



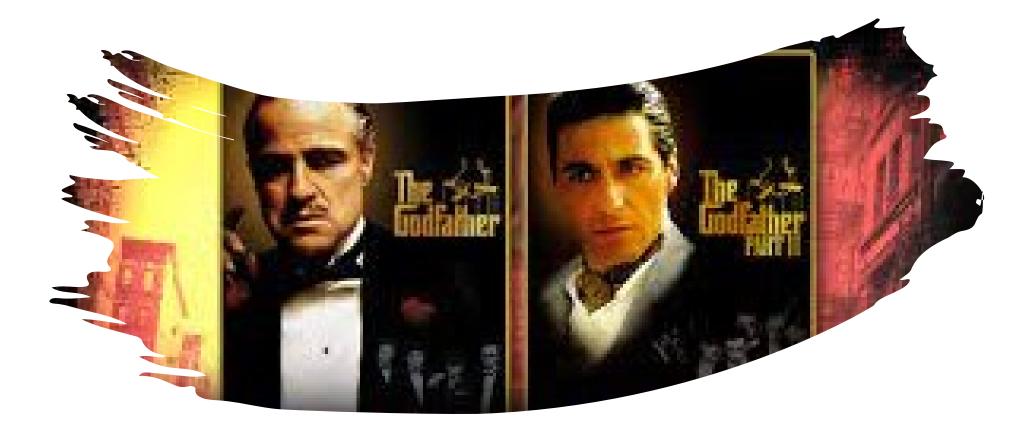
# CKM and flavour at Belle II

Jim Libby

**Indian Institute of Technology Madras** 

### Outline

- Belle II
- Highlights so far
  - Lepton flavour:
    - tau physics highlights
  - B physics highlights
    - CP violation
    - Tests of lepton-flavour universality
    - Evidence for  $B^+ \rightarrow K^+ v v$
- Prospects



#### Belle II

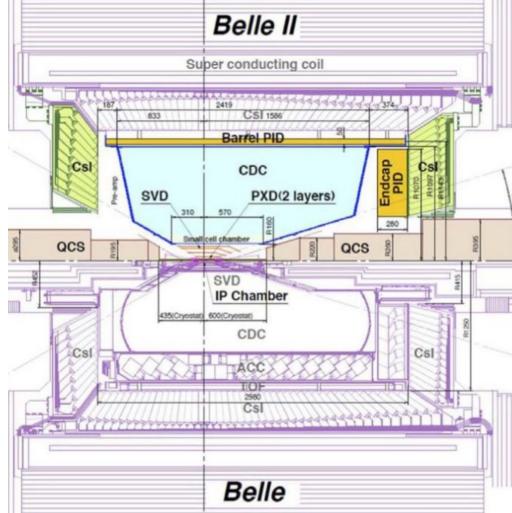
#### Will the next generation perform as well as the first?

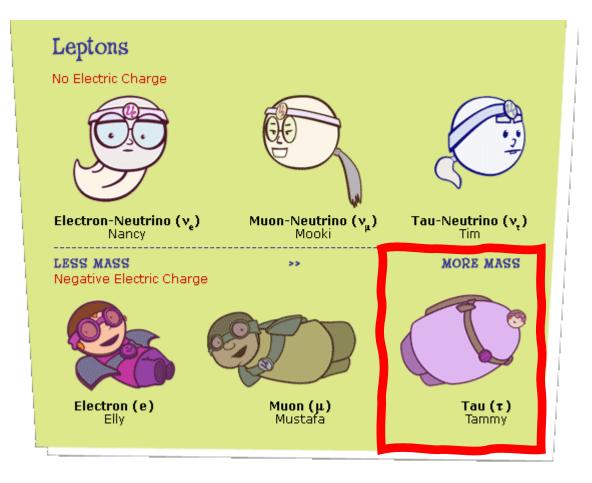
#### Detectors and data samples

- Belle + BaBar collected
   0.71+0.43=1.14 ab<sup>-1</sup> Y(4S) samples
  - Many achievements: confirmation of KM mechanism, b→cτν, direct CPV in B decay

#### • SuperKEKB + Belle II@KEK, Tsukuba

- nanobeam scheme to increase instantaneous luminosity by factor 30 to collect multi-ab<sup>-1</sup> sample
- World record 4.7×10<sup>34</sup> cm<sup>-2</sup>s<sup>-1</sup>
- Target 6×10<sup>35</sup> cm<sup>-2</sup>s<sup>-1</sup>
- So far integrated 362 fb<sup>-1</sup> at Y(4S)
- + 42 fb<sup>-1</sup> off-resonance to characterize continuum



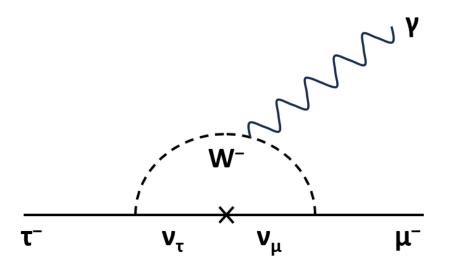


#### https://www.quarked.org/

# τphysics

### Tau physics

- 185 standard model decay modes studied
  - principally hadronic final states
- Unique laboratory to study weak interaction
- Third-generation therefore beyond-SMsensitivity anticipated
  - Any observation of lepton-flavour violation in  $\tau \rightarrow 3\mu$ ,  $\tau \rightarrow \mu\gamma$ ,  $\tau \rightarrow l\phi$  etc **new physics**
  - SM highly suppressed
- Connections to g-2 and lepton universality violation in b decay
- Also, precision measurements of lepton universality in lepton decay, V<sub>us</sub>, moments, lifetime and mass



 $e^-,\,\mu^-,\,d\,,\,s$ 

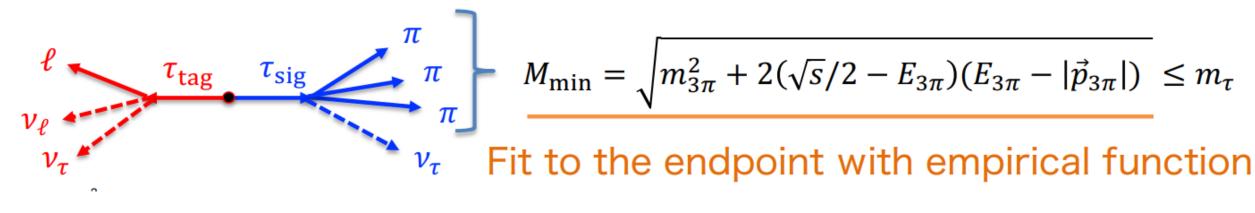
 $\bar{\nu}_{e}, \bar{\nu}_{\mu}, \bar{u}, \bar{u}$ 

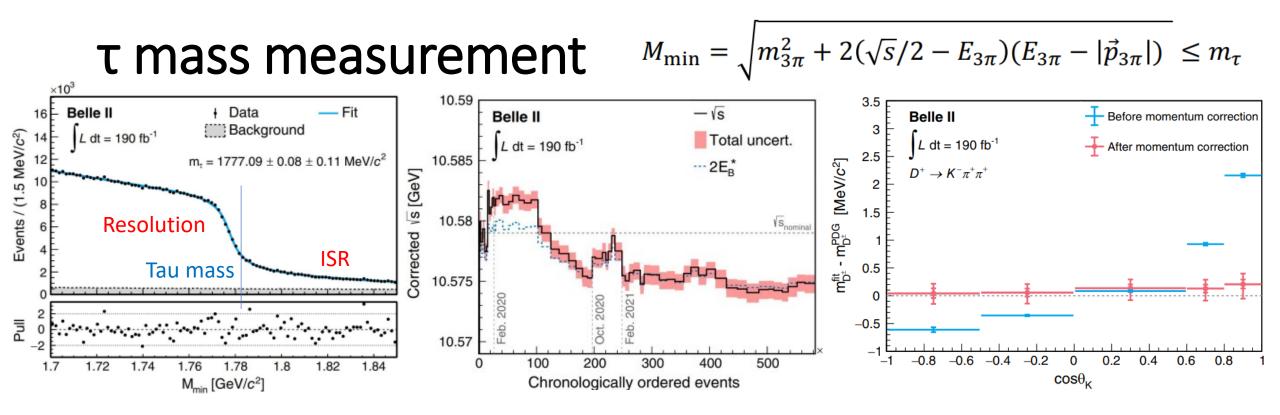
#### τ mass measurement

- Fundamental parameter of the standard model
  - Important input to lepton-flavour universality tests

$$R_e = \frac{\mathcal{B}[\tau^- \to e^- \bar{\nu_e} \nu_\tau]}{\mathcal{B}[\mu^- \to e^- \bar{\nu_e} \nu_\mu]} \qquad \left(\frac{g_\tau}{g_\mu}\right)_e = \sqrt{R_e \frac{\tau_\mu}{\tau_\tau} \frac{m_\mu^3}{m_\tau^3} (1+\delta_W)(1+\delta_\gamma)} \quad \text{(Ss are radiative corrections)}$$

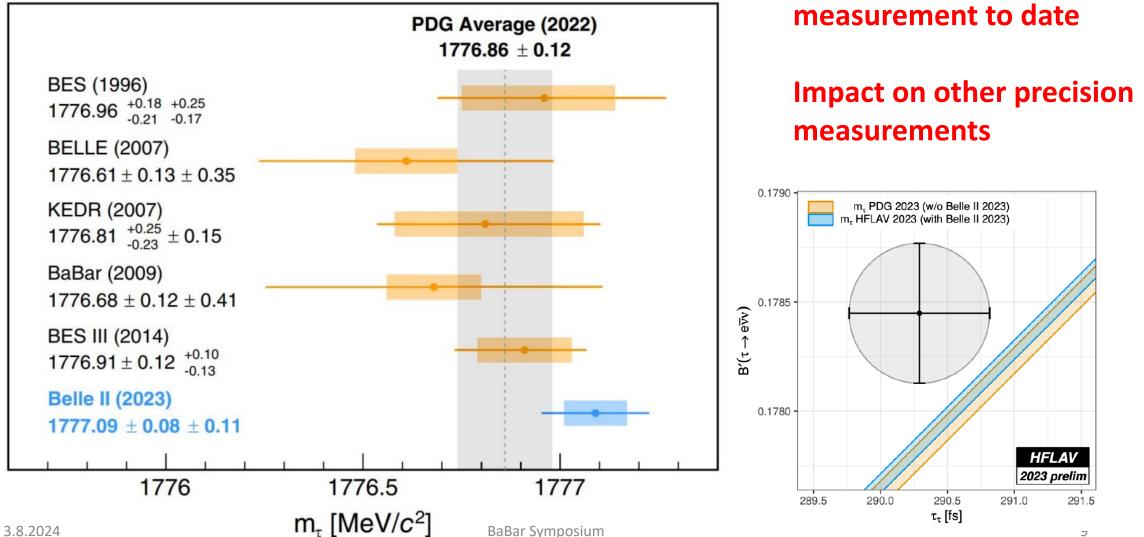
• We use the pseudomass variable to determine mass





- Fit to distribution with analytic form that accounts for ISR, FSR and resolution
- Knowing the scale key: beam energy (from E<sub>B</sub>\*) and momentum (from D mass)

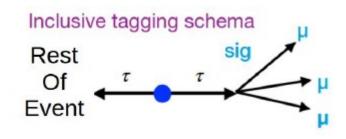
#### τ mass measurement

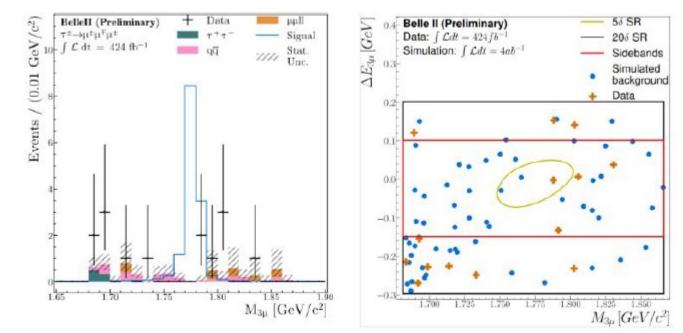


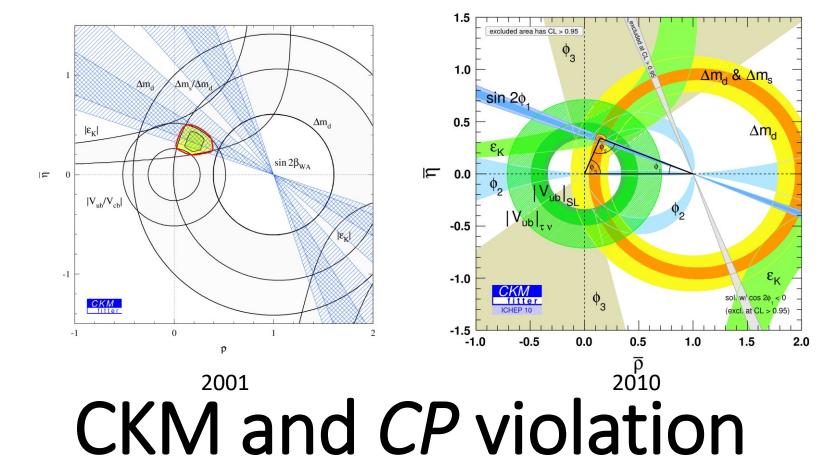
World's most precise

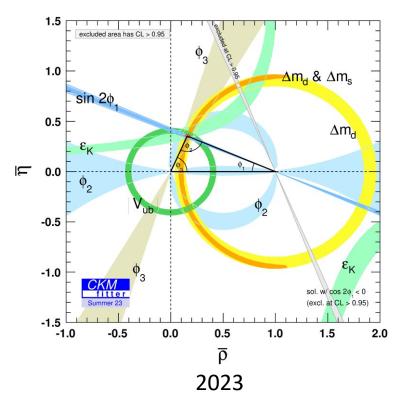
## $\tau \rightarrow 3\mu$ – lepton flavour violation search

- Inclusive tag of the non-signal τ to increase efficiency – multivariate
- Cut 'n' count in 2D plane of
  - $M_{3\mu}$  and  $\Delta E = E_{3\mu} E_{beam}$  (in c.m.)
  - Sideband derived background estimate  $0.5^{+1.4}_{-0.5}$  events
- One event observed
- World best limit
  - BF < 1.9×10<sup>-8</sup> (90% c.l.)
- Area of competition
  - <u>LHCb</u> BF < 4.1×10<sup>-8</sup> (Run 1 only)
  - <u>CMS</u> BF < 2.9×10<sup>-8</sup> (Run 1+2)





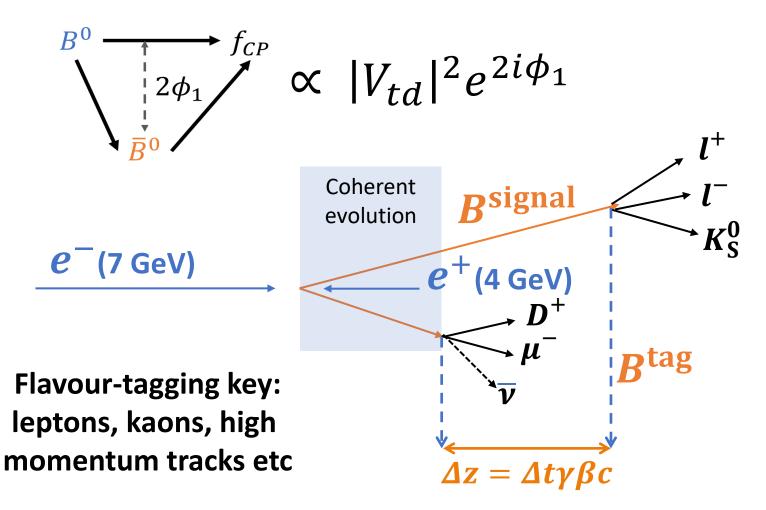


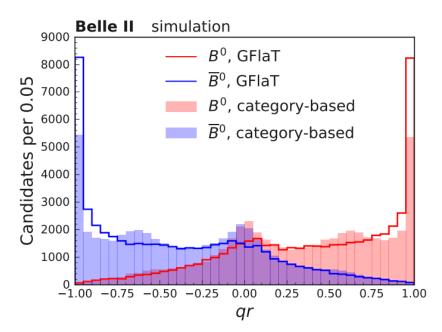


#### 3.8.2024



#### Flavour tagging improvements



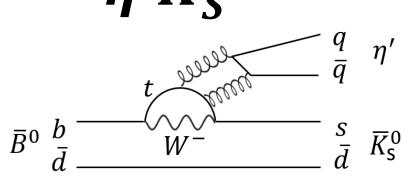


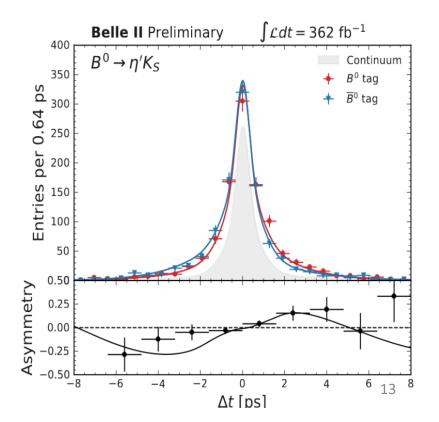
Graph-neural-network approach has improved our tagging by 18%  $\epsilon(1-2\omega) = 37.4\%$ 

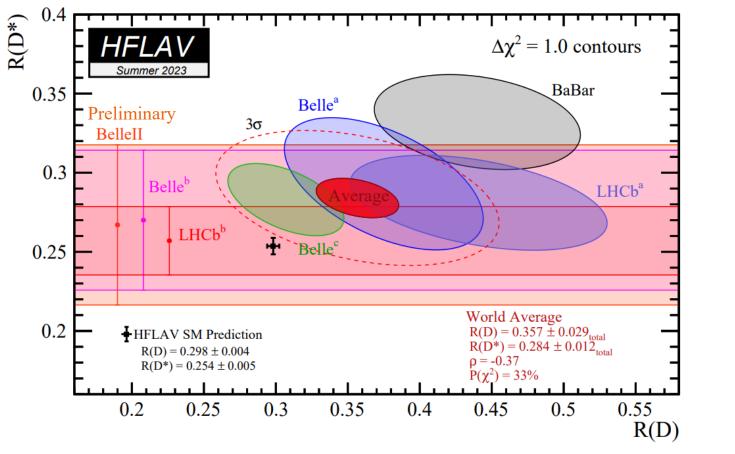
**BaBar Symposium** 

# Time-dependent *CP* violation - $B^0 \rightarrow \eta' K_S^0$

- Decay may also have a BSM phase as it is a gluonic penguin
  - alter the value of  $\phi_1$  from that measured in  $b \rightarrow c\bar{c}s$  transitions such as  $B^0 \rightarrow J/\psi K_S^0$
- Reconstructing  $\eta' \rightarrow \eta(\gamma\gamma)\pi^+\pi^-$  and  $\eta' \rightarrow \rho(\pi^+\pi^-)\gamma$  we select 829 ± 35 events in 362 fb<sup>-1</sup> sample
  - 3D fit to  $\Delta E$ ,  $m_{BC}$  and continuum suppression output
- $\sin 2\phi'_1 = 0.67 \pm 0.10 \pm 0.04$
- Consistent with current HFLAV average and that from  $b \rightarrow c \bar{c} s$  result





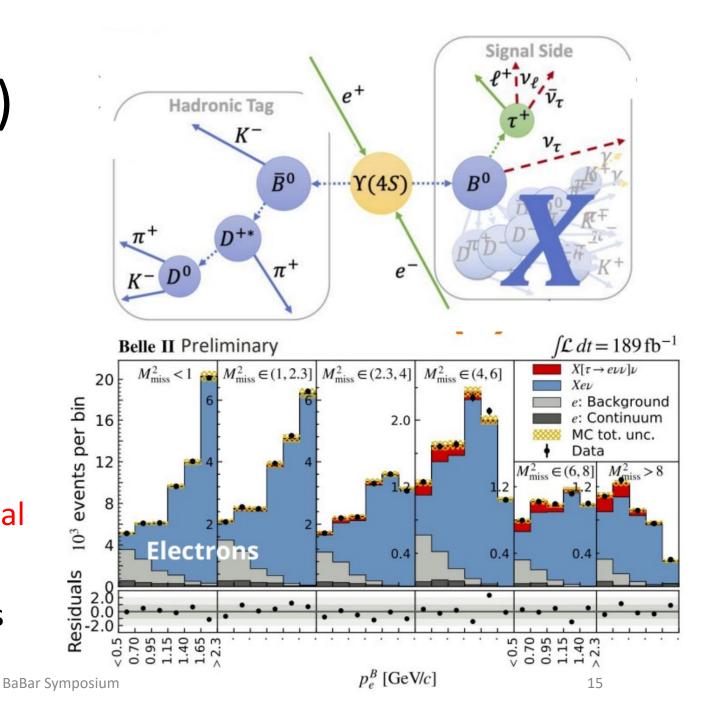




#### Lepton flavour/universality violation and rare decays

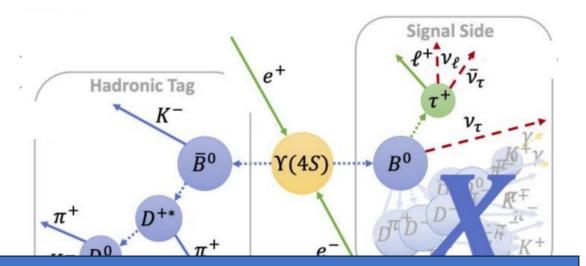
## Measurement of R(X)

- Inclusive ratio  $R(X) = \frac{BF(B \to X\tau\nu)}{BF(B \to Xl\nu)}$ 
  - A complementary alternative to R(D<sup>(\*)</sup>)
- Hadronic-tagging method with a 189 fb<sup>-1</sup> Belle II sample
  - Hadronic tag pioneered by BaBar
    - PRL 92 071802
  - MVA version at Belle II
    - <u>Comput. Softw. Big Sci. 3 (2019) 1, 6</u>
- Use missing-mass squared and lepton momentum to isolate signal above B→Xlv background
- Background templates calibrated to control samples and sidebands



## Measurement of R(X)

- Inclusive ratio  $R(X) = \frac{BF(B \to X\tau\nu)}{BF(B \to Xl\nu)}$ 
  - A complementary alternative to R(D<sup>(\*)</sup>)



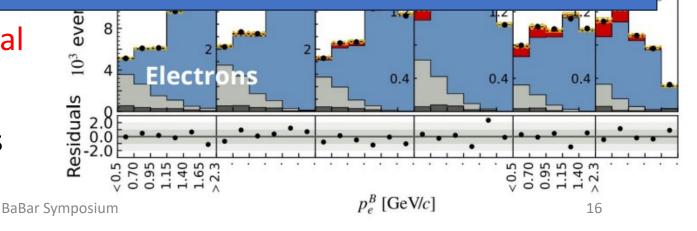
#### R(X)=0.228±0.016 (stat) ±0.036 (syst)

Systematics dominated by control sample reweighting procedures First at B factories

Agrees with SM prediction and the WA R(D<sup>(\*)</sup>) values

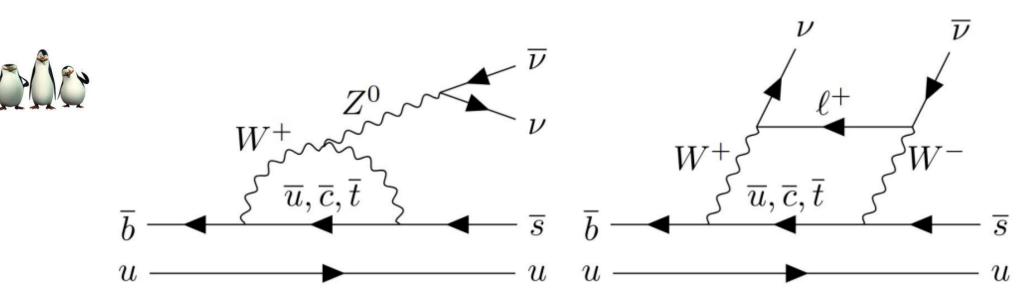
lepton momentum to isolate signal above  $B \rightarrow XIv$  background

 Background templates calibrated to control samples and sidebands



#### arXiv:2311.14647 [hep-ex] Accepted PRD

### $B^+ \rightarrow K^+ \nu \overline{\nu}$ : Motivation

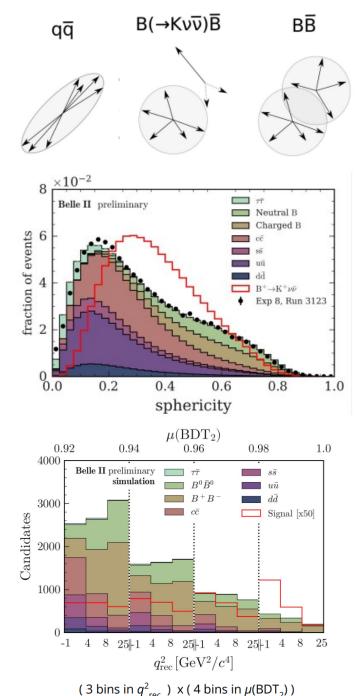


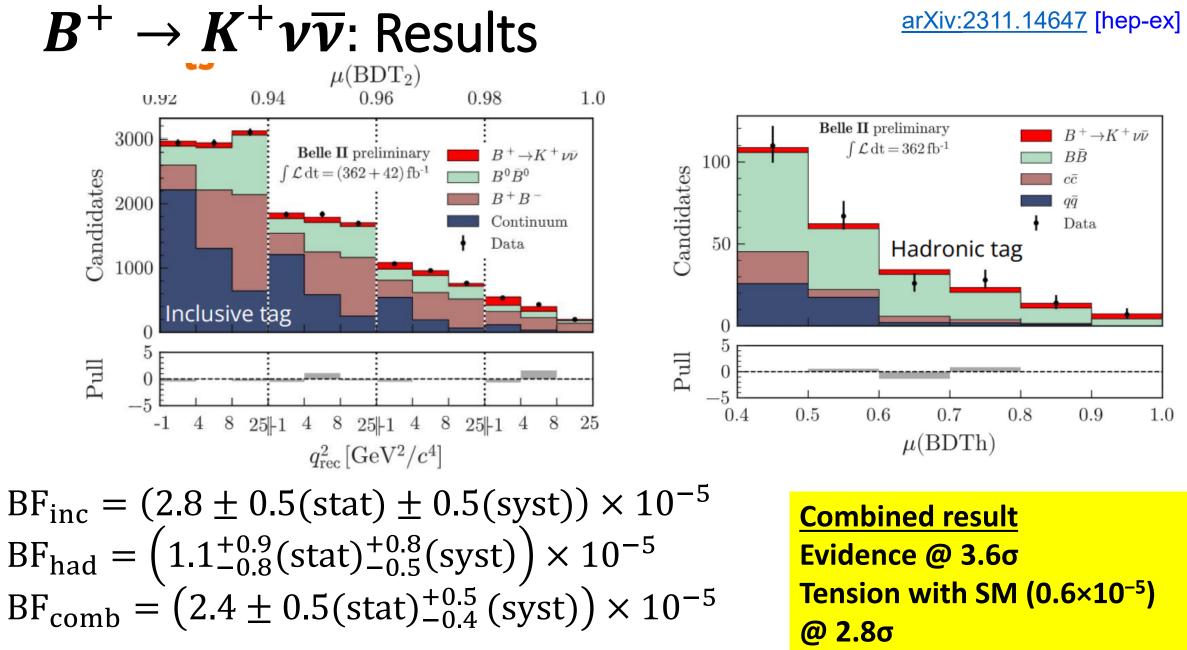
- Well known in SM but very sensitive to BSM enhancements 3<sup>rd</sup> gen
  - $B(B \rightarrow K^+ \nu \nu) = (5.6 \pm 0.4) \times 10^{-6} [arXiv:2207.13371]$
- Challenging experimentally
  - Low branching fraction with large background
  - No peak two neutrinos leads to no good kinematic constraint

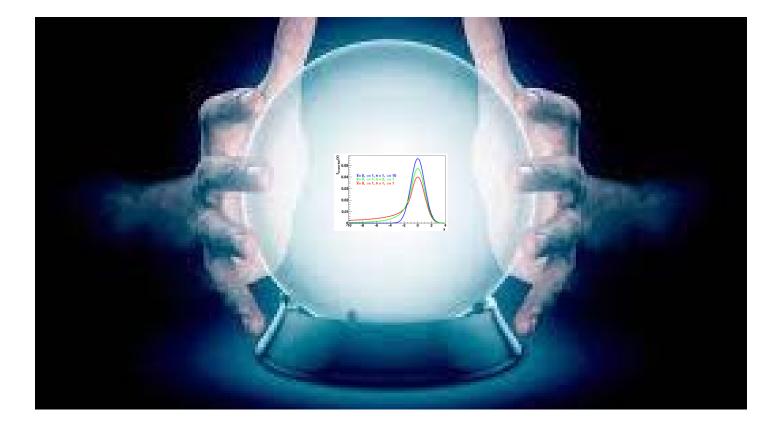
arXiv:2311.14647 [hep-ex]

### $B^+ \to K^+ \nu \overline{\nu}$ : Analysis strategy

- Two methods: an inclusive tag (8% efficiency) and conventional hadronic tag (0.4% efficiency)
  - many common features except tag
- Inclusive event variables to suppress background
  - 1. preselect events where missing momentum and signal kaon well reconstructed
  - 2. First boosted decision tree (BDT1): 12 variables
  - 3. Second BDT2: 35 variables 3 times sensitivity
  - 4. BDT2 fit extraction variable in bins of  $\nu \bar{\nu}$  mass-squared  $q^2$
- Many ystematic studies with data-driven corrections and checks with control samples





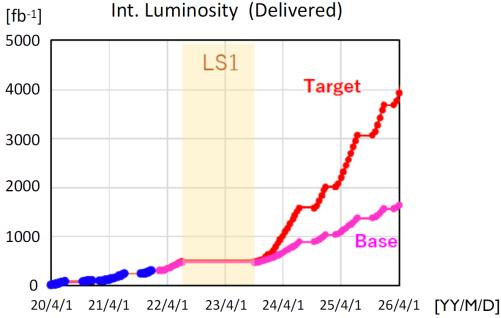


## 5) Prospects and conclusion

### Belle II: after current shutdown

- We have not collected the sample size planned to date
  - Beam conditions
- Since summer 2022 until Feb 2024 shutdown for accelerator upgrades to mitigate background and increase luminosity
- Detector upgrades too
  - two-layer pixel detector installed
- Path to 2  $\times$  10<sup>35</sup> cm  $^{-2}s^{-1}$  but new final focus to go beyond
  - Proposed upgrade from 2028+
  - see C. Checci and M. Roney next





### Goals with current data to a few inverse ab<sup>-1</sup>

- Semileptonic decay:
  - $V_{\rm cb}$  can we make progress on the inclusive vs. exclusive tension
    - KEK report in preparation
  - R(D)-R(D\*)
- Electroweak penguin
  - Missing energy modes like  $B \rightarrow K\tau\tau$  and Kvv
- CP violation
  - $\alpha$  and the **gluonic penguins**
- tau
  - LFV and precision
- Charm
  - final states with neutrals, e.g.,  $D \rightarrow \pi^0 \pi^0$
- Quarkonium
  - Y(10753) scan and isospin partners (ISR and *B* decay)
- Dark sector and low multiplicity
  - dark photon and  $e^+e^- \rightarrow \pi^+\pi^-$

Our <u>Snowmass</u> <u>submission</u> is the most up to date prospects document

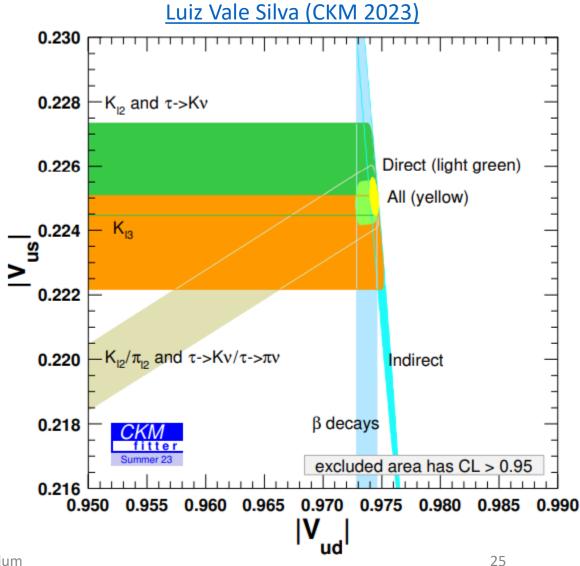
#### Conclusion

- e<sup>+</sup>e<sup>-</sup> has an important role to play in the future of flavour
  - Belle II is catching up to first generation sample size, we are producing competitive and exciting results
    - <u>37 papers</u> and 10 preliminary results with a paper in preparation
    - More before the summer with the Run 1 data
  - A lot more to come once we enter the "10<sup>35</sup> era" of Run 2 which is just starting

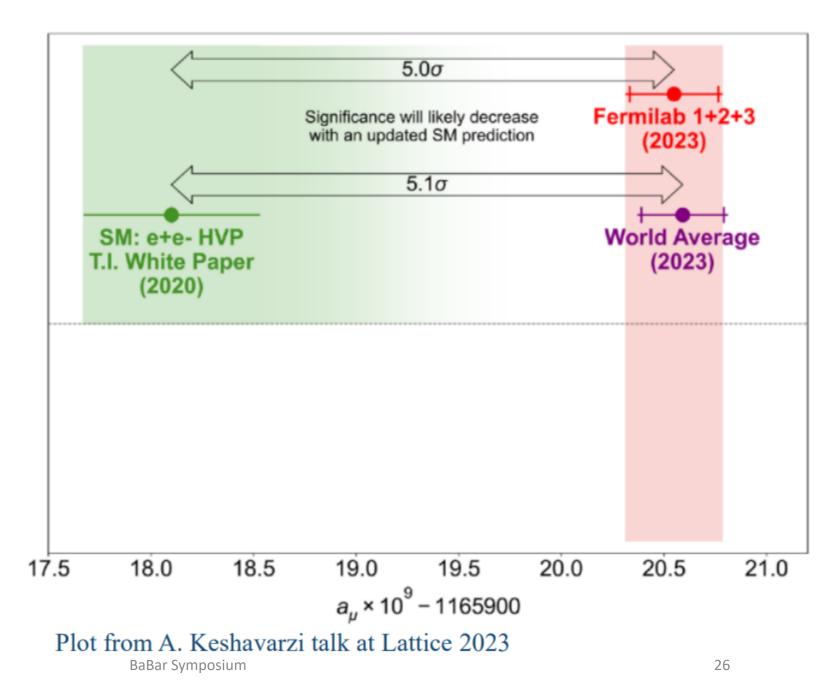
# Backup

#### Tau physics motivation II

- **Precision measurements** of the τ lepton can have significant impact
- Example:
  - first row unitarity of CKM matrix 'Cabibbo angle anomaly'
  - $B(\tau \rightarrow Kv)/B(\tau \rightarrow \pi v)$  proportional to  $|V_{us}/V_{ud}|^2$
  - Combine with lattice QCD information to provide additional constraint
- Additionally, lepton-flavour universality and dipole moments
- Mass and lifetime important inputs to these calculations

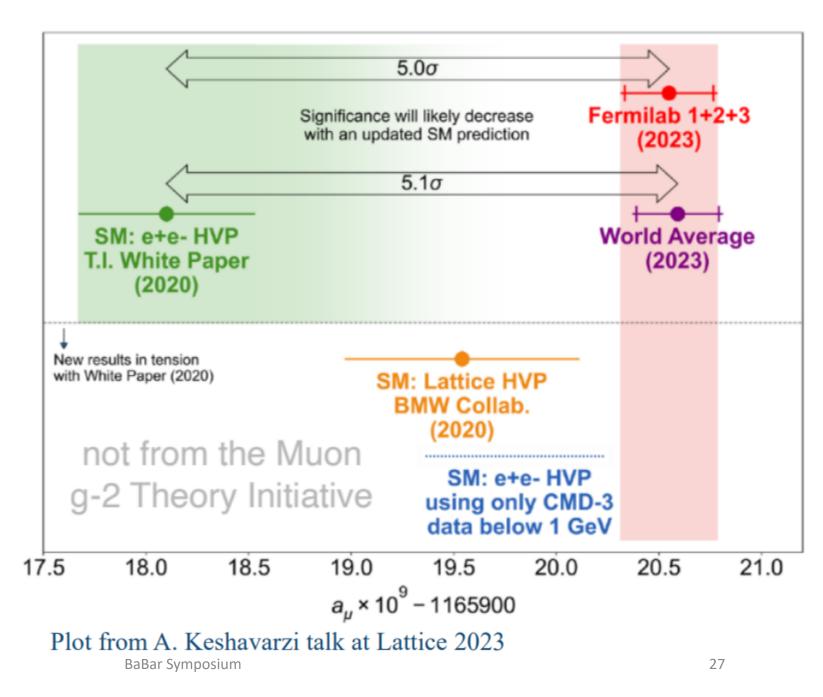


# ...away from heavy flavour muon g-2



# ...away from heavy flavour muon g-2





#### Paper in preparation

 $\sigma(e^+e^- \to \pi^+\pi^-\pi^0)$ 

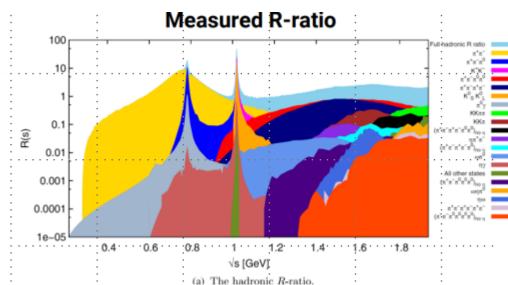
Muon anomalous magnetic moment

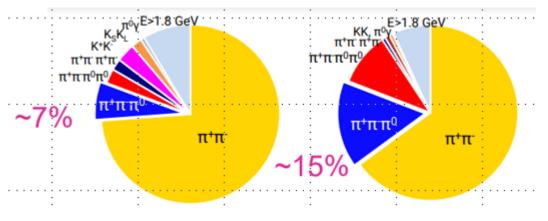
$$a_{\mu} = \frac{g^{-2}}{2} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{QCD}}$$
Hadron contribution term
$$\downarrow a_{\mu}^{\text{QCD}} = a_{\mu}^{\text{HVP}} + a_{\mu}^{\text{HLbL}}$$

$$\downarrow \text{Leading-order HVP rerm}$$

$$a_{\mu}^{\text{HVP,LO}} = \frac{\alpha^{2}}{3\pi^{2}} \int_{m_{\pi}^{2}}^{\infty} \frac{ds}{s} R(s)K(s)$$
Hadronic R-ratio
$$\downarrow R(s) = \frac{\sigma(e^{+}e^{-} \rightarrow hadrons)}{\sigma(e^{+}e^{-} \rightarrow \mu^{+}\mu^{-})}$$

2<sup>nd</sup> largest contribution to the hadronic vacuum polarization estimate as region below 1 GeV in c.m. energy dominates

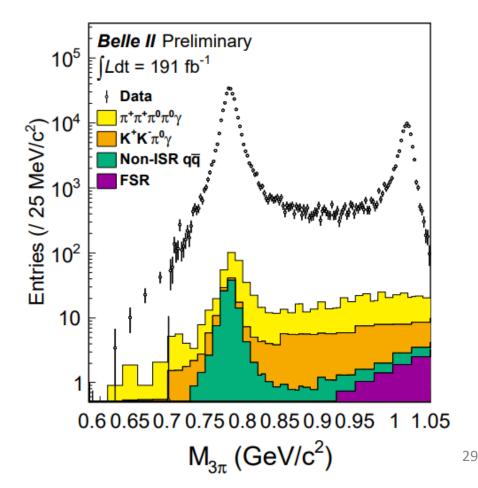




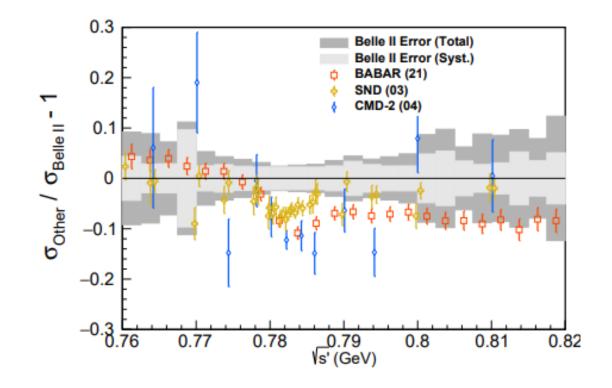
$$\sigma(e^+e^- 
ightarrow \pi^+\pi^-\pi^0)$$

- Initial-state radiation technique wide invariant mass range
- Partial Run 1 data set 191 fb<sup>-1</sup>
- Selection via kinematic fits
- Key challenge is  $\pi^0$  efficiency
  - Custom determination using  $\omega$  decay
- Background control samples for  $e^+e^- \rightarrow \pi^+\pi^-\pi^0 \pi^0\gamma_{ISR}$ ,  $e^+e^- \rightarrow q\bar{q}\gamma_{ISR}$  and  $e^+e^- \rightarrow K^+K^-\pi^0\gamma_{ISR}$

Signal process :  $e^+e^- \rightarrow \gamma_{\rm ISR}\pi^+\pi^-\pi^0(\rightarrow\gamma\gamma)$ Signal spectrum Efficiency  $\frac{dN_{\rm signal}}{dm} = \sigma_{ee \rightarrow 3\pi} \cdot \varepsilon \cdot \frac{d\mathcal{L}_{\rm eff}}{dm}$  $3\pi$  mass Cross section Effective luminosity



 $\sigma(e^+e^- \to \pi^+\pi^-\pi^0)$ 



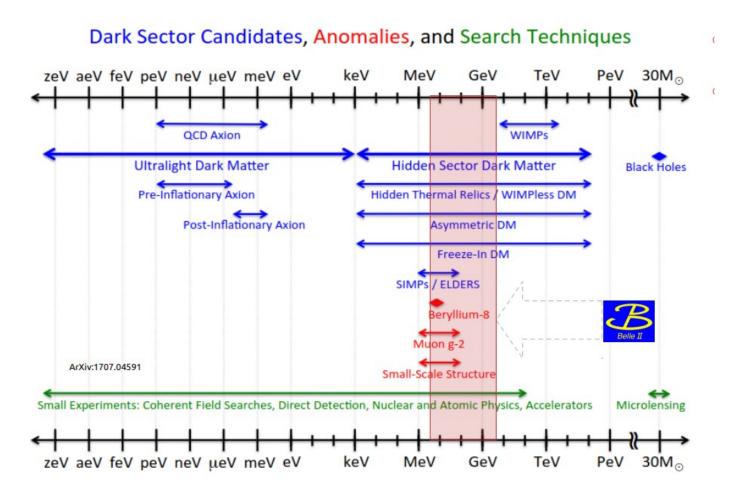
	-
Source	$0.62 - 1.05 \text{ GeV/}c^2$
Trigger	0.1 (-0.09)
ISR photon detection	0.7 (+0.15)
Tracking	0.8 (-1.35)
$\pi^0$ detection	1.0 (-1.43)
Kinematic fit $(\chi^2)$	0.6 (+0.0)
Event selection	0.2 (-1.90)
Generator	1.2
Integrated luminosity	0.6
Radiative corrections	0.5
MC statistics	0.2
Background subtraction	0.3-0.5
Unfolding	0.7 - 15
Total uncertainty	2.2-15
(Total correction $\varepsilon/\varepsilon_{\rm MC} - 1$ )	(-4.61)

$$a_{\mu}^{3\pi} = (49.02 \pm 0.23 \pm 1.07) \times 10^{-10},$$

2.6 tension with BaBar

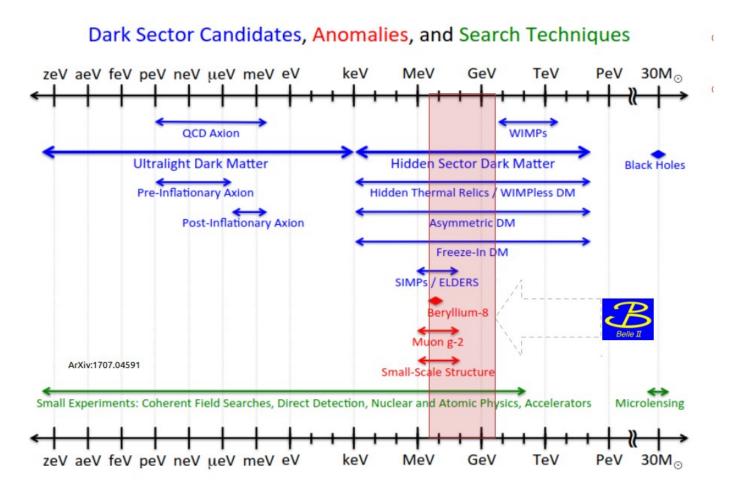
**BaBar Symposium** 

#### Light dark sector searches



- Can access the mass range favored by light dark sector
  - Possible sub-GeV scenario

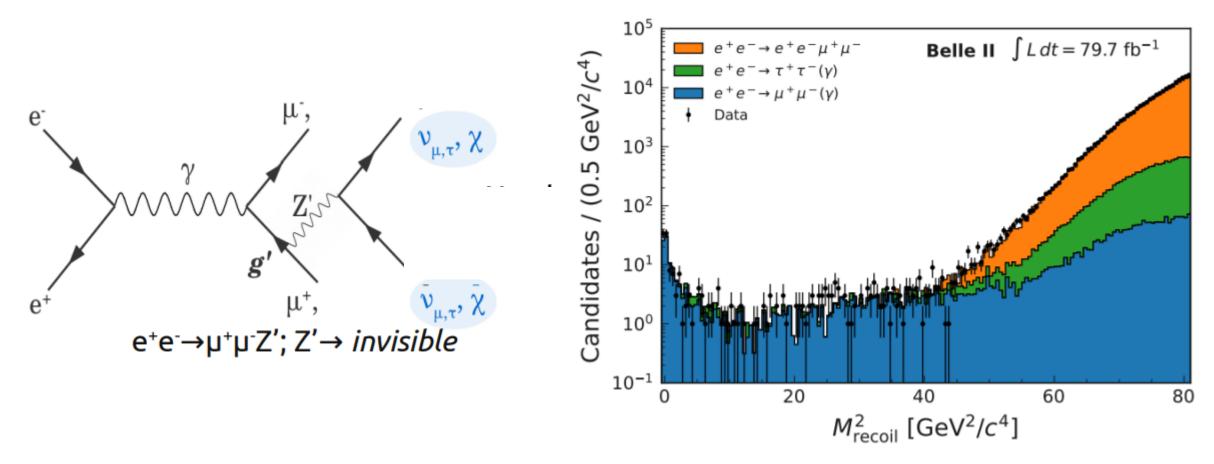
### Light dark sector searches



- Can access the mass range favored by light dark sector
  - Possible sub-GeV scenario
- DM weakly coupled to SM through a light mediator X:
  - vector (Z'/dark photon), axion like particles (ALPs), scalar (dark Higgs) or fermions (sterile v)
- Some links to anomalies, e.g., g-2

#### Invisible decay of Z' to dark matter

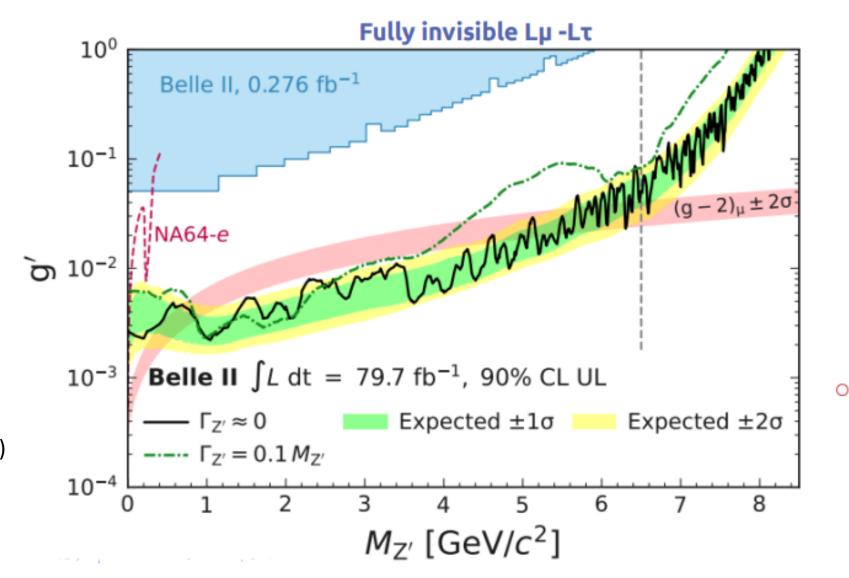
• Search for narrow peak in the recoil mass of dimuon pairs



#### Invisible decay of Z' to dark matter

- Limits on Z' coupling g' and mass
- g<sub>µ</sub>-2 region ruled out for masses from 0.8 to 5 GeV

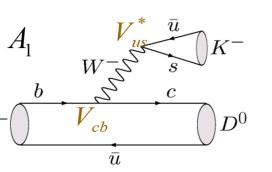
Phys. Rev. Lett. 130, 231801 (2023)

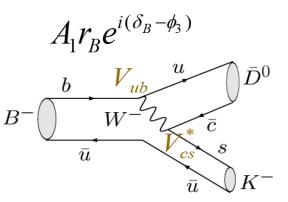


Paper in preparation

# $\gamma/\phi_3$ : power of Belle + Belle II

- Standard candle in the SM
  - Tree-level only + no theory unc.
- LHCb leads the way: γ=(63.8±3.6)°
  - <u>LHCB-CONF-2022-003</u>

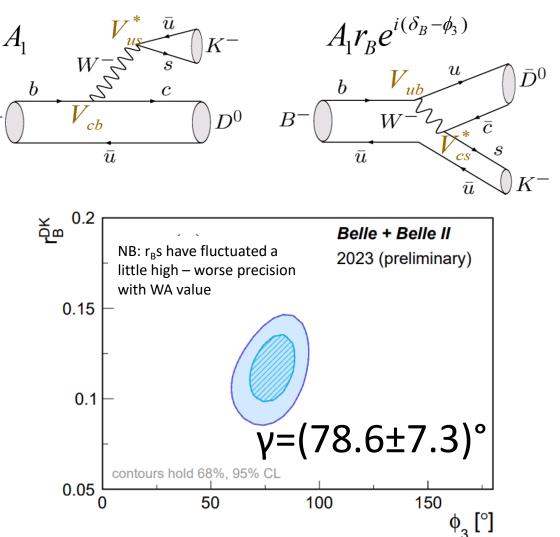




**Paper in preparation** 

# $\gamma/\phi_3$ : power of Belle + Belle II

- Standard candle in the SM
  - Tree-level only + no theory unc.
- LHCb leads the way:  $\gamma = (63.8 \pm 3.6)^{\circ}_{B}$ 
  - <u>LHCB-CONF-2022-003</u>
- Several Belle (711 fb<sup>-1</sup>) + Belle II measurements (varying sample size) – total O(1 ab<sup>-1</sup>)
  - $D \rightarrow K_{S}^{0} hh \underline{JHEP 02} (2022) 063$
  - $D \rightarrow K^0_{S} K\pi$  <u>accepted by JHEP</u>
  - $D \rightarrow K_{s}^{0} \pi^{0}$ , KK <u>arXiv:2308.05048</u>
  - + Belle-only  $D \rightarrow K\pi$  and others
- A few ab<sup>-1</sup> will give a good cross check of this SM parameter



Phys. Rev. D 109, 012001 (2024) and Phys. Rev. Lett. 131, 111803 (2023)

#### $B \rightarrow K\pi$ isospin sum rule

Relates these various penguin modes to give a null test of the SM with O(1%) SM precision – <u>PRD 59, 113002 (1999)</u>

$$I_{K\pi} = \mathcal{A}_{K^{+}\pi^{-}} + \mathcal{A}_{K^{0}\pi^{+}} \frac{\mathcal{B}(K^{0}\pi^{+})}{\mathcal{B}(K^{+}\pi^{-})} \frac{\tau_{B^{0}}}{\tau_{B^{+}}} - 2\mathcal{A}_{K^{+}\pi^{0}} \frac{\mathcal{B}(K^{+}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})} \frac{\tau_{B^{0}}}{\tau_{B^{+}}} - 2\mathcal{A}_{K^{0}\pi^{0}} \frac{\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}$$

• All inputs measured at Belle II including 'no vertex' time-dependent *CP* asymmetry for  $B \rightarrow K^0{}_s\pi^0 - 362 \text{ fb}^{-1}$  sample

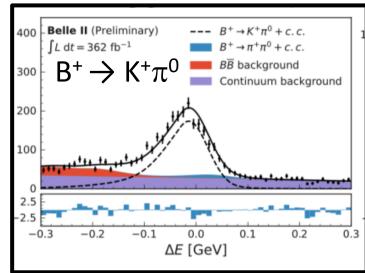
Belle II paper in preparation and PRL 131, 111803 (2023)

$$B \rightarrow K\pi$$
 isospin sum rule

Relates these various penguin modes to give a null test of the SM with O(1%) SM precision – <u>PRD 59, 113002 (1999)</u>

$$I_{K\pi} = \mathcal{A}_{K^{+}\pi^{-}} + \mathcal{A}_{K^{0}\pi^{+}} \frac{\mathcal{B}(K^{0}\pi^{+})}{\mathcal{B}(K^{+}\pi^{-})} \frac{\tau_{B^{0}}}{\tau_{B^{+}}} - 2\mathcal{A}_{K^{+}\pi^{0}} \frac{\mathcal{B}(K^{+}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})} \frac{\tau_{B^{0}}}{\tau_{B^{+}}} - 2\mathcal{A}_{K^{0}\pi^{0}} \frac{\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}$$

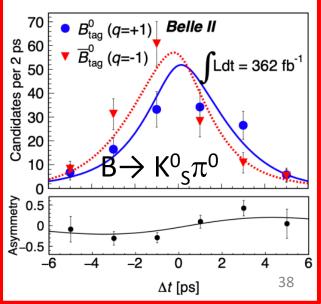
• All inputs measured at Belle II including 'no vertex' time-dependent *CP* asymmetry for  $B \rightarrow K^0_{S} \pi^0 - 362 \text{ fb}^{-1}$  sample  $70 \left[ \bullet B^0_{\text{tan}}(q=+1) \right] Belle II$ 



 $B = (14.2 \pm 0.4 \pm 0.9) \times 10^{-6}$ Large  $\pi^{0}$  efficiency syst.

> $A_{K^0} = -0.01 \pm 0.12 \pm 0.05$ Combination of time-dependent and time-integrated analyses

> > BaBar Symposium

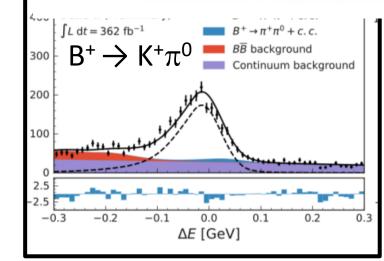


Belle II paper in preparation and <u>arXiv:2305.07555</u> (accepted PRL)

- $B \rightarrow K\pi$  isospin sum rule
- Relates these various penguin modes to give a null test of the SM with O(1%) SM precision <u>PRD 59, 113002 (1999)</u>

$$I_{K\pi} = (-3 \pm 13 \pm 5)\%$$

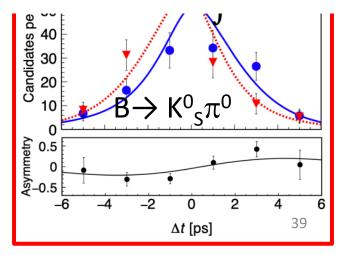
Agrees with SM. Competitive with WA:  $(-13 \pm 11)$ %.



Large  $\pi^0$  efficiency syst.

 $A_{K^0} = -0.01 \pm 0.12 \pm 0.05$ Combination of time-dependent and time-integrated analyses

BaBar Symposium

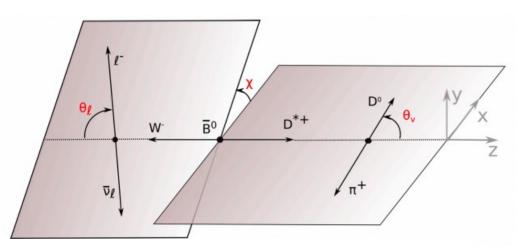


C. Schwanda talk – WG2

Belle paper in preparation

## Angular coefficients in $B \rightarrow D^* lv$ and $V_{cb}$

- Measure 4D-differential distribution in terms of decay angles and w
  - overall proportionality to  $|V_{cb}|^2$
  - w≥1 is the hadronic recoil parameter relates to mom. transfer to the leptonic system

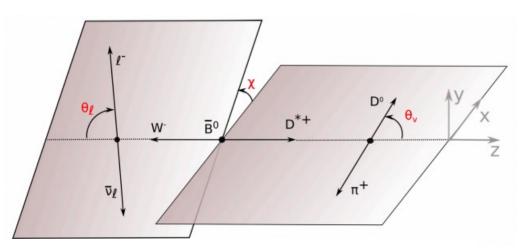


C. Schwanda talk – WG2

Belle paper in preparation

## Angular coefficients in $B \rightarrow D^* lv$ and $V_{cb}$

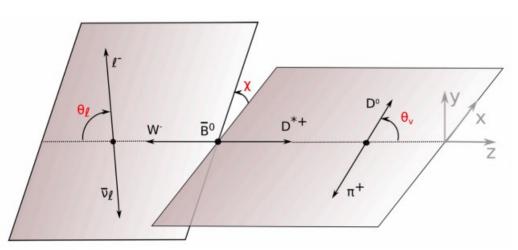
- Measure 4D-differential distribution in terms of decay angles and w
  - overall proportionality to  $|V_{cb}|^2$
  - w≥1 is the hadronic recoil parameter relates to mom. transfer to the leptonic system
- Extract 12 angular coefficients of the distribution in bins of w for the first time using full Belle 711 fb<sup>-1</sup> sample
  - hadronically tagged

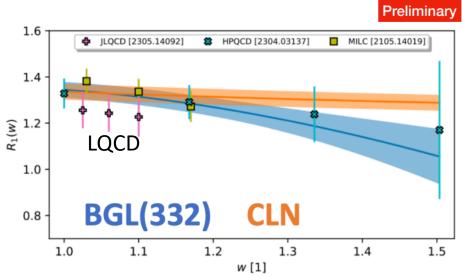


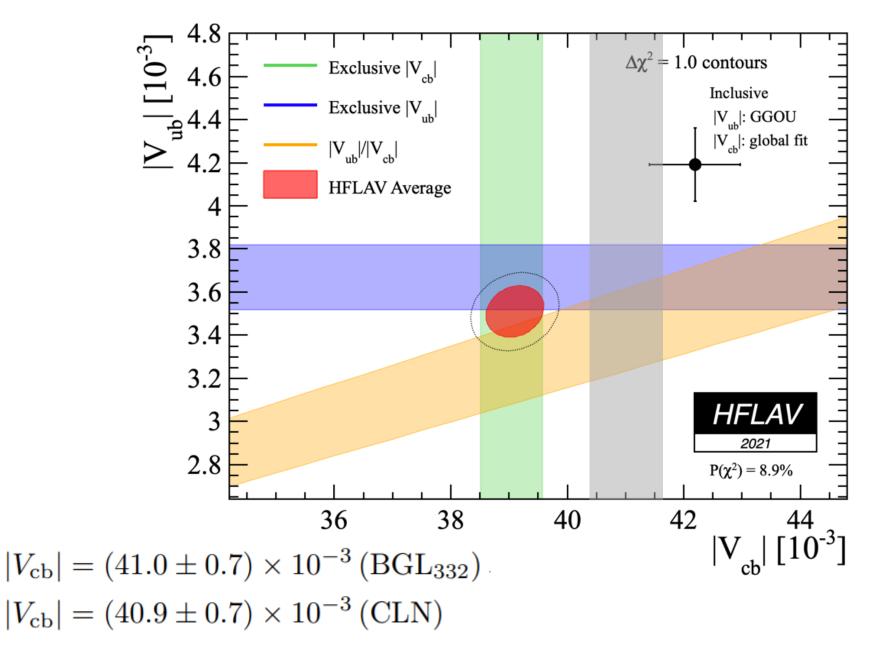
Belle paper in preparation

# Angular coefficients in $B \rightarrow D^* lv$ and $V_{cb}$

- Measure 4D-differential distribution in terms of decay angles and w
  - overall proportionality to  $|V_{cb}|^2$
  - w≥1 is the hadronic recoil parameter relates to mom. transfer to the leptonic system
- Extract 12 angular coefficients of the distribution in bins of w for the first time using full Belle 711 fb<sup>-1</sup> sample
  - hadronically tagged
- Fit performed to coefficients in different form-factor parameterizations and with LQCD inputs to extract V<sub>cb</sub> as well as parameters of the form-factor model
  - WA BF also taken externally

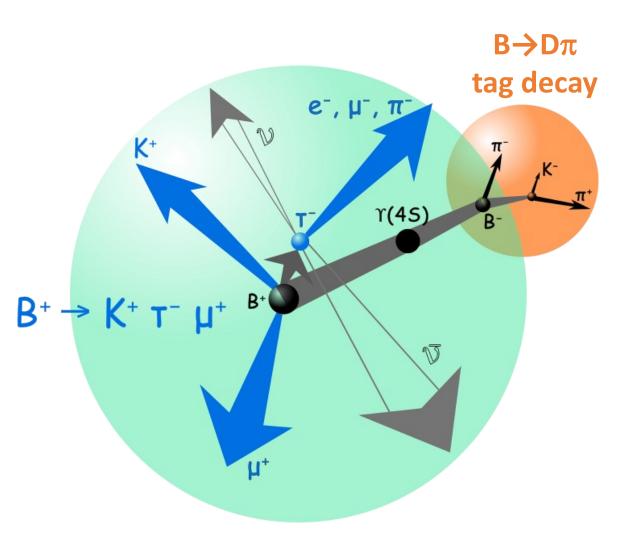






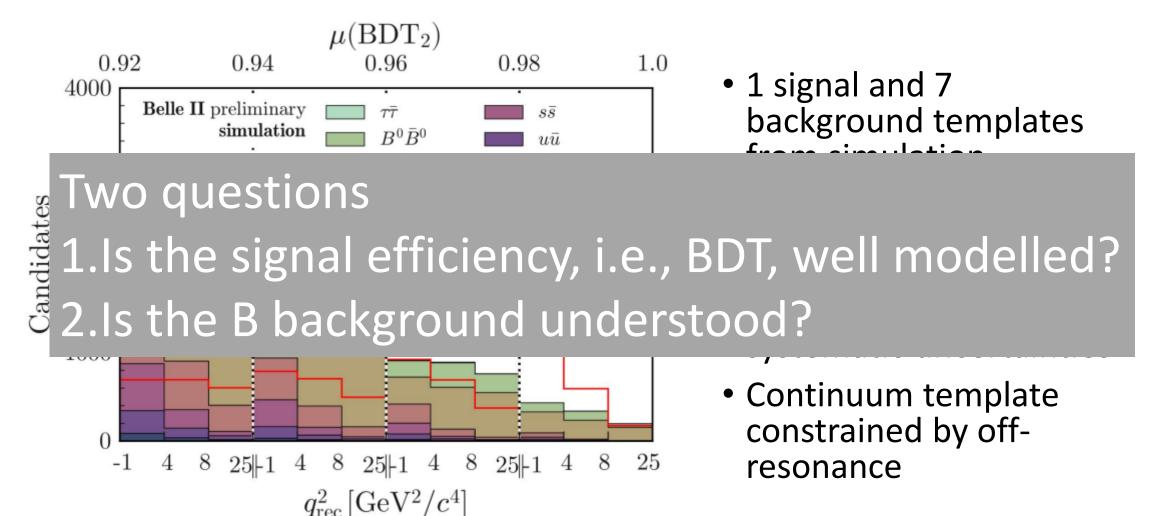
## Hadronic tag

- Full-reconstruction of one B decay in a large number of high BF modes on one side
  - $B \rightarrow D^{(*)0}\,m\pi^{\pm}n\pi^{0}$  , where  $m{\geq}1$  n  ${\geq}0$
  - BaBar Reconstruct other B as signal with missing energy
- Machine learning algorithm used to boost efficiency as much as possible
- Total efficiency < 1% but a powerful tool
- Requires calibration



arXiv:2311.14647 [hep-ex]

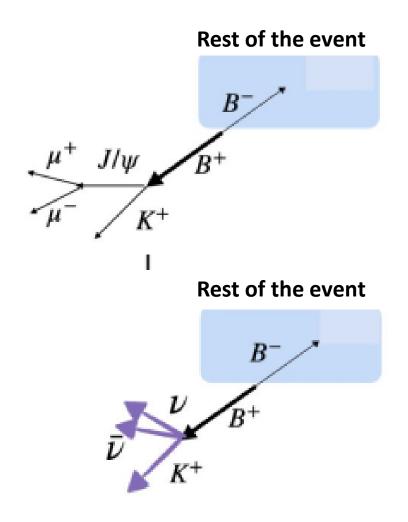
## $B^+ \rightarrow K^+ \nu \overline{\nu}$ : Inclusive signal extraction

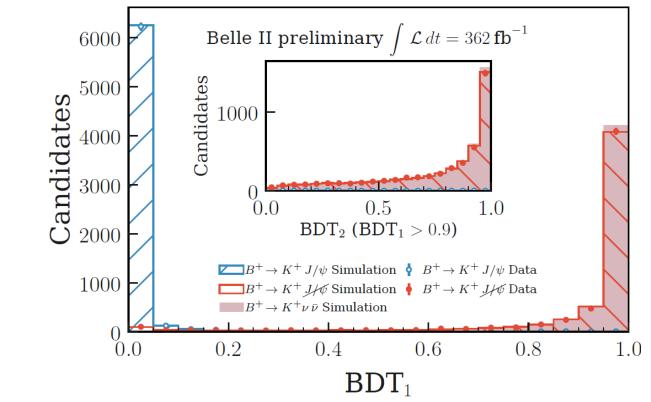


(3 bins in  $q_{rec}^2$ ) x (4 bins in  $\mu(BDT_2)$ )

arXiv:2311.14647 [hep-ex]

## $B^+ \rightarrow K^+ \nu \overline{\nu}$ : Efficiency validation



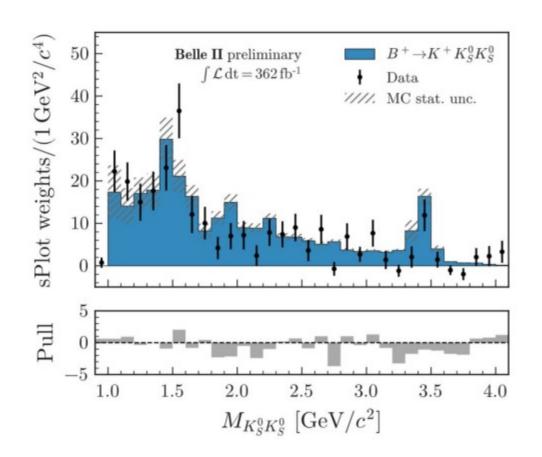


Ratio between selection on data and simulation for the control sample 1 with 3% uncertainty

BaBar Symposium

arXiv:2311.14647 [hep-ex]

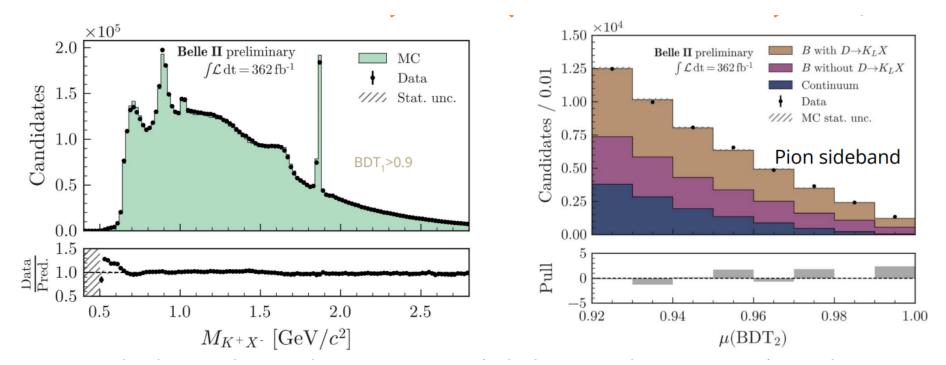
### $B^+ \rightarrow K^+ \nu \overline{\nu}$ : Background validation example



- An example of a difficult background is charmless  $B^+ \rightarrow K^+ K_L^0 K_L^0$ , where  $K_L^0$  mesons escape detection
  - has an order of magnitude larger BF than signal
- Dedicated studies  $B^+ \rightarrow K^+ K^0_S K^0_S$  show good modelling
  - generous systematics assigned
- Similar studies for  $B^+ \rightarrow K^+ n \overline{n}, B^+ \rightarrow K^+ K_L^0 K_S^0$

#### $B^+ \rightarrow K^+ \nu \overline{\nu}$ :

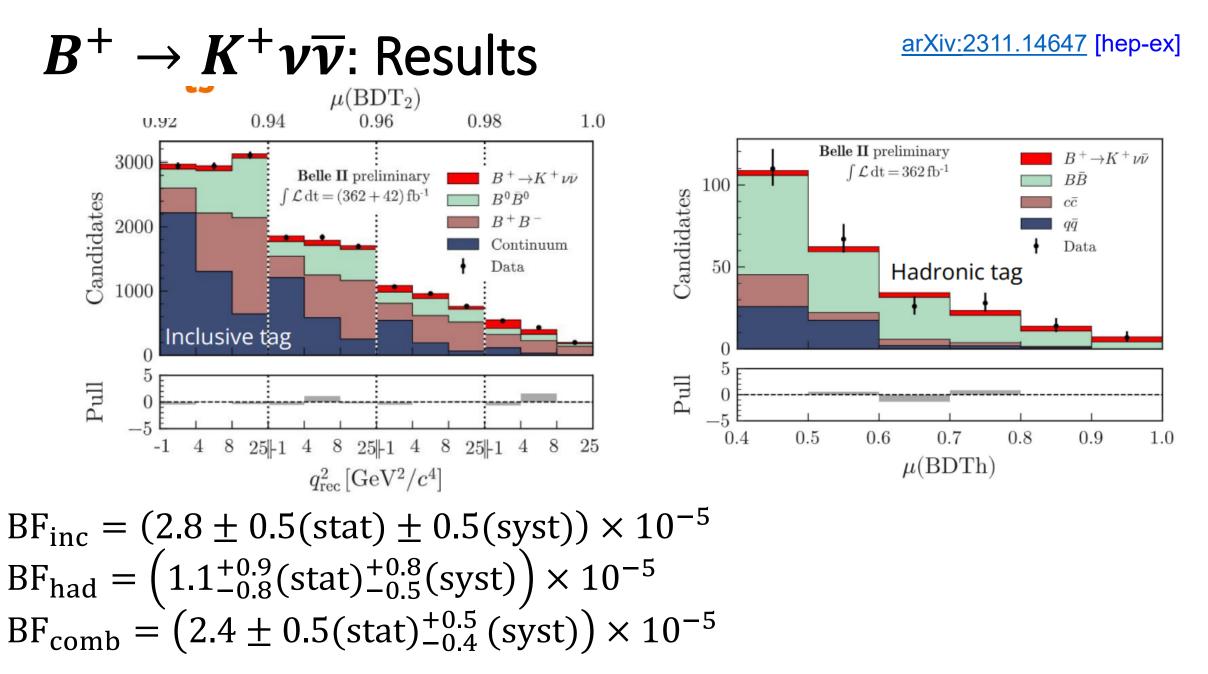
## >90% background from $B \rightarrow D(K^+X) | v + B \rightarrow D(K_LX)K^+$



- KX system agrees well between data and MC
- Prompt K<sup>+</sup> production studied using prompt  $\pi^+$  from B<sup>+</sup> $\rightarrow \pi^+$ X decays
- Systematic uncertainties on decay branching fractions, enlarged for  $D{\rightarrow}K_L X$  and  $B \rightarrow D^{**}I \, v$

## $B^+ \rightarrow K^+ \nu \overline{\nu}$ : Systematic uncertainties

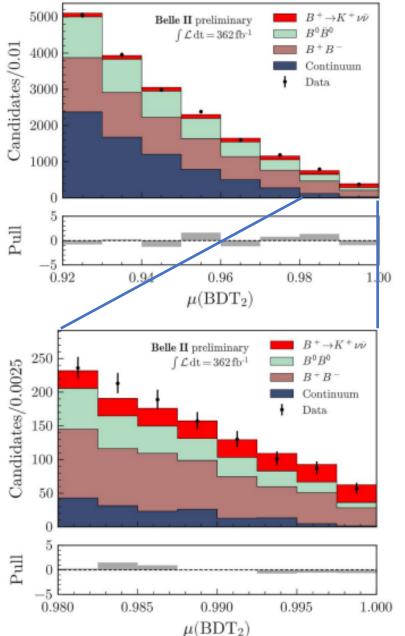
Source	Correction	Uncertainty type	Uncertainty size	Impact on $\sigma_{\mu}$
Normalization of $B\bar{B}$ background		Global, 2 NP	50%	0.88
Normalization of continuum background		Global, 5 NP	50%	0.10
Leading B-decays branching fractions		Shape, 5 NP	O(1%)	0.22
Branching fraction for $B^+ \to K^+ K^0_{\rm L} K^0_{\rm L}$	$q^2$ dependent $O(100\%)$	Shape, 1 NP	20%	0.49
$p$ -wave component for $B^+ \to K^+ K^0_{\rm S} K^0_{\rm L}$	$q^2$ dependent $O(100\%)$	Shape, 1 NP	30%	0.02
Branching fraction for $B \to D^{(**)}$		Shape, 1 NP	50%	0.42
Branching fraction for $B^+ \to n\bar{n}K^+$	$q^2$ dependent $O(100\%)$	Shape, 1 NP	100%	0.20
Branching fraction for $D \to K_L X$	+30%	Shape, 1 NP	10%	0.14
Continuum background modeling, BDT <sub>c</sub>	Multivariate $O(10\%)$	Shape, 1 NP	100% of correction	0.01
Integrated luminosity	_	Global, 1 NP	1%	< 0.01
Number of $B\bar{B}$	· · · · · · · · · · · · · · · · · · ·	Global, 1 NP	1.5%	0.02
Off-resonance sample normalization		Global, 1 NP	5%	0.05
Track finding efficiency	_	Shape, 1 NP	0.3%	0.20
Signal kaon PID	$p, \theta$ dependent $O(10 - 100\%)$	Shape, 7 NP	O(1%)	0.07
Photon energy scale		Shape, 1 NP	0.5%	0.08
Hadronic energy scale	-10%	Shape, 1 NP	10%	0.36
$K_{\rm L}^0$ efficiency in ECL	-17%	Shape, 1 NP	8%	0.21
Signal SM form factors	$q^2$ dependent $O(1\%)$	Shape, 3 NP	O(1%)	0.02
Global signal efficiency		Global, 1 NP	3%	0.03
MC statistics		Shape, $156 \text{ NP}$	O(1%)	0.52

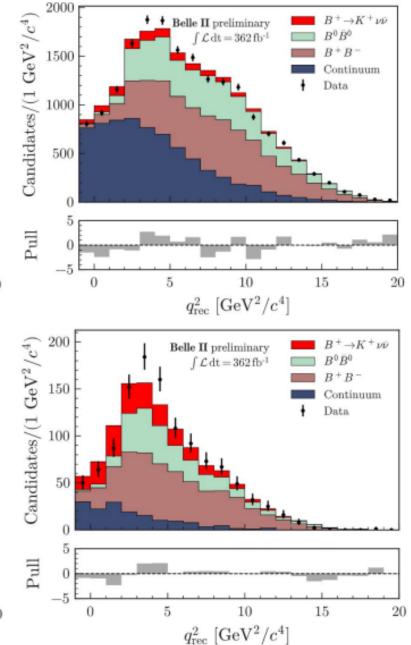


## Post-fit distributions

Upper: full fit region

Lower: most sensitive region

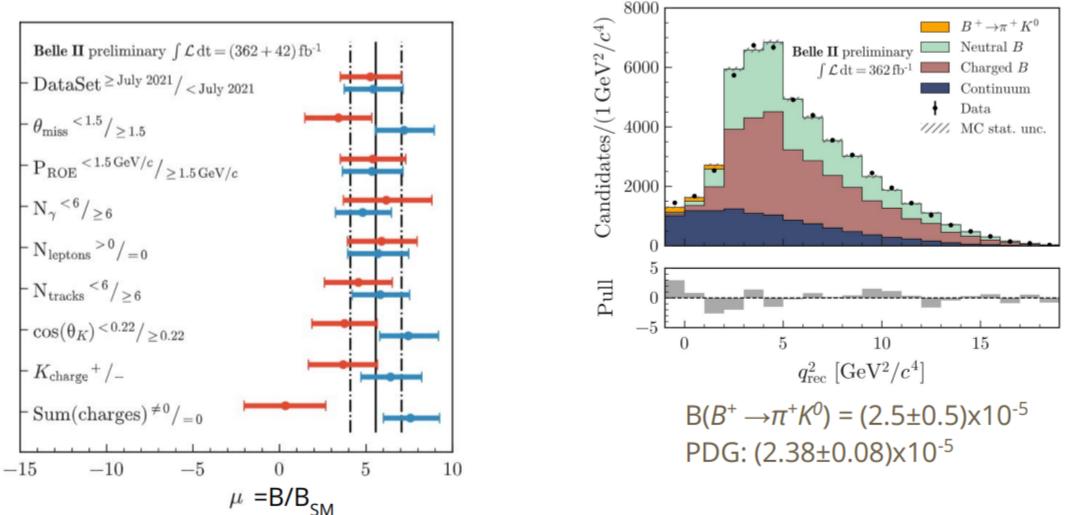




arXiv:2311.14647 [hep-ex]

#### **Cross checks**

arXiv:2311.14647 [hep-ex]



- Multiple checks of the analyses stability, including tests dividing data into approximately equal sub-samples. Reported here as measured branching fraction divided by SM expectation,  $\mu = B/B_{SM}$ .
- Control measurement of  $B^+ \rightarrow \pi^+ K^0$  decay

Slide from S. Glazov EPS