



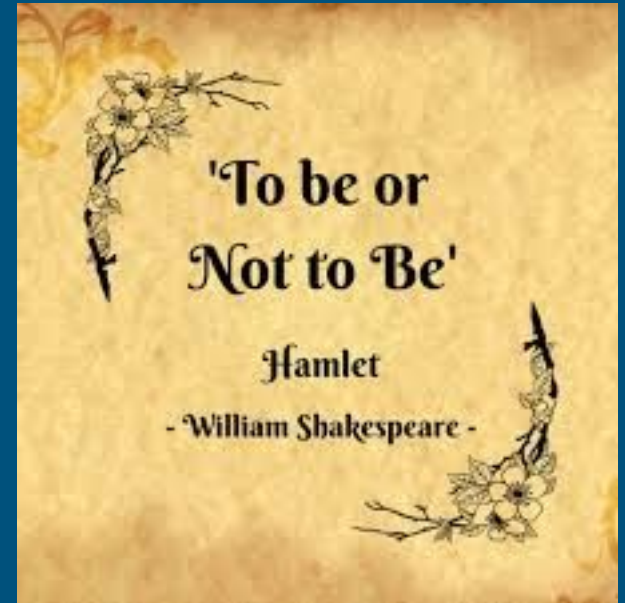
Experimental Status of Semi-Leptonic B-decays

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Talk Outline

- Introduction
- Tagging methods
- $|V_{ub}|$ from $B^0 \rightarrow \pi^- l^+ \nu$ and $B^+ \rightarrow \rho^0 l^+ \nu$
- Lepton Flavor Violation (LFV):
 - Measurement of $R(D^*)$
 - Measurement of $R(X)$
- Measurement of BR ($B \rightarrow K \nu \bar{\nu}$)
- Conclusions

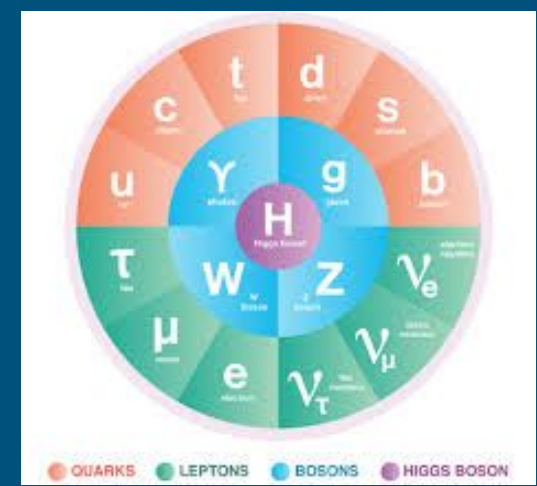
Selected modes using Belle II results shown



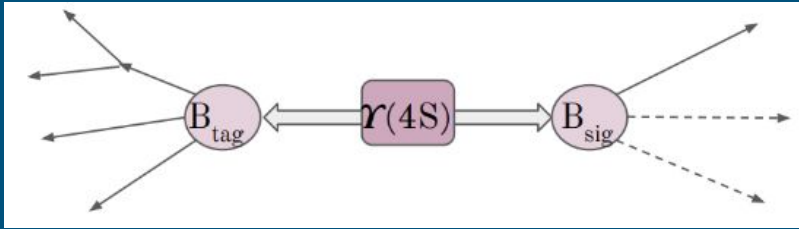
Introduction

- Unitarity of CKM matrix imposes constraints to test Standard Model.
- Belle II provides a unique testbed for SM tests in the B-sector as it is primarily a B-factory ($e^+ e^- \rightarrow \Psi(4S) \rightarrow B\bar{B}$)

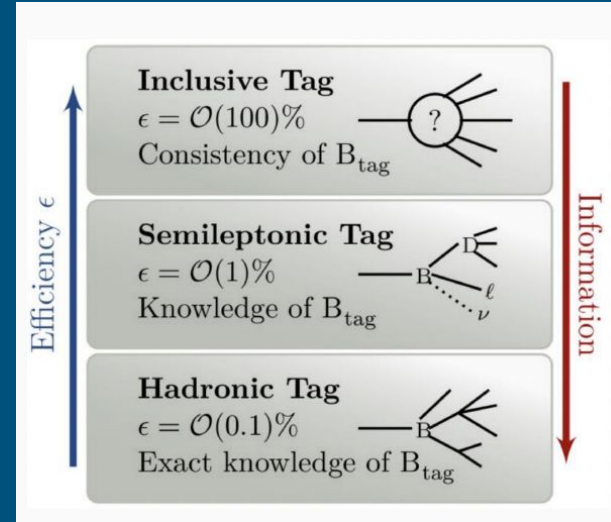
$$\begin{bmatrix} d' \\ s' \\ b' \end{bmatrix} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \begin{bmatrix} d \\ s \\ b \end{bmatrix}$$



Tagging Methods

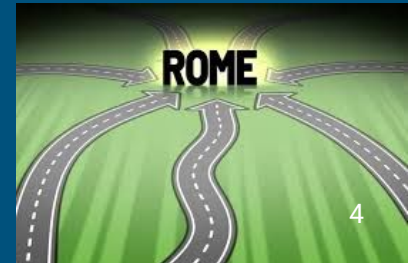


Both B_{tag} and B_{sig} are reconstructed.



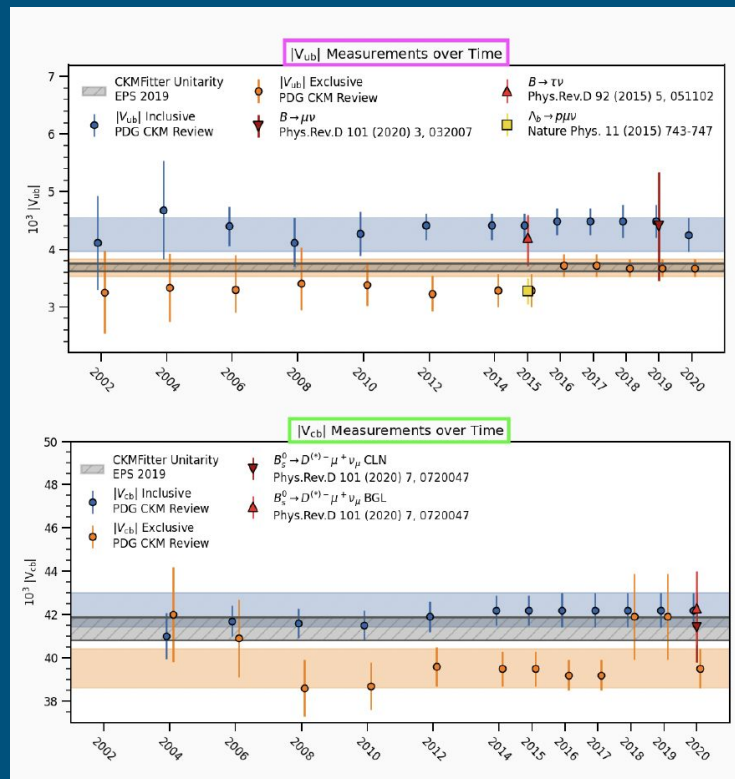
Exclusive vs. Inclusive: depends on reconstruction of B_{sig}

- Exclusive: B_{sig} is reconstructed in a specific decay mode.
- Inclusive: B_{sig} reconstructed as many modes, e.g., $B_{\text{sig}} \rightarrow X\ell\nu$.



$|V_{ub}|$ from $B^0 \rightarrow \pi^- l^+ \nu$ and $B^+ \rightarrow \rho^0 l^+ \nu$

- Tension between exclusive (orange band) and inclusive (blue band)
- Precision measurements of the CKM parameters $|V_{ub}|$ and $|V_{cb}|$ can be done using semi-leptonic B decays
- $|V_{ub}|$: $b \rightarrow u$ transitions ($B \rightarrow X_u l \nu$)
- $|V_{cb}|$: $b \rightarrow c$ transitions ($B \rightarrow X_c l \nu$)



$|V_{ub}|$

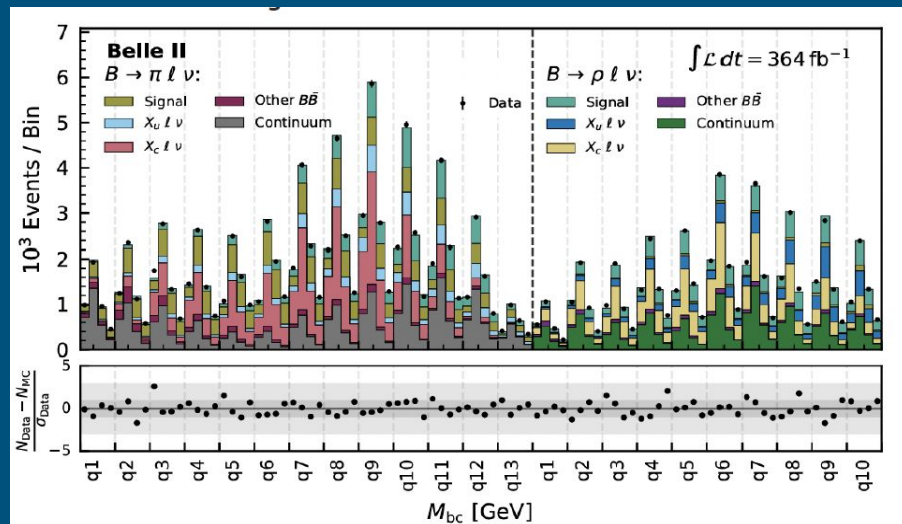
$|V_{cb}|$

$|V_{ub}|$ from $B^0 \rightarrow \pi^- l^+ \nu$ and $B^+ \rightarrow \rho^0 l^+ \nu$ arXiv:2407.17403

- Belle II, Run 1 data (364 fb^{-1}) untagged
- Background suppression done using BDTs
- Kinematic variables used are ΔE and M_{bc}
- Signal yields are extracted from these 2 kinematic variables in bins of q^2 simultaneously. For $B \rightarrow X l \nu$, $q^2 = (\mathbf{p}_B - \mathbf{p}_X)^2$

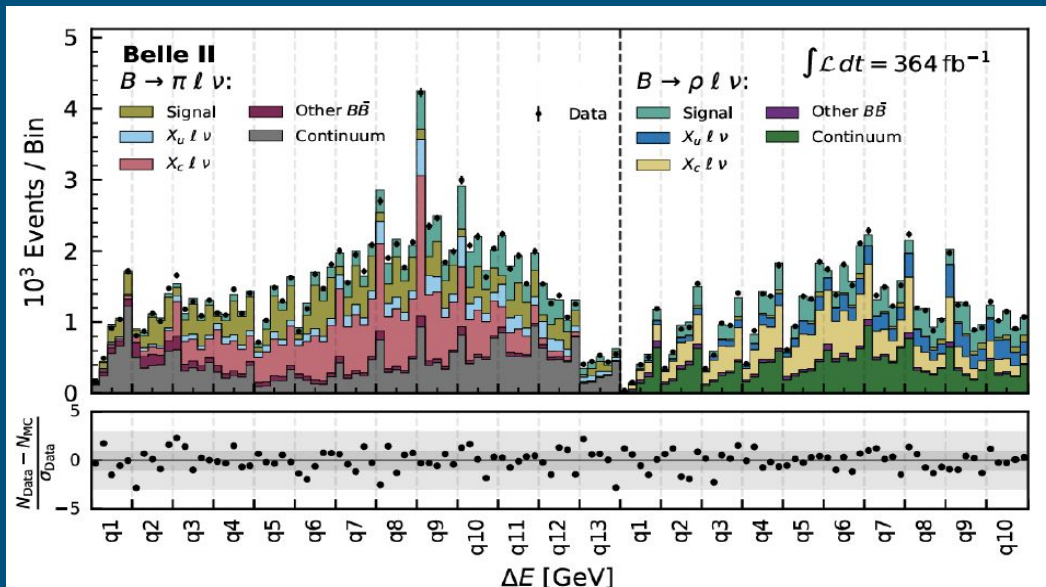
$$M_{bc}^2 = \sqrt{(E_{\text{beam}}^* - |p_{B^*}^*|^2)}$$

$$\Delta E = E_B^* - E_{\text{beam}}^*$$



$|V_{ub}|$ from $B^0 \rightarrow \pi^- l^+ \nu$ and $B^+ \rightarrow \rho^0 l^+ \nu$

- $|V_{ub}|$ is extracted separately from $B^0 \rightarrow \pi^- l^+ \nu$ and $B^+ \rightarrow \rho^0 l^+ \nu$ modes using χ^2 fits to the measurement q^2 spectra.

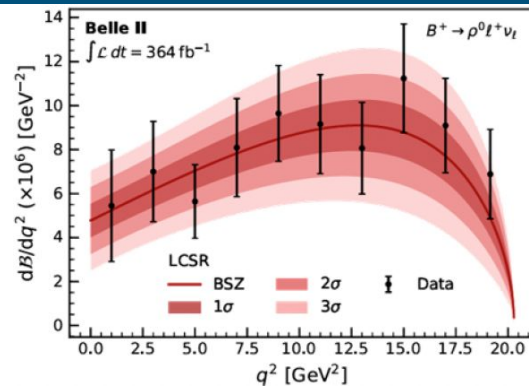
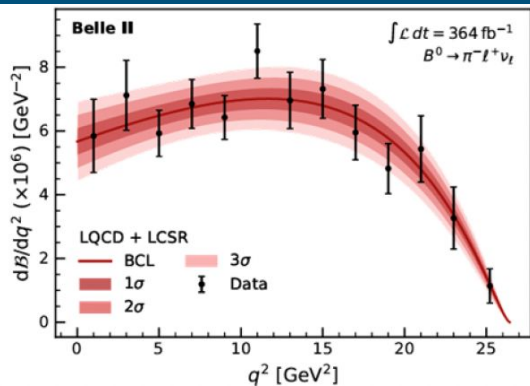
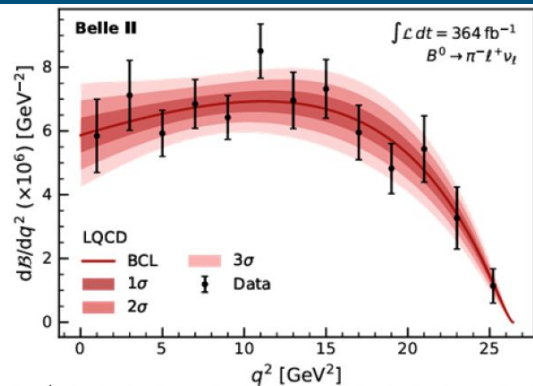


$|V_{ub}|$ from $B^0 \rightarrow \pi^- l^+ \nu$ and $B^+ \rightarrow \rho^0 l^+ \nu$

$$\mathcal{B}(B^0 \rightarrow \pi^- l^+ \nu_l) = (1.516 \pm 0.042(stat) \pm 0.059(sys)) \times 10^{-4}$$

$$\mathcal{B}(B^+ \rightarrow \rho^0 l^+ \nu_l) = (1.625 \pm 0.079(stat) \pm 0.180(sys)) \times 10^{-4}$$

Consistent with PDG



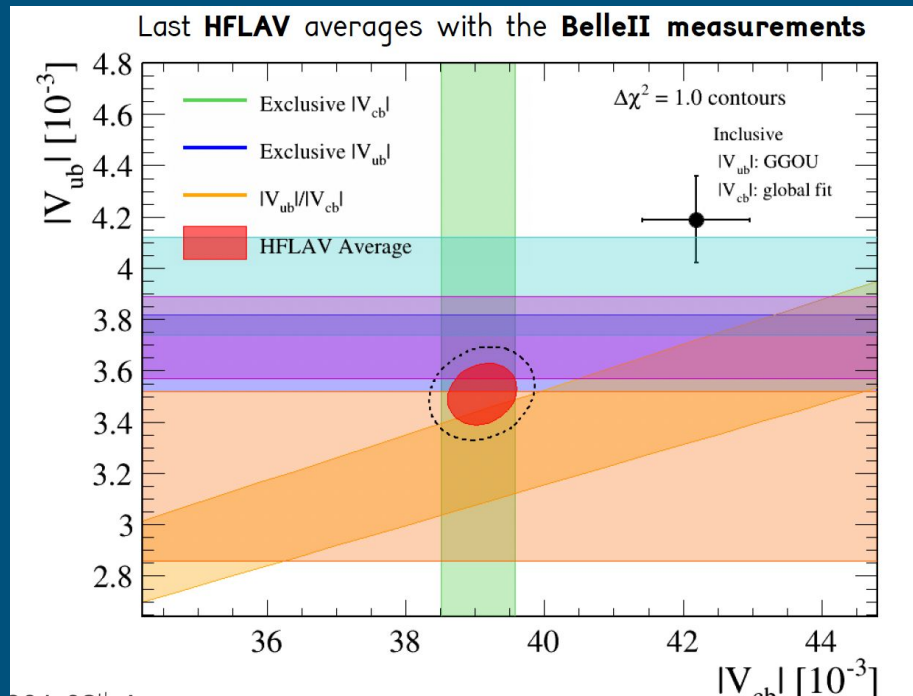
$$B^0 \rightarrow \pi^- l^+ \nu_l: |V_{ub}| = (3.93 \pm 0.09(stat) \pm 0.13(sys) \pm 0.19(theo)) \times 10^{-3} \text{ LQCD constraints}$$

$$|V_{ub}| = (3.73 \pm 0.07(stat) \pm 0.07(sys) \pm 0.16(theo)) \times 10^{-3} \text{ LQCD+LCSR constraints}$$

$$B^+ \rightarrow \rho^0 l^+ \nu_l: |V_{ub}| = (3.19 \pm 0.12(stat) \pm 0.17(sys) \pm 0.26(theo)) \times 10^{-3} \text{ LCSR constraints}$$

$|V_{ub}|$ from $B^0 \rightarrow \pi^- l^+ \nu$ and $B^+ \rightarrow \rho^0 l^+ \nu$

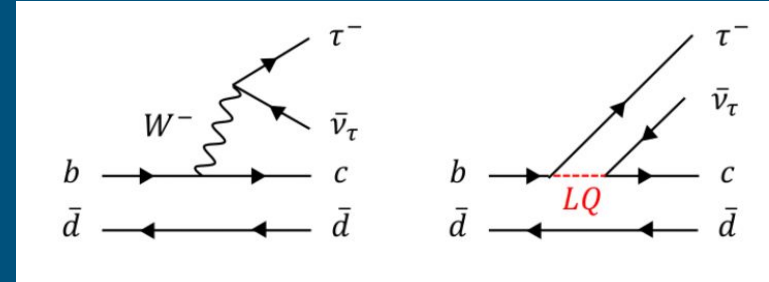
- Large uncertainty on the $|V_{ub}|$ values
- Tension with inclusive measurement is reduced.



LFV: Measurement of $R(D^*)$

- Test of LFU

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu)} \quad (\ell = e \text{ or } \mu)$$

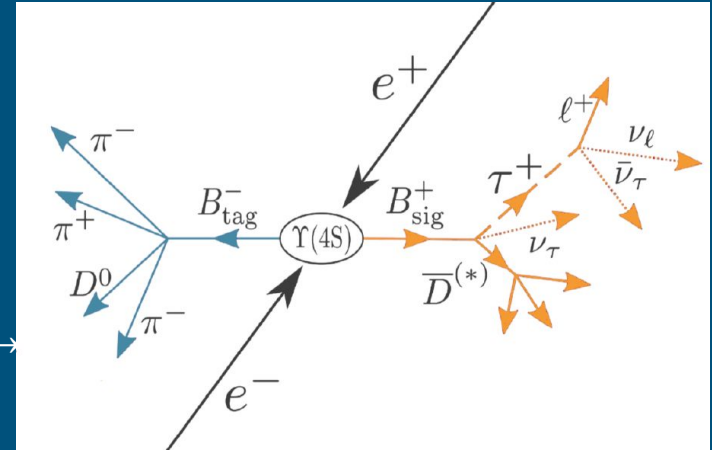


- Semileptonic B decays involving a τ lepton are sensitive to physics beyond the SM (BSM).
- Coupling to all lepton flavors is the same in the SM, but the large value of the τ mass results in a reduced phase space factor, and hence $R(D)$ and $R(D^*)$ are expected to be 0.298 ± 0.004 and 0.254 ± 0.005 , respectively in SM.

LFV: Measurement of $R(D^*)$

arXiv:2401.02840

- Belle II, Run 1 data (189 fb^{-1})
- Btag decays hadronically
- Reconstruct τ and light lepton decays into the same final state particles to cancel many systematic uncertainties
- Reconstruct the D^* in the following channels: $D^* \rightarrow D^0 \pi^+, D^+ \pi^0$ and $D^0 \pi^0$.
- Rest of the event: no good quality tracks, no π^0 candidates. Sum of all the neutral extra clusters energy is called E_{ECL} .
- Poorly understood $B \rightarrow D^{**} \ell \nu$ backgrounds is one of the major background

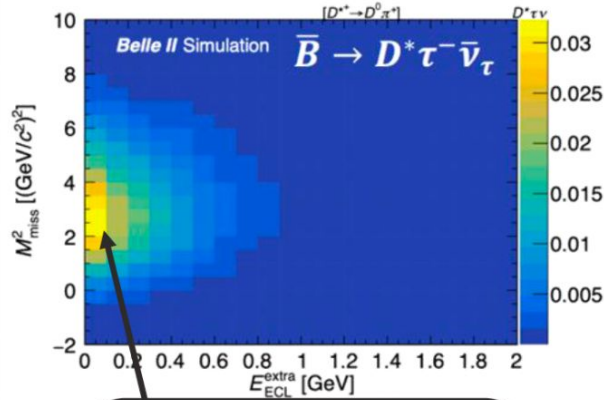


$$R(D_{\tau/\ell}^*) = \frac{B(B \rightarrow D^* \tau \nu)}{B(B \rightarrow D^* \ell \nu)}$$

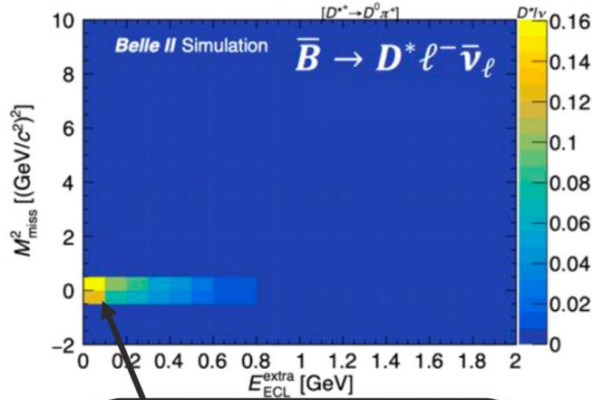
LFV: Measurement of $R(D^*)$

2D fit to E_{ECL} and missing mass of the event (M_{miss}^2)

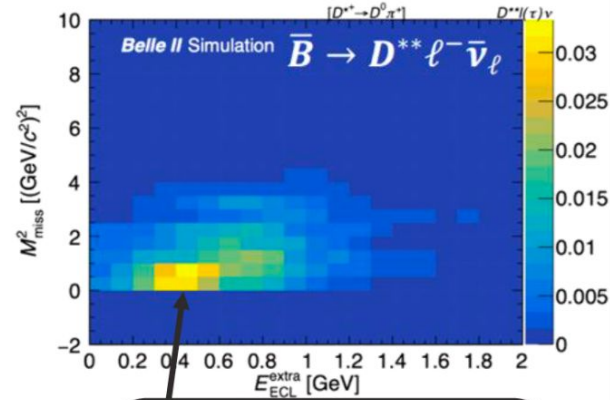
$$M_{miss}^2 = (p_{e^+e^-} - p_{B_{tag}} - p_{D^*} - p_{\ell})^2$$



Peaked around $E_{ECL} = 0$
and $M_{miss}^2 \approx 3 \text{ GeV}^2$



Peaked around $E_{ECL} = 0$
and $M_{miss}^2 = 0$



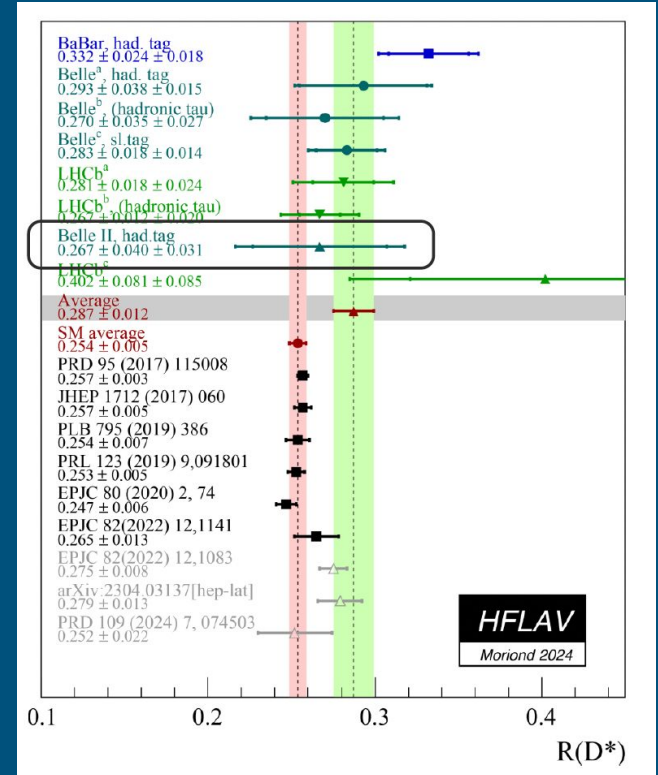
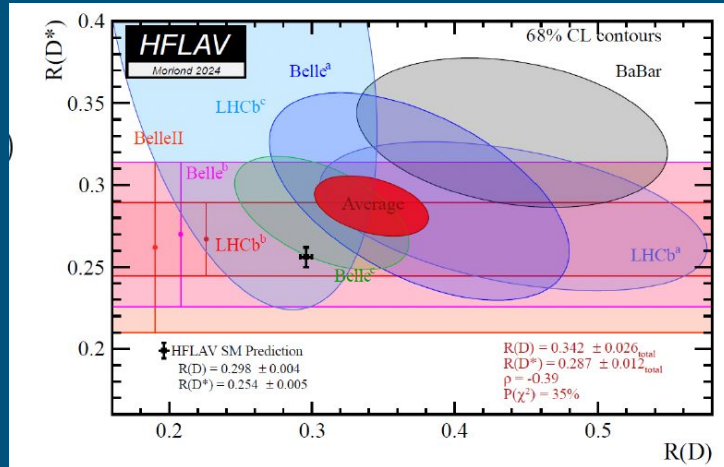
Higher E_{ECL} and M_{miss}^2 :
daughters of D^{**}

LFV: Measurement of $R(D^*)$

Belle II preliminary result

$$R(D_{\tau/\ell}^*) = 0.262_{-0.039}^{+0.041}(\text{stat})_{-0.032}^{+0.035}(\text{sys})$$

- Consistent with SM and HFLAV
- Update using 364 fb⁻¹ in progress

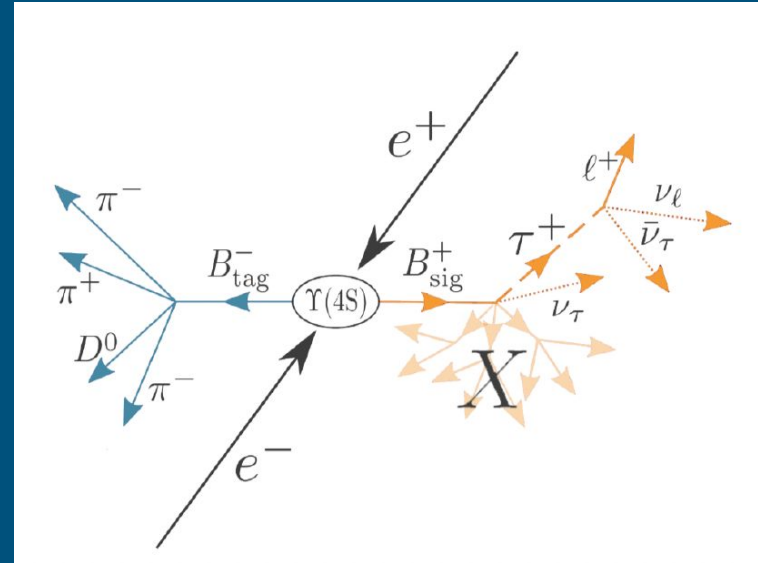


SM prediction: 0.254 ± 0.005

Measurement of $R(X)$

Phys. Rev. Lett. 132.211804 (2024)

- Belle II, Run 1 data (189 fb^{-1})
- Hadronic decay of the B_{tag}
- Reconstruct τ and light lepton decays into the same final state particles to cancel many systematic uncertainties.
- $p_e > 0.3$ (0.5) GeV and $p_\mu > 0.4$ (0.7) GeV in CMS (lab)
- The remaining particles on the signal side are collectively referred to as X
- Main challenge: correct model of backgrounds

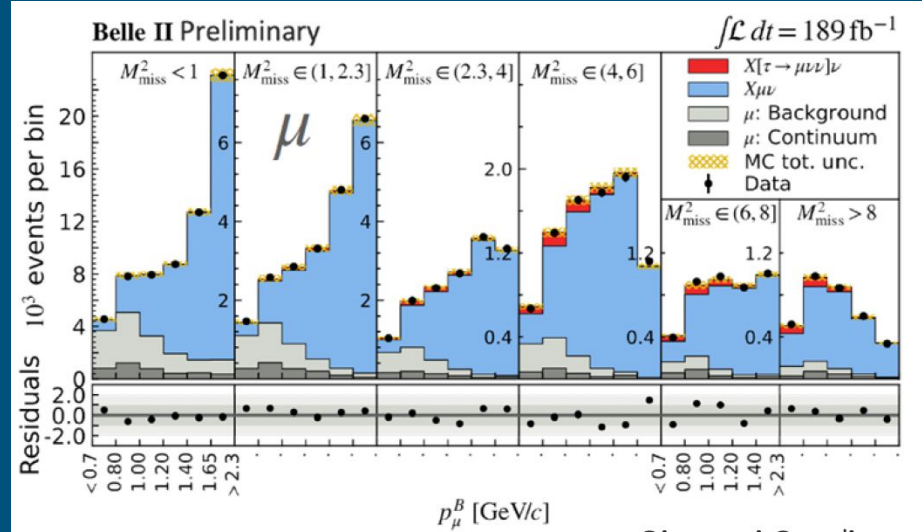
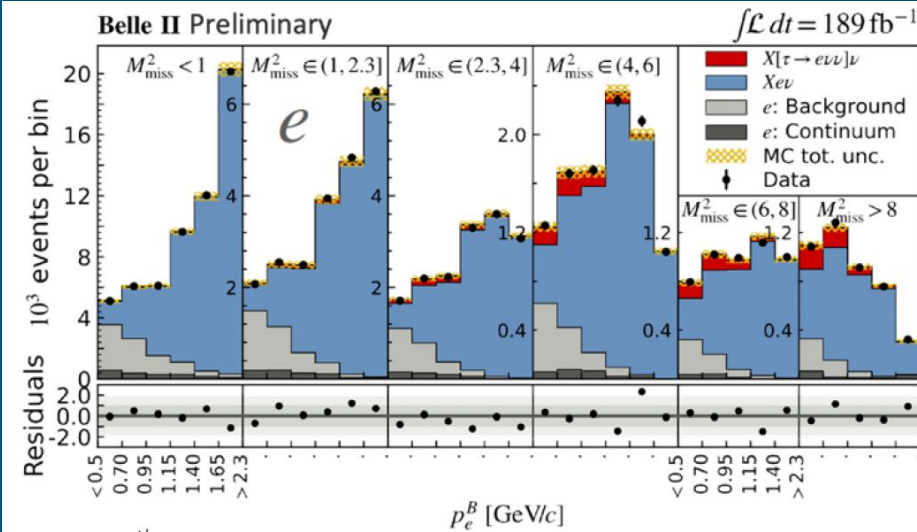


$$R(X_{\tau/\ell}) = \frac{B(B \rightarrow X\tau\nu)}{B(B \rightarrow X\ell\nu)}$$

Measurement of $R(X)$

- **MC corrections are applied**
- **Final Fit:** We extract the signal and normalization yields for the electron and muon modes from a simultaneous maximum-likelihood fit to the binned two-dimensional distributions of p_ℓ and M_{miss}^2
Fit components: $X_{\tau\nu}$, $X_{\ell\nu}$, BB background (fakes and secondaries) and continuum (off resonance data)

Measurement of R(X)



First measurement of the tau-to-light-lepton ratio of inclusive semileptonic B-meson branching fractions [complementary probe of LUV to the exclusive D^* decays]

Measurement of $R(X)$

$$R(X_{\tau/e}) = 0.232 \pm 0.020(\text{stat}) \pm 0.037(\text{syst}),$$

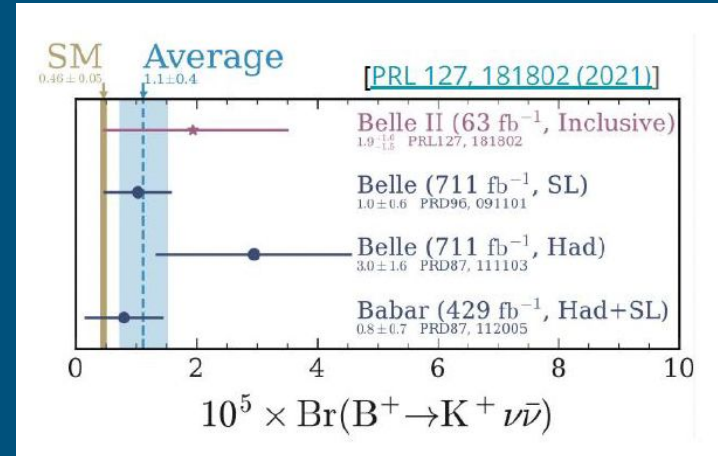
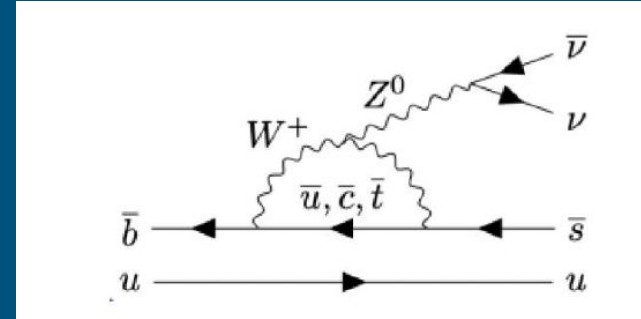
$$R(X_{\tau/\mu}) = 0.222 \pm 0.027(\text{stat}) \pm 0.050(\text{syst}),$$

$$R(X_{\tau/\ell}) = 0.228 \pm 0.016(\text{stat}) \pm 0.036(\text{syst})$$

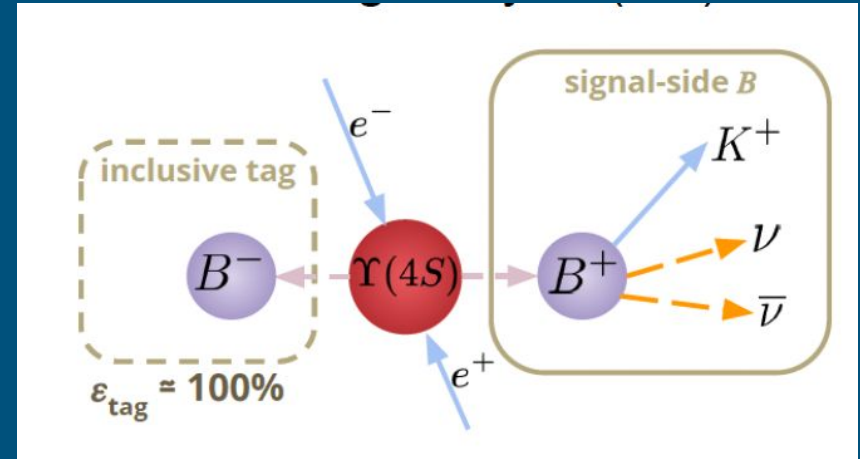
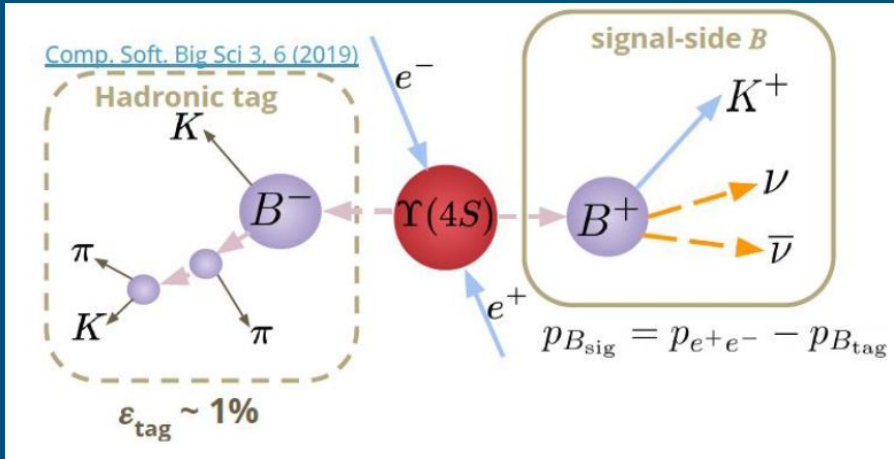
- Largest systematics: signal and background model
- Consistent with previous measurements from LEP, SM expectation, and constraints from $R(D^*)$.
- **SM expectation: $R(X_{\tau/\ell}) \approx 0.223$** [JHEP11(2022)007]

Measurement of BR ($B \rightarrow K \nu \bar{\nu}$)

- FCNC process
- SM prediction: Small BF
 $\text{BR}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (0.56 \pm 0.04) \cdot 10^{-5}$
 [PRD 107, 014511 (2023)]
- EW penguin, sensitive to NP
- Mode unique to $e^+ e^-$ colliders



Measurement of BR ($B \rightarrow K \nu \bar{\nu}$)



- Hadronic Tag (HT): Conventional method
- Reconstruct tag-side B with hadronic mode
- Lesser background

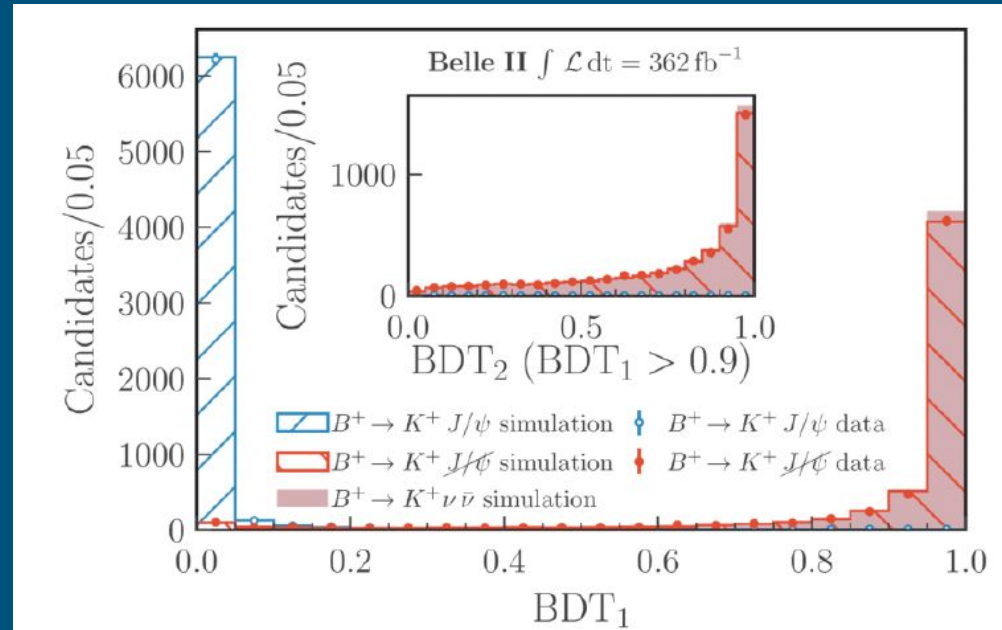
- Inclusive Tag (IT): Novel technique at Belle II— more sensitive than HT
- Reconstruct signal B (pick up K^+) only exploit the rest of the event (ROE) to suppress backgrounds.

Measurement of BR ($B \rightarrow K \nu \bar{\nu}$)

Phys. Rev. D. 109.112006 (2024)

- Belle II, Run 1 data (362 fb^{-1})
- Analysis used 2 different tagging methods: IT (innovative) and HT (conventional).
- Inclusive tag (IT): uses 2 consecutive classifiers with single kaon (one with the lowest q^2), event shape, and rest of the event information—2 BDTs

q^2 : mass squared of the neutrino pair



Measurement of BR ($B \rightarrow K \nu \bar{\nu}$)

Phys. Rev. D. 109.112006 (2024)

- **Signal Efficiency Validation done with control channel, $B \rightarrow J/\psi K$ sample, removing J/ψ and correcting K^+ kinematics**
- **Background Validation: Detailed studies of other B decay modes especially with K_L in the final states**
 - Undetected K_L in ECL can mimic neutrinos
 - K_L efficiency: $e^+e^- \rightarrow \gamma\phi \rightarrow K_L K_S$
 - Corrections for $B^+ \rightarrow K^+ K_L K_L$ background from $B^+ \rightarrow K^+ K_S K_S$
 - $B \rightarrow X_c (\rightarrow K_L)$ validated using a pion enriched sample

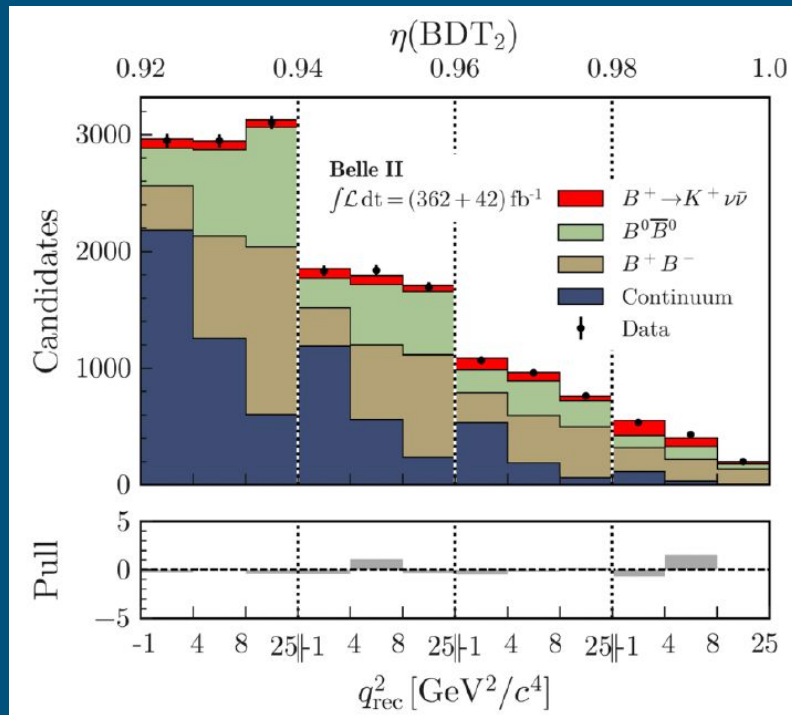
Measurement of BR ($B \rightarrow K \nu \bar{\nu}$)

Phys. Rev. D. 109.112006 (2024)

Binned maximum likelihood fit done to extract signal:

- HT fit: uses Classifier output
- IT fit: uses Classifier output and mass squared of neutrino pair

Final observables: q_{rec}^2 in bins of the second classifier (BDT)



Measurement of BR ($B \rightarrow K \nu \bar{\nu}$)

Inclusive
Tag:

$$\mathcal{B} = (2.7 \pm 0.5 \pm 0.5) \times 10^{-5}$$

3.5 σ significance wrt bkg only hypothesis

2.9 σ deviation from SM

Hadronic
Tag:

$$\mathcal{B} = (1.1^{+0.9 \ +0.8}_{-0.8 \ -0.5}) \times 10^{-5}$$

1.1 σ significance wrt bkg only

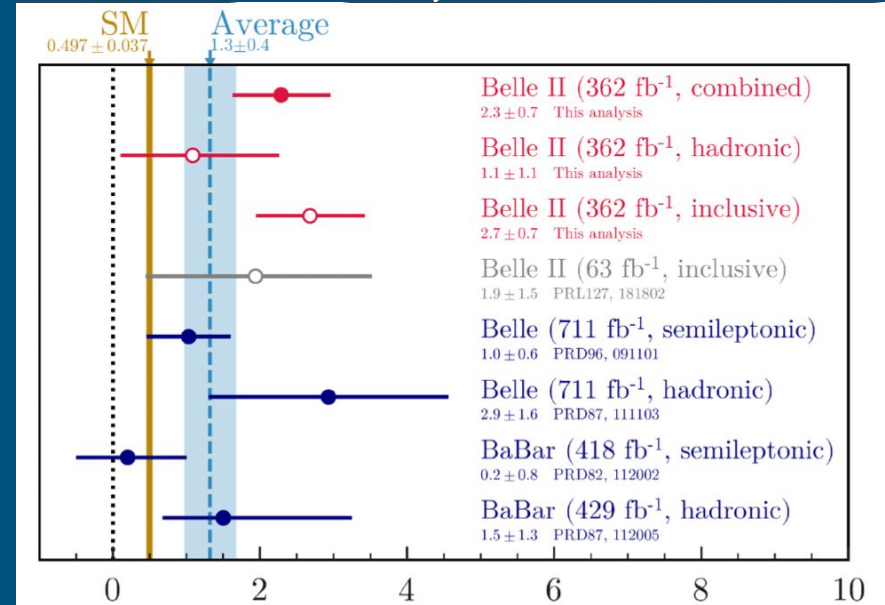
0.6 σ deviation from SM

Combination:

$$\mathcal{B} = (2.3 \pm 0.5^{+0.5}_{-0.4}) \times 10^{-5}$$

3.5 σ significance wrt bkg only

2.7 σ deviation from SM



First evidence for $B \rightarrow K \nu \bar{\nu}$

Conclusions

- New Exclusive V_{ub} measurement from untagged $B \rightarrow \pi/\rho\ell\nu$: Key to understanding exclusive-inclusive tension and important in testing CKM parameters in the context of SM predictions
- New measurement of $R(D^*)$
Important test for SM and probe beyond the SM physics
- Measurement of $R(X)$
Important test for SM and probe beyond the SM physics
- First evidence of $B^+ \rightarrow K^+ \nu\bar{\nu}$, 2.7σ above the SM prediction
Important test for SM and probe beyond the SM physics

$|V_{ub}|$ from $B^0 \rightarrow \pi^- l^+ \nu$ and $B^+ \rightarrow \rho^0 l^+ \nu$

$$\frac{d\Gamma(B \rightarrow \pi l \nu_\ell)}{dq^2 d \cos \theta_{W\ell}} = |V_{ub}|^2 \frac{G_F^2 |\vec{p}_\pi|^3}{32\pi^3} \sin^2 \theta_{W\ell} |f_+(q^2)|^2$$

$$\begin{aligned} \frac{d\Gamma(B \rightarrow \rho l \nu_\ell)}{dq^2 d \cos \theta_{W\ell}} &= |V_{ub}|^2 \frac{G_F^2 |\vec{p}_\rho| q^2}{128\pi^3 m_B^2} \\ &\times \left[\sin^2 \theta_{W\ell} |H_0(q^2)|^2 + (1 - \cos \theta_{W\ell})^2 \frac{|H_+(q^2)|^2}{2} \right. \\ &\quad \left. + (1 + \cos \theta_{W\ell})^2 \frac{|H_-(q^2)|^2}{2} \right], \end{aligned}$$

Measurement of $R(X)$

- **MC corrections are applied:**

Detailed adjustments to MC (FFs, B and D BFs)

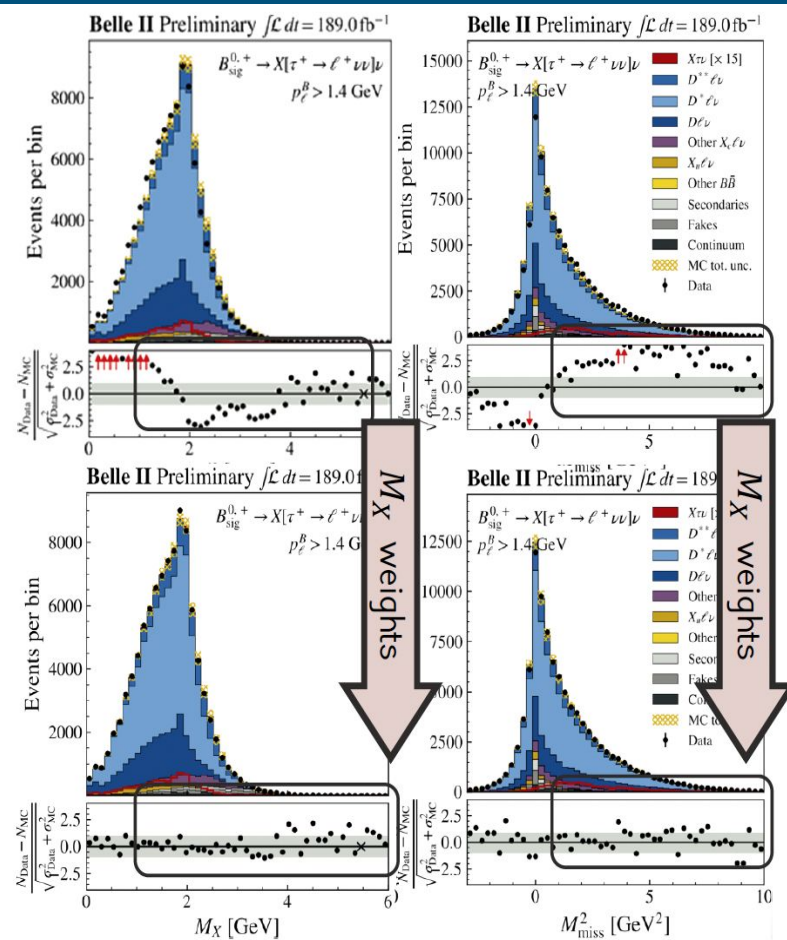
Detailed corrections based on comparisons of simulation with control regions:

low q^2 , low M_{miss}^2 , high M_X .

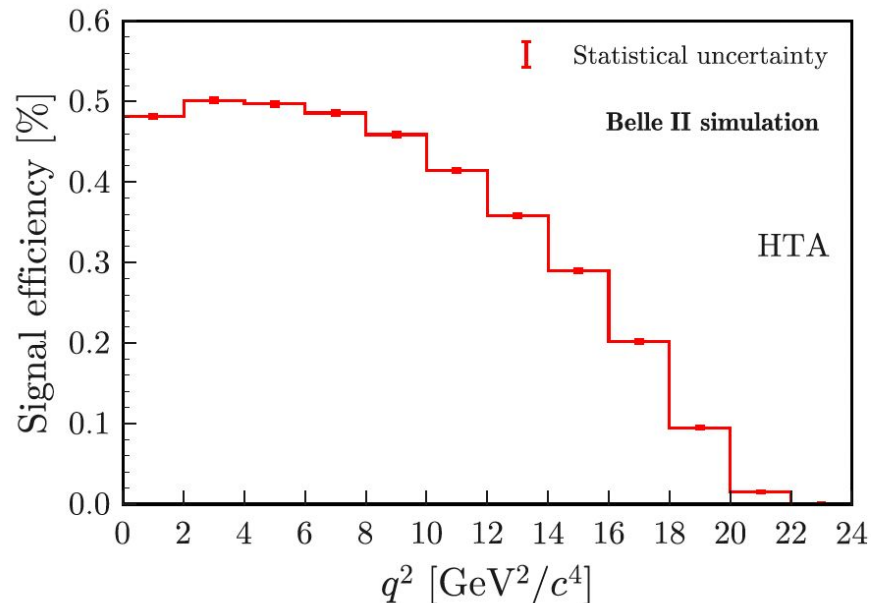
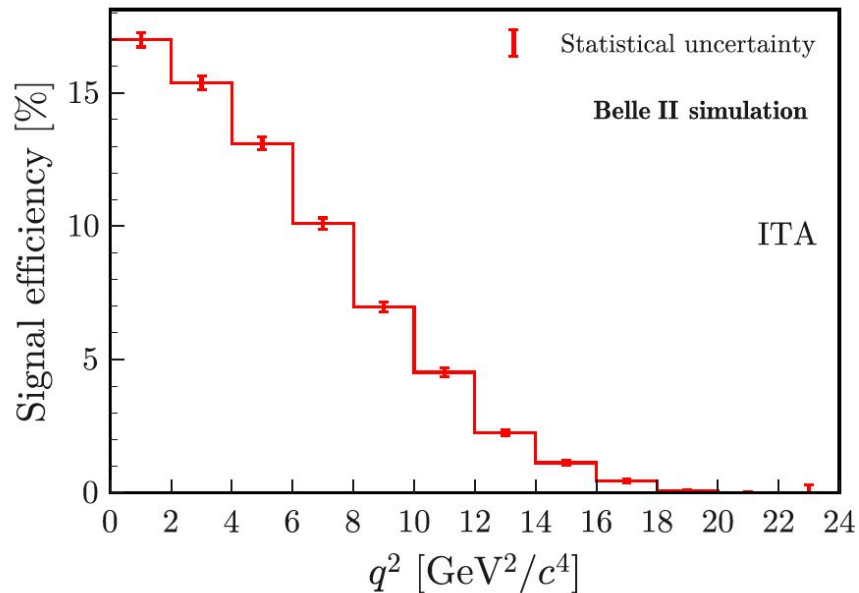
- **Final Fit:** We extract the signal and normalization yields for the electron and muon modes from a simultaneous maximum-likelihood fit to the binned two-dimensional distributions of p_ℓ and M_{miss}^2

Fit components: $X\tau\nu$, $X\ell\nu$, BB background (fakes and secondaries) and continuum (off resonance data)

Measurement of R(X)



Measurement of BR ($B \rightarrow K \nu \bar{\nu}$)



q^2 : di-neutrino mass-squared

$$q_{\text{rec}}^2 = s/(4c^4) + M_K^2 - \sqrt{s}E_K^*/c^4$$