

Search for new phenomena beyond the Standard Model at Belle and Belle II

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on behalf of the Belle II collaboration

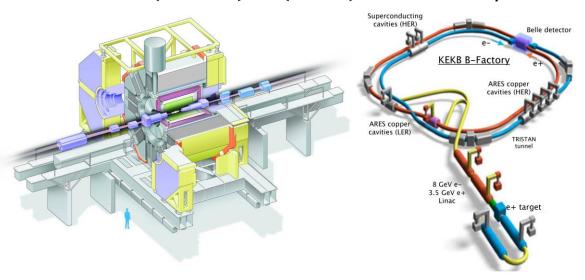
BCVSPIN 2024, Kathmandu, Nepal Dec 9-13, 2024

Belle and Belle II Experiments

- Asymmetric energy collisions of electrons and positrons
- Its energy corresponds to $\sqrt{s} = 10.58$ GeV, which is the resonance energy of $\Upsilon(4S)$
 - $\Upsilon(4S)$ mainly decays into B meson pairs

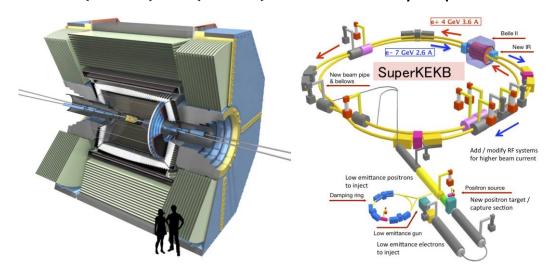
Belle experiment

- **1999 2010**
- $\mathcal{L}_{int} = 1 \ ab^{-1}$
- $e^+(3.5 \text{ GeV}) e^-(8 \text{ GeV})$ accelerated by KEKB



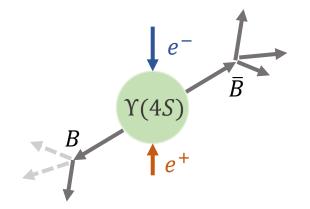
Belle II experiment

- 2019 current
- $\mathcal{L}_{int} = 0.55 \ ab^{-1}$ by November 2024
- $e^+(4 \text{ GeV}) e^-(7 \text{ GeV})$ accelerated by SuperKEKB

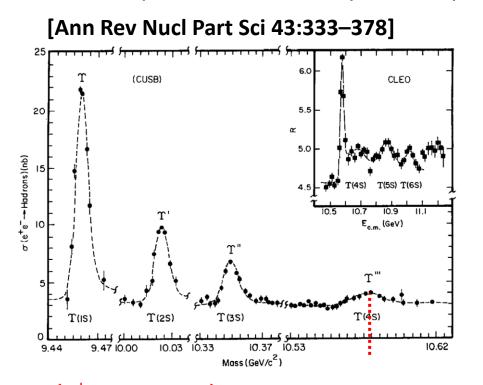


Belle and Belle II Experiments

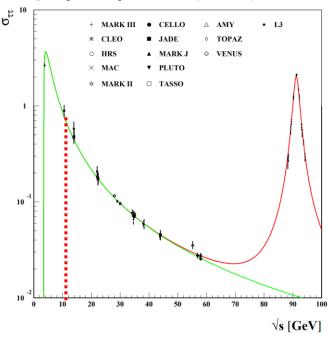
- Entire information of initial states is known in Belle II experiment.
 - → Belle II has an advantage on the decay modes with invisible particles, like neutrinos



• Belle II experiment is not only B factory, but also tau factory.



[Phys.Rept. 274 (1996) 287-376]



$$\sigma(e^+e^- \to \Upsilon(4S)) \sim 1.1 \text{ nb @ 10.58 GeV}$$
 $\sigma(e^+e^- \to \tau^+\tau^-) \sim 0.9 \text{ nb @ 10.58 GeV}$

Overview

Electroweak penguin
$$B^+ \to K^+ \nu \bar{\nu}$$
 [Phys. Rev. D 109, 112006 (2024)]

Lepton flavor violation
$$au^- o \mu^+ \mu^- \mu^-$$
 [JHEP09(2024)062]

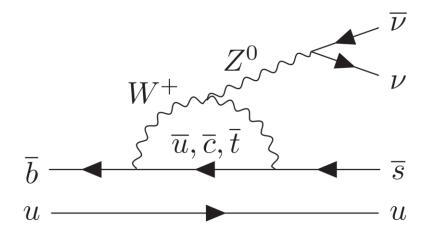
Lepton flavor universality $R(D^*)$ [Phys. Rev. D 110, 072020 (2024)]

$$B^+ \to K^+ \nu \bar{\nu}$$

[Phys. Rev. D 109, 112006 (2024)]



- $B^+ \to K^+ \nu \bar{\nu}$ decay
 - Flavour-changing neutral currents process
 - BR = $(5.6 \pm 0.4) \times 10^{-6}$ at SM [Phys. Rev. D 107, 119903 (2023)]
- This decay can give a clue for non-SM particles
 - Leptoquark [Phys. Rev. D 98, 055003]
 - Axion [Phys. Rev. D 102, 015023]
 - Dark sector mediator [Phys. Rev. D 101, 095006]

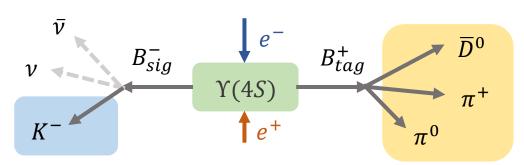


experiment	Upper limit (90% CL)	\mathcal{L}_{int}	Tagging method	reference
BABAR	3.7×10^{-5}	$429 fb^{-1}$	hadronic	Phys. Rev. D 87, 112005 (2013)
BABAR	1.3×10^{-5}	$418 fb^{-1}$	semileptonic	Phys. Rev. D 82, 112002 (2010)
Belle	5.5×10^{-5}	$711 fb^{-1}$	hadronic	Phys. Rev. D 87, 111103 (2013)
Belle	1.9×10^{-5}	$711 fb^{-1}$	semileptonic	Phys. Rev. D 96, 091101 (2018)
Belle II	4.1×10^{-5}	$63 fb^{-1}$	inclusive	Phys. Rev. Lett. 127, 181802 (2021)



$$B^+ \to K^+ \nu \bar{\nu}$$

- $362 fb^{-1}$ on-resonance data is used for this analysis
- Two tagging methods are done
 - hadronic tagging analysis (HTA)
 - inclusive tagging analysis (ITA)
- In HTA, one of B meson is reconstructed by hadronic decay modes

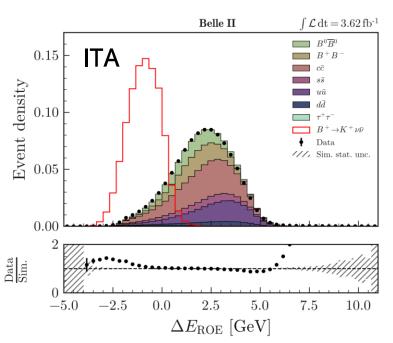


- Exact kinematics of B_{tag} is known
- high purity
- low efficiency

• In ITA, the second B meson is not explicitly reconstructed

- * ROE: rest of event
 Information of remaining particles (ROE) is used
- low purity
- high efficiency

- For the background suppression, boosted decision tree (BDT) is used as the multivariate analysis technique
 - For HTA, total 12 variables are used
 - most powerful variable:
 - \rightarrow sum of remaining energy in the electromagnetic calorimeter ($E_{
 m extra}$)
 - For ITA, total 12 and 35 variables are used for two consecutive BDTs
 - most powerful variables:
 - \Rightarrow Energy of ROE in c.m. frame $-\frac{\sqrt{s}}{2}$ (ΔE_{ROE})
 - \rightarrow event shape variable $(\cos((\text{thrust}_K), \text{thrust}_{ROE}))$



[Phys. Rev. D 109, 112006 (2024)]

HTA

0.0

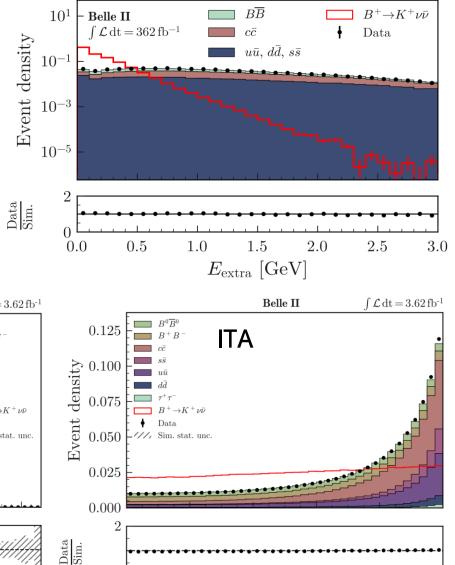
0.2

0.4

 $\cos(\text{thrust}_K, \text{thrust}_{\text{ROE}})$



0.8



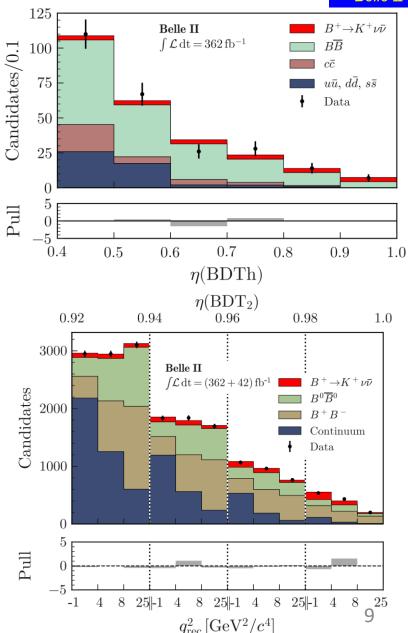
$$B^+ \to K^+ \nu \bar{\nu}$$

- Binned maximum likelihood fit is done to extract the signal yield
- Signal regions
 - For HTA, signal yield extraction is done on $\eta(\mathrm{BD}T_h)$ space
 - $\neg \eta(BDT_h)$: variables related to the efficiency as a function of BDT cut
 - For ITA, signal yield extraction is done on $\eta(\mathrm{BDT}_2) \times q_{\mathrm{rec}}^2$ space
 - $\neg \eta(BDT_2)$: variables related to the efficiency as a function of BDT cut
 - $q_{\rm rec}^2$: invariant mass square of the neutrino pair

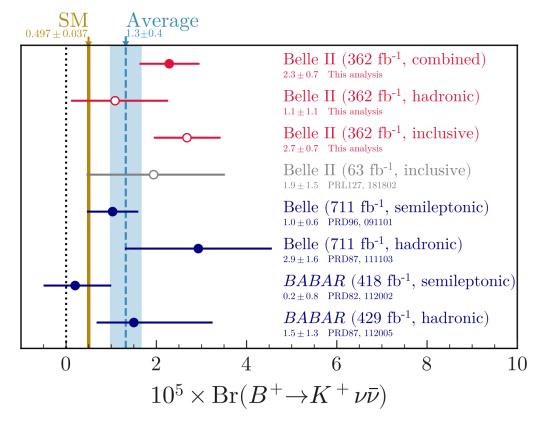
 $q_{\rm rec}^2 = s/(4c^4) + M_K^2 - \sqrt{s}E_K^*/c^4$ with assuming the signal B to be at rest in c.m. frame

[Phys. Rev. D 109, 112006 (2024)]









Hadronic tag:

$$BR(B^+ \to K^+ \nu \bar{\nu}) = \left[1.1^{+0.9}_{-0.8} (\text{stat})^{+0.8}_{-0.5} (\text{syst}) \right] \times 10^{-5}$$

• Inclusive tag:

$$BR(B^+ \to K^+ \nu \bar{\nu}) = [2.7 \pm 0.5(\text{stat}) \pm 0.5(\text{syst})] \times 10^{-5}$$

Combined result:

$$BR(B^+ \to K^+ \nu \bar{\nu}) = \left[2.3 \pm 0.5(\text{stat})^{+0.5}_{-0.4}(\text{syst})\right] \times 10^{-5}$$

 \rightarrow first evidence for the $B^+ \rightarrow K^+ \nu \overline{\nu}$ decay (3.5 σ)



• Compatibility with SM: 2.7σ

$$\tau^- \rightarrow \mu^+ \mu^- \mu^-$$
[JHEP09(2024)062]



$$\tau^- \to \mu^+ \mu^- \mu^-$$

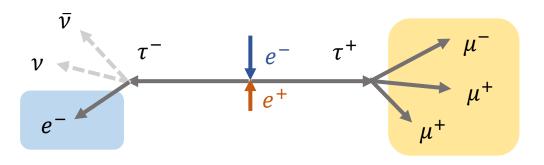
- Belle II experiment is not only B factory but also tau factory
- $\tau^- \rightarrow \mu^+ \mu^- \mu^-$ decay
 - Hard to occur in SM (BR $\sim \mathcal{O}(10^{-50})$) [Eur. Phys. J. C 79 (2019) 84]
- This decay can be enhanced by new physics
 - Inverse Seesaw mechanism [J. Phys. Conf. Ser. 888 (2017) 012029]
- $424 fb^{-1}$ data is used for the analysis

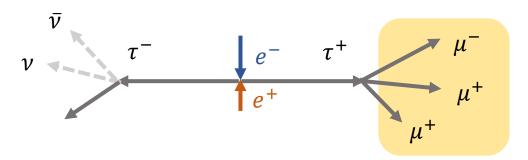
experiment	Upper limit (90% CL)	\mathcal{L}_{int}	Tagging method	reference
CLEO	1.9×10^{-6}	$4.79 fb^{-1}$	one-prong	Phys. Rev. D 57 (1998) 5903
BABAR	3.3×10^{-8}	$468 fb^{-1}$	one-prong	Phys. Rev. D 81 (2010) 111101
LHCb	4.6×10^{-8}	$3 fb^{-1}$	-	JHEP 02 (2015) 121
ATLAS	3.8×10^{-7}	$20.3 fb^{-1}$	-	Eur. Phys. J. C 76 (2016) 232
CMS	8.0×10^{-8}	$33.2 fb^{-1}$	-	JHEP 01 (2021) 163



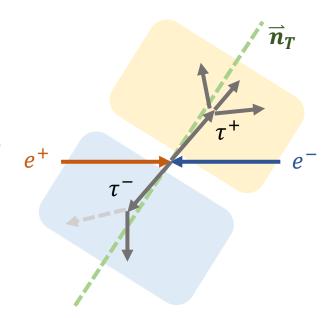
$$\tau^- \rightarrow \mu^+ \mu^- \mu^-$$

- Two analysis methods are done in this analysis
 - one-prong tagging analysis (for the validation)
 - inclusive tagging analysis





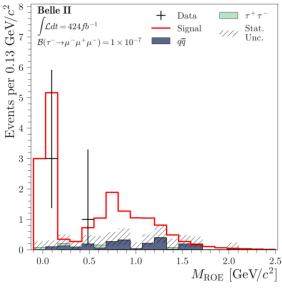
- The space is divided into two hemispheres
 - determine a vector \vec{n}_T that the sum of inner products with visible particles' momentum is maximized
 - lacktriangle Then, we can define two hemispheres by the plane perpendicular to $ec{n}_T$
 - All three μ are required to be included in the same hemisphere

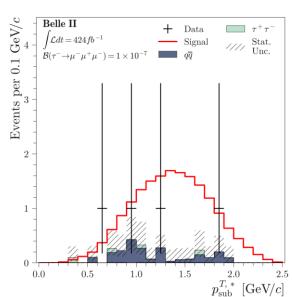


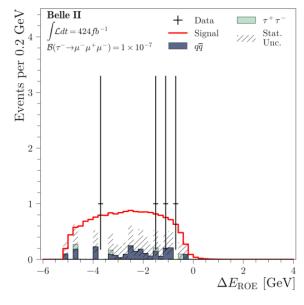


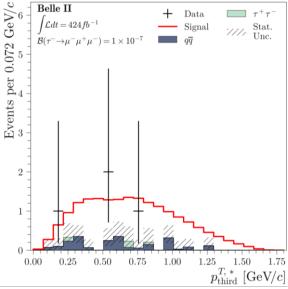
$\tau^- \rightarrow \mu^+ \mu^- \mu^-$

- BDT is used to suppress backgrounds
 - total 32 variables are used
 - the most discriminating variables:
 - □ mass of ROE (M_{ROE})
 - □ Energy of ROE in c.m. frame $-\frac{\sqrt{S}}{2}$ (ΔE_{ROE})
 - $\ ^{\square}$ transverse momentum of the second highest momentum muon $(p_{\mathrm{sub}}^{T,*})$
 - $^{\Box}$ transverse momentum of the lowest momentum muon ($p_{\mathrm{thrid}}^{T,*}$)
 - cross-validation (k-folding) algorithm † is used to reduce the impacts from the statistical fluctuation

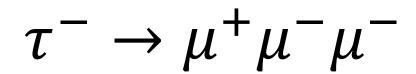




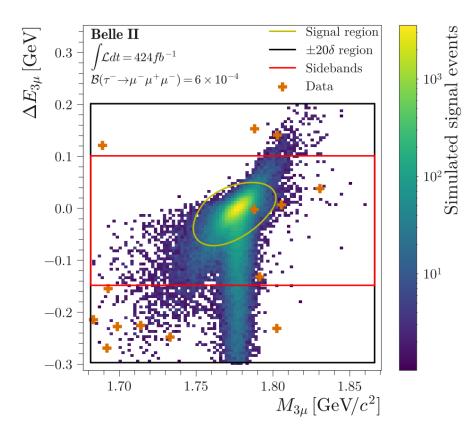








- Counting method is used in $(M_{3\mu}, \Delta E_{3\mu})$ plane
 - $M_{3\mu}$: invariant mass of three muons
 - $\Delta E_{3\mu}$: Energy of three muons in c.m. frame $-\frac{\sqrt{s}}{2}$
- The signal region and sideband region are defined
 - Signal region (yellow line):
 - elliptical region is obtained from the MC sample
 - $^{\Box}$ $\pm 5~\delta$ region, where δ is expected resolution
 - Sideband region (region between red and yellow lines)
 - $\simeq \pm 20 \ \delta_{M}$, $\pm 10 \ \delta_{\Delta E}$ wide rectangular region
- The number of expected background is obtained from the
 2D plane (BDT output) X (distance from signal peak)





$$\tau^- \rightarrow \mu^+ \mu^- \mu^-$$

- Result
 - $N_{\rm exp} = 0.7^{+0.6}_{-0.5}$: the expected number of background events
 - $N_{obs} = 1$: the number of observed events

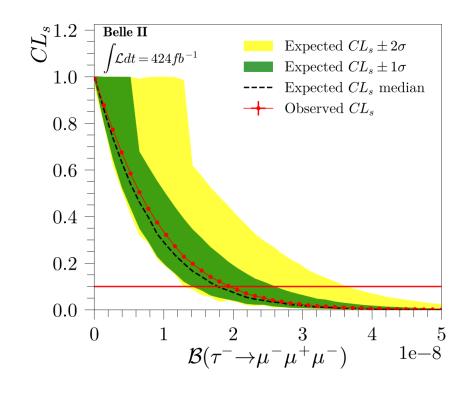
■
$$BR(\tau^- \to \mu^+ \mu^- \mu^-) = (2.1^{+5.1}_{-2.4} \pm 0.4) \times 10^{-9}$$

$$\Box BR(\tau^- \to \mu^+ \mu^- \mu^-) = \frac{N_{obs} - N_{exp}}{\mathcal{L} \times 2\sigma_{\tau\tau} \times \epsilon_{3\tau}}$$

■ Upper limit of branching ratio = 1.9×10^{-8} at 90% confidence level

→ World's best limit

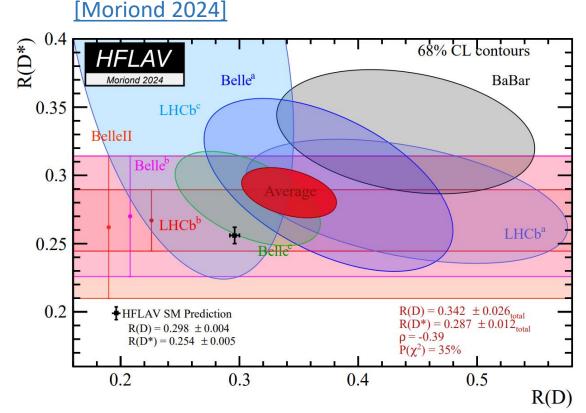




[Phys. Rev. D 110, 072020 (2024)]



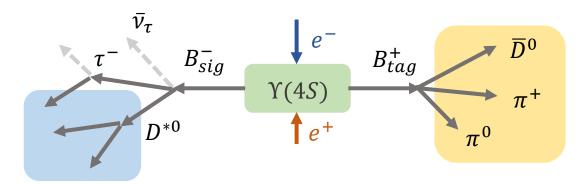
- Measuring $R(D^{(*)})$ is the direct test for the lepton flavour universality (LFU)
 - $R(D^{(*)}) = \frac{BR(\overline{B} \to D^{(*)} \tau \overline{\nu}_{\tau})}{BR(\overline{B} \to D^{(*)} \ell \overline{\nu}_{\ell})}$
 - In SM, [Phys. Rev. D 107, 052008]
 - $R(D) = 0.298 \pm 0.004$
 - $R(D^*) = 0.254 \pm 0.005$
 - Several systematic uncertainties are canceled for $R(D^{(*)})$, like quark mixing element $|V_{cb}|$
 - $R(D^{(*)})$ can be changed by new physics
 - Leptoquark [Phys. Rev. D 104, 055017]
 - W' boson [JHEP12(2016)059]



 \bullet Currently, it shows some tension from SM prediction: $\sim 3.17 \sigma$



- $189 fb^{-1}$ on-resonance data is used for this analysis
- Hadronic tagging method is used

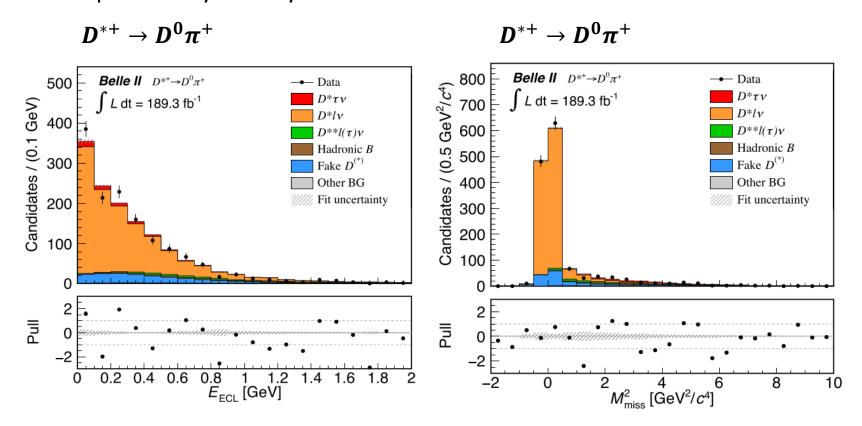


• The following decay modes are reconstructed for the signal side

particle	Decay modes	remark
τ	$e^-ar{ u}_e u_ au$ $\mu^-ar{ u}_\mu u_ au$	Leptonic mode
D^{*+}	$D^{0}\pi^{+}$ $D^{+}\pi^{0}$	
D^{*0}	$D^{0}\pi^{0}$	
D^+	$K^{-}\pi^{+}\pi^{+}$ $K_{S}^{0}\pi^{+}$ $K^{-}K^{+}\pi^{+}$	
D^{0}	$K^{-}\pi^{+}\pi^{0}$ $K^{-}\pi^{+}\pi^{-}\pi^{+}$ $K_{S}^{0}\pi^{+}\pi^{-}\pi^{0}$ $K^{-}\pi^{+}$ $K_{S}^{0}\pi^{+}\pi^{-}$ $K_{S}^{0}\pi^{0}$ $K^{-}K^{+}$ $\pi^{-}\pi^{+}$	

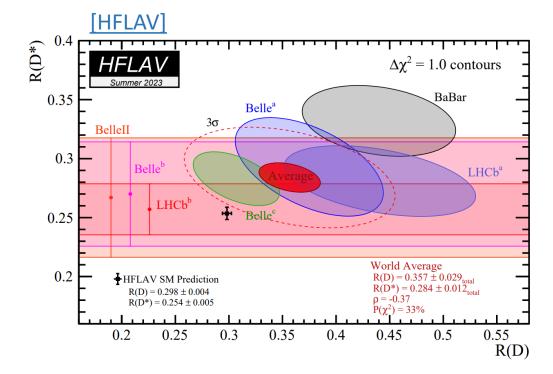


- To extract the signal yield, extended binned maximum likelihood fit is done
- Signal region
 - $E_{\text{ECL}} \times M_{\text{miss}}^2$ * $E_{\text{ECL}} = E_{\text{extra}}$
- ullet The probability density functions are constructed for each D^* modes





- Result
 - $R(D^*) = 0.262^{+0.041}_{-0.039}(stat)^{+0.035}_{-0.032}(syst)$
 - → Statistical uncertainty ($^{+15.7\%}_{-14.7\%}$) is comparable to Belle result (13.0%), even though this analysis uses much smaller data size (189 fb^{-1} vs 711 fb^{-1})
 - Consistent with SM prediction



Summary

- Belle II experiment has advantages in B and tau physics
 - Target energy is appropriate for B and tau production
 - decays with invisible particles can be analyzed
- Broad range of analysis have been successfully done in Belle II experiment
 - EWP: $B^+ \rightarrow K^+ \nu \bar{\nu}$ \rightarrow first evidence for the $B^+ \rightarrow K^+ \nu \bar{\nu}$ decay (3.5 σ)
 - LFV: $\tau^- \rightarrow \mu^+ \mu^- \mu^-$ → World's best result
 - LFU: *R*(*D**)
 - → comparable statistical uncertainty, with much smaller data size, compared to Belle experiment

Backup



$$B^+ \to K^+ \nu \bar{\nu}$$

 BDT_1



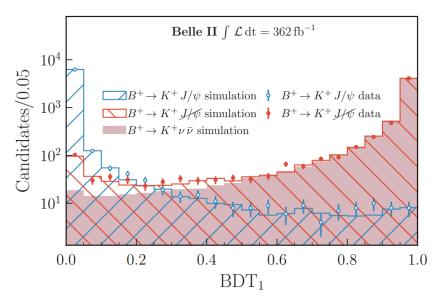
 BDT_2

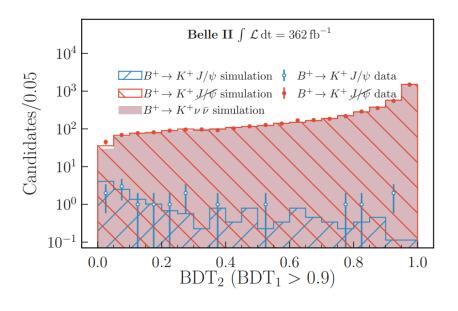
12 input variables are used

• discriminating variables: Energy of ROE in c.m. frame $-\frac{\sqrt{s}}{2}$

35 input variables are used

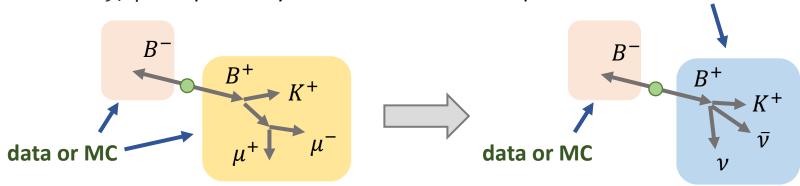
discriminating variables:cos((thrust_K), thrust_{ROE})

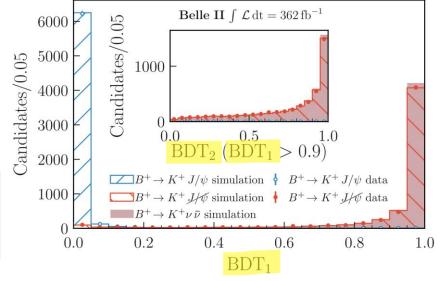




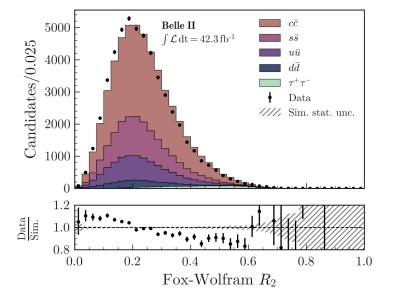


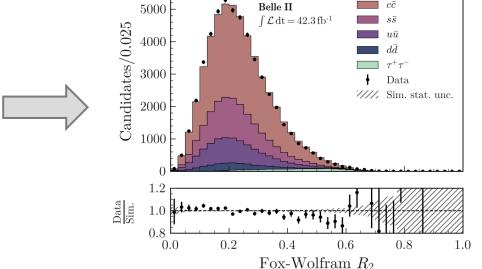
- $B^+ \to K^+ J/\psi \ (\to \mu^+ \mu^-)$ is used for the signal efficiency validation
 - K^+J/ψ is replaced by $K^+\nu\bar{\nu}$ Monte Carlo sample





• The lower beam energy sample is used to correct the $e^+e^- \to q\bar{q}$ (q=u,d,s,c) background





MC

- Different BDT is trained to distinguish between data and MC
- Output of this BDT is used as a correction factor



TABLE I. Sources of systematic uncertainty in the ITA, corresponding correction factors (if any), their treatment in the fit, their size, and their impact on the uncertainty of the signal strength μ . The uncertainty type can be "Global", corresponding to a global normalization factor common to all SR bins, or "Shape", corresponding to a bin-dependent uncertainty. Each source is described by one or more nuisance parameters (see the text for more details). The impact on the signal strength uncertainty σ_u is estimated by excluding the source from the minimization and subtracting in quadrature the resulting uncertainty from the uncertainty of the nominal fit.

Source	Correction	Uncertainty type, parameters	Uncertainty size	Impact on σ_{μ}	
Normalization of $B\bar{B}$ background Normalization of continuum background		Global, 2 Global, 5	50% 50%	0.90 0.10	data/MC for off-resonance sample
Leading B-decay branching fractions	2 1 1 (0(100%)	Shape, 6	O(1%)	0.22	•
Branching fraction for $B^+ \to K^+ K_L^0 K_L^0$ p-wave component for $B^+ \to K^+ K_S^0 K_L^0$	q^2 dependent $O(100\%)$ q^2 dependent $O(100\%)$	Shape, 1 Shape, 1	20% 30%	0.02	potential difference between $B^+ \to K^+ K_L^0 K_L^0$
Branching fraction for $B \to D^{**}$ Branching fraction for $B^+ \to K^+ n\bar{n}$	q^2 dependent $O(100\%)$	Shape, 1 Shape, 1	50% 100%	0.42 0.20	and $B^+ \rightarrow K^+ K_S^0 K_S^0$
Branching fraction for $D \to K_L^0 X$ Continuum-background modeling, BDT _c	+30% Multivariate $O(10%)$	Shape, 1 Shape, 1	10% 100% of correction	0.14 0.01	and b An Ing Ing
Integrated luminosity	white o(10%)	Global, 1	1%	< 0.01	
Number of $B\bar{B}$ Off-resonance sample normalization		Global, 1 Global, 1	1.5% 5%	0.02 0.05	
Track-finding efficiency Signal-kaon PID	p, θ dependent $O(10-100\%)$	Shape, 1 Shape, 7	$0.3\% \\ O(1\%)$	0.20 0.07	
Photon energy Hadronic energy	-10%	Shape, 1 Shape, 1	0.5% 10%	0.08 0.37	
$K_{\rm L}^0$ efficiency in ECL	-17%	Shape, 1	8.5%	0.22	
Signal SM form-factors Global signal efficiency	q^2 dependent $O(1\%)$	Shape, 3 Global, 1	O(1%) 3%	0.02 0.03	
Simulated-sample size		Shape, 156	O(1%)	0.52	26



TABLE II. Sources of systematic uncertainty in the HTA (see caption of Table I for details).

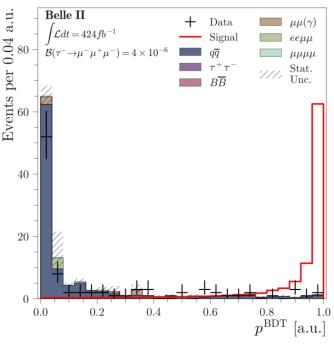
Source	Correction	Uncertainty type, parameters	Uncertainty size	Impact on σ_{μ}
Normalization of $B\bar{B}$ background		Global, 1	30%	0.91
Normalization of continuum background		Global, 2	50%	0.58
Leading <i>B</i> -decay branching fractions		Shape, 3	O(1%)	0.10
Branching fraction for $B^+ \to K^+ K_L^0 K_L^0$	q^2 dependent $O(100\%)$	Shape, 1	20%	0.20
Branching fraction for $B \to D^{**}$. ,	Shape, 1	50%	< 0.01
Branching fraction for $B^+ \to K^+ n\bar{n}$	q^2 dependent $O(100\%)$	Shape, 1	100%	0.05
Branching fraction for $D \to K_{\perp}^0 X$	+30%	Shape, 1	10%	0.03
Continuum-background modeling, BDT _c	Multivariate $O(10\%)$	Shape, 1	100% of correction	0.29
Number of $B\bar{B}$		Global, 1	1.5%	0.07
Track finding efficiency		Global, 1	0.3%	0.01
Signal-kaon PID	p, θ dependent $O(10-100\%)$	Shape, 3	O(1%)	< 0.01
Extra-photon multiplicity	n_{yextra} dependent $O(20\%)$	Shape, 1	O(20%)	0.61
$K_{\rm L}^0$ efficiency	•	Shape, 1	17%	0.31
Signal SM form-factors	q^2 dependent $O(1\%)$	Shape, 3	O(1%)	0.06
Signal efficiency	. ,	Shape, 6	16%	0.42
Simulated-sample size		Shape, 18	O(1%)	0.60

data/MC for pion enriched sampledata/MC for off-resonance sample



$$\tau^- \rightarrow \mu^+ \mu^- \mu^-$$

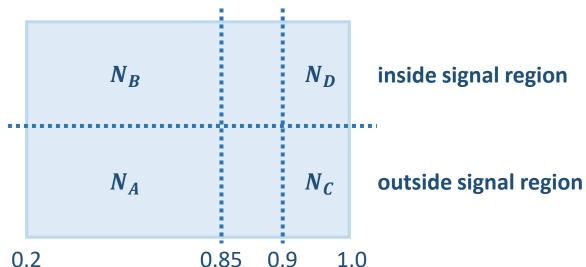
- The validation is done on the sideband region
 - Agreement on (BDT output) is checked
 - After the BDT selection,
 - □ The expected number of event in sideband = $2.0^{+0.7}_{-0.5}$
 - The observed number of event in sideband = 3



• The number of expected background is obtained from (BDT output) and distance from signal peak

BDT output

• expected $N_{\rm D} = N_C \times \frac{N_B}{N_A}$





$\tau^- \to \mu^+ \mu^- \mu^-$

		Uncer	tainty (%)	
Quantity	Source	Low	High	
	PID	2.1	2.4	
	Tracking	1.0	1.0	
	Trigger	0.9	0.9	
$arepsilon_{3\mu}$	BDT	1.5	1.5 ←	use $ au^- o \pi^- \pi^+ \pi^- \nu_ au$ sample
	Signal region	3.9	2.9 ←	change the signal region definition $\pm \delta$
$N_{ m exp}$	Momentum Scale	16	16 ←	change the scale factor of momentum obtained from $D^0 \to K^-\pi^+$
${\cal L}$		0.6	0.6	
$\sigma_{ au au}$		0.3	0.3	



experiment	R(D)	$R(D^*)$	\mathcal{L}_{int}	Tagging method	reference
Belle	0.307	0.283	$711 fb^{-1}$	semileptonic	Phys. Rev. Lett. 124, 161803 (2020)
LHCb	0.441	0.281	$3 f b^{-1}$	-	Phys. Rev. Lett. 131, 111802 (2023)
LHCb	-	0.267	$2 f b^{-1}$	-	Phys. Rev. D 108, 012018 (2023)
Belle II	-	0.262	$189 fb^{-1}$	hadronic	Phys. Rev. D 110, 072020 (2024)
LHCb	0.249	0.402	$2 f b^{-1}$	-	arXiv:2406.03387 (2024)



- ullet Dominant background comes from the misreconstructed D^* candidates:
 - (Correctly reconstructed D) + (low-momentum pion not from D^*)
 - misreconstructed D with low-momentum pion
- ullet This fake D^* yield is calibrated from the sideband for each D^* mode
 - The sideband region is defined in ΔM_{D^*} region, where $\Delta M_{D^*} = M_{D^*} - M_D$
 - The fit is done on the sideband, to obtain the data-simulation ratio of fake D^* yield

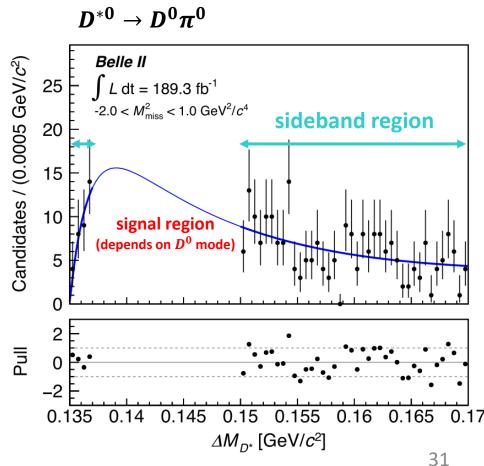




TABLE VIII. Summary of systematic uncertainties on $R(D^*)$.

Source	Uncertainty
PDF shapes	change the energy shift for E_{ECL}
Simulation sample size	change the smearing factor for $M_{ m miss}$
$\bar{B} \to D^{**} \ell^- \bar{\nu}_{\ell}$ branching fractions	$^{+4.8\%}_{-3.5\%}$
Fixed backgrounds	$^{+2.7\%}_{-2.3\%}$
Hadronic B decay branching fractions	$^{+2.1\%}_{-2.1\%}$
Reconstruction efficiency	$^{+2.0\%}_{-2.0\%}$
Kernel density estimation	$^{+2.0\%}_{-0.8\%}$
Form factors	$^{+0.5\%}_{-0.1\%}$
Peaking background in ΔM_{D^*}	$^{+0.4\%}_{-0.4\%}$
$\tau^- \to \ell^- \nu_\tau \bar{\nu}_\ell$ branching fractions	$^{+0.2\%}_{-0.2\%}$
$R(D^*)$ fit method	$^{+0.1\%}_{-0.1\%}$
Total systematic uncertainty	+13.5% -12.3%



$$\tau \to \ell V^0$$

- This decay can be enhanced by new physics $(BR \sim \mathcal{O}(10^{-10}-10^{-8}))$
 - Unparticle [Phys. Lett. B 677 (2009) 150]
 - Type-III seesaw mechanism [Phys. Rev. D 81, 113003 (2010)]
 - Littlest Higgs [JHEP09(2022)144]
- $980 fb^{-1}$ data is used for the analysis

experiment	modes	\mathcal{L}_{int}	reference
CLEO	$ ho^0$, ϕ , K^{*0} , \overline{K}^{*0}	$4.79 fb^{-1}$	Phys. Rev. D 57, 5903 (1998)
Belle	$ ho^0$, ϕ , K^{*0} , \overline{K}^{*0}	$158 fb^{-1}$	Phys.Lett.B 640 (2006)
Belle	ω , $ ho^0$, ϕ , K^{*0} , \overline{K}^{*0}	$543 fb^{-1}$	Phys.Lett.B 664 (2008)
Babar	$ ho^0$, ϕ , K^{*0} , \overline{K}^{*0}	$451 fb^{-1}$	Phys.Rev.Lett. 103 (2009) 021801
Belle	ω , $ ho^0$, ϕ , K^{*0} , \overline{K}^{*0}	$854 fb^{-1}$	Phys.Lett.B 699 (2011)



$au o \ell V^0$

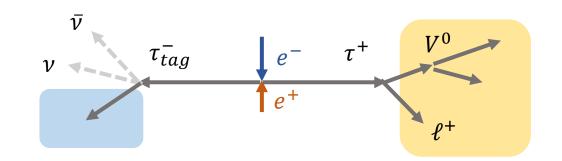
ullet Several V^0 particles are reconstructed for signal side

V^0 particle	Decay modes
$ ho^{0}$	$\pi^+\pi^-$
ϕ	K^+K^-
ω	$\pi^+\pi^-\pi^0$
K^{*0}	$K^+\pi^-$
\overline{K}^{*0}	$K^-\pi^+$

• The other side of tau is also reconstructed

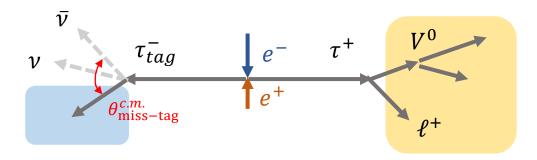
$ au_{tag}$ decay modes	Remarks
$\ell^\pm u u \pi^\pm u \pi^\pm \pi^0 u \pi^\pm \pi^0 \pi^0 u$	One charged track
$\pi^\pm\pi^\mp\pi^\pm u$	Three charged tracks

This side is called "tag side"



$au ightarrow \ell V^0$

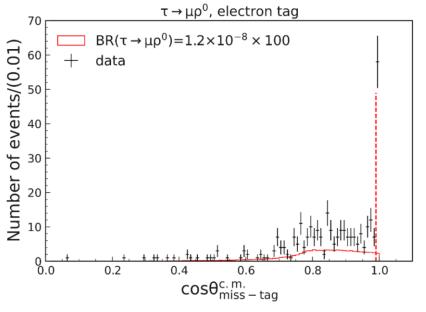
- To suppress the backgrounds, several cuts are applied
 - $\cos \theta_{\rm miss-tag}^{c.m.} > 0$, where $\theta_{\rm miss-tag}^{c.m.}$ is the angle between reconstructed tag side momentum and missing momentum

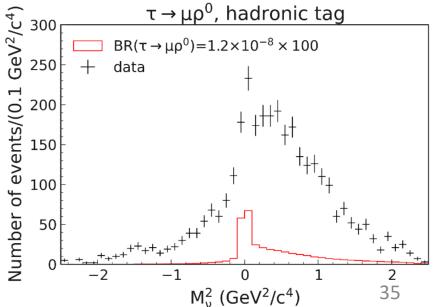


- For some V^0 modes, $\cos \theta_{\rm miss-tag}^{c.m.} < 0.99$ or 0.97 \rightarrow to suppress low-multiplicity background events
- BDT is trained to suppress more backgrounds
 - Total 9 or 11 variables, depending on V^0 modes
 - Example of input variable: missing mass squre (M_{ν}^2)











$\tau \to \ell V^0$

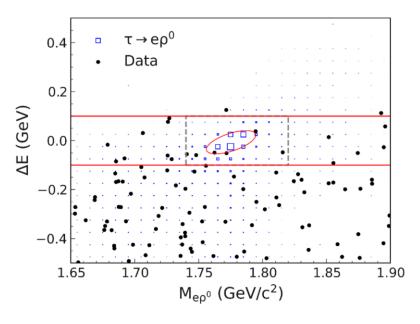
- Signal region is defined on $(M_{\ell V^0}, \Delta E)$ plane
 - $M_{\ell V^0}$: invariant mass of ℓV^0 candidate
 - ΔE : Energy of ℓV^0 candidate in c.m. frame $-\frac{\sqrt{s}}{2}$
 - Signal region (red elliptical line):
 - The size of ellipse is determined to maximize figure-of-merit (FOM)

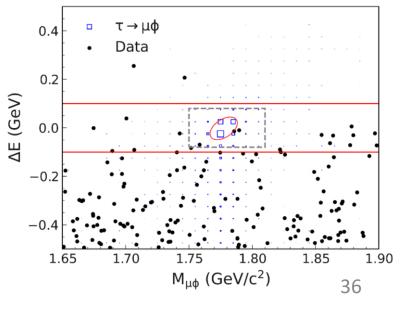
$$POM = \frac{\epsilon}{\frac{\alpha}{2} + \sqrt{N_{BK}}}$$

confidence coefficient

expected background yield

- Sideband region (region outside gray box and between red lines)
 - The number of expected background is obtained from the sideband region







$\tau \to \ell V^0$

Mode	ε (%)	$N_{ m BG}$	$\sigma_{\rm syst}$ (%)	$N_{ m obs}$	$\mathcal{B}_{\text{obs}} (\times 10^{-8})$
$\tau^{\pm} \to \mu^{\pm} \rho^0$	7.78	$0.95\pm0.20({\rm stat.}) \pm0.15({\rm syst.})$	4.6	0	< 1.7
$\tau^\pm \to e^\pm \rho^0$	8.49	$0.80\pm0.27({\rm stat.}) \pm0.04({\rm syst.})$	4.4	1	< 2.2
$ au^{\pm} o \mu^{\pm} \phi$	5.59	$0.47 \pm 0.15 (\text{stat.}) \pm 0.05 (\text{syst.})$	4.8	0	< 2.3
$ au^{\pm} o e^{\pm} \phi$	6.45	$0.38 \pm 0.21 (\text{stat.}) \pm 0.00 (\text{syst.})$	4.5	0	< 2.0
$ au^{\pm} ightarrow \mu^{\pm} \omega$	3.27	$0.32 \pm 0.23 (\text{stat.}) \pm 0.19 (\text{syst.})$	4.8	0	< 3.9
$ au^{\pm} o e^{\pm} \omega$	5.41	$0.74 \pm 0.43 (\text{stat.}) \pm 0.06 (\text{syst.})$	4.5	0	< 2.4
$\tau^{\pm} \to \mu^{\pm} K^{*0}$	4.52	$0.84 \pm 0.25 (\text{stat.}) \pm 0.31 (\text{syst.})$	4.3	0	< 2.9
$\tau^{\pm} \to e^{\pm} K^{*0}$	6.94	$0.54 \pm 0.21 (\text{stat.}) \pm 0.16 (\text{syst.})$	4.1	0	< 1.9
$ au^{\pm} o \mu^{\pm} \overline{K}^{*0}$	4.58	$0.58 \pm 0.17 (stat.) \pm 0.12 (syst.)$	4.3	1	< 4.3
$ au^{\pm} o e^{\pm} \overline{K}^{*0}$	7.45	$0.25\pm0.11({\rm stat.}) \pm0.02({\rm syst.})$	4.1	0	< 1.7



