# Measurement of CP asymmetries in singly Cabbibo suppressed $\Xi_c^+$ and $\Lambda_c^+$ decays

Dinura Hettiarachchi<sup>1</sup>, Janaka Kospalage<sup>1</sup>, Jake Bennett<sup>1</sup>, Angelo Di Canto<sup>2</sup>

<sup>1</sup>University of Mississippi, University, Mississippi 38655, USA <sup>2</sup>Brookhaven National Laboratory, Upton, New York 11973, USA

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#### Charm & CPV probes: two pathways

- Null Hypothesis:
  - Directly test the Standard Model
  - Via direct CP asymmetry measurements
  - e.g. Belle [arXiv:1712.00619]

 $a_{CP}^{dir}(D^+ \rightarrow \pi^+ \pi^0) = 0$ (isospin limit & experimental sensitivity)

$$a_{CP}^{dir}(D^+ \to \pi^+ \pi^0) = (2.31 \pm 1.24 \pm 0.23)\%$$
[arXiv:1712.00619]

- Over-constrain the Standard Model:
  - Sum rules relating CP asymmetries in different channels
  - e.g. U spin sum rule (invariance under the interchange of d and s quarks)
  - LHCb measured sum rules [arXiv:2209.03179] at level of 2.7σ

 $a_d(D^0\to K^-K^+)+a_d(D^0\to\pi^-\pi^+)\neq 0$ 

• Needs to explore other modes to get the complete picture.



### CP asymmetries in charm baryons: $\Xi_c^+ \to \Sigma^+ h^+ h^-$ and $\Lambda_c^+ \to p^+ h^+ h^-$

- LHCb studied the CP asymmetry difference in singly Cabibbo suppressed  $\Lambda_c^+$  decay channels:  $\Delta A_{CP}^W = A_{CP}(pK^-K^+) - A_{CP}^W(p\pi^-\pi^+) = (0.30 \pm 0.91 \pm 0.61)\% \text{ [JHEP 03, 182 (2018)]}$
- Direct CP asymmetries are more of a theoretical significance than asymmetry differences.
  - Belle II has unique opportunities for such measurements
- Charm meson discovery modes  $(D^0 \rightarrow K^- K^+, \pi^- \pi^+)$  are related by U spin sum rules.
  - suggest looking at  $\Lambda_c^+$  and  $\Xi_c^+$  decays.

 $A_{CP}^{dir}(\Lambda_c^+ \to pK^+K^-) + A_{CP}^{dir}(\Xi_c^+ \to \Sigma^+\pi^+\pi^-) = 0$  $A_{CP}^{dir}(\Lambda_c^+ \to p\pi^+\pi^-) + A_{CP}^{dir}(\Xi_c^+ \to \Sigma^+K^+K^-) = 0$ 

#### Methodology

• Raw asymmetry from number counting,

$$A_{raw}^{\Xi_c} = \frac{N(\Xi_c^+ \to \Sigma^+ h^+ h^-) - N(\overline{\Xi}_c^- \to \overline{\Sigma}^- h^- h^+)}{N(\Xi_c^+ \to \Sigma^+ \pi^+ \pi^-) + N(\overline{\Xi}_c^- \to \overline{\Sigma}^- h^- h^+)}$$

• Raw asymmetry includes CPV, production (forward-backward), and detection asymmetries.

$$A_{raw}^{\Xi_c} = A_{CP}^{\Xi_c} + A_{FB}^{\Xi_c} + A_p$$

- The forward-backward asymmetry is expected to be antisymmetric as a function of  $cos(\theta^*)$ 
  - cancel by averaging over bins in  $|cos(\theta^*)|$
- Take difference with CF control channel  $\Lambda_c^+ \rightarrow \Sigma^+ h^+ h^-$  to cancel the detection asymmetry

$$A_{raw}^{\Lambda_c} = A_{FB}^{\Lambda_c} + A_p$$
 (no CPV)

• Isolate CP asymmetry for signal mode

$$A_{CP}^{\Xi_c} = \frac{A_{raw}^{\Xi_c}(\cos\theta_{\Xi_c}^*) + A_{raw}^{\Xi_c}(-\cos\theta_{\Xi_c}^*)}{2} - \frac{A_{raw}^{\Lambda_c}(\cos\theta_{\Lambda_c}^*) + A_{raw}^{\Lambda_c}(-\cos\theta_{\Lambda_c}^*)}{2}$$

## Methodology $(\Lambda_c^+ \rightarrow p^+ h^+ h^-)$

• Raw asymmetry includes CPV, production (forward-backward), and detection asymmetries.

$$A_{raw}^{\Lambda_c - p h h} = A_{CP}^{\Lambda_c - p h h} + A_{FB}^{\Lambda_c - p h h} + A_p$$

- The forward-backward asymmetry is expected to be antisymmetric as a function of  $cos(\theta^*)$ 
  - cancel by averaging over bins in  $|cos(\theta^*)|$
- Take difference with CF control channel  $\Lambda_c^+ \rightarrow p^+ K^- \pi^-$  to cancel the detection asymmetry

$$A_{raw}^{\Lambda_c - p K \pi} = A_{FB}^{\Lambda_c - p K \pi} + A_p + A_{K/\pi}$$
 (no CPV)

• Take difference with CF control channel  $D^0 \to K^- \pi^+ \pi^+ \pi^-$  to cancel the K/ $\pi$  detection asymmetry

$$A_{raw}^{D^0 \to K \pi \pi \pi} = A_{FB}^{D^0 \to K \pi \pi \pi} + A_{K/\pi}$$
 (no CPV)

• Isolate CP asymmetry for signal mode

$$A_{CP}^{A_{c}-phh} = \frac{A_{raw}^{A_{c}-phh}(\cos(\theta_{A_{c}}^{*})) + A_{raw}^{A_{c}-phh}(-\cos(\theta_{A_{c}}^{*}))}{2} - \frac{A_{raw}^{A_{c}-pK\pi}(\cos(\theta_{A_{c}}^{*})) + A_{raw}^{A_{c}-pK\pi}(-\cos(\theta_{A_{c}}^{*}))}{2} + \frac{A_{raw}^{D^{0} \to K\pi\pi\pi}(\cos(\theta_{D^{0}}^{*})) + A_{raw}^{D^{0} \to K\pi\pi\pi}(-\cos(\theta_{D^{0}}^{*}))}{2}$$

#### **Reconstruction Criteria**

| Description                           | Selection                                                                                                                                                            |  |  |  |
|---------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|--|--|
| charged tracks $(K, \pi, p)$          | in CDC acceptance minimum number (> 0) of hits in CDC                                                                                                                |  |  |  |
| proton ( <i>p</i> )                   | proton trinaryID > 0.2                                                                                                                                               |  |  |  |
| Mass                                  | $\begin{array}{l} 2.35 < {\sf M}(\Xi_c) < 2.60 \; [GeV/c^2] \\ 2.15 < {\sf M}(\Lambda_c) < 2.40 \; [GeV/c^2] \\ 1.75 < {\sf M}(D^0) < 1.95 \; [GeV/c^2] \end{array}$ |  |  |  |
| CM momentum $(\Xi_c, \Lambda_c, D^0)$ | CM momentum > 2.0[GeV/c]                                                                                                                                             |  |  |  |
| treeFit $(\Xi_c, \Lambda_c, D^0)$     | chiProb > 0.001                                                                                                                                                      |  |  |  |
|                                       | $\Xi_c^+ \to \Sigma^+ h^+ h^-$                                                                                                                                       |  |  |  |
| photon ( $\gamma$ )                   | E <sub>forward</sub> > 0.080 GeV, Ebarrel > 0.030 GeV, Ebackward > 0.060 GeV,<br>clusterNHits > 1.5, 0.2967 < clusterTheta < 2.6180                                  |  |  |  |
| $\pi^0$                               | $0.125 < M(\pi^0) < 0.145 [GeV/c^2]$                                                                                                                                 |  |  |  |
| Σ                                     | $1.159 < M(\Sigma) < 1.219 [GeV/c^2]$                                                                                                                                |  |  |  |
|                                       | $D^0 \to K^- \pi^+ \pi^+ \pi^-$                                                                                                                                      |  |  |  |
| charged tracks ( $K, \pi$ )           | dr < 1 [cm] and abs(dz) < 3 [cm]                                                                                                                                     |  |  |  |
| K                                     | kaon binaryID > 0.2                                                                                                                                                  |  |  |  |

# Selection Criteria $(\Xi_c^+ \rightarrow \Sigma^+ h^+ h^-)$

| Description         | Selection                                                                                |
|---------------------|------------------------------------------------------------------------------------------|
| Mass                | 2. 40< M( $\Xi_c$ ) < 2.54 [GeV/ $c^2$ ]<br>2.24 < M( $\Lambda_c$ ) < 2.34 [GeV/ $c^2$ ] |
| kaon (K)            | kaon binaryID > 0.2                                                                      |
| proton ( <i>p</i> ) | proton trinaryID > 0.8                                                                   |

MVA – Multi Variate Analysis

|                                   | $\Xi_c^+ \to \Sigma^+ \pi^+ \pi^-$ | $\Xi_c^+ \to \Sigma^+ K^+ K^-$ |
|-----------------------------------|------------------------------------|--------------------------------|
| fake photon suppression (fps)     | fps > 0.7                          | fps > 0.3                      |
| beam background suppression (bbs) | bbs > 0.8                          | bbs > 0.8                      |
| MVA                               | MVA > 0.1                          | MVA > 0.7                      |



| • | Multi | Variate | Analy | /sis ( | (MVA) |
|---|-------|---------|-------|--------|-------|
|---|-------|---------|-------|--------|-------|

- Σ flight distance
- $\chi^2$  of vertex fit
- K dr or pi dr
- $\pi^0(\Sigma)$  CM momentum

## Mass Distributions $(\Xi_c^+ \rightarrow \Sigma^+ h^+ h^-)$

• Mass distributions of  $\Xi_c^+ \to \Sigma^+ \pi^+ \pi^-$  and  $\Lambda_c^+ \to \Sigma^+ \pi^+ \pi^-$  after reconstruction and after applying selections.



## Mass Distributions $(\Xi_c^+ \rightarrow \Sigma^+ h^+ h^-)$

• Mass distributions of  $\Xi_c^+ \to \Sigma^+ K^+ K^-$  and  $\Lambda_c^+ \to \Sigma^+ K^+ K^-$ , after reconstruction and after applying selections.



# Selection Criteria $(\Lambda_c^+ \rightarrow p^+ h^+ h^-)$

| Description                    | Selection                                                                  |                                                                      |
|--------------------------------|----------------------------------------------------------------------------|----------------------------------------------------------------------|
| Mass                           | $2.24 < M(\Lambda_c) < 2.34 [GeV/c^2]$<br>$1.80 < M(D^0) < 1.92 [GeV/c^2]$ |                                                                      |
| charged tracks ( $K, \pi, p$ ) | dr < 1 [cm] and abs(dz) < 3 [cm]                                           |                                                                      |
| 4                              | $\Lambda_c$ flight distance > 0 [ <i>cm</i> ]                              | proton trinaryID                                                     |
| $\Lambda_c$                    | $\Lambda_c$ CM momentum > 2.5[ <i>GeV</i> / <i>c</i> ]                     | <ul> <li>proton ID</li> <li>(proton ID +kaon ID +pion ID)</li> </ul> |
| kaon (K)                       | kaon binaryID > 0.7                                                        | kaon binaryID     kaon ID                                            |
| proton ( <i>p</i> )            | proton trinaryID > 0.9                                                     | $\blacksquare \frac{\text{kaon ID}}{(\text{kaon ID+pion ID})}$       |
|                                | $\Lambda_c^+ \to p^+ \pi^+ \pi^-$                                          |                                                                      |
| $\Lambda_c$                    | $\Lambda_c$ significance of distance > 0.25 [ <i>cm</i> ]                  |                                                                      |
| pion (π)                       | pion momentum > 0.30 [ <i>GeV</i> / <i>c</i> ]                             |                                                                      |
| proton ( <i>p</i> )            | proton momentum > 0.85[ <i>GeV/c</i> ]                                     |                                                                      |

• Mass distributions of  $\Lambda_c^+$  channels used in  $A_{cp}$  calculations of  $\Lambda_c^+ \rightarrow p^+ \pi^+ \pi^-$ , after reconstruction and after applying square cut selections.



• Mass distributions of  $D^0 \to K^- \pi^+ \pi^+ \pi^-$  channel used in  $A_{cp}$  calculations of  $\Lambda_c^+ \to p^+ \pi^+ \pi^-$  after reconstruction and after applying square cut selections.



• Mass distributions of  $\Lambda_c^+$  channels used in  $A_{cp}$  calculations of  $\Lambda_c^+ \rightarrow p^+ K^+ K^-$ , after reconstruction and after applying square cut selections.



• Mass distributions of  $D^0 \to K^- \pi^+ \pi^+ \pi^-$  channel used in  $A_{cp}$  calculations of  $\Lambda_c^+ \to p^+ K^+ K^-$  after reconstruction and after applying square cut selections.



#### proton detection asymmetry

- Recall, raw asymmetries include effects from CPV, production (forward-backward), and detection asymmetries.
- For the modes, that the final states have a proton(Sigma),

 $A_{raw} = A_{CP} + A_{FB} + A_p$ 

- Proton in the final state of signal channel and control channel might cover different regions of phase space.
  - Control channel proton was weighted to match the signal channel proton in phase space.
  - Weights were taken as a combination of proton momentum and proton  $\cos\theta$ .



#### hh detection asymmetry

- Recall, raw asymmetries should include  $h^+h^-$  detection asymmetry for channels with final state  $h^+h^-$ .
- We assume detection asymmetry of  $h^+h^-$  cancels out, as the final state contains both sign pions/kaons.
- $h^+$  and  $h^-$ might cover different regions of phase space.
- Initial checks suggest no significant effect of this.



## *K* and $\pi$ detection asymmetry $(\Lambda_c^+ \rightarrow p^+ h^+ h^-)$

• Recall, raw asymmetries of  $\Lambda_c^+ \rightarrow p^+ K^- \pi^-$  and  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^-$  includes effects from, production (forward-backward), and detection asymmetries

$$A_{raw}^{\Lambda_{c}} - p_{K}\pi = A_{FB}^{\Lambda_{c}} - p_{K}\pi + A_{p} + A_{K/\pi}$$
$$A_{raw}^{D^{0} \to K}\pi\pi\pi = A_{FB}^{D^{0} \to K}\pi\pi\pi + A_{K/\pi}$$

- K and  $\pi$  in the final state of these channels might cover different regions of phase space.
  - $D^0$  channel K and  $\pi$  was weighted to match the weighted  $\Lambda_c^+ \to p^+ K^- \pi^-$  channel K and  $\pi$  in phase space.
  - Weights were taken as a 2D combination of K and  $\pi$  momentum and K and  $\pi \cos\theta$ .



#### **Fitting Strategy**

- Invariant mass fits were modeled. ٠
  - **Double Gaussian** function for the signal
  - 2<sup>nd</sup> order polynomial function for the background

$$f_g(x|\mu,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)}{2\sigma^2}}$$
  
$$f_{sig}(x|\mu,\sigma_1,\sigma_2,f_g) = f_g \cdot f(x|\mu,\sigma_1) + (1-f_g) \cdot f(x|\mu,\sigma_2)$$
  
$$f_{bkg}(x|a,b) = ax + bx^2$$

- Invariant mass distribution fit for the truth matched events in the signal channel ٠
  - extract signal channel parameters
- Invariant mass distribution fit for all events in the control channel ٠
  - extract control channel parameters
- Fits of invariant mass distribution are performed in bins of  $cos(\theta^*)$ ٠
  - Simultaneously for the both signal and control channels ٠
  - $\mu + \delta \mu$ ,  $\sigma_1 \times \delta \sigma_1$ , and  $\sigma_2 \times \delta \sigma_2$  are fixed from extracted parameters

|                                                                                | <b>Parameters</b> name                                                                                                                                  | value                   | (rounded)                                                                                                  |
|--------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------|------------------------------------------------------------------------------------------------------------|
| signal parameters<br>$(\Lambda_c^+ \rightarrow p^+ \pi^+ \pi^-)$               | sig_yield<br>fg1<br>mu<br>s1<br>s2                                                                                                                      | e                       | 356198<br>0.170363<br>2.28667<br>0.0171379<br>0.00349743                                                   |
|                                                                                | Parameters<br>name                                                                                                                                      | value                   | (rounded)                                                                                                  |
| control parameters<br>$(\Lambda_c^+ \rightarrow p^+ \pi^+ K^-)$                | sig_yield<br>bkg_yield<br>fg1<br>mu<br>s1<br>s2<br>a1<br>a2                                                                                             | 1.<br>4.<br>6<br>-<br>- | 95701e+00<br>90514e+00<br>0.715278<br>2.28672<br>0.00243442<br>0.00585479<br>-0.0509389<br>-0.0306419      |
| nel                                                                            | Parameters<br>name<br>sig_sig_yield<br>sig_bkg_yield<br>smu<br>ss1                                                                                      | value<br>               | (rounded<br>84557.<br>1.87335e+0<br>8.48046e-0<br>1.3557                                                   |
| $cos(\theta^*)$ bin1 parameters<br>$(\Lambda_c^+ \rightarrow p^+ \pi^+ \pi^-)$ | ss2<br>sig_a1<br>sig_a2<br>asig_sig_yield<br>asig_bkg_yield<br>asig_a1<br>asig_a2                                                                       |                         | 1.3437<br>-0.024485<br>-0.0020113<br>78054.<br>1.7667e+0<br>-0.023878<br>-0.0015994                        |
|                                                                                | <pre>ctr_sig_yield<br/>ctr_bkg_yield<br/>ctr_fg1<br/>ctr_a1<br/>ctr_a2<br/>actr_sig_yield<br/>actr_bkg_yield<br/>actr_fg1<br/>actr_a1<br/>actr_a2</pre> |                         | 46280<br>93171<br>0.72814<br>-0.048854<br>-0.040671<br>42810<br>88737<br>0.71998<br>-0.047241<br>-0.035586 |

## Results for $\Xi_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-$ using MC15rd default MC

• Truth-matching was used to extract the raw asymmetries and compare them with results from the invariant mass fits.

| MC (~1680 /fb) | $A_{raw} \% (\Xi_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-)$ | $A_{raw} \% (\Lambda_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-)$ | $A_{cp}\% (\Xi_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-)$ |
|----------------|---------------------------------------------------------|-------------------------------------------------------------|-------------------------------------------------------|
| Truth-matched  | $6.27\pm0.59$                                           | $6.33 \pm 0.15$                                             | $\textbf{-0.05} \pm 0.61$                             |
| Fitted         | $6.22\pm2.08$                                           | $6.60 \pm 0.44$                                             | $-0.38 \pm 2.13$                                      |

• Results are consistent with the  $A_{cp} = 0$ 



•  $cos(\theta^*)$  bin 1 matter distributions of  $\Xi_c^+ \to \Sigma^+ \pi^+ \pi^-$ , and weighted  $\Lambda_c^+ \to \Sigma^+ \pi^+ \pi^-$ 

## Results for $\Xi_c^+ \rightarrow \Sigma^+ K^+ K^-$ using MC15rd default MC

• Truth-matching was used to extract the raw asymmetries and compare them with results from the invariant mass fits.

| MC (~1680 /fb) | $A_{raw} \% (\Xi_c^+ \to \Sigma^+ K^+ K^- )$ | $A_{raw} \% (\Lambda_{\mathcal{C}}^+ \to \Sigma^+ K^+ K^- )$ | $A_{cp}\%(\Xi_c^+\to\Sigma^+K^+K^-)$ |
|----------------|----------------------------------------------|--------------------------------------------------------------|--------------------------------------|
| Truth-matched  | $5.46 \pm 1.08$                              | $6.07\pm0.79$                                                | $-0.61 \pm 1.34$                     |
| Fitted         | $5.91 \pm 1.68$                              | $6.46\pm0.73$                                                | $-0.55 \pm 1.83$                     |

• Results are consistent with the  $A_{cp} = 0$ 



•  $cos(\theta^*)$  bin 1 matter distributions of  $\Xi_c^+ \to \Sigma^+ K^+ K^-$ , and weighted  $\Lambda_c^+ \to \Sigma^+ K^+ K^-$ 

# Results for $\Lambda_c^+ \rightarrow p^+ \pi^+ \pi^-$ using MC15rd default MC

- Truth-matching was used to extract the raw asymmetries and compare them with results from the invariant mass fits.
- \*Subset of the full MC sample corresponding to 105 /fb was used for  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  mode.

| MC (~1680 /fb) | $A_{raw} \% (\Lambda_c^+ \to \mathrm{p}^+ \pi^+ \pi^-)$ | $A_{\rm raw}$ % ( $\Lambda_c^+  ightarrow { m p}^+ \pi^+ K^-$ ) | $A_{raw}\% (D^0 \to K^- \pi^+ \pi^+ \pi^-)^*$ | $A_{cp}\%(\Lambda_{\mathcal{C}}^{+}\to\mathrm{p}^{+}\pi^{+}\pi^{-})$ |
|----------------|---------------------------------------------------------|-----------------------------------------------------------------|-----------------------------------------------|----------------------------------------------------------------------|
| Truth-matched  | $3.23\pm0.17$                                           | $2.80\pm0.07$                                                   | $-0.86 \pm 0.07$                              | $-0.39 \pm 0.20$                                                     |
| Fitted         | $3.79 \pm 0.53$                                         | $2.82 \pm 0.11$                                                 | $-0.95 \pm 0.19$                              | $0.02 \pm 0.57$                                                      |

• Results are consistent with the A<sub>cp</sub>= 0



•  $cos(\theta^*)$  bin 1 matter distributions of  $\Lambda_c^+ \to p^+\pi^+\pi^-$ , weighted  $\Lambda_c^+ \to p^+\pi^+K^-$ , and weighted  $D^0 \to K^-\pi^+\pi^+\pi^-$ 

## Results for $\Lambda_c^+ \rightarrow p^+ K^+ K^-$ using MC15rd default MC

- Truth-matching was used to extract the raw asymmetries and compare them with results from the invariant mass fits.
- \*Subset of the full MC sample corresponding to 105 /fb was used for  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  mode.

| MC (~1680 /fb) | $A_{raw} \% (\Lambda_c^+ \to \mathrm{p}^+ K^+ K^- )$ | A <sub>raw</sub> % ( $\Lambda_c^+  ightarrow \mathrm{p}^+ \pi^+ K^-$ ) | $A_{raw}\% (D^0 \to K^- \pi^+ \pi^+ \pi^-)^*$ | $A_{cp} \% (\Lambda_c^+ \to \mathrm{p}^+ K^+ K^-)$ |
|----------------|------------------------------------------------------|------------------------------------------------------------------------|-----------------------------------------------|----------------------------------------------------|
| Truth-matched  | $3.69\pm0.52$                                        | $3.22\pm0.06$                                                          | $-0.63 \pm 0.05$                              | $-0.16 \pm 0.53$                                   |
| Fitted         | $3.33 \pm 1.20$                                      | $3.19 \pm 0.13$                                                        | $-0.74 \pm 0.19$                              | $0.60 \pm 1.22$                                    |

• Results are consistent with the  $A_{cp} = 0$ 



•  $cos(\theta^*)$  bin 1 matter distributions of  $\Lambda_c^+ \to p^+ K^+ K^-$ , weighted  $\Lambda_c^+ \to p^+ \pi^+ K^-$ , and weighted  $D^0 \to K^- \pi^+ \pi^+ \pi^-$ 

#### Remarks

- We are looking into detection asymmetry of *hh* more closely.
- We are bootstrapping on a subset of the full Monte Carlo sample, corresponding to the integrated luminosity of the available data sample (426.6 /fb).
- We are investigating the potential reasons for the difference between the truth-matched and fitted  $A_{cp}$  values of  $A_{c}^+ \rightarrow p^+ \pi^+ \pi^-$  mode.
- We are in the final phase of completing the first version of Belle2Note.
- We hope to ask for a working group review soon.

| ctr_sig_yield  | 466665     | +/- 1.2e+03 | -1.2e+03 | +1.2e+03 | -1.2e+03 | +1.2e+03 | False |
|----------------|------------|-------------|----------|----------|----------|----------|-------|
| ctr_bkg_yield  | 940361     | +/- 1.4e+03 | -1.4e+03 | +1.4e+03 | -1.4e+03 | +1.4e+03 | False |
| ctr_fg1        | 0.26006    | +/- 0.005   | - 0.0049 | + 0.0051 | - 0.0049 | + 0.0051 | False |
| ctr_a1         | -0.0490723 | +/- 0.0018  | - 0.0018 | + 0.0018 | - 0.0018 | + 0.0018 | False |
| ctr_a2         | -0.0378251 | +/- 0.0024  | - 0.0024 | + 0.0024 | - 0.0024 | + 0.0024 | False |
| actr_sig_yield | 431170     | +/- 1.1e+03 | -1.1e+03 | +1.1e+03 | -1.1e+03 | +1.1e+03 | False |
| actr_bkg_yield | 896059     | +/- 1.3e+03 | -1.3e+03 | +1.3e+03 | -1.3e+03 | +1.3e+03 | False |
| actr_fg1       | 0.268196   | +/- 0.0051  | - 0.005  | + 0.0052 | - 0.005  | + 0.0052 | False |
| actr_a1        | -0.0474012 | +/- 0.0018  | - 0.0018 | + 0.0018 | - 0.0018 | + 0.0018 | False |
| actr_a2        | -0.032489  | +/- 0.0025  | - 0.0024 | + 0.0024 | - 0.0024 | + 0.0024 | False |
| ctr_sig_yield  | 462804     | +/- 9.6e+02 | - 1e+03  | + 1e+03  | - 1e+03  | + 1e+03  | False |
| ctr bkg vield  | 931717     | +/- 9 6e+02 | -1 2e+03 | +1 20+03 | -1 2e+03 | +1 20+03 | False |
| ctr fal        | 0.728149   | +/- 0.0042  | - 0.0041 | + 0.0041 | - 0.0041 | + 0.0041 | False |
| ctr_a1         | -0.0488542 | +/- 0.0018  | - 0.0018 | + 0.0018 | - 0.0018 | + 0.0018 | False |
| ctr_a2         | -0.0406715 | +/- 0.0022  | - 0.0022 | + 0.0022 | - 0.0022 | + 0.0022 | False |
| actr_sig_yield | 428104     | +/- 9.2e+02 | -9.8e+02 | +9.9e+02 | -9.8e+02 | +9.9e+02 | False |
| actr_bkg_yield | 887373     | +/- 9.2e+02 | -1.2e+03 | +1.2e+03 | -1.2e+03 | +1.2e+03 | False |
| actr_fg1       | 0.719981   | +/- 0.0044  | - 0.0042 | + 0.0042 | - 0.0042 | + 0.0042 | False |
| actr_a1        | -0.0472417 | +/- 0.0018  | - 0.0019 | + 0.0019 | - 0.0019 | + 0.0019 | False |
| actr_a2        | -0.0355868 | +/- 0.0023  | - 0.0023 | + 0.0023 | - 0.0023 | + 0.0023 | False |
|                |            |             |          |          |          |          |       |

initial

weighted

|                                                  | A <sub>raw</sub> % (Truth-matched) | A <sub>raw</sub> % (Fitted) |
|--------------------------------------------------|------------------------------------|-----------------------------|
| $\Lambda_c^+ \to p^+ \pi^+ K^-$                  | $2.8868 \pm 0.0694$                | $2.9217 \pm 0.1296$         |
| weighted $\Lambda_c^+ \rightarrow p^+ \pi^+ K^-$ | $2.7978 \pm 0.0698$                | $2.8219 \pm 0.1098$         |

| <pre>ctr_sig_yield ctr_bkg_yield ctr_fg1 ctr_a1 ctr_a2 actr_sig_yield actr_bkg_yield actr_fg1 actr_a1 actr_a1 actr_a1 actr_a2</pre> | 534753<br>1.56553e+06<br>0.307921<br>-0.0546453<br>-0.0281748<br>514914<br>1.53976e+06<br>0.316439<br>-0.0527385<br>-0.0294822 | +/- 1.4e+03<br>+/- 1.7e+03<br>+/- 0.0068<br>+/- 0.0014<br>+/- 0.0018<br>+/- 1.4e+03<br>+/- 1.7e+03<br>+/- 0.0069<br>+/- 0.0014<br>+/- 0.0014 | -1.4e+03<br>-1.7e+03<br>- 0.0067<br>- 0.0014<br>- 0.0018<br>-1.4e+03<br>-1.7e+03<br>- 0.0068<br>- 0.0014<br>- 0.0014 | +1.4e+03<br>+1.7e+03<br>+ 0.0069<br>+ 0.0014<br>+ 0.0018<br>+1.4e+03<br>+1.7e+03<br>+ 0.007<br>+ 0.0014<br>+ 0.0014 | -1.4e+03<br>-1.7e+03<br>- 0.0067<br>- 0.0014<br>- 0.0018<br>-1.4e+03<br>-1.7e+03<br>- 0.0068<br>- 0.0014<br>- 0.0014 | +1.4e+03<br>+1.7e+03<br>+ 0.0069<br>+ 0.0014<br>+ 0.0018<br>+1.4e+03<br>+1.7e+03<br>+ 0.007<br>+ 0.0014<br>+ 0.0014 | False<br>False<br>False<br>False<br>False<br>False<br>False<br>False |
|-------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------|
| actr_a2                                                                                                                             | -0.0294822                                                                                                                     | +/- 0.0018                                                                                                                                   | - 0.0018                                                                                                             | + 0.0018                                                                                                            | - 0.0018                                                                                                             | + 0.0018                                                                                                            | False                                                                |
|                                                                                                                                     | 500010                                                                                                                         |                                                                                                                                              | 1 2 1 2 2                                                                                                            |                                                                                                                     | 1 2                                                                                                                  | 1 2                                                                                                                 | F-1                                                                  |
| ctr_sig_yield                                                                                                                       | 539310                                                                                                                         | +/- 1.2e+03                                                                                                                                  | -1.2e+03                                                                                                             | +1.3e+03                                                                                                            | -1.2e+03                                                                                                             | +1.3e+03                                                                                                            | False                                                                |
| ctr_DRg_yield                                                                                                                       | 1.33/890+00                                                                                                                    | +/- 1.20+03                                                                                                                                  | -1.00+03                                                                                                             | +1.00+03                                                                                                            | -1.00+03                                                                                                             | +1.00+03                                                                                                            | False                                                                |
| ctr_tgi                                                                                                                             | -0 0520222                                                                                                                     | +/- 0.0052<br>+/- 0.001/1                                                                                                                    | - 0.0049                                                                                                             | + 0.0040                                                                                                            | - 0.0049                                                                                                             | + 0.0040                                                                                                            | False                                                                |
| ctr a?                                                                                                                              | -0.0286019                                                                                                                     | +/- 0.0014                                                                                                                                   | - 0.0017                                                                                                             | + 0.0014                                                                                                            | - 0.0014                                                                                                             | + 0.0017                                                                                                            | False                                                                |
| actr sig vield                                                                                                                      | 520772                                                                                                                         | +/- 1.2e+03                                                                                                                                  | -1.2e+03                                                                                                             | +1.2e+03                                                                                                            | -1.2e+03                                                                                                             | +1.2e+03                                                                                                            | False                                                                |
| actr_bkg_yield                                                                                                                      | 1.53421e+06                                                                                                                    | +/- 1.2e+03                                                                                                                                  | -1.6e+03                                                                                                             | +1.6e+03                                                                                                            | -1.6e+03                                                                                                             | +1.6e+03                                                                                                            | False                                                                |
| actr_fg1                                                                                                                            | 0.686616                                                                                                                       | +/- 0.0053                                                                                                                                   | - 0.0049                                                                                                             | + 0.0049                                                                                                            | - 0.0049                                                                                                             | + 0.0049                                                                                                            | False                                                                |
| actr_a1                                                                                                                             | -0.0522247                                                                                                                     | +/- 0.0014                                                                                                                                   | - 0.0014                                                                                                             | + 0.0014                                                                                                            | - 0.0014                                                                                                             | + 0.0014                                                                                                            | False                                                                |
| actr_a2                                                                                                                             | -0.0295979                                                                                                                     | +/- 0.0018                                                                                                                                   | - 0.0017                                                                                                             | + 0.0018                                                                                                            | - 0.0017                                                                                                             | + 0.0018                                                                                                            | False                                                                |
|                                                                                                                                     |                                                                                                                                |                                                                                                                                              |                                                                                                                      |                                                                                                                     |                                                                                                                      |                                                                                                                     |                                                                      |

initial

weighted

|                                                  | A <sub>raw</sub> % (Truth-matched) | A <sub>raw</sub> % (Fitted) |
|--------------------------------------------------|------------------------------------|-----------------------------|
| $\Lambda_c^+ \to p^+ \pi^+ K^-$                  | $2.8868 \pm 0.0694$                | $2.9217 \pm 0.1296$         |
| weighted $\Lambda_c^+ \rightarrow p^+ \pi^+ K^-$ | $2.7978 \pm 0.0698$                | $2.8219 \pm 0.1098$         |