

# Update on Bhabha $A_{LR}$ Studies

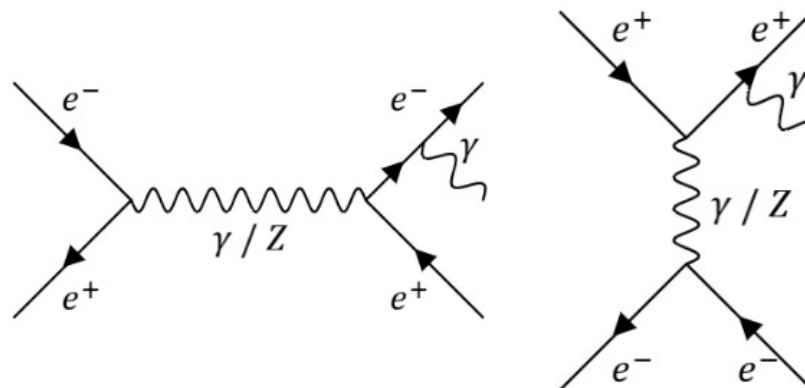
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# Comparing Two NLO Theory Calculations of $A_{LR}$

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We compare calculations of the ReneSANCe Monte Carlo generator

[R. Sadykov and V. Yermolchyk, “*Polarized NLO EW cross section calculations with ReneSANCe*”, Computer Physics Communications 256, 107445 (2020)]

with those of an independent NLO calculation

[A. G. Aleksejevs, S. G. Barkanova, Y. M. Bystritskiy, and V. A. Zykunov, “*Electroweak Corrections with Allowance for Hard Bremsstrahlung in Polarized Bhabha Scattering*”, Physics of Atomic Nuclei 83, 463 (2020)]

and determine the level of agreement

# Comparing Two NLO Theory Calculations of $A_{LR}$

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To compare ReneSANCe calculations to those of Aleksejevs *et al* the following ReneSANCe default SM parameters were changed to correspond to those in Aleksejevs *et al*:

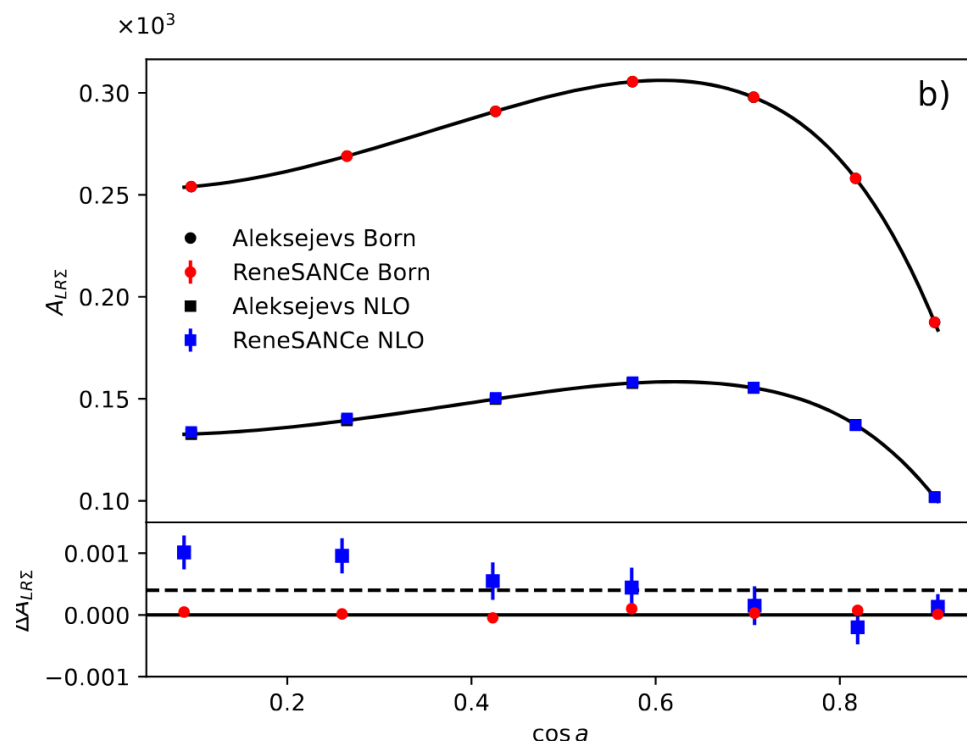
widths of the W boson and the top quark are set to 0,  
 $M_{\text{Higgs}}=125\text{GeV}$ ,  $M_Z=91.1876$ ,  $M_W=80.4628\text{GeV}$ ,  
 $M_u=69.83\text{MeV}$ ,  $M_d=69.84\text{MeV}$ ,  $M_s=0.15\text{GeV}$ ,  $M_c=1.2\text{GeV}$ ,  
 $M_b=4.6\text{GeV}$ ,  $M_t=174\text{GeV}$

CM energy = 10.577 GeV

soft photon cutoff,  $\omega_{\text{me}}$ , set to 0.002

(Note that earlier comparisons had different  $\omega_{\text{me}}$  following advice of A. Aleksejevs, likely a misunderstanding.)

# Comparing Two NLO Theory Calculations of $A_{LR}$



- Comparison of calculations of integrated  $A_{LR}$  in Bhabhas from Aleksejevs *et al* and ReneSANCe for an angular acceptance of final-state electron angle “a” integrated between  $\alpha$  and  $180^\circ - \alpha$ . Line is a cubic spline.
- The average absolute difference between the calculations is  $4.4 \times 10^{-7}$  equivalent to a relative difference of 0.3%

# Sensitivity to $A_{LR}$

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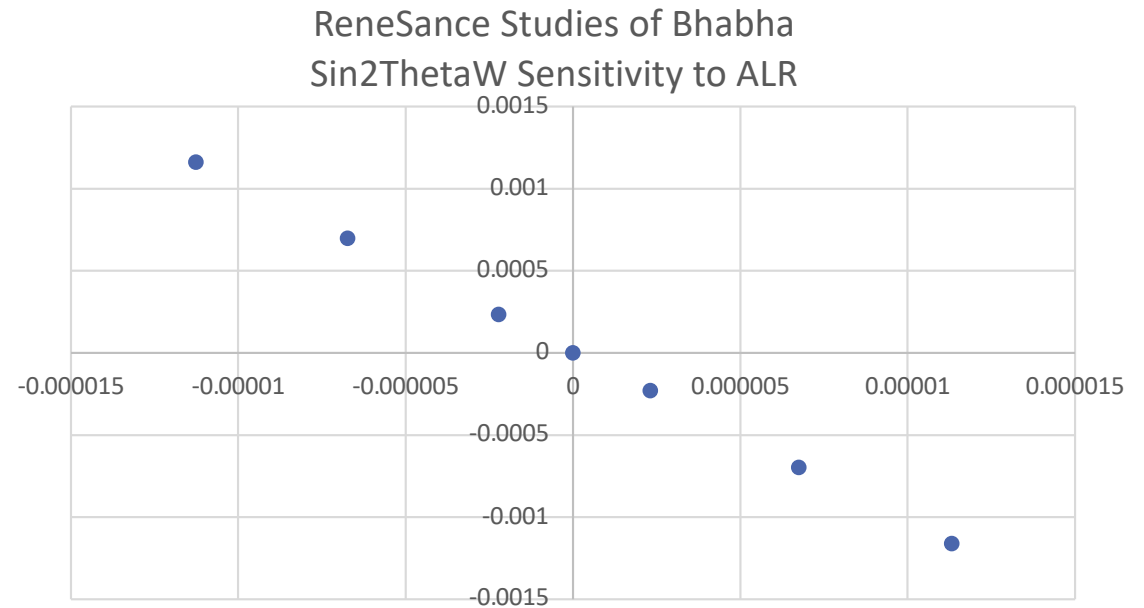
Assuming Chiral Belle achieves it's goal of a 70% polarization, and taking  $A_{LR} = 0.00012$  from ReneSANCe for the angular acceptance of

$|\cos \theta| < 0.819$ , a measured  $A_{LR} \langle Pe \rangle = 0.000098$  is predicted, with a statistical uncertainty of 2.3% for  $40 \text{ ab}^{-1}$  of data.

Dominant systematic uncertainties are expected to arise from knowledge of the beam polarization (0.4%), background modeling (0.07%), angular acceptance (1.1% assuming  $0.50^\circ$  systematic, probably conservative), and knowledge of the center-of-mass energy of the collisions (0.7%)

# $\sin^2\theta_w$ Sensitivity to $A_{LR}$

As suggested by authors of ReneSANCE, we shift values of  $M_w$  in ReneSANCE generator to determine  $\sin^2\theta_w$  sensitivity to  $A_{LR}$



# $\sin^2\theta_W$ Sensitivity

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Using the published Belle II efficiency for selecting Bhabha events from our luminosity paper:

*“Measurement of the integrated luminosity of the Phase 2 data of the Belle II experiment”, Chinese Physics C 44, 021001 (2020).*

and assuming a  $40\text{ab}^{-1}$  dataset having 70% polarization, projected uncertainty on the  $\sin^2\theta_W$  using ReneSANCe is  $\pm 0.00032$

Comparable to combined SLD-LEP uncertainty of  $\pm 0.00024$  on  $\sin^2\theta_W$  at the  $Z^0$  pole involving only the  $Z^0$ -electron couplings

(Note: recent CMS result for  $\sin^2\theta_W$  from  $Z^0 \rightarrow e+e^-$  is  $\pm 0.00041$ )

Also comparable to the MOLLER experiment’s projected uncertainty of  $(\pm 0.00028)$  at the lower 100 MeV energy scale

Chiral Belle including tau and muons – assuming lepton universality gives an uncertainty of  $\pm 0.00019$  - would be single most precise measurement of  $\sin^2\theta_W$  (NB:  $\pm 0.00016(\text{LEP} + \text{SLC})$ )

# What is size of NNLO Contributions

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The change from Born-level to NLO is large

Next Steps:

In progress of getting estimated projections of size of NNLO contributions