



Quantum Decoherence Activities at the University of Hawai'i

Timothy Mahood* & Lucas Stoetzer^a

Belle II Summer School - University of Mississippi

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University of Hawaii at Manoa

*mahood@hawaii.edu, ^alucassto@hawaii.edu

Define: Entanglement and Decoherence

Entanglement



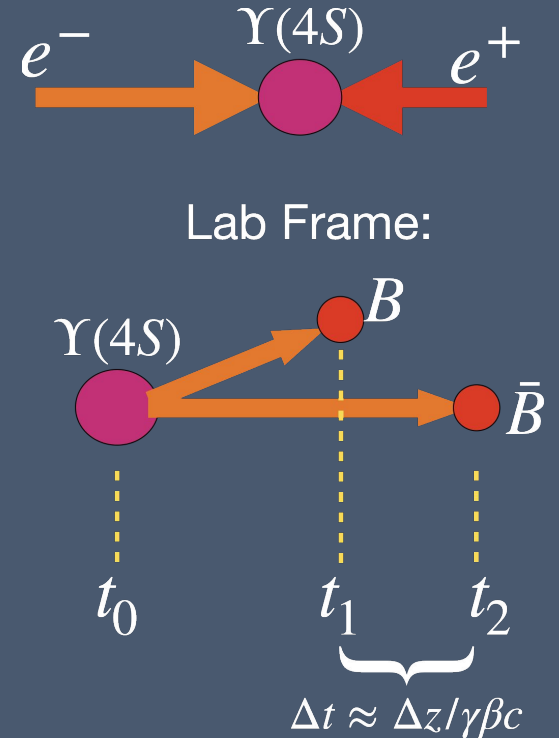
Decoherence



- When the $BB \square$ decay at the **same time ($\Delta t=0$)**, one is tagged to be the B , which makes the other **instantaneously the $B \square$**
- **Decoherence would allow same flavor \rightarrow Interesting to test!**

Using B-Factories for probing quantum effects

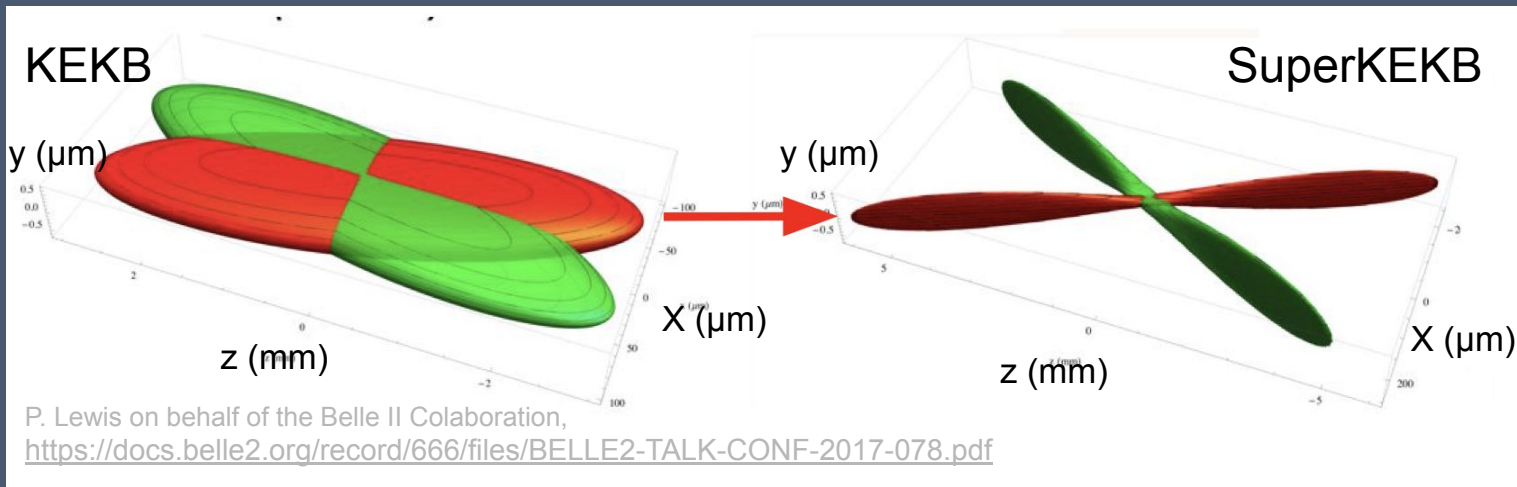
- About SuperKEKB:
 - Main purpose → produce B-meson pairs that are **quantum entangled**
 - $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$
 - Asymmetric beam energies result in boost and displaced B vertices $\Delta z \approx 200 \mu\text{m}$
 - Δz gives the decay time difference
 - **Absolute decay times t_1 & t_2 were not accessible in Belle, but how about Belle II?**



Improvements to KEKB

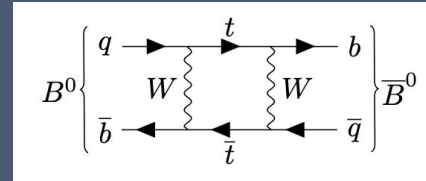
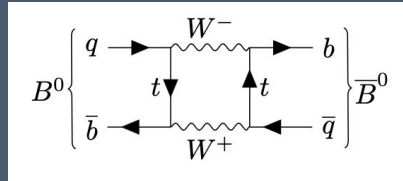
- Upgrade to SuperKEKB resulted in an increase of luminosity
- Achieved by beam focusing (“**Nanobeam collision scheme**”) using the final-focus superconducting magnet system (QCS)

	KEKB	SuperKEKB
σ_x	150 μm	10 μm
σ_y	940 nm	50 nm
σ_z , eff	7 mm	0.25 mm



BB \square quantum entanglement

$$|\Psi(t)\rangle = \frac{e^{-t/\tau_{B^0}}}{\sqrt{2}} \left[|B^0(\vec{p})\bar{B}^0(-\vec{p})\rangle - |\bar{B}^0(\vec{p})B^0(-\vec{p})\rangle \right] \text{ (Eq. 1)}$$

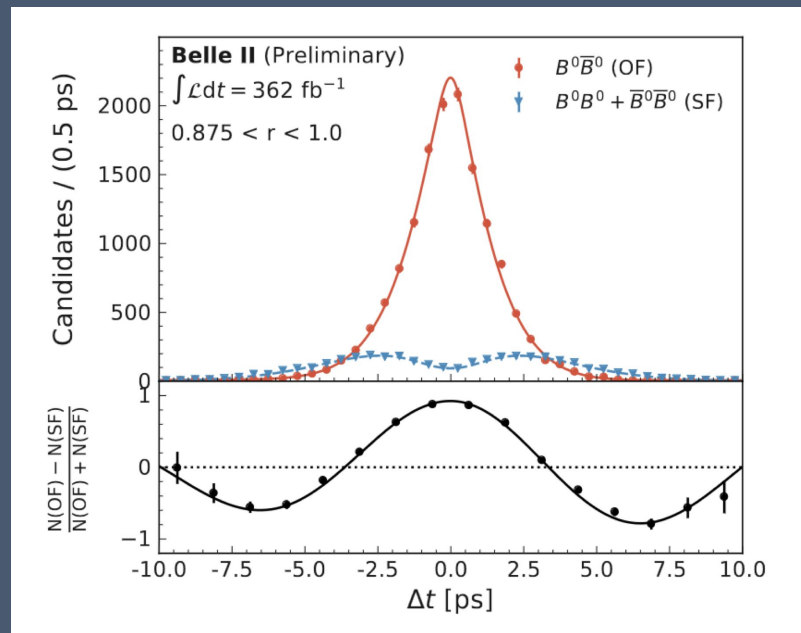


- In an $\Upsilon(4S) \rightarrow B\bar{B}$ decay the **initial state has C=-1 charge conjugation**
- In **strong interaction, charge conjugation must be conserved** \rightarrow The **BB \square pair** has to be **flavor entangled!**
- If the first meson decays at t_1 (flavor known) ...
 - ... the other meson collapse into the flavor opposite state
 - ... however, the second meson can still undergo mixing

BB \square quantum entanglement

- Up to now, flavor entanglement assumed “perfect” in B-mixing analysis
- But, searches for deviations from nominal mixing are desirable
- Belle II very well suited for this:
 - More data
 - Better vertex resolution
 - Smaller interaction point region \rightarrow access absolute decay times

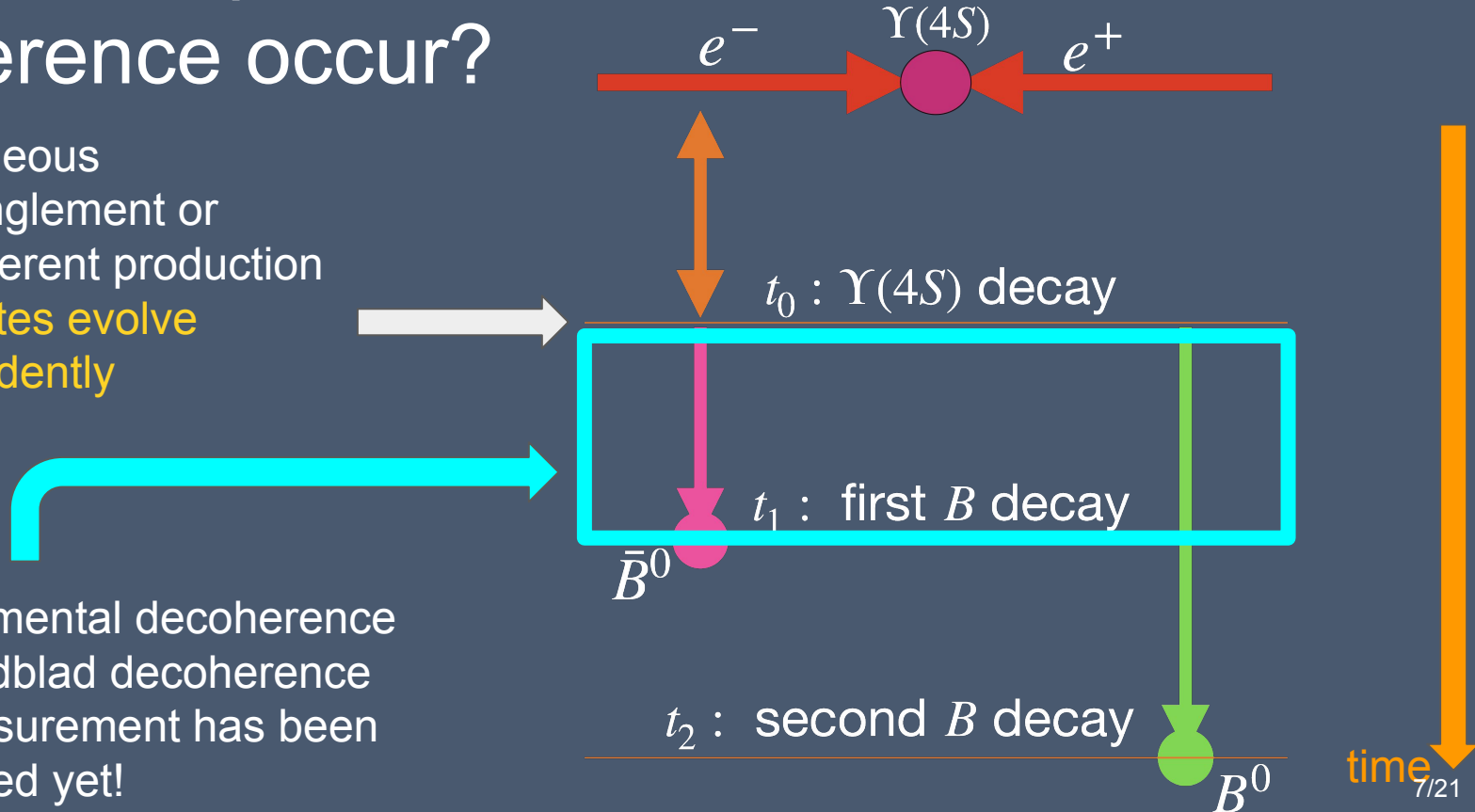
I. Adachi et al, <https://arxiv.org/pdf/2402.17260>



When does spontaneous and environmental decoherence occur?

- Spontaneous disentanglement or non-coherent production
→ B states evolve independently

- Environmental decoherence
- E.g. Lindblad decoherence
- No measurement has been performed yet!



First approaches at Belle

- Attempts to measure EPR-type flavor entanglement at Belle by A. Go 2007
- Two models where tested
 - Pompili-Selleri hidden variable model
 - Spontaneous Disentanglement of all BB pairs
- **Both models depend on the absolute decay times, not accessible at Belle!**
- Determine the asymmetry by $B \rightarrow D^{*-} \ell \nu$ decays and integrating out the absolute time dependence

Pompili-Selleri model:

$$A_{\text{PS}}^{\text{max}}(t_1, t_2) = 1 - |\{1 - \cos(\Delta m_d \Delta t)\} \cos(\Delta m_d t_{\text{min}}) + \sin(\Delta m_d \Delta t) \sin(\Delta m_d t_{\text{min}})|, \text{ and} \quad (3)$$

$$A_{\text{PS}}^{\text{min}}(t_1, t_2) = 1 - \min(2 + \Psi, 2 - \Psi), \text{ where} \quad (4)$$

$$\Psi = \{1 + \cos(\Delta m_d \Delta t)\} \cos(\Delta m_d t_{\text{min}}) - \sin(\Delta m_d \Delta t) \sin(\Delta m_d t_{\text{min}}). \quad (5)$$

Spontaneous Disentanglement:

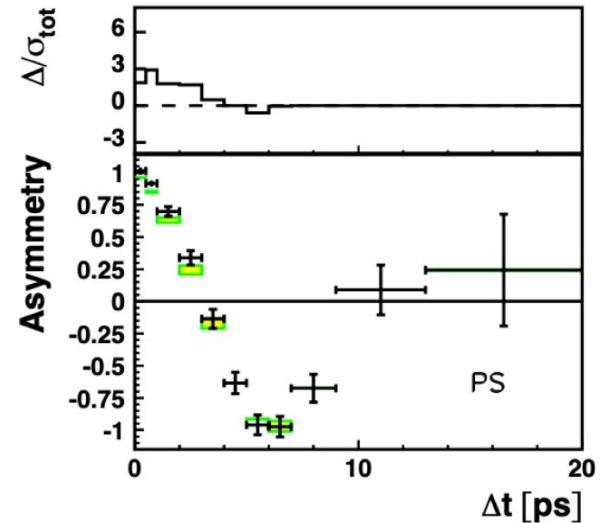
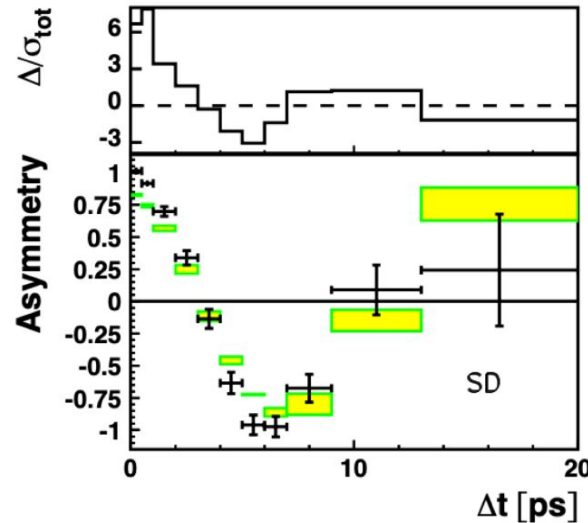
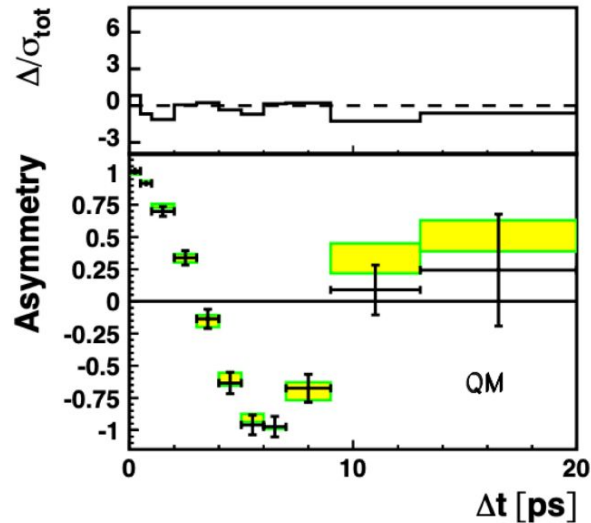
$$A_{\text{SD}}(t_1, t_2) = \cos(\Delta m_d t_1) \cos(\Delta m_d t_2) \quad (2)$$

$$= \frac{1}{2} [\cos(\Delta m_d (t_1 + t_2)) + \cos(\Delta m_d \Delta t)],$$

A. Go et al, <https://arxiv.org/pdf/quant-ph/0702267>

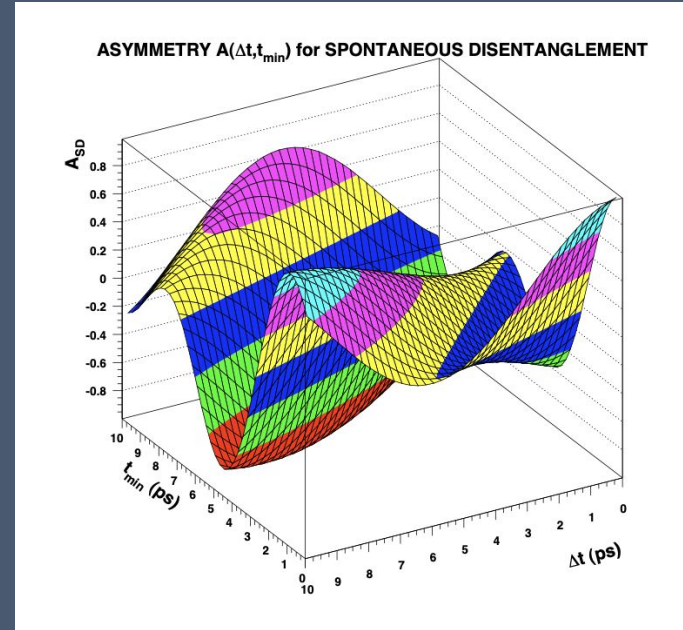
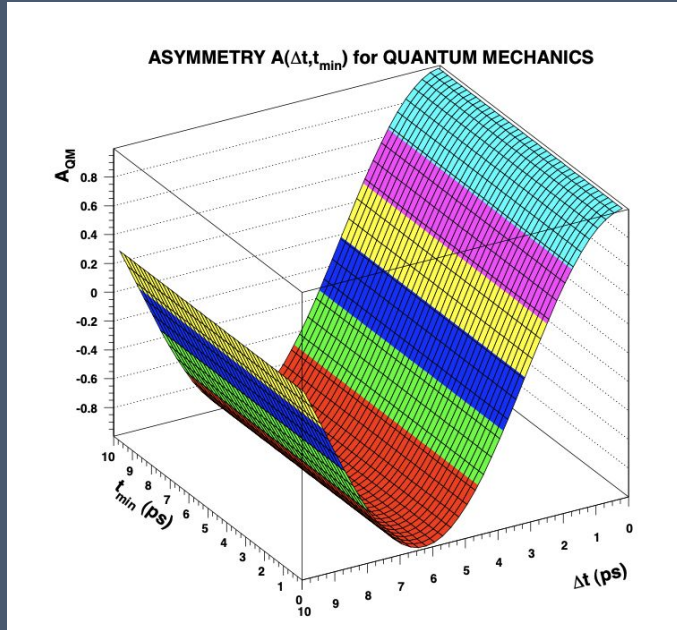
First approaches at Belle

A. Go et al, <https://arxiv.org/pdf/quant-ph/0702267>



- Total spontaneous disentanglement disfavored by 13σ
- Pompili-Selleri model disfavored by 5.1σ
- Also tested **fractional spontaneous disentanglement** $\rightarrow (3 \pm 6)\%$

The power of individual B-meson decay times



B. D. Yabsley, <https://arxiv.org/pdf/0810.1822>

- In QM only depend on Δt
- For disentanglement & decoherence, absolute time is an additional dimension
- Possible increase of sensitivity through t_1, t_2

Lindblad Type Decoherence

With our form of Lindblad type decoherence (decoherence via environmental interaction), the time-evolution of the $B^0\bar{B}^0$ pair can be written as:

$$\frac{d\rho}{dt} = -iH\rho + i\rho H^\dagger - D[\rho]$$

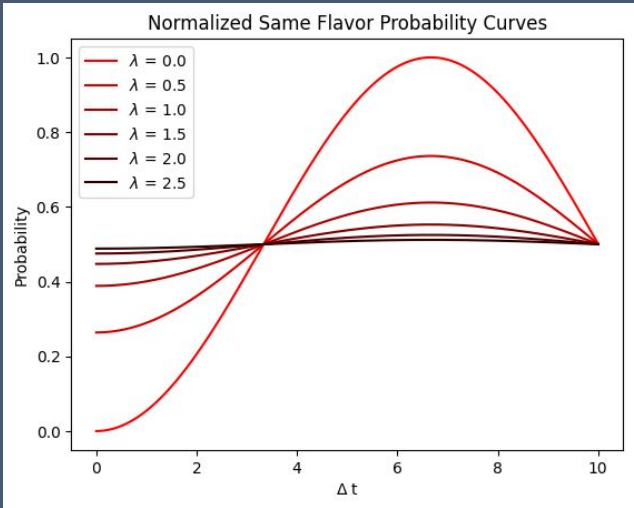
$$D[\rho] = \lambda (P_1\rho P_2 + P_2\rho P_1)$$

λ parameterizes the strength of decoherence

R.A. Bertlmann and W. Grimus
<https://arxiv.org/abs/hep-ph/0101160> (decoherence term)

This leads to a decoherence-dependent flavour distribution:

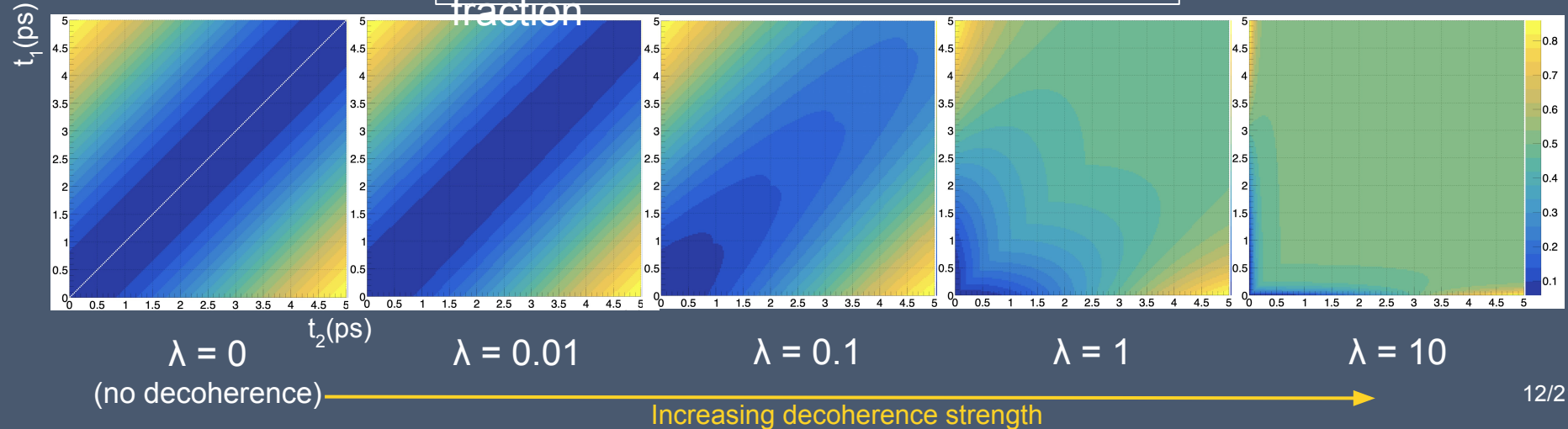
$$P = \frac{\cosh(\frac{\Delta\Gamma\Delta t}{2}) - \mu e^{-\lambda t} \cos(\Delta m\Delta t)}{2 \cosh(\frac{\Delta\Gamma\Delta t}{2})}$$



Modeling Decoherence

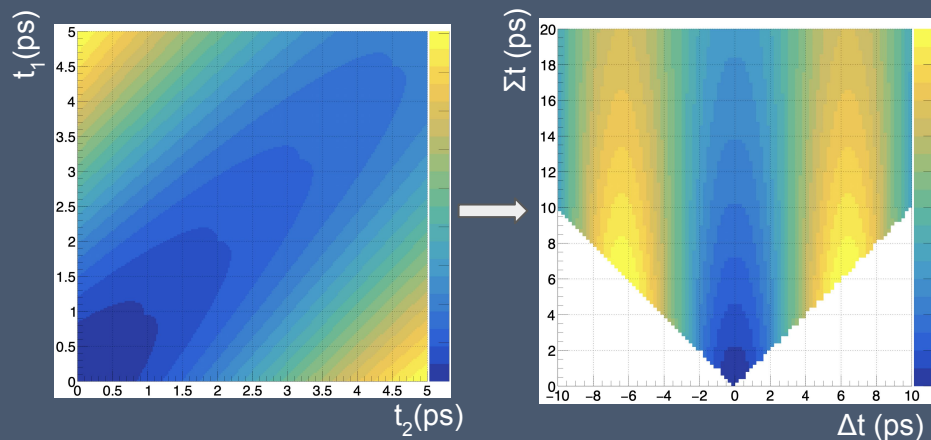
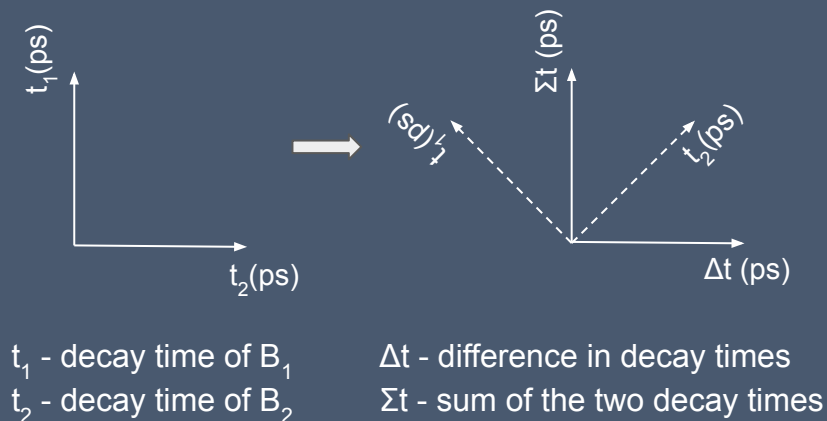
We see that increasing decoherence “washes out” the flavour correlation between the two B mesons. This decoherence pattern is distinct from mis-tagging.

$N_{BB}/(N_{BB} + N_{\bar{B}\bar{B}})$: Same-flavour fraction

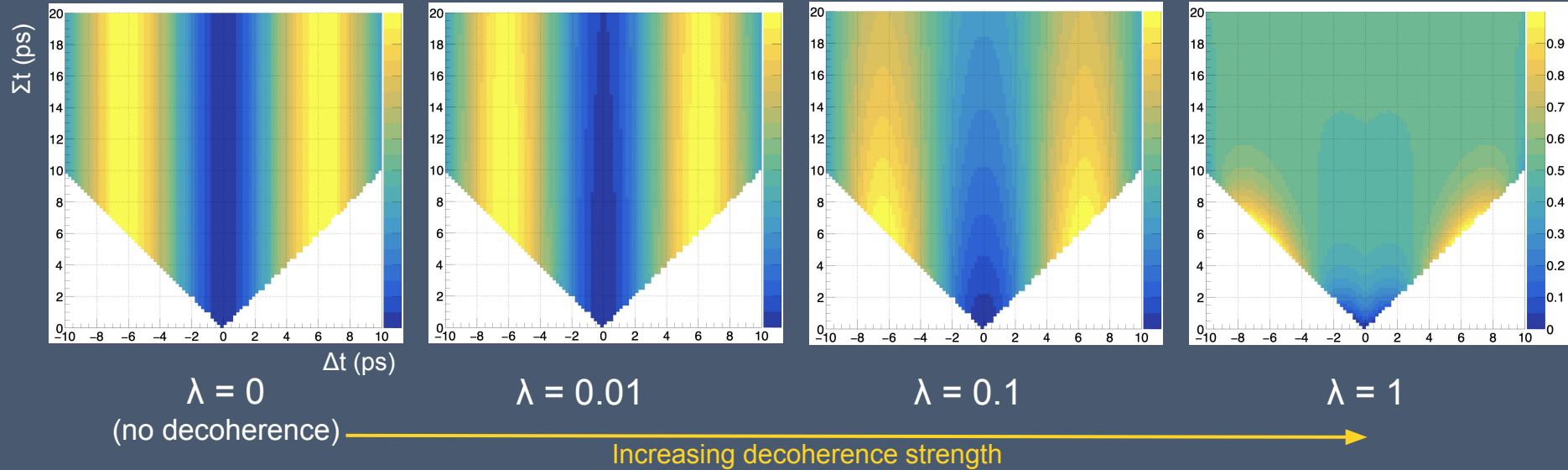


Modeling Decoherence

Changing basis to one that we can have access to at Belle II:



Modeling Decoherence

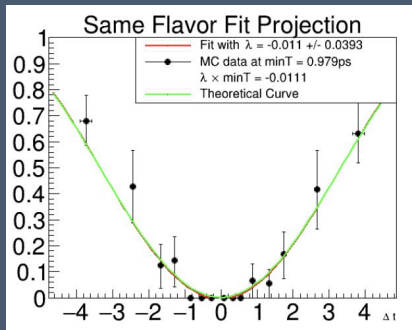


The flavour oscillation's dependence on absolute lifetime (Σt) grants us sensitivity.

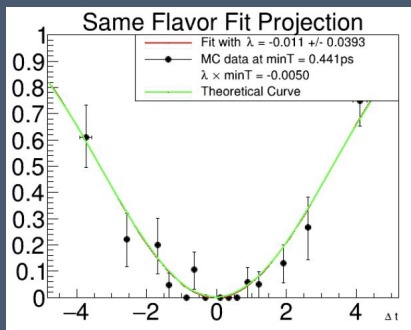
Σt is used here, but we can equivalently use one of the individual decay times.

Modeling Decoherence

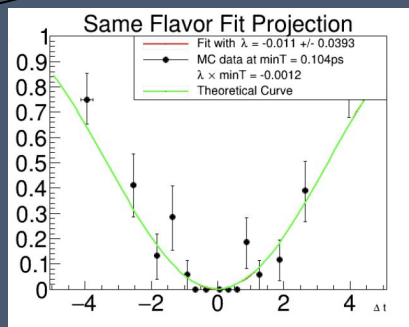
$$\lambda_{\text{gen}} = 0$$



$t_{\text{min}} = 0.979\text{ps}$

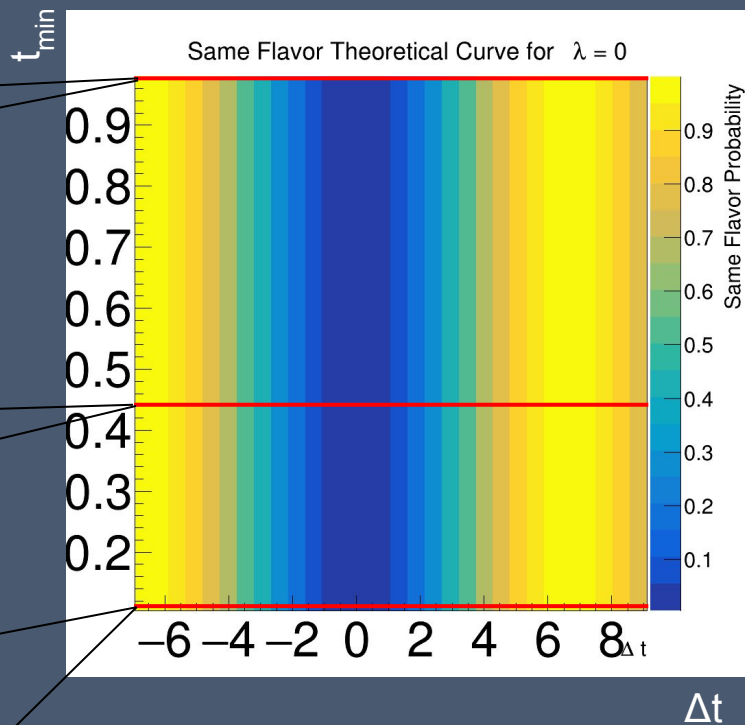


$t_{\text{min}} = 0.441\text{ps}$



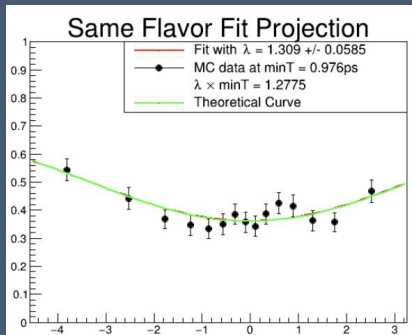
$t_{\text{min}} = 0.104\text{ps}$

$$\lambda_{\text{fit}} = -0.011 \pm 0.0393$$

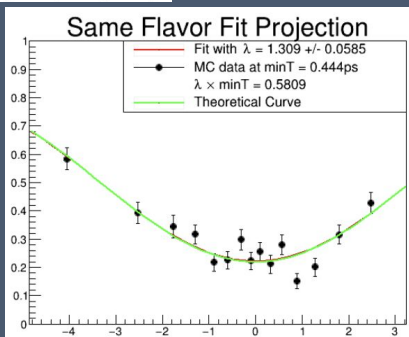


Modeling Decoherence

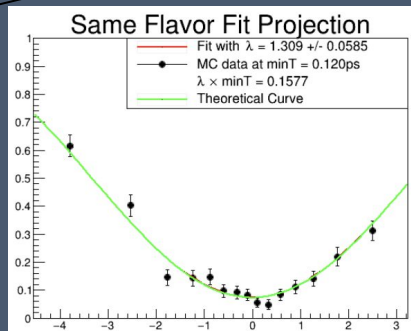
$$\lambda_{\text{gen}} = 1.3$$



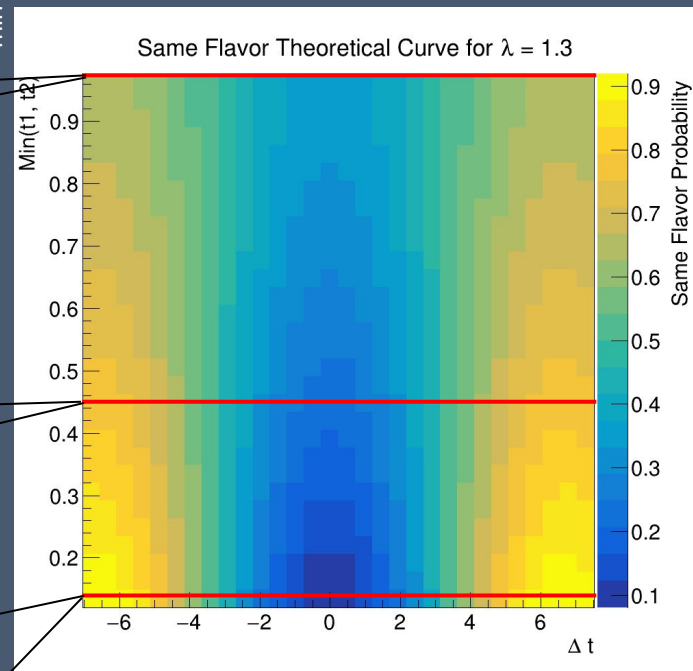
$t_{\text{min}} = 0.976\text{ps}$



$t_{\text{min}} = 0.444\text{ps}$



$t_{\text{min}} = 0.120\text{ps}$



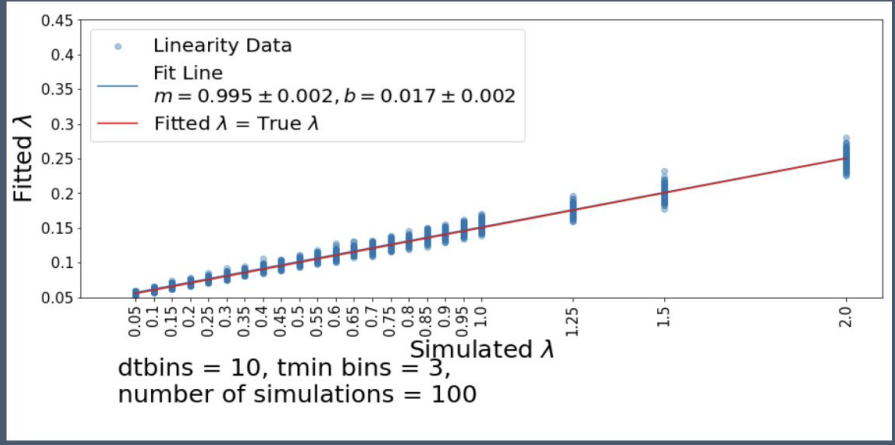
$$\lambda_{\text{fit}} = 1.309 \pm 0.0585$$

Modeling Decoherence

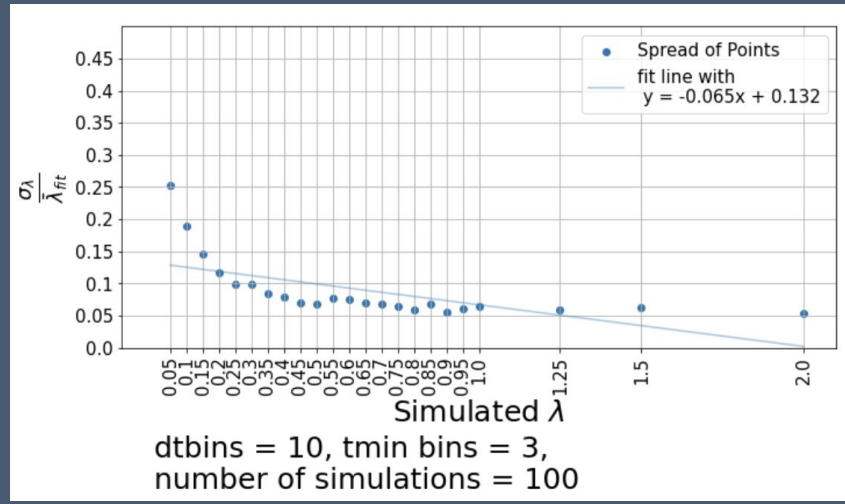
Performing a linearity test on the fitter for different λ values: Good agreement

Analyzing the sensitivity of the fitter at low λ values: Small fractional error for small λ

These made w/ 5,000 events. Anticipate ~80,000 experimental data!



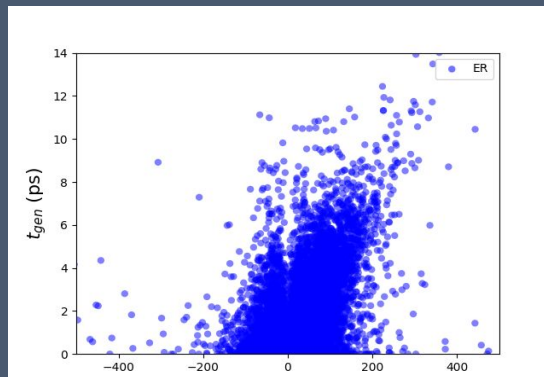
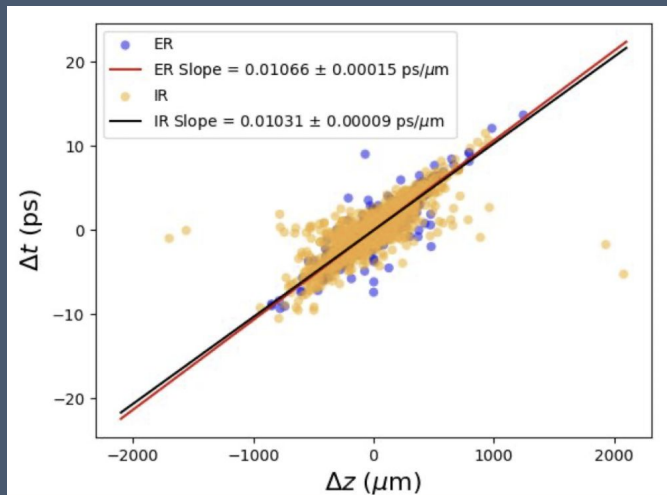
10 bins per Δt , 3 bins per t_{\min}



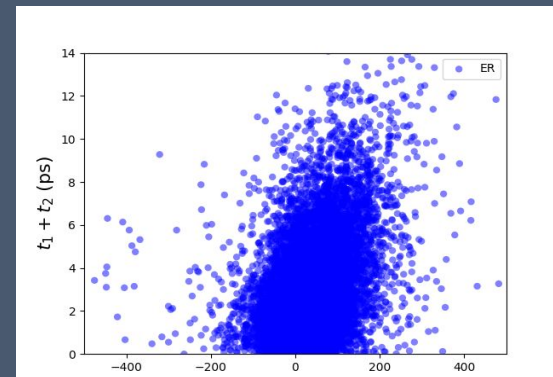
Reconstruction Efforts

At Belle II, we obtain Δt from Δz . To get t_{\min} , we see a correlation between the generated t-value and the reconstructed x-position of individual B mesons.

This gives us some sensitivity to individual decay times!



X_{max}



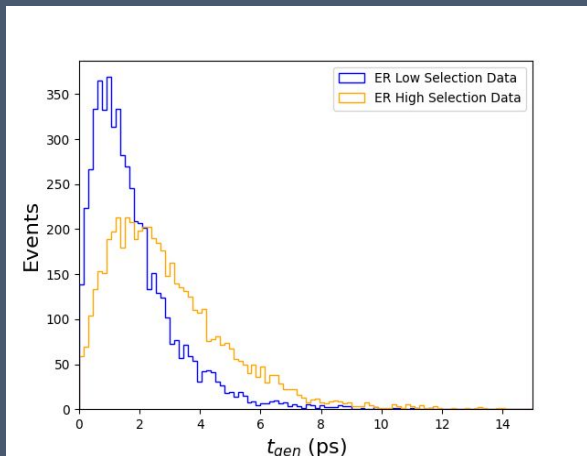
$X_{\text{min}} + X_{\text{max}}$

Reconstruction Efforts

Compare the decay time distributions for different bins in both x_{\max} and $x_{\min} + x_{\max}$

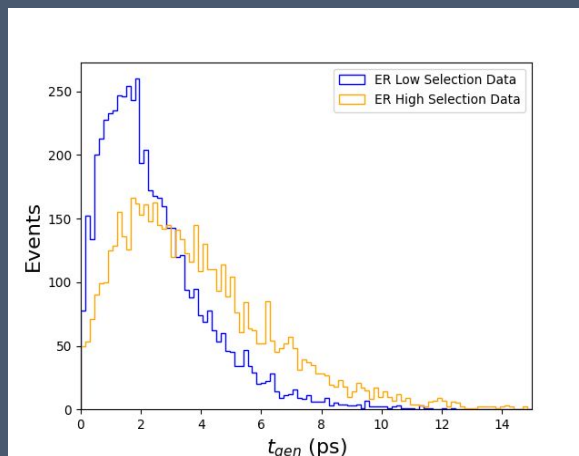
We see distinct shapes ✓

good separation



via x_{\max}

good separation



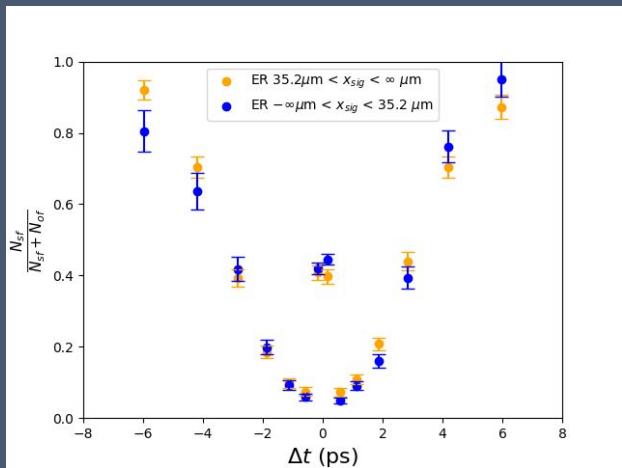
via $x_{\min} + x_{\max}$

Reconstruction Efforts

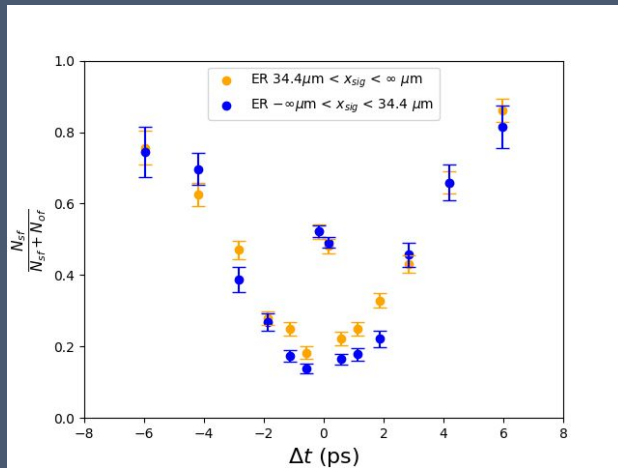
We use a modified version of EvtGen (thanks to Alexei) which implements decoherence.

We analyze two bins in x_{\max} as a proxy for t_{\max} (blue and orange).

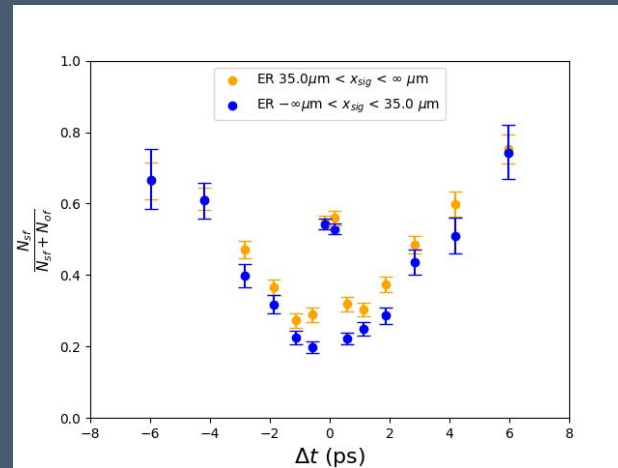
Observe separation of the two bins as λ increases \rightarrow indicates experimental feasibility



$\lambda = 0$



$\lambda = 0.5$



$\lambda = 1$

Summary & Further Plans

- Hershel and Aleczander developed a proof of concept...
 - ... that on truth-level, binned fits in the absolute decay time are sensitive to Lindblad decoherence
 - ... that an estimation of the absolute decay time is possible on reconstructed data
 - ... we are sensitive to Lindblad decoherence in reconstructed data
- We will continue to work on this topic by two UHM students...
 - Tim: “Lindblad” environmental decoherence, hadronic decays
 - Lucas: Fractional spontaneous decoherence, hadronic decays

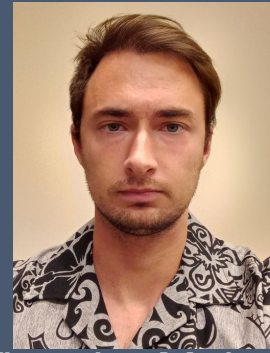
Thank you for your attention!



Prof. Sven Vahsen



Dr. Alexei Sibidanov



Timothy Mahood
(Grad)



Lucas Stoetzer
(Grad)



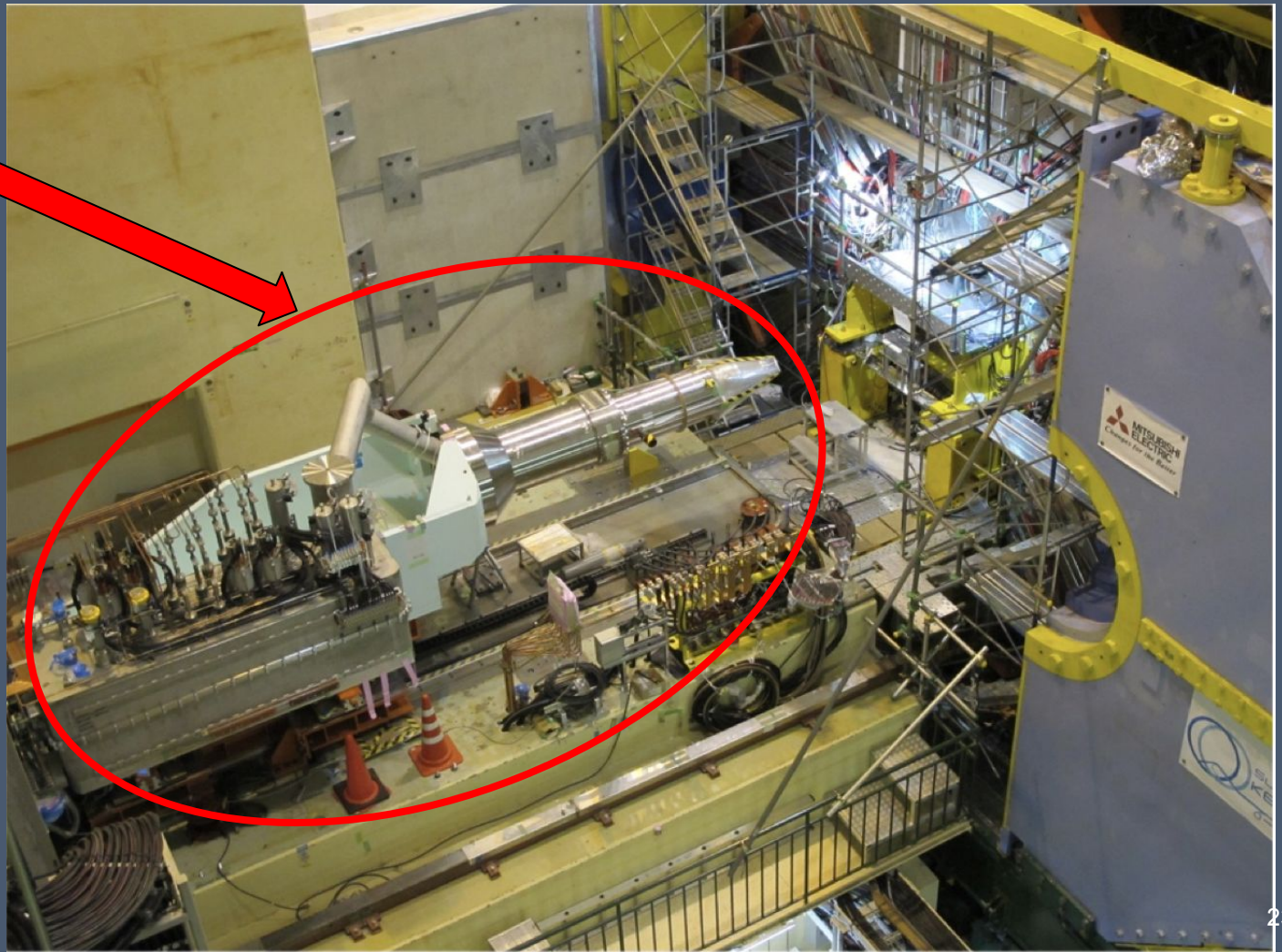
Hershel Weiner
(Undergrad)



Alecander Paul
(Undergrad)

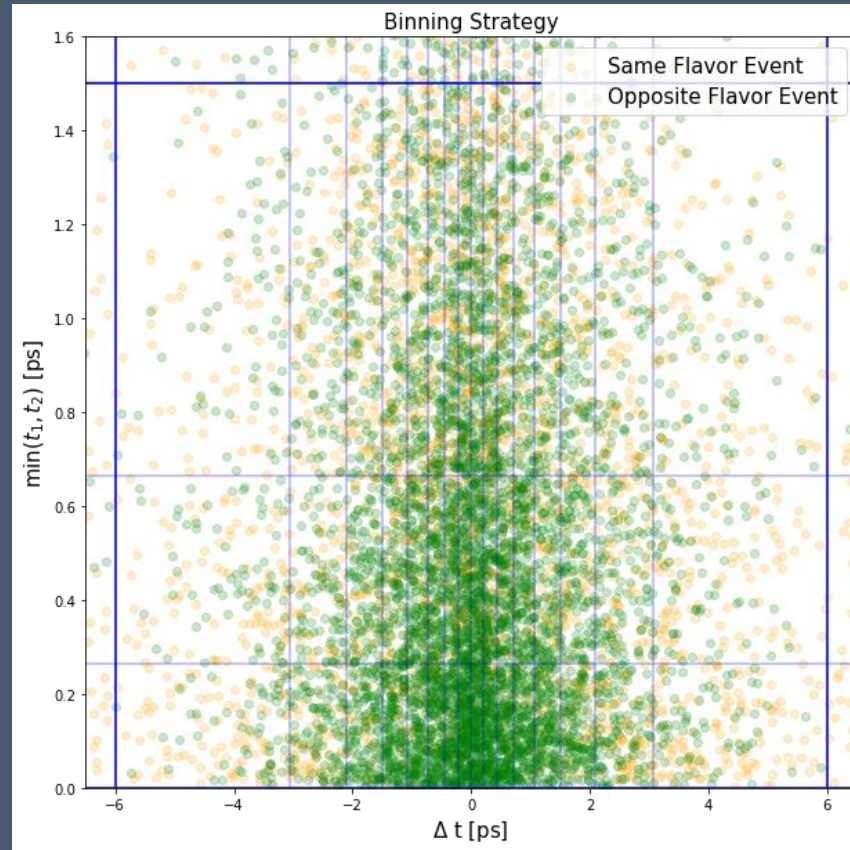
QCS

- 4 Quadrupole Magnets for each beam line
- 43 corrector/cancel coils
- 4 compensation solenoids

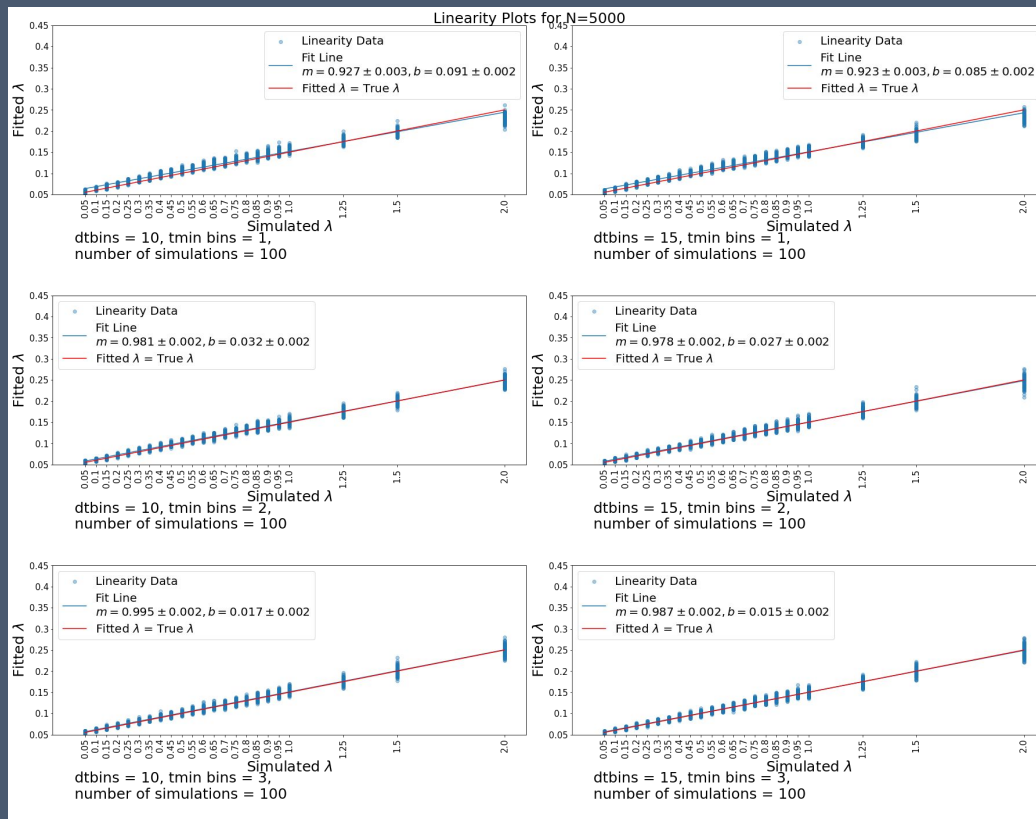


Y. Arimoto,
https://conference-indico.kek.jp/event/18/sessions/111/attachments/132/139/171212-asian_school-YA.pdf

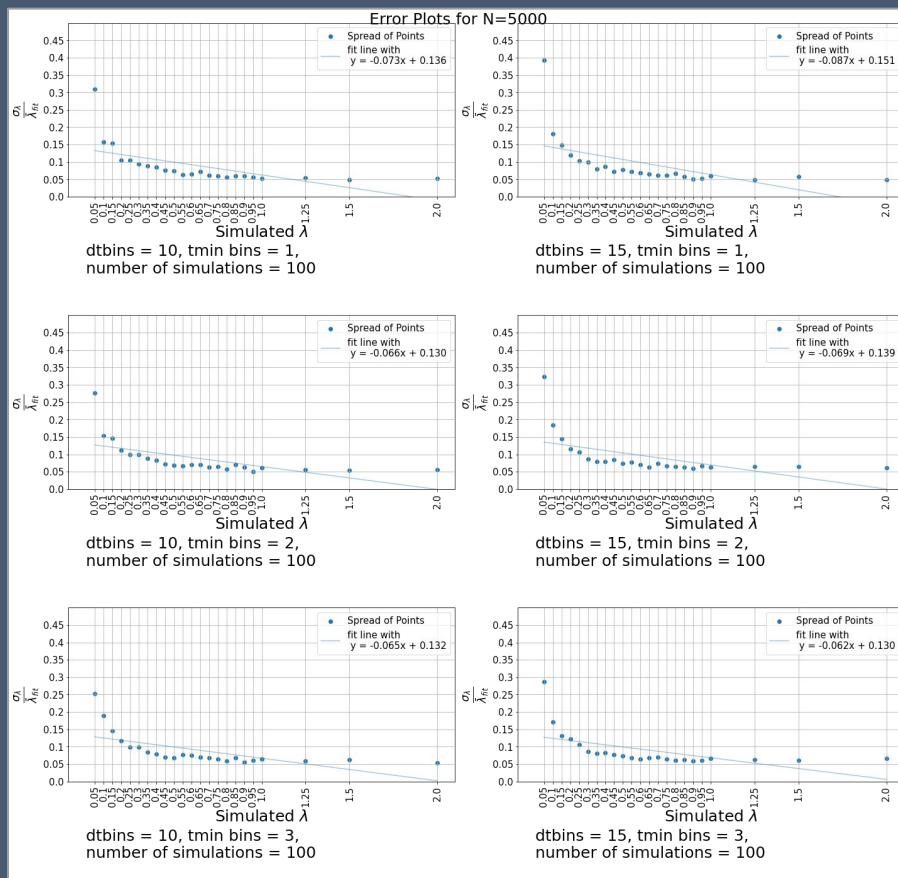
Backup - Binning



Backup - Fitter Linearity

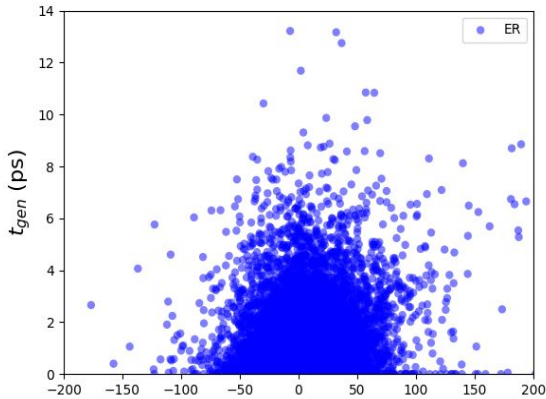


Backup - Fitter Sensitivity



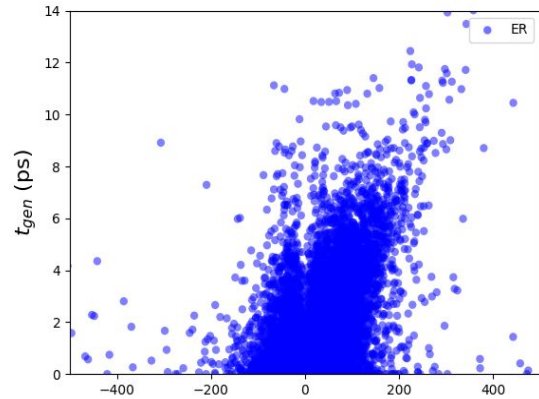
Backup - Correlation of various x-values

poor correlation



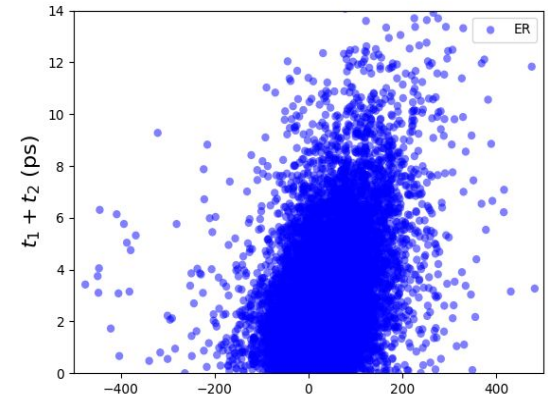
X_{min}

good correlation



X_{max}

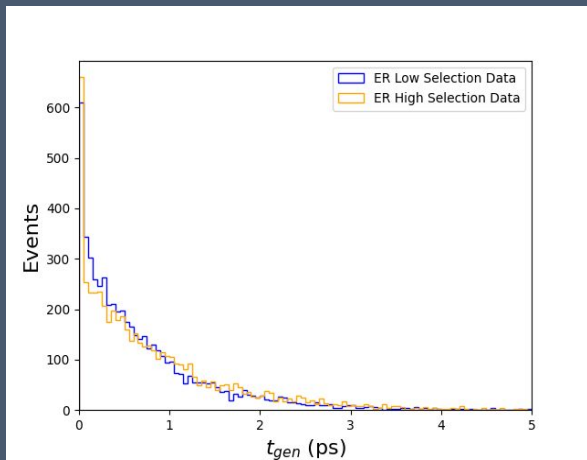
good correlation



$X_{min} + X_{max}$

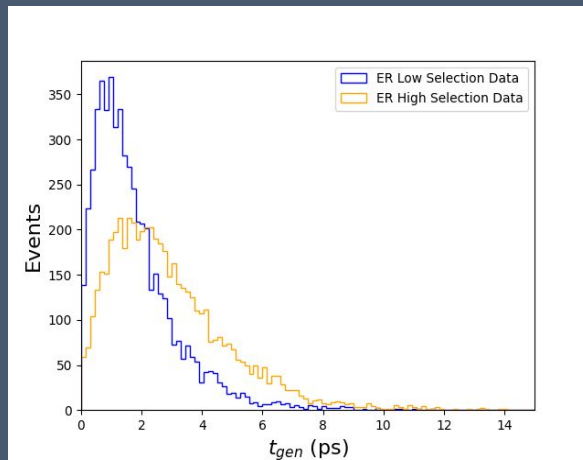
Backup - Distinguishing x-bins

poor separation



via x_{min}

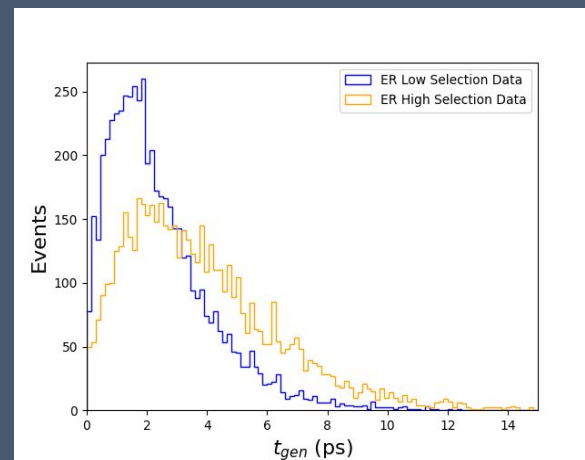
good separation



via

x_{max}

good separation



via

$x_{min} + x_{max}$