



Hot Topic in Flavour at the B Factories

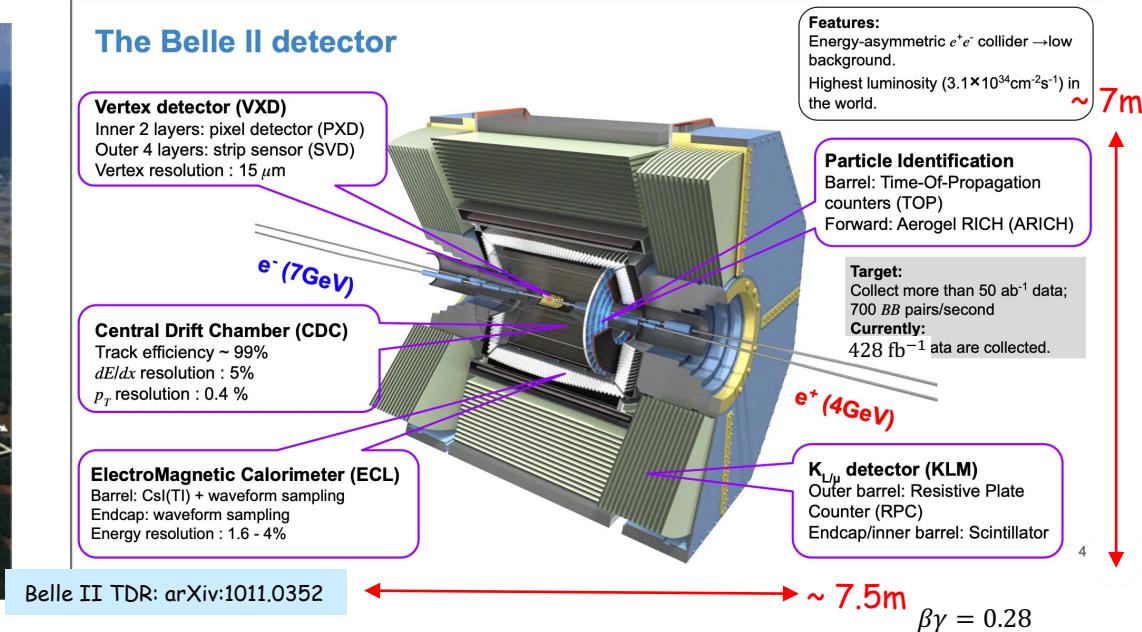
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On behalf of the Belle and Belle II Collaborations,
9th Workshop on Theory, Phenomenology and Experiments in Flavor Physics
June 19-21, 2024, Anacapri, Capri Island, Italy



Belle and Belle II experiments



The Belle II detector



- Asymmetric $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ with production cross section $\sim 1.1\text{ nb}$
 - ✓ Belle → Belle II: $e^+(3.5\text{ GeV})e^-(8\text{ GeV}) \rightarrow e^+(4\text{ GeV})e^-(7\text{ GeV})$
 - ✓ Belle II has smaller boost but improved vertex resolution
- Belle (1999-2010): 1.4 ab^{-1} with 711 fb^{-1} at $\Upsilon(4S)$, $\mathcal{L}_{peak} = 2.1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Belle II collected 428 fb^{-1} data for Run 1 with record $\mathcal{L}_{peak} = 4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
 - ✓ Restart data taking in 2024, Final goal: 50 ab^{-1} data at $\mathcal{L}_{peak} = 6.5 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$
- Belle/BelleII: Knowledge of initial state: kinematic constraints for signal reconstruction

$$\Delta E = E_B^* - \sqrt{s}/2 \quad M_{bc} = \sqrt{(\sqrt{s}/2)^2 - |\vec{p}_B^*|^2}$$

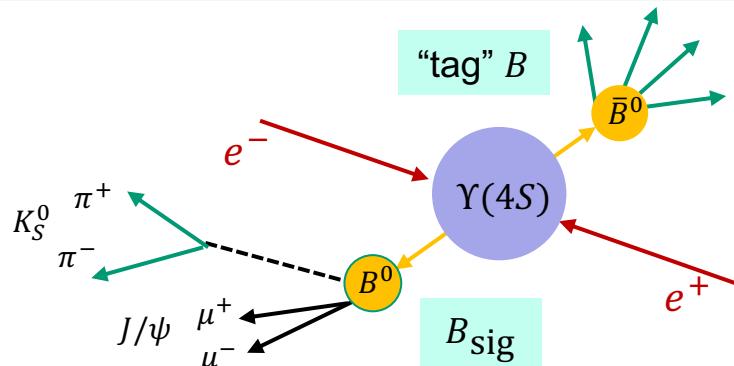
Outline of the talk

- This is not a review talk
 - ✓ Some selected recent results from Belle/Belle II
 - ✓ Focus on results sensitive to New Physics (NP)
 - ✓ Focus on measurements most sensitive at B factory
- Topics:
 - ✓ Measurements of CP Violation (CPV) in B decays
 - ✓ Rare B decays in the EWP final states
 - ✓ Rare and forbidden Charm meson decays
 - ✓ Rare and forbidden Tau decays
 - ✓ No Dark Sector: see the talk by Marita Laurenza
- Comparison to previous results and **outlook in the future**

B Flavor tagging at Belle II



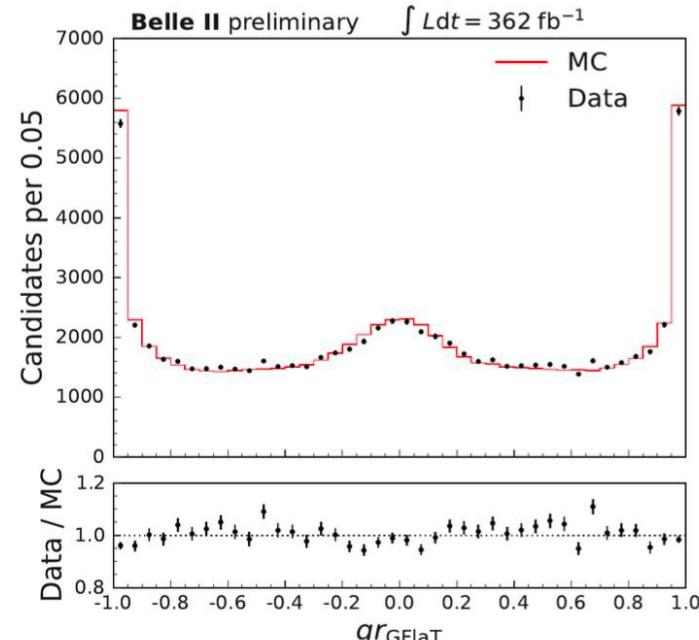
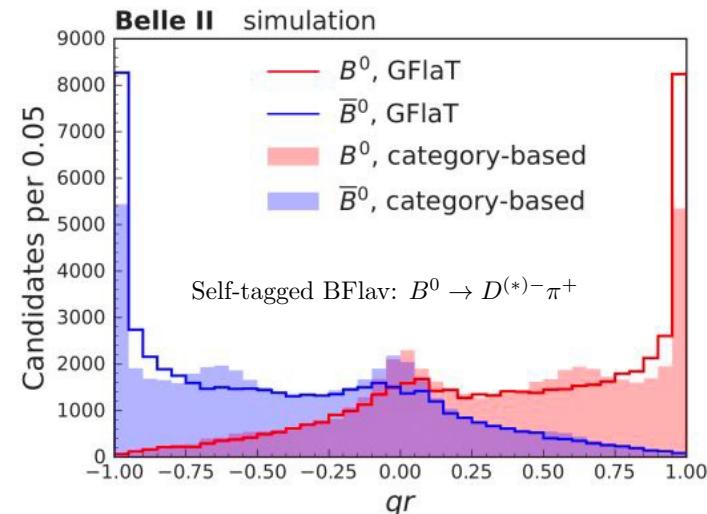
- B flavor tagging: Identify the flavor of the other B



- Belle II initial B tagging algorithm:
 - ✓ Category-based (CB): physics object as BDT input
 - ✓ Similar to Belle & Babar experiments
- Newly developed B tagging algorithm: GFlat
 - ✓ Graph convolutional neural network (GNN)
 - ✓ 25 variables for each track as GNN input
 - ✓ 18% improvement in performance

$$\epsilon_{\text{tag}}(\text{CB}) = (31.7 \pm 0.5 \pm 0.4)\%$$

$$\epsilon_{\text{tag}}(\text{GFlat}) = (37.4 \pm 0.4 \pm 0.3)\%$$

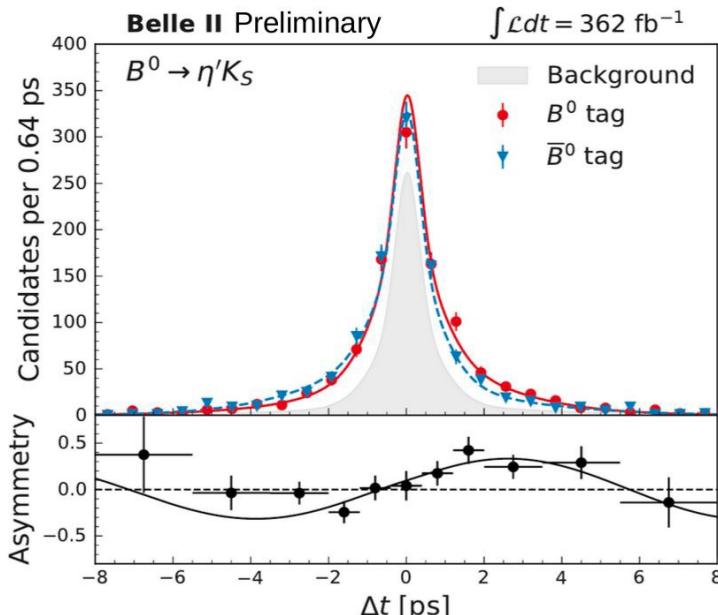


CPV in Penguin dominated B decays

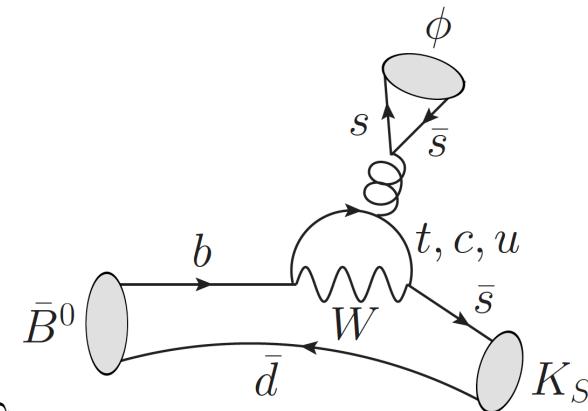


NP may induce a large discrepancy between the CP Asymmetry in $b \rightarrow c\bar{c}s$ and $b \rightarrow q\bar{q}s$, ($q = u, d, s$) transitions, such as $\eta' K_S^0$, ϕK_S^0 , $K_S^0 \pi^0$, $K_S^0 K_S^0 K_S^0$

$B^0 \rightarrow \eta' K_S^0$ with $\eta' \rightarrow \eta(\rightarrow \gamma\gamma, 3\pi)\pi^+\pi^-$ or $\eta' \rightarrow \rho\gamma$



arXiv:2402.03713, Accepted by PRD



- Large \mathcal{B} , and theoretically clean
- Signa yield: 829 ± 35
- Still use the old Belle II CB tagging:

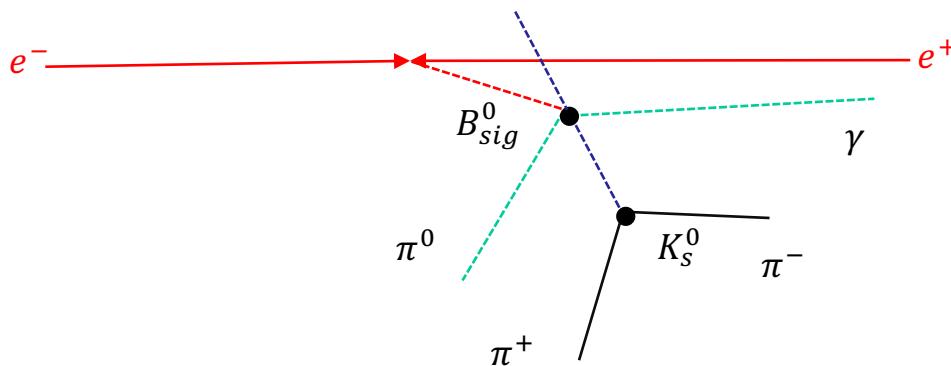
$$C_{\eta' K_S^0} = -0.19 \pm 0.08 \pm 0.03$$

$$S_{\eta' K_S^0} = +0.67 \pm 0.10 \pm 0.04$$
- Consistent with Belle measurement: 711 fb^{-1}
 - ✓ Use More final states ($K_S^0 \rightarrow \pi^0\pi^0$, K_L)
 - ✓ $\sigma_S = 0.07$
- Belle II expect ~10% improvement of σ_S for same data statistics using GFlaT

CPV in $B^0 \rightarrow K_S^0 \pi^0 \gamma$



- Amplitude dominated by electro-weak penguin loop
- Expect very small mixed-induced CPV in the Standard Model (SM)
 - ✓ $b \rightarrow s\gamma_R$ is helicity suppressed by (m_s/m_b) w.r.t. $b \rightarrow s\gamma_L$
 - ✓ $B^0 \rightarrow K_S^0 \pi^0 \gamma_L$ vs. $B^0 \rightarrow \bar{B}^0 \rightarrow K_S^0 \pi^0 \gamma_R$
- Measurements for resonance ($K^{*0} \rightarrow K_S^0 \pi^0$) and non-resonance final states
- Vertex with beamspot constraints
 - ✓ Better vertexing of K_S^0 reconstruction at Belle II



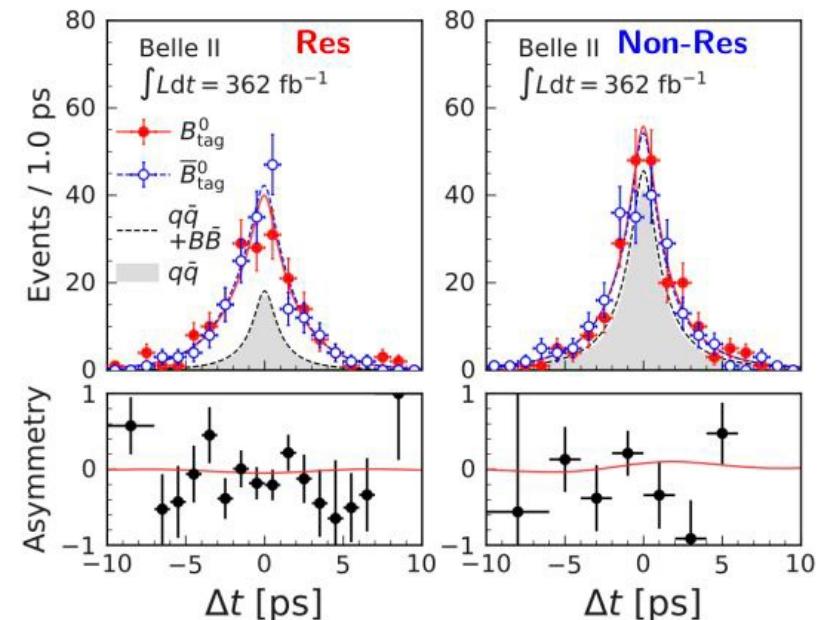
$$C_{\text{Res}} = 0.10 \pm 0.13 \pm 0.03$$

$$S_{\text{Res}} = 0.00^{+0.27}_{-0.26} {}^{+0.03}_{-0.04}$$

$$C_{\text{Non-Res}} = -0.06 \pm 0.25 \pm 0.07$$

$$S_{\text{Non-Res}} = 0.04^{+0.45}_{-0.44} \pm 0.10$$

Most precise measurements
Use CB tagging
Belle (499 fb^{-1})
BaBar (436 fb^{-1})



To be submitted to PRL

Direct CPV in $B^0 \rightarrow \pi^0\pi^0$



- Update early Belle II measurement (189 fb^{-1}) of \mathcal{B} and A_{CP}
- Improved selections, new flavour tagger (GFlaT), reduction of systemic uncertainties
 - Background dominated by continuum, then $B^+ \rightarrow \rho^+(\pi^+\pi^0)\pi^0$, $B^0 \rightarrow K_S^0(\pi^0\pi^0)\pi^0$
 - BDT photon selector, continuum suppression trained using off-resonance data
 - 4-D fit: m_{bc} , ΔE , continuum suppression BDT output, wrong B-tag probability

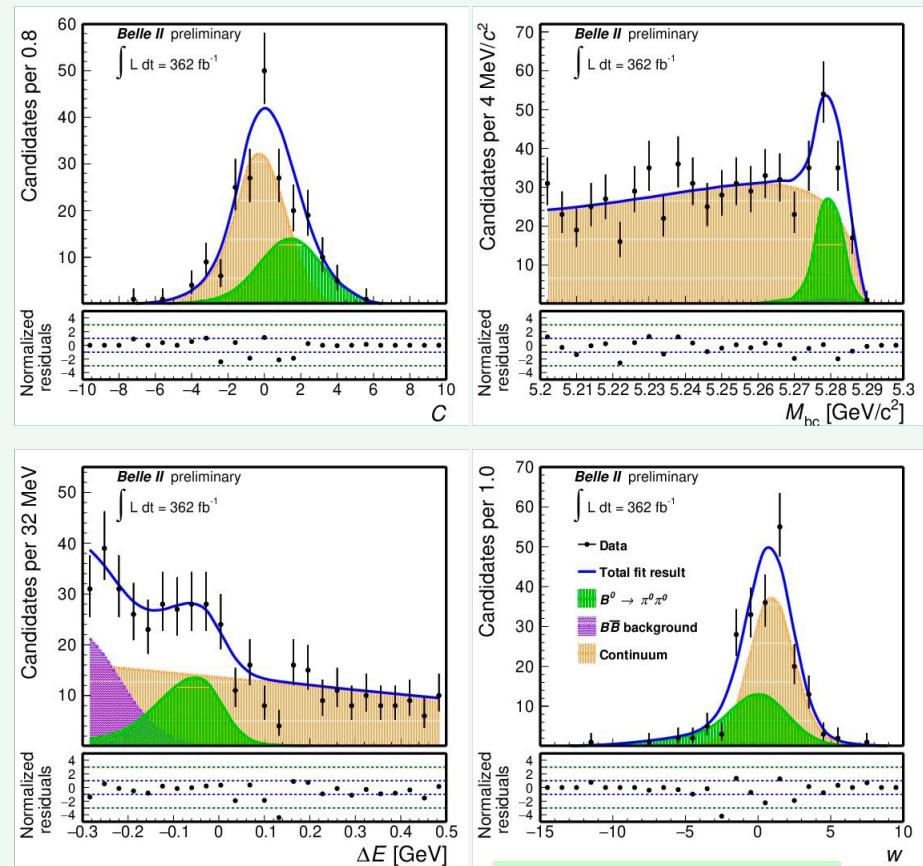
$$\mathcal{B} = (1.26 \pm 0.20 \pm 0.11)^{-6}$$

$$A_{CP} = 0.06 \pm 0.30 \pm 0.06$$

- Compatible with previous results
- World-best branching fraction
- Compatible Direct CP precision
 - ✓ Belle (499 fb^{-1}) & BaBar (436 fb^{-1})
 - ✓ World average

$$\mathcal{B} = (1.59 \pm 0.26)^{-6}$$

$$A_{CP} = 0.30 \pm 0.20$$



To be submitted to PRD

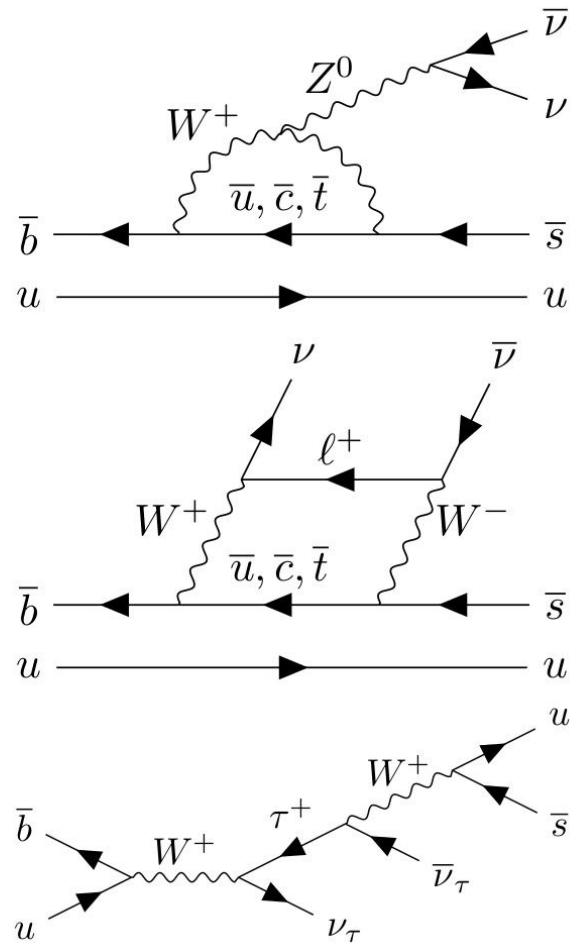
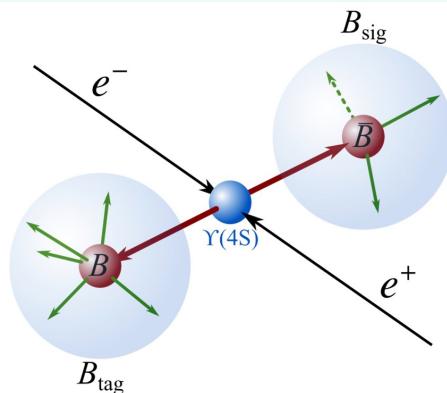
Electroweak Penguin dominated B decays



- NP may contribute in the EWP loops
 - ✓ $b \rightarrow sl^+l^-$, $b \rightarrow sv\bar{v}$, and $b \rightarrow sy$ transitions
- Some measurements have tension with SM
 - ✓ Branching fraction and angular observables
- Search for $B^+ \rightarrow K^+\nu\bar{\nu}$ at Belle II
 - ✓ Theoretically clean (no photon exchange)
 - ✓ Experimentally challenging: two neutrinos in the final state, high background and small branching fraction

$\mathcal{B}_{\text{SM}} = (5.58 \pm 0.37) \times 10^{-6}$

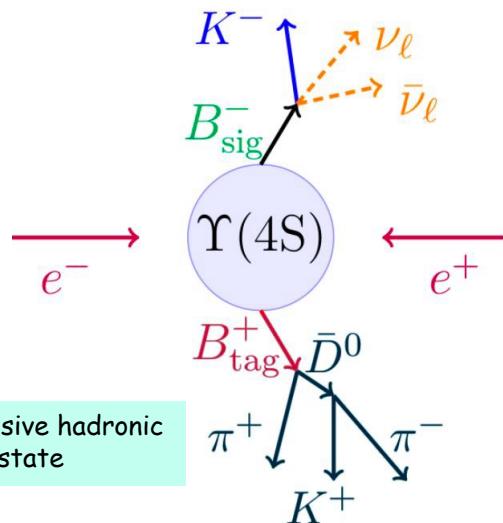
 - ✓ Only accessible at B-factories (constraint using well-known initial kinematics)



Search for $B^+ \rightarrow K^+ \nu \bar{\nu}$



Two parallel reconstructions



Hadronic Tag Analysis (HTA):

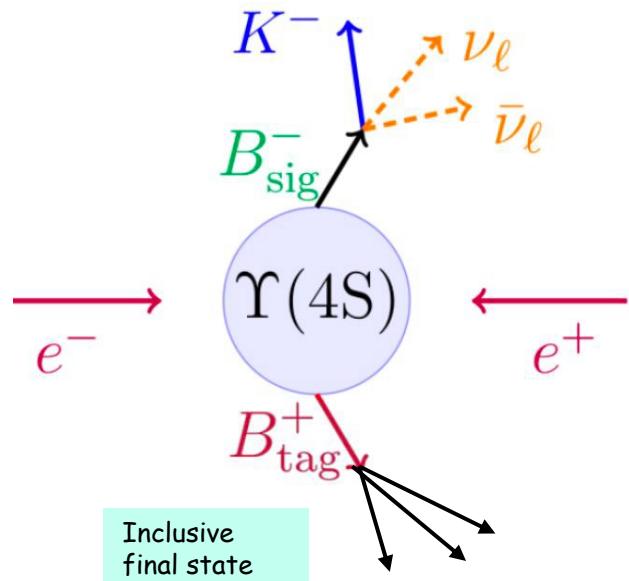
- Fully reconstruct “tag” B:
 - ✓ Better measurement of B_{sig} Kinematic variables
- Full-Event-Interpretation (FEI) at Belle II
 - ✓ Multivariate classification using BDT
 - ✓ 50% tag efficiency improvement vs Belle
- Small efficiency but significantly reduce bg
 - ✓ Signal eff = 0.4%, purity = 3.5%
- Extract signal via a BDT output

Comput. Softw. Big Sci. 3, 6 (2019)

Inclusive Tag Analysis (ITA):

- Non exclusive reconstruction of “tag” B:
- Select signal kaon that minimize

$$q_{\text{rec}}^2 = s/(4c^4) + m_K^2 - \sqrt{s}E_K^*/c^4$$
- Larger efficiency but significantly more bg
 - ✓ Signal eff = 8%, purity = 0.9%
- Extract signal using BDT output and q_{rec}^2



Search for $B^+ \rightarrow K^+ \nu \bar{\nu}$



Data driven approach with many validations

- Signal efficiency check using $B \rightarrow J/\psi(\mu\mu)K$
 - ✓ Remove J/ψ and correct kaon kinematics to match signal distributions



- Continuum validation with off-resonance data
- $B \rightarrow X_c (\rightarrow K_L^0)$ validate from pion enriched sideband
- Signal like $B \rightarrow K^+ K_L^0 K_L^0$ check with $B \rightarrow K^+ K_S^0 K_S^0$
- Similar validation for $B \rightarrow K^+ K_S^0 K_L^0$ and $B \rightarrow K^+ nn$
- Validate method to measure $B \rightarrow K^0 \pi^+$
 - ✓ $\mathcal{B} = (2.5 \pm 0.5) \times 10^{-5}$
 - ✓ Consistent with PDG: $(2.38 \pm 0.08) \times 10^{-5}$

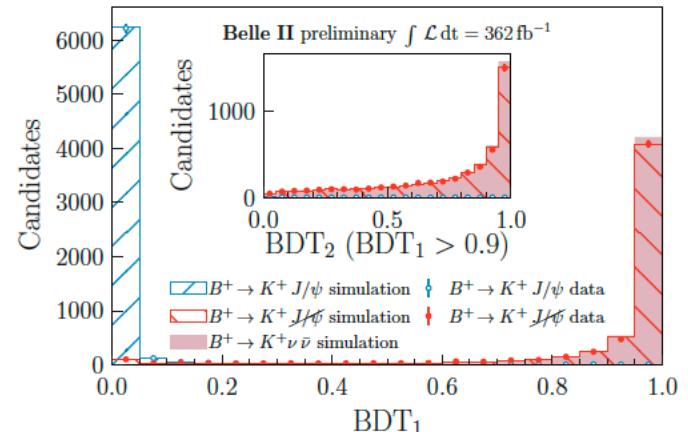
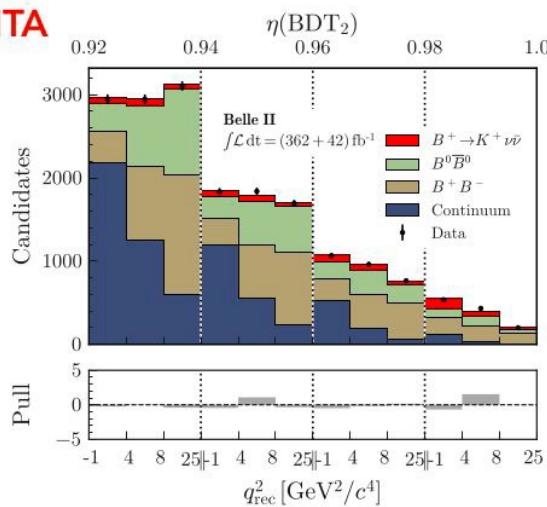


FIG. 7. Distribution of the classifier output BDT_1 (main figure) and BDT_2 for $BDT_1 > 0.9$ (inset). The distributions are shown before ($B^+ \rightarrow K^+ J/\psi$) and after ($B^+ \rightarrow K^+ J/\psi$) the muon removal and replacement of the kaon momentum of selected $B^+ \rightarrow K^+ J/\psi$ events in simulation and data. As a reference, the classifier outputs directly obtained from simulated $B^+ \rightarrow K^+ \nu \bar{\nu}$ signal events are overlaid. The simulation histograms are scaled to the total number of $B^+ \rightarrow K^+ J/\psi$ events selected in the data.

Results of $B^+ \rightarrow K^+\nu\bar{\nu}$



ITA



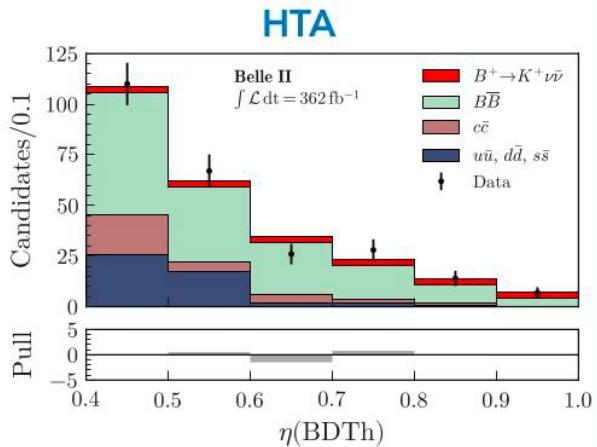
$$\mu = 5.4 \pm 1.0(\text{stat}) \pm 1.1(\text{syst})$$

corresponding to

$$\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu}) = 2.7 \pm 0.5(\text{stat}) \pm 0.5(\text{syst}) \times 10^{-5}$$

- **3.5 σ** compatibility wrt bkg only
- **2.9 σ** compatibility wrt to the SM

HTA



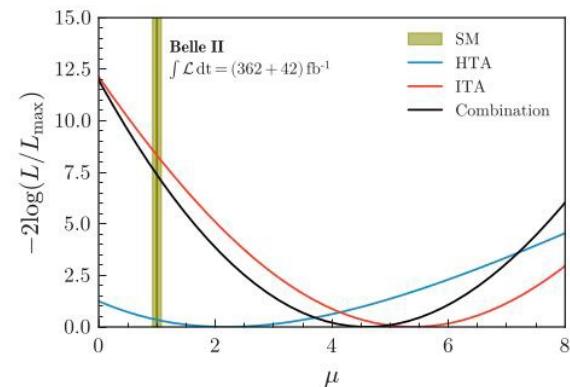
$$\mu = 2.2^{+1.8}_{-1.7}(\text{stat})^{+1.6}_{-1.1}(\text{syst})$$

corresponding to

$$\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu}) = [1.1^{+0.9}_{-0.8}(\text{stat})^{+0.8}_{-0.5}(\text{syst})] \times 10^{-5}$$

- **1.1 σ** compatibility wrt bkg only
- **0.6 σ** compatibility wrt to the SM

Combination



$$\mu = 4.6 \pm 1.0(\text{stat}) \pm 0.9(\text{syst})$$

corresponding to

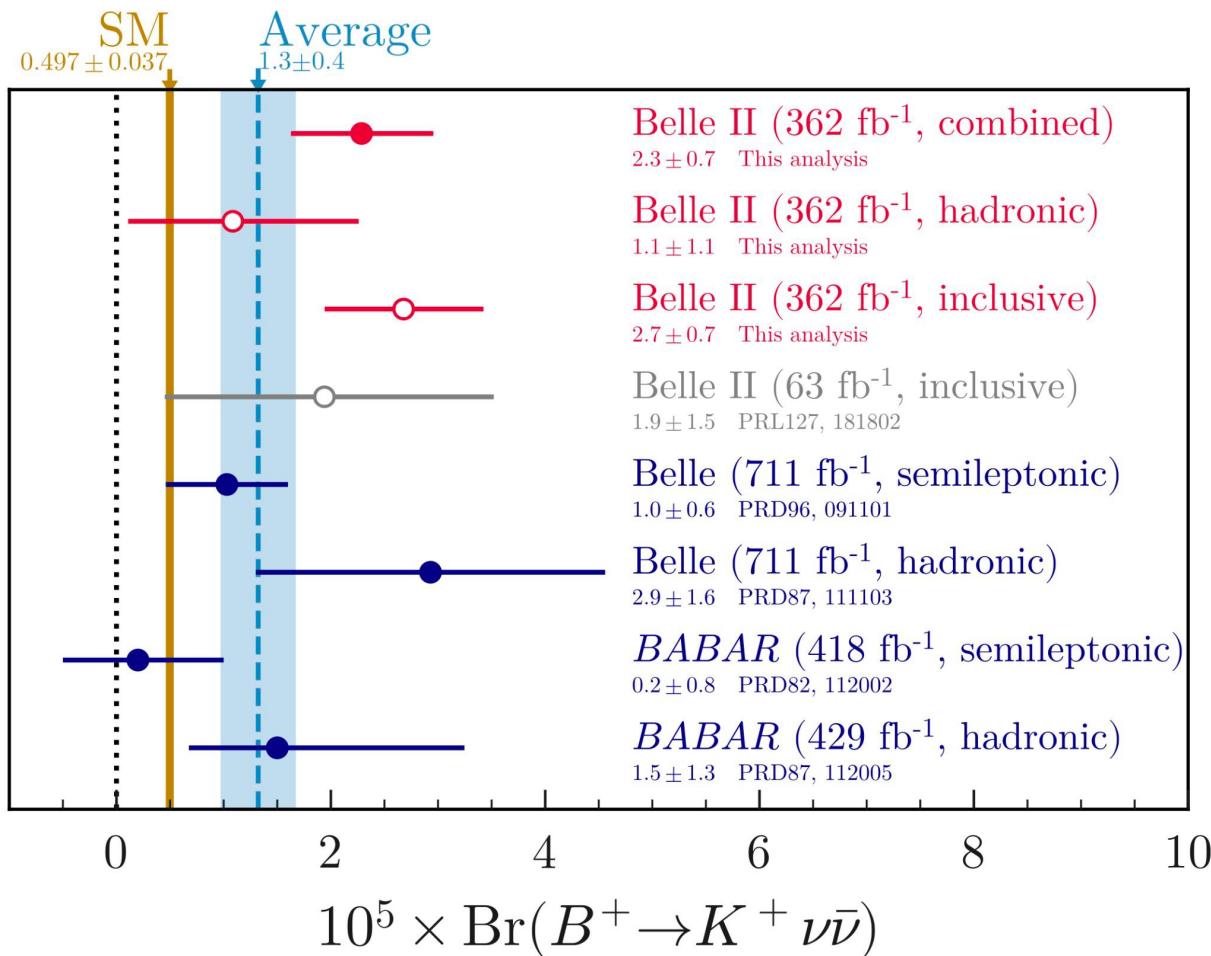
$$\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu}) = [2.3 \pm 0.5(\text{stat})^{+0.5}_{-0.4}(\text{syst})] \times 10^{-5}$$

- Combination improves the ITA-only precision by 10%
- **3.5 σ** significance wrt bkg
- **2.7 σ** significance wrt SM

arXiv:2311.14647, Accepted by PRD

- First evidence of $B^+ \rightarrow K^+\nu\bar{\nu}$ (3.5σ), branching fraction in excess of SM 2.7σ
- Measurement enabled by new inclusive techniques

Results of $B^+ \rightarrow K^+ \nu\bar{\nu}$



Other $B \rightarrow K\nu\bar{\nu}$ analysis ongoing at Belle II
Expect some results soon

Measurements of $B \rightarrow K^*(892)\gamma$



Large branching fraction and clean experimental signal

$$\mathcal{B} = \frac{N_{\overline{B}}/\epsilon_{\overline{B}} + N_B/\epsilon_B}{2 \times N_{B\overline{B}} \times f^{+-}(f^{00})}, \quad \Delta_{0+} = \frac{(\tau_+/\tau_0) \times \mathcal{B}(B^0 \rightarrow K^{*0}\gamma) - \mathcal{B}(B^+ \rightarrow K^{*+}\gamma)}{(\tau_+/\tau_0) \times \mathcal{B}(B^0 \rightarrow K^{*0}\gamma) + \mathcal{B}(B^+ \rightarrow K^{*+}\gamma)},$$

$$\mathcal{A}_{CP} = \frac{N_{\overline{B}}/\epsilon_{\overline{B}} - N_B/\epsilon_B}{N_{\overline{B}}/\epsilon_{\overline{B}} + N_B/\epsilon_B}, \quad \Delta\mathcal{A}_{CP} = \mathcal{A}_{CP}(B^+ \rightarrow K^{*+}\gamma) - \mathcal{A}_{CP}(B^0 \rightarrow K^{*0}\gamma),$$

Belle II Results: 362 fb^{-1}

$$\mathcal{B}[B^0 \rightarrow K^{*0}\gamma] = (4.16 \pm 0.10 \pm 0.11) \times 10^{-5},$$

$$\mathcal{B}[B^+ \rightarrow K^{*+}\gamma] = (4.04 \pm 0.13 \pm 0.13) \times 10^{-5},$$

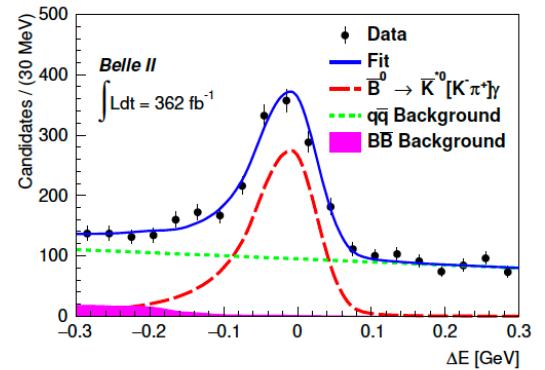
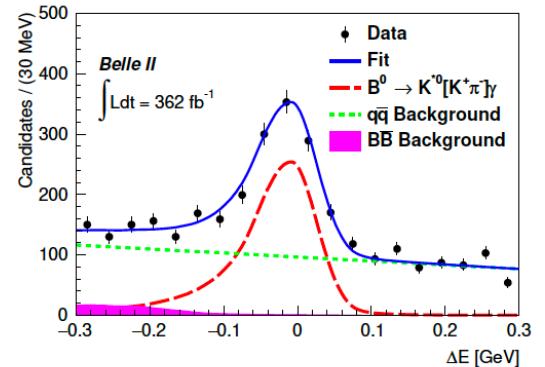
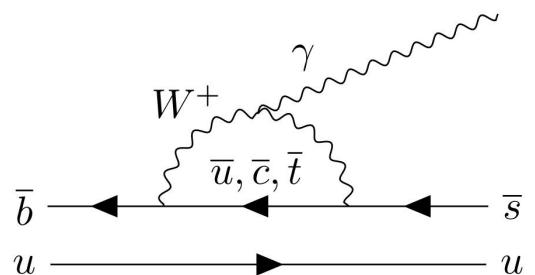
$$\mathcal{A}_{CP}[B^0 \rightarrow K^{*0}\gamma] = (-3.2 \pm 2.4 \pm 0.4)\%,$$

$$\mathcal{A}_{CP}[B^+ \rightarrow K^{*+}\gamma] = (-1.0 \pm 3.0 \pm 0.6)\%,$$

$$\begin{aligned} \Delta A_{CP} &= (2.2 \pm 3.8 \pm 0.7)\% \\ \Delta_{0+} &= (5.1 \pm 2.0 \pm 1.0 \pm 1.1)\% \end{aligned}$$

Stat Syst f^{+-}/f^{00}

Consistent with the world average and the SM expectation
Systematic uncertainties can be reduced with more data



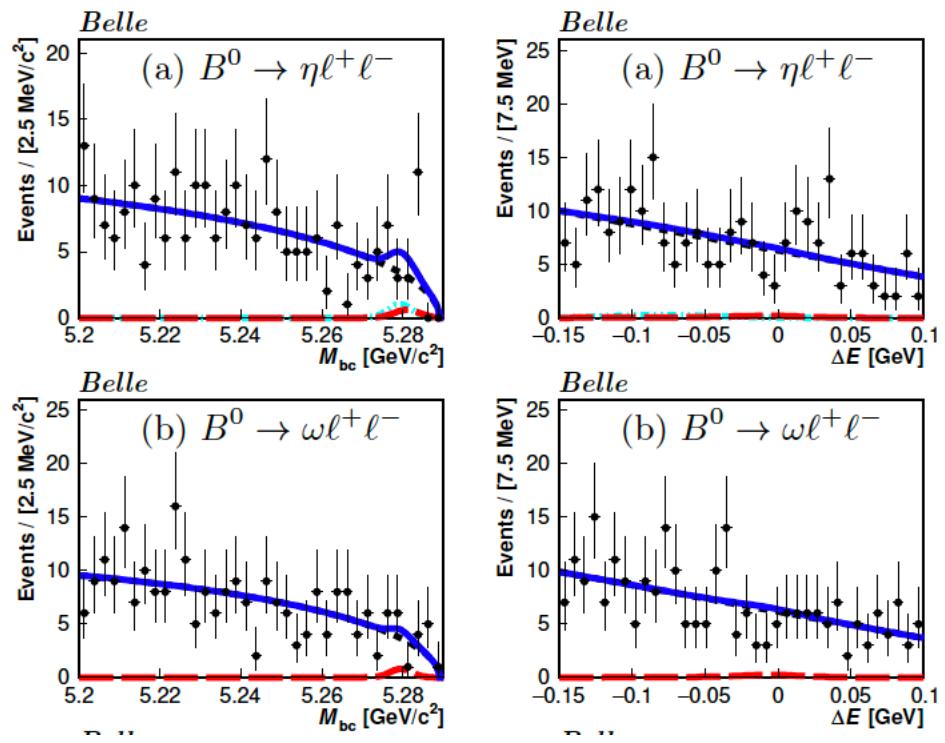
To be submitted to JHEP

Search for rare $b \rightarrow dl^+l^-$ transition



- $b \rightarrow dl^+l^-$ process via loops and highly suppressed, $\mathcal{B}_{SM} \sim O(10^{-8})$
 - ✓ LHCb (3 fb^{-1}) observed final state with π^\pm in dimuon mode
- Sensitive to NP contribution in the loop
 - ✓ Rate measurement, Lepton flavor universality

	$\mathcal{B}^{\text{UL}} (10^{-8})$	$\mathcal{B} (10^{-8})$
$B^0 \rightarrow \eta e^+e^-$	< 10.5	$0.0^{+4.9}_{-3.4} \pm 0.1$
$B^0 \rightarrow \eta\mu^+\mu^-$	< 9.4	$1.9^{+3.4}_{-2.5} \pm 0.2$
$B^0 \rightarrow \eta l^+l^-$	< 4.8	$1.3^{+2.8}_{-2.2} \pm 0.1$
$B^0 \rightarrow \omega e^+e^-$	< 30.7	$-2.1^{+26.5}_{-20.8} \pm 0.2$
$B^0 \rightarrow \omega\mu^+\mu^-$	< 24.9	$7.7^{+10.8}_{-7.5} \pm 0.6$
$B^0 \rightarrow \omega l^+l^-$	< 22.0	$6.4^{+10.7}_{-7.8} \pm 0.5$
$B^0 \rightarrow \pi^0 e^+e^-$	< 7.9	$-5.8^{+3.6}_{-2.8} \pm 0.5$
$B^0 \rightarrow \pi^0 \mu^+\mu^-$	< 5.9	$-0.4^{+3.5}_{-2.6} \pm 0.1$
$B^0 \rightarrow \pi^0 l^+l^-$	< 3.8	$-2.3^{+2.1}_{-1.5} \pm 0.2$
$B^+ \rightarrow \pi^+ e^+e^-$	< 5.4	$0.1^{+2.7}_{-1.8} \pm 0.1$
$B^0 \rightarrow \rho^0 e^+e^-$	< 45.5	$23.6^{+14.6}_{-11.2} \pm 1.1$
$B^+ \rightarrow \rho^+ e^+e^-$	< 46.7	$-38.2^{+24.5}_{-17.2} \pm 3.4$
$B^+ \rightarrow \rho^+ \mu^+\mu^-$	< 38.1	$13.0^{+17.5}_{-13.3} \pm 1.1$
$B^+ \rightarrow \rho^+ l^+l^-$	< 18.9	$2.5^{+14.6}_{-11.8} \pm 0.2$



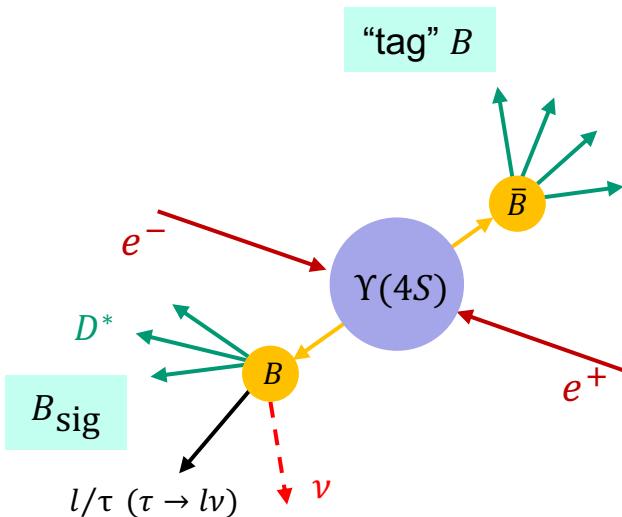
Belle (711 fb^{-1})

World best limits in all channels. First search for ωl^+l^- , $\rho^0 e^+e^-$, $\rho^\pm l^+l^-$ modes

Measurements of R_{D^*} and R_D

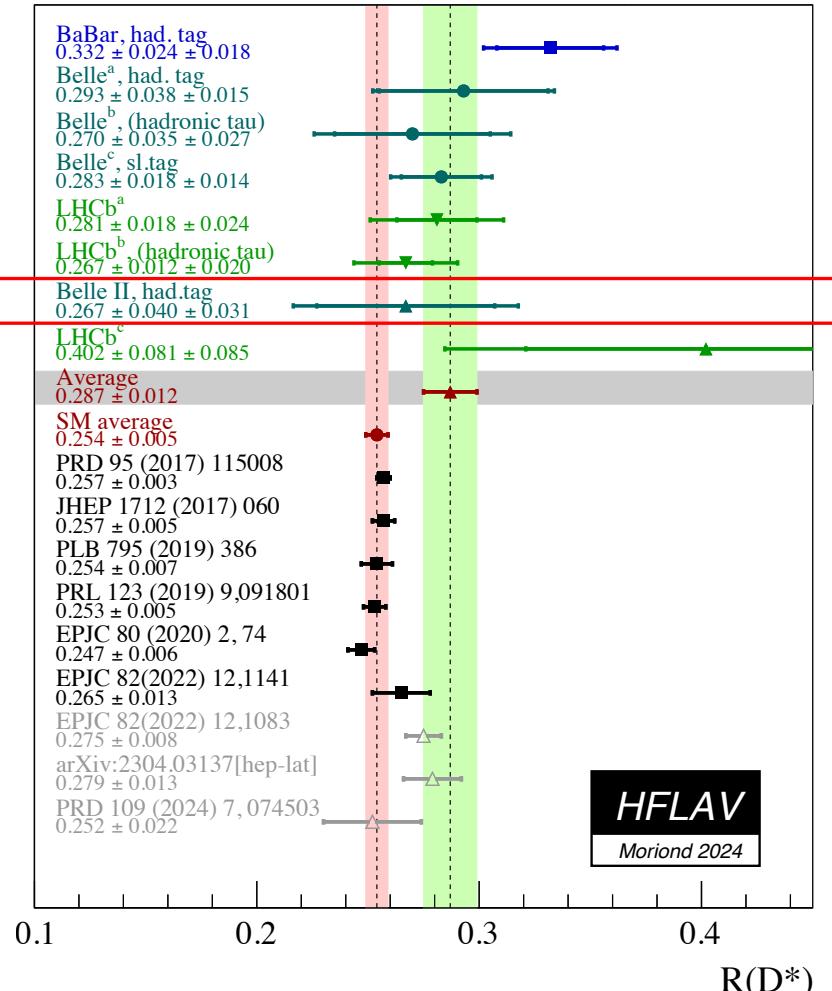
$$R_{D^*} = \frac{\mathcal{B}(B \rightarrow D^* \tau \nu)}{\mathcal{B}(B \rightarrow D^* l \nu)} \quad R_D = \frac{\mathcal{B}(B \rightarrow D \tau \nu)}{\mathcal{B}(B \rightarrow D l \nu)}$$

- Uncertainty from form factor and V_{cb} drop out
 - ✓ Small uncertainty for the SM prediction
- Ratios test lepton universality
 - ✓ NP change rate, angular and q^2 distributions
- Measurements above the SM prediction



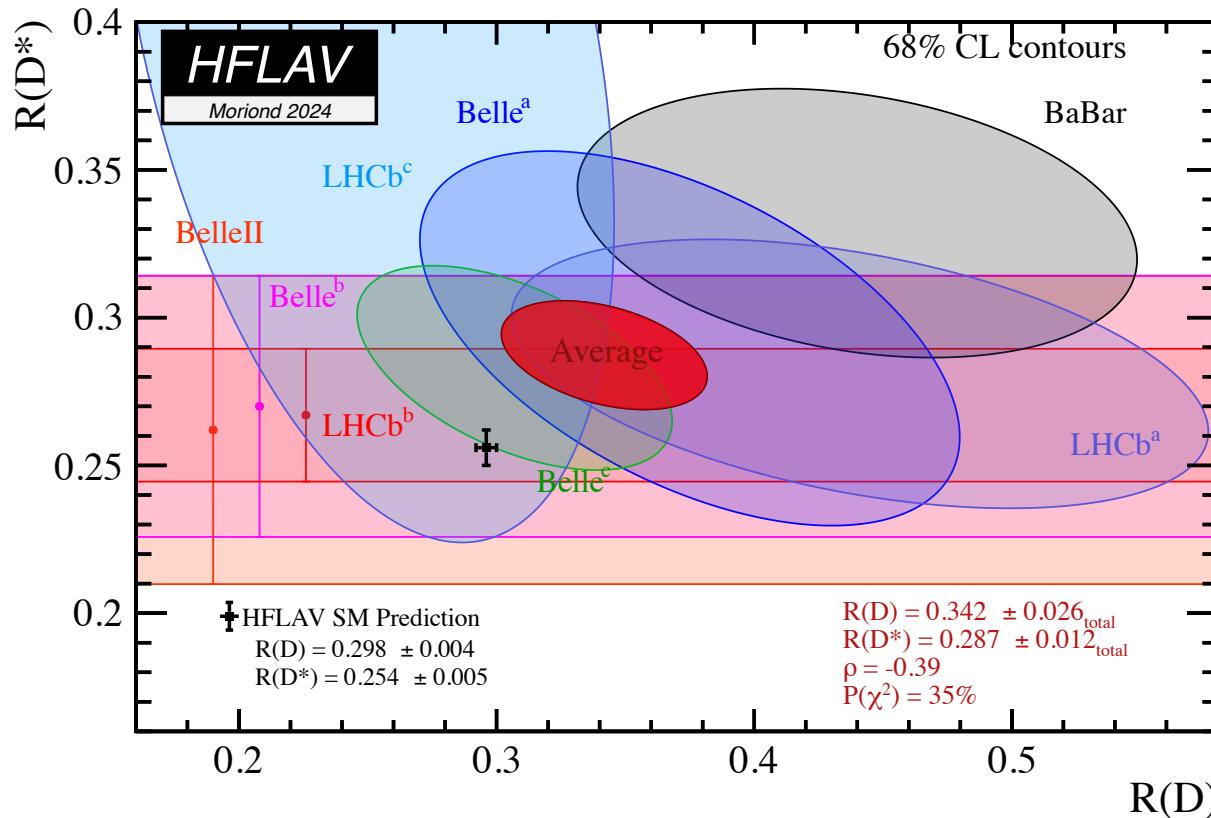
$$R_{D^*} = 0.267^{+0.041}_{-0.039}(\text{stat.})^{+0.028}_{-0.033}(\text{syst.})$$

arXiv:2401.02840, submitted to PRD



- Belle II: 189 fb^{-1} data
- Improved sensitivities from FEI
- Dominant systematic due to MC statistics and E_{ECL} can be reduced with more data

Measurements of R_{D^*} and R_D



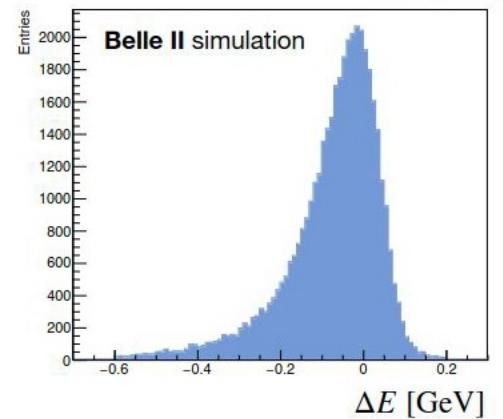
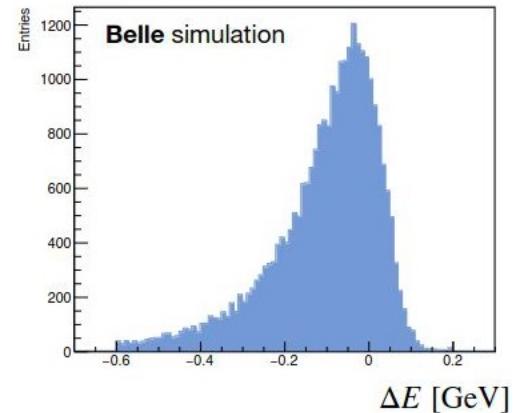
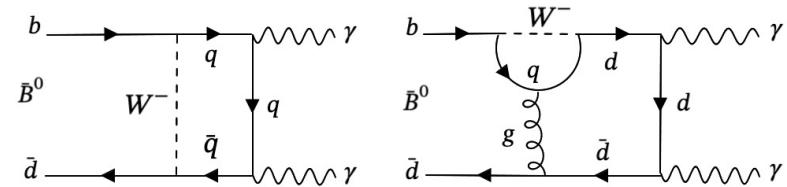
Measurement of R_D and R_{D^*} exceed the SM predictions by 1.6σ & 2.5σ , respectively, the combined deviation above the SM is 3.31σ

- Other ongoing Belle II measurements
 - ✓ Not systematic limited, reduce with more data
- Future measurement as a function of q^2 and angular distributions

Measurements of $B \rightarrow \gamma\gamma$

- Combined Belle (694 fb^{-1}) and Belle II (362 fb^{-1}) measurement
- Small branching fraction & high background
- Analysis strategy:
 - ✓ Dedicated BDT to suppress continuum, $\pi^0 \rightarrow \gamma\gamma$ and $\eta^0 \rightarrow \gamma\gamma$
 - ✓ Multivariable fit to: ΔE , M_{bc} , and BDT output
 - ✓ Control sample: $B^0 \rightarrow K^*(892)[K^+\pi^-]\gamma$
- Significant improvement at Belle II vs Belle
 - ✓ Better signal efficiency
 - ✓ Improved ΔE resolution

	Belle	Belle II
Sig efficiency	23%	31%
Exp. bkg/fb ⁻¹	~ 0.8	



Measurements of $B \rightarrow \gamma\gamma$

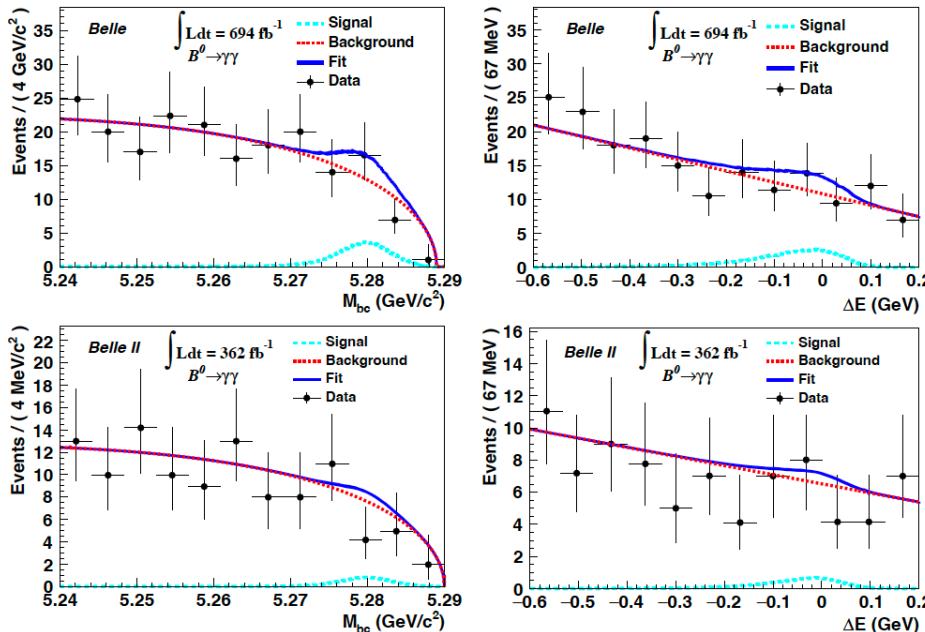


TABLE III. Summary of $\mathcal{B}(B^0 \rightarrow \gamma\gamma)$ measurements and UL's at 90% credibility level.

	$\mathcal{B}(B^0 \rightarrow \gamma\gamma)$	UL on $\mathcal{B}(B^0 \rightarrow \gamma\gamma)$
Belle	$(5.4^{+3.3}_{-2.6} \pm 0.5) \times 10^{-8}$	$< 9.9 \times 10^{-8}$
Belle II	$(1.7^{+3.7}_{-2.4} \pm 0.3) \times 10^{-8}$	$< 7.4 \times 10^{-8}$
Combined	$(3.7^{+2.2}_{-1.8} \pm 0.5) \times 10^{-8}$	$< 6.4 \times 10^{-8}$

Experiment	Integrated Luminosity ($\int \mathcal{L} dt$)	Limit @ 90 C.L.
L3	73 pb^{-1}	3.9×10^{-5}
Belle	104 fb^{-1}	6.2×10^{-7}
Babar	426 fb^{-1}	3.2×10^{-7}

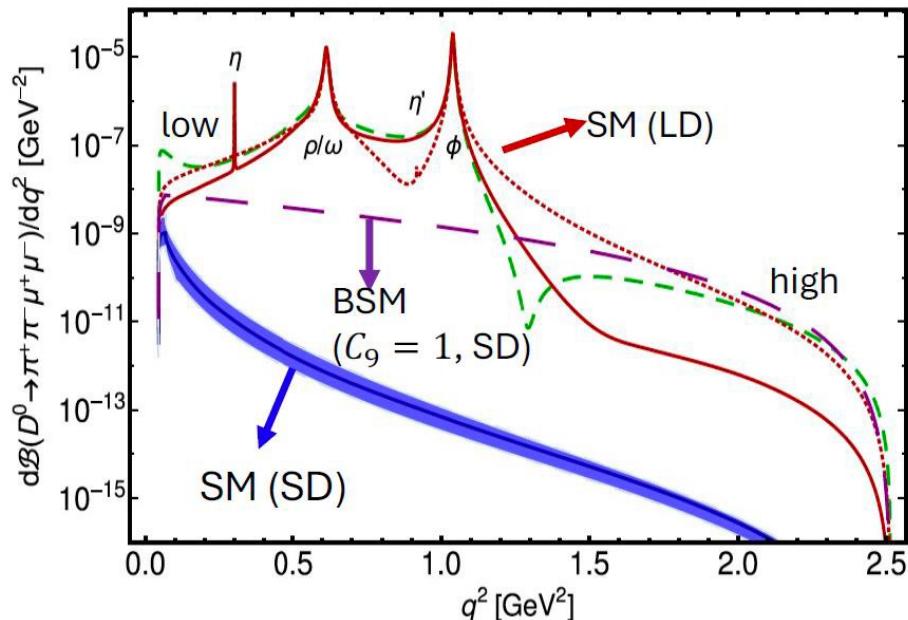
- Combined signal yield: $11.0^{+6.5}_{-5.5}$
 - ✓ 2.5σ significance
- Sensitivity approach SM prediction
 - ✓ SM: $\mathcal{B} = (1.4^{+1.4}_{-0.8}) \times 10^{-8}$
- JHEP 12, 169 (2020)
- Expected UL: $\mathcal{B} < 4.4 \times 10^{-8}$
- UL has 5x improvement over previous best UL by Babar
- Significant better sensitivity improvement at Belle II

arXiv:2405.19734, submitted to PRD

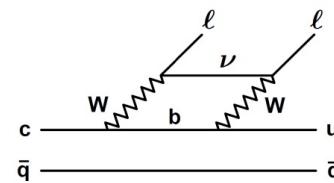
L3: PLB 363 (1995) 137-144
 Belle: PRD 73, 051107 (2006)
 BaBar: PRD 83, 032006 (2011)

Search for Rare Charm decays: $D^0 \rightarrow h^+h^-e^+e^-$

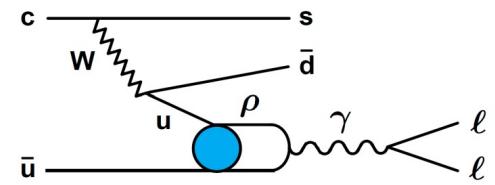
- Flavor changing neutral current (FCNC) $c \rightarrow u\bar{u}$ process is suppressed in the SM
- LD mainly from vector meson dominated mode
- Search for NP and Lepton Flavor Universality (LFU) test



Short distance (SD)



Long distance (LD)



Some previous measurements of Br and UL @90%

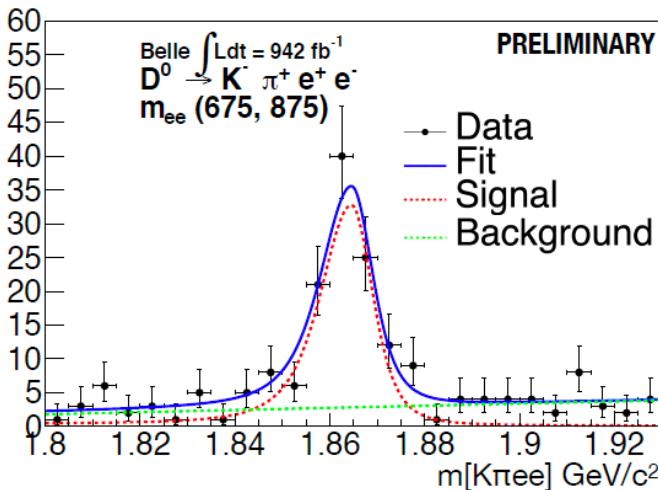
Experiment	$K^-K^+e^+e^-$	$\pi^-\pi^+e^+e^-$	$K^-\pi^+e^+e^-$
Babar (2019)			$40.0 \pm 5.0 \pm 2.3 (\rho^0/\omega)$ stat syst
BESIII (2019)	< 110	< 70	< 410
	$K^-K^+\mu^+\mu^-$	$\pi^-\pi^+\mu^+\mu^-$	$K^-\pi^+\mu^+\mu^-$
LHCb (2016-2017)	$1.54 \pm 0.27 \pm 0.19$	$9.64 \pm 0.48 \pm 1.10$	$4.17 \pm 0.12 \pm 0.40 (\rho^0/\omega)$

BaBar: PRL 122, 081802 (2019)

BESIII: PRD 97, 072015 (2019)

LHCb: PLB 517, 558 (2016); PRL 119, 181805 (2017)

Search for rare charm decays: $D^0 \rightarrow h^+h^-e^+e^-$



To be submitted to PRL

TABLE I. $D^0 \rightarrow h^-h^{(\prime)+}e^+e^-$ modes yields, significance, branching fractions, branching fraction upper limits, and the efficiencies of each m_{ee} region [$\times 10^{-7}$]. A fitted yield and a branching fraction are not reported for $K^-K^+e^+e^-$ mode with m_{ee} in the m_η region since only one event is observed, and the significance is determined from the CL_s distribution.

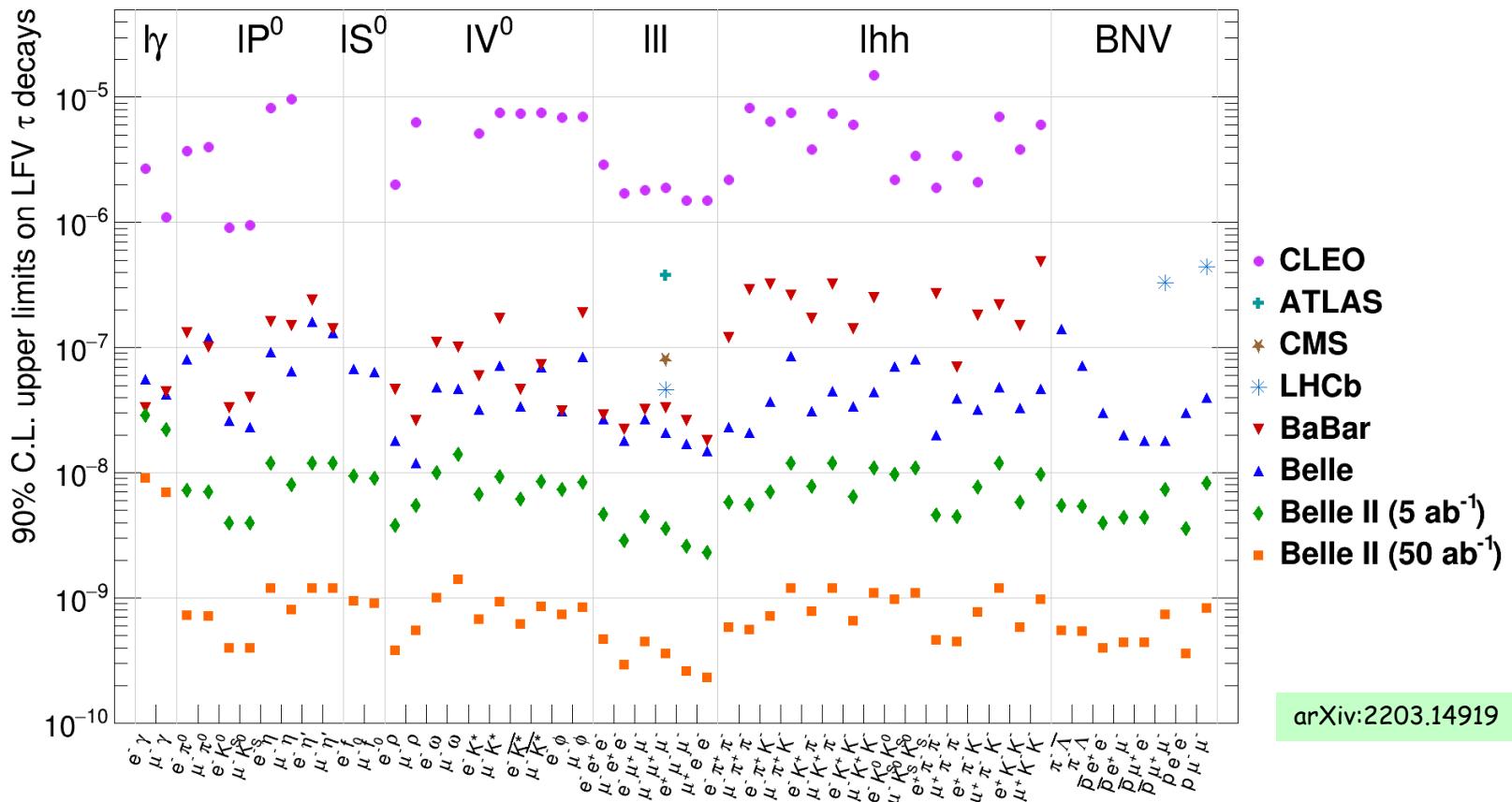
m_{ee} region	[MeV/ c^2]	Yield	Significance	\mathcal{B}	UL @ 90% CL	Efficiency
$K^-K^+e^+e^-$						
η	520-560	-	$< 0.1\sigma$	-	< 2.3	3.53 ± 0.04
ρ^0/ω	> 675	2.6 ± 1.8	2.0σ	$1.2 \pm 0.9 \pm 0.1$	< 3.0	6.00 ± 0.06
non-resonant	$> 200^a$	3.5 ± 3.3	1.5σ	$3.1 \pm 3.0 \pm 0.4$	< 7.7	3.19 ± 0.04
$\pi^-\pi^+e^+e^-$						
η	520-560	0.6 ± 2.3	0.3σ	$0.4 \pm 1.4 \pm 0.2$	< 3.2	5.31 ± 0.05
ρ^0/ω	675-875	3.7 ± 4.1	0.9σ	$2.0 \pm 2.2 \pm 0.8$	< 6.1	5.69 ± 0.05
ϕ	995-1035	3.6 ± 3.2	1.1σ	$1.1 \pm 1.1 \pm 0.2$	< 3.1	9.41 ± 0.06
non-resonant	> 200	-0.2 ± 4.1	$< 0.1\sigma$	$-0.2 \pm 3.4 \pm 0.9$	< 7.2	3.69 ± 0.04
$K^-\pi^+e^+e^-$						
η	520-560	4.0 ± 2.7	1.6σ	$2.2 \pm 1.5 \pm 0.5$	< 5.6	5.09 ± 0.04
ρ^0/ω	675-875	110 ± 13	11.8σ	$39.6 \pm 4.5 \pm 2.9$	-	8.01 ± 0.06
ϕ	990-1034	4.6 ± 2.4	2.5σ	$1.4 \pm 0.8 \pm 0.3$	< 2.9	9.19 ± 0.06
non-resonant	> 560	2.2 ± 4.2	0.4σ	$1.3 \pm 2.4 \pm 0.6$	< 6.5	4.89 ± 0.09

^a Excluding resonance regions, which is same for all three modes.

- Belle measurement with 942 fb^{-1} data
- Observe $D^0 \rightarrow K^-\pi^+e^+e^-$ in ρ/ω region (11.8σ)
 - ✓ Compatible with Babar and SM expectation
$$\mathcal{B} = (39.06 \pm 4.5(\text{stat}) \pm 2.9(\text{syst})) \times 10^{-7}$$
- No significant signal on other final states
 - ✓ UL at 90% around $(2.3 - 7.7) \times 10^{-7}$
 - ✓ World's best limits to date

Search for Rare τ lepton decays

- Many rare or forbidden τ decays are excellent probes to NP beyond the SM
- B-factories generated large τ decay data samples
 - ✓ Searches in many different final states with high precisions
 - ✓ Not limited by systematics, sensitivities increases with higher luminosity
 - ✓ Better sensitivities than other experiments in many final states



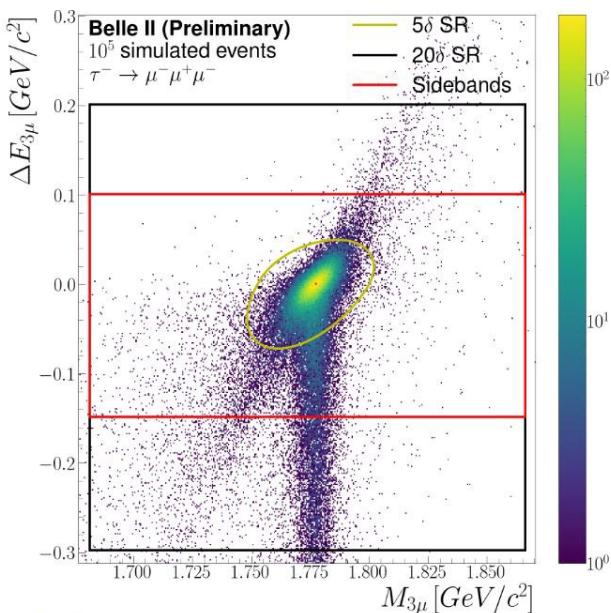
Search for LFV $\tau \rightarrow \mu\mu\mu$ decay



- Belle II measurements: 424 fb^{-1} data
- Fully reconstructed final state
- Two independent variables:

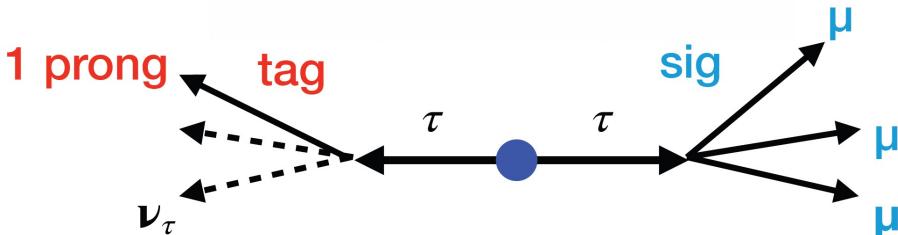
$$M_{3\mu} = \sqrt{E_{3\mu}^2 - |\vec{p}_{3\mu}|^2}$$

$$\Delta E = E_{3\mu}^{\text{CM}} - E_{\text{beam}}^{\text{CM}}$$



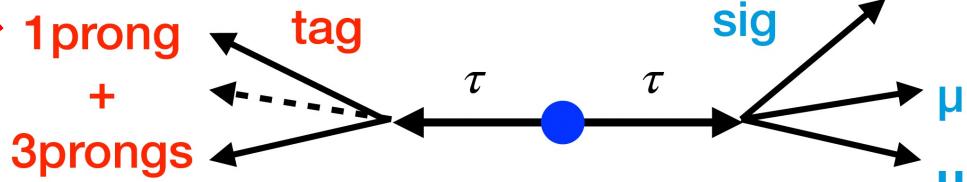
$M_{3\mu}$ close to τ mass, ΔE close to zero
Tail due to initial and final radiations

- 1-prong: Belle & BaBar method



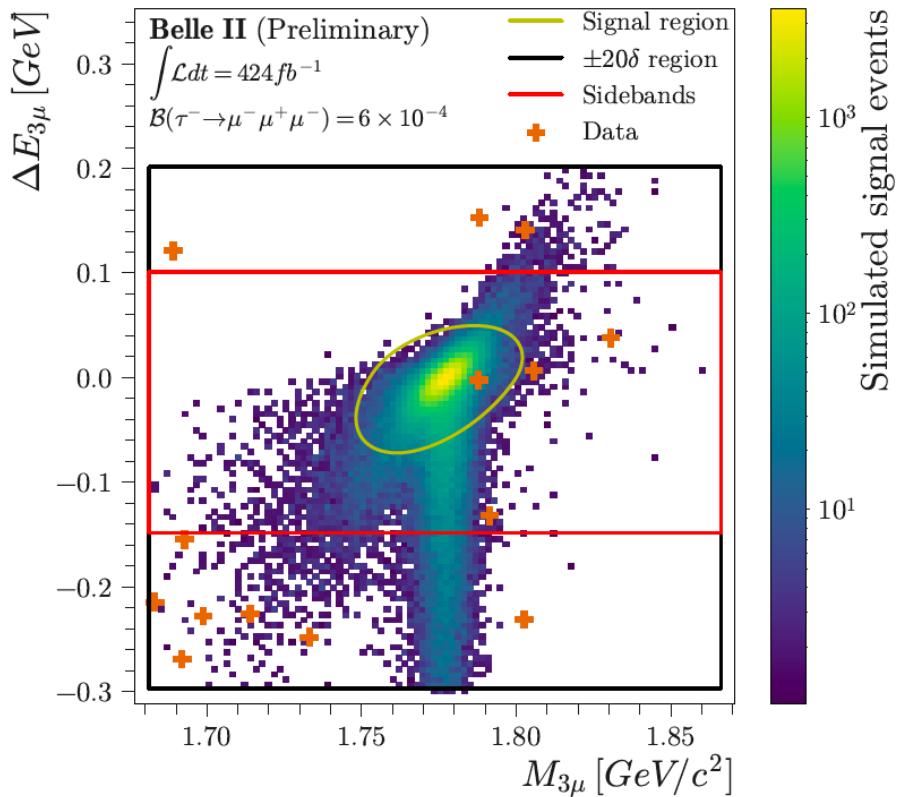
- Cut-based selection
- Signal efficiency: 14.9% ($2 \times$ Belle efficiency)
- Expected background: 0.43 (simulation)

Inclusive approach: Belle II



- Boost Decision Tree based selection
- Signal efficiency: 20.4% ($2.7 \times$ Belle efficiency)
- Expected background: 0.5 (simulation)

Search for LFV $\tau \rightarrow \mu\mu\mu$ decay



Experiment	Upper Limit at 90% C.L.
ATLAS	$3.8 \times 10^{-7} (\mathcal{L} = 20.3 \text{ fb}^{-1})$
LHCb	$4.6 \times 10^{-8} (\mathcal{L} = 3.0 \text{ fb}^{-1})$
CMS	$2.9 \times 10^{-8} (\mathcal{L} = 131 \text{ fb}^{-1})$

CMS - PLB 853 (2024) 138633

Experiment	Upper Limit at 90% C.L.
Belle	$2.1 \times 10^{-8} (\mathcal{L} = 782 \text{ fb}^{-1})$
BaBar	$3.3 \times 10^{-8} (\mathcal{L} = 486 \text{ fb}^{-1})$
Belle II	$1.9 \times 10^{-8} (\mathcal{L} = 424 \text{ fb}^{-1})$

Belle II - arXiv:2405.07386

Most stringent limit to date

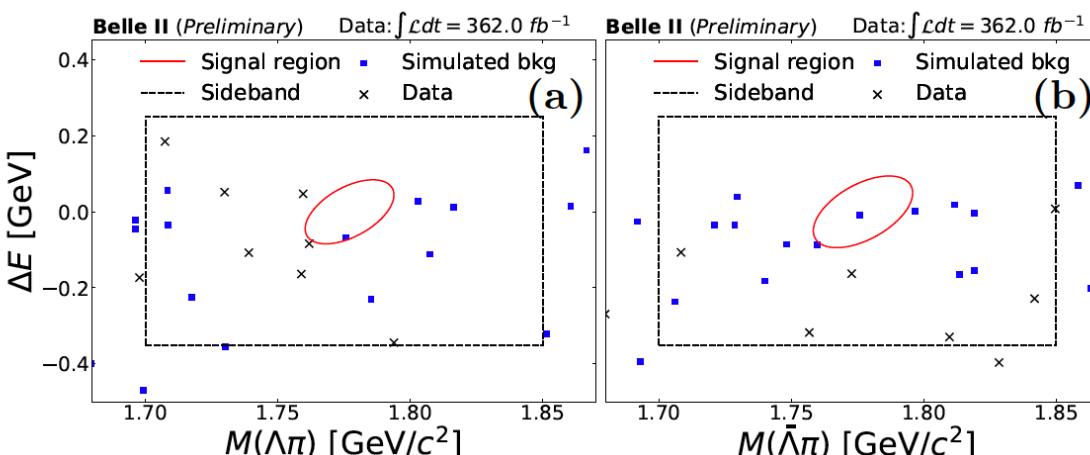
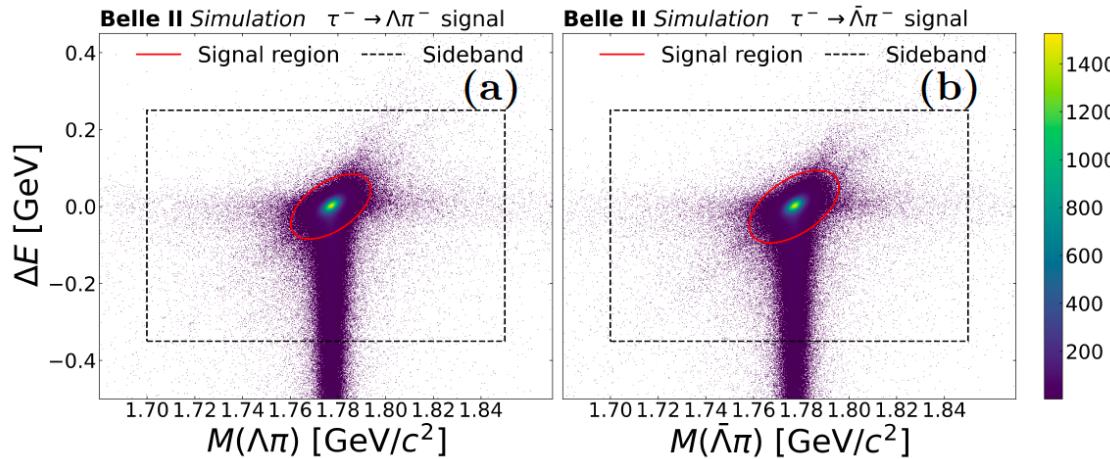
Lepton & baryon number violating τ decay



- Search for Lepton number & baryon number violating τ decays

$$\tau^- \rightarrow \Lambda\pi^- \quad \text{and} \quad \tau^- \rightarrow \bar{\Lambda}\pi^-$$

- Belle II measurements: 362 fb^{-1} data, Similar to $\tau \rightarrow \mu\mu\mu$ analysis



$\mathcal{B}(\tau^- \rightarrow \Lambda\pi^-) < 4.7 \times 10^{-8}$ @90%CL
 $\mathcal{B}(\tau^- \rightarrow \bar{\Lambda}\pi^-) < 4.3 \times 10^{-8}$ @90%CL

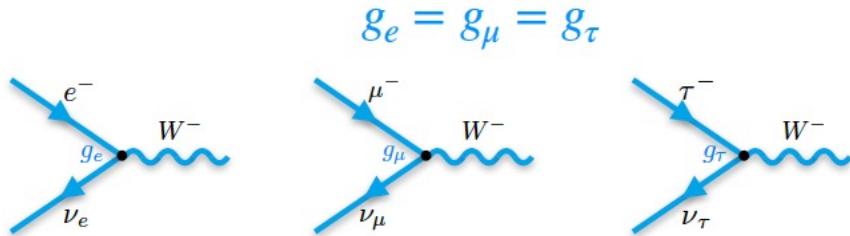
To be submitted to PRD

Test of Lepton flavour universality in τ decay

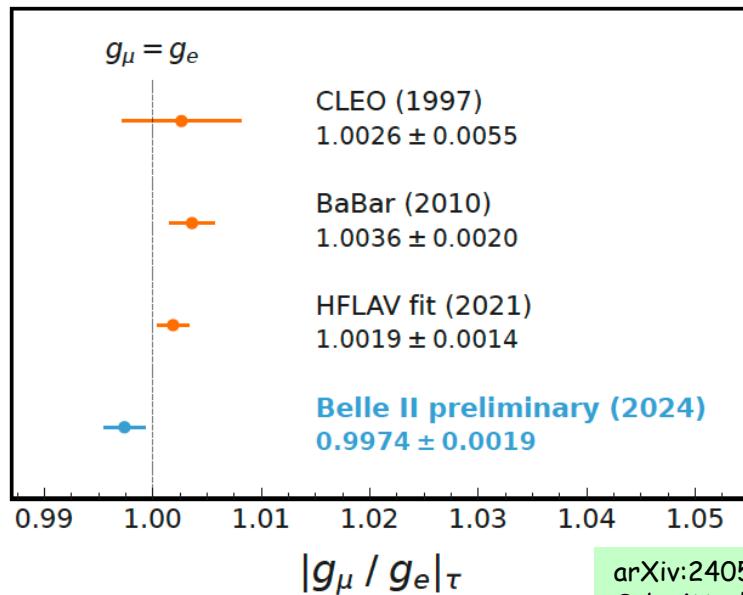
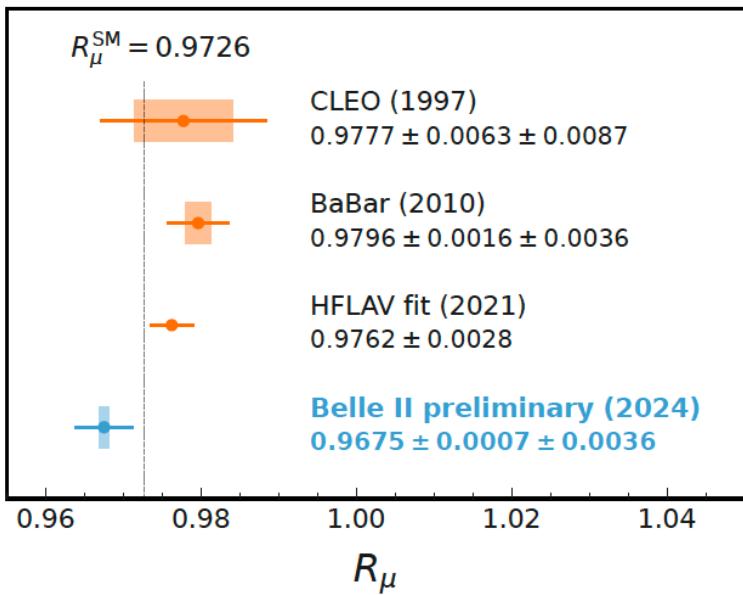


- Coupling between lepton and W is flavour-independent in the SM
- Test $\mu - e$ universality in τ decays by measuring decay rates (362 fb^{-1})

$$R_\mu = \frac{B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)} \stackrel{\text{SM}}{=} 0.9726$$



$$\left(\frac{g_\mu}{g_e} \right)_\tau^2 \propto R_\mu \times \frac{f(m_e^2/m_\tau^2)}{f(m_\mu^2/m_\tau^2)} \stackrel{\text{SM}}{=} 1$$



arXiv:2405.14625
Submitted to PRD

- Most precise test of $\mu - e$ universality in τ decays by a single measurement
- Consistent with the SM expectation at 1.4σ level
- Dominated by the systematic uncertainty: can be reduced with more data

Summary and Prospect

- A few selected recent highlights from Belle(II)
- Improved sensitivities at Belle II (better detector and analysis)
- **More exciting results will eventually come with more data (soon)**

Roadmap of possible new evidences and observations

Rare decay BSM

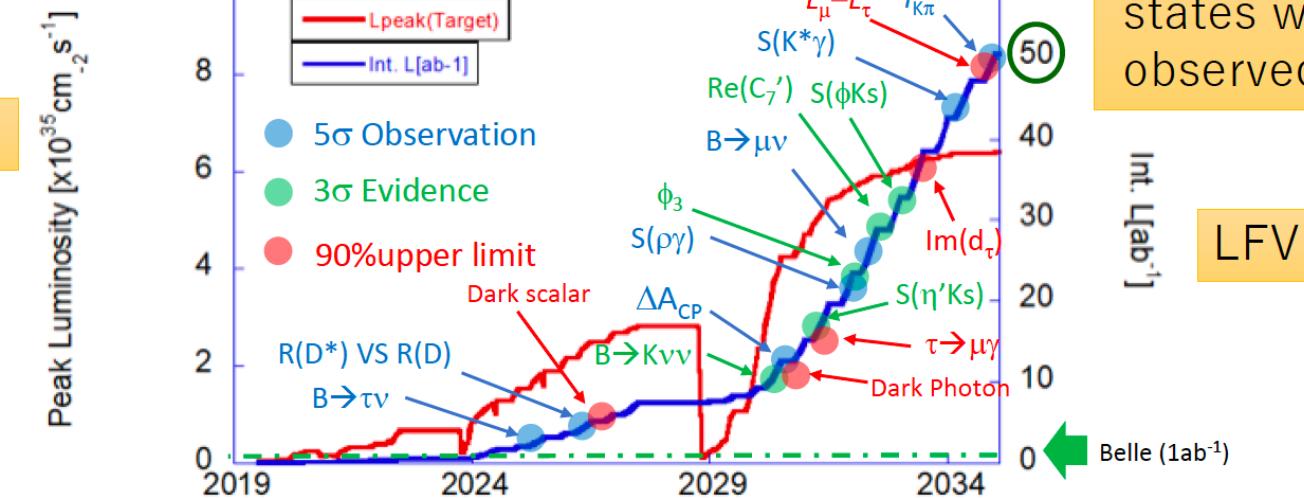
Additional CP violation in Quark Sector

Many interesting quark composite states will be also observed.

Dark Sector

Connection
to Lattice

Anomalies



Both Particle Phys.+
Nuclear Phys.
can enjoy.

Model Independent?

Backup

SuperKEKB/Belle II luminosity projection

