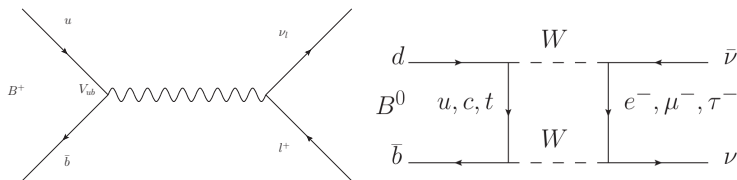


Full Event Interpretation at Belle II



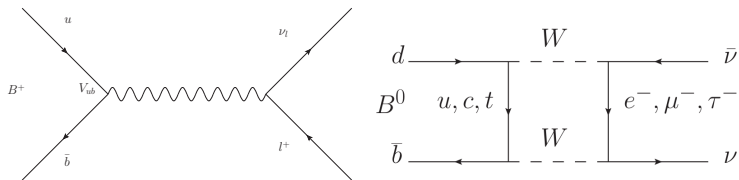
Why we need Full Event Interpretation

- Interesting physics can be obtained from several challenging modes with missing neutrinos ($B \rightarrow D^{(*)}\tau\nu$, $B \rightarrow l\nu$, $B \rightarrow X_u l\nu$, $B \rightarrow h\nu\bar{\nu}$)



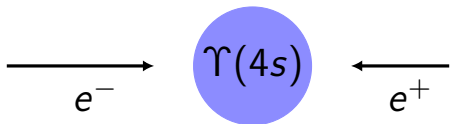
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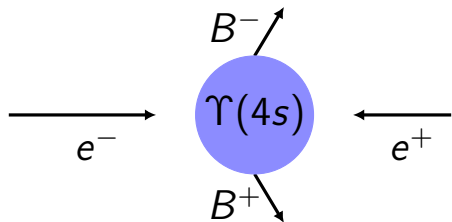
Tag-side B reconstruction

- Collide e^+ and e^- at the energy to make $\Upsilon(4S)$ particles



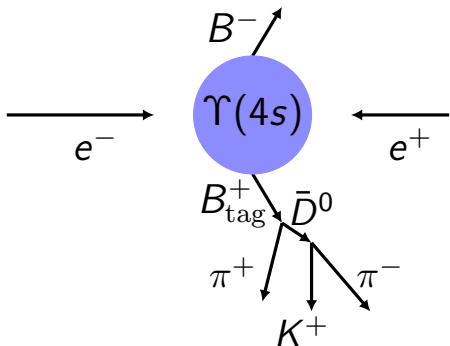
Tag-side B reconstruction

- Collide e^+ and e^- at the energy to make $\Upsilon(4S)$ particles
- $\Upsilon(4S)$ decays to B^+B^- and $B^0\bar{B}^0$ 96% of the time.



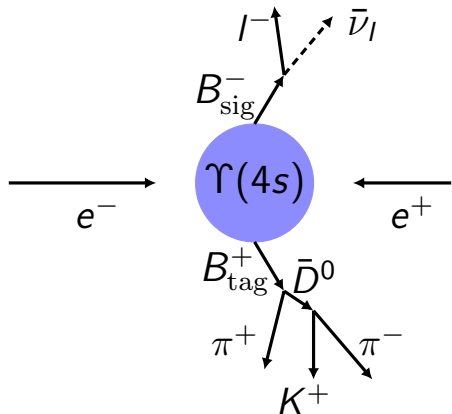
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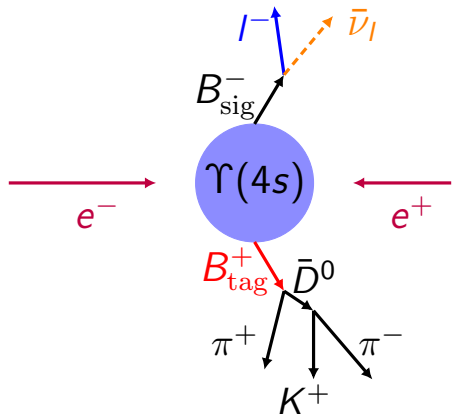
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- Flavour constraints:
 $B_{\text{tag}}^+ \implies B_{\text{sig}}^-$
 Kinematic constraints:

$$p_{\nu} = p_{e^+e^-} - p_{\mu^-} - p_{B^+}$$



Tag-side B reconstruction

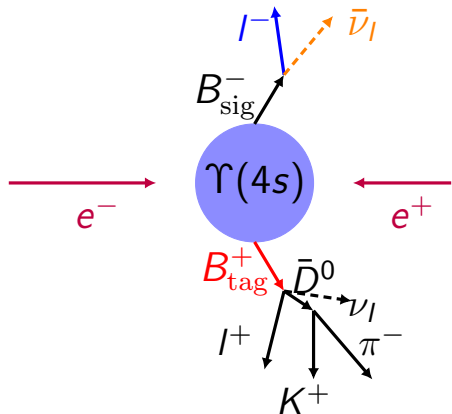
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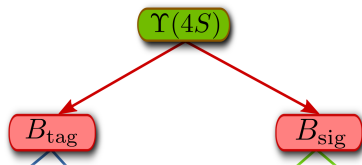
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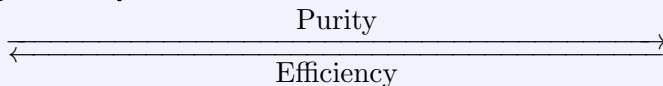
$$p_{\nu} = p_{e^+e^-} - p_{\mu^-} - p_{B^+}$$



Which tag-side reconstruction?



Tagging techniques

**Inclusive**

$B \rightarrow \text{anything}$
 $\epsilon \approx \mathcal{O}(100\%)$

Very large statistics;
 Also very large background

Semileptonic

$B \rightarrow D^{(*)} l \nu_l$
 $\epsilon \approx \mathcal{O}(1\%)$

Mid-range reconstruction
 efficiency;
 Less information about B_{tag}
 due to neutrino

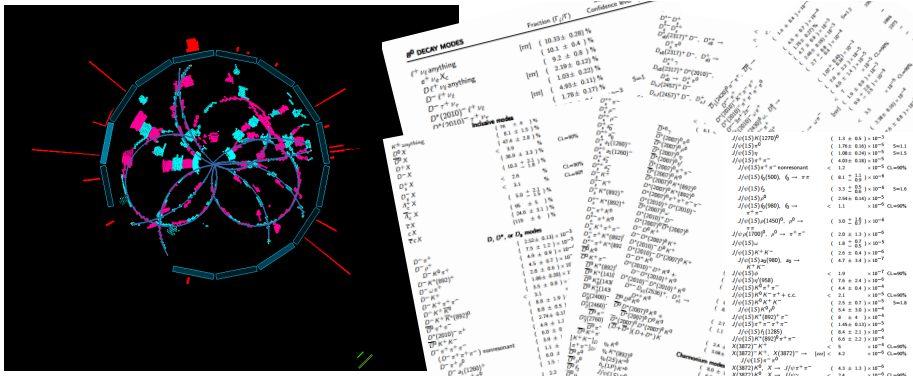
Hadronic

$B \rightarrow \text{hadrons}$
 $\epsilon \approx \mathcal{O}(0.1\%)$

Cleaner sample
 Knowledge of $p(B_{\text{sig}})$;
 Lower tag-side efficiency

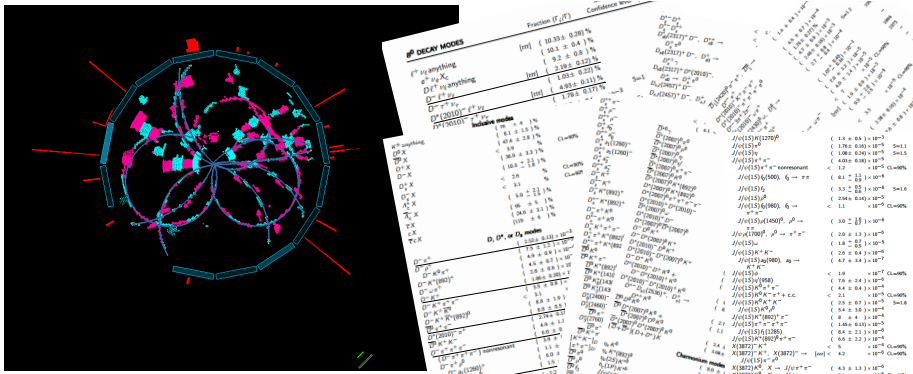
The Task

- Must reconstruct a substantial number of modes (e.g $O(50)$ hadronic modes of B mesons)
- Face combinatorics which scale as the factorial of the number of tracks \implies Require selections early on

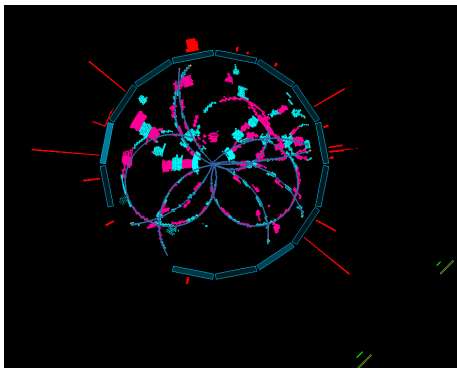


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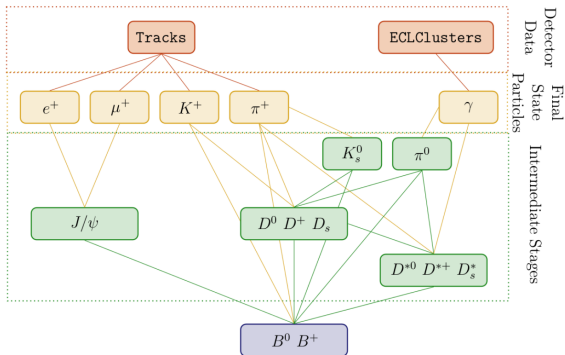
Combinatorics



- ~ 10 tracks in this event
- Let's assume 5 positively charged and 5 negatively charged.
- Now let's reconstruct $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$
- $\binom{5}{2}^2 = 100$ possible combinations
- Reconstructing $B^+ \rightarrow (D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-) \pi^+$ introduces $\binom{3}{1} \times 100 = 300$ combinations.

The Full Event Interpretation

- Utilises $O(200)$ decay channels with classifiers (BDTs) trained for each.
- Reconstructs $O(10000)$ unique decays chains in six stages.



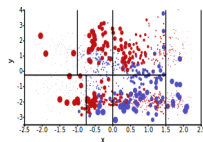
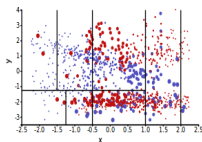
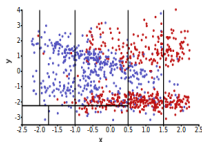
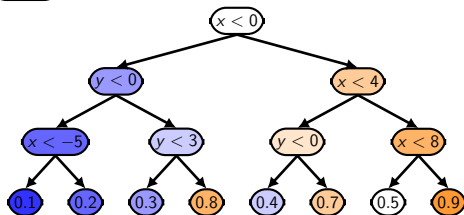
arxiv1807.08680, Keck, T. et al.

Keck, T., PhD Thesis

Classifiers

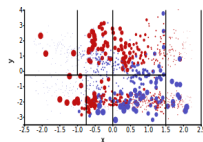
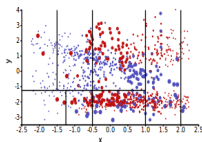
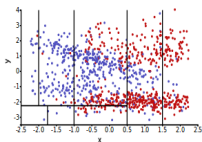
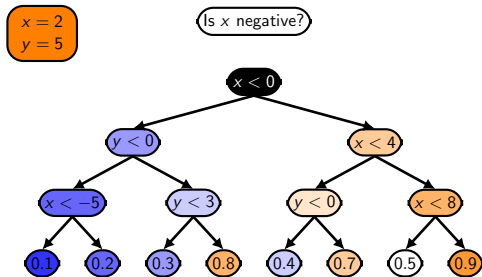
- Describe decay channels with features x_i .
- Labelled training datasets obtained from simulation.
- Train classifiers for each channel, $\mathcal{P}(x_i)$
- The FEI by default uses Boosted Decision Trees.

$x = 2$
 $y = 5$



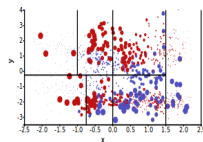
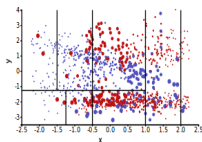
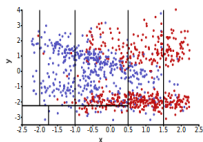
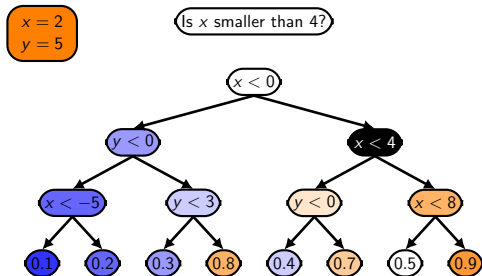
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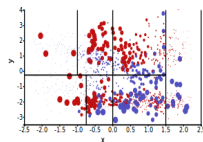
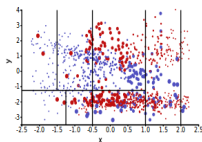
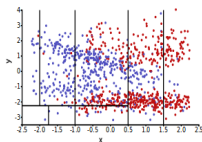
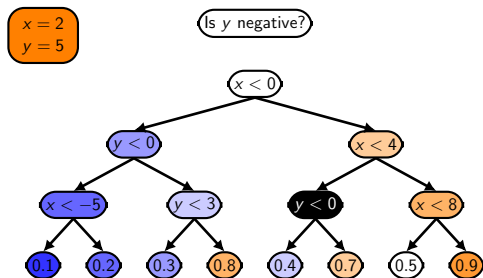
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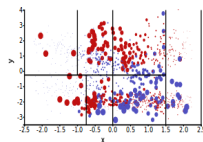
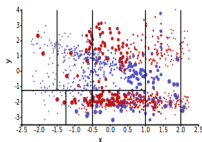
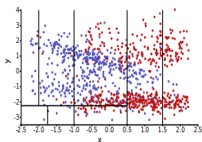
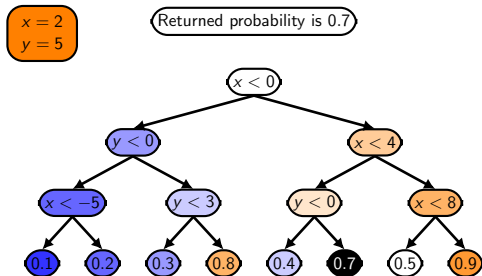
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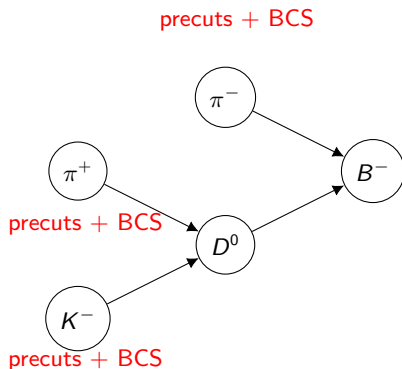
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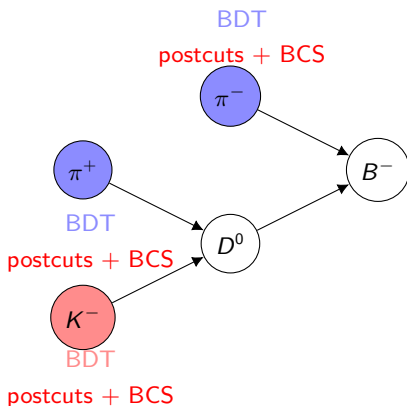
The Algorithm

- Particle candidates assigned from tracks and clusters after a **precuts + Best Candidate Selection (BCS)**.



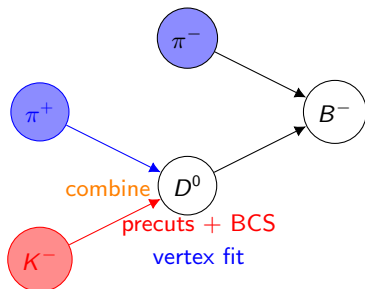
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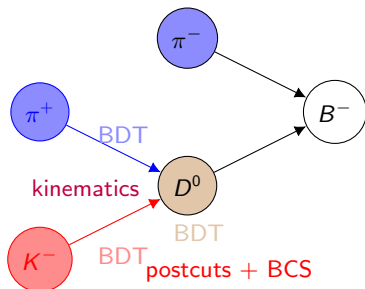
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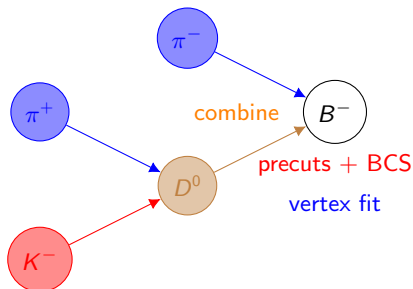
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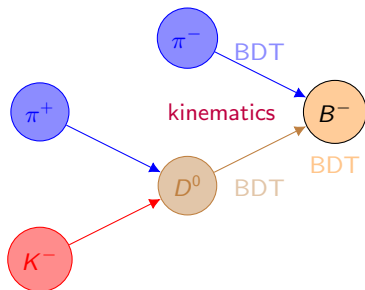
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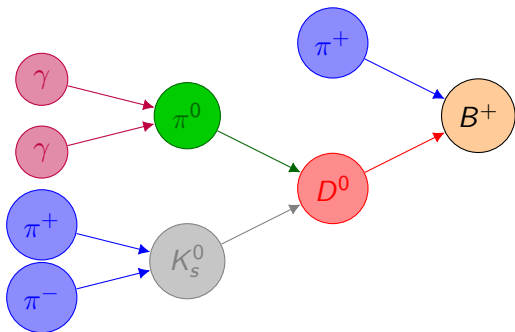


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- B classifier takes daughter classifiers and **kinematics** as inputs.

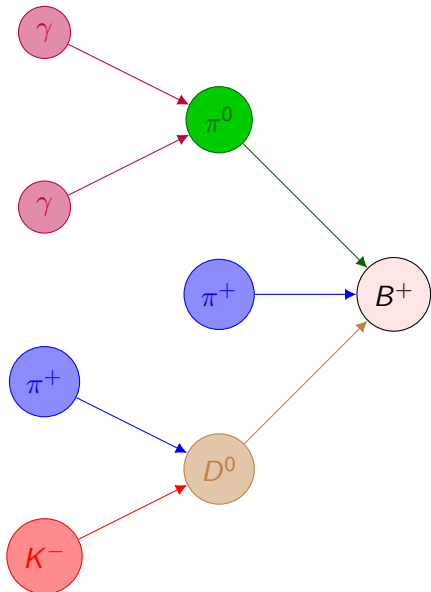


The Algorithm



- Same $B^+ \rightarrow D^0 \pi^+$ classifier.
- Different decay chain as $D^0 \rightarrow K_S^0 \pi^0$.
- $D^0 \rightarrow K_S^0 \pi^0$ has its own classifier.

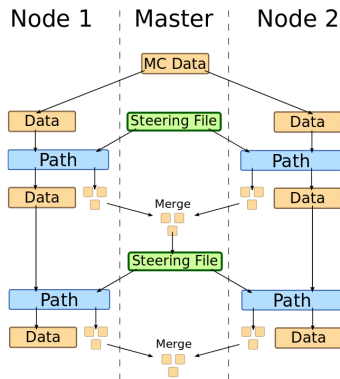
The Algorithm



- Different $B^+ \rightarrow D^0 \pi^+ \pi^0$ decay with its own classifier.
- Original D decay chain as $D^0 \rightarrow K^- \pi^+$.

Training the FEI

- Both training and application phases can be distributed via a map reduce approach.
- For training:
 - ▶ $O(100M)$ simulated $\Upsilon(4S) \rightarrow B\bar{B}$ events
 - ▶ Monte carlo is partitioned and processed at different nodes.
 - ▶ At each of the reconstruction phases training data is generated.
 - ▶ Training data of each stage is subsequently merged and classifiers trained.

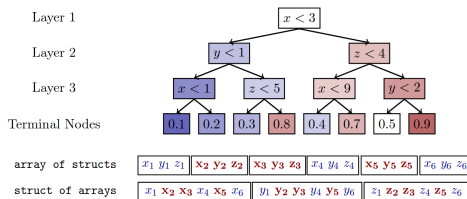


Need for speed

- Utilise FastBDT:
 - ▶ Computes cumulative probability histograms (CPH) of nodes in the same level simultaneously.
 - ▶ Stores data as an array of structs.

[arxiv1609.06119](https://arxiv.org/abs/1609.06119), Keck, T.

- Utilise FastFit ([GitHub link](#)):
 - ▶ Uses eigen libraries to gain from vectorisation.
 - ▶ Overall factor of 2.7 speed up in the FEI

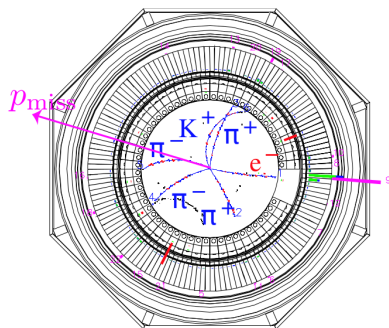
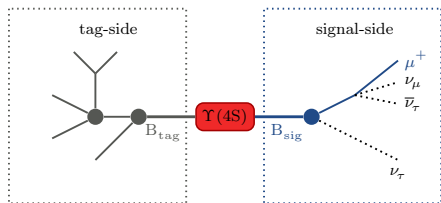


Task	Training	Application
read/write DataStore	30	0
vertex fitting	26	38
particle combination	19	27
classifier inference	11	15
training data & monitoring	6	0
best candidate selection	3	6
other	5	14

- In application 38% of the time is spent on vertex fitting, 27% on particle combination and 15% on classifier inference.

Specific vs Generic FEI

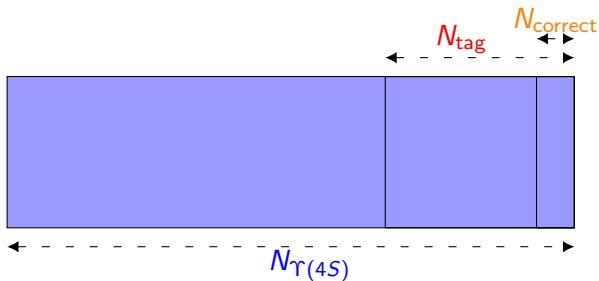
- **Generic FEI** - Reconstruct signal after reconstructing a tag-side B candidate.
- **Specific FEI** - Reconstruct a tag-side B candidate after reconstructing signal



$$B_{tag}^+ \rightarrow \bar{D}^0 \pi^+ \pi^+ \pi^- \quad B_{sig}^- \rightarrow \tau^- \bar{\nu}_\tau$$

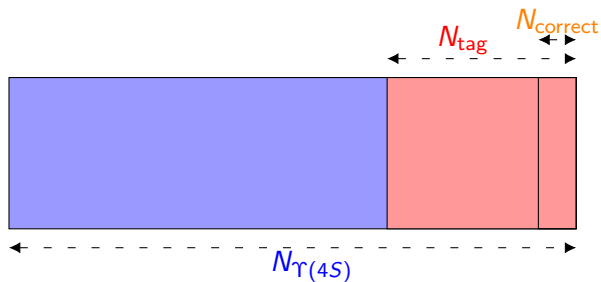
$$\quad \quad \quad \hookrightarrow K^+ \pi^- \quad \quad \quad \hookrightarrow e^- \bar{\nu}_e \nu_\tau$$

How does one quantify tagging performance?



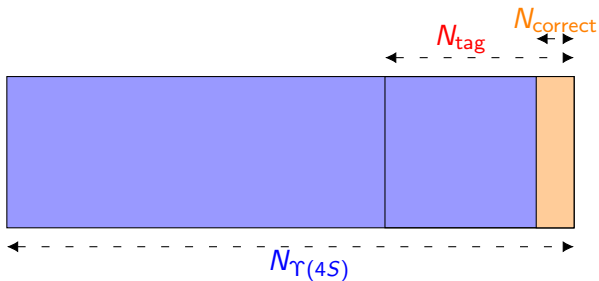
- tagging efficiency = $N_{tag}/N_{\Upsilon(4S)}$

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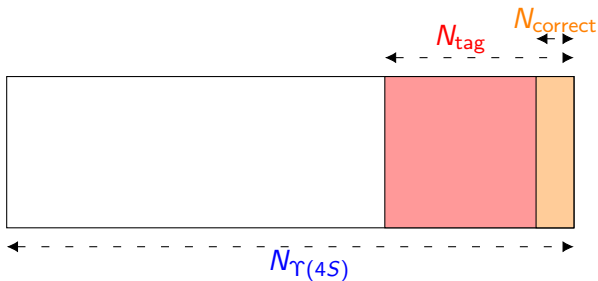
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How does one quantify tagging performance?



- tagging efficiency = $N_{tag}/N_{\Upsilon(4S)}$
- tag-side efficiency = $N_{correct}/N_{\Upsilon(4S)}$

How does one quantify tagging performance?



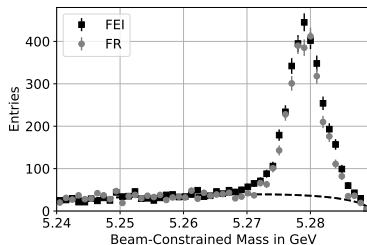
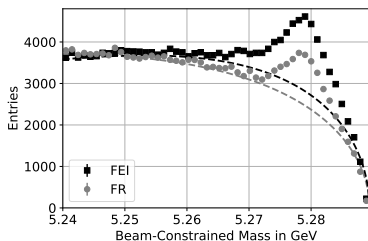
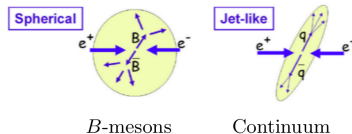
- **tagging efficiency** = $N_{tag}/N_{\Upsilon(4S)}$
- **tag-side efficiency** = $N_{correct}/N_{\Upsilon(4S)}$
- **purity** = $N_{correct}/N_{tag}$

Tagging performance in Belle data

$$m_{bc} = \sqrt{E_B^2 - p_B^2}$$

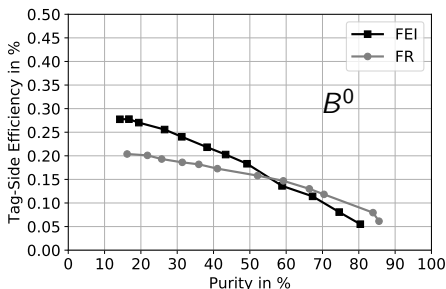
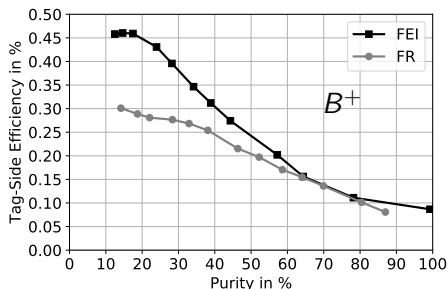
$$E_B = \sqrt{s}/2$$

Different event topologies



Tagging performance

Tag-side efficiency purity in Belle data



Maximum tag-side efficiency

Tag	FR	SER	FEI Belle MC	FEI Belle II MC
Hadronic B^+	0.28%	0.4%	0.76%	0.66%
Hadronic B^0	0.18%	0.2%	0.46%	0.38%
SL B^+	0.31%	0.3%	1.80%	1.45%
SL B^0	0.34%	0.6%	2.04%	1.94%

FR = Full Reconstruction (Belle Algorithm), SER = Semi-Exclusive Reconstruction (BaBar Algorithm)

Conclusion

- The Full Event Interpretation (FEI) is an algorithm for tag-side B reconstruction at Belle 2.
- It trains $O(200)$ decay channel classifiers which are used in the reconstruction of $O(10000)$ decay chains.
- The FEI outperforms its predecessors with a higher tag-side efficiency.
- The FEI is an essential to the Belle II physics program and resolving the B physics anomalies.

References

The Full Event Interpretation – An exclusive tagging algorithm for the Belle II experiment - Thomas Keck et al. <https://arxiv.org/abs/1807.08680>

Machine learning algorithms for the Belle II experiment and their validation on Belle data - Thomas Keck <https://publikationen.bibliothek.kit.edu/1000078149>

Analysis Software and Full Event Interpretation for the Belle II Experiment - Christian Pulvermacher <http://ekp-invenio.physik.uni-karlsruhe.de/record/48741>

FastBDT: A speed-optimized and cache-friendly implementation of stochastic gradient-boosted decision trees for multivariate classification - Thomas Keck <https://arxiv.org/abs/1609.06119>

Tutorial

- Log in to kekcc with port forwarding:
`ssh username@login.cc.kek.jp -L 8300:localhost:8300`
- Note that you should choose a different port.
- Clone repository at <https://stash.desy.de/users/sutclw/repos/feitutorial/browse>:
`git clone ssh://git@stash.desy.de:7999/~sutclw/feitutorial.git`
- Within the tutorial directory run: `source setup_basf2_rel3.sh`
- Run jupyter note book with the following command:
`jupyter-notebook --port 8300 --no-browser`
- If problems see:
<https://confluence.desy.de/display/BI/Running+Jupyter+Notebook+on+KEKCC>