

Electroweak and radiative penguin B meson decays at Belle and Belle II

Giulio Dujany

on behalf of the Belle and Belle II collaborations

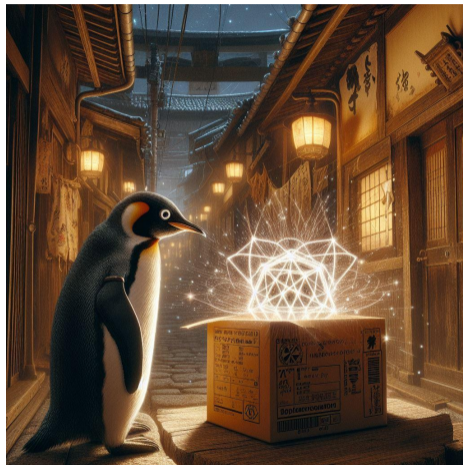
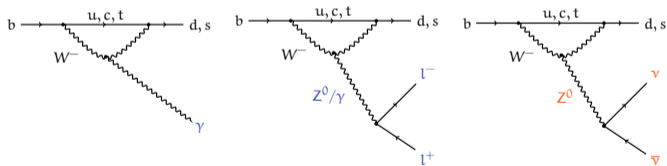


Moriond QCD 2024



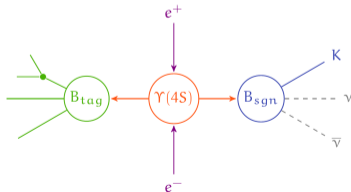
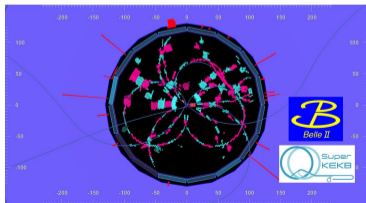
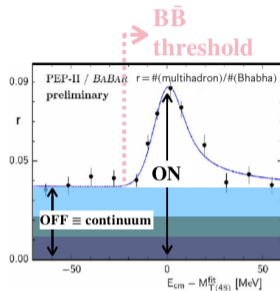
Electroweak and radiative penguin B decays

- Flavour changing neutral currents present only at loop level in the Standard Model
- Formidable place to look for New Physics that could interfere with radiative and electroweak penguin loops



Advantages of an $e^+ e^-$ flavour factory

- Known initial kinematics and good hermeticity
 - possible to fully reconstruct events with invisible particles
- Run at the $\Upsilon(4S)$ mass just above $B\bar{B}$ threshold
 - Relatively low background
 - Data off-resonance provide control sample without $B\bar{B}$
- Clean environment (average 11 tracks per event)
 - efficient detection of neutrals ($\gamma, \pi^0, \eta, \dots$)

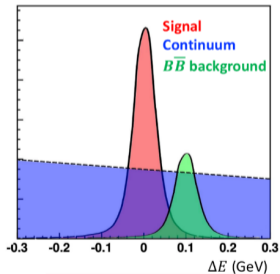


Hadronic cross-section
 @ $\sqrt{s} = 10.58 \text{ GeV}$

Tools at an $e^+ e^-$ flavour factory

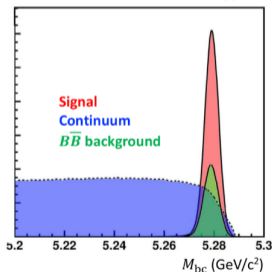
- Optimised variables to exploit information on initial kinematics
- Exploit different event shape to separate $B\bar{B}$ from continuum background

$$\Delta E = E_B^* - \sqrt{s}/2$$

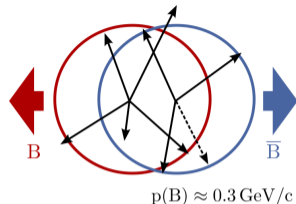


Expected $\Delta E \simeq 0$

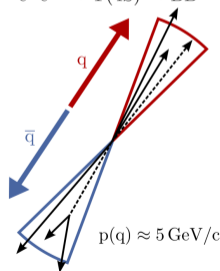
$$M_{bc} = \sqrt{(\sqrt{s}/2)^2 - \vec{p}_B^{*2}}$$



Expected $M_{bc} \simeq m_B$



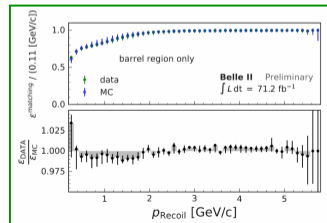
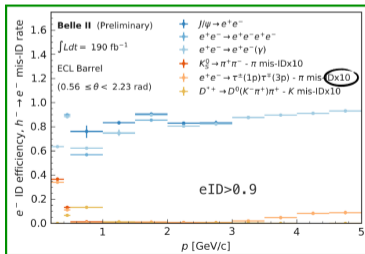
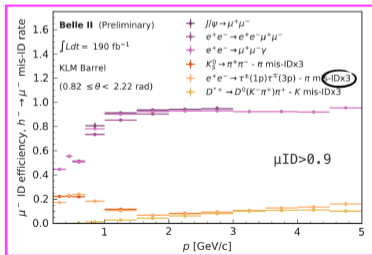
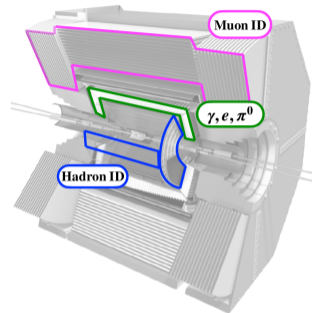
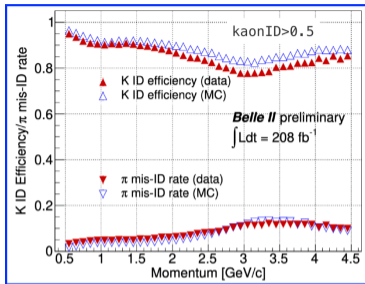
$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$



$$e^+e^- \rightarrow q\bar{q} \quad (q \in \{u, d, s, c\})$$

Key Belle II performances



- Good kaon identification in full momentum range
 - ▶ $\varepsilon(K) \sim 90\%$, $\pi \rightarrow K \sim 6\%$
- High photon efficiency
 - ▶ $\varepsilon(\gamma) \sim 90\%$ ($p > 1.5$ GeV)
- Good lepton ID performance
 - ▶ $\varepsilon(\mu) \sim 90\%$, $\pi \rightarrow \mu \sim 7\%$
 - ▶ $\varepsilon(e) \sim 86\%$, $\pi \rightarrow e \sim 0.4\%$



New results since last Moriond QCD

- $\mathcal{B}, A_{\text{CP}}$ and Δ_{+0} of $B \rightarrow K^* \gamma$
- $\mathcal{B}, A_{\text{CP}}$ and A_I of $B \rightarrow \rho \gamma$
- Search for $B^0 \rightarrow \gamma \gamma$
- Search for rare $b \rightarrow ll$ decays
- First evidence of $B^+ \rightarrow K^+ \nu \bar{\nu}$

Datasets

	on-resonance	off-resonance
	711 fb ⁻¹	90 fb ⁻¹
	362 fb ⁻¹	42 fb ⁻¹





$$B \rightarrow K^* \gamma$$

$B \rightarrow K^* \gamma$: motivation

- Flavour changing neutral current decays sensitive to new physics
- CP (A_{CP}) and isospin (Δ_{+0}) asymmetries are theoretically clean thanks to form factor cancellations
- Latest Belle measurement found evidence of isospin asymmetry at 3.1σ [[Phys. Rev. Lett. 119, 191802 \(2017\)](#)]

$$A_{CP} = \frac{\Gamma(\bar{B} \rightarrow \bar{K}^* \gamma) - \Gamma(B \rightarrow K^* \gamma)}{\Gamma(\bar{B} \rightarrow \bar{K}^* \gamma) + \Gamma(B \rightarrow K^* \gamma)}$$

$$\Delta_{+0} = \frac{\Gamma(B^0 \rightarrow K^{*0} \gamma) - \Gamma(B^+ \rightarrow K^{*+} \gamma)}{\Gamma(B^0 \rightarrow K^{*0} \gamma) + \Gamma(B^+ \rightarrow K^{*+} \gamma)}$$

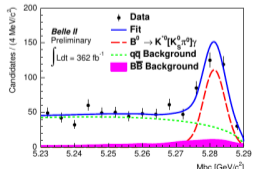
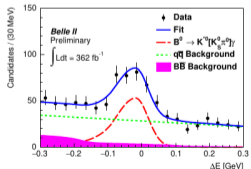
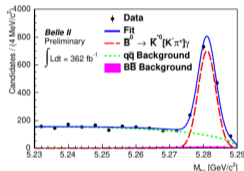
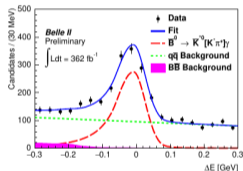
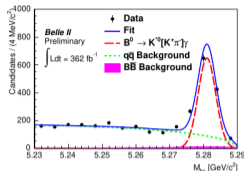
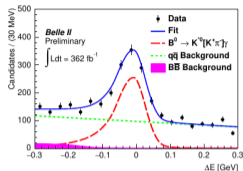
Goal

Using the 362 fb^{-1} Belle II run 1 dataset

- Measure $\mathcal{B}(B^{\pm,0} \rightarrow K^{*\pm,0} \gamma)$ with $K^* \rightarrow K^+ \pi^-, K_S^0 \pi^0, K^+ \pi^0$ and $K_S^0 \pi^+$
- Measure A_{CP} for all modes except $B^0 \rightarrow K^{*0} (\rightarrow K_S^0 \pi^0) \gamma$

$B \rightarrow K^* \gamma$: analysis strategy

- Reconstruct 4 K^* modes: $K^+ \pi^-$, $K_S^0 \pi^0$, $K^+ \pi^0$ and $K_S^0 \pi^+$
- 2 MVA classifiers to reject
 - photons from asymmetric $\pi^0 \rightarrow \gamma\gamma$ and $\eta \rightarrow \gamma\gamma$ decays
 - continuum events
- Improve M_{bc} resolution and reduce correlation with ΔE by replacing magnitude photon momentum with $E_{\text{beam}}^* - E_{K^*}$
- 2D $M_{bc} - \Delta E$ fit to extract
 - Simultaneously yields of B and anti- B for self-tagged modes for A_{CP} and \mathcal{B}
 - Yield of $B \rightarrow K^{*0} (\rightarrow K_S^0 \pi^0) \gamma$ for \mathcal{B}



$B \rightarrow K^* \gamma$: results

- Consistent with World average and SM
- Similar sensitivity as Belle despite smaller sample

$$\mathcal{B}[B^0 \rightarrow K^{*0} \gamma] = (4.16 \pm 0.10 \pm 0.11) \times 10^{-5},$$

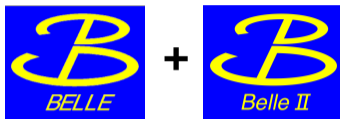
$$\mathcal{B}[B^+ \rightarrow K^{*+} \gamma] = (4.04 \pm 0.13 \pm 0.13) \times 10^{-5},$$

$$\mathcal{A}_{CP}[B^0 \rightarrow K^{*0} \gamma] = (-3.2 \pm 2.4 \pm 0.4)\%,$$

$$\mathcal{A}_{CP}[B^+ \rightarrow K^{*+} \gamma] = (-1.0 \pm 3.0 \pm 0.6)\%,$$

$$\Delta \mathcal{A}_{CP} = (2.2 \pm 3.8 \pm 0.7)\%, \text{ and}$$

$$\Delta_{0+} = (5.1 \pm 2.0 \pm 1.5)\%,$$



$B \rightarrow \rho\gamma$

$B \rightarrow \rho\gamma$: motivation

- Flavour changing neutral current decays sensitive to new physics,
- SM \mathcal{B} suppressed by $|V_{td}/V_{ts}| \simeq 0.04$ with respect to $B \rightarrow K^*\gamma$
- Previously observed at Belle [[Phys.Rev.Lett.101:111801,2008](#)] and BaBar [[Phys.Rev.D78:112001,2008](#)]
- Almost 2σ tension between current world average $A_I = (30_{-13}^{+16}\%)$ and SM $(5.2 \pm 2.8)\%$ [[Lyon, Zwicky '13](#)]

$$A_{\text{CP}}(B \rightarrow \rho\gamma) = \frac{\Gamma(\bar{B} \rightarrow \bar{\rho}\gamma) - \Gamma(B \rightarrow \rho\gamma)}{\Gamma(\bar{B} \rightarrow \bar{\rho}\gamma) + \Gamma(B \rightarrow \rho\gamma)}$$

$$A_I = \frac{2\Gamma(\bar{B}^0 \rightarrow \rho^0\gamma) - \Gamma(B^\pm \rightarrow \rho^\pm\gamma)}{2\Gamma(\bar{B}^0 \rightarrow \rho^0\gamma) + \Gamma(B^\pm \rightarrow \rho^\pm\gamma)}$$

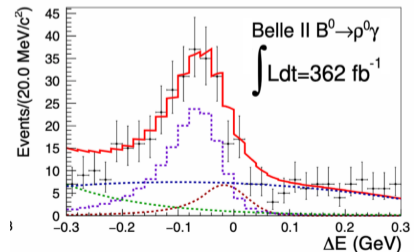
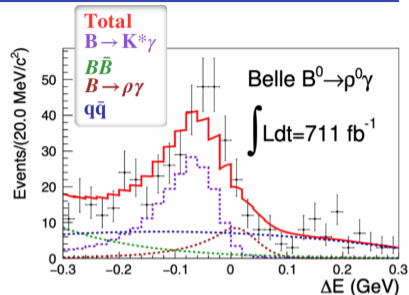
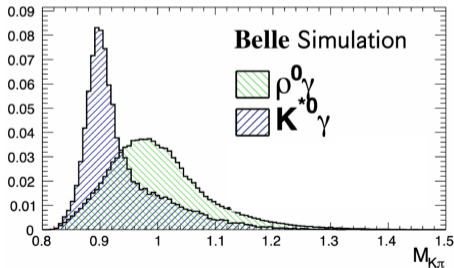
Goal

Using the 362 fb^{-1} Belle II run 1 dataset

- Measure $\mathcal{B}(B^{\pm,0} \rightarrow \rho^{\pm,0}\gamma)$ with $\rho^0 \rightarrow \pi^+\pi^-$, and $\rho^\pm \rightarrow \pi^\pm\pi^0$
- Measure $A_{\text{CP}}(B^+ \rightarrow \rho^+\gamma)$ and $A_I(B \rightarrow \rho\gamma)$

$B \rightarrow \rho\gamma$: analysis strategy

- 2 MVA classifiers against photons from π^0/η and continuum events
- Improve M_{bc} resolution for $B^0 \rightarrow \rho^0\gamma$ replacing magnitude photon momentum with $E_{\text{beam}}^* - E_{\rho^0}$
- Large background from $B \rightarrow K^*\gamma$ ($K \rightarrow \pi$ misID)
- Belle+Belle II simultaneous 3D fit of M_{bc} , ΔE and $M_{K\pi}$



$B \rightarrow \rho\gamma$: results

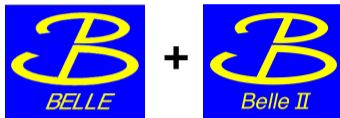
- Obtain most precise measurements to date
- A_I consistent with SM at 0.6σ

$$\mathcal{B}(B^+ \rightarrow \rho^+ \gamma) = (13.1_{-1.9}^{+2.0} {}_{-1.2}^{+1.3}) \times 10^{-7},$$

$$\mathcal{B}(B^0 \rightarrow \rho^0 \gamma) = (7.5 \pm 1.3_{-0.8}^{+1.0}) \times 10^{-7},$$

$$A_{\text{CP}}(B^+ \rightarrow \rho^+ \gamma) = (-8.2 \pm 15.2_{-1.2}^{+1.6}) \%,$$

$$A_I(B \rightarrow \rho\gamma) = (10.9_{-11.7}^{+11.2} {}_{-6.2}^{+6.8} {}_{-3.9}^{+3.8}) \%,$$



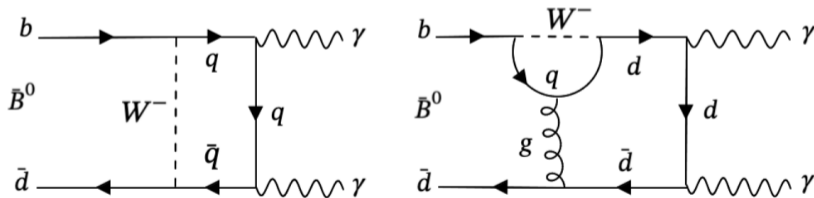
$$B^0 \rightarrow \gamma\gamma$$

$B^0 \rightarrow \gamma\gamma$: motivation

- Flavour changing neutral current decay sensitive to new physics
- Expected $\mathcal{B}(B^0 \rightarrow \gamma\gamma) = 1.4_{-0.8}^{+1.4} \times 10^{-8}$
[Shen, Wang, Wei '09]
- Current best upper limit by BaBar
 $\mathcal{B}(B^0 \rightarrow \gamma\gamma) < 3.2 \times 10^{-7}$
[Phys.Rev.D83:032006,2011]

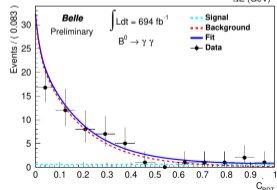
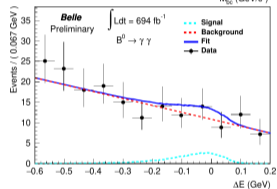
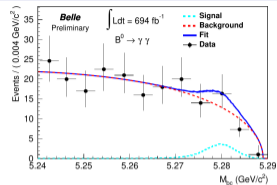
Goal

Search for the $B^0 \rightarrow \gamma\gamma$ decay using the 1.07 ab^{-1} Belle + Belle II dataset



$B^0 \rightarrow \gamma\gamma$: analysis strategy

- Combine two high energy photons from the barrel
- 2 MVA classifiers against photons from π^0/η and continuum events
- Photon timing cuts to suppress peaking background in M_{bc} from combinations of back-to-back off-time photons
- Belle+Belle II simultaneous 3D fit on M_{bc} , ΔE and output MVA classifier
 - Use KDE to model $M_{bc} - \Delta E$ correlation for signal
- Use $B^0 \rightarrow K^{*0}(\rightarrow K^+\pi^-)\gamma$ as control channel to derive data/MC efficiency corrections



$B^0 \rightarrow \gamma\gamma$: results

- $9.1_{-4.4}^{+5.6}/615 \pm 25$ and $1.9_{-2.8}^{+4.2}/317 \pm 18$ signal/background events in Belle and Belle II datasets
- 2.5σ combined significance
- 90% CL upper limit improved by a factor 5 over BaBar

	$\mathcal{B}(B^0 \rightarrow \gamma\gamma)$	$\mathcal{B}(B^0 \rightarrow \gamma\gamma)$ (at 90% CL)
Belle	$(5.4_{-2.6}^{+3.3} \pm 0.5) \times 10^{-8}$	$< 9.9 \times 10^{-8}$
Belle II	$(1.7_{-2.4}^{+3.7} \pm 0.3) \times 10^{-8}$	$< 7.4 \times 10^{-8}$
Combined	$(3.7_{-1.8}^{+2.2} \pm 0.7) \times 10^{-8}$	$< 6.4 \times 10^{-8}$



Rare $b \rightarrow ll$

Rare $b \rightarrow ll$: motivation

$b \rightarrow dll$ transitions

- FCNC sensitive to new physics complementary to $b \rightarrow sll$
- Extra CKM suppression $|V_{td}/V_{ts}|^2 \sim 0.04$ wrt $b \rightarrow sll$
- Typical $\mathcal{B} = \mathcal{O}(10^{-8})$ or smaller

Channel	UL or BR	Collaboration
$B^0 \rightarrow \eta ee$	$< 10.8 \times 10^{-8}$	BaBar
$B^0 \rightarrow \eta \mu\mu$	$< 11.2 \times 10^{-8}$	BaBar
$B^0 \rightarrow \pi^0 ee$	$< 8.4 \times 10^{-8}$	BaBar
$B^0 \rightarrow \pi^0 \mu\mu$	$< 6.9 \times 10^{-8}$	BaBar
$B^+ \rightarrow \pi^+ ee$	$< 8.0 \times 10^{-8}$	Belle
$B^+ \rightarrow \pi^+ \mu\mu$	$(1.78 \pm 0.22 \pm 0.03) \times 10^{-8}$	LHCb
$B^0 \rightarrow \rho^0 \mu\mu$	$(1.98 \pm 0.53) \times 10^{-8}$	LHCb

Goal

Look for all the $B^{\pm,0} \rightarrow (\eta, \omega, \pi^{\pm,0}, \rho^{\pm,0})ll$ decays (except $B^+ \rightarrow \pi^+ \mu\mu$ and $B^+ \rightarrow \rho^0 \mu\mu$ already seen by LHCb)

BaBar: [[Phys.Rev.D 88 \(2013\) 3, 032012](#)]

Belle: [[Phys.Rev.D 78 \(2008\) 011101](#)]

LHCb: [[JHEP 10 \(2015\) 034](#), [Phys.Lett.B 743 \(2015\) 46](#)]

Rare $b \rightarrow ll$: analysis strategy

- Reconstruct 12 decay chains

$$B \rightarrow \{\pi, \rho, \eta, \omega\} \ell \ell \quad \begin{cases} \rho^{+,0} \rightarrow \pi^+ \pi^{0,-} \\ \eta \rightarrow \gamma \gamma, \pi^+ \pi^- \pi^0 \\ \omega \rightarrow \pi^+ \pi^- \pi^0 \end{cases}$$

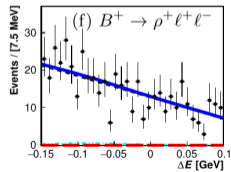
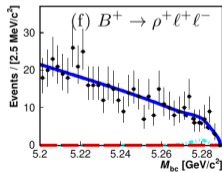
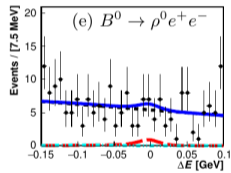
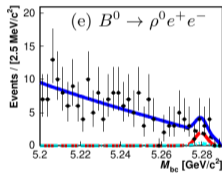
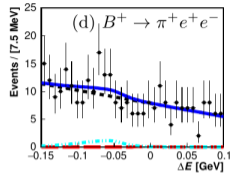
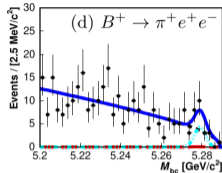
- MVA classifier against continuum background

- Suppress specific peaking backgrounds

- Veto around J/ψ and $\psi(2S)$ masses
- Veto 2-misID $D^0 \rightarrow K^+ \pi^-$ in $B^+ \rightarrow \rho^+ ll$
- $p_{\pi^0} > 1 \text{ GeV}$ and $p_{\pi^+} > 1 \text{ GeV}$ in $B^+ \rightarrow \pi^+ ll$ against 2-photon backgrounds
- $q_{ee}^2 > 0.045 \text{ GeV}^2$ against photon conversions and π^0 Dalitz decays

- 2D fit on M_{bc} and ΔE to extract signal yields

- Model remaining peaking background (charmless, $B^+ \rightarrow K^+ e^+ e^-$)



Rare $b \rightarrow ll$: results

No signal observed, set 90% CL upper limits

channel	N_{sig}	$N_{\text{sig}}^{\text{UL}}$	ϵ (%)	\mathcal{B}^{UL} (10^{-8})	\mathcal{B} (10^{-8})
$B^0 \rightarrow \eta e^+ e^-$	$0.0^{+1.4}_{-1.0}$	3.1	3.9	< 10.5	$0.0^{+4.9}_{-3.4} \pm 0.1$
$B^0 \rightarrow \eta \mu^+ \mu^-$	$0.8^{+1.5}_{-1.1}$	4.2	5.9	< 9.4	$1.9^{+3.4}_{-2.5} \pm 0.2$
$B^0 \rightarrow \eta \ell^+ \ell^-$	$0.5^{+1.0}_{-0.8}$	1.8	4.9	< 4.8	$1.3^{+2.8}_{-2.2} \pm 0.1$
$B^0 \rightarrow \omega e^+ e^-$	$-0.3^{+3.2}_{-2.5}$	3.7	1.6	< 30.7	$-2.1^{+26.5}_{-20.8} \pm 0.2$
$B^0 \rightarrow \omega \mu^+ \mu^-$	$1.7^{+2.3}_{-2.7}$	5.5	2.9	< 24.9	$7.7^{+10.8}_{-7.5} \pm 0.6$
$B^0 \rightarrow \omega \ell^+ \ell^-$	$1.0^{+1.8}_{-1.3}$	3.6	2.2	< 22.0	$6.4^{+10.7}_{-7.8} \pm 0.5$
$B^0 \rightarrow \pi^0 e^+ e^-$	$-2.9^{+1.8}_{-1.4}$	4.0	6.7	< 7.9	$-5.8^{+3.6}_{-2.8} \pm 0.5$
$B^0 \rightarrow \pi^0 \mu^+ \mu^-$	$-0.5^{+3.6}_{-2.7}$	6.1	13.7	< 5.9	$-0.4^{+3.5}_{-2.6} \pm 0.1$
$B^0 \rightarrow \pi^0 \ell^+ \ell^-$	$-1.8^{+1.6}_{-1.1}$	2.9	10.2	< 3.8	$-2.3^{+2.1}_{-1.5} \pm 0.2$
$B^+ \rightarrow \pi^+ e^+ e^-$	$0.1^{+2.5}_{-1.6}$	5.0	11.5	< 5.4	$0.1^{+2.7}_{-1.8} \pm 0.1$
$B^0 \rightarrow \rho^0 e^+ e^-$	$5.6^{+3.5}_{-2.7}$	10.8	3.2	< 45.5	$23.6^{+14.6}_{-11.2} \pm 1.1$
$B^+ \rightarrow \rho^+ e^+ e^-$	$-4.4^{+2.3}_{-2.0}$	5.3	1.4	< 46.7	$-38.2^{+24.5}_{-17.2} \pm 3.4$
$B^+ \rightarrow \rho^+ \mu^+ \mu^-$	$3.0^{+4.0}_{-3.0}$	8.7	2.9	< 38.1	$13.0^{+17.5}_{-13.3} \pm 1.1$
$B^+ \rightarrow \rho^+ \ell^+ \ell^-$	$0.4^{+3.3}_{-1.8}$	3.0	2.0	< 18.9	$2.5^{+14.6}_{-11.8} \pm 0.2$

- Obtained upper limits in the range $(3.8 - 47) \times 10^{-8}$
- Best upper limit for all searched decay modes
- $B^0 \rightarrow \omega ll$, and $B^{\pm,0} \rightarrow \rho^{\pm,0} ll$ searched for the first time



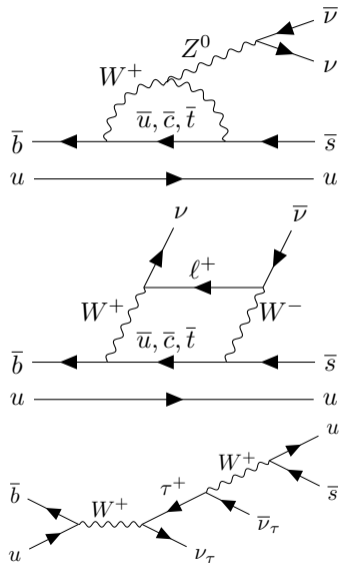
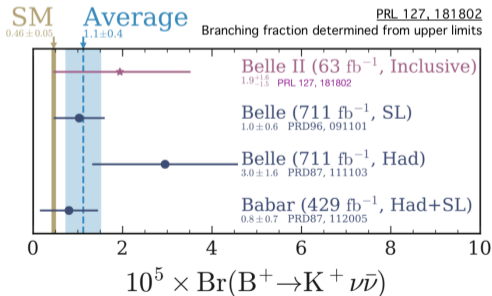
$$B^+ \rightarrow K^+ \nu \bar{\nu}$$

[arXiv:2311.14647]

Evidence for $B^+ \rightarrow K^+ \nu \bar{\nu}$: motivations

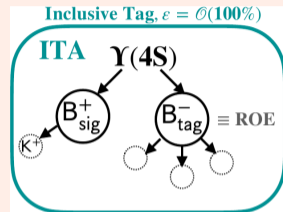
[arXiv:2311.14647]

- $B^+ \rightarrow K^+ \nu \bar{\nu}$ known with high accuracy in the SM
 - ▶ Clean SM computation (no charm loop contributions)
 - ▶ $\mathcal{B}_{SM} = (5.58 \pm 0.37) \times 10^{-6}$ [Parrott, Bouchard, Davies '23]
 - ▶ New physics could increase significantly the rate
 - ▶ Possible to recast to look for $B^+ \rightarrow K^+ X_{dark}$
- Very challenging experimentally, not yet observed
 - ▶ Low \mathcal{B} , high background contributions
 - ▶ 3-body kinematics, no good variable to fit



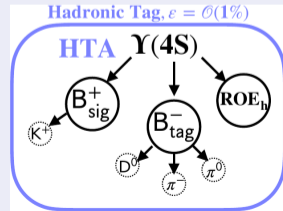
Inclusive tagged analysis (ITA): approach leading to the final sensitivity

- Select first signal kaon that minimises q_{rec}^2 (computed as K^+ recoil)
- Two consecutive MVA classifiers
- Total efficiency $\sim 8\%$, purity $\sim 0.8\%$
- Binned fit to q_{rec}^2 and output MVA classifier simultaneously for on and off resonance

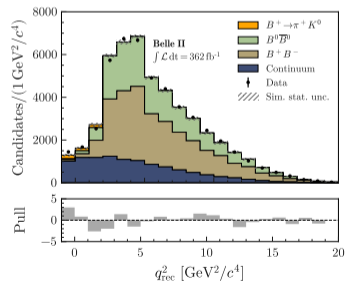
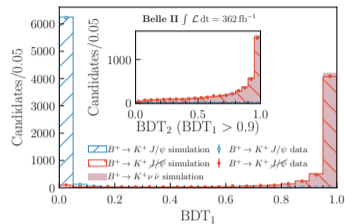


Hadronically tagged analysis (HTA): Less sensitive but well-established

- Select first tag B decaying hadronically
- One MVA classifier to reject background
- Total efficiency $\sim 0.4\%$, purity $\sim 3.5\%$
- Fit output MVA classifier

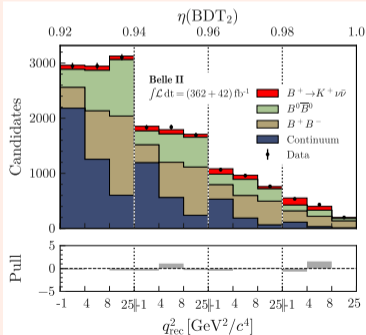


- Analysis relies on simulation for background suppression and background templates for the fit
 - Simulation is validated via several control channels on data
- Signal validation
 - Total efficiency with $B^+ \rightarrow J/\psi K^+$, removing J/ψ and correcting the kaon kinematics to match the signal
 - Kaon ID selection validated with $B^+ \rightarrow \bar{D}^0 (\rightarrow K^+ \pi^-) K^+$
- Background validation
 - Off-resonance data to correct for data/MC differences in normalisation and shape
 - Size of $B \rightarrow X_c(K_L^0 X)$ corrected using pion-enriched sideband
 - Modelling of K_L^0 detection efficiency in the calorimeter corrected using $e^+ e^- \rightarrow \gamma \phi (\rightarrow K_S^0 K_L^0)$
 - Cross check $B^+ \rightarrow K^+ K_S^0 K_S^0$ to validate $B^+ \rightarrow K^+ K_L^0 K_L^0$
- Closure test measuring $\mathcal{B}(B^+ \rightarrow \pi^+ K^0) = (2.5 \pm 0.5) \times 10^{-5}$
 - compatible with PDG $(2.38 \pm 0.08) \times 10^{-5}$



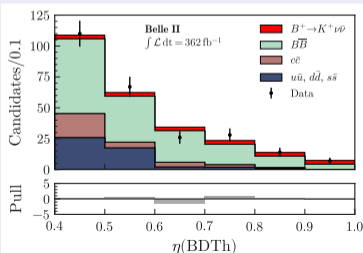
ITA

- $\mathcal{B} = (2.7 \pm 0.5 \pm 0.5) \times 10^{-5}$
- 3.5σ significance
- 2.9σ deviation from SM



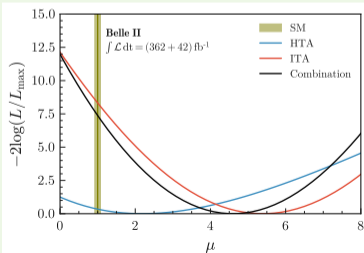
HTA

- $\mathcal{B} = (1.1^{+0.9+0.8}_{-0.8-0.5}) \times 10^{-5}$
- 1.1σ significance
- 0.6σ deviation from SM



Combination

- 1.2σ agreement between ITA and HTA, 2% common events
- $\mathcal{B} = (2.3 \pm 0.5^{+0.5}_{-0.5}) \times 10^{-5}$
- 3.5σ significance
- 2.7σ deviation from SM



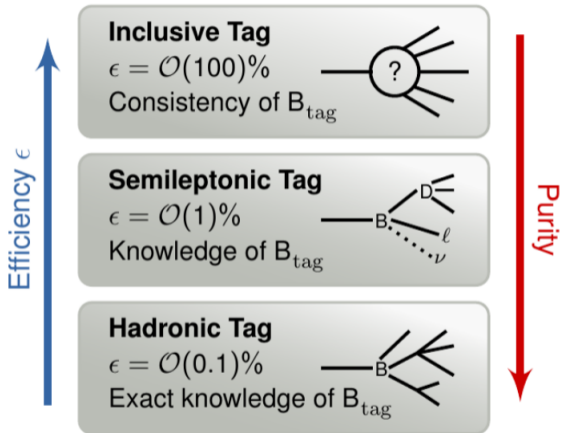
Conclusion

- Electroweak and radiative penguin B decays are promising place to look for New Physics
- Five Belle and Belle II new results since last Moriond
 - New measurements of \mathcal{B} , A_{CP} and Δ_{+0} of $B \rightarrow K^* \gamma$ with Belle II
 - Best measurements of \mathcal{B} , A_{CP} and A_I of $B \rightarrow \rho \gamma$ with Belle+Belle II
 - Best upper limit on $B^0 \rightarrow \gamma \gamma$ with Belle+Belle II
 - Best upper limits on rare $b \rightarrow ll$ decays with Belle
 - First evidence of $B^+ \rightarrow K^+ \nu \bar{\nu}$ with Belle II
- Results statistically limited; Belle II Run 2 data taking just started, stay tuned for updates

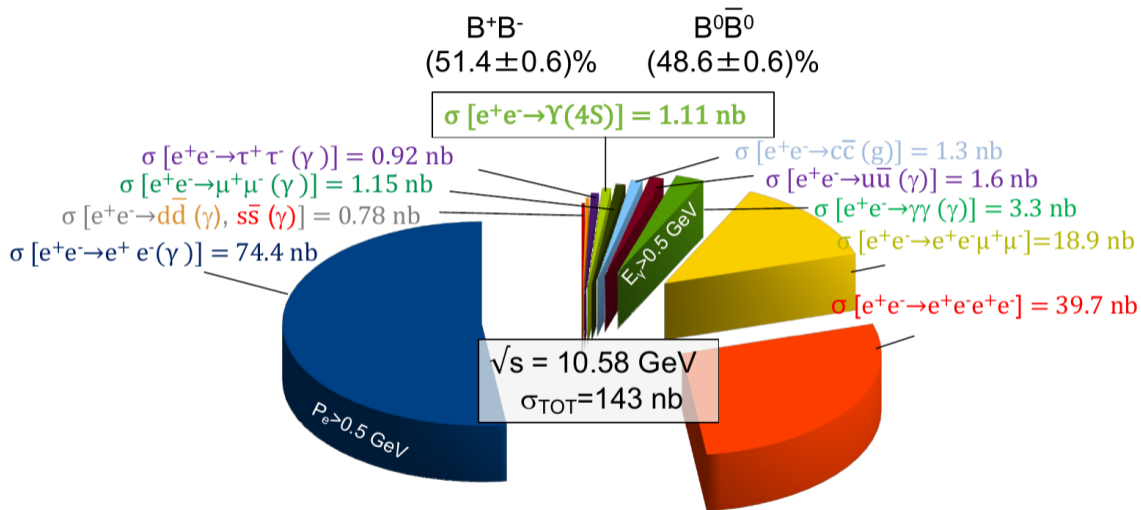


BACKUP

Tagging strategies



Cross sections at the $\Upsilon(4S)$



$B \rightarrow \rho\gamma$: systematics

Source	$\mathcal{B}_{\rho^+\gamma} \times 10^8$	$\mathcal{B}_{\rho^0\gamma} \times 10^8$	A_I	A_{CP}
Reconstruction	4.1	1.3	1.4%	0.5%
Selection	9.0	3.4	4.0%	0.5%
Fixed PDF	1.1	2.7	1.8%	0.2%
Signal shape	4.7	3.0	3.1%	0.5%
Histogram PDF	1.0	0.6	0.5%	0.1%
$K^*\gamma$ yield	3.4	5.4	3.1%	0.1%
$B\bar{B}$ peaking yield	2.2	0.8	0.9%	0.2%
$B\bar{B}$ peaking A_{CP}	0.1	0.0	0.1%	1.0%
Number of $B\bar{B}$'s	1.7	1.4	0.3%	0.1%
Other parameters	4.0	3.6	3.9%	0.0%
Total	12.5	8.6	7.5%	1.4%

TABLE I. Summary of systematic uncertainties on the signal yield.

Source	Belle (events)	Belle II (events)
Fit bias	+0.16	+0.12
PDF parameterization	+0.56 -0.48	+0.30 -0.32
Shape Modeling	+0.06	+0.04
Total (sum in quadrature)	+0.58 -0.48	+0.30 -0.32

TABLE II. Summary of systematic uncertainties on signal efficiencies.

Source	Belle (%)	Belle II (%)
Photon Detection Efficiency	4.0	2.7
Reconstruction Efficiency (ϵ_{rec})	0.6	0.5
Number of $B\bar{B}$	1.3	1.5
f^{00}	2.5	2.5
C_{BDT} requirement	0.4	0.9
π^0/η veto	0.3	0.4
Timing requirement efficiency	2.8	–
Total (sum in quadrature)	5.7	4.1

Rare $b \rightarrow ll$: systematics

source	ηee	$\eta \mu\mu$	ωee	$\omega \mu\mu$	$\pi^0 ee$	$\pi^0 \mu\mu$	$\pi^+ ee$	$\rho^0 ee$	$\rho^0 \mu\mu$	$\rho^+ ee$	$\rho^+ \mu\mu$
μ	—	0.6	—	0.6	—	0.6	—	—	0.6	—	0.6
e	0.8	—	0.8	—	0.8	—	0.8	0.8	—	0.8	—
π^+	1.0	1.0	1.0	1.0	—	—	0.5	1.0	1.0	0.5	0.5
π^0	2.3	2.3	2.3	2.3	2.3	2.3	—	—	—	2.3	2.3
γ	4.0	4.0	—	—	—	—	—	—	—	—	—
BDT	7.1	6.6	7.1	6.6	7.1	6.6	1.4	1.4	0.8	7.1	6.6
MC	0.48	0.37	0.73	0.53	0.34	0.24	0.24	0.53	0.34	0.80	0.54
track	0.7-1.4	0.7-1.4	1.4	1.4	0.7	0.7	1.05	1.4	1.4	1.05	1.05
PDF	0.04	0.04	0.43	0.07	0.10	0.09	0.50	0.20	0.06	0.34	0.32
$f^{+-/00}$	2.45	2.45	2.45	2.45	2.45	2.45	2.45	2.45	2.45	2.45	2.45
$N_{B\bar{B}}$	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4	1.4
Total	9.27	8.87	8.25	7.78	8.06	7.60	3.50	3.72	3.47	8.15	7.68

$$B^+ \rightarrow K^+ \nu \bar{\nu}$$

