

# Measurements of lepton-flavour universality in semileptonic $B$ decays at Belle and Belle II

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# Lepton Flavour Universality in B decays

- W boson couples equally to  $e, \mu, \tau$  in the SM  $\rightarrow$  **Lepton Flavour Universality (LFU)**.

- Accidental symmetries, not required by first principles.

Non-SM contributions ( $H^+, LQ, \text{SUSY} \dots$ ) can generally violate LFU.

- Tree-level semileptonic B decays offer a rich phenomenology for LFU tests:

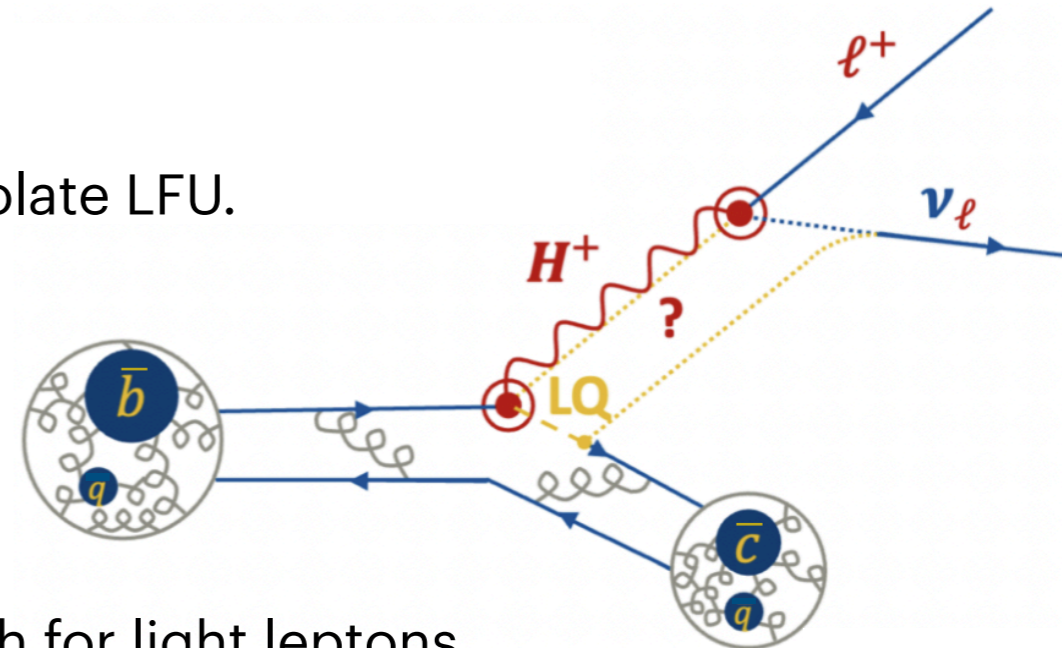
- Asymmetries in angular distributions enhance the reach for light leptons.

Exploit high rates of  $B \rightarrow D^* \ell \nu$  decays.

- Ratio of rates suppress most theoretical and experimental uncertainties.

Persistent anomaly observed between tau and light leptons,  $R(D_{\tau/\ell}^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)}$ .

- Today: LFU tests from Belle and Belle II. Most are new since last FPCP.



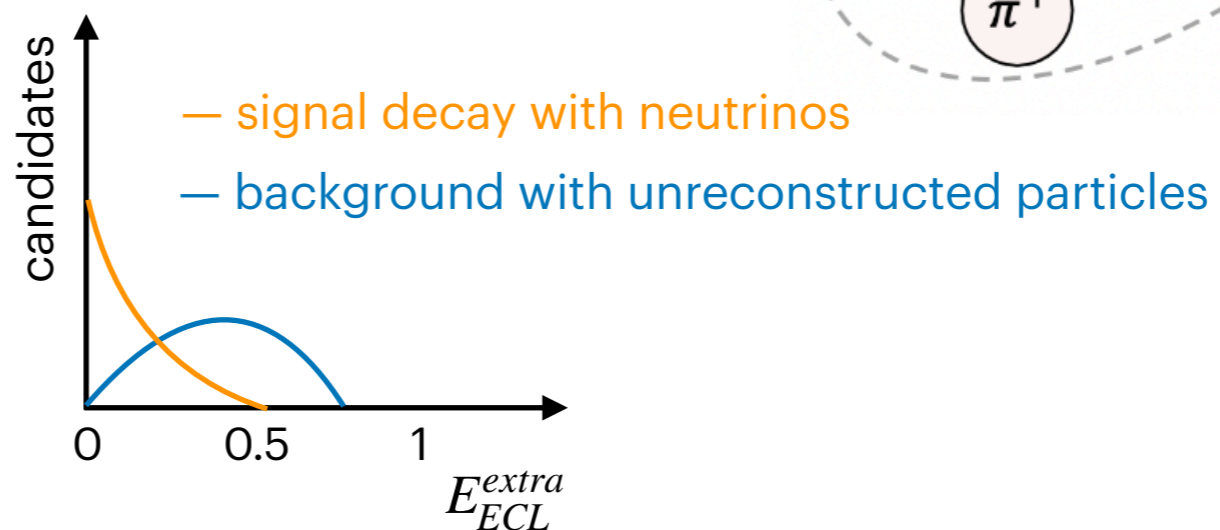
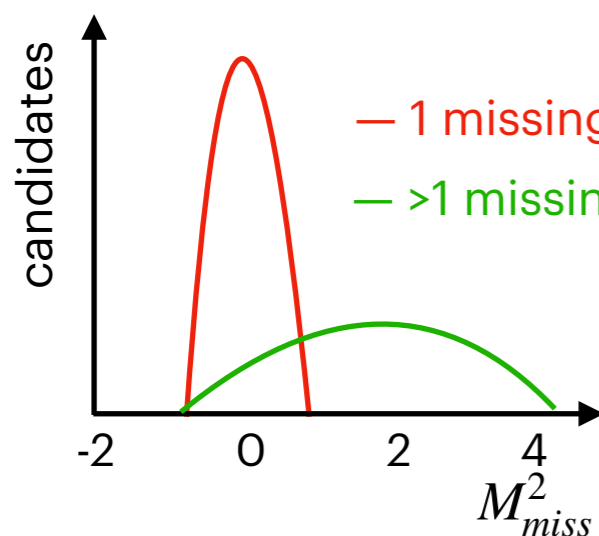
# Dealing with missing energy

Belle (II) ideally suited to study decay with missing energy: hermetic detector, at-threshold  $B\bar{B}$  production with precisely known energy.

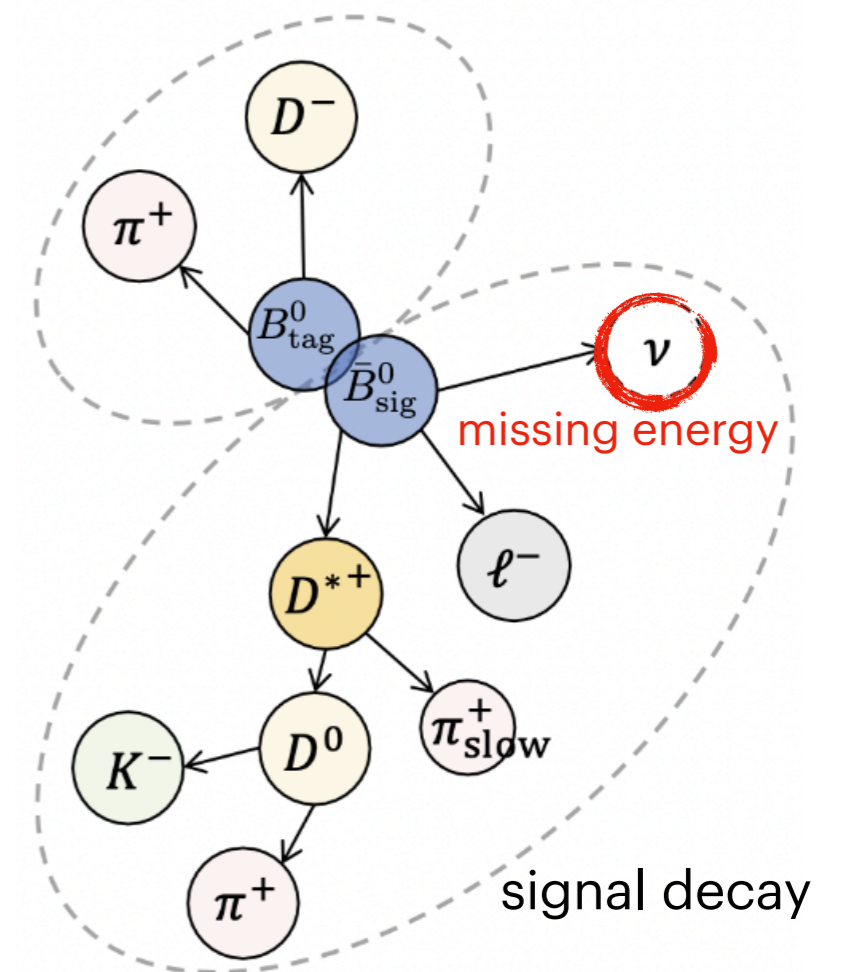
- Fully reconstruct the partner  $B$  meson in hadronic decay mode. ( $B_{tag}$  efficiency  $<1\%$ , purity up to 90% [FEI]).
- Match remaining particles with signal decay.
- Identify invisible particles using:

1. Missing mass of undetected particles  $M_{miss}^2 = (p_{e^+e^-} - p_{visible})^2$ .

2. Residual energy in the calorimeter  $E_{ECL}^{extra}$ .



## hadronic tag decay

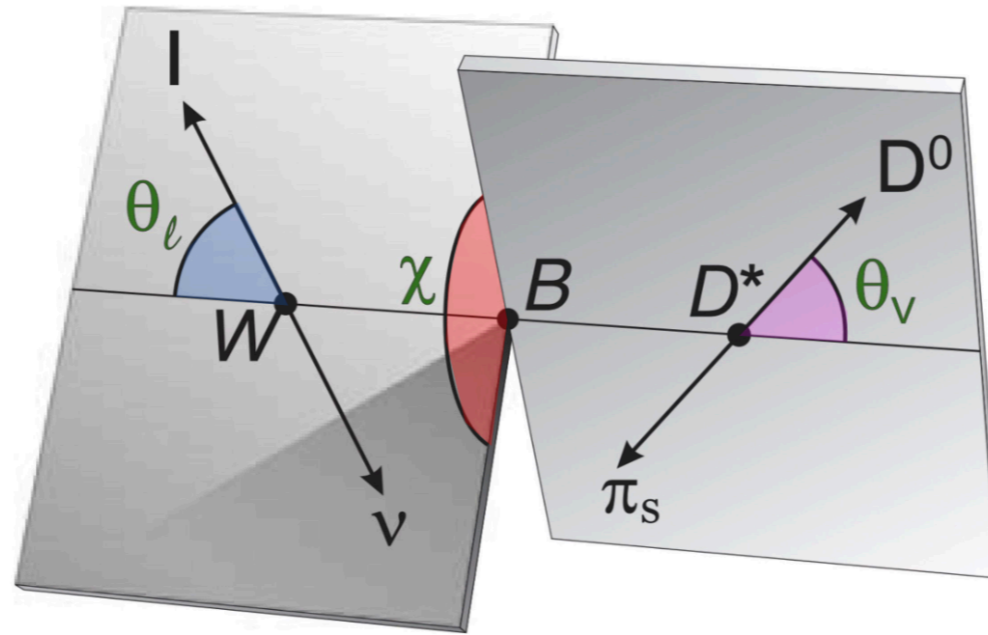


All the analyses shown in this talk are tagged.

# LFU tests with angular asymmetries for light leptons

# Angular analysis: basics

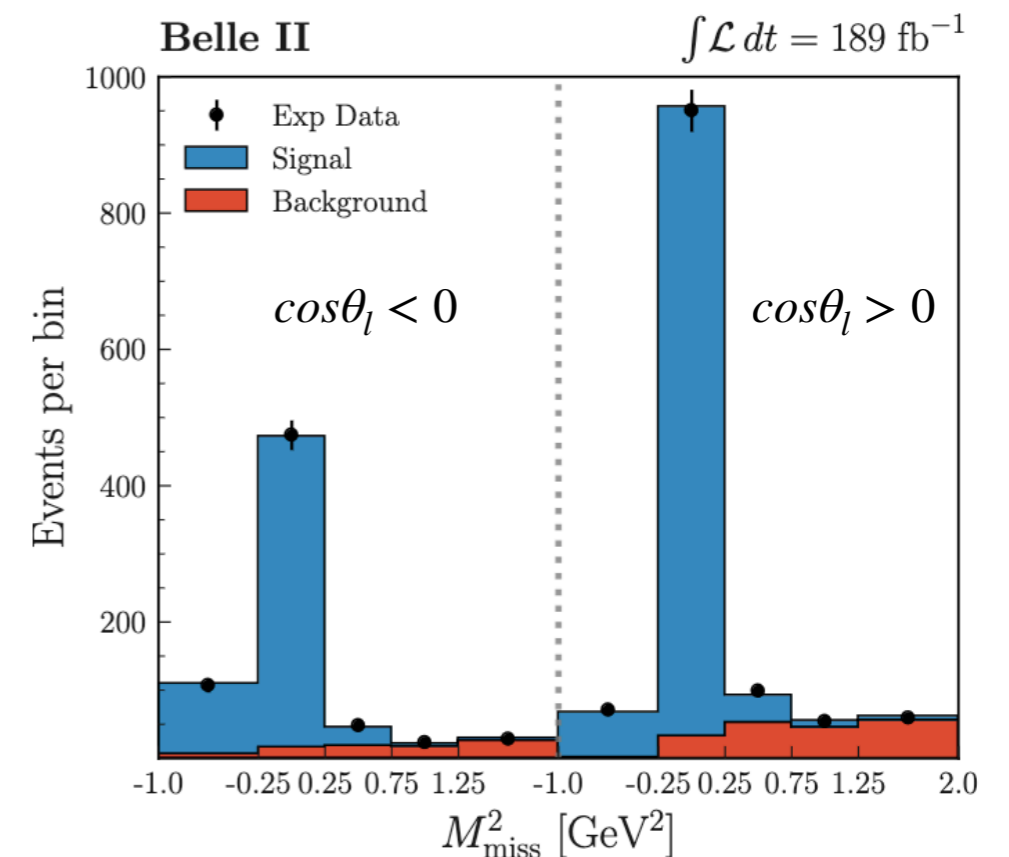
$B \rightarrow D^* \ell \nu$  decay: rich phenomenology due to different decay amplitudes (configurations of angular momentum). Encoded in angular distributions as a function of the recoil energy  $w$  of the  $D^*$ .



Comparing angular observables between muons and electrons gives **powerful LFU tests**.

## Experimentally:

1. Reconstruct the distributions by measuring signal yields in bins of (combinations of) angular variables.
2. Signal/background separation by fitting  $M_{miss}^2$ .
3. Correct for detector acceptance, reconstruction efficiencies and resolution effects using simulation.



# $B \rightarrow D^* \ell \nu$ angular asymmetries

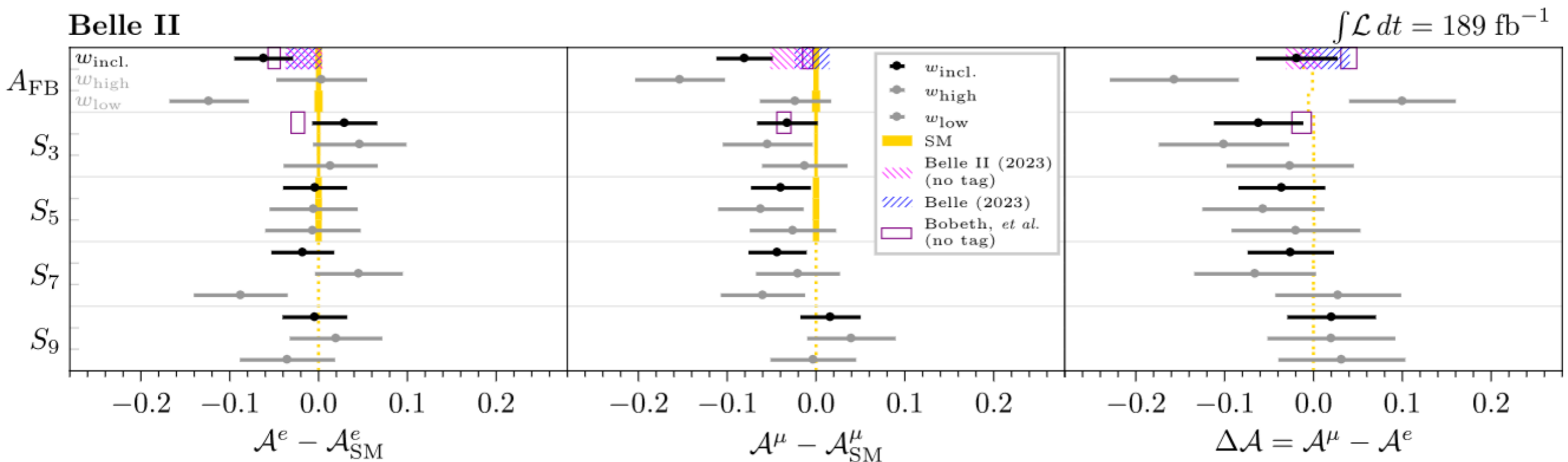
PRL 131, 181801 (2023)

Pheno analysis of Belle data [Bobeth et al.] pointed to possible LFU violation. Need a verification.

**Goal:** measure 5 angular asymmetries and compare them for muons and electrons:

- $A_{FB}$  : tendency of the lepton to travel along the  $W$  direction.
- $S_3, S_9$  : sensitive to alignment of lepton and  $D^*$  direction.
- $S_5, S_7$  : measure coupled alignments in the orientation of the  $D$  with respect to the  $D^*$ .

Reconstruct D mesons in different modes:  $D \rightarrow K(n)\pi$  and  $D \rightarrow KK$ .



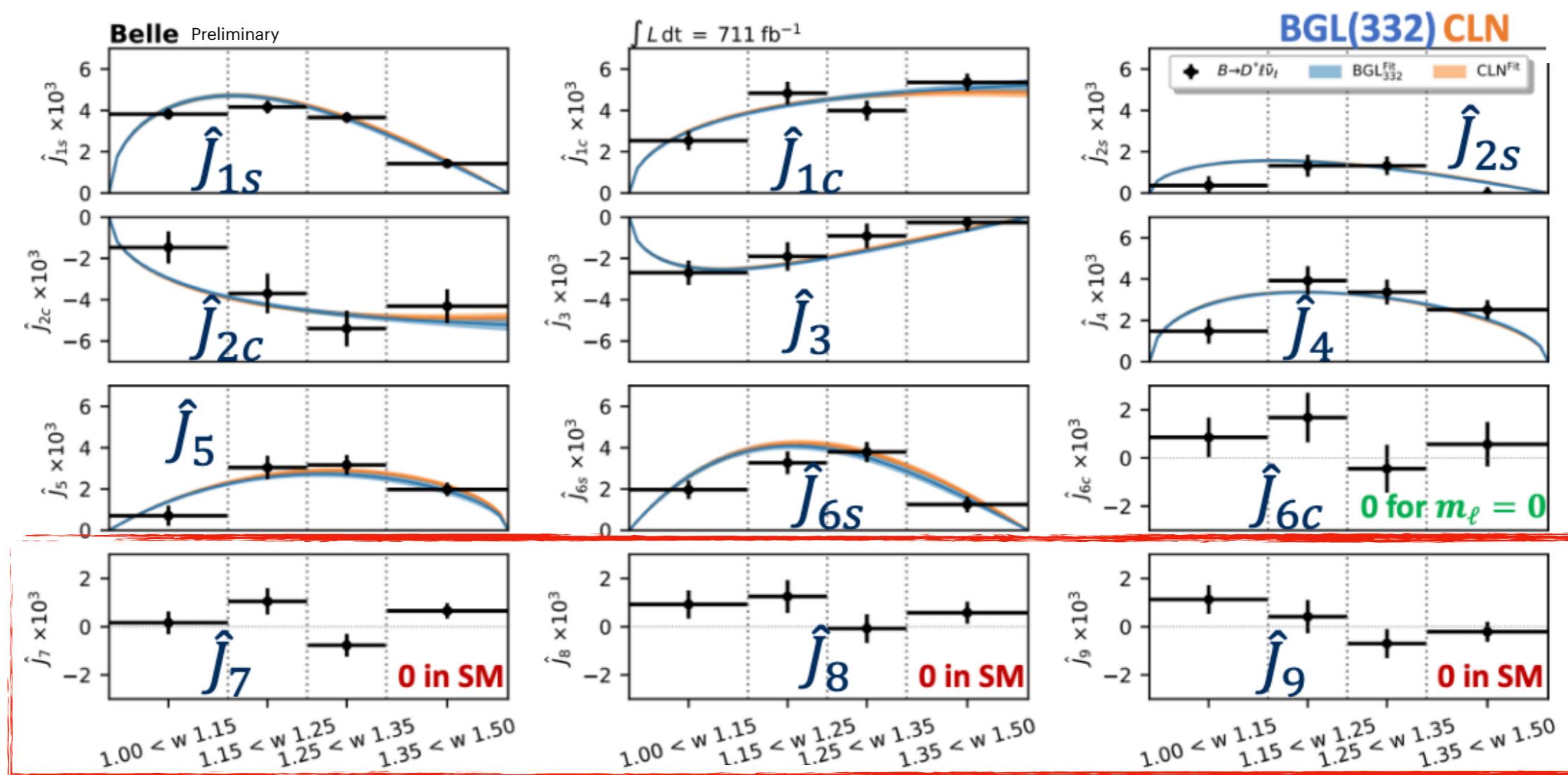
All asymmetry measurements are statistics limited.  
Compatible with SM, no evidence for LFU violation.

# $B \rightarrow D^* \ell \nu$ angular coefficients

- The differential decay rate can be decomposed in a basis of angular functions with 12 coefficients  $J_i$ , all dependent on  $w$ .

**Goal:** measuring of  $J_i$  in 4 bins of  $w$ . Provide information on form-factors and test SM expectations.

- Reconstruct D mesons in different modes:  $D \rightarrow KK, D \rightarrow KK(n)\pi$  and  $D \rightarrow K(n)\pi$ .

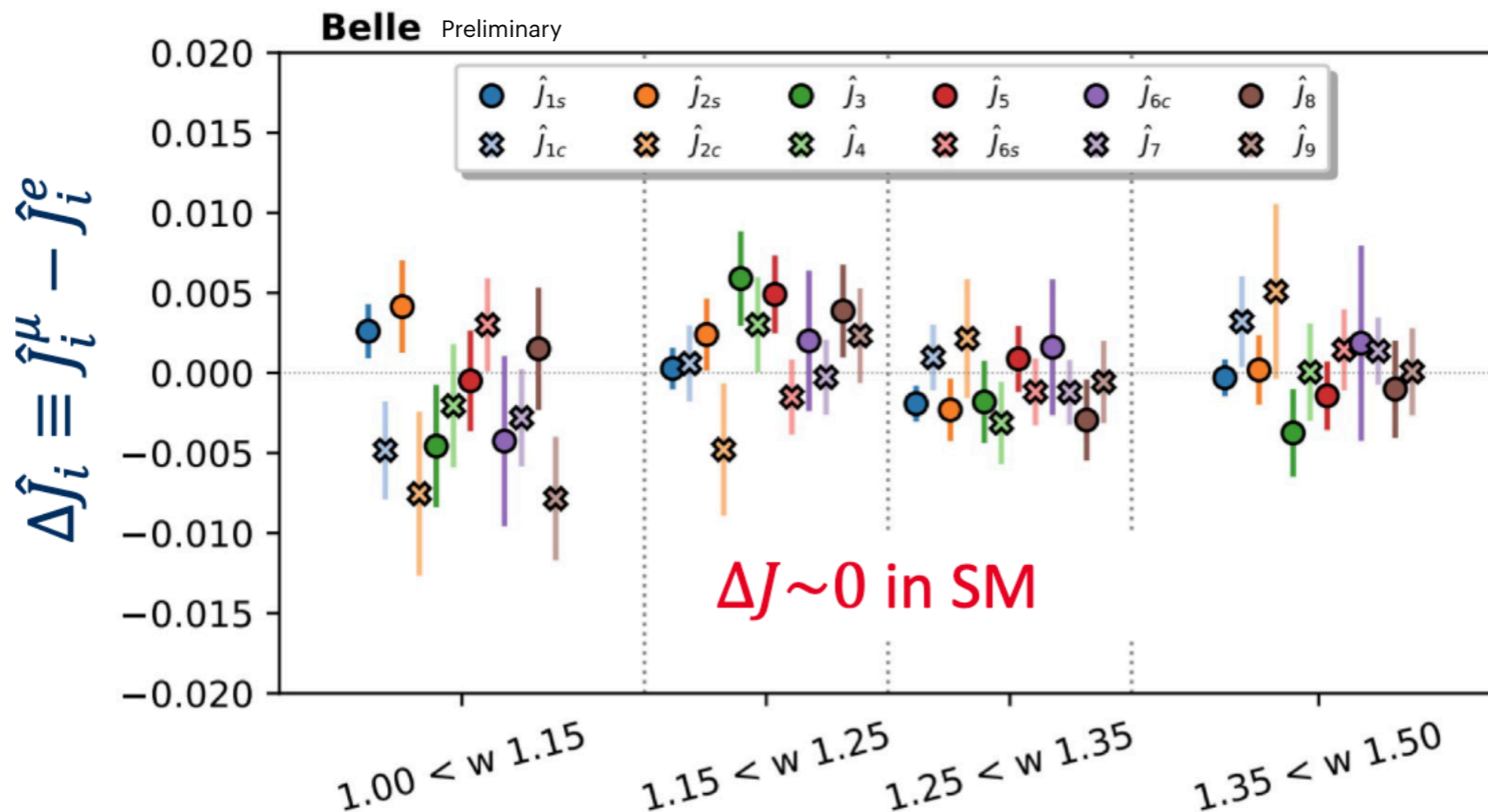


Coefficients are in good agreement with the fit using BGL(332) and CLN form-factor parametrizations.

Coefficients consistent with the SM prediction.

# $B \rightarrow D^* \ell \nu$ angular coefficients

Difference between electron and muon sensitive to LFU:  $\Delta J_i = J_i^\mu - J_i^e$ .



No significant deviations observed from the SM.

Aside: determination of  $|V_{cb}|$  using CLN and BGL parametrizations and lattice data from [1-2-3]:

$$|V_{cb}|_{BGL} = (41.0 \pm 0.7) \cdot 10^{-3}$$

$$|V_{cb}|_{CLN} = (40.9 \pm 0.6) \cdot 10^{-3}$$

Similar values, closing the gap with the inclusive  $|V_{cb}|$  measurement.



LFU tests with the third generation:  
 $R(D^*)$  and  $R(X)$  measurements

# Measurement of $R(D^*)$

**Goal:** measure  $R(D^*_{\tau/\ell}) = \frac{\mathcal{B}(B \rightarrow D^* \tau \nu_\tau)}{\mathcal{B}(B \rightarrow D^* \ell \nu_\ell)}$

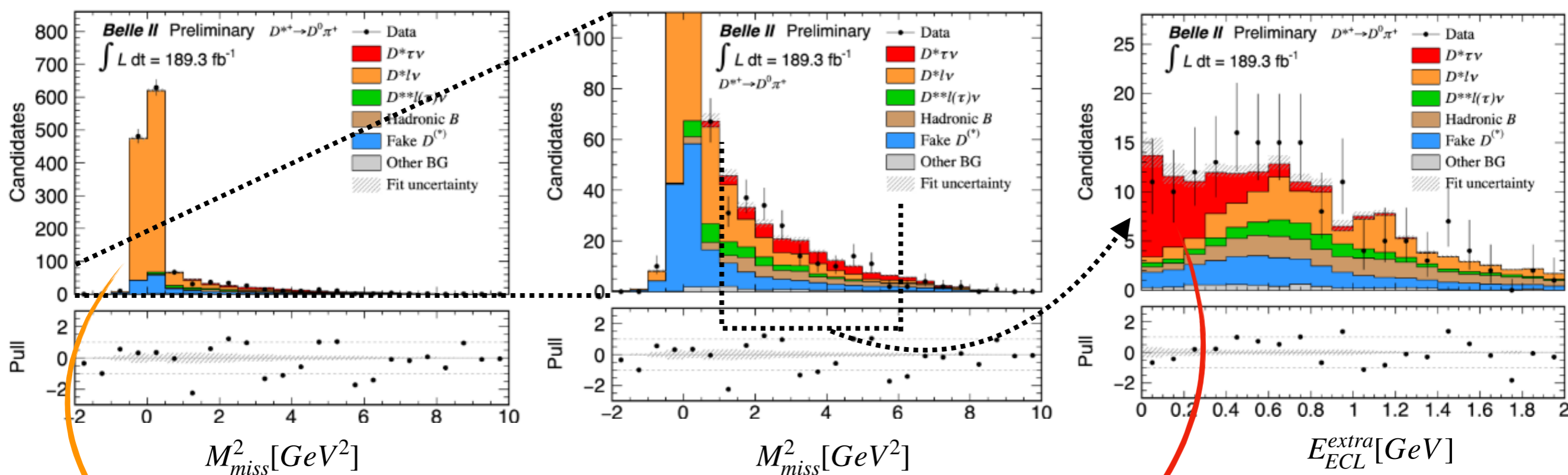
- Three signal modes:  $D^{*+} \rightarrow D^0 \pi^+$ ,  $D^+ \pi^0$  and  $D^{*0} \rightarrow D^0 \pi^0$ . Identify lepton from  $\tau \rightarrow \ell \nu \bar{\nu}$ .

**Extract signal and normalisation yields** using a simultaneous 2D likelihood fit to  $E_{ECL}^{extra}$  and  $M_{miss}^2$ .

$M_{miss}^2$  projection  
for  $D^{*+} \rightarrow D^0 \pi^+$  mode

Zoom of  $M_{miss}^2$  projection  
for  $D^{*+} \rightarrow D^0 \pi^+$  mode

Signal-enhanced projection  
for  $D^{*+} \rightarrow D^0 \pi^+$  mode



normalisation yield:  $2163 \pm 79$

signal yield:  $108 \pm 16$

# Measurement of $R(D^*)$

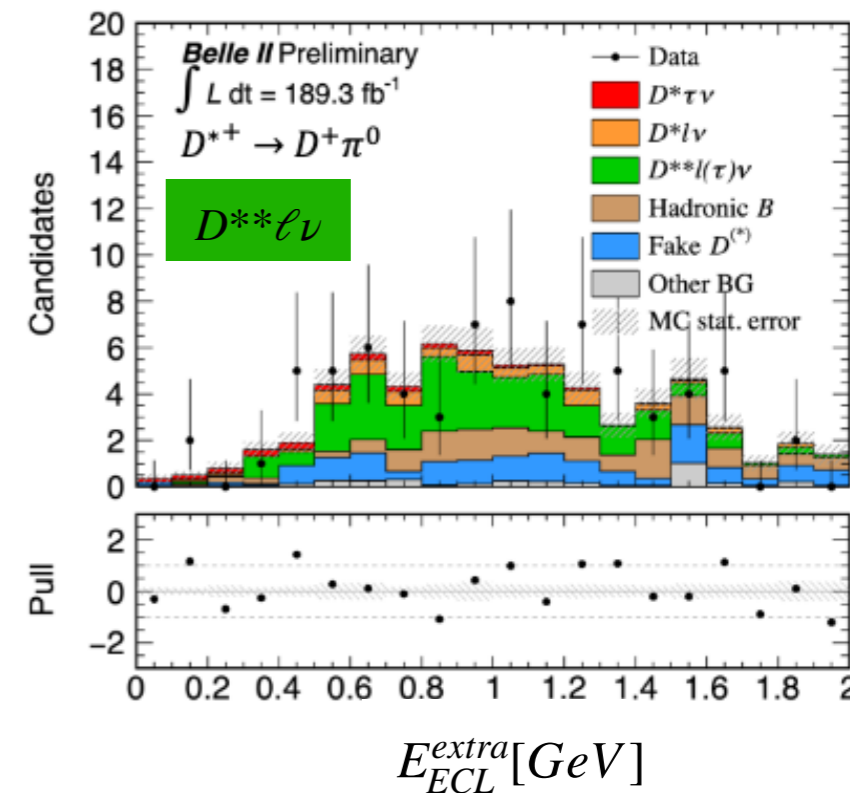
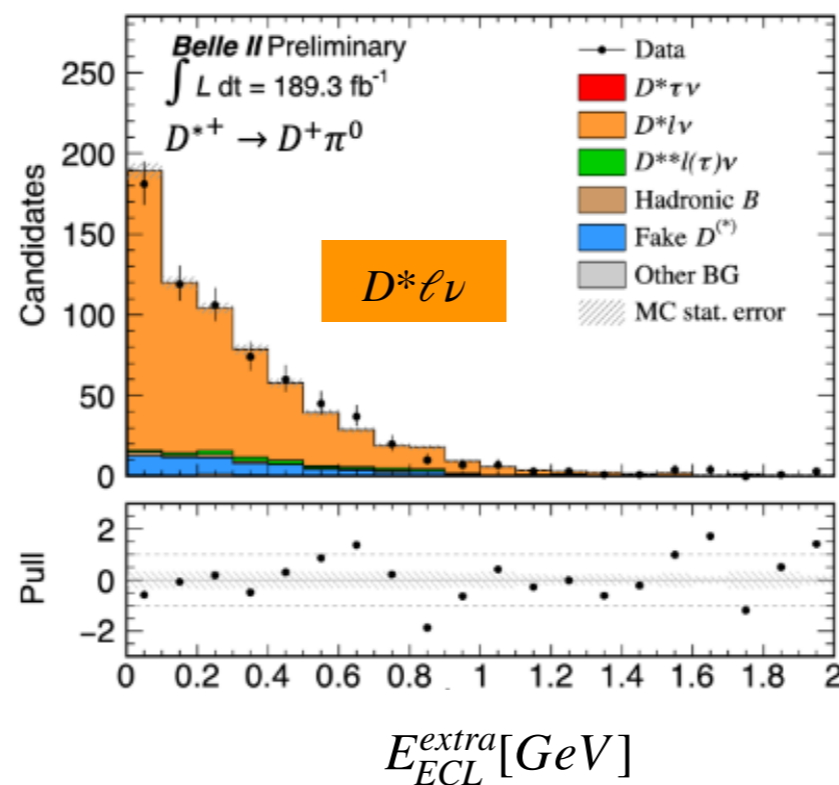
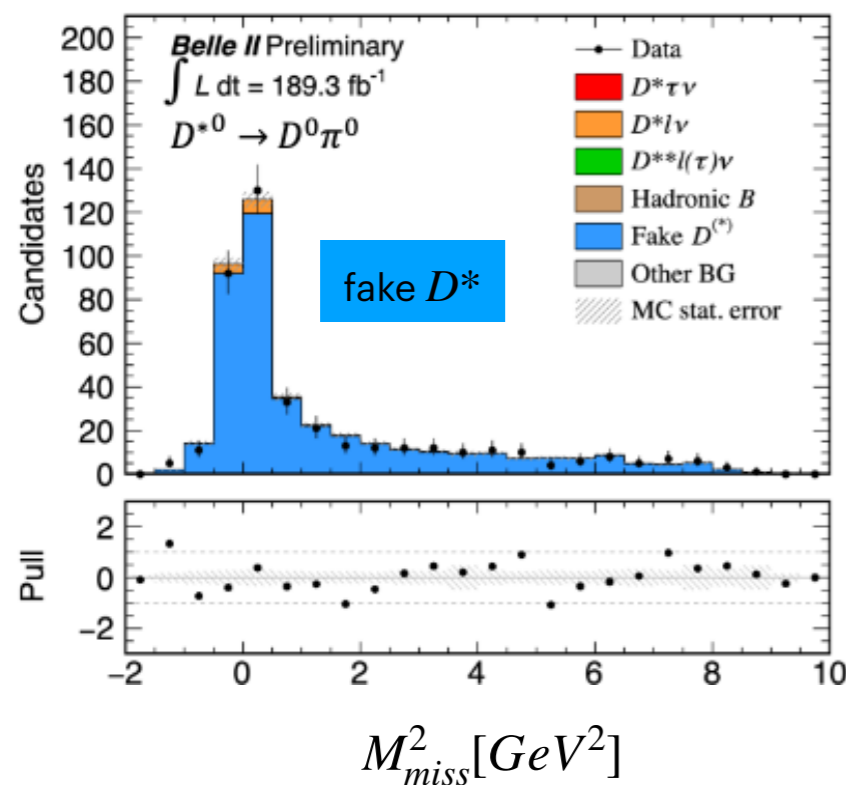
**Main challenge:** validate modelling of background/normalization fit templates.

**Data-driven validation** of background and signal model based on studies of **control regions**.

$m(D\pi) > m(D^*)$  sideband:  
validate fake  $D^*$  modelling

$q^2 < 3.5\text{GeV}^2$  sideband:  
validate  $E_{ECL}$

Reconstruct  $D^*\pi^0\ell\nu$ :  
validate  $D^{**}$  modelling



All the major sources of background are well described in the sideband regions.

**Main sources of syst. uncertainties:** PDF shapes:  $+9.1\%$  /  $-8.3\%$ , MC statistics:  $+7.5\%$  /  $-7.5\%$ ,  $\mathcal{B}(B \rightarrow D^{**}\ell\nu)$ :  $+4.8\%$  /  $-3.5\%$

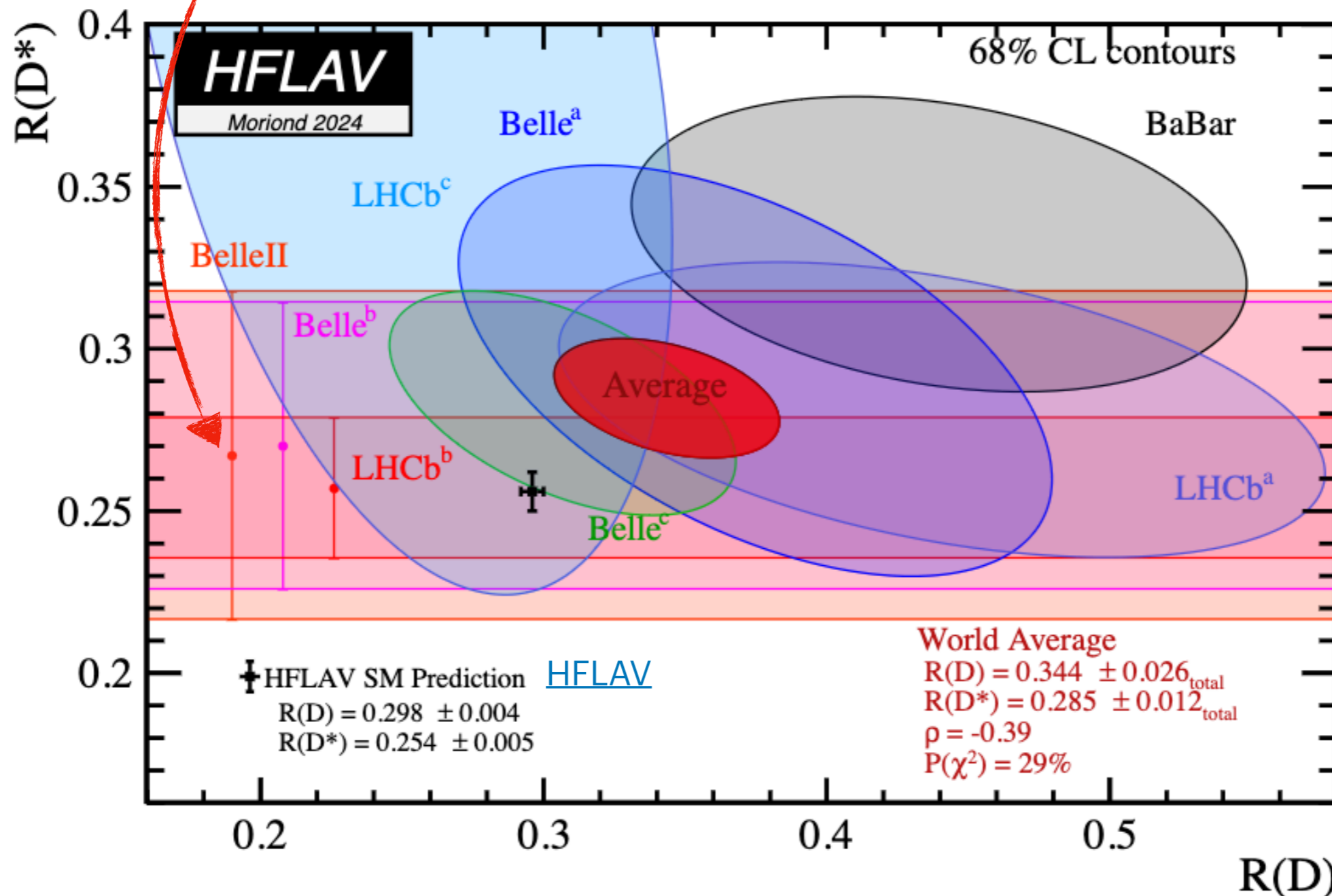
**Statistical uncertainty:** experimental sample size:  $+15.7\%$  /  $-14.7\%$

# Measurement of $R(D^*)$ : results

$$R(D^*) = 0.262^{+0.041}_{-0.039}(stat)^{+0.035}_{-0.032}(syst)$$

HFLAV 23:  $R(D^*) = 0.285 \pm 0.012$

Consistent with the previous measurements.



3.3 $\sigma$  tension between the LFU-sensitive quantities  $R(D)$  and  $R(D^*)$  and SM predictions.

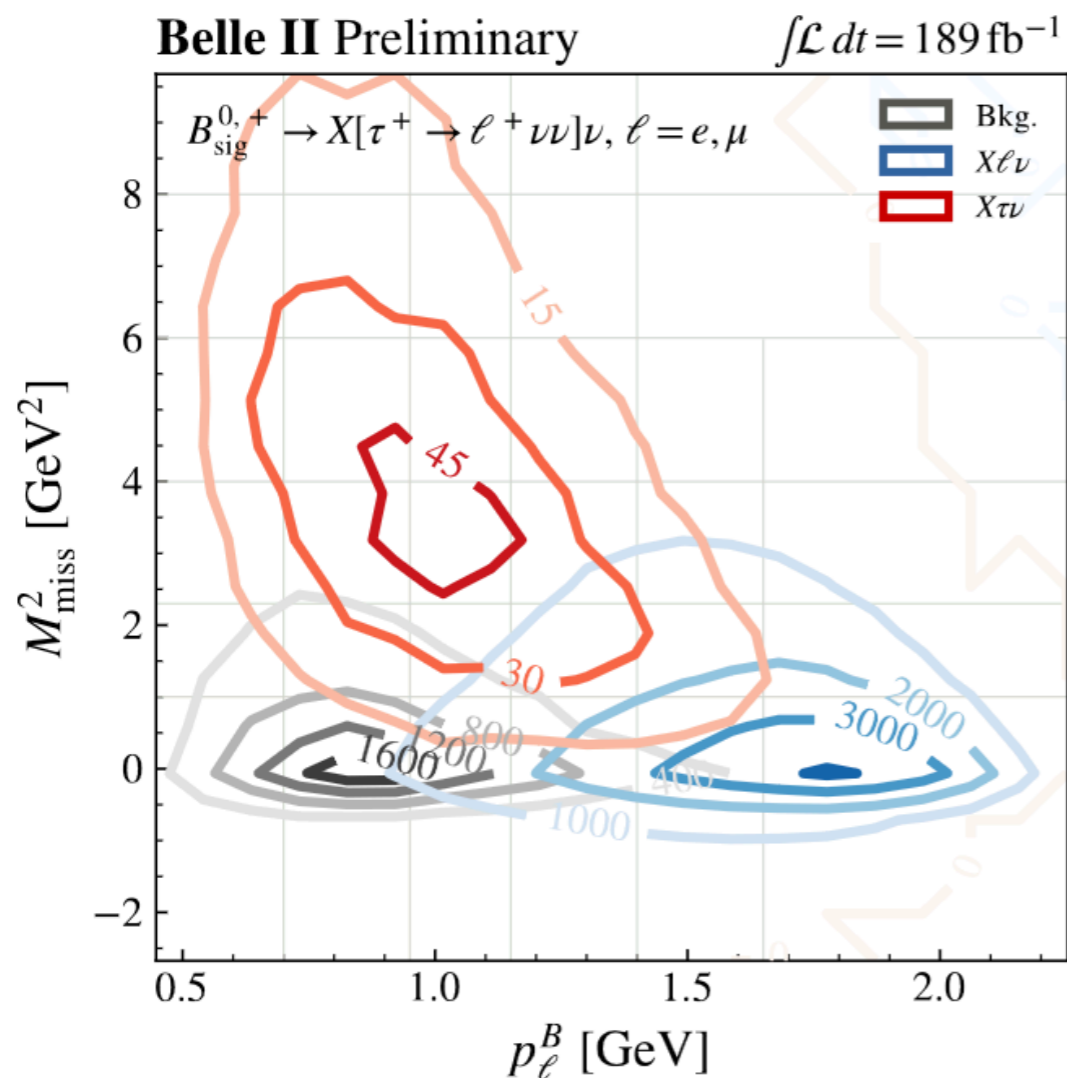
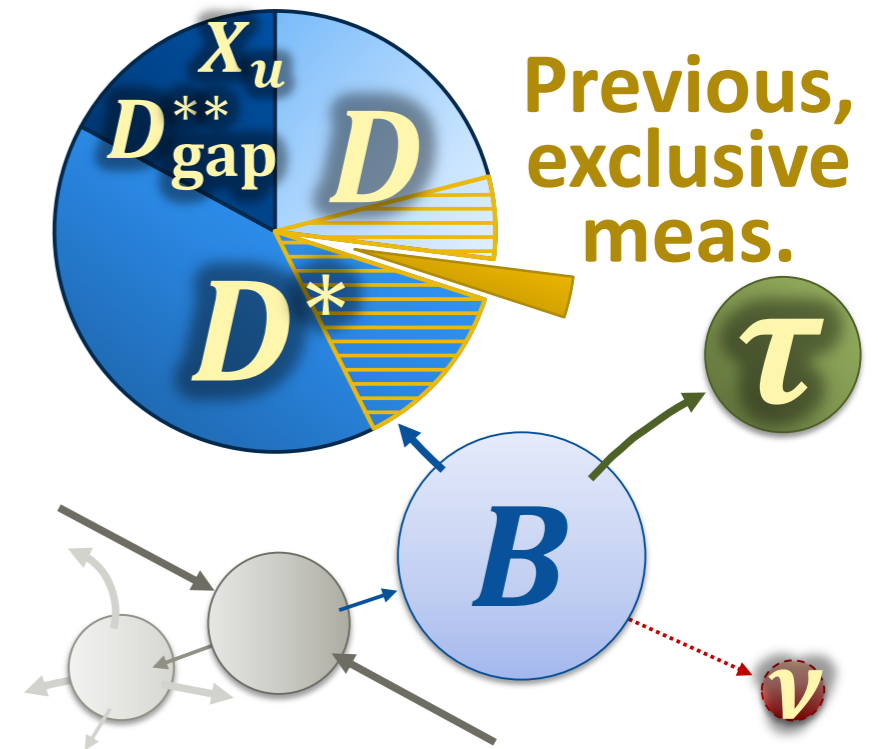
# Measurement of $R(X_{\tau/\ell})$

**Goal:** measure  $R(X_{\tau/\ell}) = \frac{\mathcal{B}(B \rightarrow X\tau\nu_\tau)}{\mathcal{B}(B \rightarrow X\ell\nu_\ell)}$

Innovative and complementary measurement w.r.t.  $R(D^{(*)})$ : potentially more precise with different sources of systematics.

- Select events with  $B_{tag} + \ell$ , remaining particles attributed to  $X$ .

## Inclusive meas.



**Extract signal and normalisation yields** using a simultaneous 2D likelihood fit to lepton momentum  $p_l^B$  (B rest frame) and  $M_{miss}^2$ .

$B \rightarrow X\tau\nu$  and  $B \rightarrow X\ell\nu$  well separated in the 2D plane.

# Measurement of $R(X_{\tau/\ell})$

**Main challenge:** modelling the  $X$  system.

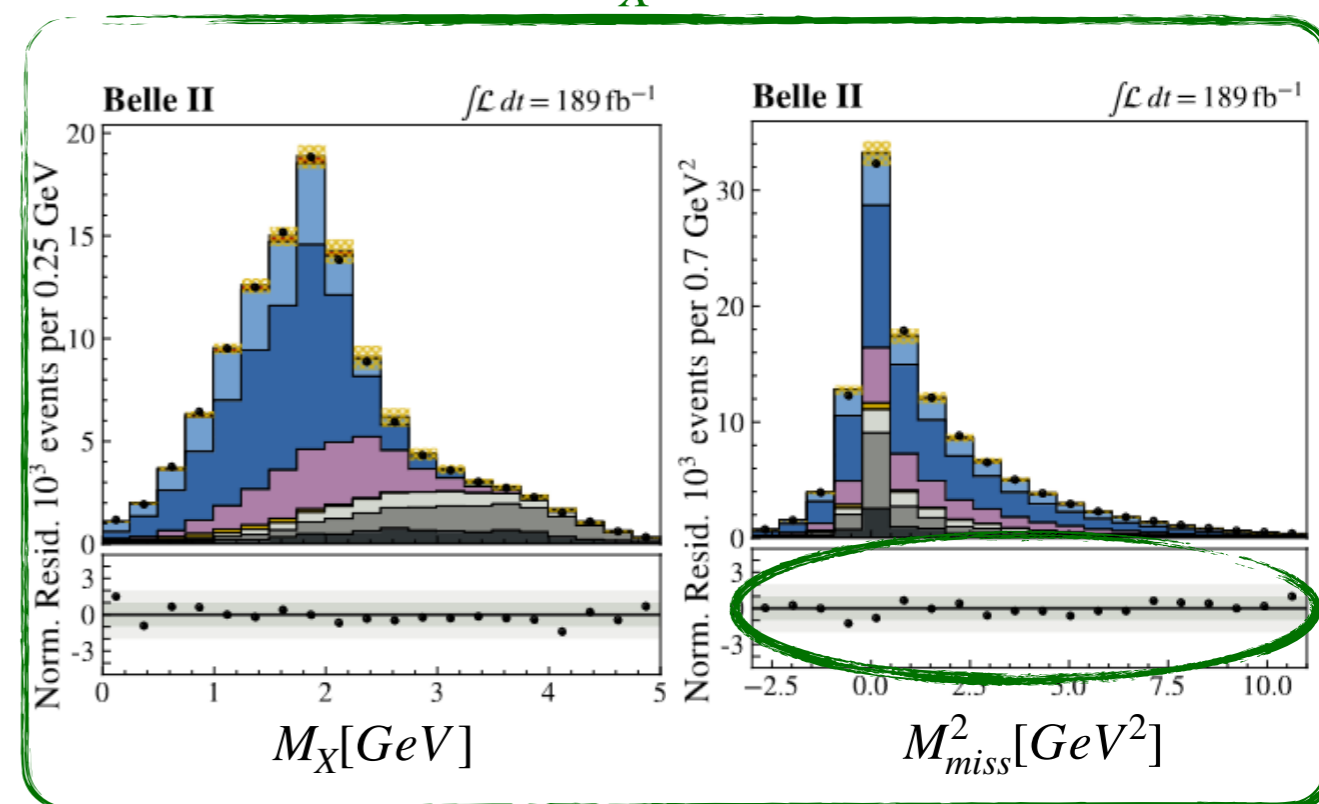
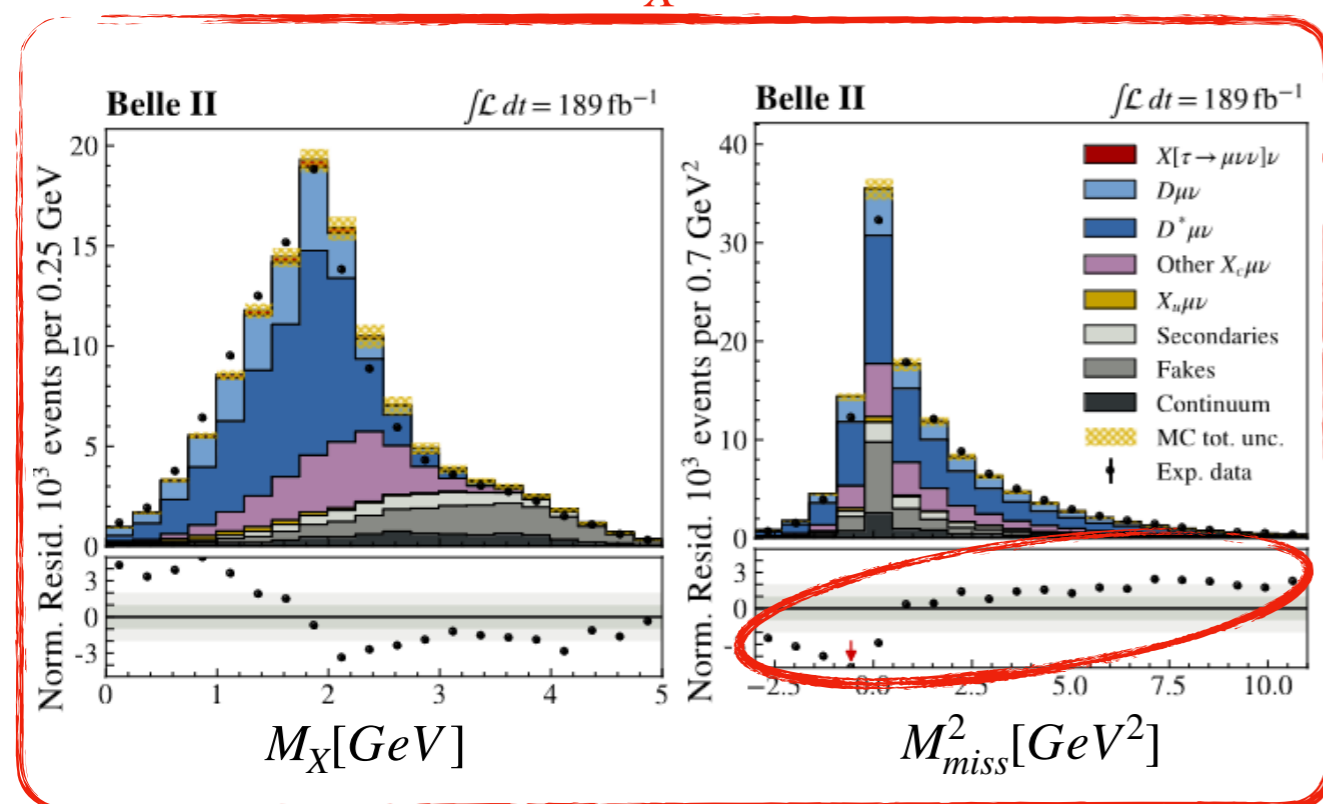
Detailed adjustments to simulation: form factors,  $B$  and  $D$  branching fractions.

Corrections based on comparison of simulation with **control regions**.

Example:

before  $M_X$  reweighting

after  $M_X$  reweighting

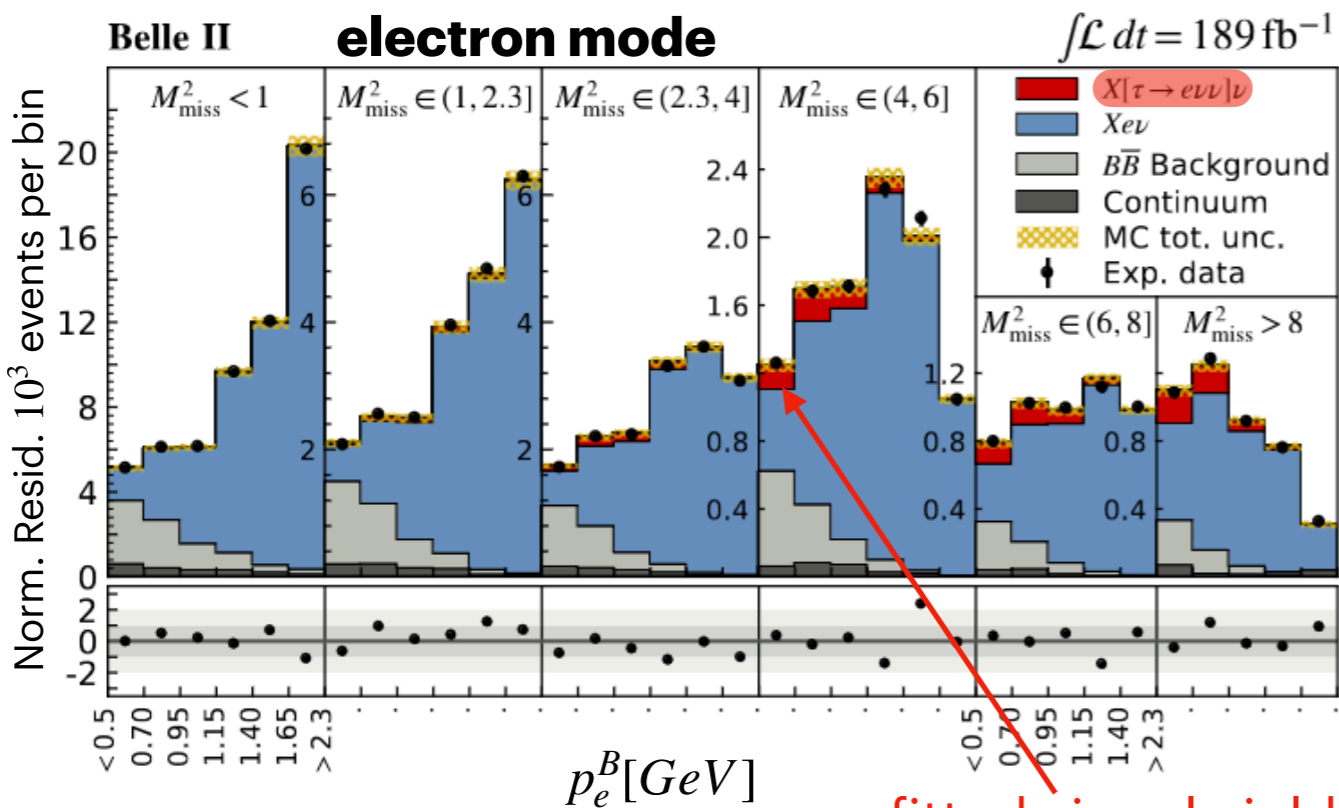


Adjusting  $M_X$  distribution in high  $p_i^B$  sideband also improves modelling in  $M_{miss}^2$ .

**Main sources of syst. uncertainties:**  $X_c \ell \nu$   $M_X$  shape: 7.1%,  $\mathcal{B}(B \rightarrow X \ell \nu)$ : 7.7%,  $X_c \tau(\ell) \nu$  form factors: 7.8%

**Statistical uncertainty:** experimental sample size: 7.1%

# Measurement of $R(X_{\tau/\ell})$ : results

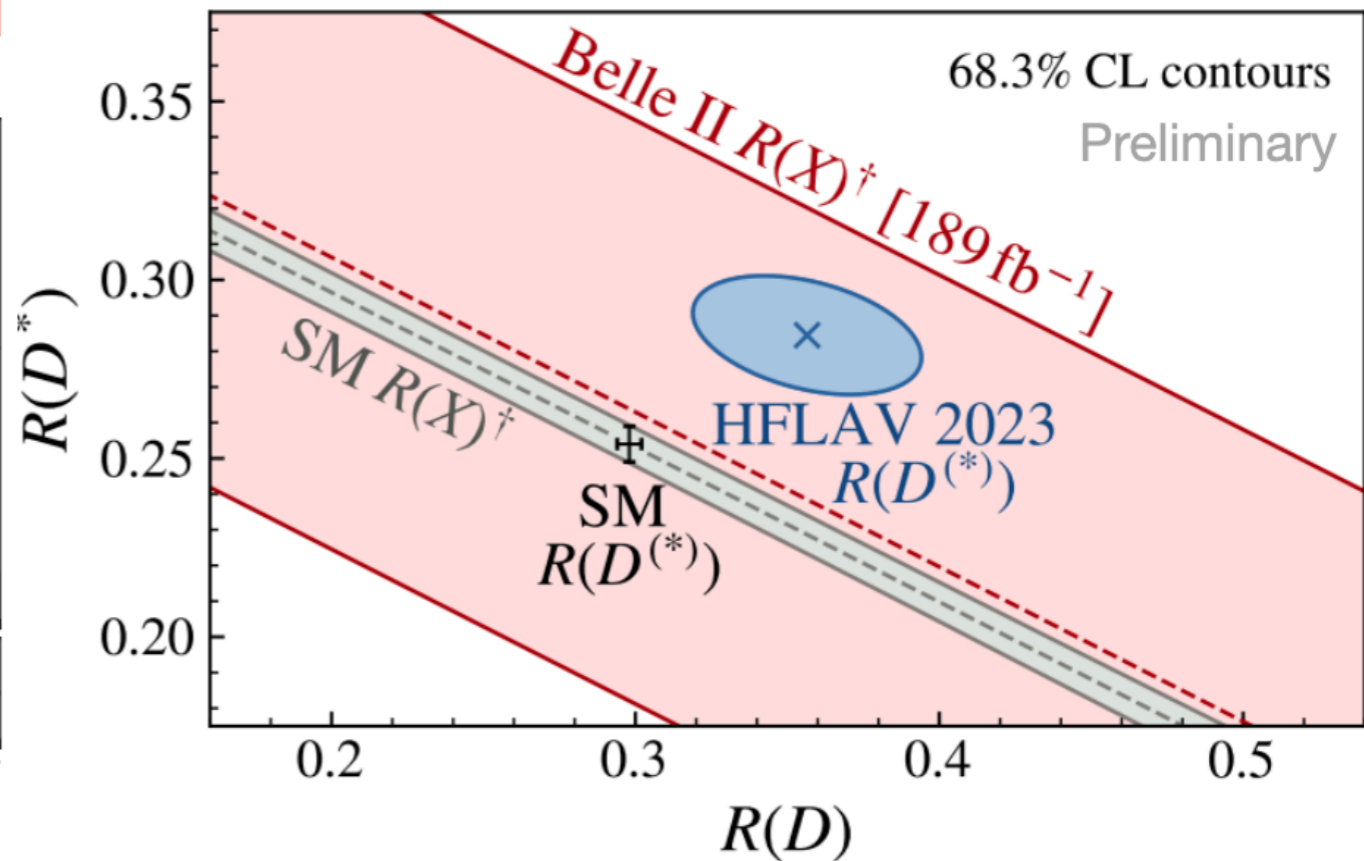
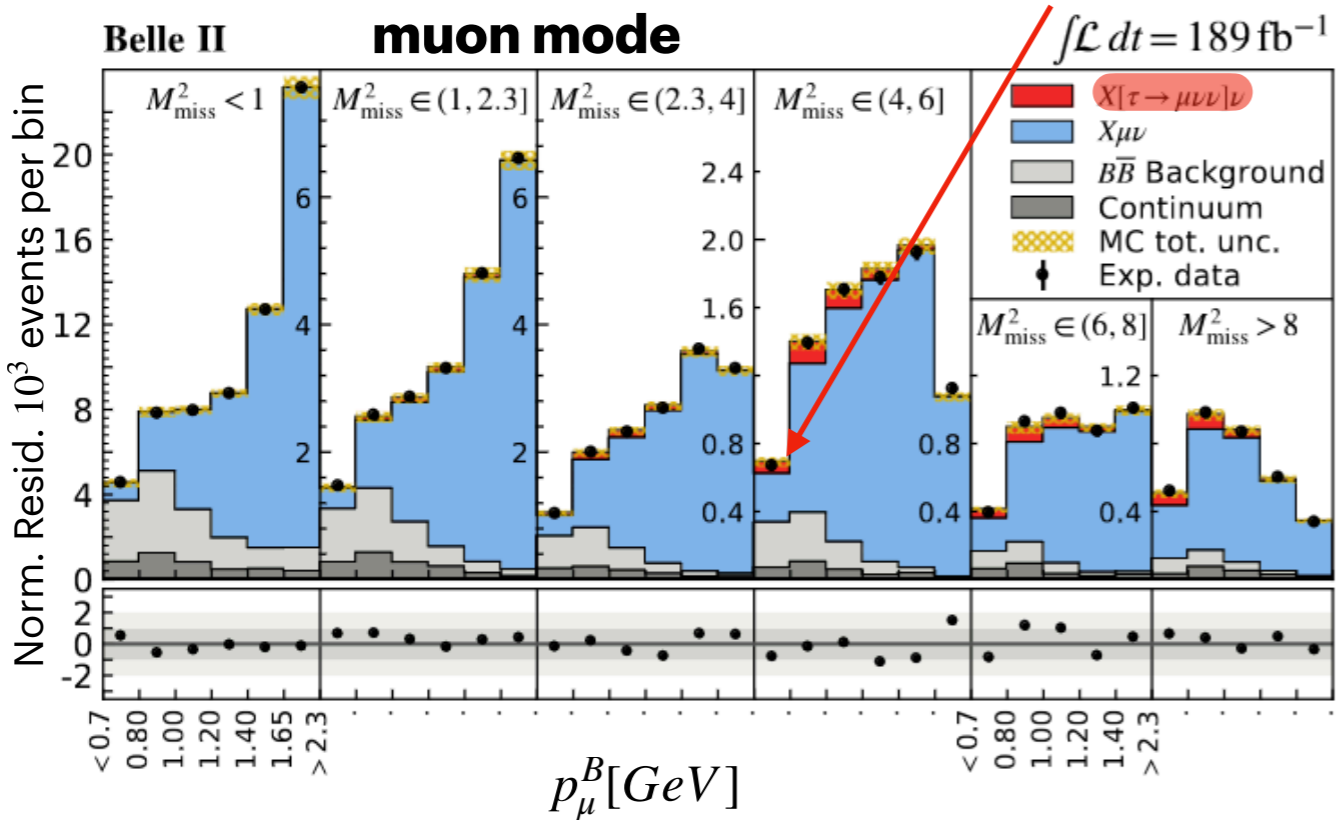


$$R(X_{\tau/\ell}) = 0.228 \pm 0.016(\text{stat}) \pm 0.036(\text{syst})$$

(average of electron and muon channels)

SM prediction:  $R(X_{\tau/\ell}) = 0.223 \pm 0.005$

Compatible with SM and  $R(D^{(*)})$  measurements.



# Summary

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- Many new exciting measurements from both Belle and Belle II.  
The results are in good agreement with LFU and SM.
- With half of collected data set ( $189fb^{-1}$ ), Belle II already produces **world-leading and unique results**.
- Belle data still fruitful after >10 years.
- Continuous effort from **experiment** and **theory** needed:
  - Higher precision expected at Belle II for the next  $R(X)$  and  $R(D^*)$  results using the full collected data set.
  - Some **systematic uncertainties** could be reduced with improved modelling.

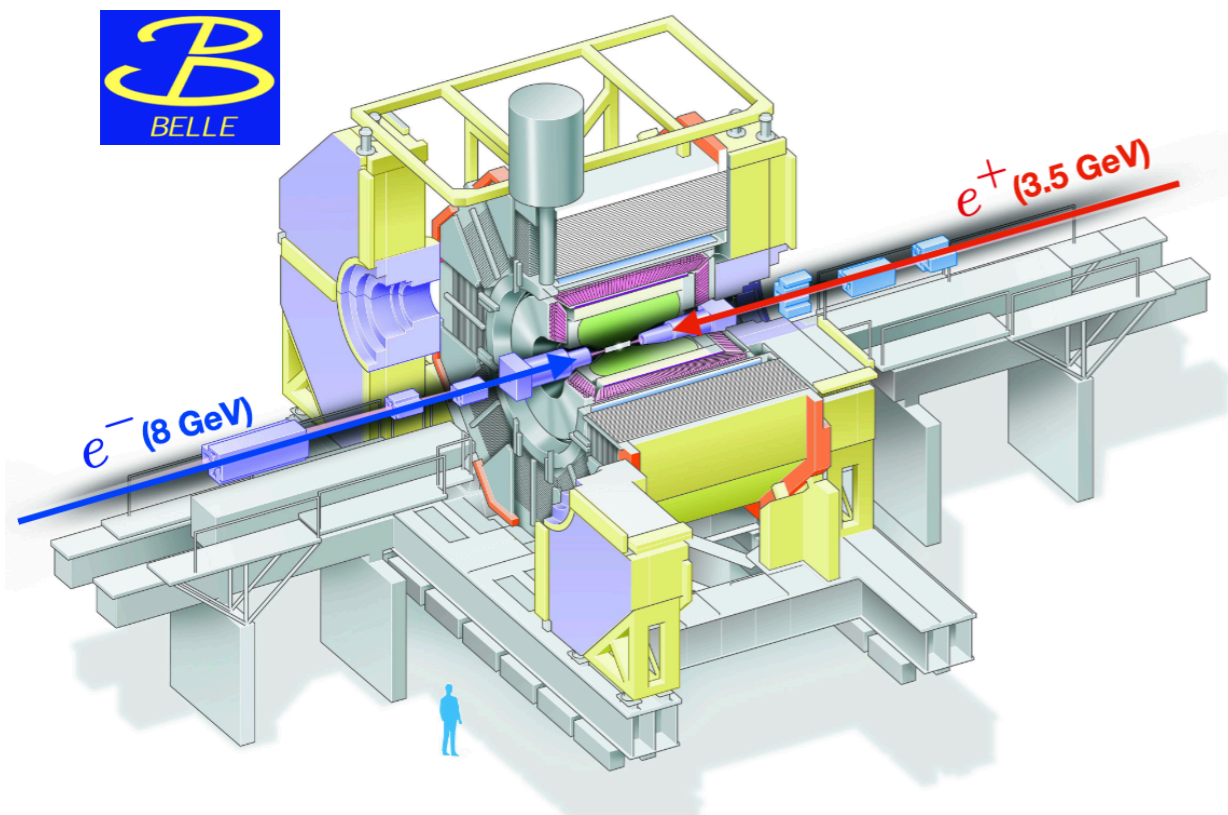


Backup

# From Belle...to Belle II

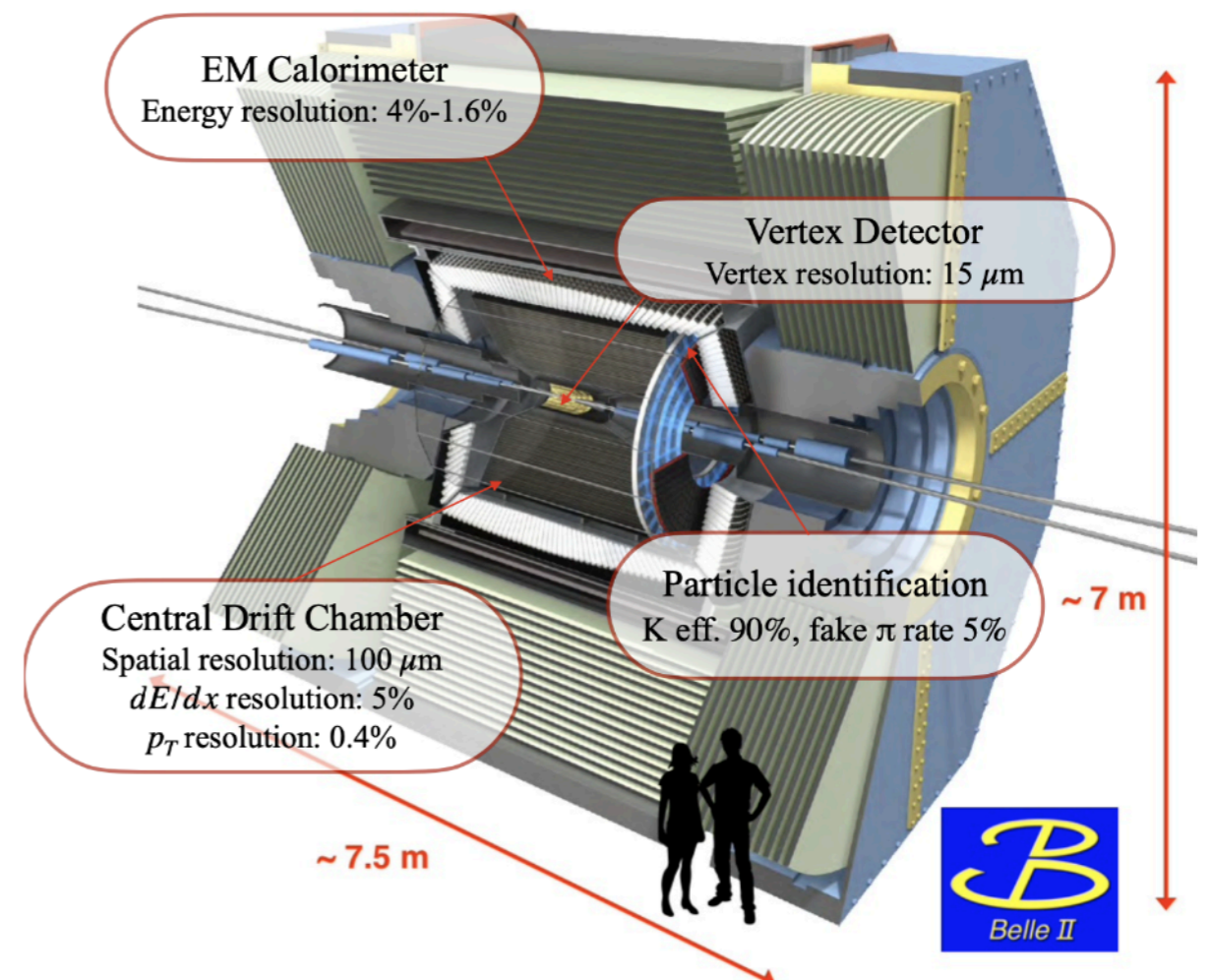
## Belle

- From 1999 to 2010 at KEK (Japan).
- 3.5-on-8 GeV  $e^+e^-$  collider at  $\Upsilon(4S)$  resonance.
- Collected  $772 \cdot 10^6$   $B\bar{B}$  pairs.



## Belle II

- From Belle: structure, magnets, calorimeter crystals,  $K_L$  &  $\mu$  detector.
- Run 1: collected  $387 \cdot 10^6$   $B\bar{B}$  pairs.
- Starting Run 2 after improving vertex detector.
- **First Run 2 collision: 20 Feb 2024, 22:12 JST.**



Promising with multiple neutral particles and neutrinos in the final states.

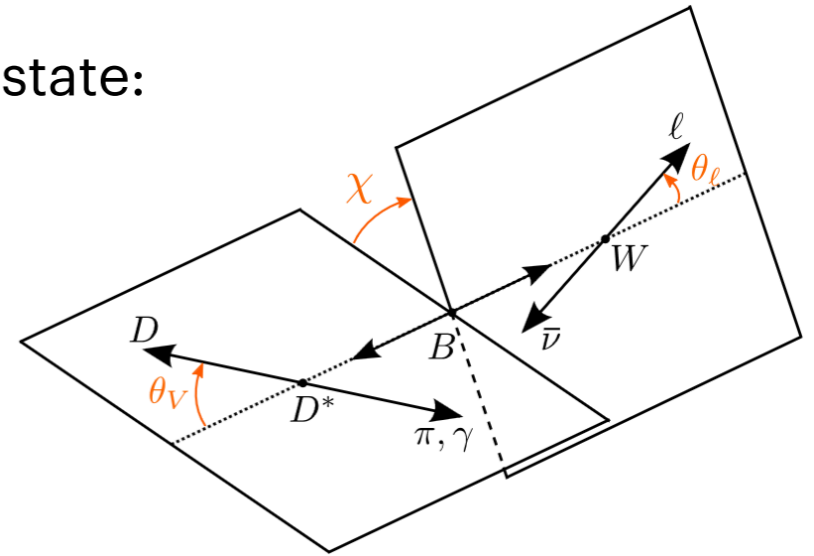
# Topology of $B \rightarrow D^* \ell \nu$ decays

To theoretically describe  $B \rightarrow D^* \ell \nu$  four kinematic variables are needed:

- $w$  is related to the velocity transfer from the initial to the final state:

$$w = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

- 3 angles:  $\theta_V$ ,  $\theta_\ell$  and  $\chi$ .



Asymmetries between electron and muon in the angular distributions sensitive to LFU:

$$A_x(w) = \left( \frac{d\Gamma}{dw} \right)^{-1} \left[ \int_0^1 - \int_{-1}^0 \right] dx \frac{d^2\Gamma}{dw dx}$$

↓      ↓      ↓  
+      -       $\mathcal{A}_{FB}(w) \quad dx \rightarrow d(\cos \theta_\ell)$   
+      -       $\mathcal{S}_3(w) \quad dx \rightarrow d(\cos 2\chi)$   
+      -       $\dots$

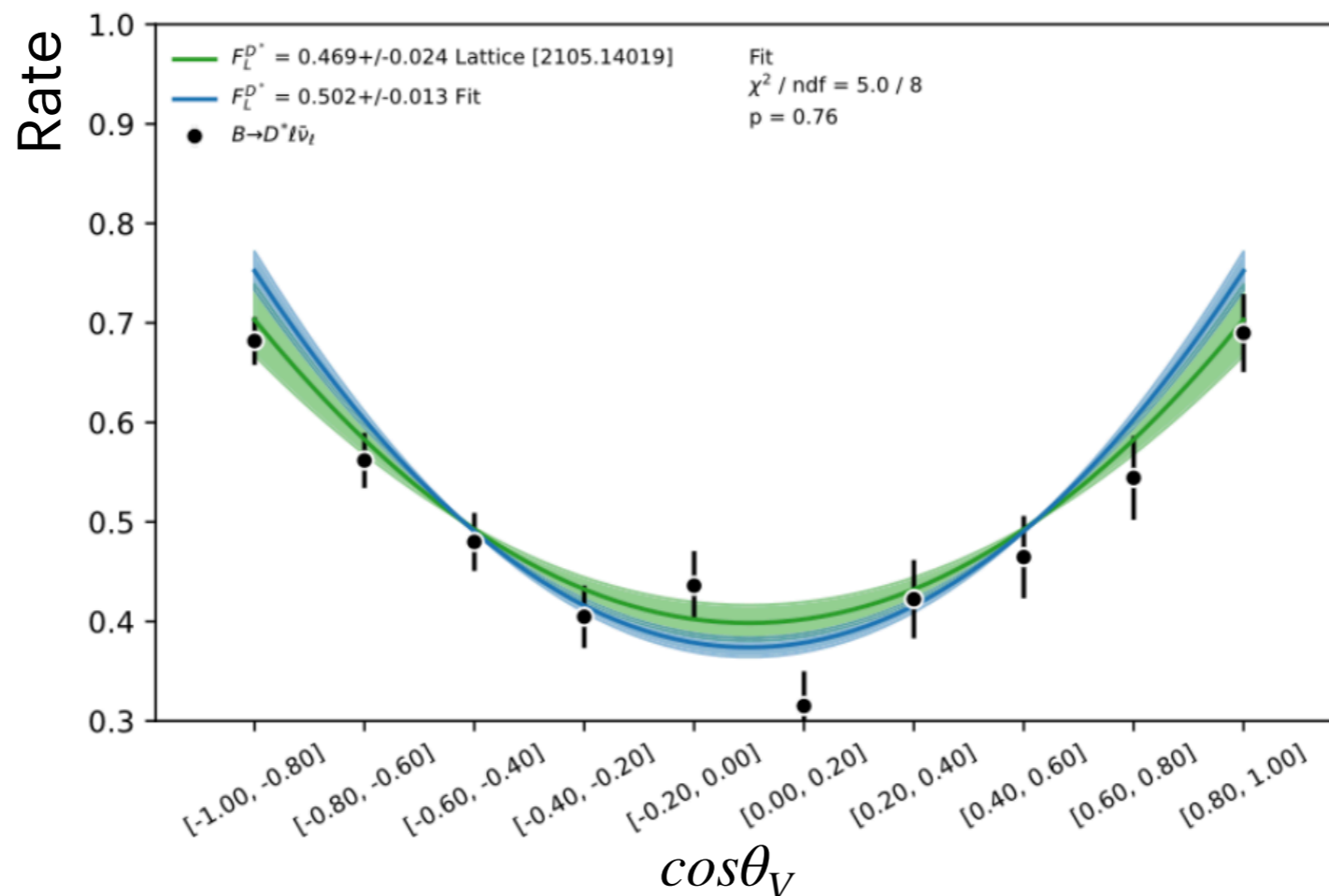
## Experimental strategy:

1. Reconstruct the angular distributions.
2. Signal extraction by fitting  $M_{miss}^2$ .
3. Increase the sensitivity of LFU tests by measure asymmetries in bins of  $w$ .

# $B \rightarrow D^* \ell \nu$ angular asymmetries

PRD 108, 012002 (2023)

**Goal:** measure LFU sensitive observables using  $B \rightarrow D^* \ell \nu$  final states.



Measure difference of electron and muon  $D^*$  longitudinal polarization fraction:

$$\Delta F_L^{D^*} = 0.030 \pm 0.025 \pm 0.007$$

Measure difference of electron and muon FB asymmetry:

$$\Delta A_{FB} = 0.028 \pm 0.028 \pm 0.008$$

Light lepton universality test :

$$R_{e/\mu}(D^*) = \mathcal{B}(B \rightarrow D^* e \nu_e) / \mathcal{B}(B \rightarrow D^* \mu \nu_\mu) = 0.993 \pm 0.023(stat) \pm 0.023(syst)$$

Consistent with SM and previous measurements.

# Measurement of $R(X_{e/\mu})$

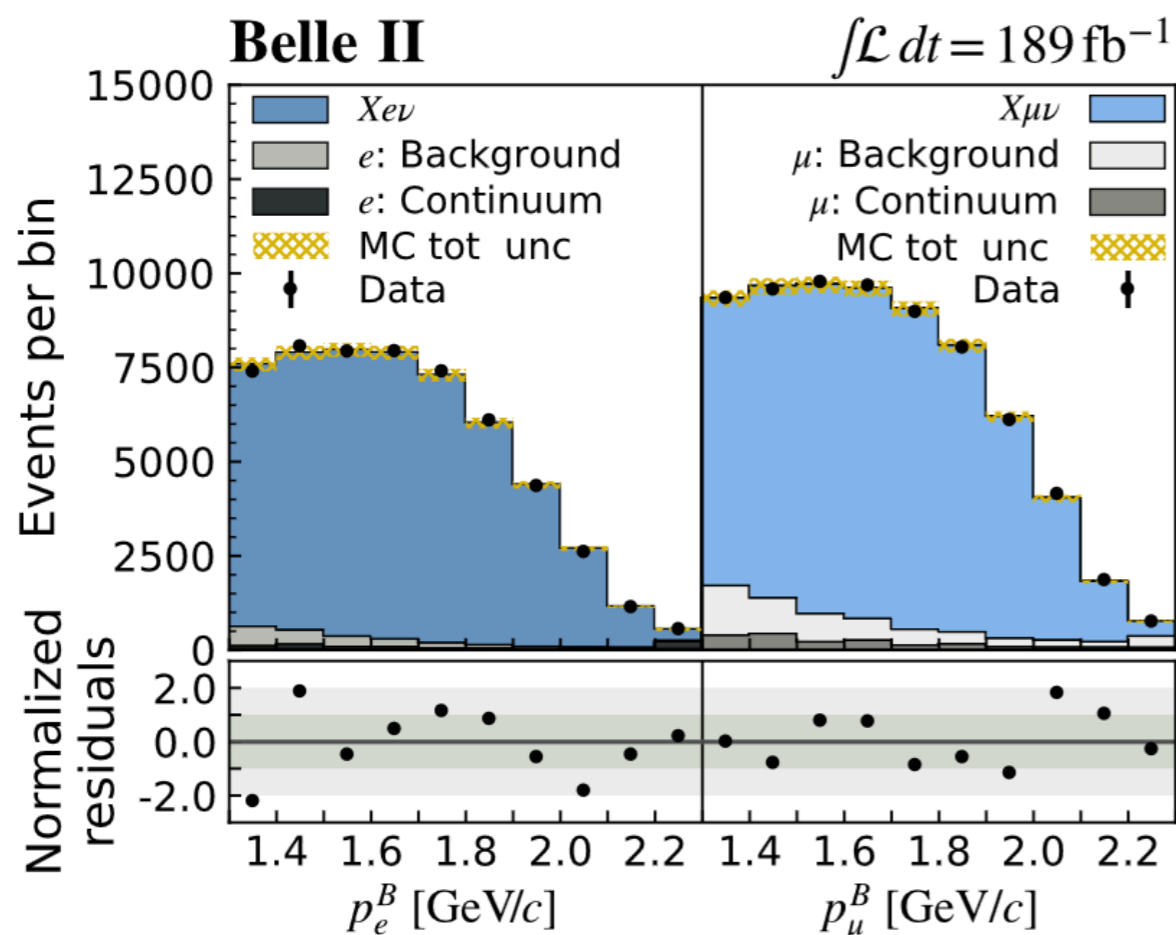
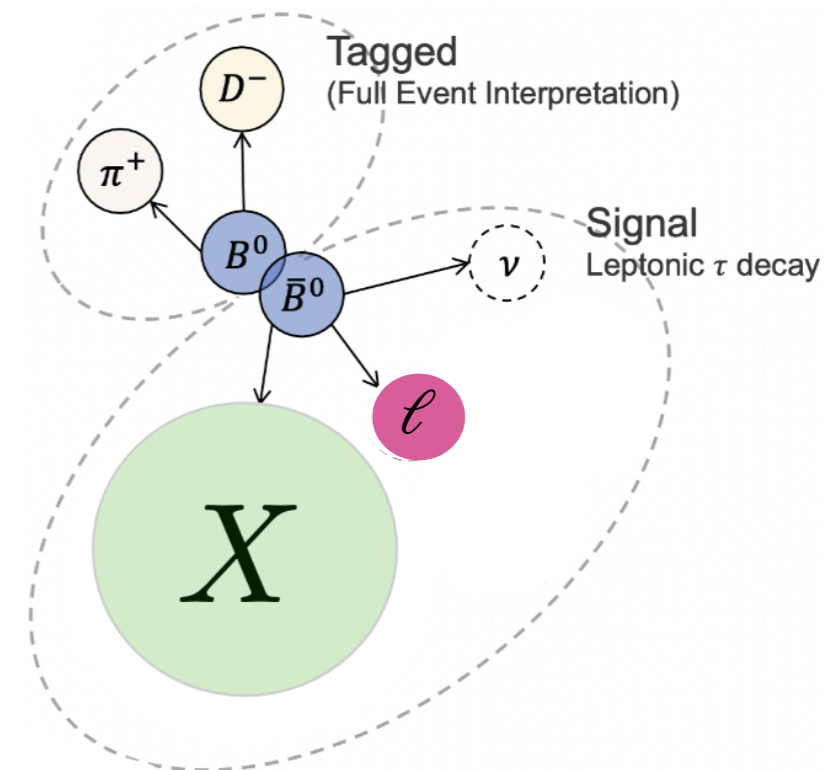
PRL 131, 051804

**Goal:** measure  $R(X_{e/\mu}) = \frac{\mathcal{B}(B \rightarrow X e \nu_e)}{\mathcal{B}(B \rightarrow X \mu \nu_\mu)}$

The most precise test of  $e - \mu$  universality in semileptonic B decays.

**Extract signal** with simultaneous maximum-likelihood templates fits to  $p_e^B$  and  $p_\mu^B$  spectra.

**Main challenge:** modelling  $X\ell\nu$ , fake leptons and secondaries. Use a sideband to validate these components.



**Main systematic:** lepton  $e/\mu$  identification (1.9%)

$$R_{e/\mu}(X) = 1.007 \pm 0.0009(stat) \pm 0.019(syst)$$

Compatible with SM and previous measurements.