

# HIRSCHEGG 2024 – Strong Interaction Physics of Heavy Flavors



## Multiquark states –

Recent results in charm-strange and bottomonium spectroscopy

Elisabetta Prencipe, JLU-Giessen (DE)\*

# Outline

- Introduction
- Status-of-the-art in  $cs$  spectroscopy
- $c\bar{c}s\bar{s}$  spectroscopy
- Analyses in the continuum at Belle
- Analyses in the bottomonium sector at Belle and Belle II

# Outline

- Introduction
- Status-of-the-art in  $c\bar{c}$  spectroscopy
- $c\bar{c}s\bar{s}$  spectroscopy
- Analyses in the continuum at Belle
- Analyses in the bottomonium sector at Belle and Belle II
- Future perspectives
- Summary



This talk is focused on  
**BELLE & Belle II**  
results

# The CQM Model

- Gell-Mann Zweig idea: **Constituent Quark Model (CQM)**, 1964). Still valid after 60 years



A SCHEMATIC MODEL OF BARYONS AND MESONS \*

M. GELL-MANN

California Institute of Technology, Pasadena, California

Received 4 January 1964

If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" <sup>1-3</sup>, we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dynamical "bootstrap" model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightfold symmetry from self-consistency alone <sup>4</sup>. Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the F-spin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

Even if we consider the scattering amplitudes of strongly interacting particles on the mass shell only and treat the matrix elements of the weak, electromagnetic, and gravitational interactions by means

ber  $n_t - n_{\bar{t}}$  would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin  $\frac{1}{2}$  and  $z = -1$ , so that the four particles  $d^-$ ,  $s^-$ ,  $u^0$  and  $b^0$  exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $b$  if we assign to the triplet  $t$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ . We then refer to the members  $u^{\frac{2}{3}}$ ,  $d^{-\frac{1}{3}}$ , and  $s^{-\frac{1}{3}}$  of the triplet as "quarks" <sup>6</sup>  $q$  and the members of the anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc. It is assuming that the lowest baryon configuration  $(qqq)$  gives just the representations 1, 8, and 10 that have been observed, while the lowest meson configuration  $(q\bar{q})$  similarly gives just 1 and 8.

AN SU<sub>3</sub> MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING

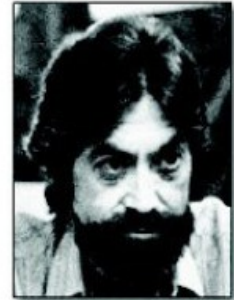
G. Zweig <sup>\*)</sup>

CERN - Geneva

8182/TH.401

17 January 1964

ABSTRACT



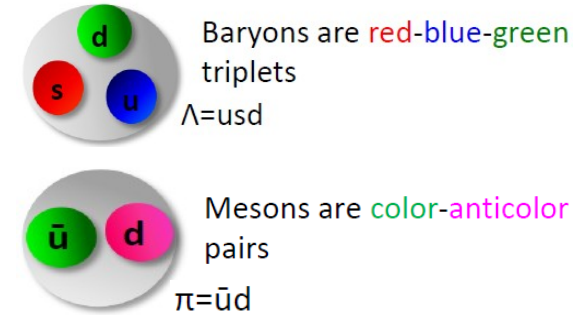
...

In general, we would expect that baryons are built not only from the product of three aces, AAA, but also from AAAAA, AAAAAA, etc., where  $\bar{A}$  denotes an anti-ace. Similarly, mesons could be formed from  $\bar{A}A$ , AAAA etc. For the low mass mesons and baryons we will assume the simplest possibilities,  $\bar{A}A$  and AAA, that is, "deuces and treys".

sch

# The CQM Model

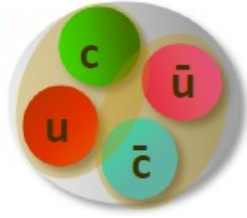
- QCD describes the force binding quarks into hadrons
- Perturbation theory: limited applicability at scale corresponding to the separation between quarks inside hadrons
- Many models available to describe spectra and properties of hadrons
- QCD-motivated models predict the existence of hadrons with more complex structures than simple  $qq$  or  $qqq$ .
- **Lots of experimental effort to prove it!**
- The study of Charm-onium(-like) spectrum ( $c\bar{c}$ ) +  $xx$ ) and Bottomonium spectrum ( $b\bar{b}$ ) +  $xx$ ) have uncovered a number of candidates that seem not to conform CQM expectations
- Exotic states predicted to exist in the light meson spectrum
  - difficult to disentangle from the dense background of conventional states
- Charmonium spectrum provide a cleaner environment:  $\bar{c}c$  +  $xx$  exotics easier to identify



# What are the possibilities?

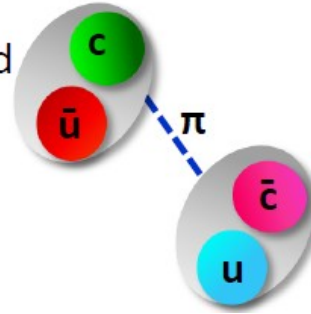
## Tetraquark

Tightly bound  
diquark &  
anti-diquark

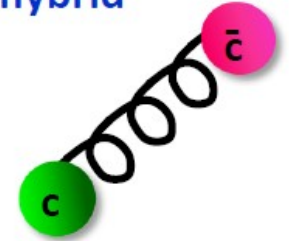


## Molecule

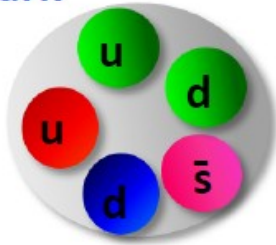
loosely bound  
meson-  
antimeson  
“molecule”



## $q\bar{q}$ -gluon hybrid mesons

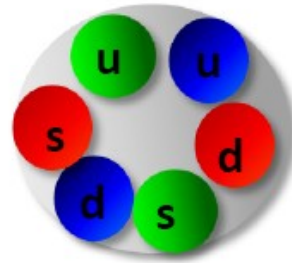


## Pentaquark



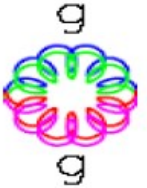
## H di-Baryon

Tightly bound  
6 quark state














## Glueball

Color-singlet multi-  
gluon bound state



...and superimposition of states. Everything which does not fit CQM!

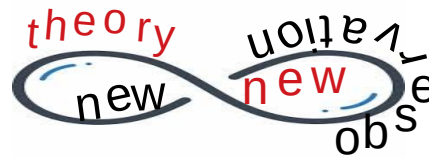
# Where to find these new multiquark states?

- Direct production in  $e^+e^-$  collisions  
- Production in  $B \rightarrow K c\bar{c}$   
- Photon-photon scattering  $\gamma\gamma^* \rightarrow (c\bar{c})$  
- Double charmonium  $e^+e^- \rightarrow (c\bar{c})(c\bar{c})$  
- Prompt production    
- Direct production in  $p\bar{p}$   (??)

- How to find multiquark states?

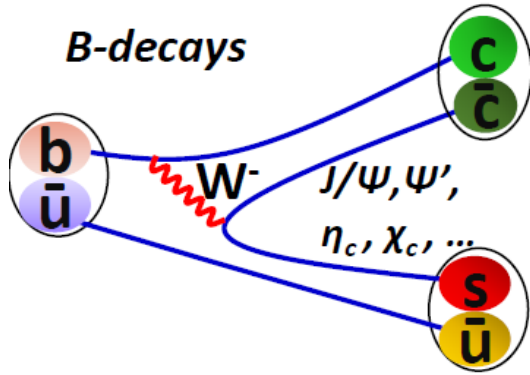
Choose the right detector, make your analysis!

- Interplay between theory-experiments: the infinite loop

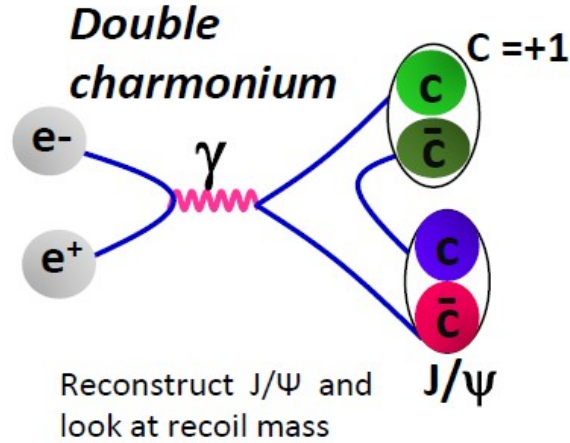
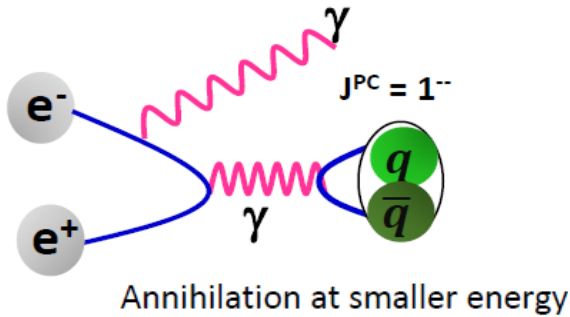




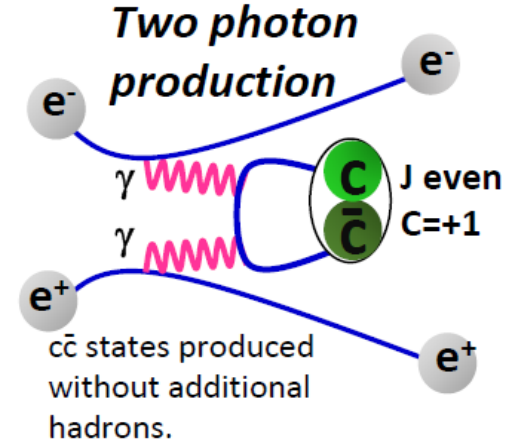
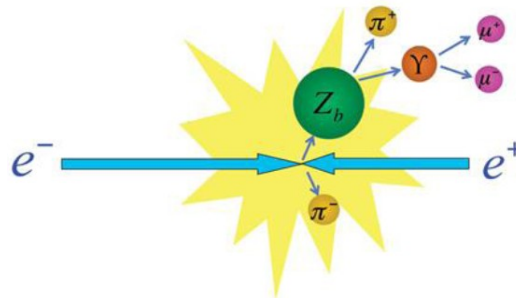
@ B-factories



**Initial state radiation**



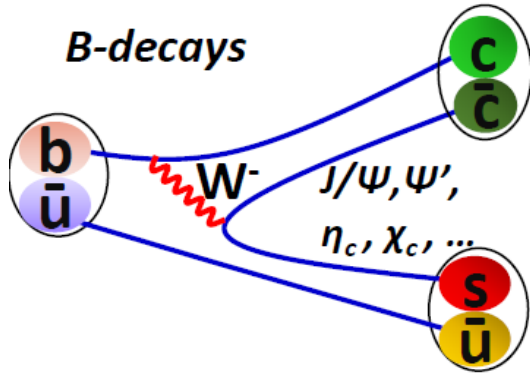
**Quarkonium decay/transitions**



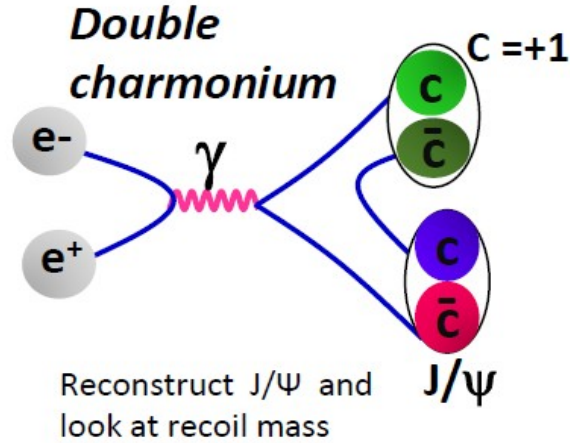
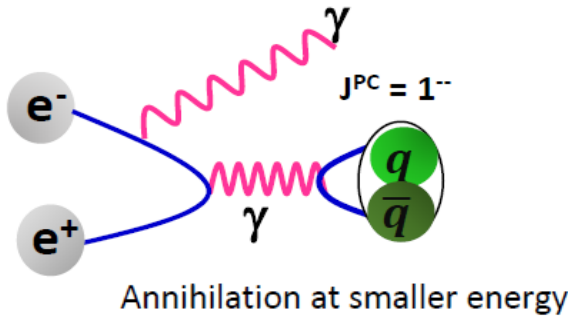
**Advantages @ B-factory**

- “Clean” events
- Huge data sets available
- Several mechanisms to search for exotics

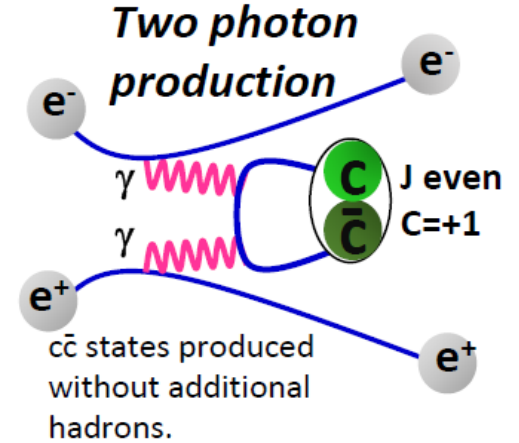
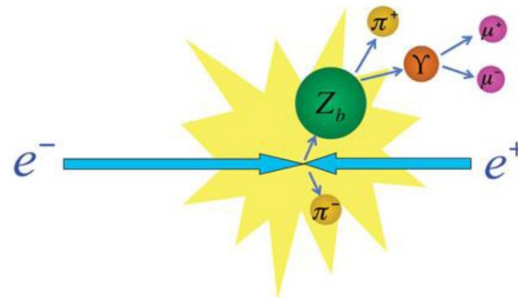
@ B-factories



**Initial state radiation**

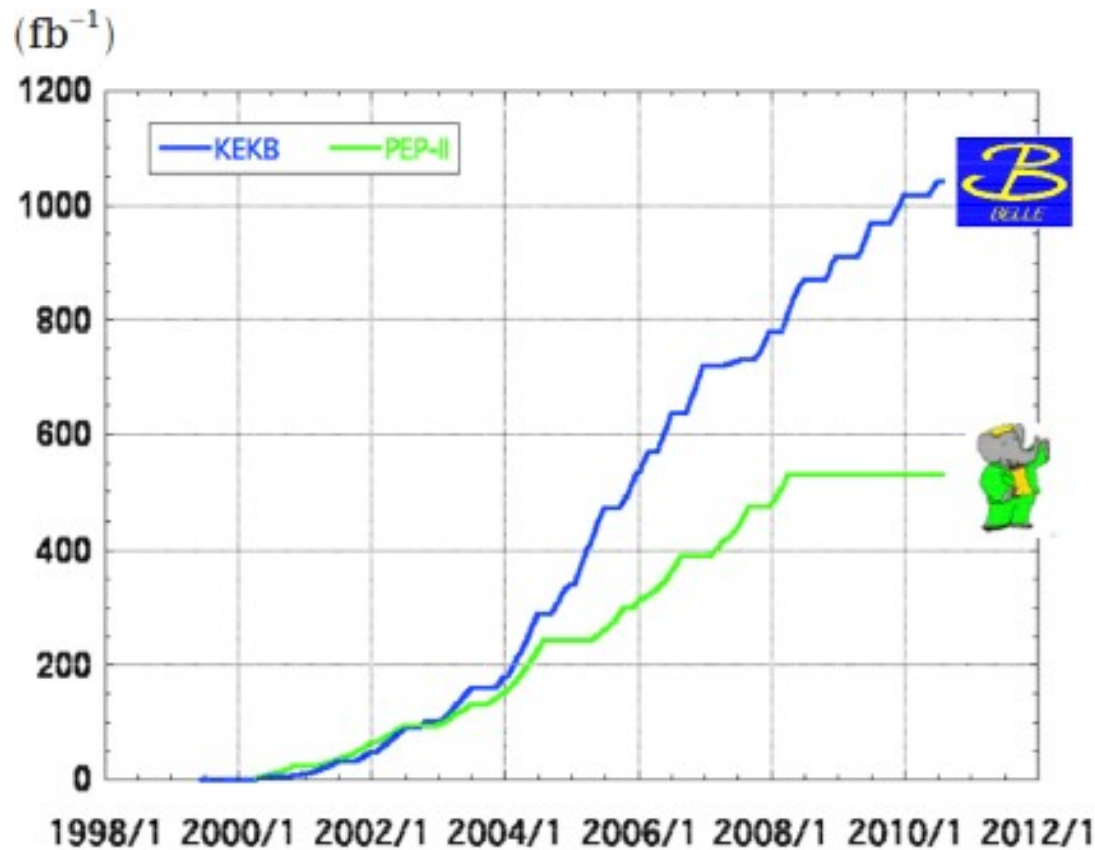


**Quarkonium decay/transitions**



**Disadvantages @ B-factory**

- No all  $J^{PC}$  in production
- Small cross sections



**> 1 ab<sup>-1</sup>**

**On resonance:**

Y(5S): 121 fb<sup>-1</sup>

Y(4S): 711 fb<sup>-1</sup>

Y(3S): 3 fb<sup>-1</sup>

Y(2S): 25 fb<sup>-1</sup>

Y(1S): 6 fb<sup>-1</sup>

**Off reson./scan:**

~ 100 fb<sup>-1</sup>

**~ 550 fb<sup>-1</sup>**

**On resonance:**

Y(4S): 433 fb<sup>-1</sup>

Y(3S): 30 fb<sup>-1</sup>

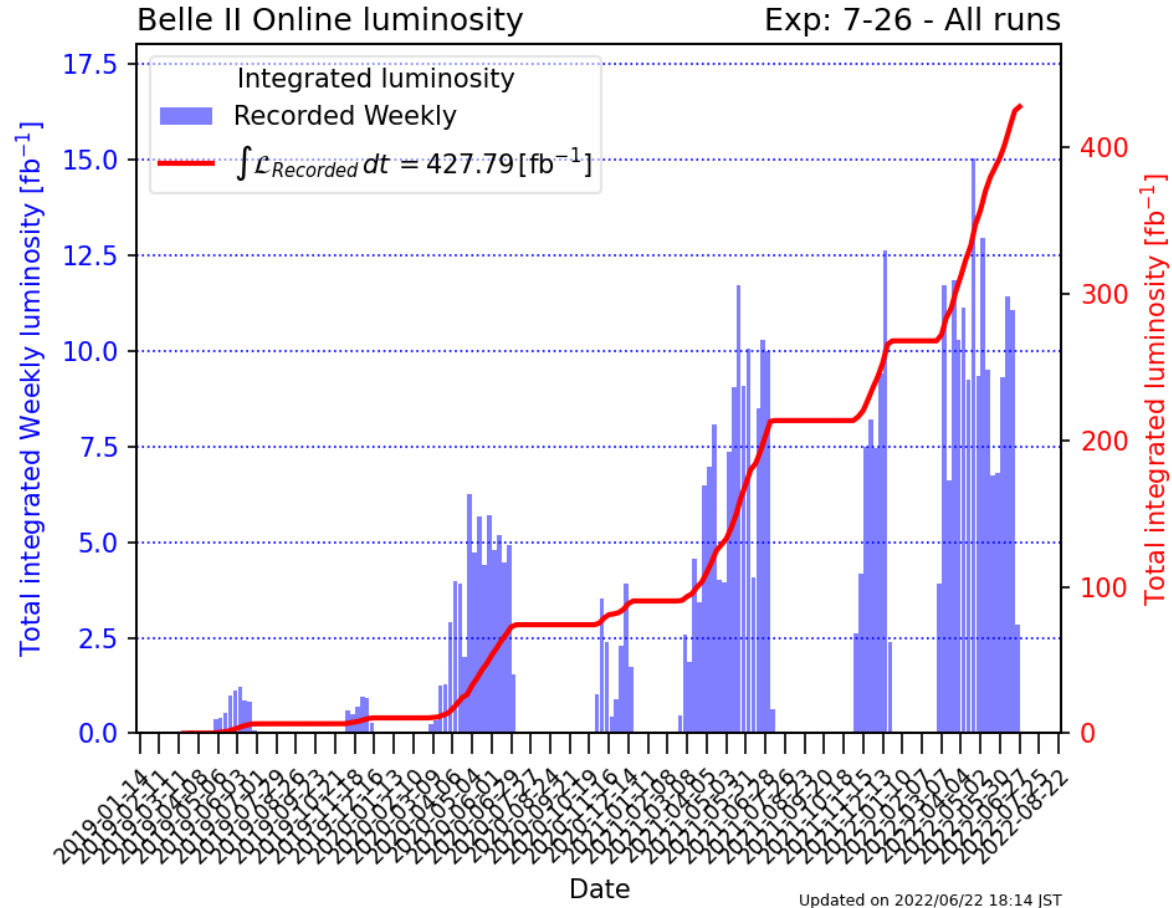
Y(2S): 14 fb<sup>-1</sup>

**Off resonance:**

~ 54 fb<sup>-1</sup>

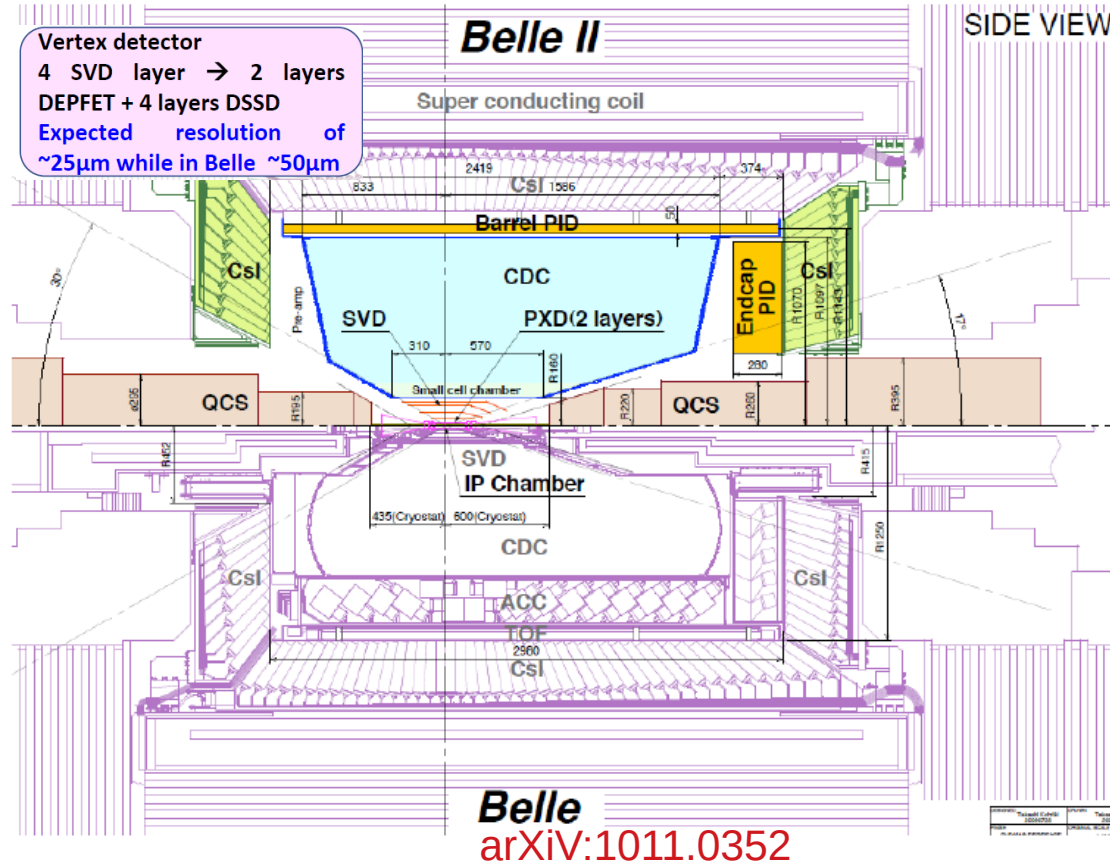
| Resonance | BaBar    | Belle      |
|-----------|----------|------------|
| Y(3S)     | 121 M    | 12 M       |
| Y(2S)     | 98+(3) M | 175 M      |
| Y(1S)     | (23) M   | 113+(32) M |

# ...and the story continues



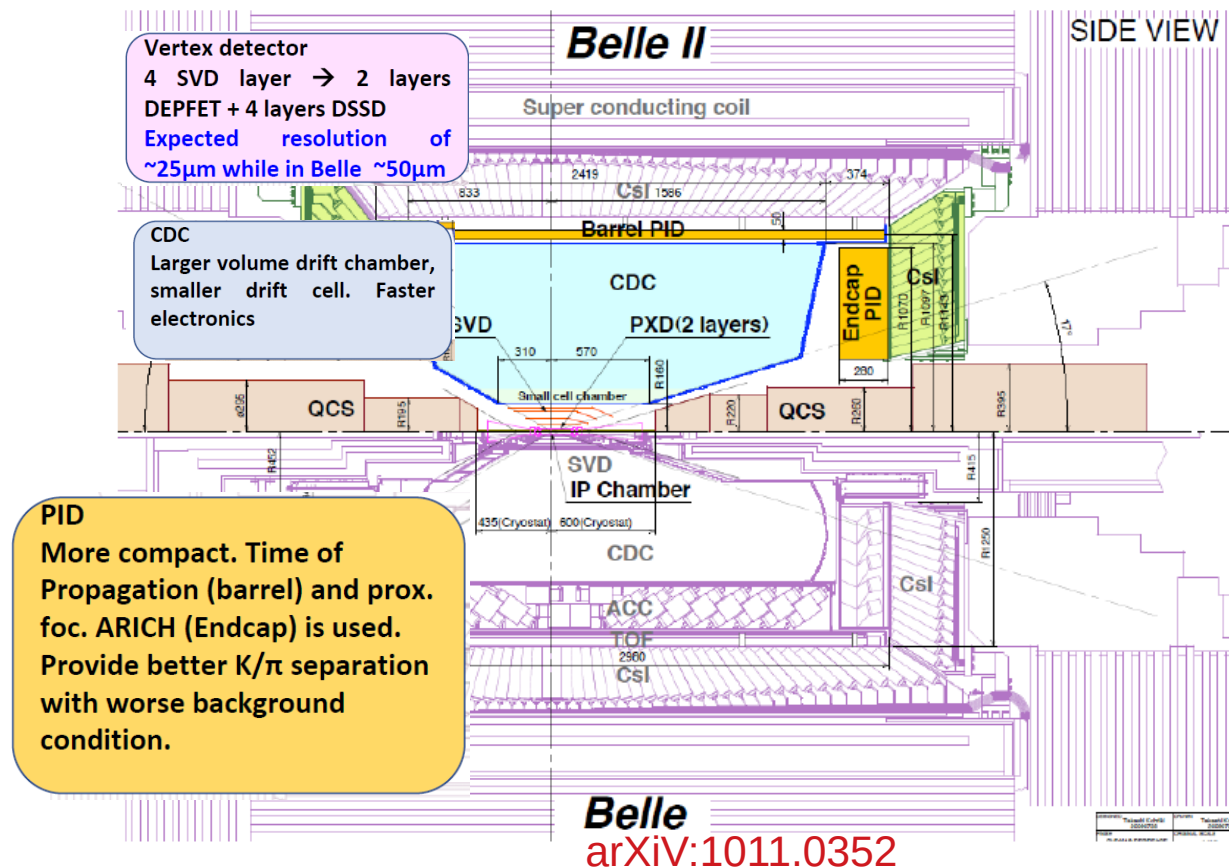


# The Belle II Detector





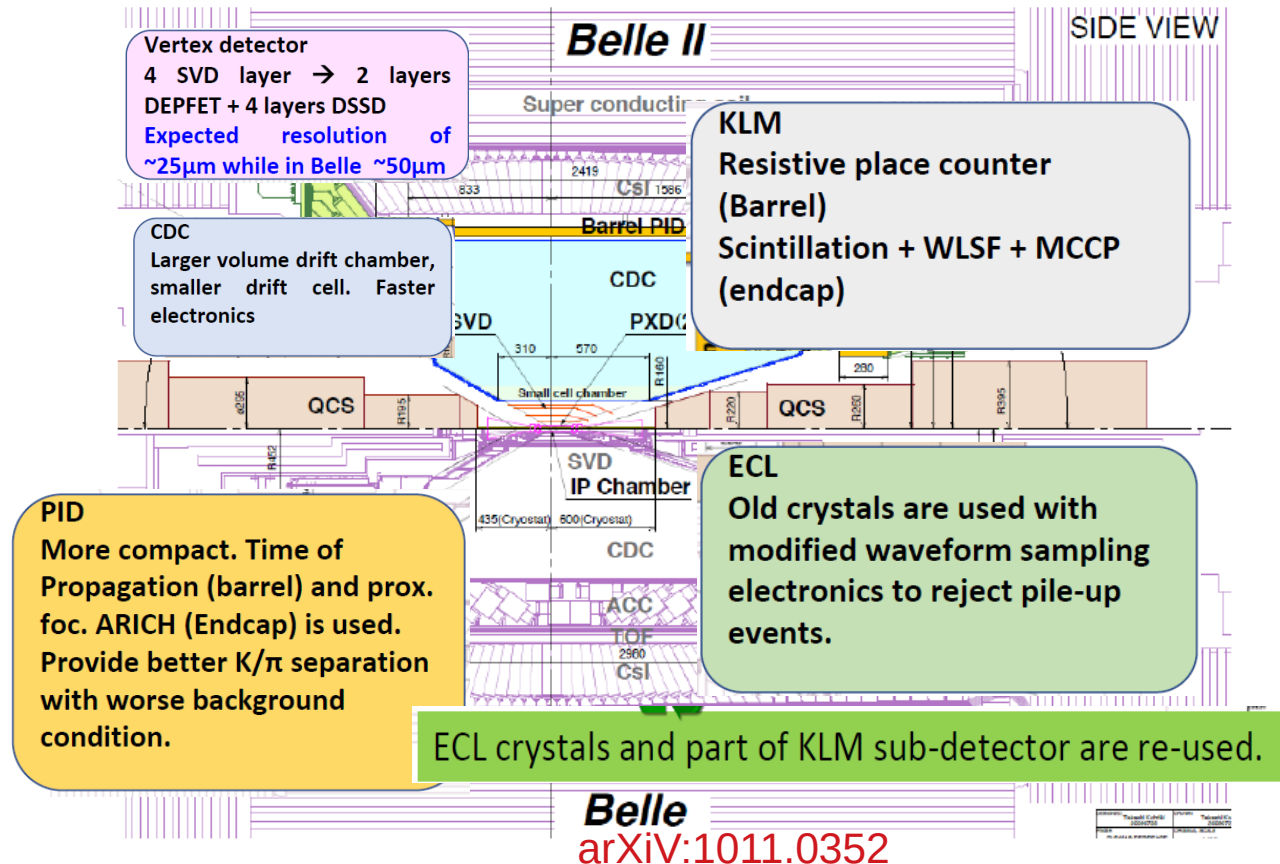
# The Belle Detector







# The Belle II Detector



# *Topics of this talk*

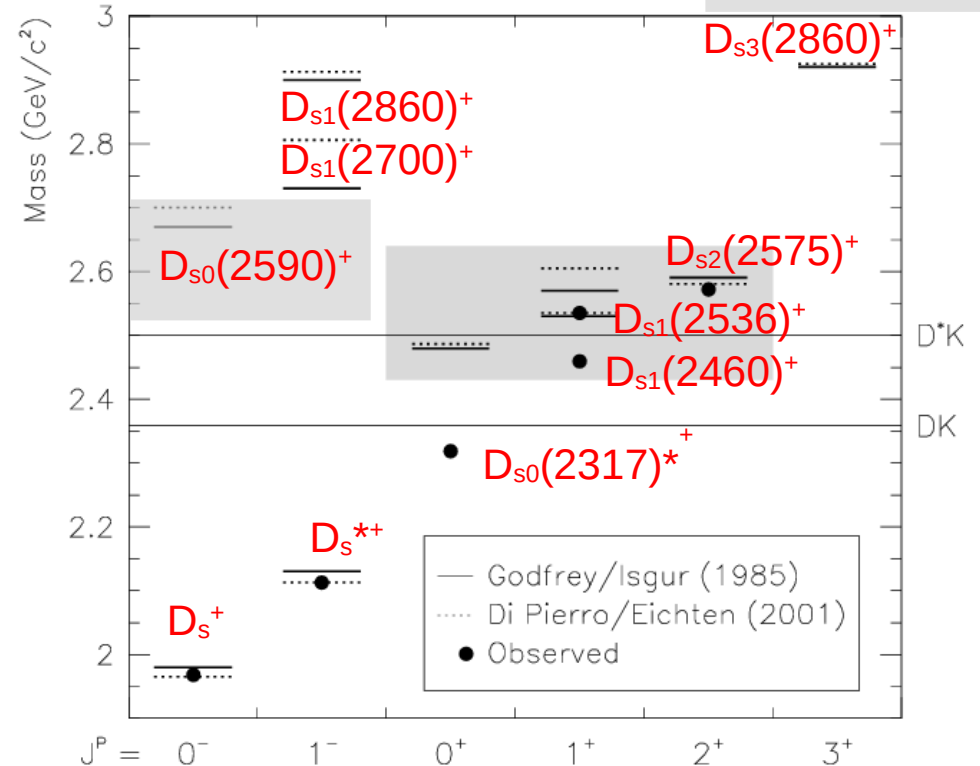
- Heavy-light systems at **Belle and Belle II**
  - $D_s^{(*)}D_{sJ}^{(*)}$  analysis in the continuum
- Pentaquarks search at **Belle and Belle II**
- Bottomonium at **Belle and Belle II**

# The heavy-light systems

- Recent boost to the search for *cs* (and *double cs*) resonances:

$D_s(3040)^+$

- LHCb and Belle
- Very interesting case:  
s-quark (light) + c-quark (heavy)
- Can we make predictions?
- Perturbative calculations work pretty well for the heavy sector, and should be also in the heavy-light systems: but....



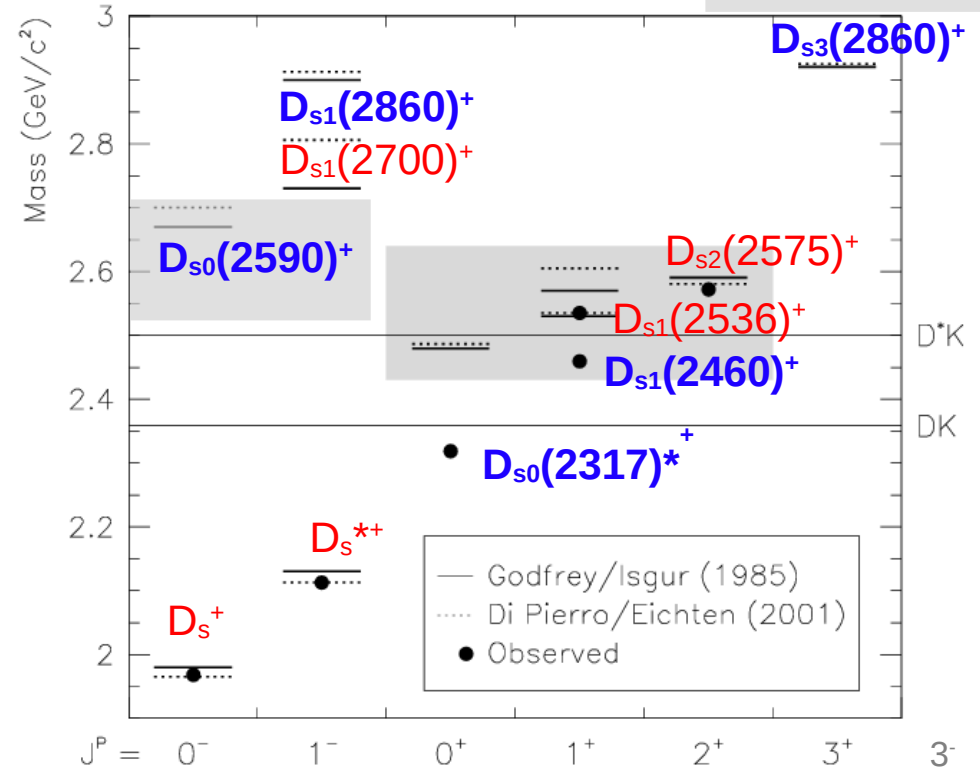
# The heavy-light systems

- Recent boost to the search for *cs* (and *double cs*) resonances:

LHCb and Belle

- Very interesting case:  
s-quark (light) + c-quark (heavy)
- Can we make predictions?
- Perturbative calculations work pretty well for the heavy sector, and should be also in the heavy-light systems: but....

**$D_s(3040)^+$**



# *How has the $c_s$ -story begun?*

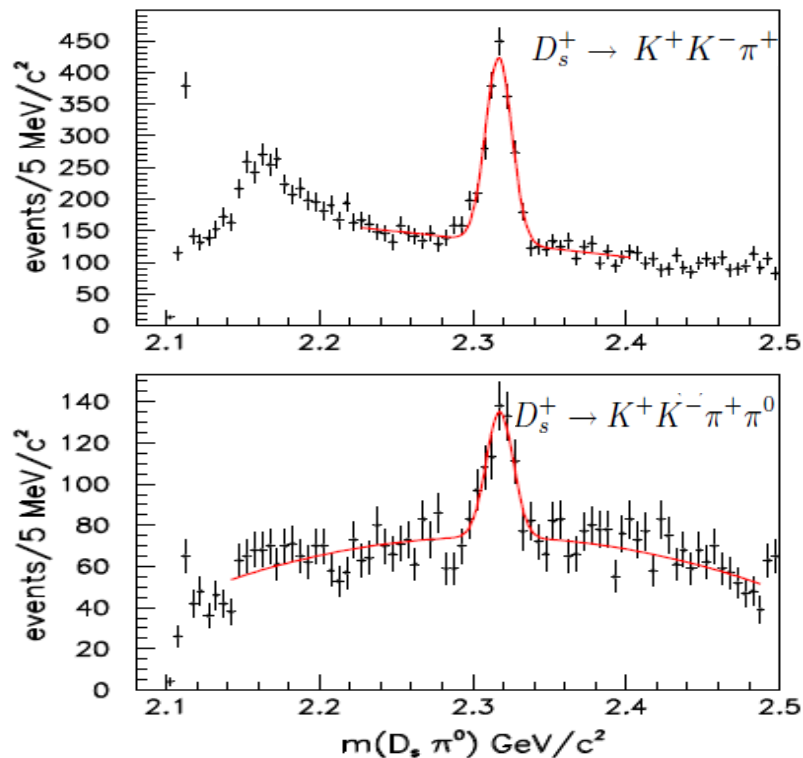
**Phys. Rev. Lett. 90 (2003) 242001** BaBar, accepted 17 June 2003

**Observation of a Narrow Meson State Decaying to  $D_s^+ \pi^0$  at a Mass of 2.32 GeV/c<sup>2</sup>**

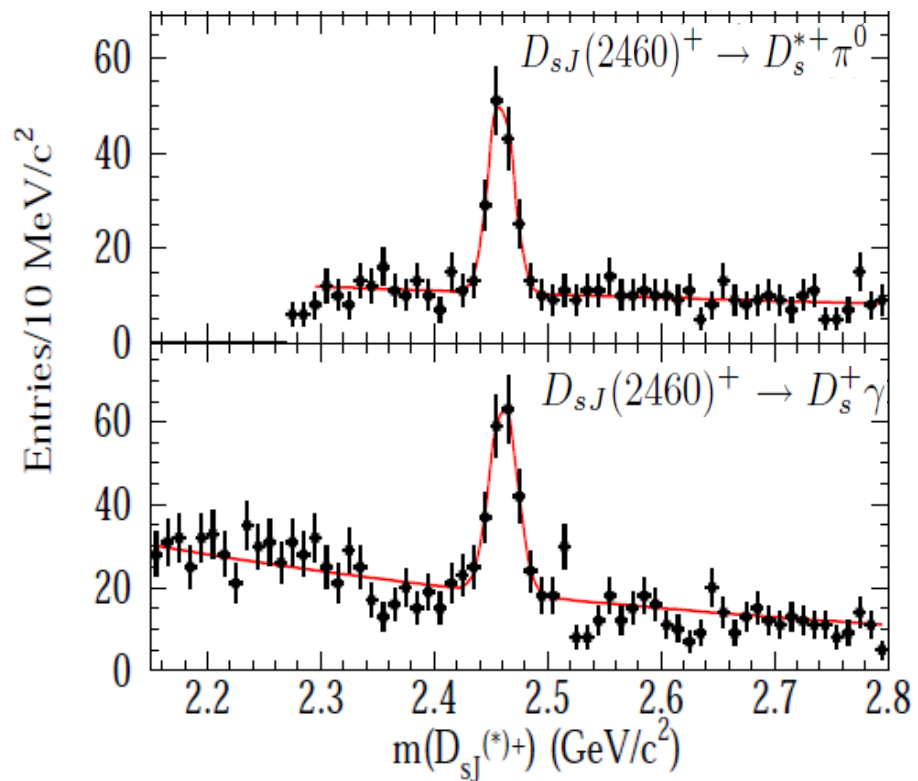
**990 citations**




















# The puzzling case of the $D_{s0}(2317)^{*+}$ and $D_{s1}(2460)^{+}$

BABAR, PRL 90 (2003) 242001



BABAR, PRL 93 (2004) 181801



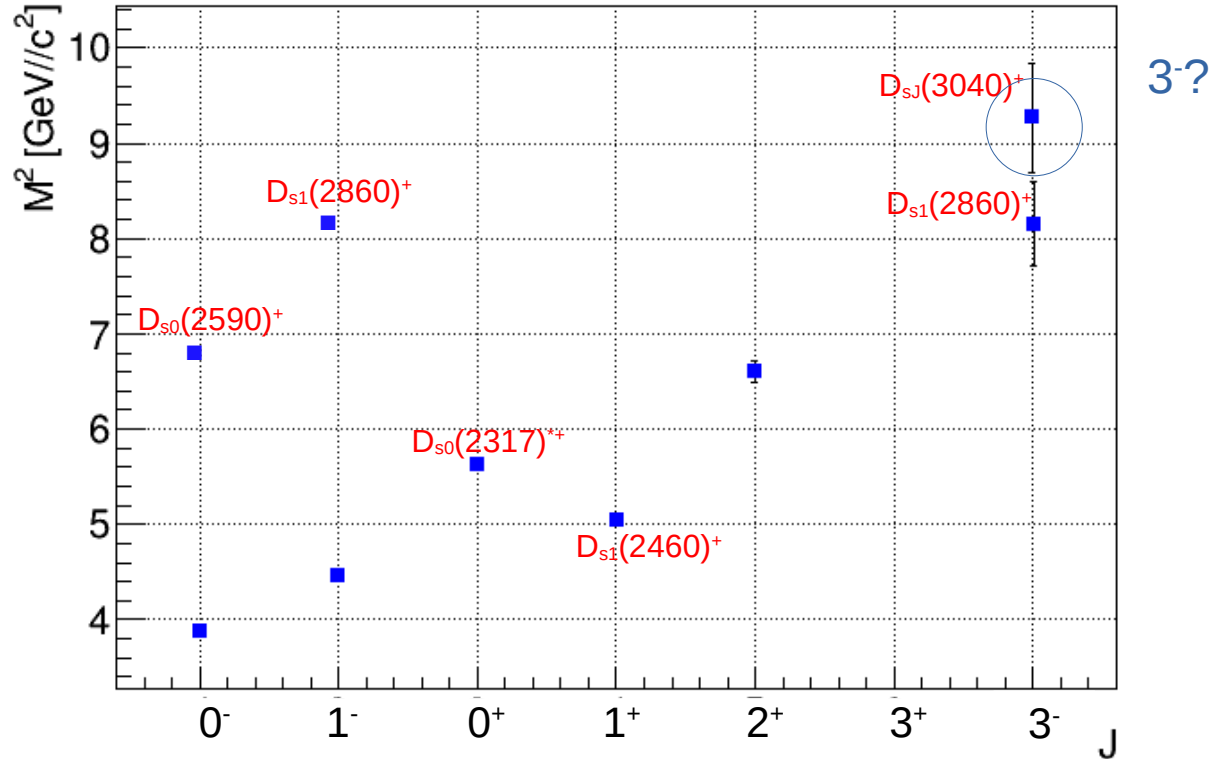
| cs meson                             | Mass (MeV/c <sup>2</sup> )        | Width (MeV) | I(J <sup>P</sup> ) | Experiment   | Match exp/theory |
|--------------------------------------|-----------------------------------|-------------|--------------------|--|------------------|
| D <sub>s</sub> <sup>+</sup>          | 1968.35±0.07                      |             | 0(0 <sup>-</sup> ) | MRK3, CLEO, etc.   | ✓                |
| D <sub>s</sub> <sup>*+</sup>         | 2112.2±0.4                        | < 1.9       | 0(? <sup>?</sup> ) | MRK3   | ✓                |
| D <sub>s0</sub> (2317) <sup>*+</sup> | 2371.8±0.5                        | < 3.8       | 0(0 <sup>+</sup> ) |         | ✗                |
| D <sub>s1</sub> (2460) <sup>+</sup>  | 2459.5±0.6                        | < 3.5       | 0(1 <sup>+</sup> ) |    | ✗                |
| D <sub>s1</sub> (2536) <sup>+</sup>  | 2535.11±0.06                      | 0.92±0.05   | 0(1 <sup>+</sup> ) |    ALEP | ✓                |
| D <sub>s1</sub> (2575) <sup>+</sup>  | 2569.1±0.5                        | 16.9±0.7    | 0(2 <sup>+</sup> ) |         | ✓                |
| D <sub>s0</sub> (2590) <sup>+</sup>  | 2591±9                            | 89±20       | 0(0 <sup>-</sup> ) |   | ✗                |
| D <sub>s1</sub> (2700) <sup>+</sup>  | 2714±5                            | 122±10      | 0(1 <sup>-</sup> ) |         | ✓                |
| D <sub>s1</sub> (2860) <sup>+</sup>  | 2859±27                           | 159±80      | 0(1 <sup>-</sup> ) |   | ✓                |
| D <sub>s3</sub> (2860) <sup>+</sup>  | 2860±7                            | 53±10       | 0(3 <sup>-</sup> ) |    | ✗                |
| D <sub>sJ</sub> (3040) <sup>+</sup>  | 3044 <sup>+31</sup> <sub>-9</sub> | 239±60      | 0(? <sup>?</sup> ) |    | ✗                |



# Remarks on $cs$ mesons

- Charged particles
- Perturbative calculations cannot explain the whole spectrum:  
 $D_{s0}(2317)^{*+}$  and  $D_{s1}(2460)^+$  are not isolated cases
- High interest in understanding the  $cs$  spectrum:  
heavy-light systems analyzed as a probe of chiral symmetry
- Analyses in the continuum at B factories offer a useful tool

# Regge trajectories for $D_s$ : an experimental view



# *Test of chiral symmetry breaking (I)*

- $D_{s0}(2317)^{*+}$  and  $D_{s1}(2460)^+$  : many different theoretical interpretations
  - pure cs mesons
  - dynamically-generated molecules
  - four-quark states
  - first chiral partners of hadrons theoretically built out of light (s) and heavy (c) quarks; etc...

they represent rather a pattern of spontaneous breakdown of chiral symmetry than isolated events!

# Test of chiral symmetry breaking (II)

- (u, d, s) **light quarks**; (c, t, b) **heavy quarks**
- **Spontaneous breaking of chiral symmetry** characterizes the light sector, while the heavy sector exhibits heavy-quark symmetry
- What happens in the **heavy-light systems**?
- Assume the limit: light quark massless, heavy quark with infinite mass  $\Rightarrow$   
the spontaneous chiral symmetry breaking yields a mass splitting of the chiral doublers of about **345 MeV/c<sup>2</sup>** (when the pion coupling to the doublers is half its coupling to a free quark)
- This mass splitting never observed in the **B<sub>s</sub> sector**  $\Rightarrow$   
this measurement in the D<sub>s</sub> sector even more intriguing
- What is the status-of-the-art in the **D<sub>s</sub> sector**?

# Study of chiral symmetry in the $D_s$

|                                |                   |
|--------------------------------|-------------------|
| $m_{D_s} - m_D$                | $98.69 \pm 0.05$  |
| $m_{D_s^*} - m_{D_s}$          | $143.8 \pm 0.4$   |
| $m_{D_{s0}(2317)^*} - m_{D_s}$ | $349.4 \pm 0.5$   |
| $m_{D_{s1}(2460)} - m_{D_s^*}$ | $347.3 \pm 0.7$   |
| $m_{D_{s1}(2460)} - m_{D_s}$   | $481.1 \pm 0.6$   |
| $m_{D_{s1}(2536)} - m_{D_s^*}$ | $422.9 \pm 0.4$   |
| $m_{D_{s1}(2536)} - m_{D^*}$   | $524.85 \pm 0.04$ |
| $m_{D_{s1}(2536)} - m_{D_0^*}$ | $528.26 \pm 0.05$ |
| $m_{D_{s2}(2575)} - m_{D_0}$   | $704.0 \pm 3.2$   |

From PDG 2023

# Study of the $c\bar{c}s\bar{s}$ resonances

- Proposal shown at HIRSGHEGG2018 (DFG project <https://gepris.dfg.de/gepris/person/324081743>):

| Physics process under study  | Mass Range [GeV/c <sup>2</sup> ] |
|--|----------------------------------|
| $B \rightarrow J/\psi\phi K$   | [4.117-4.78]                     |
| Analysis in the continuum: $e^+e^- \rightarrow D_s D_{sJ}^{(*)} A$ ,<br>$e^+e^- \rightarrow J/\psi\phi A$ , $A = \text{anything else}$<br>( $D_{sJ}^{(*)} = D_{s0}(2317)/D_{s1}(2460)$ ) | [4.117-6.765]                    |
| $B_s \rightarrow D_s^{(*)} D_{sJ}^{(*)} \pi^0$   |                                  |
| ISR: $e^+e^- \rightarrow \gamma_{\text{ISR}} D_s D_{sJ}^{(*)}$   |                                  |

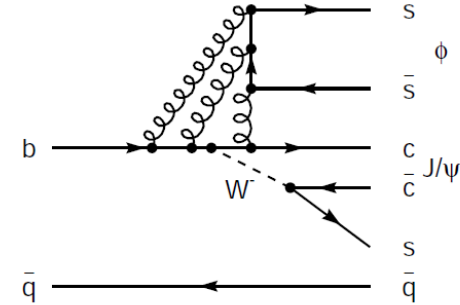
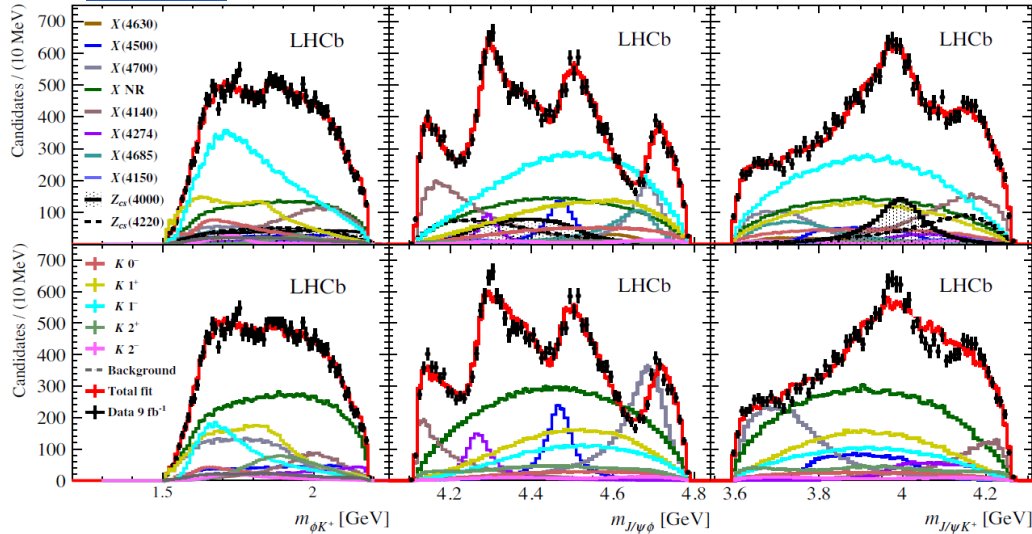
- Many possibilities, in 2018 almost nothing explored!

# $B \rightarrow J/\psi \phi K$



Phys. Rev. Lett. 127 (2021) 082001

$B^+ \rightarrow J/\psi \phi K^+$



Full amplitude analysis!

# $B \rightarrow J/\psi\phi K$

A. Thampi, PhD (2021), Belle

<https://hss-opus.ub.ruhr-uni-bochum.de/opus4/frontdoor/deliver/index/docId/8685/file/diss.pdf>

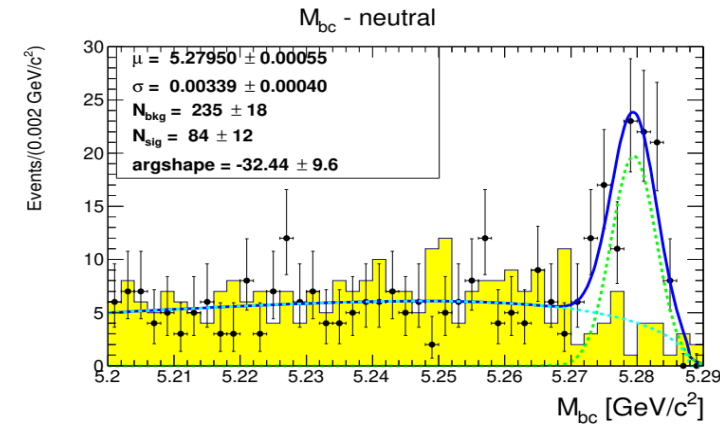
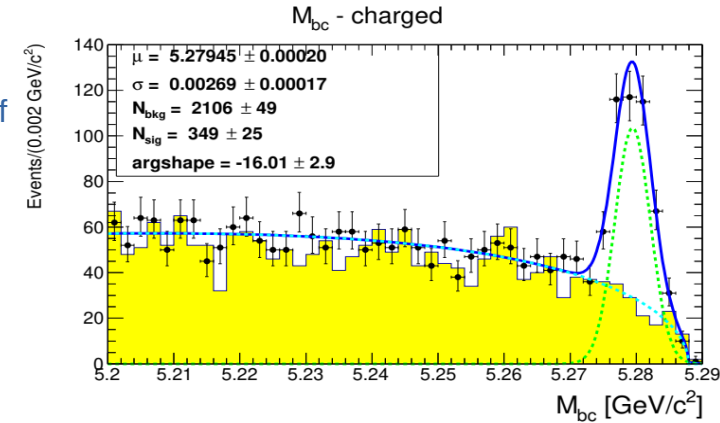
$B^\pm \rightarrow J/\psi\phi K^\pm$ ,  $J/\psi \rightarrow e^+e^-$  or  $\mu^+\mu^-$ ,  $\phi \rightarrow K^+K^-$   
 $B^0 \rightarrow J/\psi\phi K_S^0$ ,  $J/\psi \rightarrow e^+e^-$  or  $\mu^+\mu^-$ ,  $\phi \rightarrow K^+K^-$ ,  $K_S^0 \rightarrow \pi^+\pi^-$

| Mode                                 | Efficiency, $\epsilon$ (%) | $\mathcal{BF}$ ( $\times 10^{-5}$ ) | PDG value ( $\times 10^{-5}$ ) | Ratio( $B^0/B^\pm$ )     |
|--------------------------------------|----------------------------|-------------------------------------|--------------------------------|--------------------------|
| $B^\pm \rightarrow J/\psi\phi K^\pm$ | $17.87 \pm 0.09$           | $4.35 \pm 0.31 \pm 0.19$            | $5.0 \pm 0.4$                  | $0.48 \pm 0.10 \pm 0.04$ |
| $B^0 \rightarrow J/\psi\phi K_S^0$   | $8.94 \pm 0.09$            | $2.10 \pm 0.30 \pm 0.07$            | $2.4 \pm 0.5$                  |                          |

Excellent agreement with former BaBar analysis,  
 PRD 91 (2015) 012003 and PDG.

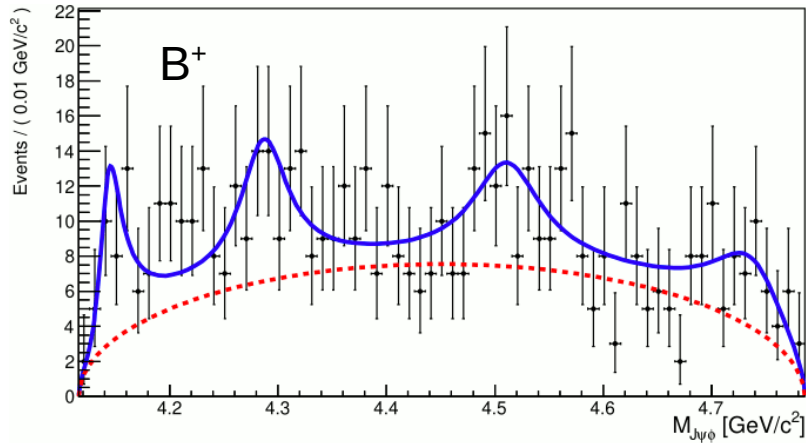
01/08/24

Elisabetta Prencipe - Hirscheegg 2024

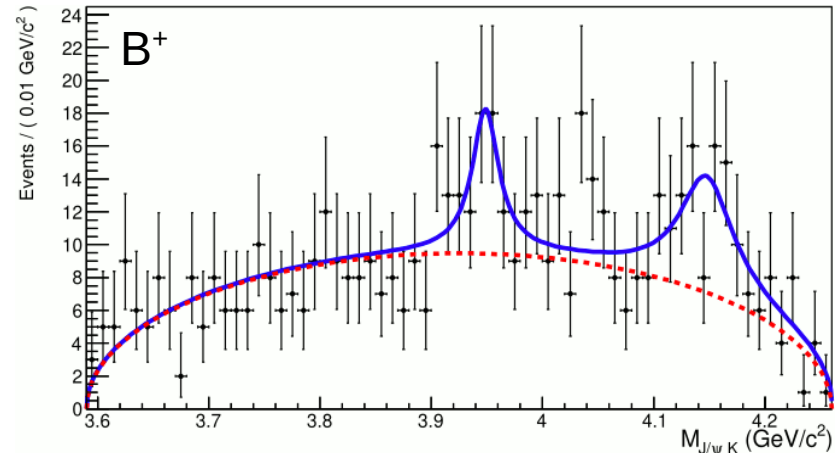
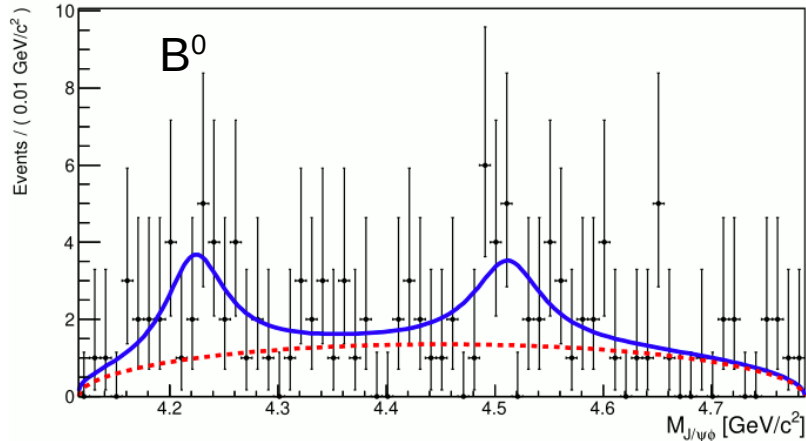




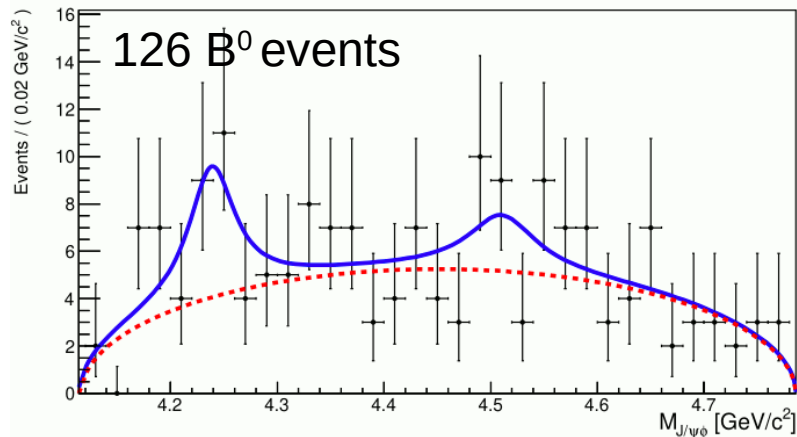
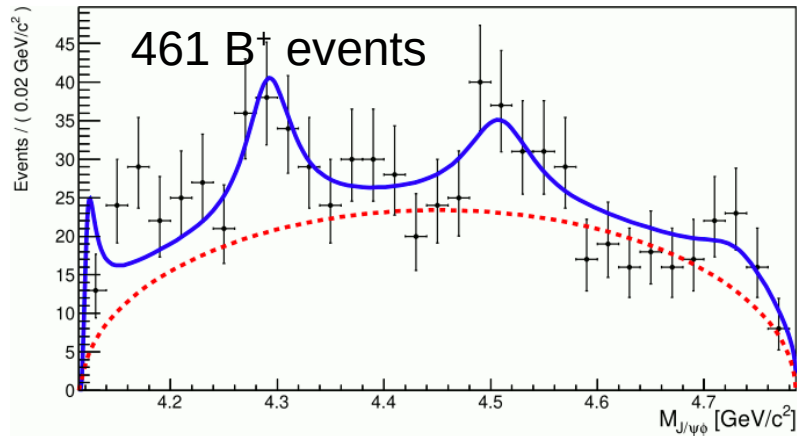
- Main issue found with efficiency: not smooth (problem see in BaBar and Belle data)
- *pdf function* corrected for the efficiency
- Limited statistics: need to perform a full amplitude analysis with full Belle II data



Belle



# Combining BaBar and Belle data



My homework:

BaBar: Phys.Rev.D 91 (2015) 012003

Belle: <https://hss-opus.ub.ruhr-uni-bochum.de/opus4/frontdoor/deliver/index/docId/8685/file/diss.pdf>  
(Ashish Thampi PhD thesis)

Fit parameters for the X(4140) fixed to:  
PRL 127 (2021) 082001

Total luminosity: 711 (BaBar) + 424 (Belle) =  
1135  $\text{fb}^{-1}$

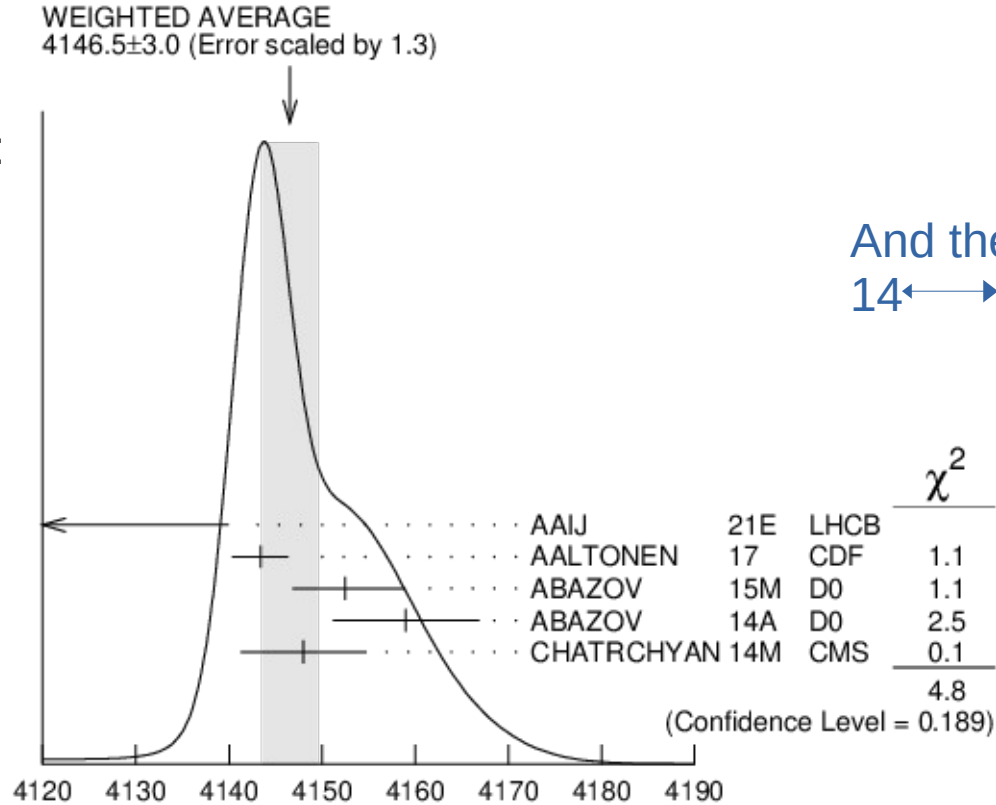
Total  $B^+$ : 461 events

Total  $B^0$ : 126 events

*Full amplitude analysis will be performed with Belle II*

# The infinite saga of the X(4140)

From PDG 2023:

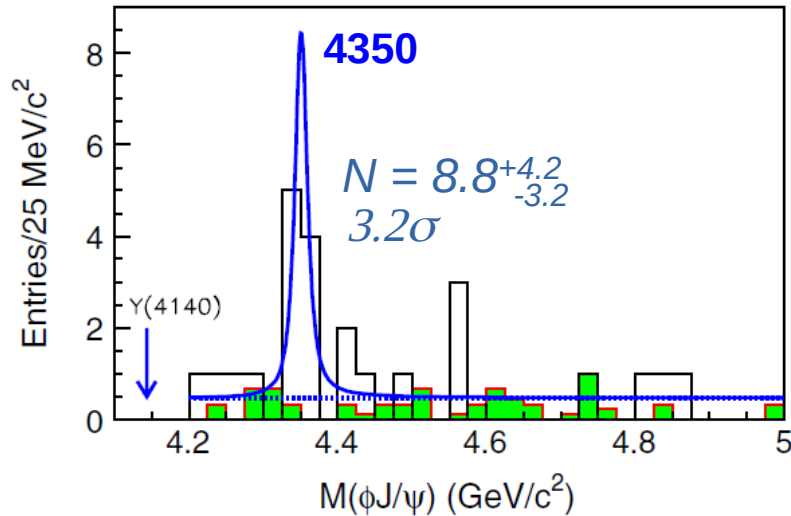


And the width?

$14 \longleftrightarrow 162$  MeV...

# Study of $J/\psi\phi$ via two-photon interaction at Belle

$J/\psi\phi$ , PRL 104 (2010) 112004



- 825 fb<sup>-1</sup> integrated luminosity (Belle)

$$M = [4350.6^{+4.6}_{-4.6}(\text{stat}) \pm 0.7(\text{syst})] \text{ MeV}/c^2$$
$$\Gamma = [13^{+18}_{-9}(\text{stat}) \pm 4(\text{syst})] \text{ MeV}$$

- Need to repeat the analysis with full Belle II data

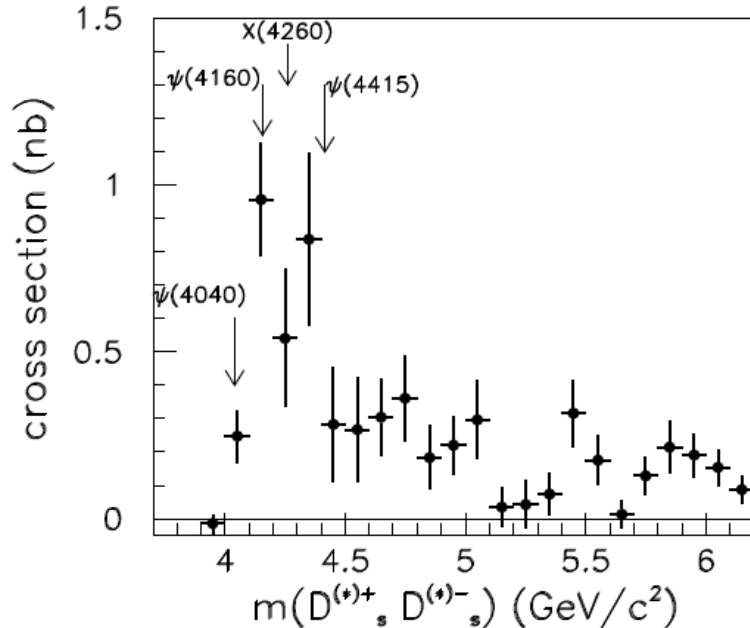
Today we know that for X(4140)  $J^{PC} = 1^{++}$   
But what is the X(4350), if confirmed?

- X(4350) mass consistent with predicted  $\bar{c}c\bar{s}s$  tetraquark (J. Phys. G37 (2010) 075017)
- Compatibility with  $D_s^{*+}D_{s0}^{*-}(2317)^-$  molecule state (prediction: CTP 54 (2010) 1075)
- Compatibility with possible  $\chi''_{c2}$  charmonium state (prediction: PRL 104 (2010) 122001)

# $c\bar{c}s\bar{s}$ search via ISR

Analyzing  $e^+e^- \rightarrow D_s^+ D_s^-$ ,  $e^+e^- \rightarrow D_s^{*+} D_s^-$ ,  $e^+e^- \rightarrow D_s^{*+} D_s^{*-}$  via **ISR** BaBar looked for the  $Y(4260)$

Phys .Rev. D82 (2010) 052004



$$\frac{B(Y(4260) \rightarrow D_s^+ D_s^-)}{B(Y(4260) \rightarrow J/\psi \pi^+ \pi^-)} < 0.7,$$

$$\frac{B(Y(4260) \rightarrow D_s^{*+} D_s^-)}{B(Y(4260) \rightarrow J/\psi \pi^+ \pi^-)} < 44,$$

$$\frac{B(Y(4260) \rightarrow D_s^{*+} D_s^{*-})}{B(Y(4260) \rightarrow J/\psi \pi^+ \pi^-)} < 30.$$

If  $Y(4260)$  is  $1^-$  **charmonium state**, it should decay mostly to open charm

If  $Y(4260)$  is a **tetraquark**, it should decay to  $D_s^- D_s^+$

01/08

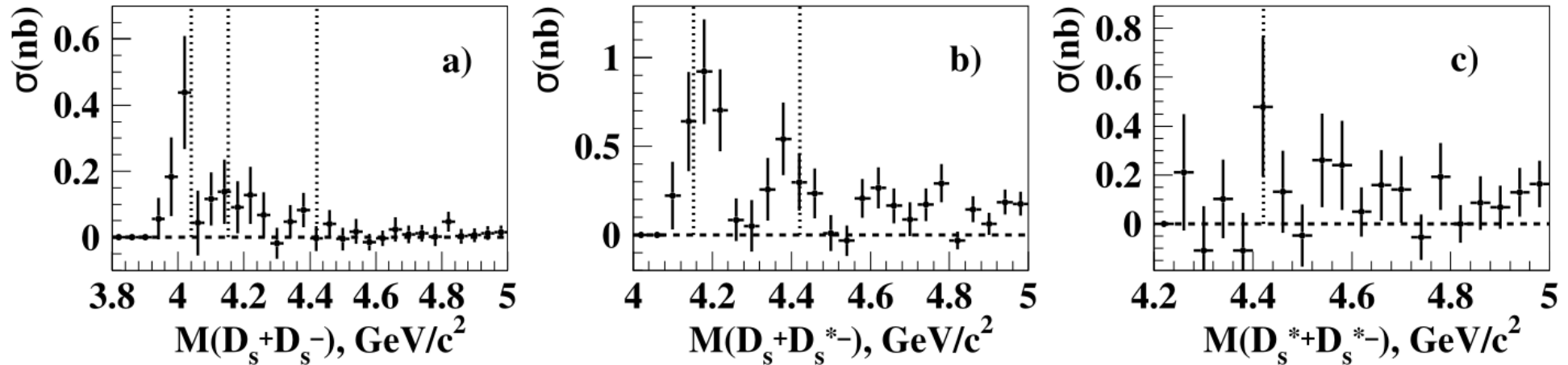
it does not happen @95%c.l. with  $525 \text{ fb}^{-1}$  (BaBar data set)!

37

# $c\bar{c}s\bar{s}$ search via ISR at Belle

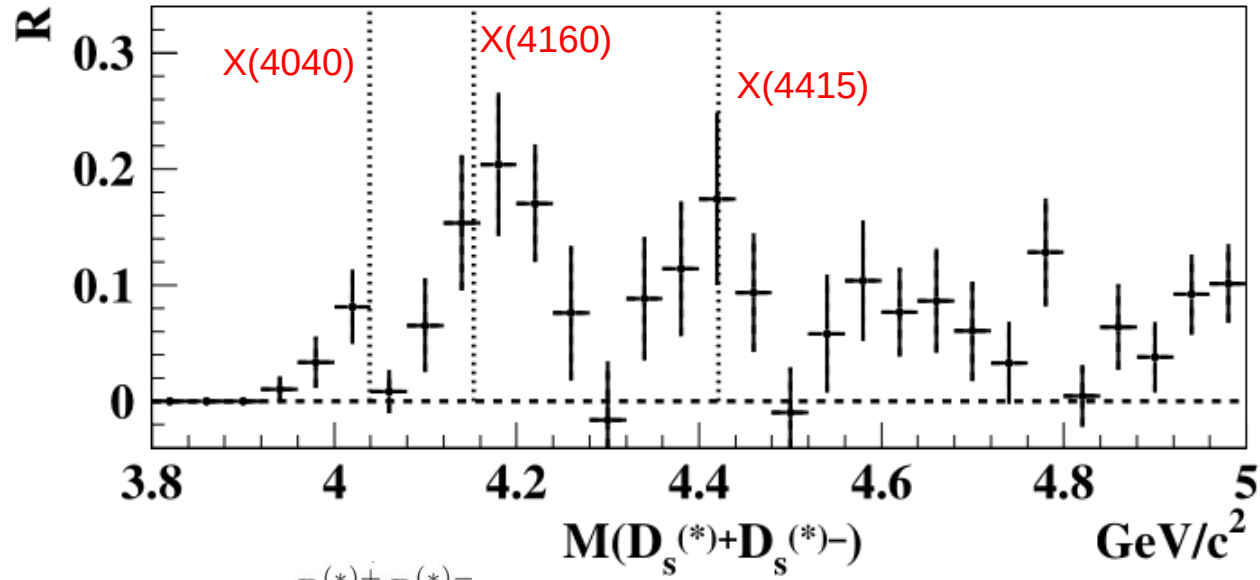
PRD 83 (2011) 011101

Found evidence for the  $X(4040)$ ,  $X(4160)$  and  $X(4415)$   
Integrated luminosity:  $967 \text{ fb}^{-1}$



# $c\bar{c}s\bar{s}$ search via ISR at Belle

PRD 83 (2011) 011101



$R = \sigma(e^+e^- \rightarrow \text{hadrons}) / \sigma(e^+e^- \rightarrow \mu^+\mu^-)$

$\sigma(e^+e^- \rightarrow \mu^+\mu^-) = 4\pi\alpha^2/3s$

$D_s^{(*)+} D_s^{(*)-}$

More data are needed!  
Belle II will help to solve the puzzle



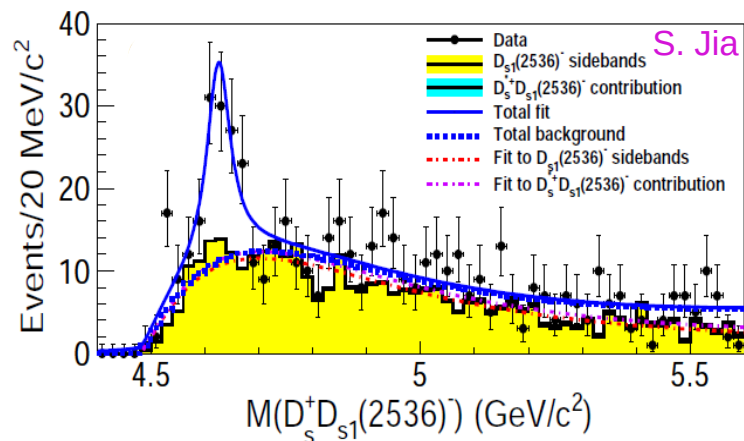
Need to look at the  $D_s^{(*)}D_{sJ}^{(*)}$  invariant mass!

**Belle and Belle II:**  
excellent calorimeter performance to detect low energy  
photons (down 48 MeV/c),  
essential ingredient for the analysis of the  $D_{sJ}$  resonant  
states below the DK threshold

ISR physics, two-photon interactions and continuum:  
unique physics cases at  $e^+e^-$  detectors



# Results in ISR at Belle: $X \rightarrow D_s^+ D_{s1}(2536)^-$



$e^+e^- \rightarrow D_s^+ D_{s1}(2536)^-$  via ISR

First observation of the  $Y(4620)$

$J^{PC} = 1^{--}$

compatible with  $Y(4660)$

$5.9\sigma$  significance

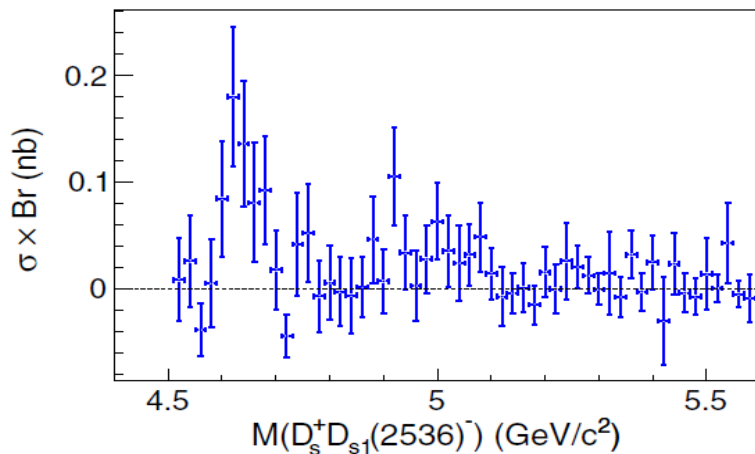
Luminosity:  $921.9 \text{ fb}^{-1}$

PRD 100 (2019) 111103

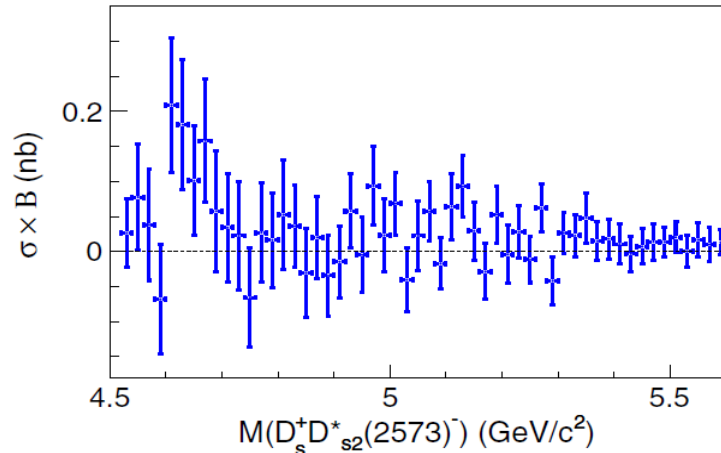
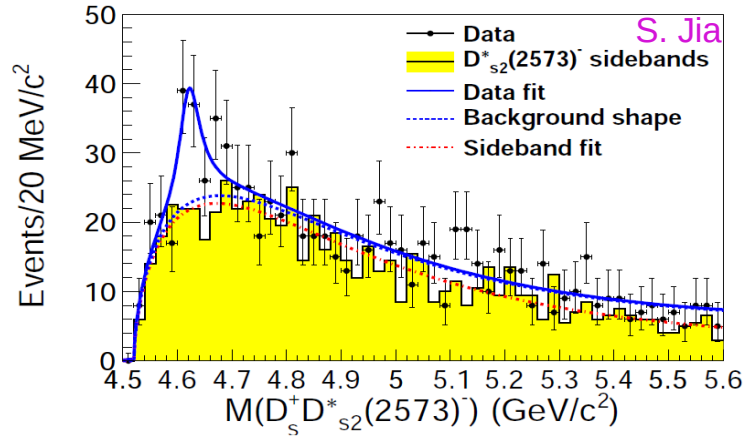
$$M = (4625.9_{-6.0}^{+6.2}(\text{stat}) \pm 0.4(\text{syst})) \text{ MeV}/c^2$$

$$\Gamma = (49.8_{-11.5}^{+13.9}(\text{stat}) \pm 4.0(\text{syst})) \text{ MeV}$$

$$\begin{aligned} \Gamma_{ee} \times \mathcal{B}(Y(4626) \rightarrow D_s^+ D_{s1}(2536)^-) \times \mathcal{B}(D_{s1}(2536)^- \rightarrow \bar{D}^{*0} K^-) \\ = (14.3_{-2.6}^{+2.8}(\text{stat}) \pm 1.5(\text{syst})) \text{ eV} \end{aligned}$$



# Results in ISR at Belle: $X \rightarrow D_s^+ D_{s1}(2573)^-$



$e^+e^- \rightarrow D_s^+ D_{s2}^*(2573)^-$  via ISR

Evidence of the  $Y(4620)$

$JPC = 1^{--}$

compatible with  $Y(4660)$

$3.4\sigma$  significance

Luminosity:  $921.9 \text{ fb}^{-1}$

PRD 101 (2020) 091101

$$M = (4619.8_{-8.0}^{+8.9}(\text{stat.}) \pm 2.3(\text{syst.})) \text{ MeV}/c^2$$

$$\Gamma = (47.0_{-14.8}^{+31.3}(\text{stat.}) \pm 4.6(\text{syst.})) \text{ MeV}$$

$$\Gamma_{ee} \times \mathcal{B}(Y(4620) \rightarrow D_s^+ D_{s2}^*(2573)^-) \times \mathcal{B}(D_{s2}^*(2573)^- \rightarrow \bar{D}^0 K^-)$$

$$(14.7_{-4.5}^{+5.9}(\text{stat.}) \pm 3.6(\text{syst.})) \text{ eV}$$

# *Analysis in the continuum to search for $c\bar{c}s\bar{s}$ resonant states*

- Too little is known
- Huge background, but higher efficiency
- Analyze the invariant mass on the recoil of anything else
- High potential discovery

# Observation of $cs$ meson pair production in $\Upsilon(2S)$ at Belle

PRD 108 (2023) 112015

Data set: 24.7 fb<sup>-1</sup> @  $\Upsilon(2S)$

$$\mathcal{B}(\Upsilon(2S) \rightarrow D_c^+ D_{c1}(2536)^-) \mathcal{B}(D_{c1}(2536)^- \rightarrow K^- D^*(2007)^0) = (1.6 \pm 0.3 \pm 0.2) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow D_s^{*+} D_{s1}(2536)^-) \mathcal{B}(D_{s1}(2536)^- \rightarrow K^- D^*(2007)^0) = (1.4 \pm 0.4 \pm 0.2) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow D_s^+ D_{s2}^*(2573)^-) \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K^- D^0) = (1.4 \pm 0.4 \pm 0.2) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow D_s^{*+} D_{s2}^*(2573)^-) \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K^- D^0) = (0.9 \pm 0.5 \pm 0.2) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow D_s^+ D_{s1}(2536)^-) \mathcal{B}(D_{s1}(2536)^- \rightarrow K_S^0 D^*(2010)^-) = (0.84 \pm 0.18 \pm 0.15) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow D_s^{*+} D_{s1}(2536)^-) \mathcal{B}(D_{s1}(2536)^- \rightarrow K_S^0 D^*(2010)^-) = (0.82 \pm 0.25 \pm 0.19) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow D_s^+ D_{s2}^*(2573)^-) \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K_S^0 D^-) = (0.69 \pm 0.20 \pm 0.22) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow D_s^{*+} D_{s2}^*(2573)^-) \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K_S^0 D^-) = (0.54 \pm 0.31 \pm 0.47) \times 10^{-5}$$

# Observation of $cs$ meson pair production in $\Upsilon(2S)$ at Belle

PRD 108 (2023) 112015

Data set: 24.7 fb-1 @  $\Upsilon(2S)$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_c^+ D_{c1}(2536)^-) \mathcal{B}(D_{c1}(2536)^- \rightarrow K^- D^*(2007)^0) = (67 \pm 8 \pm 6) \text{ fb}$$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_s^{*+} D_{s1}(2536)^-) \mathcal{B}(D_{s1}(2536)^- \rightarrow K^- D^*(2007)^0) = (84 \pm 11 \pm 11) \text{ fb}$$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_s^+ D_{s2}^*(2573)^-) \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K^- D^0) = (56 \pm 9 \pm 13) \text{ fb}$$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_s^{*+} D_{s2}^*(2573)^-) \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K^- D^0) = (106 \pm 17 \pm 12) \text{ fb}$$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_c^+ D_{c1}(2536)^-) \mathcal{B}(D_{c1}(2536)^- \rightarrow K_c^0 D^*(2010)^-) = (34 \pm 5 \pm 4) \text{ fb}$$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_s^{*+} D_{s1}(2536)^-) \mathcal{B}(D_{s1}(2536)^- \rightarrow K_S^0 D^*(2010)^-) = (41 \pm 6 \pm 6) \text{ fb}$$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_s^+ D_{s2}^*(2573)^-) \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K_S^0 D^-) = (27 \pm 6 \pm 5) \text{ fb}$$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_s^{*+} D_{s2}^*(2573)^-) \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K_S^0 D^-) = (51 \pm 11 \pm 9) \text{ fb}$$

Recall:  $\sigma^{\text{Born}}(e^+e^- \rightarrow \mu^+\mu^-) = 0.784 \text{ nb}$  @10.52 GeV

# Observation of $cs$ meson pair production in $\Upsilon(2S)$ at Belle

PRD 108 (2023) 112015

Data set: 24.7 fb<sup>-1</sup> @  $\Upsilon(2S)$

$$\sigma^{\text{Born}}(e^+e^- \rightarrow D_s^{(*)+} D_{sJ}^-) / \sigma^{\text{Born}}(e^+e^- \rightarrow \mu^+ \mu^-) \left\{ \begin{array}{ll} 9.7 \pm 2.3 \pm 1.1 & D_s^+ D_{s1}(2536)^- \\ 6.8 \pm 2.1 \pm 0.8 & D_s^{*+} D_{s1}(2536)^- \\ 10.2 \pm 3.3 \pm 2.5 & D_s^+ D_{s2}^*(2573)^- \\ 3.4 \pm 2.1 \pm 0.8 & D_s^{*+} D_{s2}^*(2573)^- \end{array} \right.$$

 Strong decays dominate in the  $\Upsilon(2S) \rightarrow D_s^{(*)+} D_{sJ}^-$  process

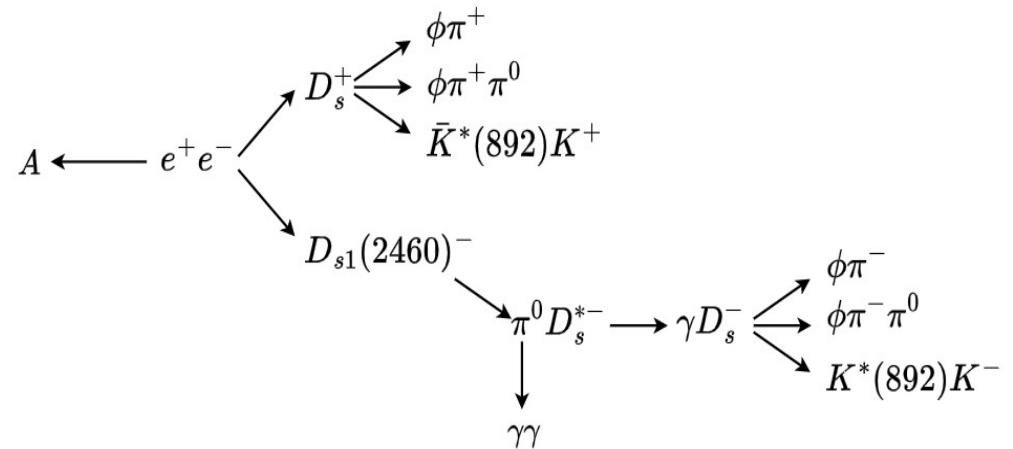
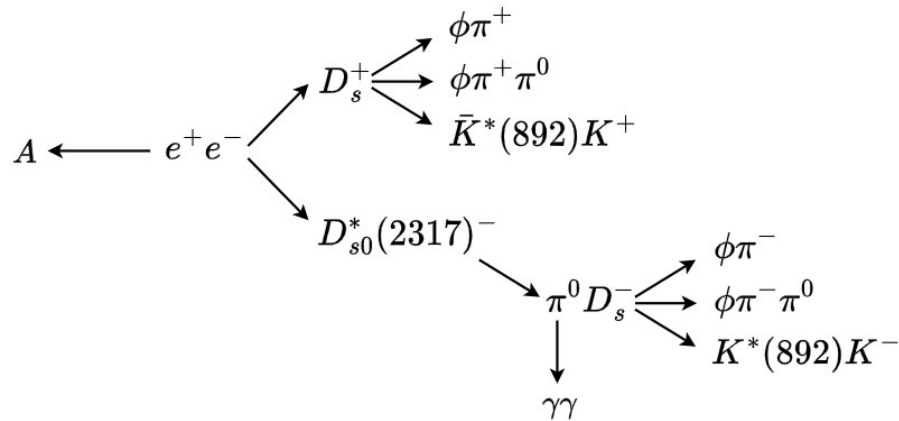
$$\mathcal{B}(D_{s1}(2536)^- \rightarrow K_S^0 D^*(2010)^-) / \mathcal{B}(D_{s1}(2536)^- \rightarrow K^- D^*(2007)^0) = 0.48 \pm 0.07 \pm 0.02$$

$$\mathcal{B}(D_{s2}^*(2573)^- \rightarrow K_S^0 D^-) / \mathcal{B}(D_{s2}^*(2573)^- \rightarrow K^- D^0) = 0.49 \pm 0.10 \pm 0.02. \text{ First measurement}$$

 Isospin symmetry

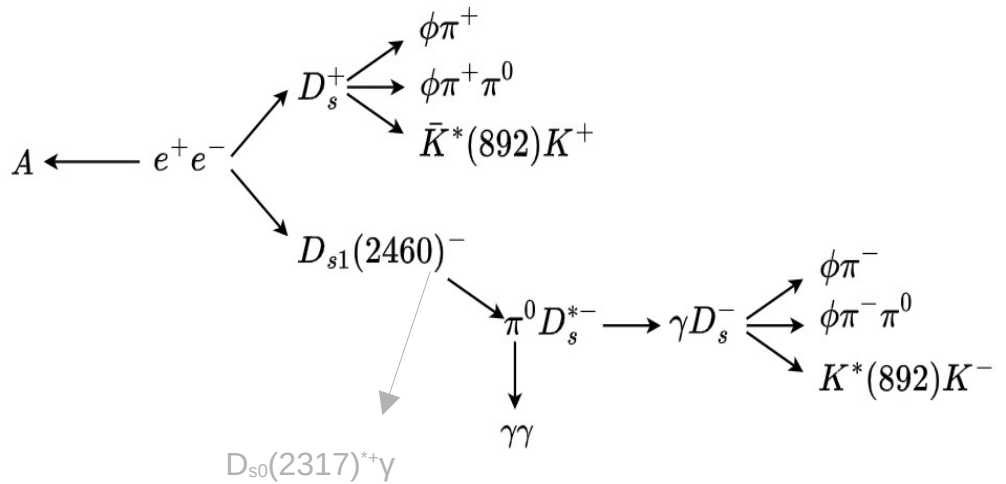
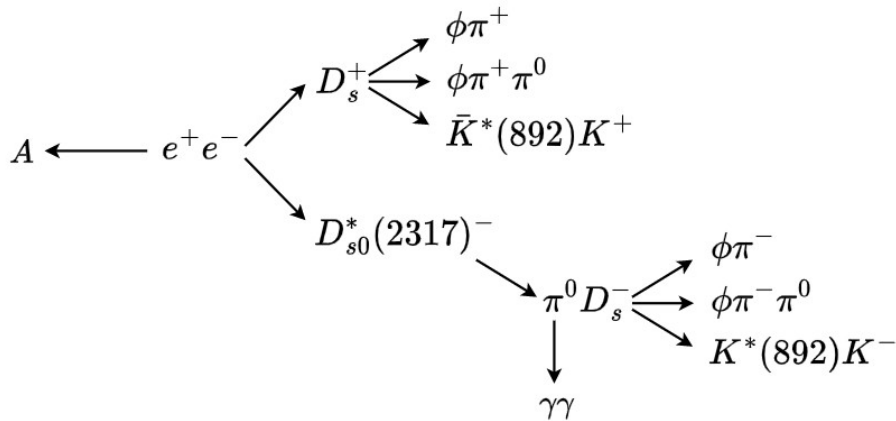
# Study of the $e^+e^- \rightarrow D_s^+ D_{s0}(2317)^{-} A$ and $e^+e^- \rightarrow D_s^+ D_{s1}(2460)^{-} A$ in the continuum at Belle

FIRST MEASUREMENT  
PRELIMINARY



# Study of the $e^+e^- \rightarrow D_s^+ D_{s0}(2317)^* A$ and $e^+e^- \rightarrow D_s^+ D_{s1}(2460) A$ in the continuum at Belle

FIRST MEASUREMENT  
PRELIMINARY



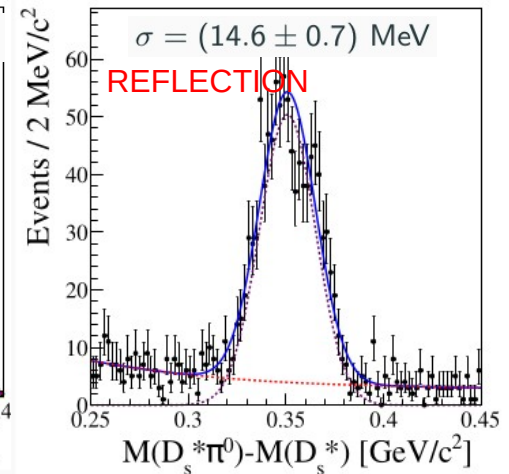
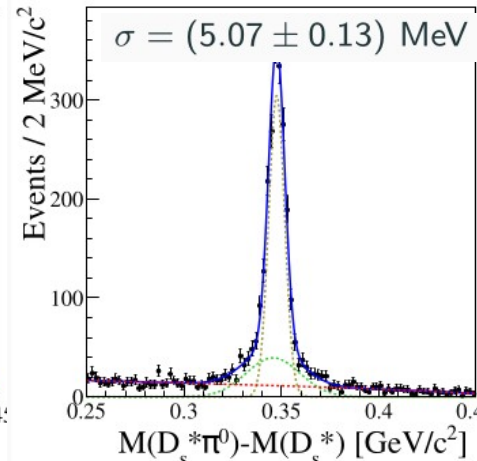
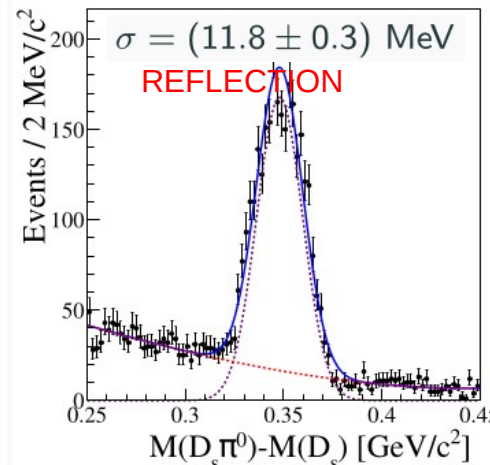
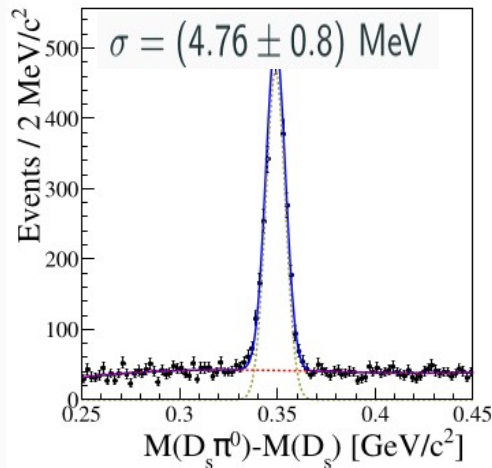


# Study of the $e^+e^- \rightarrow D_s^+ D_{s0}(2317)^- A$ and $e^+e^- \rightarrow D_s^+ D_{s1}(2460)^- A$ in the continuum at Belle

FIRST MEASUREMENT  
PRELIMINARY

- Complicated cross-feed background to study
- Poor knowledge from theory: MC model not appropriate
- Still limited statistics with Belle, but...

## SIGNAL MC



01/08/24

Elisabetta Prencipe - Frascati 2024

# Study of the $e^+e^- \rightarrow D_s^+ D_{s0}(2317)^- A$ and $e^+e^- \rightarrow D_s^+ D_{s1}(2460)^- A$ in the continuum at Belle

FIRST MEASUREMENT  
PRELIMINARY

| Topology type                | $\mu$ , [MeV]   | $\sigma$ , [MeV] | N                  |
|------------------------------|-----------------|------------------|--------------------|
| True $D_{s0}^*(2317)$ signal | $349.3 \pm 0.2$ | $5.97 \pm 0.25$  | $3,797 \pm 137$    |
| Feed-down background         | 345.1 (fixed)   | 13.5 (fixed)     | $0.3297 \cdot N_2$ |
| True $D_{s1}(2460)$ signal   | $347.1 \pm 0.5$ | $5.46 \pm 0.60$  | $811 \pm 155$      |
| Feed-up background           | 352.0 (fixed)   | 13.9 (fixed)     | $3.042 \cdot N_1$  |
| $D_{s1}(2460)$               | 346.7 (fixed)   | 22.7 (fixed)     | $1.189 \cdot N_2$  |

$$N_1 = 3,843 \pm 67, \mu = 348.9 \pm 0.1, \sigma = 6.20 \pm 0.10$$

$$N_2 = 835 \pm 31, \mu = 347.1 \pm 0.2, \sigma = 5.80 \pm 0.20$$

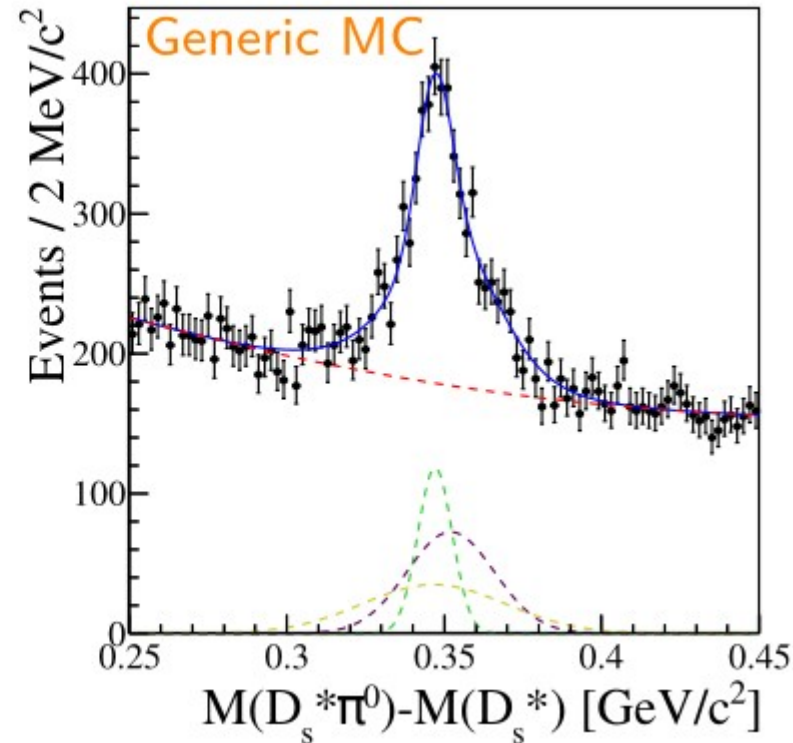
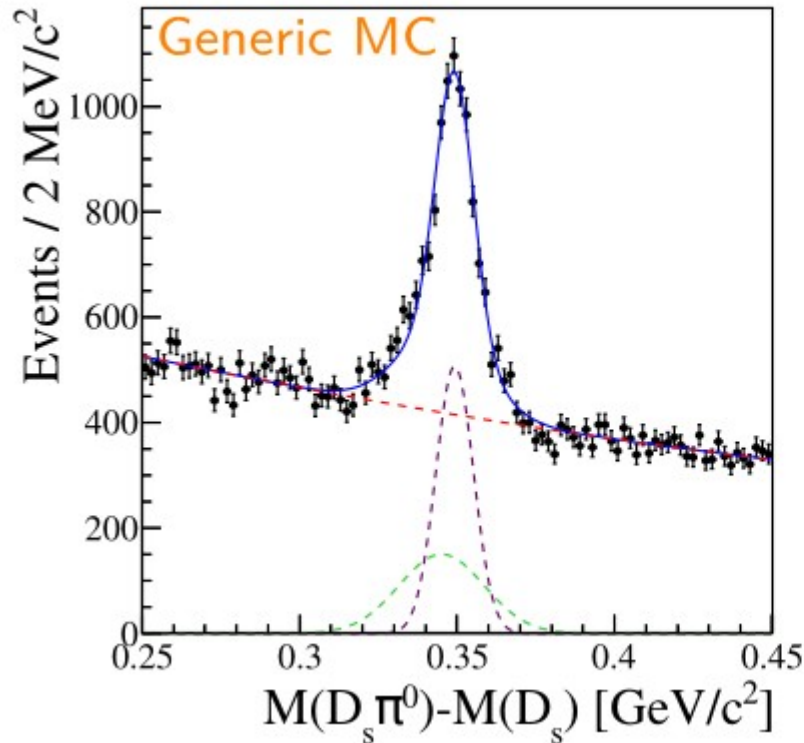
Fit functions:

$$\Delta M(D_s \pi^0) = N_1 G(\mu_1, \sigma_1) + f^{\text{down}} N_2 G(\mu^{\text{down}}, \sigma^{\text{down}})$$

$$\Delta M(D_s^* \pi^0) = N_2 G(\mu_2, \sigma_2) + f^{\text{up}} N_1 G(\mu^{\text{up}}, \sigma^{\text{up}}) + f^{\text{broken}} N_2 G(\mu^{\text{broken}}, \sigma^{\text{broken}})$$

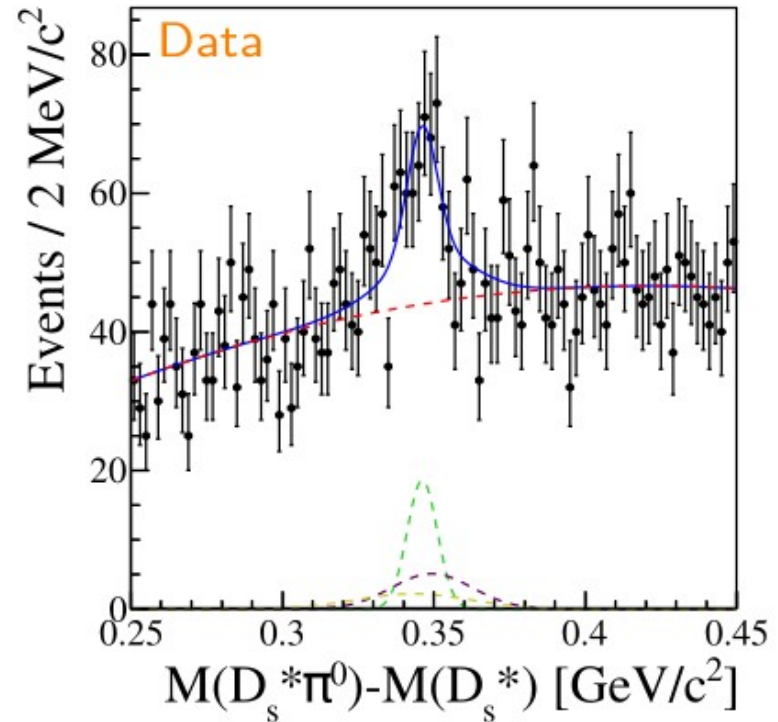
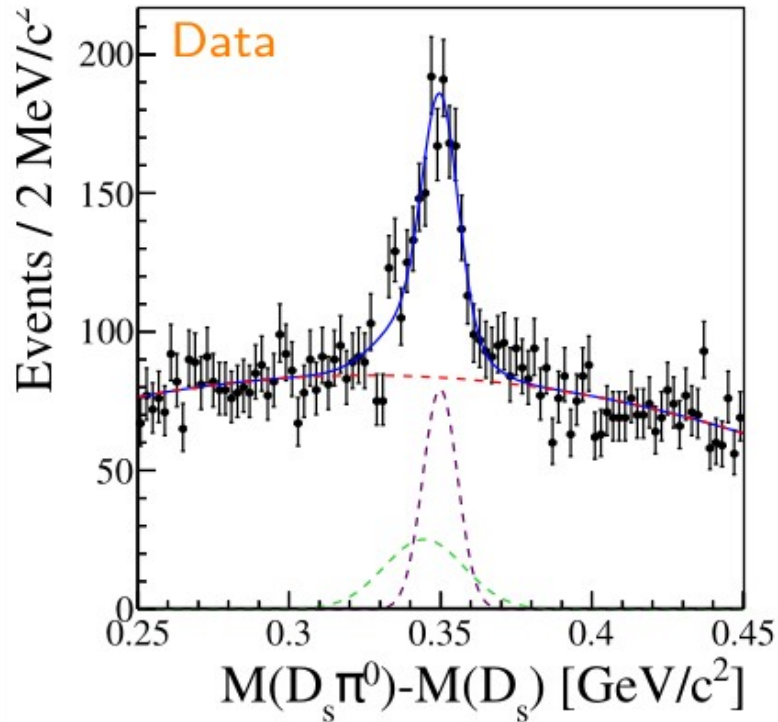
# Study of the $e^+e^- \rightarrow D_s^+ D_{s0}(2317)^- A$ and $e^+e^- \rightarrow D_s^+ D_{s1}(2460)^- A$ in the continuum at Belle

FIRST MEASUREMENT  
PRELIMINARY



# Study of the $e^+e^- \rightarrow D_s^+ D_{s0}(2317)^- A$ and $e^+e^- \rightarrow D_s^+ D_{s1}(2460)^- A$ in the continuum at Belle

FIRST MEASUREMENT  
PRELIMINARY



# Study of the $e^+e^- \rightarrow D_s^+ D_{s0}(2317)^- A$ and $e^+e^- \rightarrow D_s^+ D_{s1}(2460)^- A$ at Belle

FIRST MEASUREMENT  
PRELIMINARY

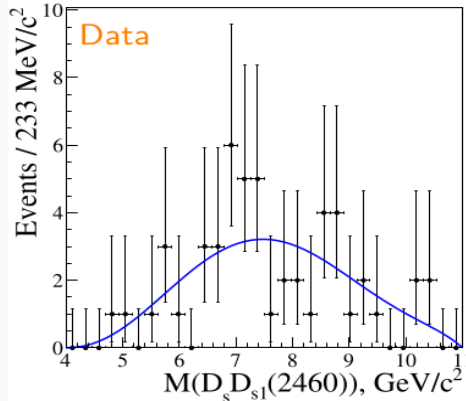
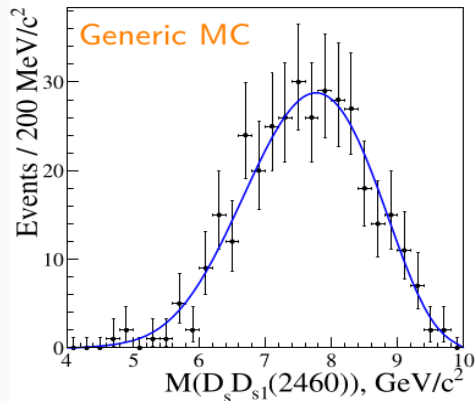
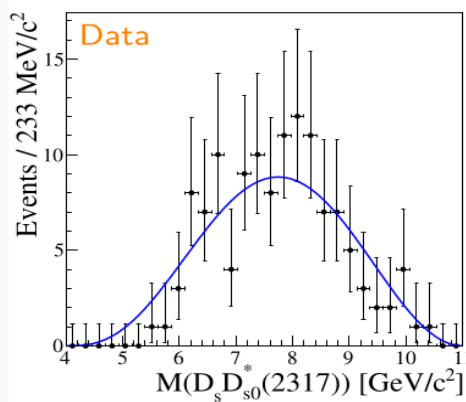
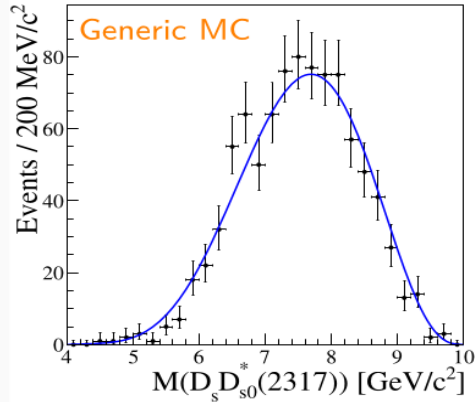
DATA

| Topology type                | $\mu$ , [MeV]   | $\sigma$ , [MeV] | N                 |
|------------------------------|-----------------|------------------|-------------------|
| True $D_{s0}^*(2317)$ signal | $349.6 \pm 0.5$ | $7.16 \pm 0.59$  | $792 \pm 62$      |
| Feed-down background         | 344.0 (fixed)   | 13.4 (fixed)     | $0.170 \cdot N_2$ |
| True $D_{s1}(2460)$ signal   | $347.3 \pm 1.8$ | $6.98 \pm 1.72$  | $137 \pm 36$      |
| Feed-up background           | 349.6 (fixed)   | 14.6 (fixed)     | $2.097 \cdot N_1$ |
| $D_{s1}(2460)$ broken signal | 345.5 (fixed)   | 17.0 (fixed)     | $0.231 \cdot N_2$ |

NN-analysis performed: a factor 2 gain compared to a cut-based analysis!

# Study of the $e^+e^- \rightarrow D_s^+ D_{s0}(2317)^- A$ and $e^+e^- \rightarrow D_s^+ D_{s1}(2460)^- A$ in the continuum at Belle

FIRST MEASUREMENT  
PRELIMINARY



No evidence for resonant states found  
up to  $980.15 \text{ fb}^{-1}$

$$\frac{Br(D_{s1}(2460) \rightarrow D_s^* \pi^0)}{Br(D_{s0}^*(2317) \rightarrow D_s \pi^0)} \times \frac{\sigma(D_{s1}(2460), p^* > 3.5 \text{ GeV}/c)}{\sigma(D_{s0}^*(2317), p^* > 3.5 \text{ GeV}/c)} =$$

$$0.33 \pm 0.09(\text{stat}) \pm 0.01(\text{syst})$$

a factor 10 lower than the theory predicts

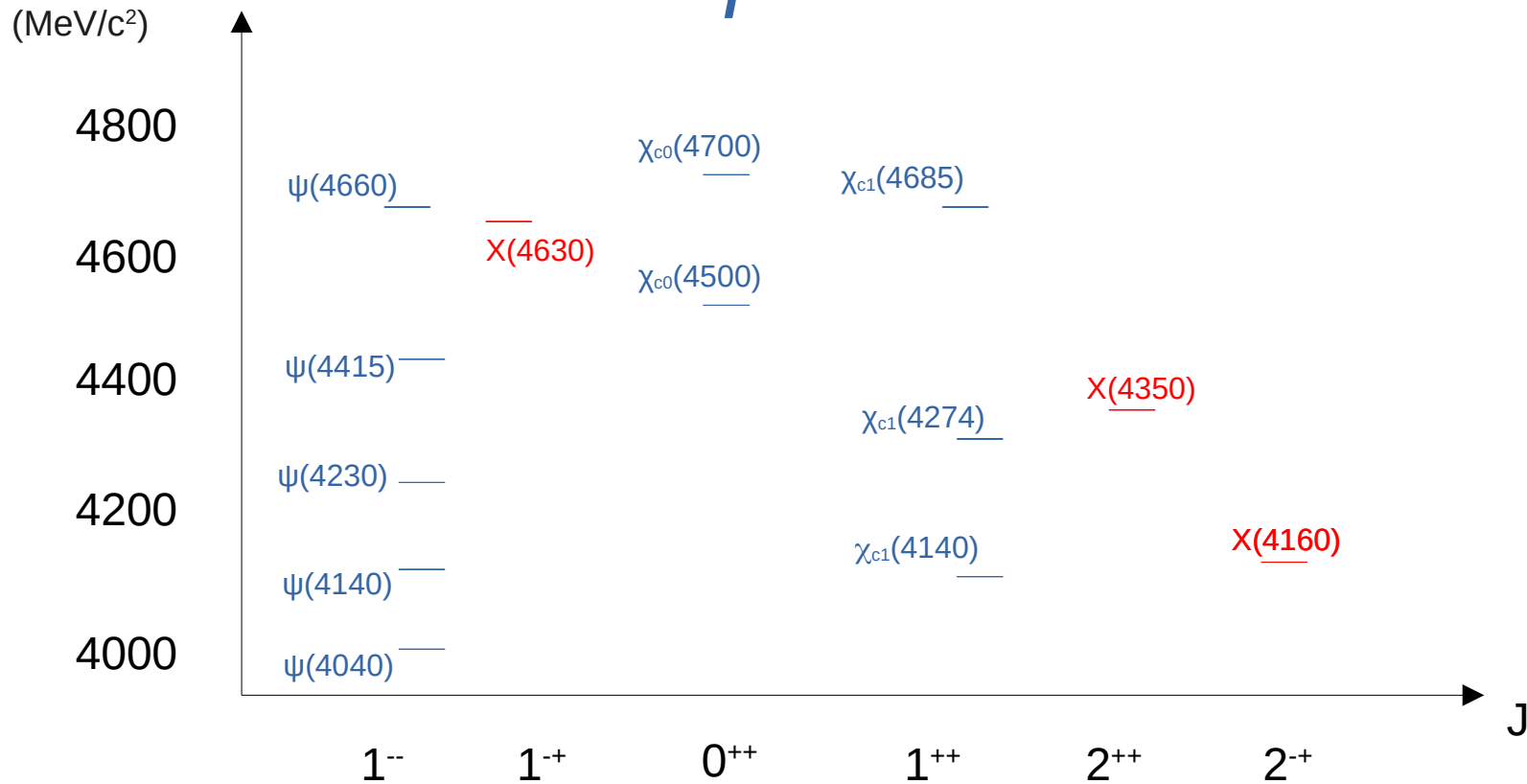
# Study of the $e^+e^- \rightarrow D_s^+D_{s0}(2317)^*A$ and $e^+e^- \rightarrow D_s^+D_{s1}(2460)A$ in the continuum at Belle

FIRST MEASUREMENT  
PRELIMINARY

Upper limits determined on the resonant states seen in  $J/\psi\phi$  mass via B decays

| Mode                          | $N^{UL}$ | Tot. err. [%] | $\sigma^{UL} \times \mathcal{B}(X \rightarrow D_s D_{sJ}^{(*)})$ [fb] |
|-------------------------------|----------|---------------|---|
| $e^+e^- \rightarrow X(4274)A$ | 2.4      | 10.1          | 99.1  |
| $e^+e^- \rightarrow X(4685)A$ | 1.9      | 11.2          | 78.1  |
| $e^+e^- \rightarrow X(4630)A$ | 1.9      | 14.9          | 153.2   |
| $e^+e^- \rightarrow X(4500)A$ | 2.3      | 14.7          | 189.3   |
| $e^+e^- \rightarrow X(4700)A$ | 2.1      | 15.3          | 171.3   |

# Summary of the $c\bar{c}s\bar{s}$ states: an experimental view





# Search for pentaquarks at Belle

# Search for a penta-quark state in $pJ/\psi$ final state from the $Y(1, 2S)$ inclusive decays at Belle

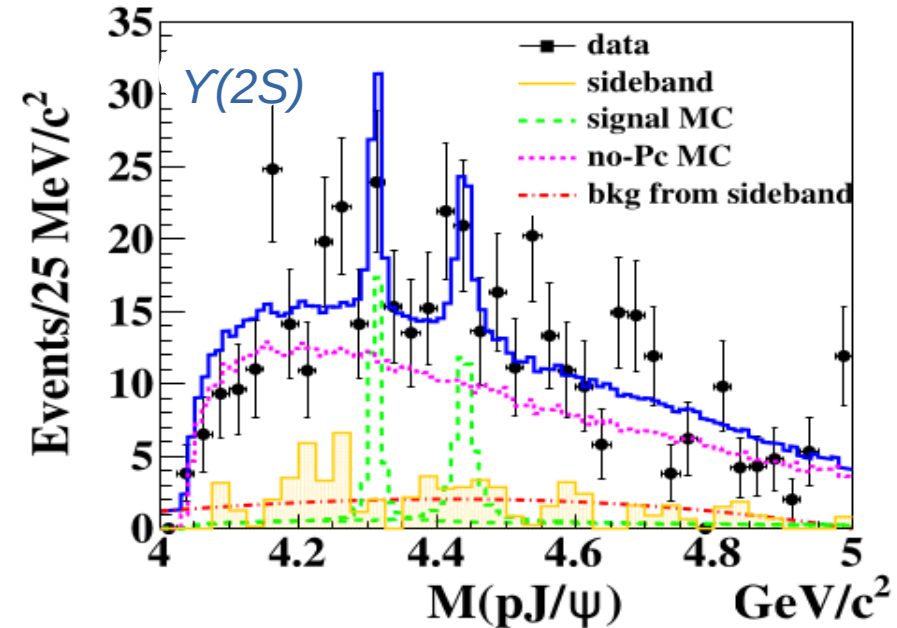
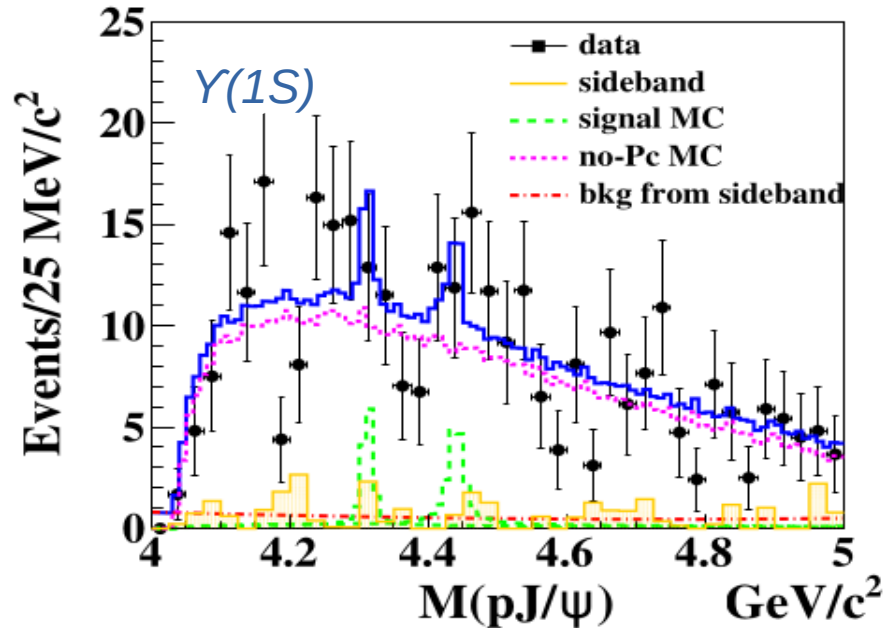
PRELIMINARY

- Total integrated luminosity used:  $Y(1S) + Y(2S) = 30.5 \text{ fb}^{-1}$
- Inclusive analysis = reconstruction of  $P_c$  candidates on the recoil of anything else
- Use also  $89 \text{ fb}^{-1}$  data @60 MeV below the  $Y(4S)$  peak → analysis in the continuum
- Eliminate Bhabha bkg and reflection peak imposing  $M^2(pJ/\psi) > 10 \text{ GeV}^2/c^4$

# Search for a penta-quark state in $pJ/\psi$ final state from the $Y(1, 2S)$ inclusive decays at Belle

PRELIMINARY

- No clear signal found for  $P_c^+(4312)$ ,  $P_c^+(4440)$ ,  $P_c^+(4457)$



# Search for a penta-quark state in $pJ/\psi$ final state from the $\Upsilon(1, 2S)$ inclusive decays at Belle

PRELIMINARY

$$\mathcal{B}[\Upsilon(1S) \rightarrow pJ/\psi + any] = (4.43 \pm 0.25 \pm 0.17) \times 10^{-5}$$

$$\mathcal{B}[\Upsilon(2S) \rightarrow pJ/\psi + any] = (3.82 \pm 0.20 \pm 0.16) \times 10^{-5}$$

$$\sigma(e^+e^- \rightarrow pJ/\psi + any) = (67 \pm 2 \pm 2) \text{ fb at } \sqrt{s} = 10.52 \text{ GeV}$$

$$\mathcal{B}^{\text{UL}}[\Upsilon(1S) \rightarrow P_c(4312)^+ + any] \cdot \mathcal{B}[P_c(4312)^+ \rightarrow pJ/\psi] < 4.5 \times 10^{-6}$$

$$\mathcal{B}^{\text{UL}}[\Upsilon(1S) \rightarrow P_c(4440)^+ + any] \cdot \mathcal{B}[P_c(4440)^+ \rightarrow pJ/\psi] < 6.8 \times 10^{-6}$$

$$\mathcal{B}^{\text{UL}}[\Upsilon(1S) \rightarrow P_c(4457)^+ + any] \cdot \mathcal{B}[P_c(4457)^+ \rightarrow pJ/\psi] < 4.9 \times 10^{-6}$$

$$\mathcal{B}^{\text{UL}}[\Upsilon(2S) \rightarrow P_c(4312)^+ + any] \cdot \mathcal{B}[P_c(4312)^+ \rightarrow pJ/\psi] < 5.3 \times 10^{-6}$$

$$\mathcal{B}^{\text{UL}}[\Upsilon(2S) \rightarrow P_c(4440)^+ + any] \cdot \mathcal{B}[P_c(4440)^+ \rightarrow pJ/\psi] < 7.2 \times 10^{-6}$$

$$\mathcal{B}^{\text{UL}}[\Upsilon(2S) \rightarrow P_c(4457)^+ + any] \cdot \mathcal{B}[P_c(4457)^+ \rightarrow pJ/\psi] < 2.4 \times 10^{-6}$$

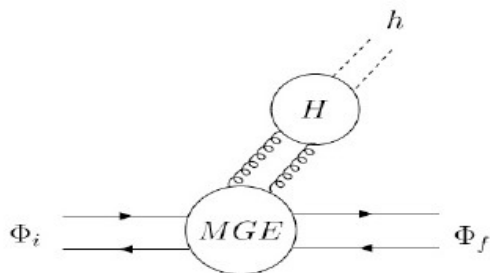
# Bottomonium physics at Belle and Belle II

Unique physics case at Belle II

# Bottomonium

- Hadronic transitions between heavy quarkonium states can be described with the **QCD multiple expansion model (QCDME)** PRD 24, 2874 (1981)

- in analogy with electromagnetism, it is possible to expand in terms of  $(ak)$  gluon radiation if the radius  $a$  of the bound  $q\bar{q}$  state is much smaller than the wavelength  $1/k$
- vicinity to threshold opening can modify **QCDME** predictions



$$m^3S^1 \rightarrow \pi\pi$$

$$n^3S^1 \text{ (E1E1)}$$

$$m^3S^1 \rightarrow \eta$$

$$n^3S^1 \text{ (E1M2 or M1M1)}$$

- When/how did the *bottomonium* story begin?

# Bottomonium: how it started

- From Belle, PRL 100 (2008) 112001:

## Observation of anomalous $\Upsilon(1S)\pi^+\pi^-$ and $\Upsilon(2S)\pi^+\pi^-$ production near the $\Upsilon(5S)$ resonance

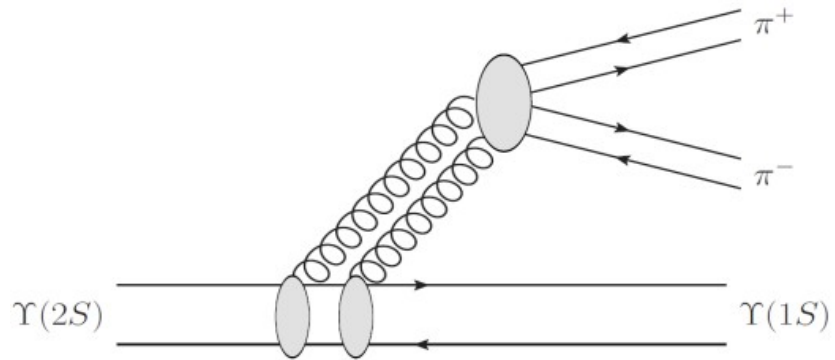
- First observation of  $e^+e^- \rightarrow \Upsilon(1S)\pi^+\pi^-$  and  $e^+e^- \rightarrow \Upsilon(2S)\pi^+\pi^-$
- First evidence for  $e^+e^- \rightarrow \Upsilon(3S)\pi^+\pi^-$  and  $e^+e^- \rightarrow \Upsilon(1S)K^+K^- \sim \Upsilon(5S)$

$$\Gamma(\Upsilon(5S) \rightarrow \Upsilon(1S)\pi^+\pi^-) = 0.59 \pm 0.04(\text{stat}) \pm 0.09(\text{syst}) \text{ MeV}$$

$$\Gamma(\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-) = 0.85 \pm 0.07(\text{stat}) \pm 0.16(\text{syst}) \text{ MeV}$$

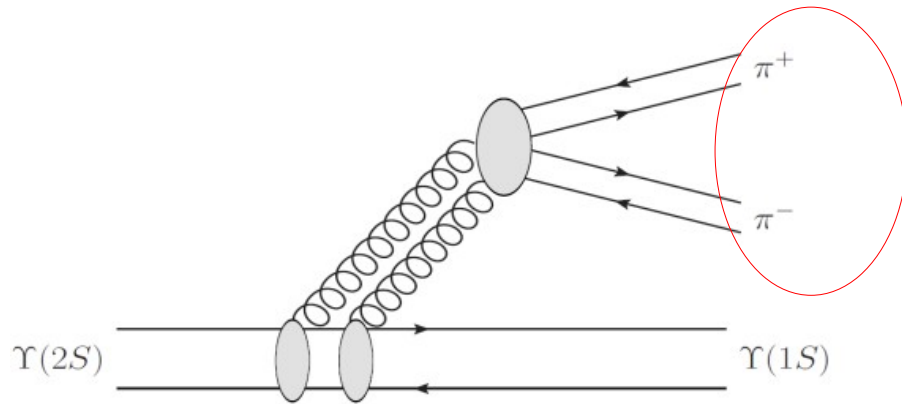
- From BaBar, PRD 78 (2008) 112022:  $\frac{\Gamma(\Upsilon(4S) \rightarrow \Upsilon(1S)\eta)}{\Gamma(\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-)} = 2.4 \pm 0.4$

# *Hadronic transition in Bottomonium*

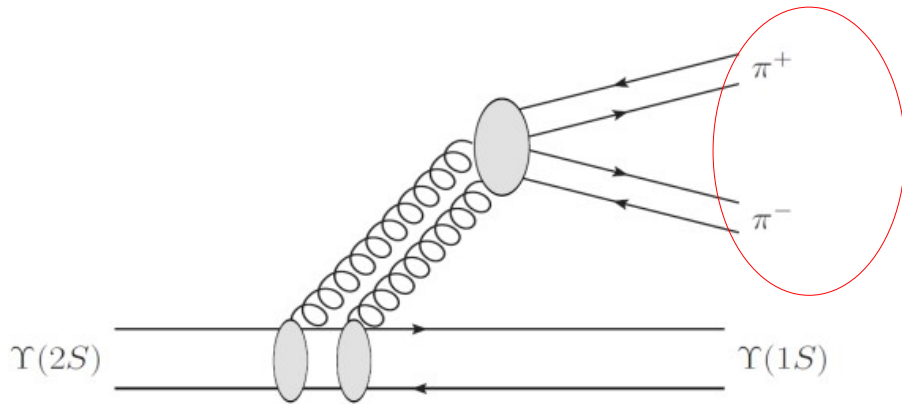




# Hadronic transition in Bottomonium



# Hadronic transition in Bottomonium



$\pi^+\pi^-$  :  $E1E1$  gluons

$$\Gamma(\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-) = 5.7 \pm 0.5 \text{ keV}$$

$$\Gamma(\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-) = 0.89 \pm 0.08 \text{ keV}$$

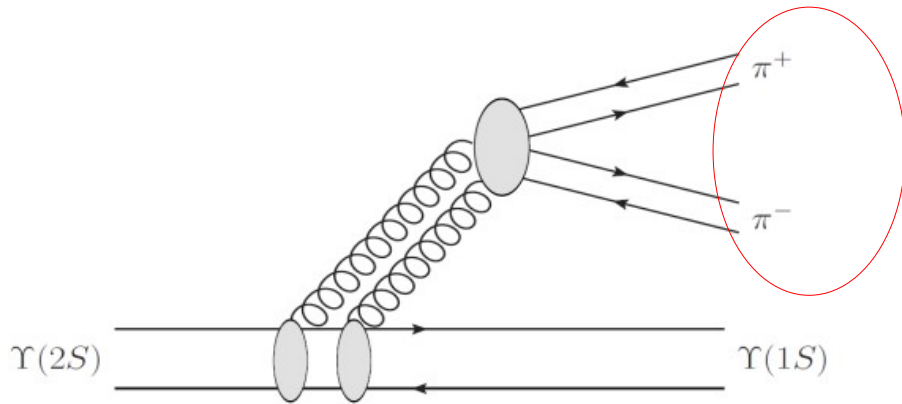
$$\Gamma(\Upsilon(3S) \rightarrow \Upsilon(2S)\pi^+\pi^-) = 0.57 \pm 0.06 \text{ keV}$$

partial widths are small



$$\Gamma(\Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^-) \sim 1 \text{ MeV}$$

# Hadronic transition in Bottomonium



$\pi^+\pi^-$  :  $E1E1$  gluons

$$\Gamma(\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-) = 5.7 \pm 0.5 \text{ keV}$$

$$\Gamma(\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-) = 0.89 \pm 0.08 \text{ keV}$$

$$\Gamma(\Upsilon(3S) \rightarrow \Upsilon(2S)\pi^+\pi^-) = 0.57 \pm 0.06 \text{ keV}$$

partial widths are small



$$\Gamma(\Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^-) \sim 1 \text{ MeV}$$

$\eta$  :  $E1M2$  gluons

Amplitude  $\propto$  chromomagnetic moment of  $b$  quark  $\propto 1/m_b$

$$\Gamma(\Upsilon(2S) \rightarrow \Upsilon(1S)\eta) = (9.3 \pm 1.5) \times 10^{-3} \text{ keV}$$

$$\Gamma(\Upsilon(3S) \rightarrow \Upsilon(1S)\eta) < 2 \times 10^{-3} \text{ keV}$$

additional suppression

$$\frac{\Gamma(\Upsilon(4S) \rightarrow \Upsilon(1S)\eta)}{\Gamma(\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-)} = 2.4 \pm 0.4$$



# How that can happen?

- Alternative explanation is that the transitions  $Y(nS) \rightarrow Y(mS)$  proceed via **exotic admixture**

- The decay into constituents dominates
- If  $p_B$  is high enough, rescattering is suppressed

- Then:  $Y(4S) |B\bar{B}\rangle,$

$$Y(5S) |B_s^* \bar{B}_s^*\rangle \quad |B_s^* B^0\rangle ?$$

$$Y(6S) |B_1 \bar{B}\rangle$$

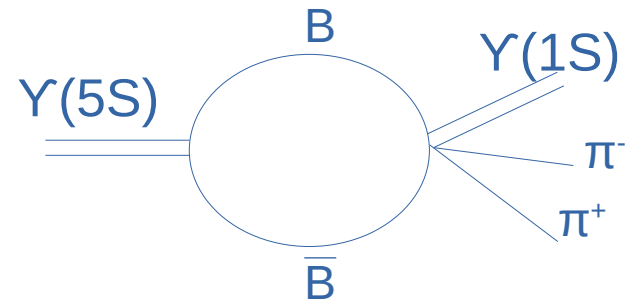
- New decay mechanism : exotic admixture

- Possibilities: **hadroquarkonium**, **compact tetraquark**, **hybrids**

$$|Y(2S) f_0\rangle$$

$$|bq \bar{b}q\rangle$$

$$|b\bar{b} g\rangle$$



# Angular momentum wave functions

$$\begin{aligned} |B\bar{B}\rangle &\equiv |S_{b\bar{q}} = 0, L_{b\bar{q}} = 0, S_{\bar{b}q} = 0, L_{\bar{b}q} = 0, L = 1\rangle && \text{PRD 85, 034024 (2012)} \\ &= \frac{1}{2\sqrt{3}} |S_{b\bar{b}} = 1, J_{q\bar{q}} = 0\rangle \rightarrow \Upsilon(1S) \pi^+ \pi^- \text{ in S wave} \\ &+ \frac{1}{2} |S_{b\bar{b}} = 1, J_{q\bar{q}} = 1\rangle \rightarrow \Upsilon(1S) \eta \\ &+ \frac{\sqrt{5}}{2\sqrt{3}} |S_{b\bar{b}} = 1, J_{q\bar{q}} = 2\rangle \rightarrow \Upsilon(1S) \pi^+ \pi^- \text{ in D wave} \\ &+ \frac{1}{2} |S_{b\bar{b}} = 0, J_{q\bar{q}} = 1\rangle \rightarrow h_b(1P) \eta \end{aligned}$$

Rescattering  $\Rightarrow$  many transitions are allowed

| Transition | Partial width (keV) |
|------------|---------------------|
|------------|---------------------|

|                            |               |
|----------------------------|---------------|
| $\Upsilon(4S) \rightarrow$ |               |
| $\Upsilon(1S) \pi^+ \pi^-$ | $1.7 \pm 0.2$ |
| $\Upsilon(1S) \eta$        | $4.0 \pm 0.8$ |
| $\Upsilon(2S) \pi^+ \pi^-$ | $1.8 \pm 0.3$ |
| $h_b(1P) \eta$             | $45 \pm 7$    |

Bondar, RM, Voloshin MPLA 32, 1750025 (2017)

|   |                |
|---|----------------|
| $\Upsilon(5S) \rightarrow$                              |                |
| $\Upsilon(1S) \pi^+ \pi^-$                              | $238 \pm 41$   |
| $\Upsilon(1S) \eta$                                     | $39 \pm 11$    |
| $\Upsilon(1S) K^+ K^-$                                  | $33 \pm 11$    |
| $\Upsilon(2S) \pi^+ \pi^-$                              | $428 \pm 83$   |
| $\Upsilon(2S) \eta$                                     | $204 \pm 44$   |
| $\Upsilon(3S) \pi^+ \pi^-$                              | $153 \pm 31$   |
| $\chi_{b1}(1P) \omega$                                  | $84 \pm 20$    |
| $\chi_{b1}(1P) (\pi^+ \pi^- \pi^0)_{\text{non-}\omega}$ | $28 \pm 11$    |
| $\chi_{b2}(1P) \omega$                                  | $32 \pm 15$    |
| $\chi_{b2}(1P) (\pi^+ \pi^- \pi^0)_{\text{non-}\omega}$ | $33 \pm 20$    |
| $\Upsilon_J(1D) \pi^+ \pi^-$                            | $\sim 60$      |
| $\Upsilon_J(1D) \eta$                                   | $150 \pm 48$   |
| $Z_b(10610)^\pm \pi^\mp$                                | $2070 \pm 440$ |
| $Z_b(10650)^\pm \pi^\mp$                                | $1200 \pm 300$ |

So variety of transitions support the interpretation as **molecular admixture**

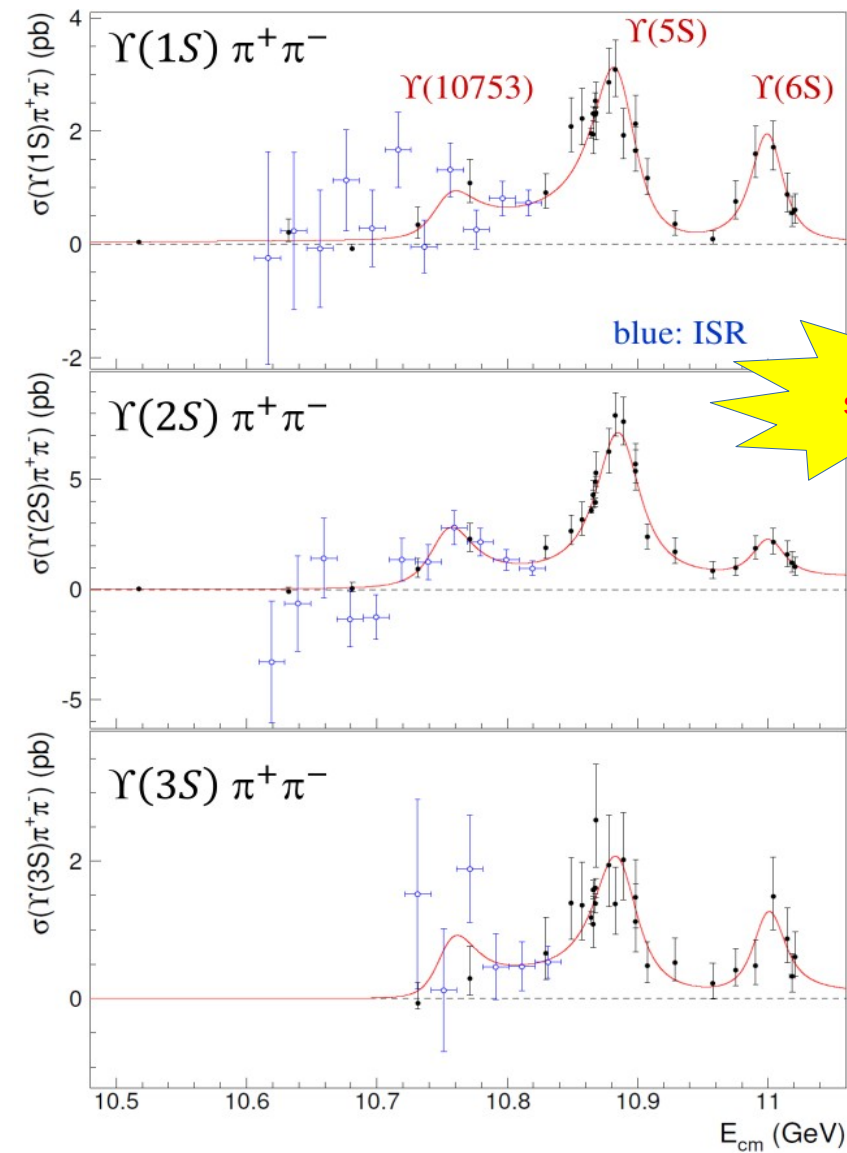
|                                 |               |
|---------------------------------|---------------|
| $\Upsilon(6S) \rightarrow$      |               |
| $\Upsilon(1S) \pi^+ \pi^-$      | $137 \pm 32$  |
| $\Upsilon(2S) \pi^+ \pi^-$      | $183 \pm 43$  |
| $\Upsilon(3S) \pi^+ \pi^-$      | $77 \pm 28$   |
| $Z_b(10610, 10650)^\pm \pi^\mp$ | $1300 - 6600$ |

# *How to perform Bottomonium analysis?*

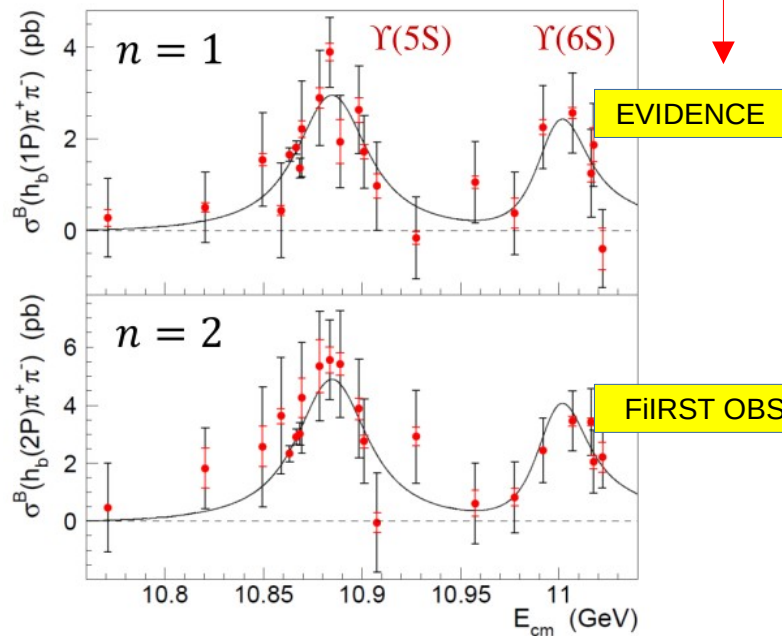
- Measurement at a single energy can:
  - show non-resonant contribution
  - reveal other resonances
- Energy scan is needed!

# Bottomonium at Belle

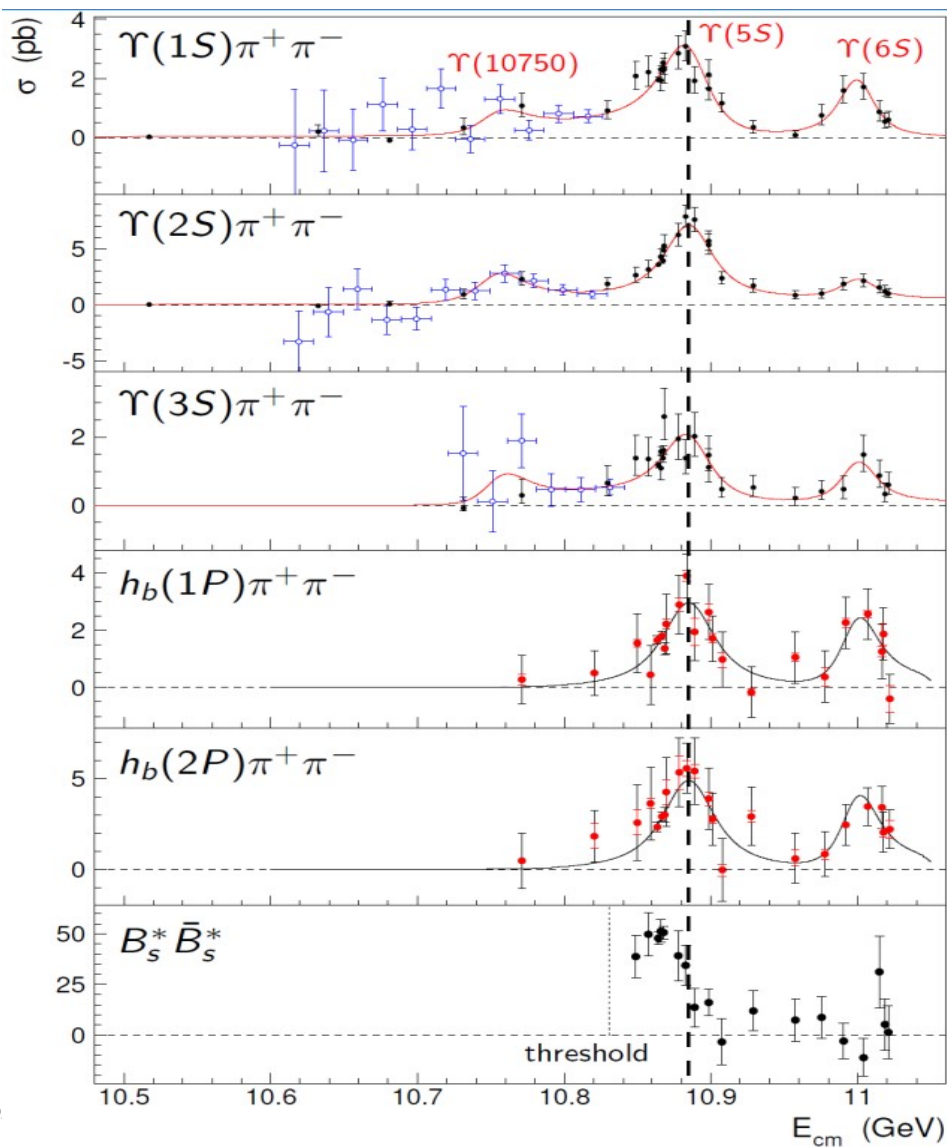
PRL 117 (2016) 142001  
JHEP 10 (2019) 220



$$Z_b^+ \pi^- \rightarrow h_b(nP) \pi^+ \pi^-$$







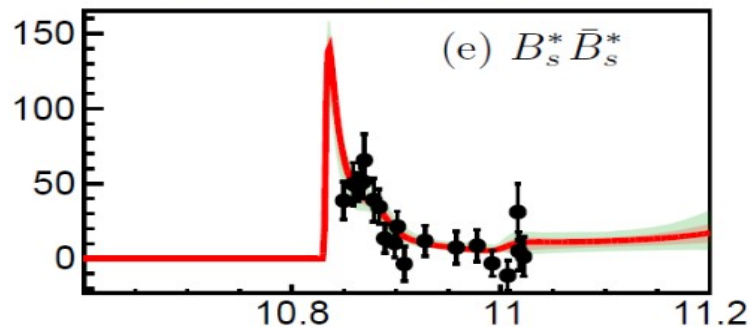
PRL 117 (2016) 142001  
 JHEP 10 (2019) 220

$\Upsilon(5S)$  peak in  $B_s^* \bar{B}_s^*$  channel  
 is shifted by 20 MeV  
 w.r.t. bottomonium channels.

Two states near  $\Upsilon(5S)$  ?

Hüsken, Mitchell, Swanson, PRD 106, 094013 (2022)

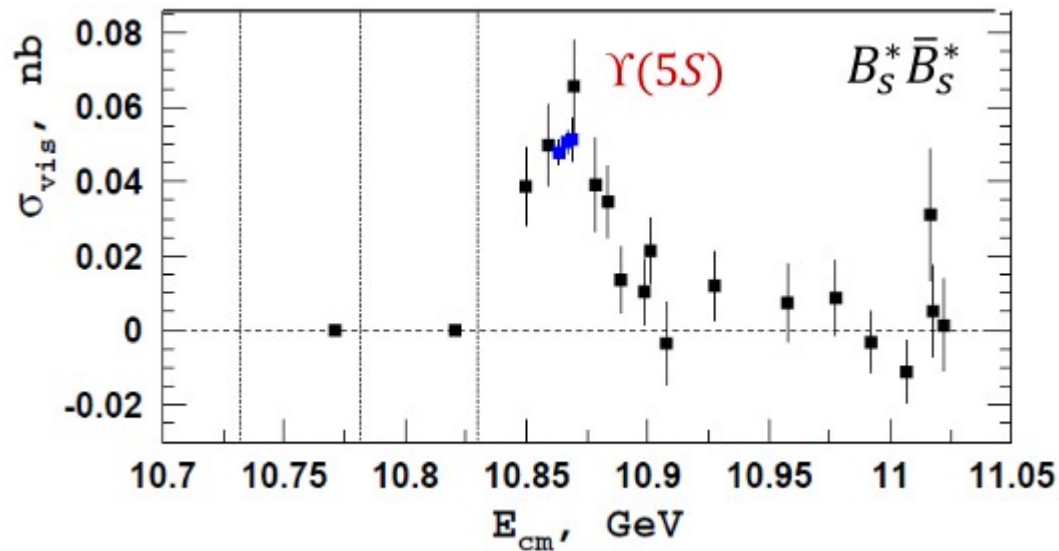
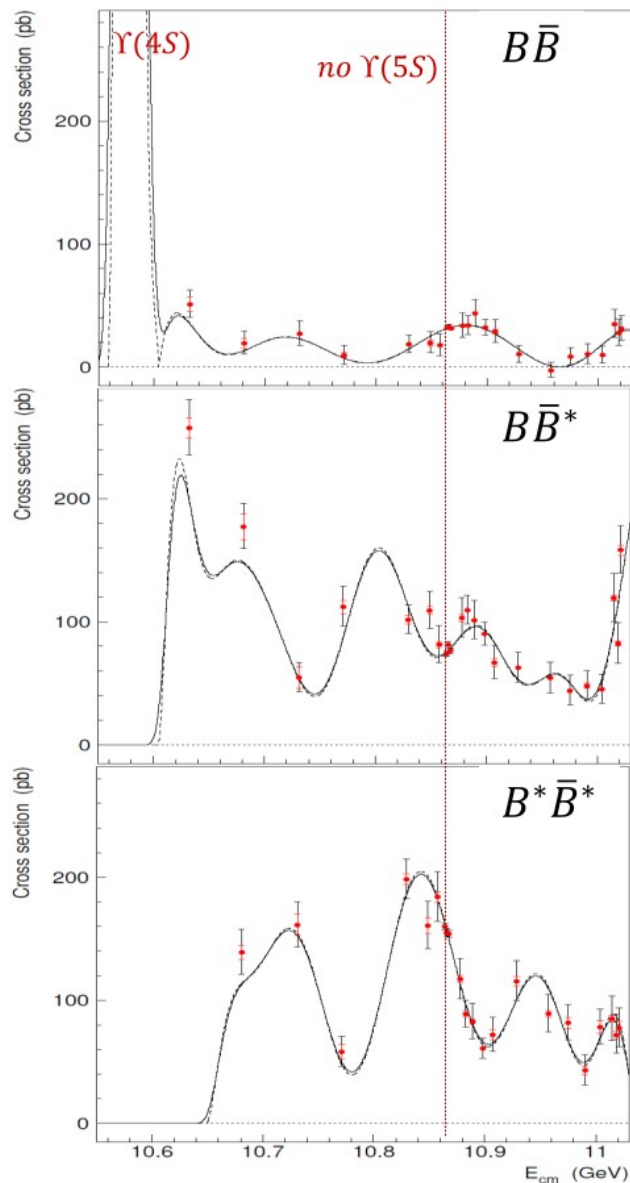
Coupled-channel analysis:



$\Rightarrow$  Improve accuracy in  $B_s^* \bar{B}_s^*$

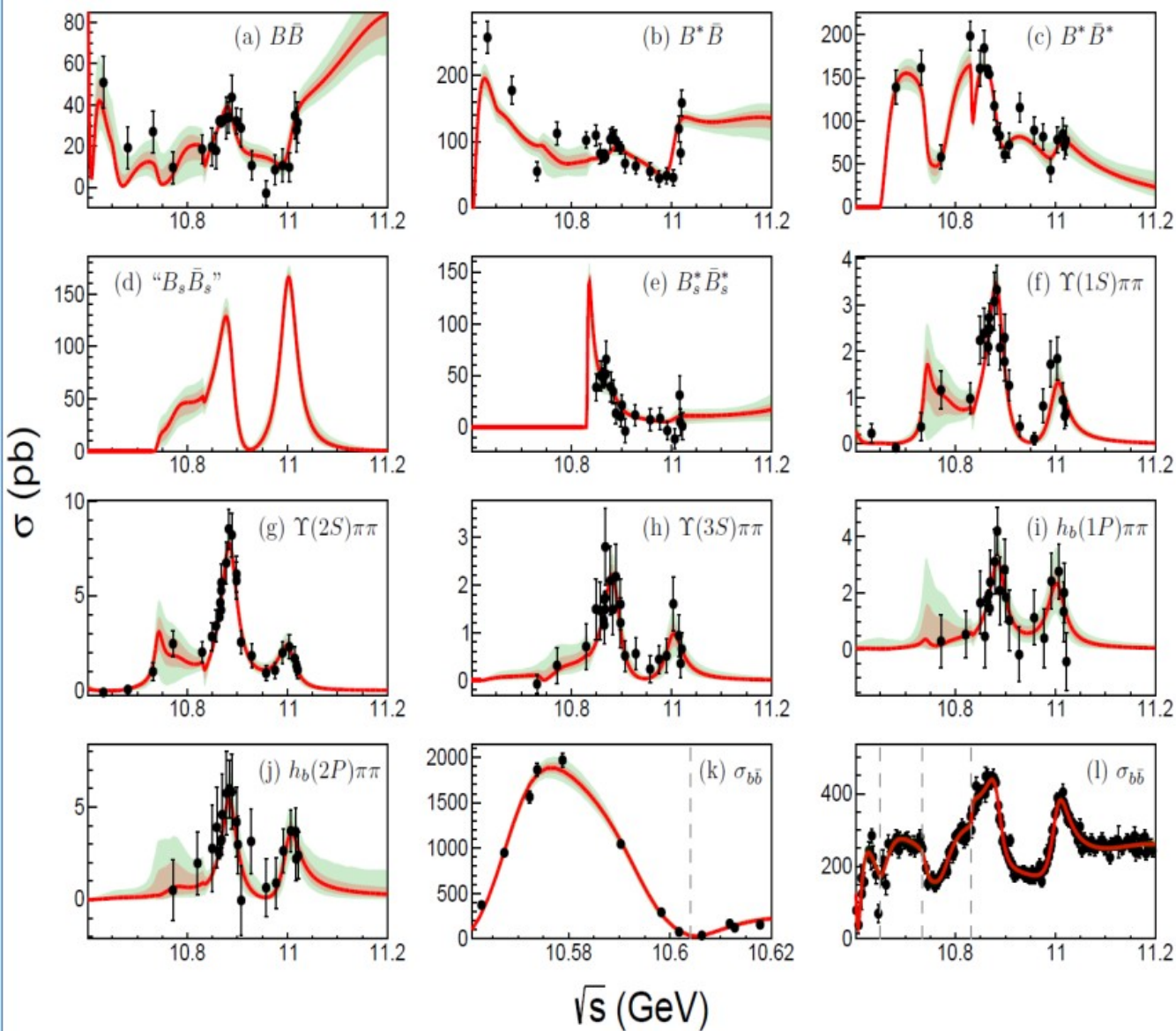
# Bottomonium at Belle

JHEP 06 (2021) 137



No clear  $\Upsilon(5S)$  peak:  
"oscillatory" non-resonant contribution?

# A note about Coupled-channel analysis:

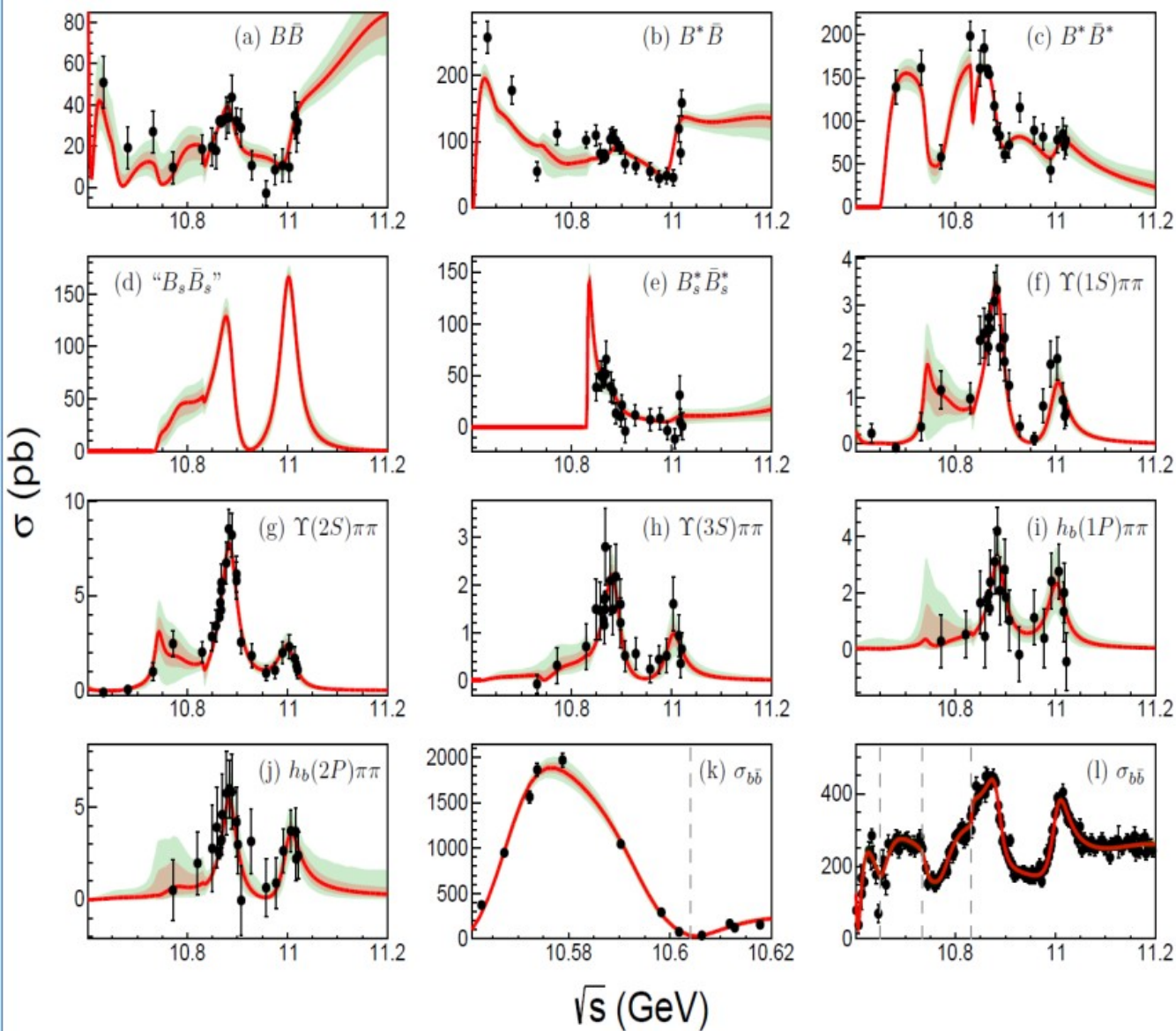


Husken, Mitchell, Swanson,  
PRD 106 (2022) 094013

- Assume  $\Upsilon(10753)$  is a 4S-3D mixture
- All available scan data
- Global and unitary analysis of  $e^+e^- \rightarrow b\bar{b}$  cross section
- Pole positions are determined for  $\Upsilon(4S)$ ,  $\Upsilon(10753)$ ,  $\Upsilon(5S)$ , and  $\Upsilon(6S)$
- Strong evidence for the new  $\Upsilon(10753)$

Accuracy above  $\Upsilon(6S)$   
and near  $\Upsilon(10753)$   
needs improvement.

Husken, Mitchell, Swanson,  
PRD 106 (2022) 094013



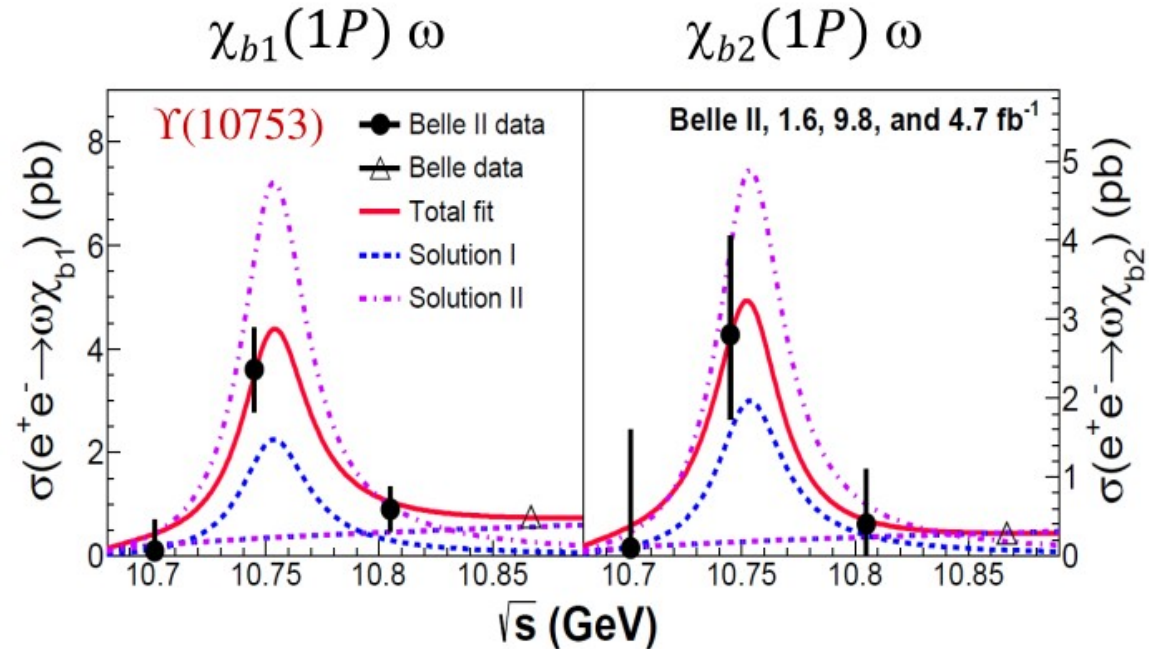
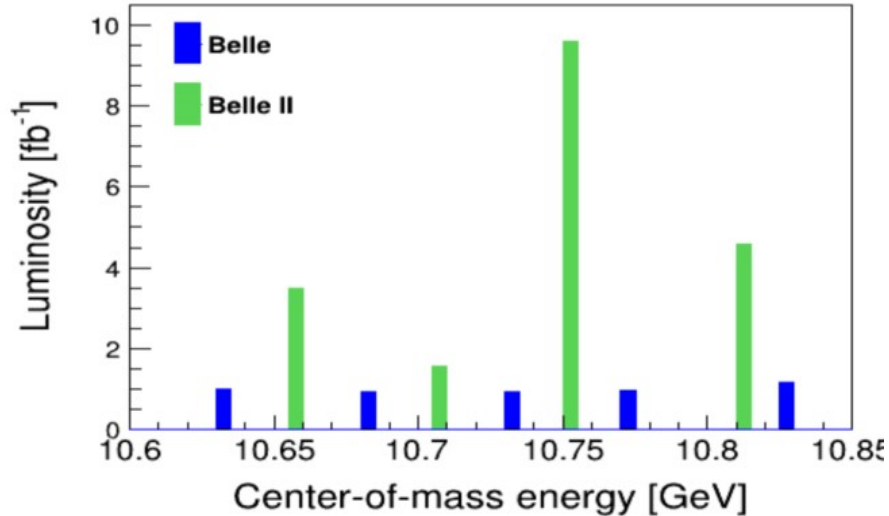
- Assume  $\Upsilon(10753)$  is a 4S-3D mixture
- All available scan data
- Global and unitary analysis of  $e^+e^- \rightarrow b\bar{b}$  cross section
- Pole positions are determined for  $\Upsilon(4S)$ ,  $\Upsilon(10753)$ ,  $\Upsilon(5S)$ , and  $\Upsilon(6S)$
- Strong evidence for the new  $\Upsilon(10753)$**

**Plan in Belle II  
to run @  $\Upsilon(6S)$**

# Belle II energy scan

PRL 130 (2023) 091902

- Luminosity:  $20 \text{ fb}^{-1}$  ( Nov 2021)
- Goal: study  $Y(10753)$  and  $B^* \bar{B}^*$  threshold region
- Found:  $Y(10753)$  and  $Y(5S)$  have different pattern: different structure?



Full reconstruction:  $\Upsilon(nS) \rightarrow \mu^+ \mu^-$

$\Upsilon(10753)$  significance:

|                            | Belle       | Belle + Belle II |
|----------------------------|-------------|------------------|
| $\Upsilon(1S) \pi^+ \pi^-$ | $2.7\sigma$ | $4.1\sigma$      |
| $\Upsilon(2S) \pi^+ \pi^-$ | $5.4\sigma$ | $7.5\sigma$      |

$\Upsilon(10753)$  parameters:

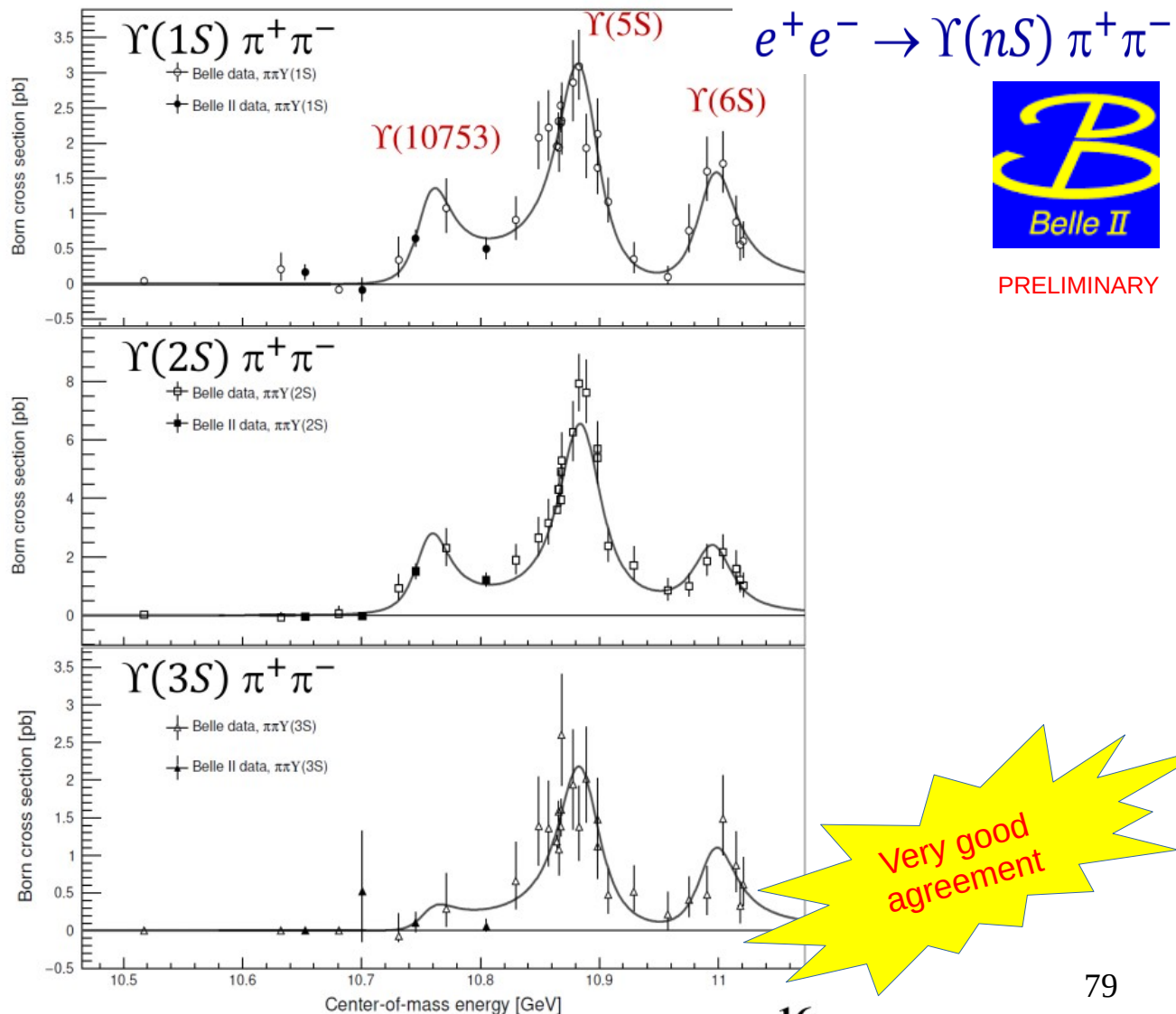
$$M = (10756.3 \pm 2.7 \pm 0.6) \text{ MeV}$$

$$\Gamma = (29.7 \pm 8.5 \pm 1.1) \text{ MeV}$$

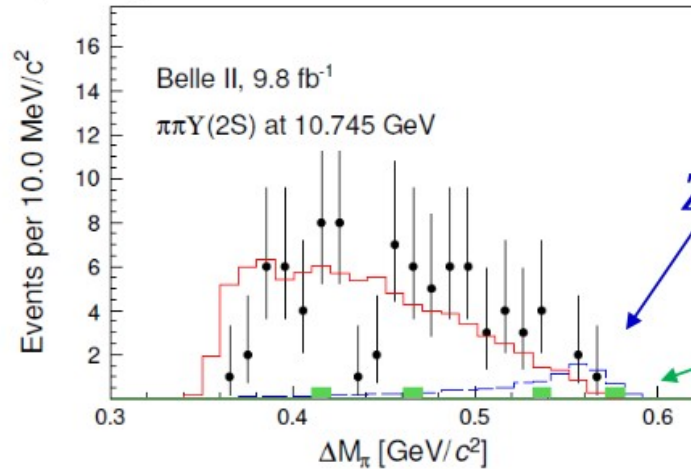
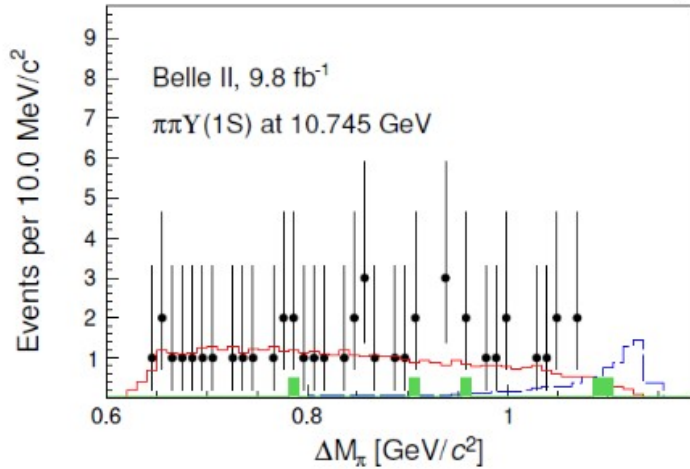
c.f. Belle

$$M = (10752.7 \pm 5.9^{+0.7}_{-1.1}) \text{ MeV}$$

$$\Gamma = (35.5^{+17.6}_{-11.3} \text{ } ^{+3.9}_{-3.3}) \text{ MeV}$$



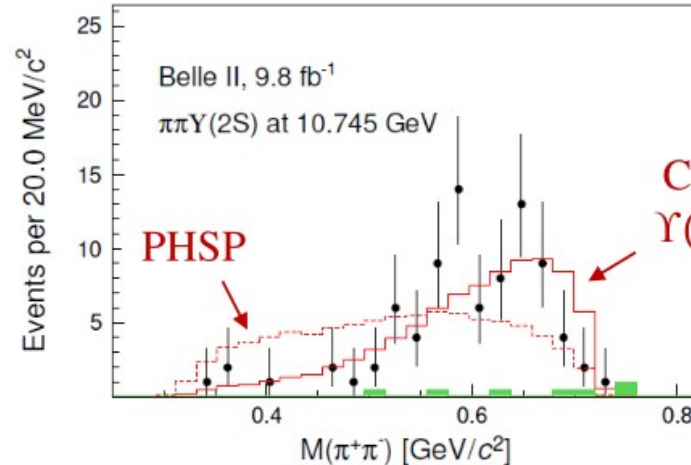
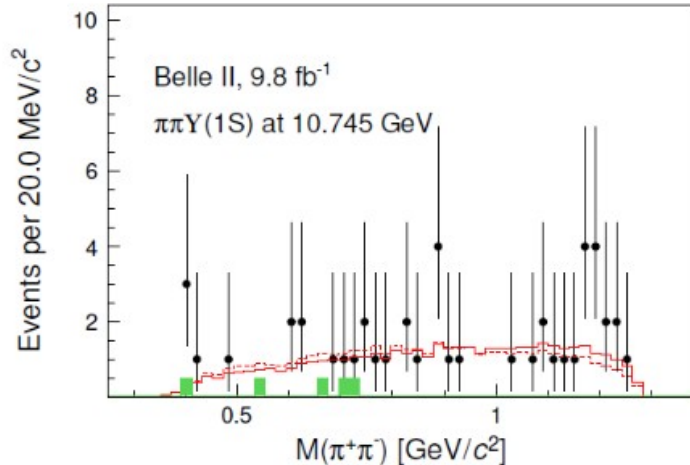
# $M(\Upsilon(nS) \pi^\pm)$



PRELIMINARY

- Resonant substructure of  $\Upsilon(10753) \rightarrow \Upsilon(nS)\pi^+\pi^-$

# $M(\pi^+\pi^-)$

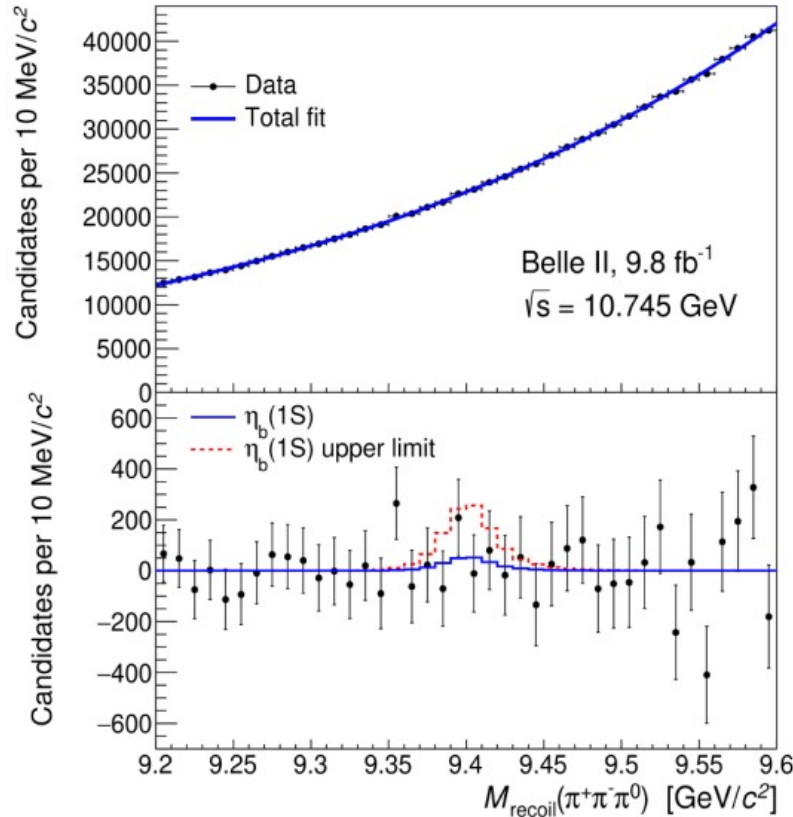




# Testing tetraquark model for the $Y(10753)$ at Belle II



PRELIMINARY



$Y(10753) \rightarrow \eta_b(1S)\omega / \chi_{b0}(1P)\omega$

- Predicted for the tetraquark model
- **No signal found**

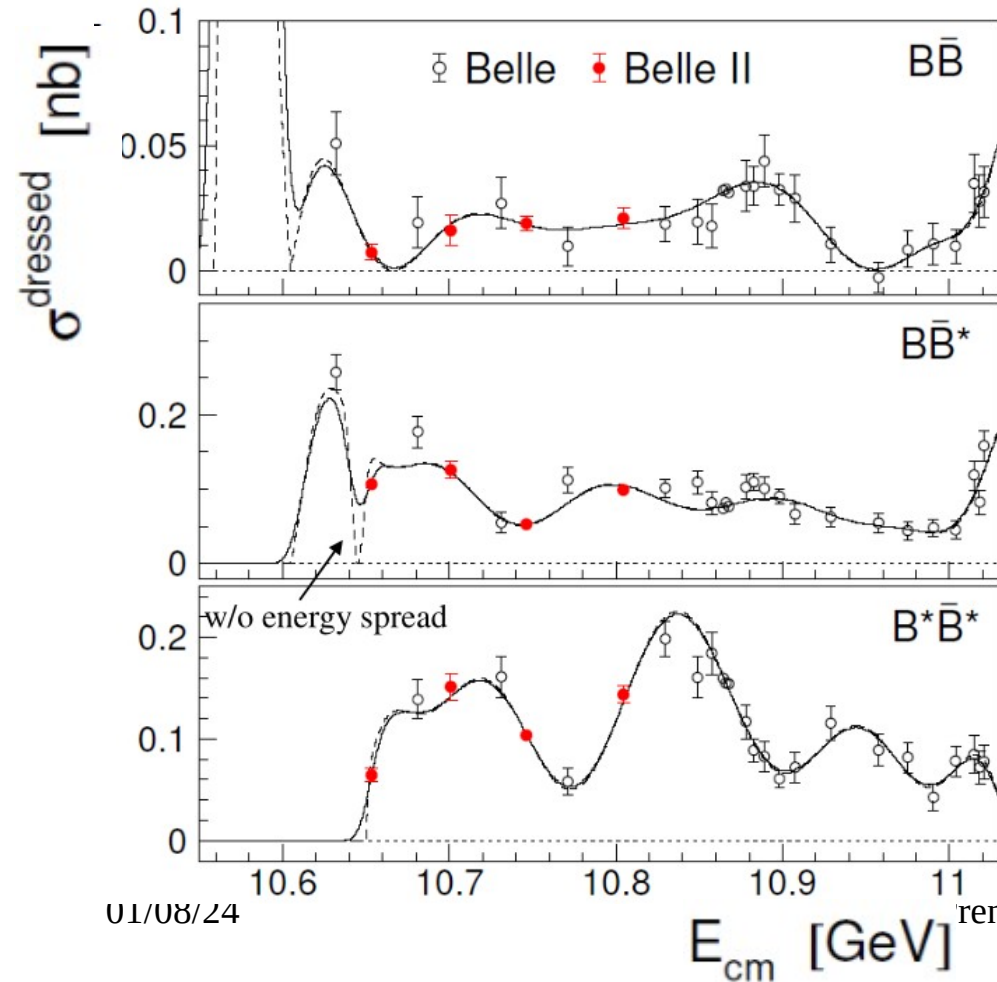
$$\sigma(e^+e^- \rightarrow \eta_b(1S)\omega) < 2.5 \text{ pb} \quad 90\% \text{ CL}$$

$$\text{c.f. } \sigma(e^+e^- \rightarrow Y(1,2S)\pi^+\pi^-) = (1 - 3) \text{ pb}$$

$$\sigma(e^+e^- \rightarrow \chi_{b0}(1P)\omega) < 7.8 \text{ pb}$$

$$\text{c.f. } \sigma(\chi_{b1}(1P)\omega / \chi_{b2}(1P)\omega) = (3.6 / 2.8) \text{ pb}$$

# Study of $e^+e^- \rightarrow B\bar{B}, B\bar{B}^*, B^*\bar{B}^*$ at Belle II



- Reconstruct B meson in 1000 final states



PRELIMINARY

- Rapid rise of the  $B^*\bar{B}^*$  cross section close to threshold: hint for molecular state?

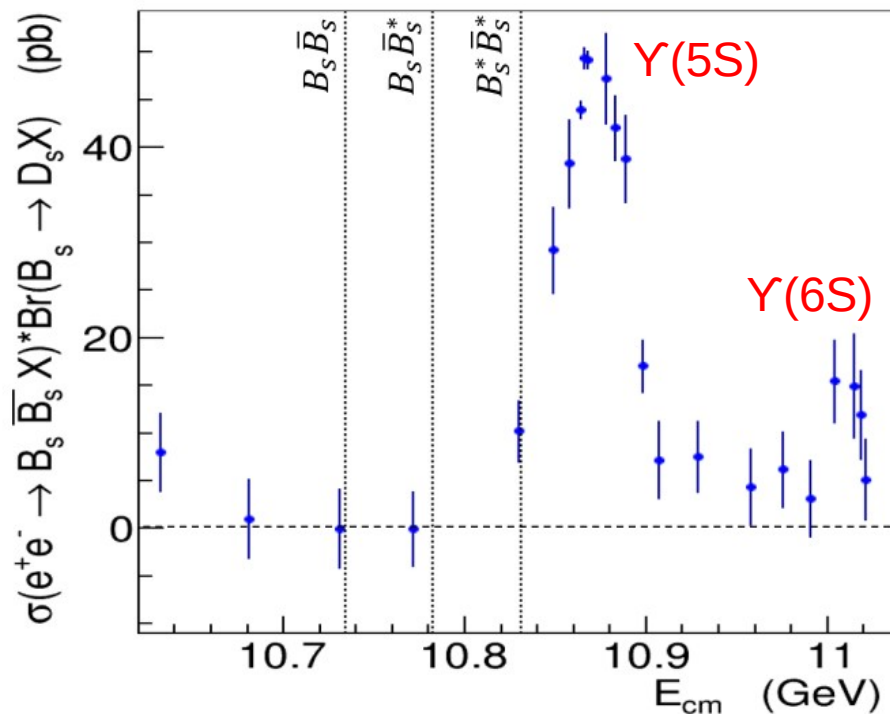
# Study of $e^+e^- \rightarrow B_s\bar{B}_s X$ at Belle II

JHEP 08 (2023) 131

- Inclusive analysis

$$\frac{Br(B_s \rightarrow D^0 X)}{Br(B_s \rightarrow D_s X)} = 0.415 \pm 0.094$$

- Clear  $Y(5S)$  peak, seen also  $Y(6S)$



$$\sigma(B_s\bar{B}_s X) = \sigma(B_s^{(*)}\bar{B}_s^{(*)}) \text{ – up to the } B_s\bar{B}_s\pi^0\pi^0 \text{ threshold at } 11.004 \text{ GeV}$$

# Summary

- Belle shut down: 2010. After 14 years still great physics results show up with Belle data sets!
- Most of the interesting results use the whole Belle luminosity: update with Belle II is planned
- A remarkable fraction of data taking @Belle II will be above/below  $\Upsilon(4S)$  c.m. energy
- Great potential in the continuum and ISR physics
- Amplitude analysis to search for  $c\bar{c}s\bar{s}$  resonances and more
- Bottomonium physics: unique at Belle and Belle II
- Belle II is in excellent shape: already collected  $\sim$ BaBar luminosity (**424 fb<sup>-1</sup> in 2022**)
- Analysis plan: combining Belle + Belle II data sets ( $\sim 1.5 \text{ ab}^{-1}$ )
- Data taking at Belle II: **50 ab<sup>-1</sup> by 2035**
- Pentaquark search: so far no results with Belle data set. More investigation is ongoing

**STAY tuned!**