

# Search for charged-lepton flavor violation in $\Upsilon(2S) \rightarrow \ell^\mp \tau^\pm (\ell = e, \mu)$ decays at Belle

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① The Belle Experiment

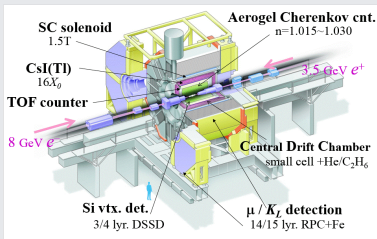
② Motivation

③  $\Upsilon(2S) \rightarrow \ell^\mp \tau^\pm (\ell = e, \mu)$  study at Belle.

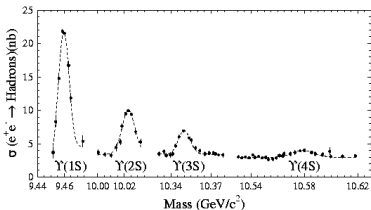
④ Results

# The Belle Experiment

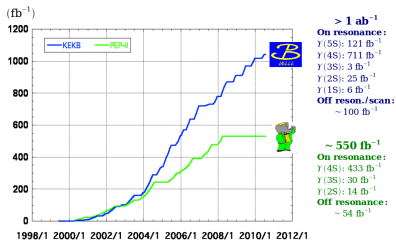
Well known to measure the CP-violation in the B-meson decays.



Measured by CUSB.



## Integrated luminosity of B factories



- KEKB: An asymmetric-energy  $e^-$  (8 GeV) $e^+$  (3.5 GeV) collider, collided at the center-of-mass energy of 10.58 GeV.
- Belle detector was placed at the interaction point (IP) of KEKB.
- Collected most of the data at  $\Upsilon(4S)$  resonance, however it also collected data at  $\Upsilon(1S)$ ,  $\Upsilon(2S)$ ,  $\Upsilon(3S)$ , and so on.

- The lepton flavor conservation is an intrinsic property of the Standard Model (SM).
- The experimental evidence of lepton flavor violation has already been observed in neutrino oscillation.
- The transitions involving charged-lepton flavor violation (CLFV) are mediated by  $W^\pm$  bosons and massive neutrinos to account for neutrino oscillation.
- In consequence, the CLFV transitions  $\Rightarrow$  significantly suppressed  $\sim m_\nu^2/m_W^2$ . For e.g.,  $\mathcal{B}(\mu \rightarrow e\gamma) \sim 10^{-54}$
- Several new physics models (for e.g. leptoquarks) predict the enhanced BF for such transitions  $\Rightarrow$  high luminosity experiments.
- With the current statistics, CLFV cannot be seen in  $\Upsilon(4S)$ ; it decays immediately to pair of B mesons. So, CLFV in  $\Upsilon(nS)$  ( $n=1,2,3$ ) is a good probe for the physics beyond the SM.
- Any observation of CLFV  $\Rightarrow$  clearest evidence of the new physics.

# CLFV in $\Upsilon(nS)$ decays

- BaBar, CLEO, and recently Belle searched for CLFV in  $\Upsilon(nS) \rightarrow \ell\tau$  ( $n=1,2,3$ ) decays.

Table: Experimental results on  $\Upsilon(nS)$  CLFV transitions

Decay modes	Upper limits	Experiments	References
$B(\Upsilon(1S) \rightarrow \mu\tau)$	$< 6 \times 10^{-6}$	CLEO	<a href="#">PRL 101, 201601 (2008)</a>
$B(\Upsilon(1S) \rightarrow e\tau)$	$< 2.7 \times 10^{-6}$	Belle	<a href="#">JHEP 05 2022, 095 (2022)</a>
$B(\Upsilon(1S) \rightarrow \mu\tau)$	$< 2.7 \times 10^{-6}$	Belle	<a href="#">JHEP 05 2022, 095 (2022)</a>
$B(\Upsilon(2S) \rightarrow \mu\tau)$	$< 14.4 \times 10^{-6}$	CLEO	<a href="#">PRL 101, 201601 (2008)</a>
$B(\Upsilon(2S) \rightarrow e\tau)$	$< 3.2 \times 10^{-6}$	BaBar	<a href="#">PRL 104, 151802 (2010)</a>
$B(\Upsilon(2S) \rightarrow \mu\tau)$	$< 3.3 \times 10^{-6}$	BaBar	<a href="#">PRL 104, 151802 (2010)</a>
$B(\Upsilon(3S) \rightarrow \mu\tau)$	$< 26.3 \times 10^{-6}$	CLEO	<a href="#">PRL 101, 201601 (2008)</a>
$B(\Upsilon(3S) \rightarrow e\tau)$	$< 4.2 \times 10^{-6}$	BaBar	<a href="#">PRL 104, 151802 (2010)</a>
$B(\Upsilon(3S) \rightarrow \mu\tau)$	$< 3.1 \times 10^{-6}$	BaBar	<a href="#">PRL 104, 151802 (2010)</a>

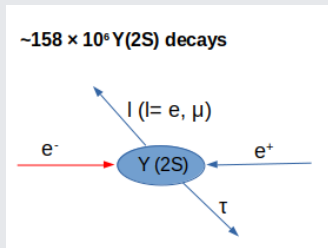
- No signal observed yet!

Table: Data sample and the number of  $\Upsilon(nS)$  at B-factories and CLEO

Experiment	$\Upsilon(1S)$ data ( $N_{\Upsilon(1S)}$ )	$\Upsilon(2S)$ data ( $N_{\Upsilon(2S)}$ )	$\Upsilon(3S)$ data ( $N_{\Upsilon(3S)}$ )
CLEO	$1.1 \text{ fb}^{-1}$ (20.8 M)	$1.3 \text{ fb}^{-1}$ (9.3 M)	$1.4 \text{ fb}^{-1}$ (5.9 M)
Belle	$6 \text{ fb}^{-1}$ (119 M)	$25 \text{ fb}^{-1}$ (158 M)	$3 \text{ fb}^{-1}$ (11 M)
BaBar	-	$14 \text{ fb}^{-1}$ (98.6 M)	$30 \text{ fb}^{-1}$ (116.7 M)

# $\Upsilon(2S) \rightarrow \ell^\mp \tau^\pm (\ell = e, \mu)$ decays at Belle

- We search for decays  $\Upsilon(2S) \rightarrow \ell_1^\mp \tau^\pm$  with  $\tau^+ \rightarrow \ell_2^+ \nu_{\ell_2} \bar{\nu}_\tau$  or  $\tau^+ \rightarrow \pi^+ \pi^0 \bar{\nu}_\tau$ . Charge conjugation is applied.
- We don't consider the combination of the same flavored  $\ell_1$  and  $\ell_2$ . For e.g.  $\Upsilon(2S) \rightarrow \mu^\mp \tau^\pm (\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau)$  to avoid the background contribution from  $e^+ e^- \rightarrow \mu^+ \mu^-$  events.
- We also don't use this mode,  $\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau$  since  $\pi^+$  can fake as  $\mu/e$  and can contribute to the background.
- Reconstruct:  $\Upsilon(2S)$  from  $\ell_1$  and  $\tau$ ;  $\tau$  from  $\ell_2$  or  $\pi^+ \pi^0$ .  $\Upsilon(2S)$  cannot be fully reconstructed!
- Decay modes in study:
  - $\Upsilon(2S) \rightarrow \mu^\mp \tau^\pm (\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau)$  [ $\mu - e$ ]
  - $\Upsilon(2S) \rightarrow e^\mp \tau^\pm (\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau)$  [ $e - \mu$ ]
  - $\Upsilon(2S) \rightarrow \mu^\mp \tau^\pm (\tau^+ \rightarrow \pi^+ \pi^0 \bar{\nu}_\tau)$  [ $\mu - \pi \pi^0$ ]
  - $\Upsilon(2S) \rightarrow e^\mp \tau^\pm (\tau^+ \rightarrow \pi^+ \pi^0 \bar{\nu}_\tau)$  [ $e - \pi \pi^0$ ]
- Trigger simulation is done to simulate the trigger effect.



## $\Upsilon(2S) \rightarrow \ell^\mp \tau^\pm (\ell = e, \mu)$ decays at Belle

- Signal MC: 5 million signal MC events of  $\Upsilon(2S) \rightarrow \ell^\mp \tau^\pm$ , where  $\tau$  can decay to anything are generated with EVTGEN.
- Background MC:
  - $e^+e^- \rightarrow e^+e^-$ ,  $e^+e^- \rightarrow \mu^+\mu^-$ ,  $e^+e^- \rightarrow \tau^+\tau^-$
  - $e^+e^- \rightarrow e^+e^-\mu^+\mu^-$ ,  $e^+e^- \rightarrow e^+e^-e^+e^-$
  - Inclusive  $\Upsilon(2S)$  decays.
  - $e^+e^- \rightarrow q\bar{q}$  ( $q = u, d, s, c$ ) processes generated with an initial state radiation (ISR) photon.

Most of the background samples  $\approx 25 \text{ fb}^{-1}$ .

Signal signature of  $\Upsilon(2S) \rightarrow \ell_1^\mp \tau^\pm$  is a monochromatic momentum of primary lepton ( $p_1^*$ ) with,

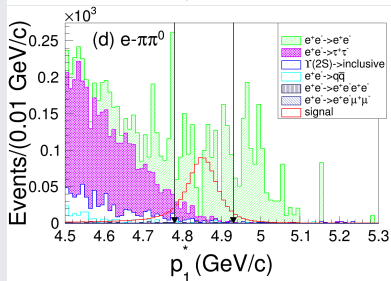
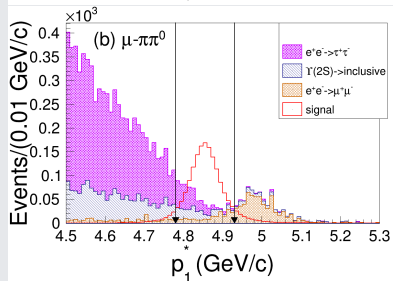
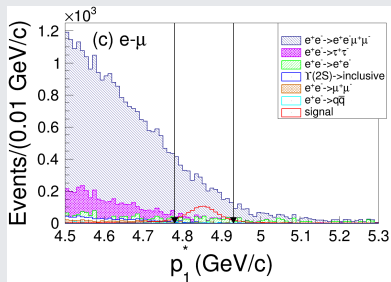
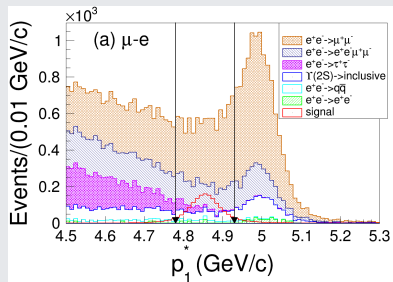
$$p_1^* = \sqrt{\frac{(m_{\Upsilon(2S)}^2 - m_{\ell_1}^2 - m_\tau^2)^2 - 4m_{\ell_1}^2 m_\tau^2}{4m_{\Upsilon(2S)}^2}};$$

peaks around  $4.85 \text{ GeV}/c$  in the c.m. frame.

Signal window:  $4.78 < p_1^* < 4.93 \text{ GeV}/c$  ( $2\sigma$  around the expected  $p_1^*$ ).

Sideband region:  $p_1^* \notin [4.7, 5.0]$ .

# Distribution of $p_1^*$ in MC

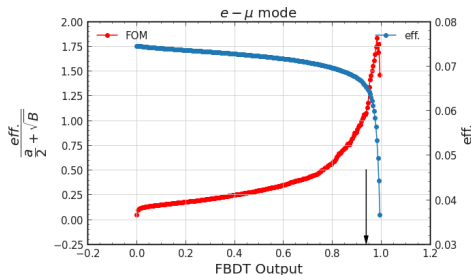
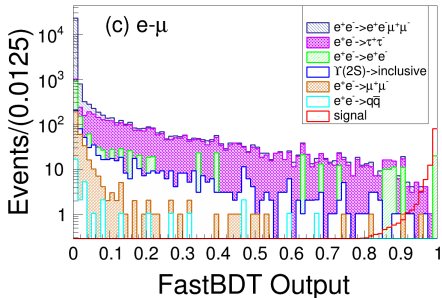


Huge background!



# Background suppression

- We use the multi-variate analysis (MVA) to further suppress the background.
- Classifier: FastBDT (trained on MC-simulated events).
- Input variable are:  $E_{ECL}$ ,  $E_{vis}^*$ ,  $M_{miss}^{*2}$ ,  $\cos\theta_{12}^*$ ,  $\cos\theta_{miss}^*$  based on energy of cluster, missing momentum, and the cosine angles.



We choose  $\mathcal{O}_{\text{FBDT}} > 0.94$ , which rejects more than 99% of the background events for all the modes while retaining 86%, 66%, 89%, and 66% of the signal events for the  $\mu-e$ ,  $\mu-\pi^0$ ,  $e-\mu$ , and  $e-\pi\pi^0$  modes.

# Background estimation

The expected number of background events ( $N_{\text{exp}}^{\text{bkg}}$ ) is calculated from,

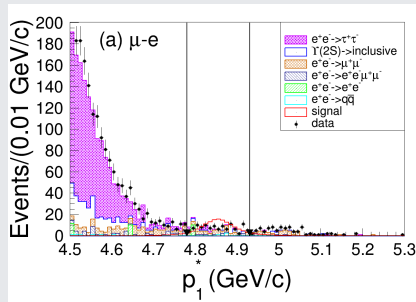
$$N_{\text{exp}}^{\text{bkg}} = N_{\text{data}}^{\text{SB}}(\text{BDT}) \times \left( \frac{N_{\text{MC}}}{N_{\text{MC}}^{\text{SB}}} \right) \text{ (loose BDT)}$$

where,

$N_{\text{data}}^{\text{SB}}$  - number of data events in the sideband region

$N_{\text{MC}}^{\text{SB}}$  - numbers of MC events in the sideband region

$N_{\text{MC}}$  - number of MC events in the signal region.

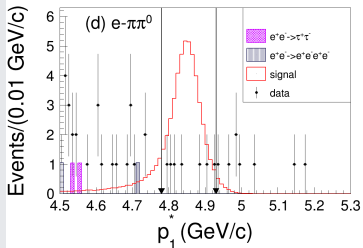
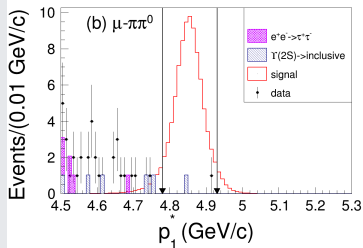
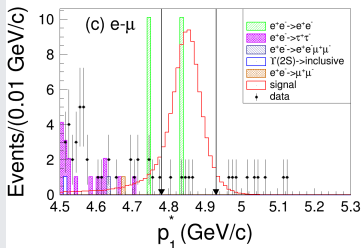
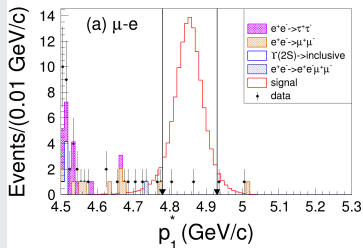


We estimate  $N_{\text{exp}}^{\text{bkg}}$  with  $\mathcal{O}_{\text{FBDT}} > 0.4$  as a nominal value and take the difference of the central value from  $0.2 < \mathcal{O}_{\text{FBDT}} < 0.4$  as a systematic error due to background estimation.

$$\text{For } \Upsilon(2S) \rightarrow \mu^{\mp} \tau^{\pm}, \quad N_{\text{exp}}^{\text{bkg}} = 3.9 \pm 1.8$$

$$\text{For } \Upsilon(2S) \rightarrow e^{\mp} \tau^{\pm}, \quad N_{\text{exp}}^{\text{bkg}} = 5.9 \pm 2.6$$

# Distribution of $p_1^*$ in MC and data with $\mathcal{O}_{\text{FBDT}} > 0.94$



For  $\Upsilon(2S) \rightarrow \mu^\mp \tau^\pm$ ,  $N_{\text{obs}} = 3$  which is consistent with the expectation.

For  $\Upsilon(2S) \rightarrow e^\mp \tau^\pm$ ,  $N_{\text{obs}} = 12$  which is larger than the expectation; the probability of obtaining 12 or more events with  $N_{\text{exp}}^{\text{bkg}} = 5.9 \pm 2.6$  is 8%.

Table: Summary of systematic uncertainties.

Source	Systematic uncertainty (%)	
	$\Upsilon(2S) \rightarrow \mu^+ \tau^\pm$	$\Upsilon(2S) \rightarrow e^+ \tau^\pm$
Number of $\Upsilon(2S)$	2.3	2.3
Tracking	0.7	0.7
Particle identification and $\pi^0$ reconstruction	3.4	3.3
$\tau$ branching fraction	0.2	0.2
MVA selection	5.1	5.0
Trigger	2.3	11.9
Total	7.0	13.5

# Results

We use the Feldman-Cousins method to set the upper limits on  $\mathcal{B}$  @ 90% CL.

$$\mathcal{B} = \frac{N_{\text{obs}} - N_{\text{exp}}^{\text{bkg}}}{\epsilon_{\text{sig}} \times N_{\Upsilon(2S)}}$$

$\epsilon_{\text{sig}}$ - signal reconstruction efficiency.

$N_{\Upsilon(2S)}$ - number of  $\Upsilon(2S)$ . =  $(157.8 \pm 3.6) \times 10^6$ .

Recent results from Belle, arxiv:2309.02739.

Modes	$\epsilon_{\text{sig}}$ (%)	$N_{\text{exp}}^{\text{bkg}}$	$N_{\text{obs}}$	$\mathcal{B}$ @ 90% CL
$\Upsilon(2S) \rightarrow \mu^{\mp} \tau^{\pm}$	$12.3 \pm 0.8$	$3.9 \pm 1.8$	3	$< 0.23 \times 10^{-6}$
$\Upsilon(2S) \rightarrow e^{\mp} \tau^{\pm}$	$8.1 \pm 1.1$	$5.9 \pm 2.6$	12	$< 1.12 \times 10^{-6}$

- $\mathcal{B}(\Upsilon(2S) \rightarrow \mu^{\mp} \tau^{\pm}) < 0.23 \times 10^{-6}$  @ 90% CL.  
 $\mathcal{B}(\Upsilon(2S) \rightarrow e^{\mp} \tau^{\pm}) < 1.12 \times 10^{-6}$  @ 90% CL.
- We obtain **14** times better results for  $\Upsilon(2S) \rightarrow \mu^{\mp} \tau^{\pm}$  and **3** times for  $\Upsilon(2S) \rightarrow e^{\mp} \tau^{\pm}$  from the previous results from the BaBar collaboration.
- Will be published soon! (Accepted by JHEP).

Thank You!

Back Up

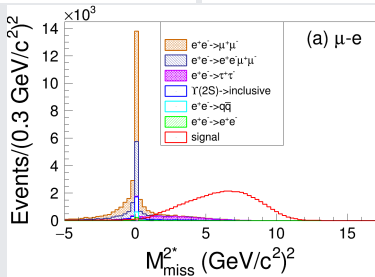
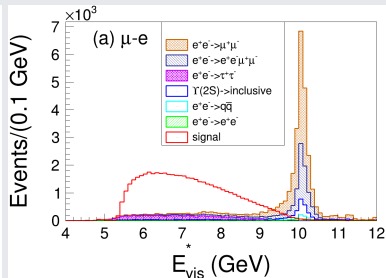
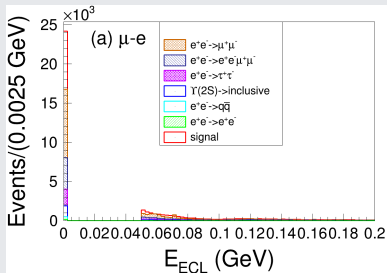
Table: Lists of all selection criteria corresponding to the variable for each mode.

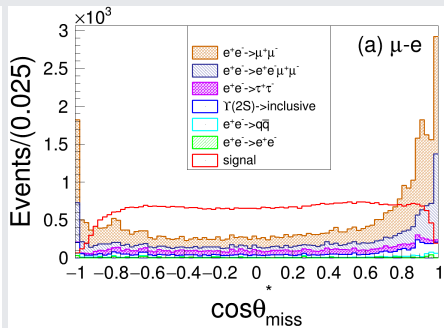
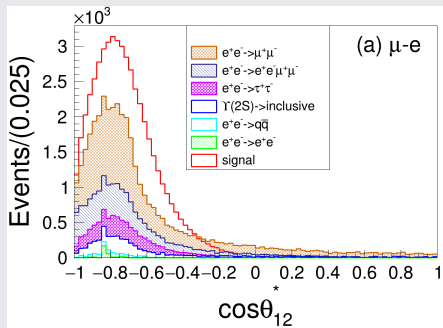
Variables	$\mu$ -e	e- $\mu$	$\mu$ - $\pi\pi^0$	e- $\pi\pi^0$
Impact parameters			$ dr  < 2.0$ cm $ dz  < 5.0$ cm	
PID			$e(\mu)ID > 0.8$ $\pi ID > 0.6$	
$p_1^*$			$> 4.5$ GeV/c	
$E_\gamma$		-	$> 50/100/150$ MeV	
$M_{\pi^0}^*$		-	$0.125 < M_{\pi^0}^* < 0.145$ GeV/c <sup>2</sup>	
$p_2^*$	$> 0.5$ GeV/c		-	
$p_{\pi^+}^*$		-	$0.3 < p_{\pi^+}^* < 4.0$ GeV/c	
$p_{\pi^0}^*$		-	$> 0.4$ GeV/c	
$M_{\pi^+\pi^0}^*$		-	$0.5 < M_{\pi^+\pi^0}^* < 1.0$ GeV/c <sup>2</sup>	
$E_{vis}^*$			$< 9.8$ GeV (e-mode only)	



Table: Decay modes chosen for  $\tau$  with their branching fractions (B.F.).

$\tau$ decay modes	B.F. (in %)
$\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau$	$17.82 \pm 0.04$
$\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau$	$17.39 \pm 0.04$
$\tau^+ \rightarrow \pi^+ \pi^0 \bar{\nu}_\tau$	$25.49 \pm 0.09$





- Distinguishing variables used to classify signal and background events are:
  - $E_{\text{ECL}}$  - It is the sum of the energy of neutral ECL clusters that are related to the particles in the rest of the event in the lab frame.
  - $E_{\text{vis}}^*$  - It is the sum of the energy of all neutral clusters and charged tracks in the c.m. frame.
  - $M_{\text{miss}}^{*2}$  - It is the invariant mass squared of the missing momentum in the c.m. frame.
  - $\cos \theta_{12}^*$  - It is the cosine of the angle between  $p_1^*$  and  $p_2^*$  for  $\mu$ - $e$  and  $e$ - $\mu$  modes or between  $p_1^*$  and  $p_{\pi^+}^* + p_{\pi^0}^*$  for  $\mu$ - $\pi\pi^0$  and  $e$ - $\pi\pi^0$  modes in the c.m. frame.
  - $\cos \theta_{\text{miss}}^*$  - It is the cosine of the polar angle of the missing momentum in the c.m. frame.