lepton in pseudo rest frame

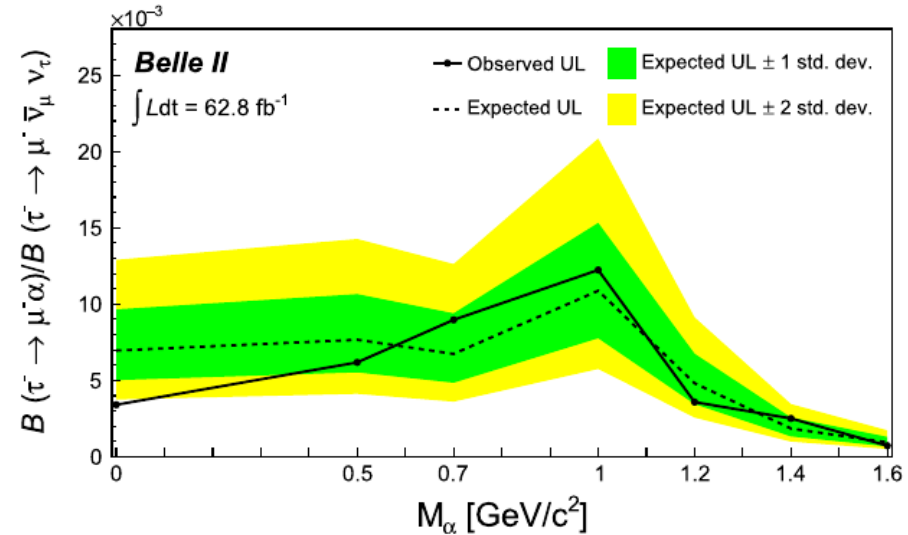
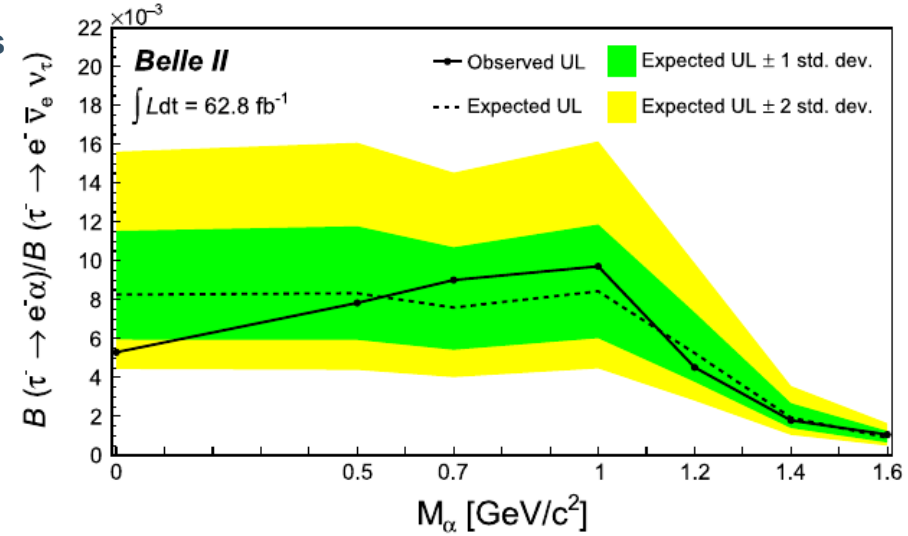
$$x_\ell \equiv \frac{E_\ell^*}{m_\tau c^2 / 2}$$



PRL 130 181803 (2023)

# LFV : $\tau \rightarrow l\alpha - II$

- Simulation derived templates fit for different  $\alpha$  mass hypotheses
- Measure 
$$\mathcal{B}_{\ell\alpha}/\mathcal{B}_{\ell\bar{\nu}\nu} \equiv \mathcal{B}(\tau^- \rightarrow \ell^- \alpha) / \mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$$
 with  $\tau \rightarrow l\nu\nu$  as normalization channel 
$$\int \mathcal{L} dt = 62.8 \text{ fb}^{-1}$$
- 2 to 14 times more stringent than ARGUS  $\sim 57.7$  Million  $ee \rightarrow \tau\tau$ 
  - Still only early data set in use  $\rightarrow$  stay tuned

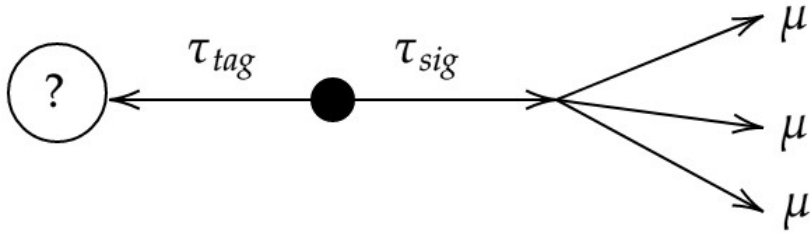


$M_\alpha$ [GeV/c <sup>2</sup> ]	$\mathcal{B}_{e\alpha}/\mathcal{B}_{e\bar{\nu}\nu}$ ( $\times 10^{-3}$ )	UL at 95% C.L. ( $\times 10^{-3}$ )	UL at 90% C.L. ( $\times 10^{-3}$ )
0.0	$-8.1 \pm 3.9$	5.3(0.94)	4.3(0.76)
0.5	$-0.9 \pm 4.3$	7.8(1.40)	6.5(1.15)
0.7	$1.7 \pm 4.0$	9.0(1.61)	7.6(1.36)
1.0	$1.7 \pm 4.2$	9.7(1.73)	8.2(1.47)
1.2	$-1.1 \pm 2.6$	4.5(0.80)	3.7(0.66)
1.4	$-0.3 \pm 1.0$	1.8(0.32)	1.5(0.26)
1.6	$0.2 \pm 0.5$	1.1(0.19)	0.9(0.16)

$M_\alpha$ [GeV/c <sup>2</sup> ]	$\mathcal{B}_{\mu\alpha}/\mathcal{B}_{\mu\nu}$ ( $\times 10^{-3}$ )	UL at 95% C.L. ( $\times 10^{-3}$ )	UL at 90% C.L. ( $\times 10^{-3}$ )
0.0	$-9.4 \pm 3.7$	3.4(0.59)	2.7(0.47)
0.5	$-3.2 \pm 3.9$	6.2(1.07)	5.1(0.88)
0.7	$2.7 \pm 3.4$	9.0(1.56)	7.8(1.35)
1.0	$1.7 \pm 5.4$	12.2(2.13)	10.3(1.80)
1.2	$-0.2 \pm 2.4$	3.6(0.62)	2.9(0.51)
1.4	$0.9 \pm 0.9$	2.5(0.44)	2.2(0.38)
1.6	$-0.3 \pm 0.5$	0.7(0.13)	0.6(0.10)

# LFV : $\tau \rightarrow \mu \mu \mu - I$ (NEW)

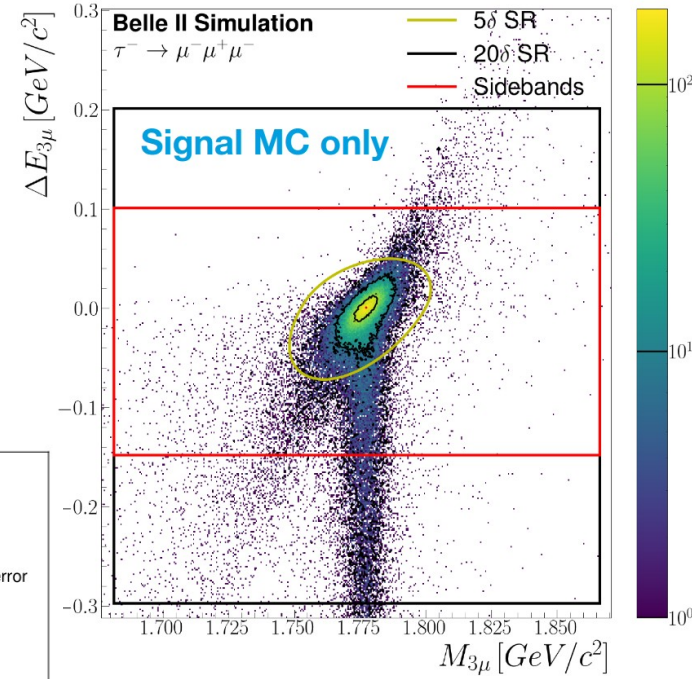
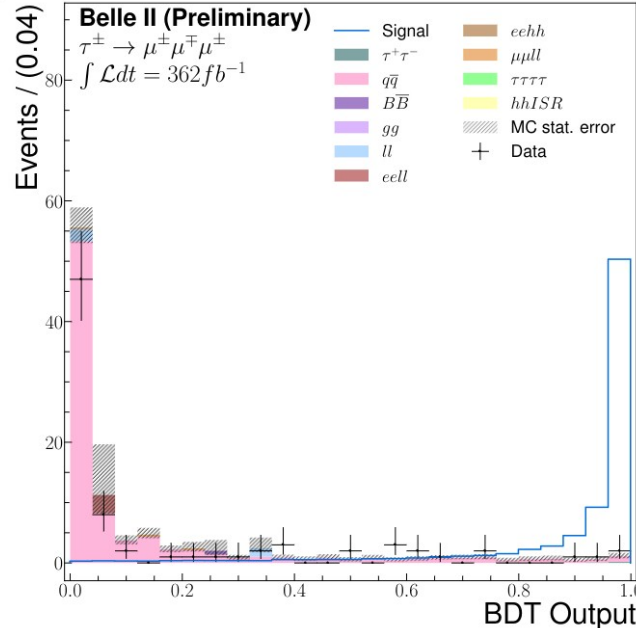
- Best previous upper limit from Belle  $2.1 \times 10^{-8}$  @90% CL with 782/fb
- Inclusive  $\rightarrow$  ~30% gain in signal efficiency, larger backgrounds
  - Selection and background rejection based on BDT



- Fully reconstructed tau signal
- No peaking background from SM processes

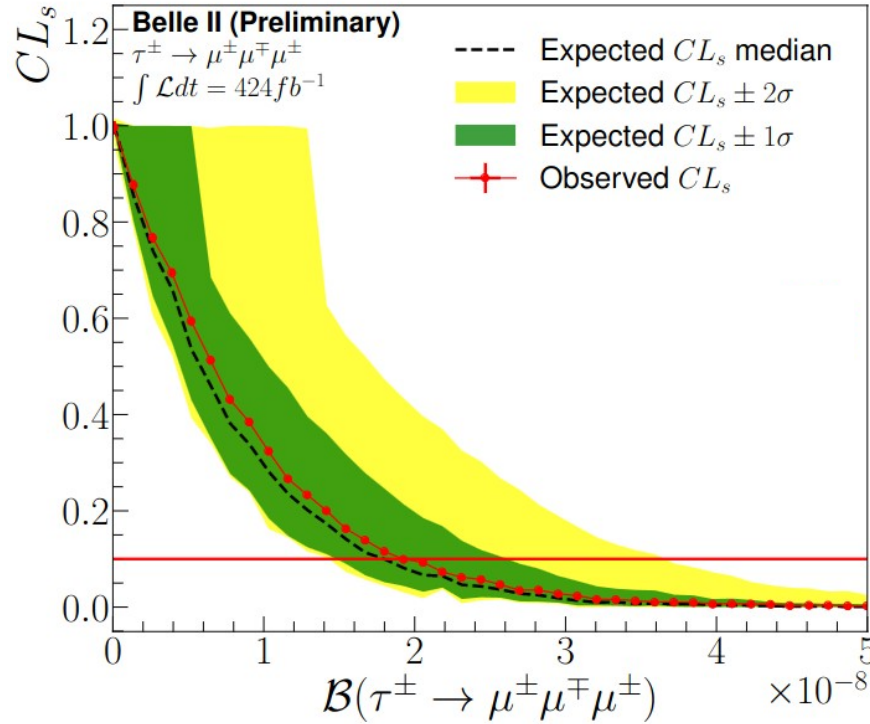
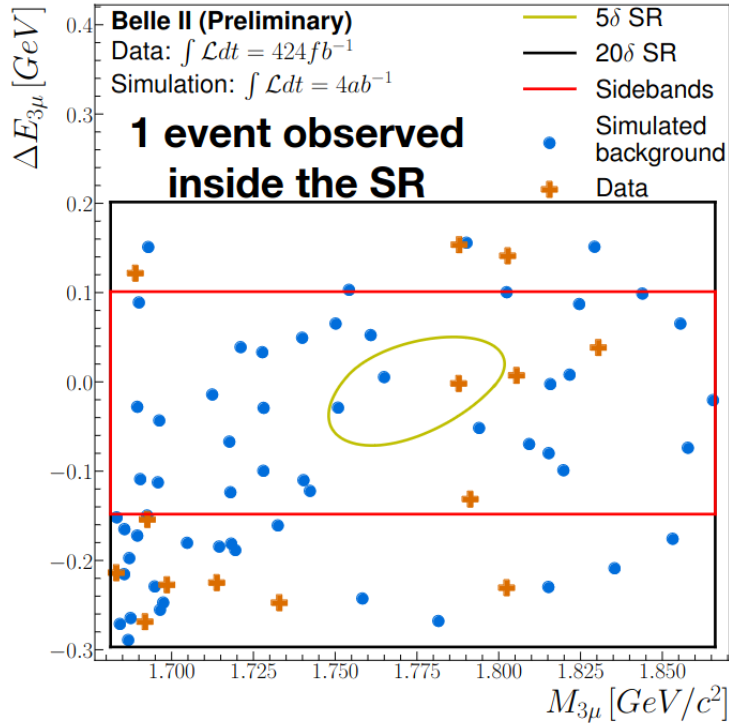
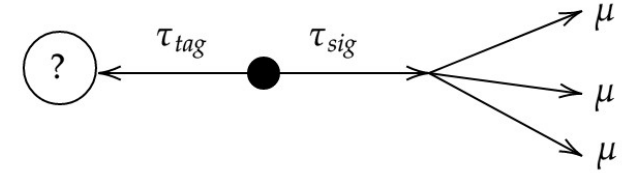
$$\int \mathcal{L} dt = 424 \text{ fb}^{-1}$$

$$\sim 391 \text{ Million } ee \rightarrow \tau\tau$$



# LFV : $\tau \rightarrow \mu \mu \mu$ - II (NEW)

- XGBoost BDT with 32 variables
  - Inputs from signal tau, event tag-side and event shape/kinematic variables
  - $\epsilon = 20.42\%$  ~ 3 times larger than Belle
  - Expected background events :  $0.5^{+1.4}_{-0.5}$
- No significant excess  $\rightarrow$  calculate UL @90% CL with 424/fb using CLs method



UL :  $1.9 \times 10^{-8}$   
 $\rightarrow$  most stringent!

# Summary

- **B factories are a good environment for tau physics!**
- **Belle and Belle II will contribute to the understanding of tau lepton properties**
  - Searches for BSM physics
  - LFU
  - Precision measurements of SM parameters
- **Analysis with combined Belle & Belle II data sets are ongoing**
- **A lot more to come with more data**
  - Now 424/fb, next run starting in the coming weeks
- **Topics not covered:**
  - Michel Parameters : [PRL 131.021801 \(2023\)](#)
  - Tau lifetime → ongoing study
  - LFV → ongoing studies