

2024 Belle-II Physics Week KEK, Oct. 14-18



- Lepton Universality
- Lorentz structure of the charged current

Opportunities with Tau Leptonic decays at Belle-II



- Lepton Universality
- Lorentz structure of the charged current (including possible heavy sterile neutrinos)

Opportunities with Tau Leptonic decays at Belle-II

# $\begin{array}{c} \downarrow & \checkmark^{\mathsf{V}_{\mathsf{L}}} \\ & \checkmark^{\mathsf{V}_{\mathsf{L}}} \\ W & \checkmark^{\mathsf{V}_{\mathsf{L}}} \\ \hline & W & \checkmark^{\mathsf{V}_{\mathsf{L}}} \end{array}$

#### Lepton Universality



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**Figure 6**. Observed momentum distribution for muon (left) and electron (right) candidates with fit results overlaid. The lower panel shows the ratio between data and fit results. The hatched area indicates the possible variation of the fitted yields due to systematic effects, with the constraints of the nuisance parameters reduced to their fit uncertainties and correlations taken into account.



Figure 7. Determinations of  $R_{\mu}$  (left) and  $|g_{\mu}/g_e|_{\tau}$  (right) from previous individual measurements [11, 12] and the fit from the Heavy Flavor Averaging Group [15], compared with the result of this work. The shaded areas represent the statistical uncertainties, while the error bars indicate the total uncertainties. The vertical dashed line indicates the SM prediction, including mass effects.

Pich, Prog.Part.Nucl.Phys. 75 (2014) 41-85; Bryman-Cirigliano-Crivellin-Inguglia Ann.Rev.Nucl.Part.Sci. 72 (2022) 69-91

#### This result in the context of other purely leptonic tests of LU

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#### This result in the context of other purely leptonic tests of LU

$$R^{\tau}_{\mu/e} = \frac{\operatorname{Br}[\tau^- \to \mu^- \bar{\nu_{\mu}} \nu_{\tau}]}{\operatorname{Br}[\tau^- \to \mathrm{e}^- \bar{\nu_{\mathrm{e}}} \nu_{\tau}]} \,,$$

$$R_{\tau/\mu}^{\tau} = \frac{\operatorname{Br}[\tau^{-} \to e^{-} \bar{\nu_{e}} \nu_{\tau}]}{\operatorname{Br}[\mu^{-} \to e^{-} \bar{\nu_{e}} \nu_{\mu}]}, \text{and}$$
$$R_{\tau/e}^{\tau} = \frac{\operatorname{Br}[\tau^{-} \to \mu^{-} \bar{\nu_{\mu}} \nu_{\tau}]}{\operatorname{Br}[\mu^{-} \to e^{-} \bar{\nu_{e}} \nu_{\mu}]},$$

From W leptonic decays:



Belle-II '24 =>  $g_{\mu}/g_e$ =0.9974(19) 1.4 $\sigma$ 

 $g_{\tau}/g_{\mu}=1.0010(14)$  0.7 $\sigma$ 

 $g_{\tau}/g_{e}=1.0029(14)$  2.1 $\sigma$ 



NP constrained at few TeV level

#### Lepton Universality

 $\Gamma \sim G_F^2 m_L^5$ 

It can also be checked benefitting from the Belle-II  $\tau$  mass measurement, using the leptonic BR determination:



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#### Lepton Universality

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Still from LEP!!

#### Lorentz structure of the charged current

$$\mathcal{H} = 4 \frac{G_{\ell'\ell}}{\sqrt{2}} \sum_{n,\epsilon,\omega} g_{\epsilon\omega}^n \left[ \overline{\ell'_{\epsilon}} \Gamma^n(\nu_{\ell'})_{\sigma} \right] \left[ \overline{(\nu_{\ell})_{\lambda}} \Gamma_n \ell_{\omega} \right]$$

It depends on 4S, 4V & 2T complex couplings labelled also by charged lepton chiralities.

Opportunities with Tau Leptonic decays at Belle-II

#### Lorentz structure of the charged current

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It depends on 4S, 4V & 2T complex couplings labelled also by charged lepton chiralities.

$$1 = \frac{1}{4} \left( |g_{RR}^{S}|^{2} + |g_{RL}^{S}|^{2} + |g_{LR}^{S}|^{2} + |g_{LL}^{S}|^{2} \right) + 3 \left( |g_{RL}^{T}|^{2} + |g_{LR}^{T}|^{2} \right) \\ + \left( |g_{RR}^{V}|^{2} + |g_{RL}^{V}|^{2} + |g_{LR}^{V}|^{2} + |g_{LL}^{V}|^{2} \right) .$$

Opportunities with Tau Leptonic decays at Belle-II

#### Lorentz structure of the charged current

$$\mathcal{H} = 4 \frac{G_{\ell'\ell}}{\sqrt{2}} \sum_{n,\epsilon,\omega} g_{\epsilon\omega}^n \left[ \overline{\ell'_{\epsilon}} \Gamma^n(\nu_{\ell'})_{\sigma} \right] \left[ \overline{(\nu_{\ell})_{\lambda}} \Gamma_n \ell_{\omega} \right] ,$$

It depends on 4S, 4V & 2T complex couplings.

Opportunities with Tau Leptonic decays at Belle-II



Five additional parameters if the l' polarization is also measured.

**Opportunities with Tau Leptonic decays at Belle-II** 

Lorentz structure of the charged current							
$\frac{d^2\Gamma_{\ell\to\ell'}}{dxd\cos\theta} = \frac{m_\ell\omega^4}{2\pi^3}G_{\ell'\ell}^2\sqrt{x^2 - x_0^2}\left\{F(x) - \frac{\xi}{3}\mathcal{P}_\ell\sqrt{x^2 - x_0^2}\cos\thetaA(x)\right\}^{\ \cos\theta = \mathbf{s}_{\mathbf{l}}\cdot\mathbf{p}_{\mathbf{l}}}$							
	$\omega \equiv (m_{\ell}^2 + m_{\ell'}^2)/2m_{\ell}  F(x) = x(1-x) + \frac{2}{9}\rho \left(4x^2 - 3x - x_0^2\right) + \eta x_0(1-x),$						
x	$x \equiv E_{\ell'}/\omega$ i $x_0 \equiv m_{\ell'}/\omega$ $A(x) = 1 - x + \frac{2}{3}\delta\left(4x - 4 + \sqrt{1 - x_0^2}\right)$ .						
SM		$\mu^- \to e^- \bar{\nu}_e \nu_\mu$	$\tau^-  o \mu^- \bar{\nu}_\mu \nu_\tau$	$\tau^- \to e^- \bar{\nu}_e \nu_\tau$	$\tau^- \to \ell^- \bar{\nu}_\ell \nu_\tau$		
3/4	ρ	$0.74979 \pm 0.00026$	$0.763 \pm 0.020$	$0.747 \pm 0.010$	$0.745 \pm 0.008$		
0	$\eta$	$0.057 \pm 0.034$	$0.094 \pm 0.073$		$0.013 \pm 0.020$		
1	ξ	$1.0009 \ {}^+ \ {}^{0.0016}_{0.0007}$	$1.030\pm0.059$	$0.994 \pm 0.040$	$0.985 \pm 0.030$		
3/4	ξδ	$0.7511 \ {}^+ \ {}^{0.0012}_{0.0006}$	$0.778 \pm 0.037$	$0.734 \pm 0.028$	$0.746 \pm 0.021$		
1	$\xi'$	$1.00\pm0.04$					
1	$\xi''$	$0.65\pm0.36$					

	Lorentz structure of the charged current					
$\frac{d^2\Gamma_{\ell\to\ell'}}{dxd\cos\theta} = \frac{m_\ell\omega^4}{2\pi^3}G^2_{\ell'\ell}\sqrt{x^2-x_0^2}\left\{\right.$			$\left\{F(x) - \frac{\xi}{3} \mathcal{P}_{\ell} \sqrt{x^2 - x_0^2} \cos \theta A(x)\right\} \cos \theta = \mathbf{s}_{\mathbf{l}} \cdot \mathbf{p}_{\mathbf{l}'}$			
00	$\omega \equiv (m_{\ell}^2 + m_{\ell'}^2)/2m_{\ell}  F(x) = x(1-x) + \frac{2}{9}\rho \left(4x^2 - 3x - x_0^2\right) + \eta x_0(1-x),$					
x	$x = E_{\ell'}/\omega \qquad x_0 \equiv m_{\ell'}/\omega  A(x) = 1 - x + \frac{2}{3}\delta \left(4x - 4 + \sqrt{1 - x_0^2}\right).$					
SM		$\mu^- \to e^- \bar{\nu}_e \nu_\mu$	$\tau^-  o \mu^- \bar{\nu}_\mu \nu_\tau$	$\tau^- \to e^- \bar{\nu}_e \nu_\tau$	$\tau^- \to \ell^- \bar{\nu}_\ell \nu_\tau$	
3/4	ρ	$0.74979 \pm 0.00026$	$0.763 \pm 0.020$	$0.747 \pm 0.010$	$0.745 \pm 0.008$	
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3/4	ξδ	$0.7511 \stackrel{+}{}{}^{+}{}^{0.0012}_{-}{}^{-}{}^{0.0006}$	$0.778 \pm 0.037$	$0.734 \pm 0.028$	$0.746 \pm 0.021$	
1	ξ'	$1.00\pm0.04$	0.22±0. <del>9</del> 4±0.42 —	D	ominated by statistics.	
1	ξ"	$0.65\pm0.36$	Belle Phys.Rev.Lett. 13	1 (2023) 2 <u>, 02</u> 1801 O	pportunity for Belle-II	
	Phys.Rev.D 108 (2023) 1, 012003					

	Lorentz structure of the charged current					
$\frac{d^2 \Gamma_{\ell \to \ell'}}{dx  d \cos \theta} = \frac{m_\ell  \omega^4}{2\pi^3}  G_{\ell'\ell}^2  \sqrt{x^2 - x_0^2}  \left\{ F(x) - \frac{\xi}{3} \mathcal{P}_\ell  \sqrt{x^2 - x_0^2}  \cos \theta  A(x) \right\}  \cos \theta = \mathbf{s}_{\mathbf{f}} \cdot \mathbf{p}_{\mathbf{f}}$					cosθ= <b>s</b> <sub>l</sub> ∙ <b>p</b> <sub>l'</sub>	
r	$\omega \equiv (m_{\ell}^2 + m_{\ell'}^2)/2m_{\ell}  F(x) = x(1-x) + \frac{2}{9}\rho \left(4x^2 - 3x - x_0^2\right) + \eta x_0(1-x),$					
$x = E_{\ell'}/\omega \qquad x_0 \equiv m_{\ell'}/\omega  A(x) = 1 - x + \frac{2}{3}\delta \left(4x - 4 + \sqrt{1 - x_0^2}\right).$					$\overline{-x_0^2}$ ).	
SM		$\mu^- \to e^- \bar{\nu}_e \nu_\mu$	$\hat{C} = C$	$m_{\ell'} g(m_{\ell'}^2/m_{\ell}^2)$	$\overline{)}$ $\tau^- \to \ell^- \bar{\nu}_\ell \nu_\tau$	
3/4	ho	$0.74979 \pm 0.00026$	$G_{\ell'\ell} = G_{\ell'\ell} \bigvee^{1}$	$+4\eta \overline{m_\ell} \overline{f(m_{\ell'}^2/m_\ell^2)}$	$\overline{)}$ 0.745 ± 0.008	
0	$\eta$	$0.057 \pm 0.034$	$0.094 \pm 0.073$		$0.013 \pm 0.020$	
1	ξ	$1.0009 \ {}^+_{-} \ {}^{0.0016}_{0.0007}$	$1.030 \pm 0.059$	$0.994 \pm 0.040$	$0.985 \pm 0.030$	
3/4	$\xi\delta$	$0.7511 \ {}^+_{-} \ {}^{0.0012}_{0.0006}$	$0.778 \pm 0.037$	$0.734 \pm 0.028$	$0.746 \pm 0.021$	
1	$\xi'$	$1.00\pm0.04$	0.22±0.94±0.42			
1	ξ"	$0.65\pm0.36$	Belle Phys.Rev.Lett. 13	1 (2023) 2 <u>, 02</u> 1801		
	-		Phys.Rev.D 108 (2	.023) 1, 012003		

	Lorentz structure of the charged current					
$\frac{d^2\Gamma}{dxd}$	$\frac{d^2 \Gamma_{\ell \to \ell'}}{dx  d \cos \theta} = \frac{m_\ell  \omega^4}{2\pi^3}  G_{\ell'\ell}^2  \sqrt{x^2 - x_0^2}  \left\{ F(x) - \frac{\underline{\xi}}{3} \mathcal{P}_\ell  \sqrt{x^2 - x_0^2}  \cos \theta  A(x) \right\}  \cos \theta = \mathbf{s}_{I} \cdot \mathbf{p}_{I'}$					
x	$\omega \equiv (m_{\ell}^2 + m_{\ell'}^2)/2m_{\ell}  F(x) = x(1-x) + \frac{2}{9}\rho \left(4x^2 - 3x - x_0^2\right) + \eta x_0(1-x),$ $x \equiv E_{\ell'}/\omega  x_0 \equiv m_{\ell'}/\omega  A(x) = 1 - x + \frac{2}{5}\delta \left(4x - 4 + \sqrt{1 - x_0^2}\right)$					
SM		$\mu^- \to e^- \bar{\nu}_e \nu_\mu$		$\frac{3}{m_{w}} \frac{1}{a(m^2/m^2)}$	$\tau^- \to \ell^- \bar{\nu}_\ell \nu_\tau$	
3/4	ρ	$0.74979 \pm 0.00026$	$\widehat{G}_{\ell'\ell} \equiv G_{\ell'\ell} \sqrt{1} +$	$-4\eta \frac{m_{\ell'}}{m_{\ell}} \frac{g(m_{\ell'}/m_{\ell})}{f(m_{\ell'}^2/m_{\ell}^2)}$	$0.745 \pm 0.008$	
0	$\eta$	$0.057 \pm 0.034$	$0.094 \pm 0.073$		$0.013 \pm 0.020$	
1	ξ	$1.0009$ $\eta = \frac{1}{2}$ Re	$e \left[ g_{LL}^V g_{RR}^{S*} + g_{RR}^V g_{LL}^{S*} \right]$	$+ g_{LR}^V \left( g_{RL}^{S*} + 6 g_{RL}^{T*} \right)$	$) + g_{RL}^{V} \left( g_{LR}^{S*} + 6  g_{LR}^{T*} \right) $	
3/4	$\xi\delta$	0.7511 - 0.0006	<u> </u>	·····	·····	
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	,		Phys.Rev.D 108 (2	023) 1, 012003		

Massive case

Opportunities with Tau Leptonic decays at Belle-II

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What is new:

- We write our expressions in the PDG parametrization form, in a way that complements all previous results, facilitating their application to model-dependent scenarios.
- We classify the Dirac and Majorana contributions with the help of a flag parameter  $\epsilon = 0, 1$ , making easier to distinguish between Dirac and Majorana nature of neutrinos.
- We discuss their main differences, together with some examples of its Dirac application to model-dependent theories.
- We also introduced and discussed the leading W-boson propagator correction to the differential decay rate including the final charged-lepton polarization.

Study suggested by Denis Epifanov (generalizing earlier work by Michel, Bouchiat-Michel, Fetscher-Gerber-Johnson, Langacker-London, Shrock, Doi-Kotani-Takasugi, etc.) JHEP 11 (2022) 117

**Figure 6**: Neutrino mass contribution to Dirac and Majorana distributions.

Michel parameters in presence of massive Dirac or Majorana neutrinos (Juanma Márquez, Gabriel López Castro & P. R., JHEP11(2022)117)

Majorana











This paper apparently avoids the Kayser's confusion theorem 'Any property differentiating Dirac/Majorana neutrinos will be suppressed by active neutrino masses, with neutrinos coupling to the SM's SU(2)<sub>L</sub>'.

**Opportunities with Tau Leptonic decays at Belle-II** 

This paper apparently avoids the Kayser's confusion theorem 'Any property differentiating Dirac/Majorana neutrinos will be suppressed by active neutrino masses, with neutrinos coupling to the SM's SU(2)<sub>L</sub>'.

The idea is to use 4-body decays including a pair or vs and another pair of particles, and go to the back-to-back (b2b) configuration for these pairs, in which the properties of the neutrinos can be inferred without actually measuring them, thus avoiding Kaiser's Th.

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Looking in depth (Juanma Márquez, Diego Portillo & P. R., PRD109 (2024) 3, 033005), there is a loophole in their derivation. When corrected, it yields observables which are orders or magnitude smaller than initially thought, likely preventing the observation of this effect.

+ Opportunities with Tau Leptonic decays at Belle-II

See also Akhmedov&Trautner, JHEP109 (2024) 3, 033005

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In fact, applying Kim's paper one should get BRs~10<sup>-4</sup> for the b2b configuration, while we predict rates ~ 10<sup>-10</sup>. Belle-II can disprove the former prediction!

Opportunities with Tau Leptonic decays at Belle-II

See also Akhmedov&Trautner, JHEP109 (2024) 3, 033005



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