

# Prospects on the magnetic/electric dipole moment of the tau and polarized beams

$u^b$

UNIVERSITÄT  
BERN

AEC  
ALBERT EINSTEIN CENTER  
FOR FUNDAMENTAL PHYSICS

Martin Hoferichter

Albert Einstein Center for Fundamental Physics,  
Institute for Theoretical Physics, University of Bern

Oct 14, 2024

2024 Belle II Physics Week, KEK, Tsukuba

Talk by J. Michael Roney at 2024 US Belle II Summer Workshop  
<https://indico.belle2.org/event/11190/contributions/76575/>

The Belle II Detector Upgrades Framework Conceptual Design Report, arXiv:2406.19421

Snowmass 2021 White Paper, Upgrading SuperKEKB with a Polarized Electron Beam:  
Discovery Potential and Proposed Implementation, arXiv:2205.12847

Crivellin, MH, Roney PRD 106 (2022) 093007

Gogniat, MH, Ulrich work in progress

# Why do we need a polarized electron beam?

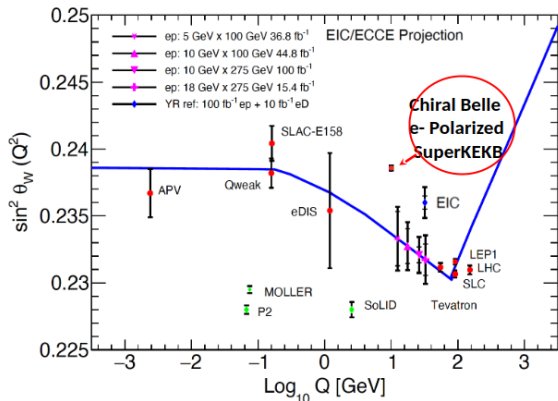


Figure adapted from Boughezal et al. 2022, used in EIC Snowmass paper 2203.13199

## ● Main motivation: **precision neutral-current electroweak program**

- With  $40 \text{ ab}^{-1}$ ,  $\Delta \sin^2 \theta_W = 0.00018$  (combined leptons)
  - ↪ same precision as Z-pole measurements, but at  $s \simeq (10 \text{ GeV})^2$ !
- Precision probe of running of  $\sin^2 \theta_W$ , complementary to MOLLER, P2, ...
- Probes  $e, \mu, \tau, c, b$  couplings, not “just” first generation

# Left-right asymmetries

$f$	SM	LEP+SLAC	Chiral Belle $\Delta g_V^f$			$\Delta \sin^2 \theta_W$
	$g_V^f(M_Z)$	$g_V^f$	1 ab <sup>-1</sup>	20 ab <sup>-1</sup>	40 ab <sup>-1</sup>	40 ab <sup>-1</sup>
$b$	-0.3437(1)	-0.3220(77)	0.0022	0.002	0.002	0.003
$c$	0.1920(2)	0.1873(70)	0.0036	0.001	0.001	0.0008
$\tau$	-0.0371(3)	-0.0366(10)	0.0049	0.001	0.0008	0.0004
$\mu$	-0.0371(3)	-0.03667(23)	0.0031	0.0007	0.0005	0.0003
$e$	-0.0371(3)	-0.03816(47)	0.0039	0.0009	0.0006	0.0003

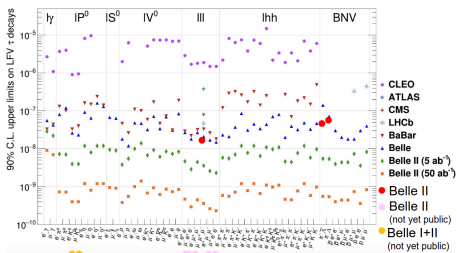
ICHEP talk by Roney

- **Vector couplings** from  $Z-\gamma$  interference

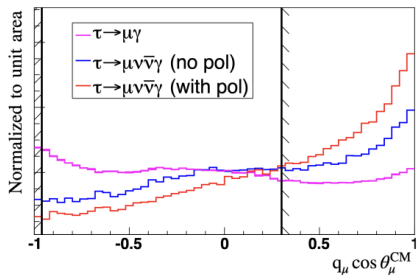
$$A_{LR} = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = \frac{4}{\sqrt{2}} \left( \frac{G_{FS}}{4\pi\alpha Q_f} \right) g_A^e g_V^f \langle \text{Pol} \rangle \quad g_V^f = T_3^f - 2Q_f \sin^2 \theta_W$$

- Major improvements for 2<sup>nd</sup> and 3<sup>rd</sup> generation, by factors {4, 6, 3} for { $b, c, \mu$ }
- Average of { $e, \mu, \tau$ } for  $\sin^2 \theta_W$  same precision as  $Z$ -pole measurements
- Universality of  $g_V^f$  even better tested because dominant  $\langle \text{Pol} \rangle$  uncertainty cancels

# Polarization upgrade: broader physics program



talk by S. Prell



2205.12847

- Improved sensitivity to **lepton-flavor-violating decays**:  $\tau \rightarrow \mu\gamma$  and  $\tau \rightarrow e\gamma$

↔  $e^-$  beam polarization helps reduce backgrounds

- Improved precision measurements of  $\tau$  **Michel parameters**

- Precision QCD studies

- Dipole moments of the  $\tau$**

- Anomalous magnetic moment  $a_\tau$  via Pauli form factor  $F_2(s)$  at  $s \simeq (10 \text{ GeV})^2$
- EDM  $d_\tau$  via  $F_3(s)$  at  $s \simeq (10 \text{ GeV})^2$

↔ focus of this talk

## EFT definition

$$\mathcal{L}_{\text{dipole}} = -c_R^{\ell\ell} \bar{l} \sigma^{\mu\nu} P_R l F_{\mu\nu} + \text{h.c.} \quad P_R = \frac{1 + \gamma_5}{2} \quad \ell \in \{e, \mu, \tau\}$$
$$a_\ell = -\frac{4m_\ell}{e} \text{Re } c_R^{\ell\ell} \quad d_\ell = -2 \text{Im } c_R^{\ell\ell}$$

- **Hermiticity** leaves only two dipole structures  
     $\hookrightarrow a_\ell, d_\ell$  real quantities by definition
- But PDG lists limits [Belle 2022](#)

$$\text{Re } d_\tau = -0.62(63) \times 10^{-17} \text{ e cm} \quad \text{Im } d_\tau = -0.40(32) \times 10^{-17} \text{ e cm}$$

$\hookrightarrow$  to understand what's going on need to look at **form factors**

## Form factors

$$\langle p' | j_{em}^\mu | p \rangle = e \bar{u}(p') \left[ \gamma^\mu F_1(q^2) + \frac{i\sigma^{\mu\nu} q_\nu}{2m_\ell} F_2(q^2) + \frac{\sigma^{\mu\nu} q_\nu \gamma_5}{2m_\ell} F_3(q^2) + \left( \gamma^\mu - \frac{2m_\ell q^\mu}{q^2} \right) \gamma_5 F_4(q^2) \right] u(p)$$

$$F_1(0) = 1 \quad F_2(0) = a_\ell \quad F_3(0) = \frac{2m_\ell}{e} d_\ell \quad F_4(0) = \text{anapole moment} \quad q = p' - p$$

- At  $e^+ e^- \rightarrow \tau^+ \tau^-$ , don't measure  $F_i(0)$ , but  $F_i(s)$  with  $s \simeq (10 \text{ GeV})^2$   
 $\hookrightarrow F_i(s)$  can develop an imaginary part!
- Limits should read (strictly speaking)

$$\frac{e}{2m_\tau} \text{Re } F_3(s) = -0.62(63) \times 10^{-17} \text{ e cm} \quad \frac{e}{2m_\tau} \text{Im } F_3(s) = -0.40(32) \times 10^{-17} \text{ e cm}$$

- Still interesting because of EFT: heavy new physics decouples  
 $\hookrightarrow \text{Re } F_3(s) \simeq d_\tau$  if  $M_{\text{BSM}}^2 \gg s$
- Imaginary part not related to EDM

- Idea: write  $e^+e^- \rightarrow \tau^+\tau^-$  matrix element as

$$\mathcal{M}^2 = \mathcal{M}_{\text{SM}}^2 + \text{Re } d_\tau \mathcal{M}_{\text{Re}}^2 + \text{Im } d_\tau \mathcal{M}_{\text{Im}}^2 + \cancel{|d_\tau|^2 \mathcal{M}_{\text{CP}}^2}$$

- CP-odd terms**

$$\mathcal{M}_{\text{Re}}^2 \propto (\mathbf{S}_+ \times \mathbf{S}_-) \cdot \hat{\mathbf{k}}, \quad (\mathbf{S}_+ \times \mathbf{S}_-) \cdot \hat{\mathbf{p}}$$

$$\mathcal{M}_{\text{Im}}^2 \propto (\mathbf{S}_+ - \mathbf{S}_-) \cdot \hat{\mathbf{k}}, \quad (\mathbf{S}_+ - \mathbf{S}_-) \cdot \hat{\mathbf{p}}$$

with  $\tau^\pm$  spin vectors  $\mathbf{S}_\pm$  and CMS momenta  $\hat{\mathbf{k}}$  ( $\tau^-$ ),  $\hat{\mathbf{p}}$  ( $e^-$ )

- Problem: cannot reconstruct  $\mathbf{S}_\pm$  and  $\hat{\mathbf{k}}$  exactly due to neutrinos  
 $\hookrightarrow$  method of optimal observables, need to vary  $m_{\nu\nu}$
- Includes average over  $e\mu$ ,  $e\pi$ ,  $\mu\pi$ ,  $e\rho$ ,  $\mu\rho$ ,  $\pi\rho$ ,  $\rho\rho$ ,  $\pi\pi$  channels

# Indirect limits for $\tau$ EDM and future improvements

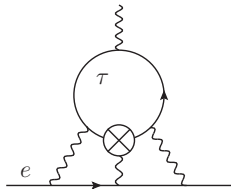
- Another EFT argument:  $d_\tau$  generates contribution to  $d_e$

- ThO:  $d_e \leq 1.1 \times 10^{-29} e \text{ cm}$  [Andreev et al. 2018](#)
- HfF<sup>+</sup>:  $d_e \leq 4.1 \times 10^{-30} e \text{ cm}$  [Roussy et al. 2023](#)

via 3-loop diagram [Grozin, Khriplovich, Rudenko 2009](#)

$$d_\tau \leq \left[ \left( \frac{15}{4} \zeta(3) - \frac{31}{12} \right) \frac{m_e}{m_\tau} \left( \frac{\alpha}{\pi} \right)^3 \right]^{-1} d_e$$
$$= \{1.6 \times 10^{-18}, 5.9 \times 10^{-19}\} e \text{ cm}$$

- For  $d_\tau$ , no changes due to  $d_e$  vs.  $d_e^{\text{equiv}}$  in ThO (and likely HfF) molecule due to  $1/m_\tau^3$  scaling [Ema, Gao, Pospelov 2022](#)
- Limit can be evaded by cancellation with other  $d_\tau$  source  
↔ need to check explicitly
- Projections for Belle II:
  - 50 ab<sup>-1</sup>, no polarization:  $d_\tau \simeq 10^{-19} e \text{ cm}$
  - With polarization:  $d_\tau \simeq 10^{-20} e \text{ cm}$ , **how?**





# What about the magnetic dipole moment?

## • Current status:

$$-0.052 < a_\tau < 0.013 \quad 95\% \text{ CL} \quad \text{DELPHI 2004}$$

$$-0.057 < a_\tau < 0.024 \quad 95\% \text{ CL} \quad \text{ATLAS 2023}$$

$$-0.088 < a_\tau < 0.056 \quad 68\% \text{ CL} \quad \text{CMS 2023}$$

## • Points of comparison:

- SM prediction [Keshavarzi et al. 2020](#):

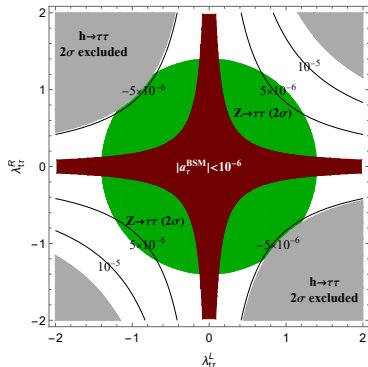
$$a_\tau^{\text{SM}} = 1,177.171(39) \times 10^{-6}$$

- Schwinger term:

$$a_\tau^{\text{1-loop QED}} = \frac{\alpha}{2\pi} = 1.16141 \dots \times 10^{-3}$$

- Electroweak contribution:  $a_\tau^{\text{EW}} \simeq 0.5 \times 10^{-6}$

- Concrete models:  $S_1$  leptoquark model promising due to **chiral enhancement** with  $\frac{m_t}{m_\tau}$   
 $\hookrightarrow$  can get  $a_\tau^{\text{BSM}} \simeq (\text{few}) \times 10^{-6}$  without violating  $h \rightarrow \tau\tau$  and  $Z \rightarrow \tau\tau$



Crivellin, MH, Roney 2021

## • Can one probe the interesting range at Belle II?

# Why do we care about tau dipole moments?

- **Interplay with electron and muon:**

- Already stringent limits on  $d_e$  from atomic systems
  - ↪ will further improve in the future
- Current limit on  $d_\mu < 1.8 \times 10^{-19} e \text{ cm}$  BNL 2009
  - ↪ will improve in the next years with new experiments Fermilab, J-PARC, PSI
- $a_e$  to be probed at  $10^{-13}$ , limited by tension in  $\alpha(\text{Cs})$  and  $\alpha(\text{Rb})$ 
  - ↪ improved atom interferometry experiments ongoing
- $a_\mu$  to be probed at  $10^{-10}$  Fermilab 2025, J-PARC 2028-, limited by tensions in HVP
  - ↪ theory effort ongoing to resolve this

- Comparing  $a_\ell, d_\ell$ , for all  $\ell = \{e, \mu, \tau\}$  reveals hints about **flavor structure**
  - ↪ scaling with lepton masses, complex phases, lepton flavor universality

- Rest of the talk: how would polarization at Belle II help in constraining  $d_\tau, a_\tau$ ?
  - ↪ look at cross section and asymmetries for **general  $\gamma^* \tau\tau$  vertex**

## First attempt: total cross section

Differential cross section for  $e^+e^- \rightarrow \tau^+\tau^-$  with general  $\gamma^*\tau\tau$  vertex

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2\beta}{4s} \left[ (2 - \beta^2 \sin^2 \theta) (|F_1|^2 - \gamma^2 |F_2|^2) + 4\text{Re}(F_1 F_2^*) + 2(1 + \gamma^2) |F_2|^2 + \beta^2 \gamma^2 \sin^2 \theta |F_3|^2 \right]$$

with scattering angle  $\theta$ ,  $\beta = \sqrt{1 - 4m_\tau^2/s}$ ,  $\gamma = \sqrt{s}/(2m_\tau)$

- Interference term  $4\text{Re}(F_1 F_2^*)$  in principle provides sensitivity to  $F_2(s)$
- Same EFT argument as for  $d_\tau$ :  $\text{Re} F_2(s) = \text{Re} F_2^{\text{SM}}(s) + a_\tau^{\text{BSM}}$  if  $M_{\text{BSM}}^2 \gg s$
- Could be determined by fit to  $\theta$  dependence
- But: need to measure total cross section at  $10^{-5}$  (at least)  
 $\hookrightarrow$  **can we use asymmetries instead?**
- Usual forward-backward asymmetry ( $z = \cos \theta$ )

$$\sigma_{\text{FB}} = 2\pi \left[ \int_0^1 dz \frac{d\sigma}{d\Omega} - \int_{-1}^0 dz \frac{d\sigma}{d\Omega} \right]$$

alone does not help

## Second attempt: $\tau$ polarization

- Idea: use **polarization information of the  $\tau^\pm$**

$\hookrightarrow$  semileptonic decays  $\tau^\pm \rightarrow h^\pm \nu_\tau^{(-)}$ ,  $h = \pi, \rho, a_1, \dots$

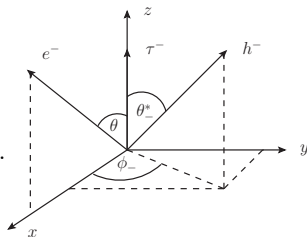
Bernabéu et al. 2007–2009

- Polarization characterized by

$$\mathbf{n}_\pm^* = \mp \alpha_\pm \begin{pmatrix} \sin \theta_\pm^* \cos \phi_\pm \\ \sin \theta_\pm^* \sin \phi_\pm \\ \cos \theta_\pm^* \end{pmatrix} \quad \alpha_\pm \equiv \begin{cases} 1 & h^\pm = \pi^\pm \\ \frac{m_\tau^2 - 2m_{h^\pm}^2}{m_\tau^2 + 2m_{h^\pm}^2} & h^\pm = \rho^\pm \\ 0.02 & h^\pm = a_1^\pm \end{cases}$$

$\hookrightarrow$  angles in  $\tau^\pm$  rest frame

- Can get additional information when separating L, T components of  $\rho, a_1$
- Construct asymmetries from **spin-dependent cross section**



## Second attempt: normal asymmetry

Spin-dependent cross section for  $e^+e^- \rightarrow \tau^+\tau^-$  with general  $\gamma^* \tau\tau$  vertex

$$\frac{d\sigma^S}{d\Omega} = \frac{\alpha^2\beta}{8s} \left[ (s_- - s_+)_x X_- + (s_- + s_+)_y Y_+ + (s_- - s_+)_z Z_- \right]$$

$$X_- = \beta\gamma \sin\theta \cos\theta \left[ \text{Im}(F_3 F_1^*) + \text{Im}(F_3 F_2^*) \right] \quad Z_- = -\beta \sin^2\theta \left[ \text{Im}(F_3 F_1^*) + \gamma^2 \text{Im}(F_3 F_2^*) \right]$$

$$Y_+ = \beta^2 \gamma \cos\theta \sin\theta \text{Im}(F_2 F_1^*)$$

### • Normal asymmetry

$$A_N^\pm = \frac{\sigma_L^\pm - \sigma_R^\pm}{\sigma_{\text{tot}}} = \pm \alpha_\pm \frac{\pi \alpha^2 \beta^3 \gamma}{3s\sigma_{\text{tot}}} \text{Im}(F_2 F_1^*) \quad \sigma_L^\pm = \int_\pi^{2\pi} d\phi_\pm \frac{d\sigma_{\text{FB}}}{d\phi_\pm} \quad \sigma_R^\pm = \int_0^\pi d\phi_\pm \frac{d\sigma_{\text{FB}}}{d\phi_\pm}$$

↪ only get access to  $\text{Im} F_2$

- Can also project out  $\text{Im} F_3$ , but neither one tests  $a_\tau$  or  $d_\tau$  (in the EFT sense above)

↪ need **electron polarization**

## Polarized cross section for $e^+e^- \rightarrow \tau^+\tau^-$ with general $\gamma^*\tau\tau$ vertex

$$\frac{d\sigma^{S\lambda}}{d\Omega} = \frac{\alpha^2\beta\lambda}{16s} \left[ (s_- + s_+)_x X_+ + (s_- - s_+)_y Y_- + (s_- + s_+)_z Z_+ \right]$$

$$X_+ = \frac{\sin\theta}{\gamma} \left[ |F_1|^2 + (1 + \gamma^2) \text{Re}(F_2 F_1^*) + \gamma^2 |F_2|^2 \right] \quad Z_+ = \cos\theta |F_1 + F_2|^2$$

$$Y_+ = -\beta\gamma \sin\theta \left[ \text{Re}(F_3 F_1^*) + \text{Re}(F_3 F_2^*) \right]$$

- Can now construct helicity difference

$$d\sigma_{\text{pol}}^S = \frac{1}{2} \left( d\sigma^{S\lambda} \Big|_{\lambda=1} - d\sigma^{S\lambda} \Big|_{\lambda=-1} \right)$$

- The normal asymmetry with  $d\sigma_{\text{FB}} \rightarrow d\sigma_{\text{pol}}^S$  in  $\sigma_L^\pm, \sigma_R^\pm$  gives

$$A_N^\pm = \frac{\sigma_L^\pm - \sigma_R^\pm}{\sigma_{\text{tot}}} = \alpha_\pm \frac{\pi^2 \alpha^2 \beta^2 \gamma}{4s\sigma_{\text{tot}}} \left[ \text{Re}(F_3 F_1^*) + \text{Re}(F_3 F_2^*) \right]$$

$\hookrightarrow$  provides access to  $d_\tau$ !

## Third attempt: electron polarization

- To isolate  $a_\tau$ , consider **transverse and longitudinal asymmetries** Bernabéu et al. 2007

$$A_T^\pm = \frac{\sigma_R^\pm - \sigma_L^\pm}{\sigma_{\text{tot}}} \quad A_L^\pm = \frac{\sigma_{\text{FB}, R}^\pm - \sigma_{\text{FB}, L}^\pm}{\sigma_{\text{tot}}}$$

defined via

$$\sigma_R^\pm = \int_{-\pi/2}^{\pi/2} d\phi_\pm \frac{d\sigma_{\text{pol}}^S}{d\phi_\pm} \quad \sigma_L^\pm = \int_{\pi/2}^{3\pi/2} d\phi_\pm \frac{d\sigma_{\text{pol}}^S}{d\phi_\pm} \quad \sigma_{\text{FB}, R}^\pm = \int_0^1 dz_\pm^* \frac{d\sigma_{\text{FB}, \text{pol}}^S}{dz_\pm^*} \quad \sigma_{\text{FB}, L}^\pm = \int_{-1}^0 dz_\pm^* \frac{d\sigma_{\text{FB}, \text{pol}}^S}{dz_\pm^*}$$

- Linear combination

$$A_T^\pm - \frac{\pi}{2\gamma} A_L^\pm = \mp \alpha_\pm \frac{\pi^2 \alpha^2 \beta^3 \gamma}{4s\sigma_{\text{tot}}} \left[ \text{Re}(F_2 F_1^*) + |F_2|^2 \right]$$

gives access to  $a_\tau$

# How to make use of this in practice?

Contributions to $\text{Re } F_2^{\text{eff}}(s) \times 10^6$	$s = 0$	$s = (10 \text{ GeV})^2$
1-loop QED	1161.41	-265.90
e loop	10.92	-2.43
$\mu$ loop	1.95	-0.34
2-loop QED (mass independent)	-0.42	-0.24
HVP	3.33	-0.33
EW	0.47	0.47
total	1177.66	-268.77

$$\text{Re } F_2^{\text{eff}}((10 \text{ GeV})^2) \simeq \mp \frac{0.73}{\alpha_{\pm}} (A_T^{\pm} - 0.56 A_L^{\pm})$$

## ● Strategy:

- Measure effective  $F_2(s)$

$$\text{Re } F_2^{\text{eff}} = \mp \frac{8(3 - \beta^2)}{3\pi\gamma\beta^2\alpha_{\pm}} (A_T^{\pm} - \frac{\pi}{2\gamma} A_L^{\pm}) \quad \sigma_{\text{tot}} \simeq \frac{2\pi\alpha^2\beta(3 - \beta^2)}{3s}$$

- Compare measurement to SM prediction for  $\text{Re } F_2^{\text{eff}}$ , difference gives constraint on  $a_T^{\text{BSM}}$
- A measurement of  $A_T^{\pm} - \frac{\pi}{2\gamma} A_L^{\pm}$  at  $\lesssim 1\%$  would already be competitive with current limits
- Detector systematics cancel in asymmetries

$\hookrightarrow$  polarization largest uncertainty, but  $\lesssim 0.5\% \times \text{Re } F_2^{\text{eff}}(s) \simeq 1 \times 10^{-6}$



# How to make use of this in practice?

## ● Challenges (experiment):

- Cancellation in  $A_T^\pm - \frac{\pi}{2\gamma} A_L^\pm$ :  $A_{T,L}^\pm = \mathcal{O}(1)$ , difference  $\mathcal{O}(\alpha)$   
↪ need  $m_\tau$  and  $M_{\Upsilon(1S)}$  at same level as target precision for  $a_\tau$
- With  $40 \text{ ab}^{-1}$  and 60% selection efficiency,  $10^{-5}$  for  $\text{Re } F_2^{\text{eff}}$  realistic  
↪ [Snowmass 2205.12847](#) also gives a formulation of  $\text{Re } F_2^{\text{eff}}$  in terms of count rates
- Beyond  $10^{-5}$ , need more statistics and  $m_\tau$ ,  $M_{\Upsilon(1S)}$

## ● Challenges (theory):

- Form factor only dominates for resonant  $\tau^+\tau^-$  pairs

$$|H(M_\Upsilon)|^2 = \left( \frac{3}{\alpha} \text{Br}(\Upsilon \rightarrow e^+e^-) \right)^2 \simeq 100$$

- However: continuum pairs dominate even at  $\Upsilon(nS)$ ,  $n = 1, 2, 3$ , due to energy spread
- Need to consider  $A_T^\pm$ ,  $A_L^\pm$  also for nonresonant  $\tau^+\tau^-$ , requires full calculation of  $e^+e^- \rightarrow \tau^+\tau^-$  including box diagrams
- Ultimately, need two-loop accuracy

- Next slides: first results for implementation in MC integrator MCMULE

# What is MCMULE?

## MCMULE

Fixed-order NNLO QED framework Monte Carlo for MUons and other LEptons

- Provided: matrix elements by MCMULE or others
- Output: **physical cross section** for any physical observable
- MCMULE: phase space generation, subtraction, stabilization, integration, event generation, etc.
- All leptonic  $2 \rightarrow 2$  processes in QED at NNLO (+ a few others)
- Stable public version is an integrator
- Generator on development branch

Get the code here: <https://mule-tools.gitlab.io>

Read the docs here: <https://mcmule.readthedocs.io>

Further reading: [1811.06461](#), [1909.10244](#), [2007.01654](#), [2112.07570](#), [2212.06481](#)

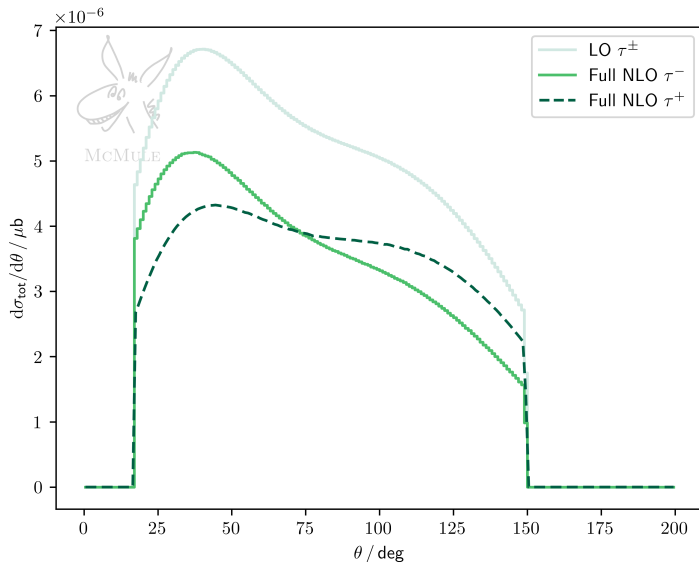


MCMULE

# Processes in McMULE

Process	Experiment	Physics motivation	Order
$e\mu \rightarrow e\mu$	MUonE	HVP to $(g - 2)_\mu$	NNLO+
$\ell p \rightarrow \ell p$	P2, MUSE, PRad, QWeak, ...	proton radius and weak charge	NNLO
$eN \rightarrow eN$	PRad, ULQ2	background	NNLO-
$e^- e^- \rightarrow e^- e^-$	PRad 2	normalization	NNLO
	MOLLER, ...	$\sin^2 \theta_W$ at low $Q^2$	
$e^+ e^- \rightarrow e^+ e^-$	any $e^+ e^-$ collider	luminosity measurement	NNLO
$ee \rightarrow \ell\ell$	VEPP, BES, DAΦNE, ...	$R$ -ratio	NNLO+
	<b>Belle II</b>	<b><math>\tau</math> properties</b>	
$ee \rightarrow \gamma\gamma$	DAΦNE	dark searches	NNLO-
	any $e^+ e^-$ collider	luminosity measurement	
$e\nu \rightarrow e\nu$	DUNE	flux & $\sin^2 \theta_W$	NNLO-
$\mu \rightarrow \nu\bar{\nu}e$	MEG	ALP searches	NNLO+
	DUNE	beam-line profiling	
$\mu \rightarrow \nu\bar{\nu}e\gamma$	MEG, Mu3e, PIONEER	background	NLO
$\mu \rightarrow \nu\bar{\nu}eee$	MEG, Mu3e	background	NLO
$ee \rightarrow \pi\pi$	VEPP, BES, DAΦNE, ...	$R$ -ratio	NLO+
$ee \rightarrow \ell\ell\gamma$	VEPP, BES, DAΦNE, ...	$R$ -ratio	NLO+

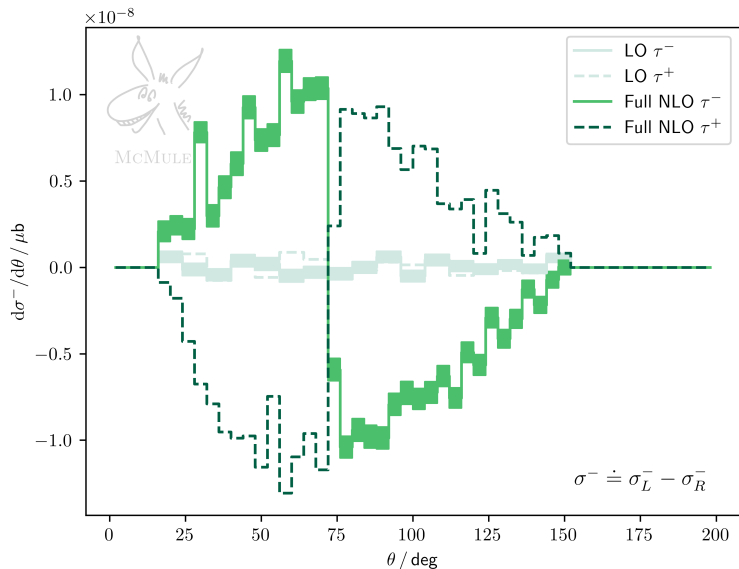
# Some first results for $e^+e^- \rightarrow \tau^+\tau^-$ (w/o polarization): $\sigma_{\text{tot}}$



Cuts (lab frame):

- Scattering angle  
 $\theta \in [17^\circ, 150^\circ]$
- Photon energy  
 $E < 50 \text{ MeV}$

# Some first results for $e^+e^- \rightarrow \tau^+\tau^-$ (w/o polarization): $\sigma_L - \sigma_R$



# McMULE: getting started

McMule

Search docs

CONTENTS:

- Getting started
- Structure of McMule
- General aspects of using McMule
- Technical aspects of McMule
- Implementing new processes in McMule
- The FKS<sup>2</sup> scheme
- Glossary
- Bibliography
- Particle ID
- Available processes and which piece
- Fortran reference guide
- pymule user guide
- pymule reference guide

McMule

View page source

## McMule

Yannick Ulrich <sup>1</sup>, Pulak Banerjee <sup>2</sup>, Antonio Coutinho <sup>3</sup>, Tim Engel <sup>4</sup>, Andrea Gurgone <sup>5</sup>  
<sup>6</sup>, Franziska Hagelstein <sup>7,8</sup>, Sophie Kollatzsch <sup>8,9</sup>, Luca Naterop <sup>8,9</sup>, Marco Rocco <sup>8</sup>,  
Nicolas Schalch <sup>1</sup>, Vladyslava Sharkovska <sup>8,9</sup>, Adrian Signer <sup>8,9</sup>

- [1,2] Albert Einstein Center for Fundamental Physics, Universität Bern, CH-3012 Bern, Switzerland
- [2] Department of Physics, Indian Institute of Technology Guwahati, Guwahati-781039, Assam, India
- [3] IFIC, Universitat de València - CSIC, Parc Científic, Catedrático José Beltrán, 2, E-46100 Paterna, Spain
- [4] Albert-Ludwigs-Universität Freiburg, Physikalisches Institut, Hermann-Herder-Straße 3, D-79104 Freiburg, Germany
- [5] Dipartimento di Fisica, Università di Pavia, I-27100 Pavia, Italy
- [6] INFN, Sezione di Pavia, I-27100 Pavia, Italy
- [7] Institut für Kernphysik & PRISMA\* Cluster of Excellence, Johannes Gutenberg Universität Mainz, D-55099 Mainz, Germany
- [8] [1,2,3,4,5] Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland
- [9] [1,2,3,4] Physik-Institut, Universität Zürich, Winterthurerstrasse 190, CH-8057 Zürich, Switzerland

### Contents:

- Getting started
  - Obtaining the code
  - Simple runs at LO
  - Running at NLO and beyond
  - More complicated runs
- Structure of McMule
  - Modular structure of the code
  - What happens when running

- McMULE manual at <https://mule-tools.gitlab.io/manual/>
- For general questions contact Yannick Ulrich [yannick.ulrich@liverpool.ac.uk](mailto:yannick.ulrich@liverpool.ac.uk)
- For  $e^+e^- \rightarrow \tau^+\tau^-$  contact Joël Gogniat [gogniat@itp.unibe.ch](mailto:gogniat@itp.unibe.ch)

## ● Exciting physics program at **Chiral Belle**

- Unprecedented precision for neutral-current vector couplings:  $\sin^2 \theta_W$ , **universality**
- Highly complementary to low- and high-energy probes of parity violation
- Improved precision of  $\tau$  Michel parameters
- Improved sensitivity to  $\tau \rightarrow \mu\gamma, \tau \rightarrow e\gamma$

## ● **Dipole moments of the $\tau$**

- EDM: could probe  $d_\tau \simeq 10^{-20} e\text{cm}$
- $(g-2)_\tau$ : could probe  $a_\tau^{\text{BSM}} \simeq 10^{-5}$  (assuming current projections for statistics and  $m_\tau, M_{\Upsilon(1S)}$ )
- Program for  $a_\tau$  requires theory development up to two-loop level, being implemented into MCMULE
- Important especially in view of ongoing developments for  $\ell = \{e, \mu\}$

