

Measurements of τ decays at Belle and Belle II

Lake Louise Winter Institute 2025

Wednesday 5th March, 2025

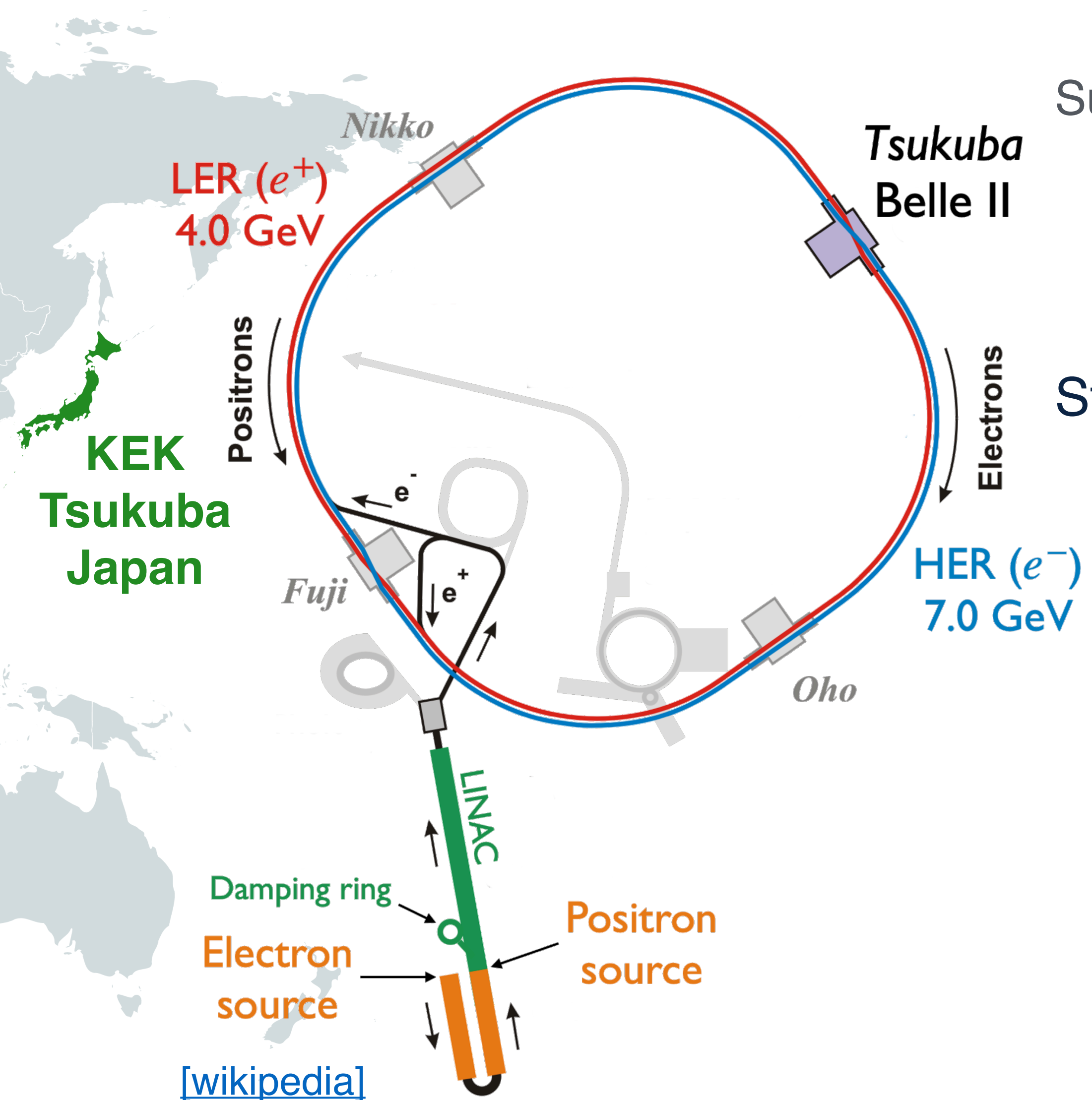
Robin Leboucher, on behalf of the Belle and Belle II collaborations



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SuperKEKB/Belle II for τ^- physics



KEKB (1999-2010) e^-e^+ collider at 10.58 GeV:

- Recorded luminosity $\approx 1 \text{ ab}^{-1}$

SuperKEKB e^-e^+ collider at 10.58 GeV:

- World Record instantaneous luminosity = $5.1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Recorded luminosity = 575 fb^{-1}
- Run 1 = 424 fb^{-1} (363 @ $\Upsilon(4S)$ + 61 off-resonance)

Strengths for τ^- physics:

- **High cross-section:**
 - $\sigma(e^-e^+ \rightarrow \Upsilon(4S)) = 1.05 \text{ nb}$
 - $\sigma(e^-e^+ \rightarrow c\bar{c}) = 1.3 \text{ nb}$
 - $\sigma(e^-e^+ \rightarrow \tau^-\tau^+) = 0.92 \text{ nb}$
- } *B, c and τ -factory*

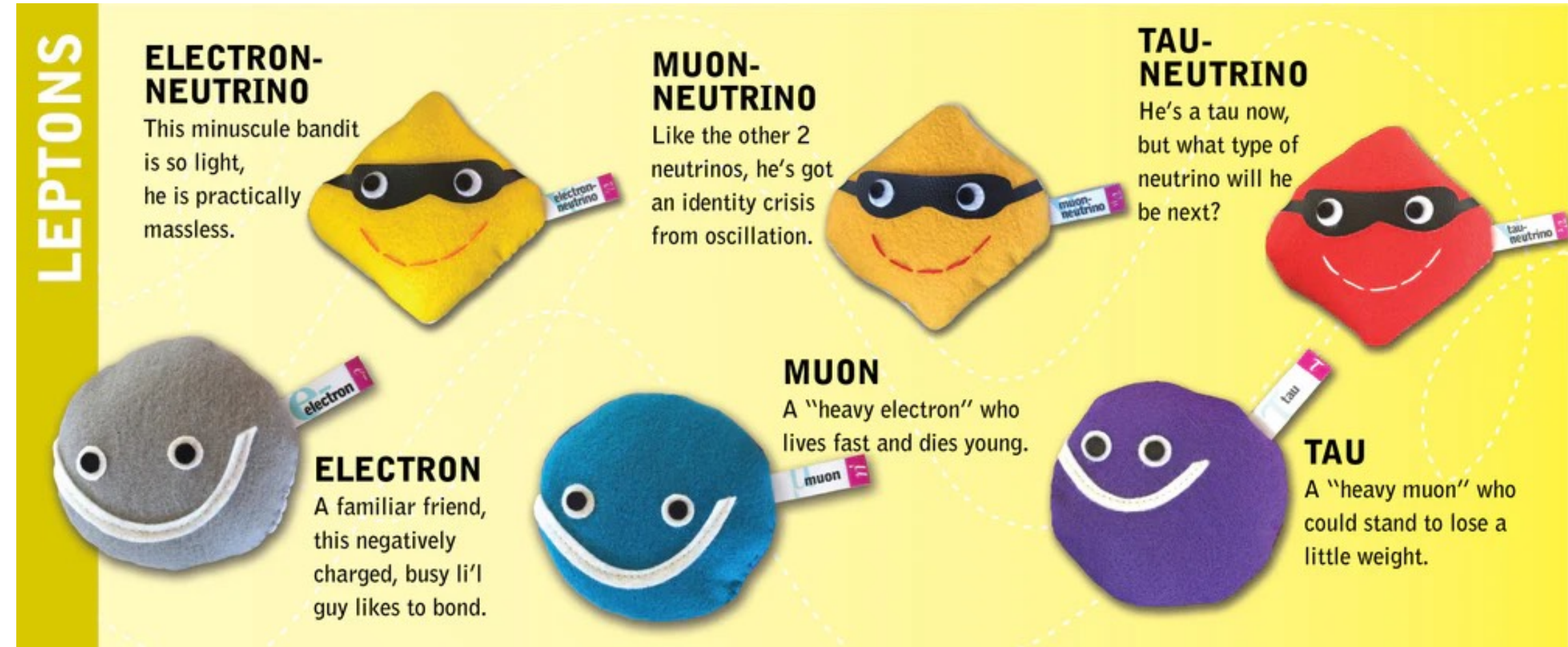
- **Good missing energy reconstruction:**
 - Clean collision environment
 - Hermetic detector (90% solid angle coverage)
- **Excellent vertexing and track reconstruction**
- **Good particle identification** (leptonID, π/K separation)

[\[wikipedia\]](#)

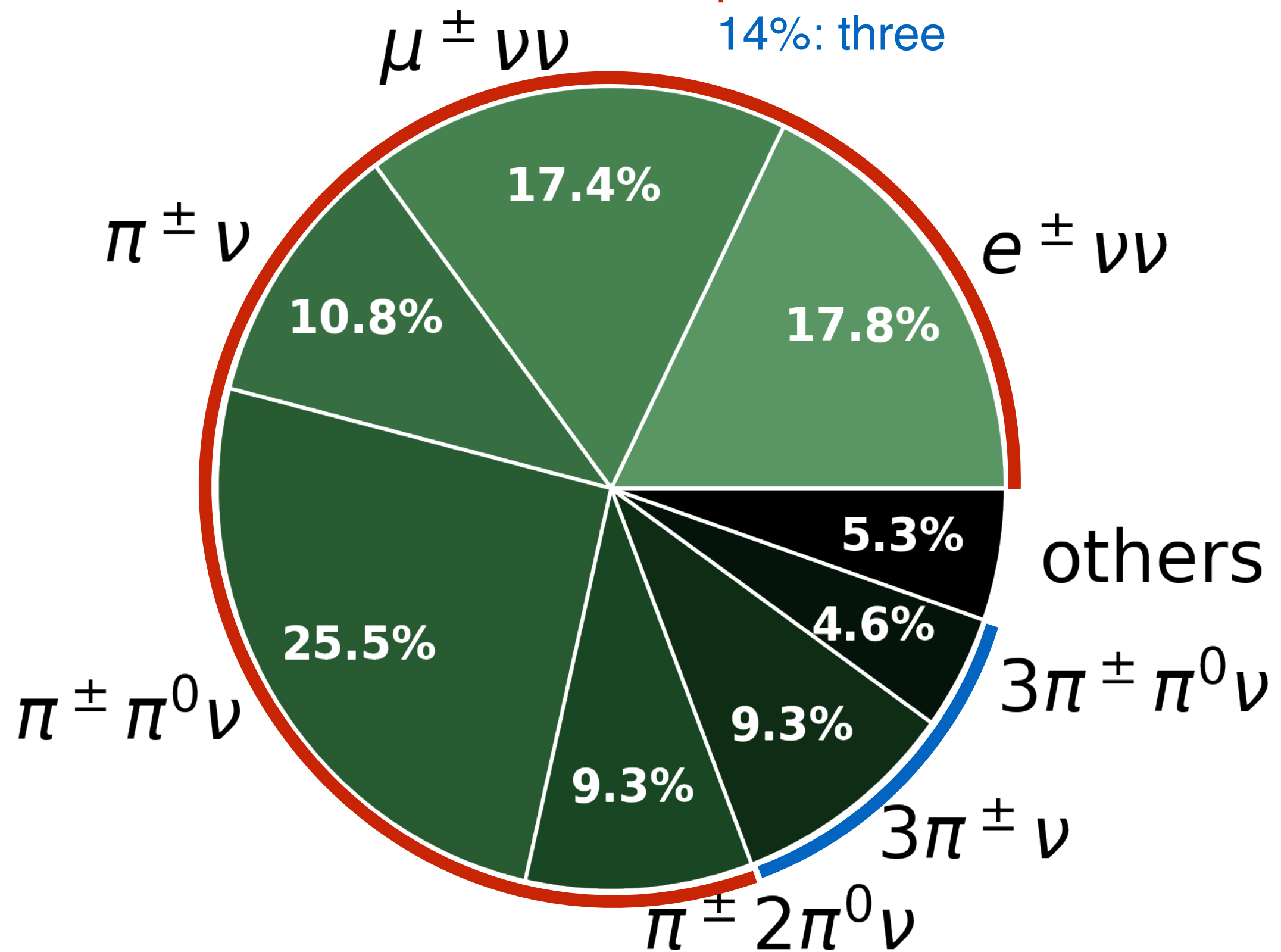
Belle II τ^- Physics

The τ^- is the heaviest lepton in the SM:

- Decays into leptons and hadrons
- Decays into one or three final-state particles
- Sensitive to more new physics models (large mass)



81%: one charged particle final state
14%: three



- ### Tests of the standard model (SM):
- τ^- mass
 - τ^- lifetime
 - Electric/Magnetic DM
 - V_{us} measurement
 - Lepton flavour universality
 - Michel parameters
 - CP violation

- ### Direct new physics searches:
- Lepton flavour violation (LFV)
 - Baryon number violation (BNV)
 - Heavy neutrinos
 - ...
- *In this talk*

Working with τ^- at Belle (II)

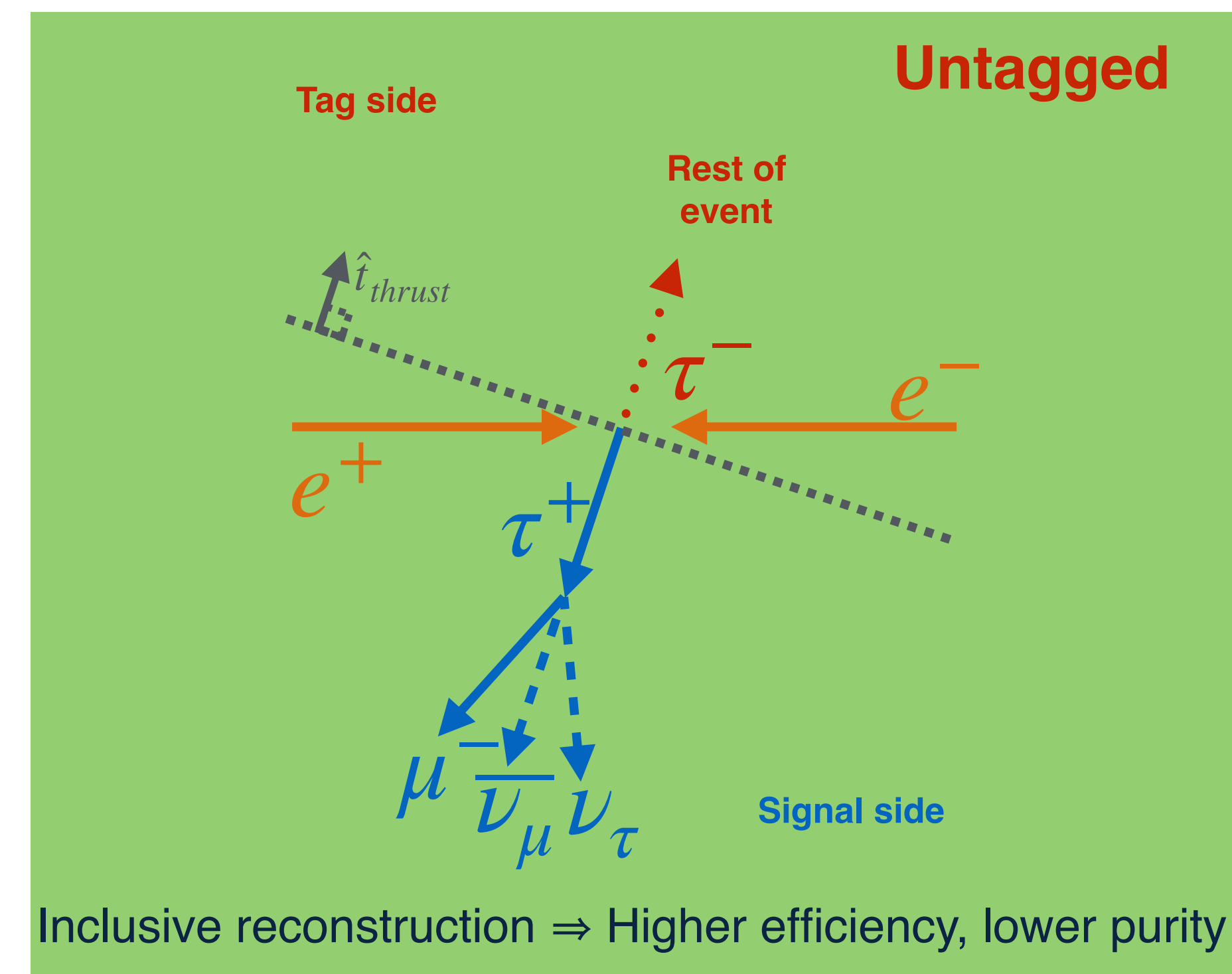
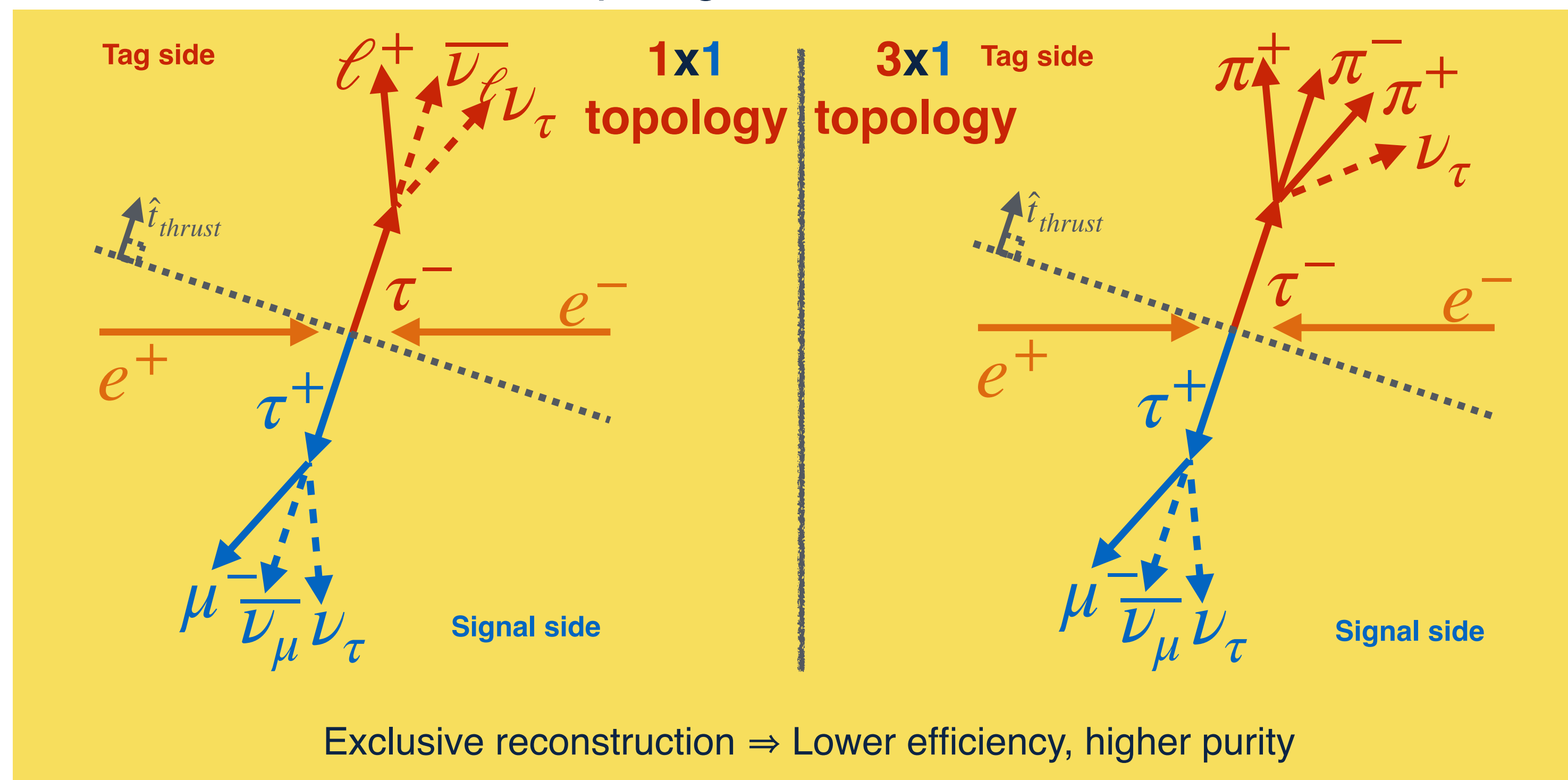
In e^-e^+ , τ^- pairs are produced **back to back and boosted**

\Rightarrow We can exploit the τ^- pairs geometry by defining **two hemispheres** wrt to a plane perpendicular

to the thrust axis \hat{t}_{thrust} maximising

$$T = \max_{\hat{t}} \left(\frac{\sum_i |\mathbf{p}_i^{CMS} \cdot \hat{t}|}{\sum_i |\mathbf{p}_i^{CMS}|} \right)$$

Reconstruct three kinds of topologies:



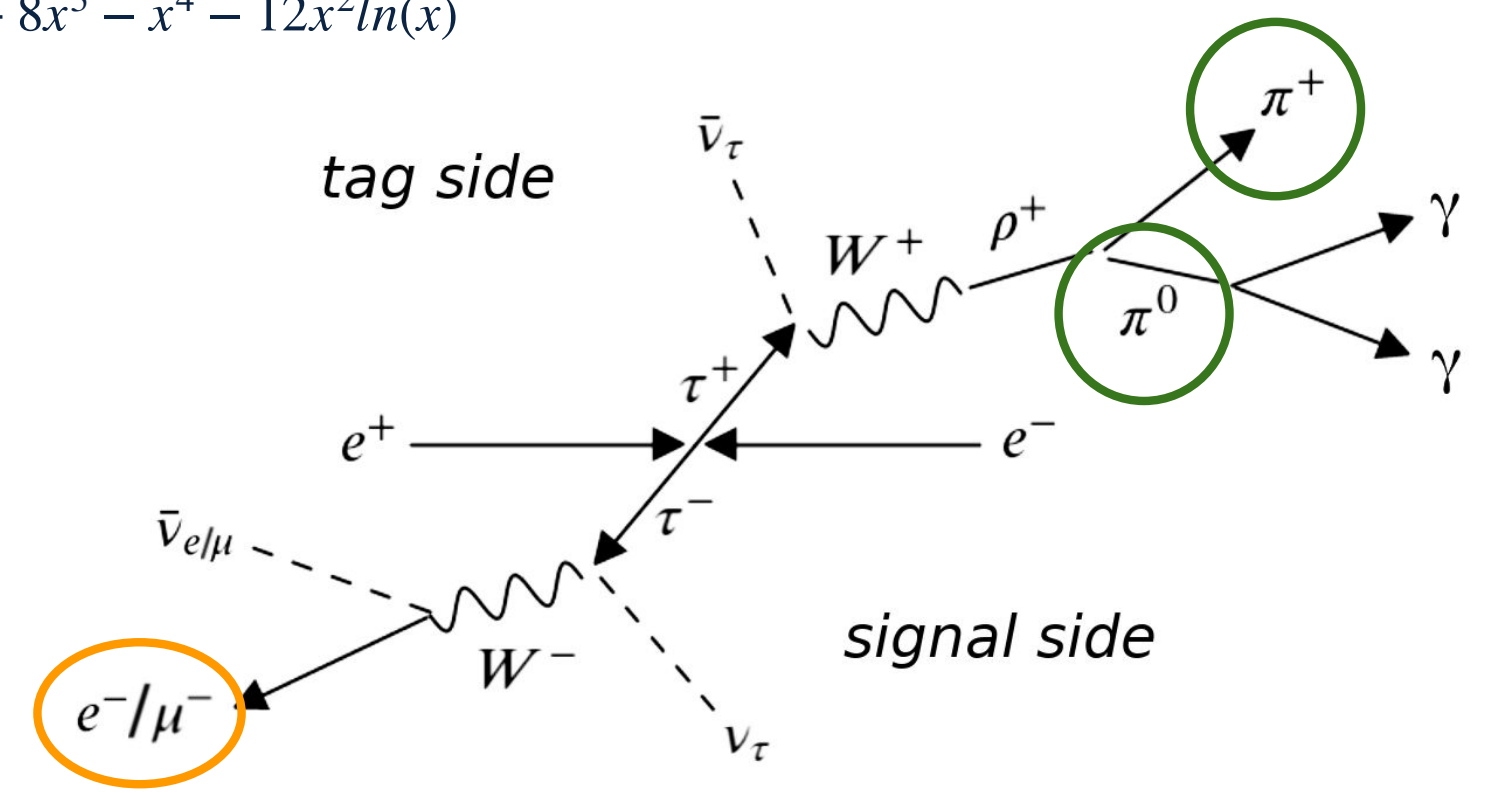
Belle II - Lepton Flavour Universality Measurement

Test if the W gauge bosons have the same couplings g as the three generations of leptons $g_e = g_\mu = g_\tau$ as predicted in the SM:

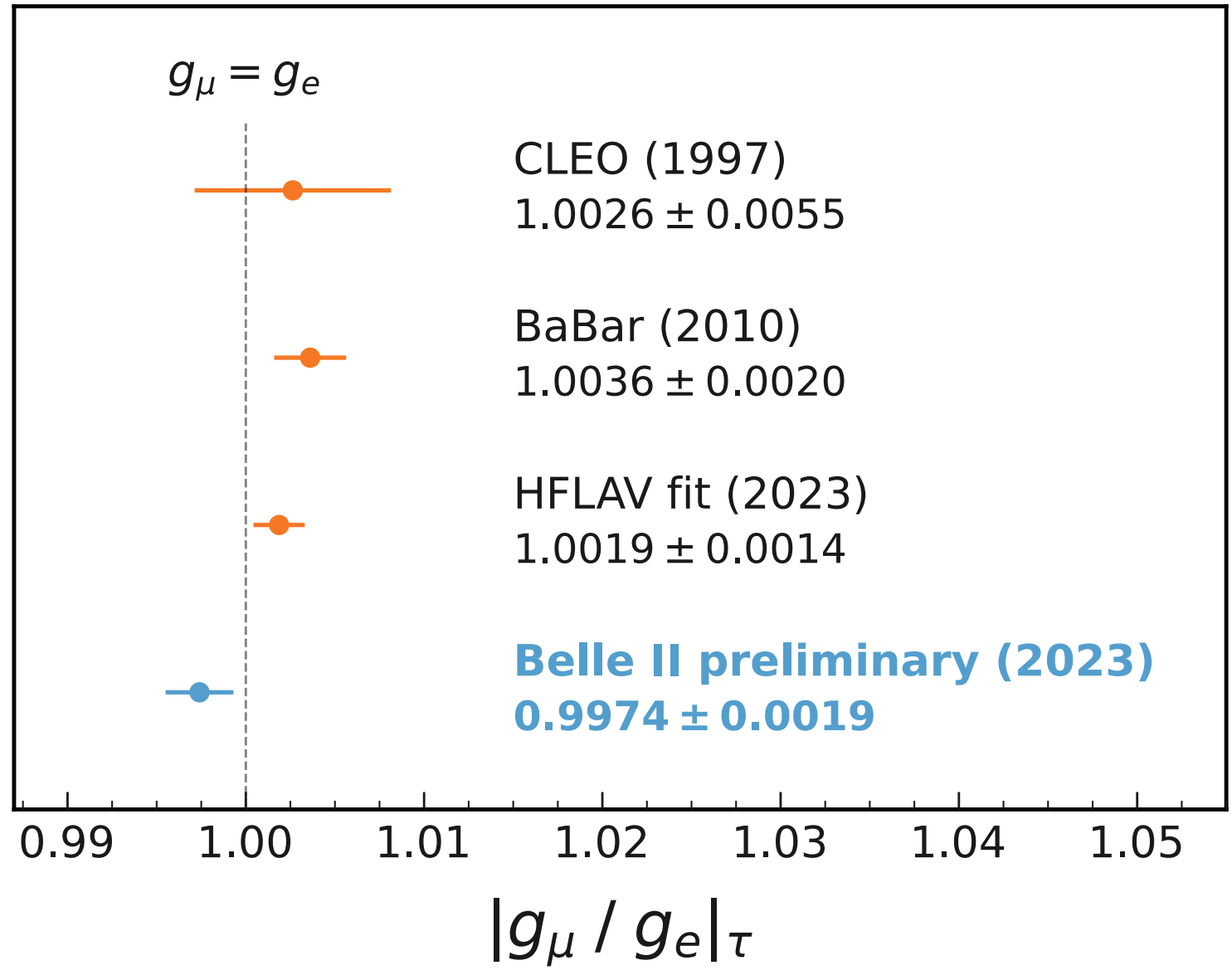
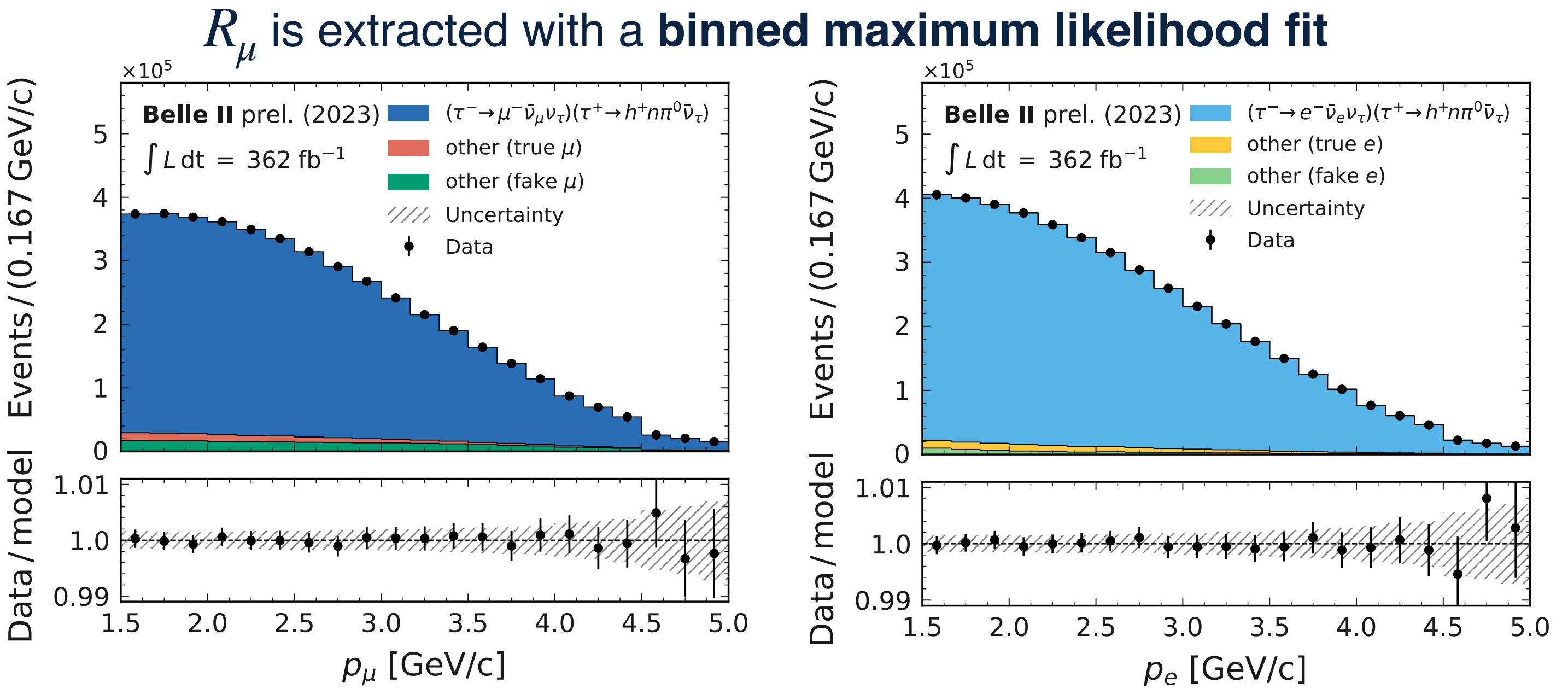
$$\left(\frac{g_\mu}{g_e}\right)_\tau^2 = R_\mu \frac{f(m_e^2/m_\tau^2)}{f(m_\mu^2/m_\tau^2)} \stackrel{\text{SM}}{=} 1$$

$$R_\mu \equiv \frac{\mathcal{B}(\tau^- \rightarrow \nu_\tau \mu^- \bar{\nu}_\mu)}{\mathcal{B}(\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e)} \stackrel{\text{SM}}{=} 0.9726$$

$$f(x) = 1 - 8x + 8x^3 - x^4 - 12x^2 \ln(x)$$



- Event selection is performed with **rectangular cuts** and a **neural network**
- 94% purity with 9.6% signal efficiency for the combined sample
- Main systematics are from **PID** (0.32%) and **trigger** (0.1%)



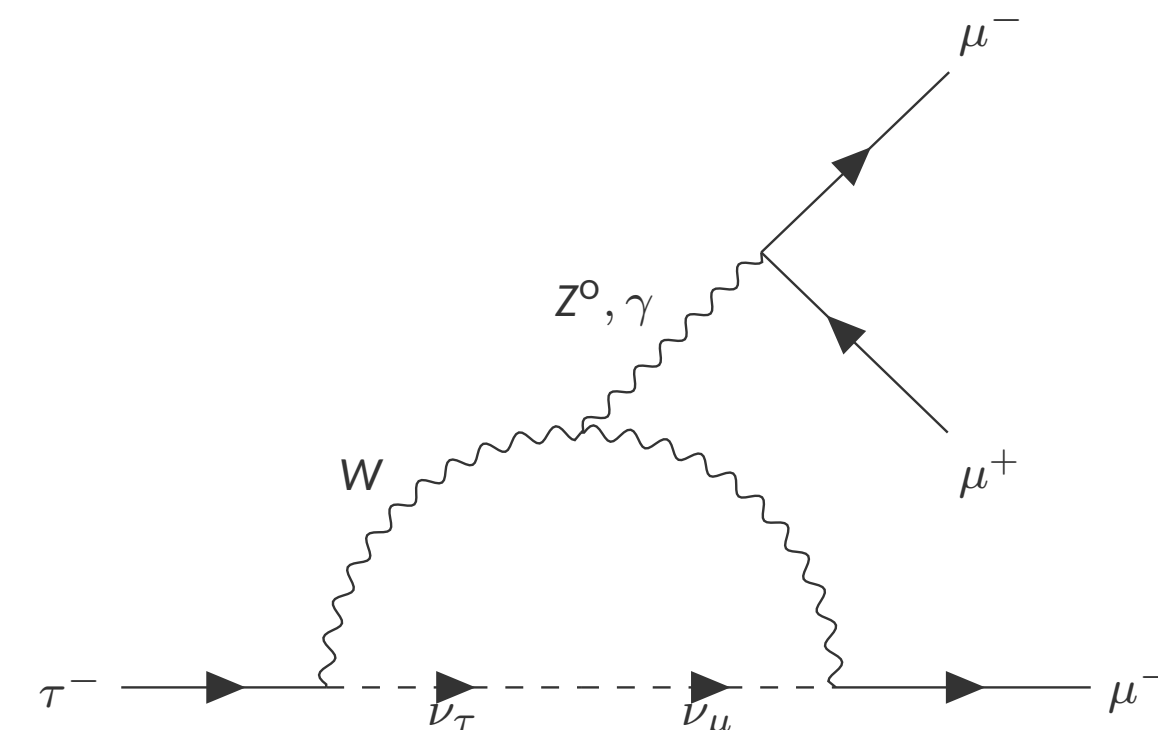
• **No deviation from the SM**

• **World's most precise R_μ and g_μ/g_e in τ^- decays from a single measurement**

$R_\mu = 0.9675 \pm 0.0007 \pm 0.0036$
 stat. sys.

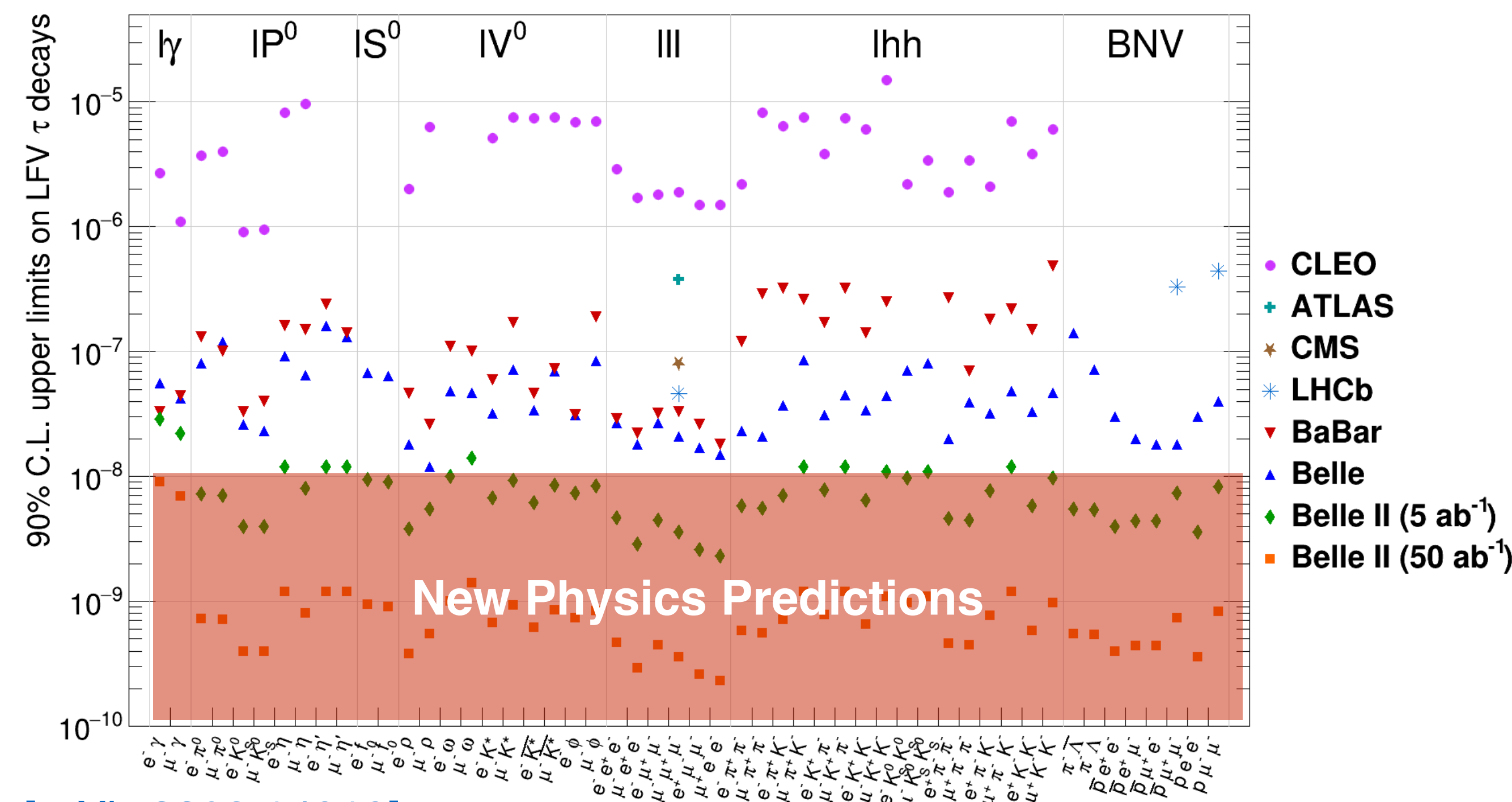
New Physics Direct Searches

- In SM, the Charged Lepton Flavour Violation is allowed through weak charged current and neutrino oscillation
 - Order $\mathcal{O}(10^{-55}) \Rightarrow$ **no Flavour Violation in current experiments**
- Various **New Physics predict Lepton Flavour Violation** at observable rates $\mathcal{O}(10^{-8} - 10^{-10})$
 - e.g leptoquarks for $\tau^- \rightarrow \ell^- V^0$ related $b \rightarrow c\tau\nu$ anomalies



Physics Models	$\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)$
SM	10^{-55}
SM + Seesaw	10^{-10}
SUSY + Higgs	10^{-8}
SUSY + SO(10)	10^{-10}
Non-universal Z'	10^{-8}

[PhysRevD.77.073010]



[arXiv.2203.14919]

A lot of interesting decays at e^-e^+ colliders with 50 modes:

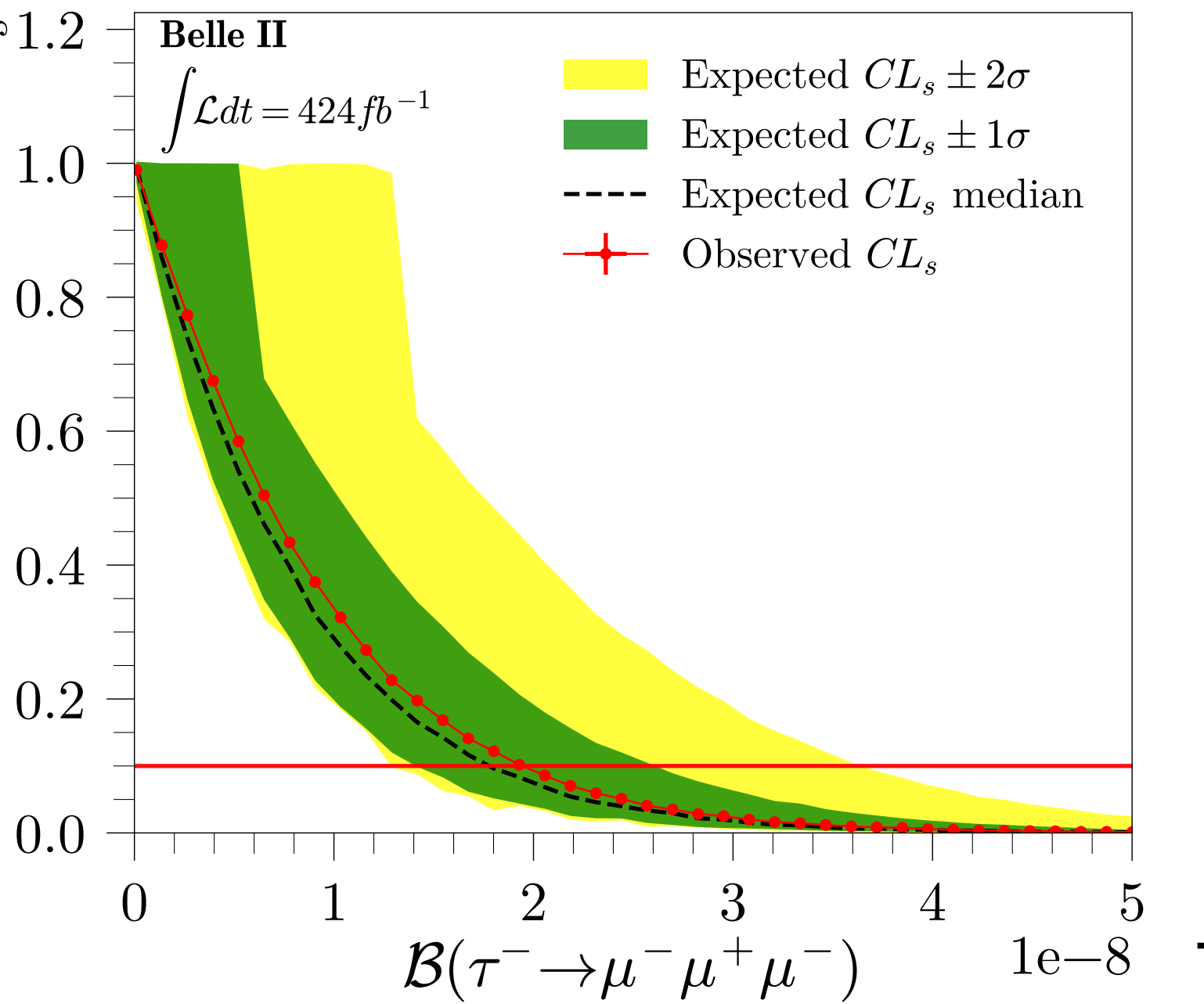
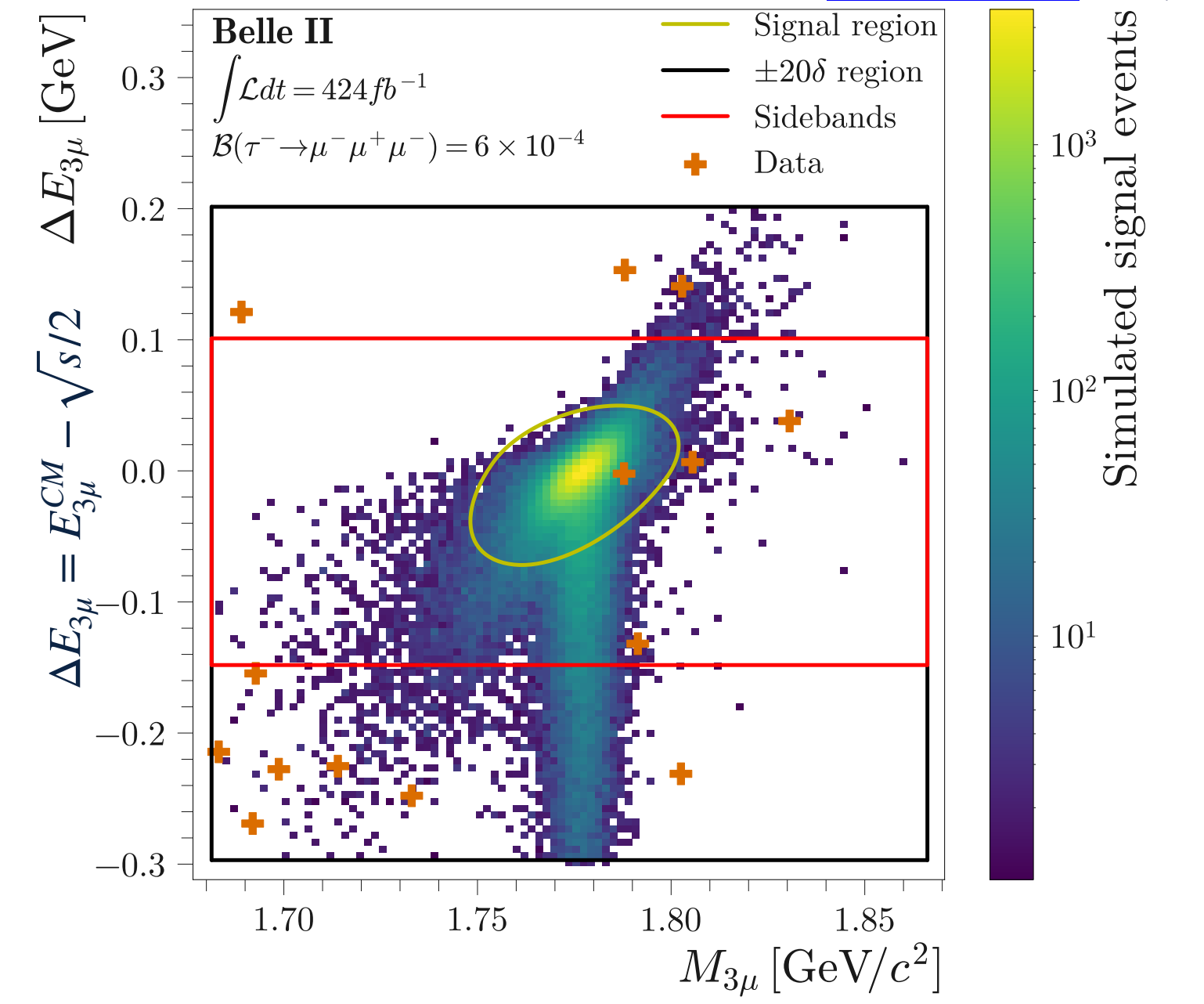
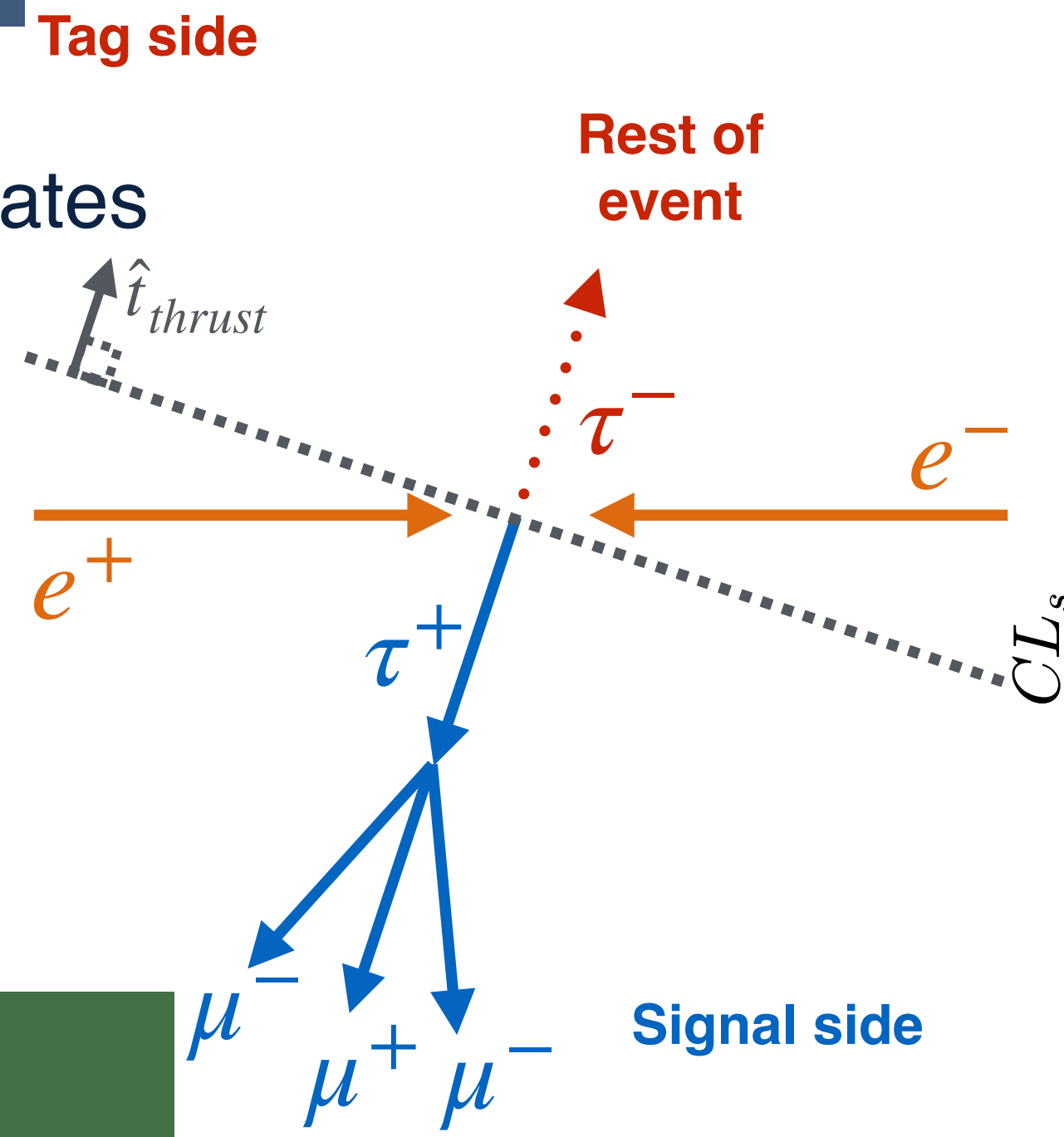
- $\tau^- \rightarrow \mu^- \mu^+ \mu^-$ most accessible
- $\tau^- \rightarrow \ell^- \phi$ linked to $b \rightarrow c\tau\nu$ within the Leptoquarks models
- $\tau^- \rightarrow \Lambda(\bar{\Lambda})\pi^-$ violated the Baryon number \Rightarrow condition for matter/antimatter asymmetry
- $\tau^- \rightarrow \ell^- \alpha$ new boson candidate for dark matter

Belle II - $\tau^- \rightarrow \mu^- \mu^+ \mu^-$ Lepton Flavour Violation

- Almost **free from SM background**
 - Excellent resolution on energy and momentum
 - Also probed by LHC experiments
- Existing measurements: 2.1×10^{-8} by Belle
 2.9×10^{-8} by CMS

- Signal efficiency challenge:**
- **Untagged τ reconstruction** to cover more final states
 - **BDT classifier:** reject main backgrounds $e^-e^+ \rightarrow q\bar{q}$ using signal, rest of event and kinematic variables
 - $\epsilon_{sig} \simeq 20.41\%$, 3 times Belle efficiency
 - Extract expected backgrounds $0.7^{+0.6}_{-0.5} \pm 0.01$ by rescaling yields from sidebands data in signal region (ABCD)

- **Observed 1 event in $424fb^{-1}$**
- **Set 90% CL upper limit on the branching fraction**
 $\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-) < 1.9 \times 10^{-8}$
- **World's best limit**
- Results confirmed by a conventional 3 by 1 tag method



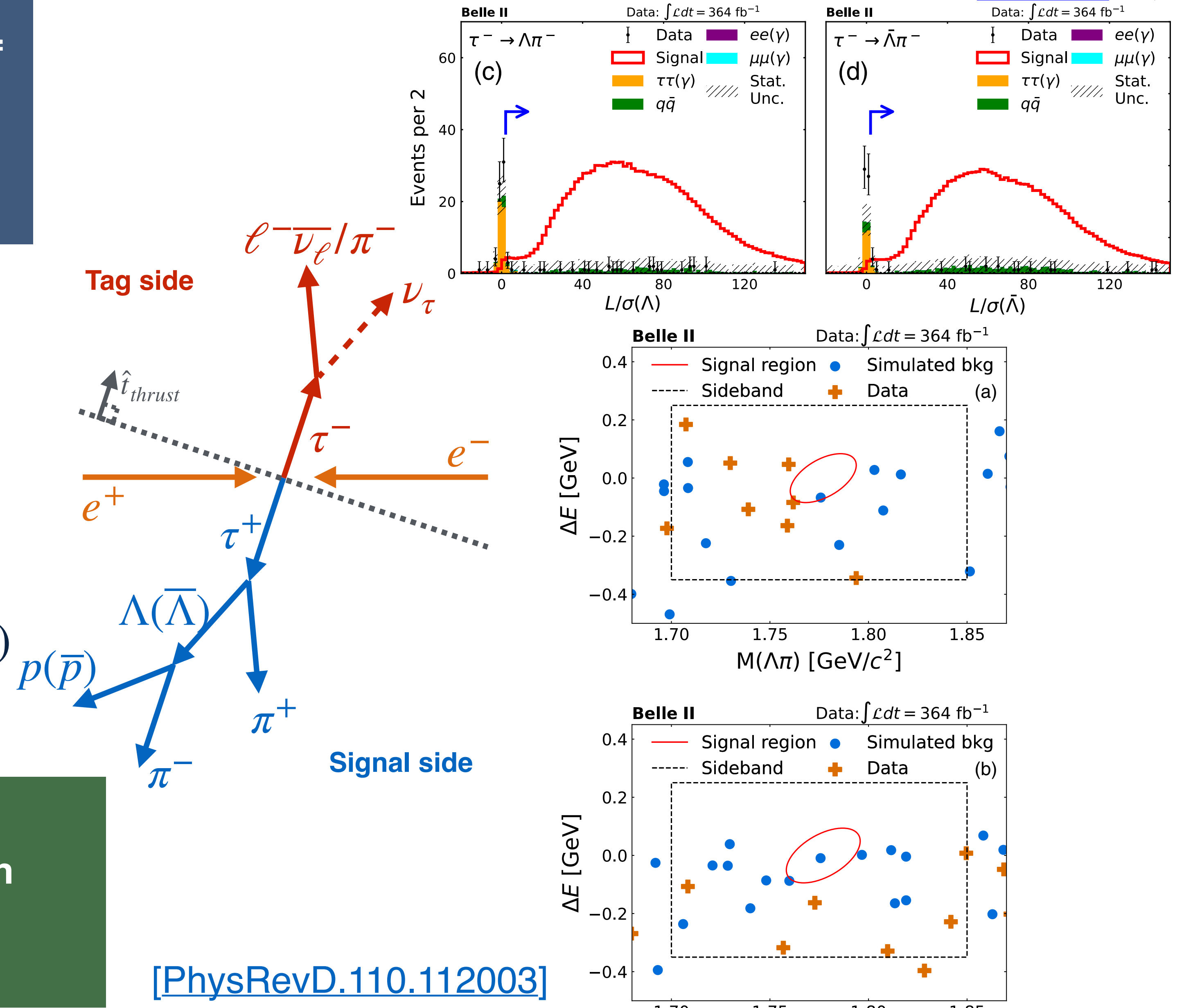
[JHEP09(2024)062]

Belle II - $\tau^- \rightarrow \Lambda\pi^- / \tau^- \rightarrow \bar{\Lambda}\pi^-$ Baryon Number Violation

- BNV is a key ingredient to explain asymmetry of matter
- Plenty of BSM scenarios allow it
- Belle result: $7.2(14) \times 10^{-8}$ with $154fb^{-1}$

- Reconstruct 4 charged particles (0 net charge) in **1x3 topology**
- $\Lambda(\bar{\Lambda})$ reconstructed from $p(\bar{p})$ and π^-
- Background suppression: **loose preselection** (flight significance most discriminant) + **gradient BDT**
- $\epsilon_{sig} \simeq 9.5(9.9)\%$ for $\tau^- \rightarrow \Lambda(\bar{\Lambda})\pi^-$
- Extract expected backgrounds $1.0^{+1.3}_{-1.1}(0.5 \pm 0.6)$ by rescaling yields from sidebands data in signal region

- No observed event in $364fb^{-1}$
- Set 90% CL upper limit on the branching fraction $\mathcal{B}(\tau^- \rightarrow \Lambda(\bar{\Lambda})\pi^-) < 4.7(4.3) \times 10^{-8}$
- New, most stringent limit

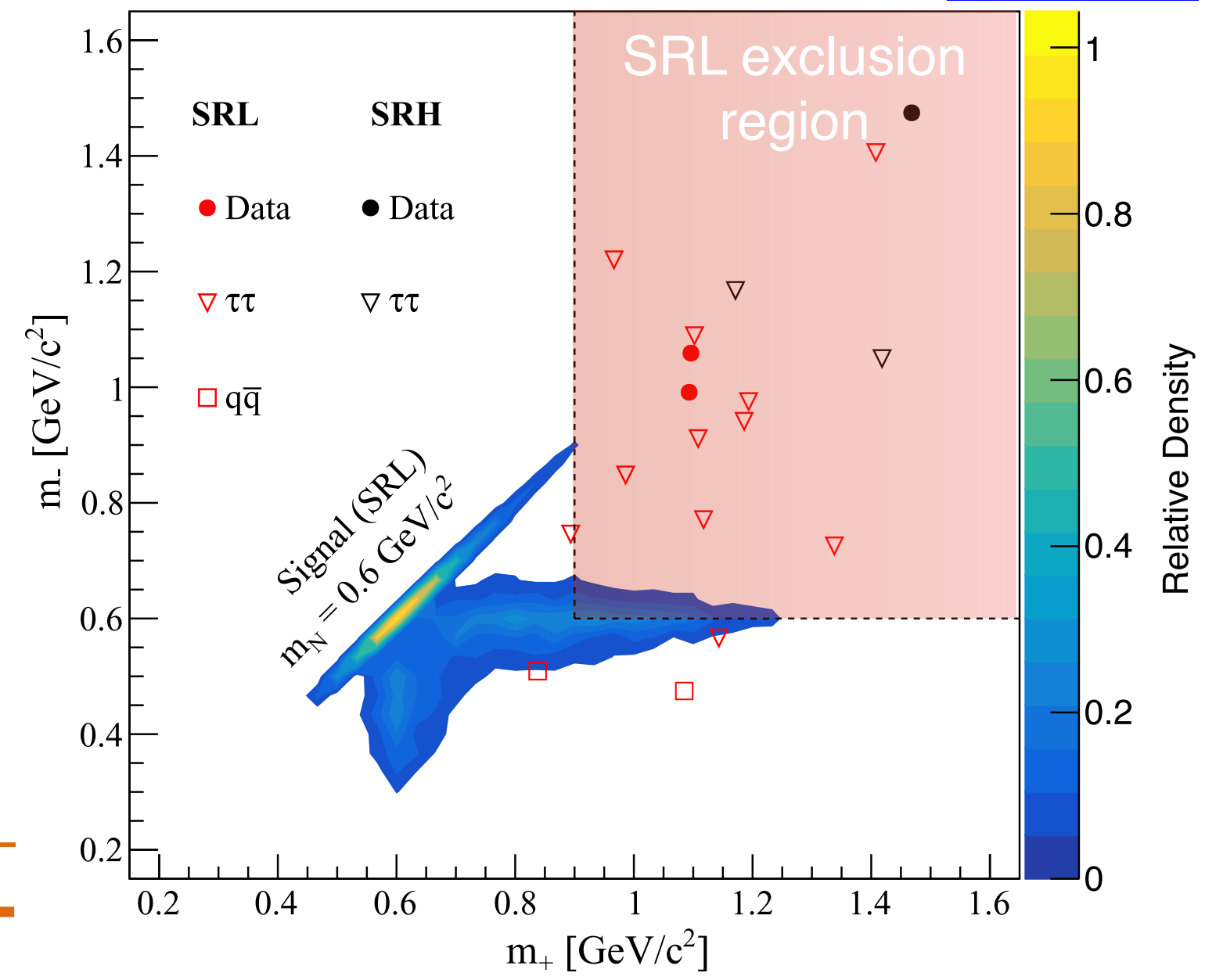
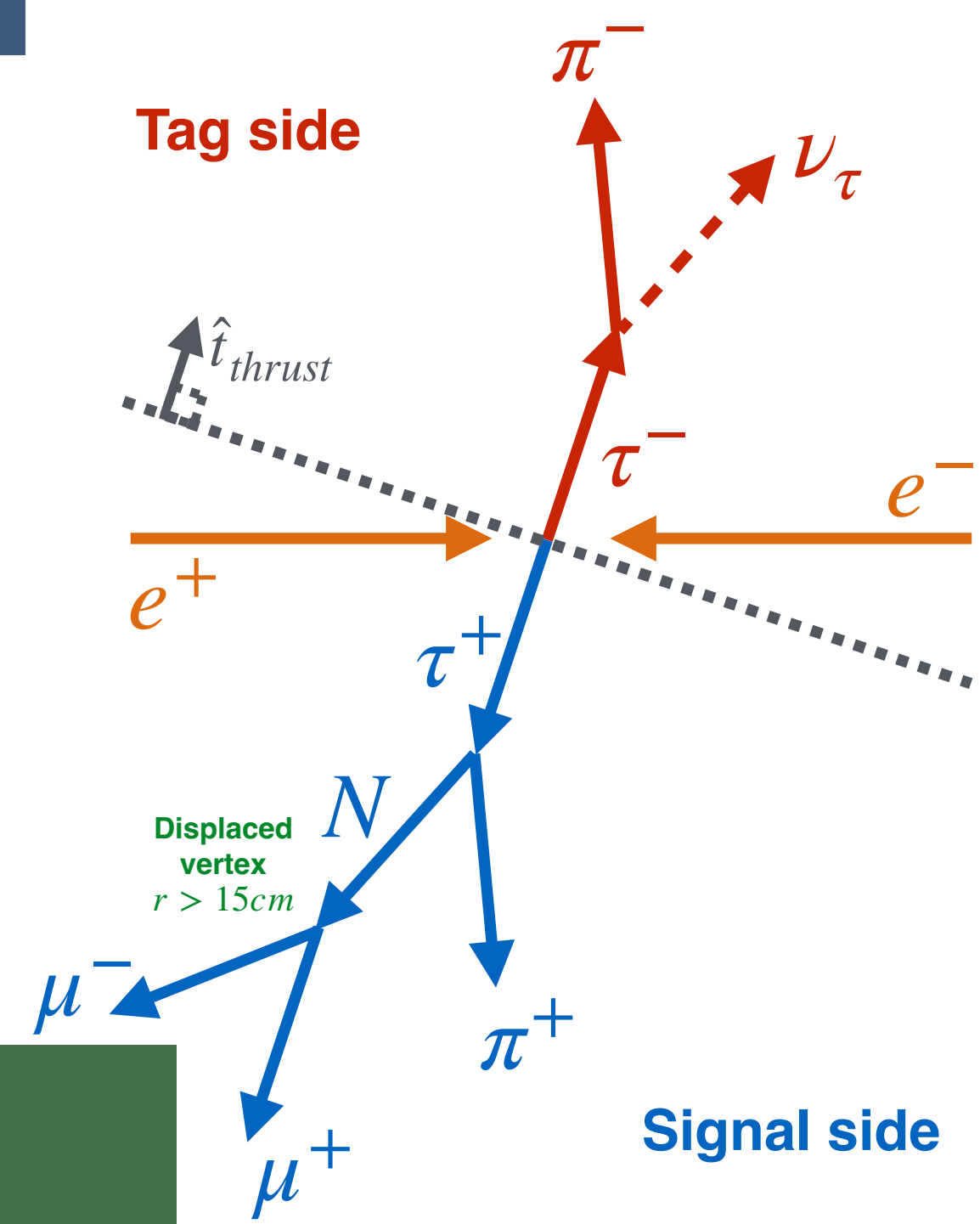


Belle - Search for Heavy Neutral Lepton

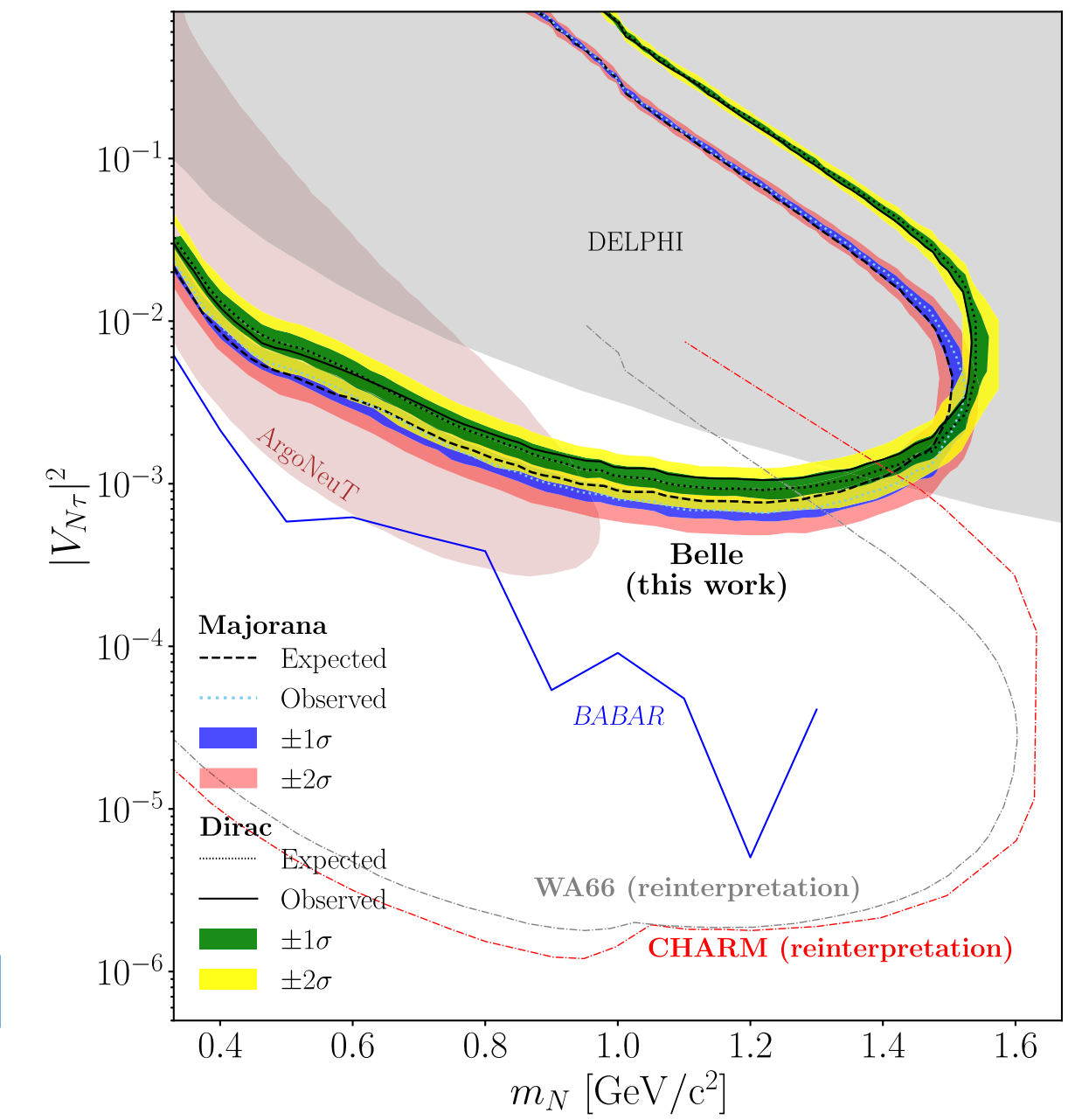
- Can interact with ν_{SM} via $N \leftrightarrow \nu_{SM}$ mixing
- Long lifetime \rightarrow Displaced vertex
- Probe $m_N < m_\tau$ in $\tau^- \rightarrow N\pi^-$ decay

SRH: $m_{DV} > 520 \text{ MeV}/c^2$
 SRL: $m_{DV} < 420 \text{ MeV}/c^2$
 Excluded $100 \text{ MeV}/c^2$ window to reject K_S^0 contamination

- Reconstruction in **1x1** topology:
 - Tag $\tau^+ \rightarrow \pi^+ \nu_\tau$
 - Signal $\tau^- \rightarrow N(\rightarrow \mu^- \mu^+) \pi^-$:
 - Fit the $\mu^- \mu^+$ displaced vertex
- Use the **displaced vertex** properties to extract m_N and suppress background to unit level



- First-time $N \rightarrow \mu^- \mu^+$ displaced vertex method
- Observation in agreement with background expectations with 915 fb^{-1}
- Set limit on the mixing coefficient $|V_{N\nu_\tau}|^2$ between $300 < m_N < 1600 \text{ MeV}/c^2$



[PhysRevD.109.L111102]

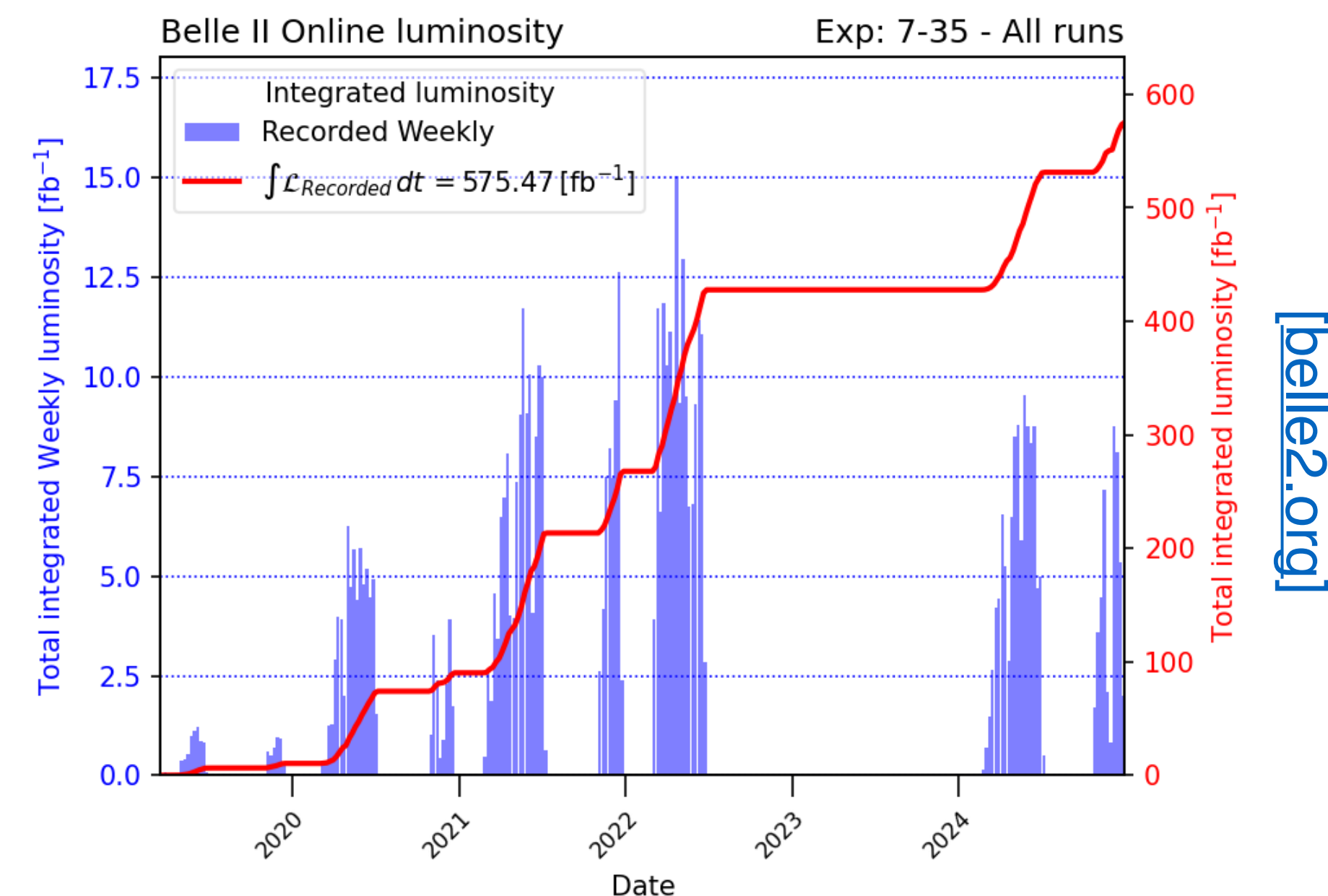
Summary

- Belle and Belle II are leading the τ^- physics research on several key areas:
 - Various studies related to Standard Model parameters
 - Searches for phenomena beyond the Standard Model
- There are many opportunities for improvement in these areas:
 - Increasing the size of the data sample
 - Enhancing analysis techniques and reducing systematic uncertainties
 - Developing more accurate physics models

- **Many more results to come:**

This is only the beginning for precision and rare decay searches with τ^- at Belle II

Thank you!





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Backups

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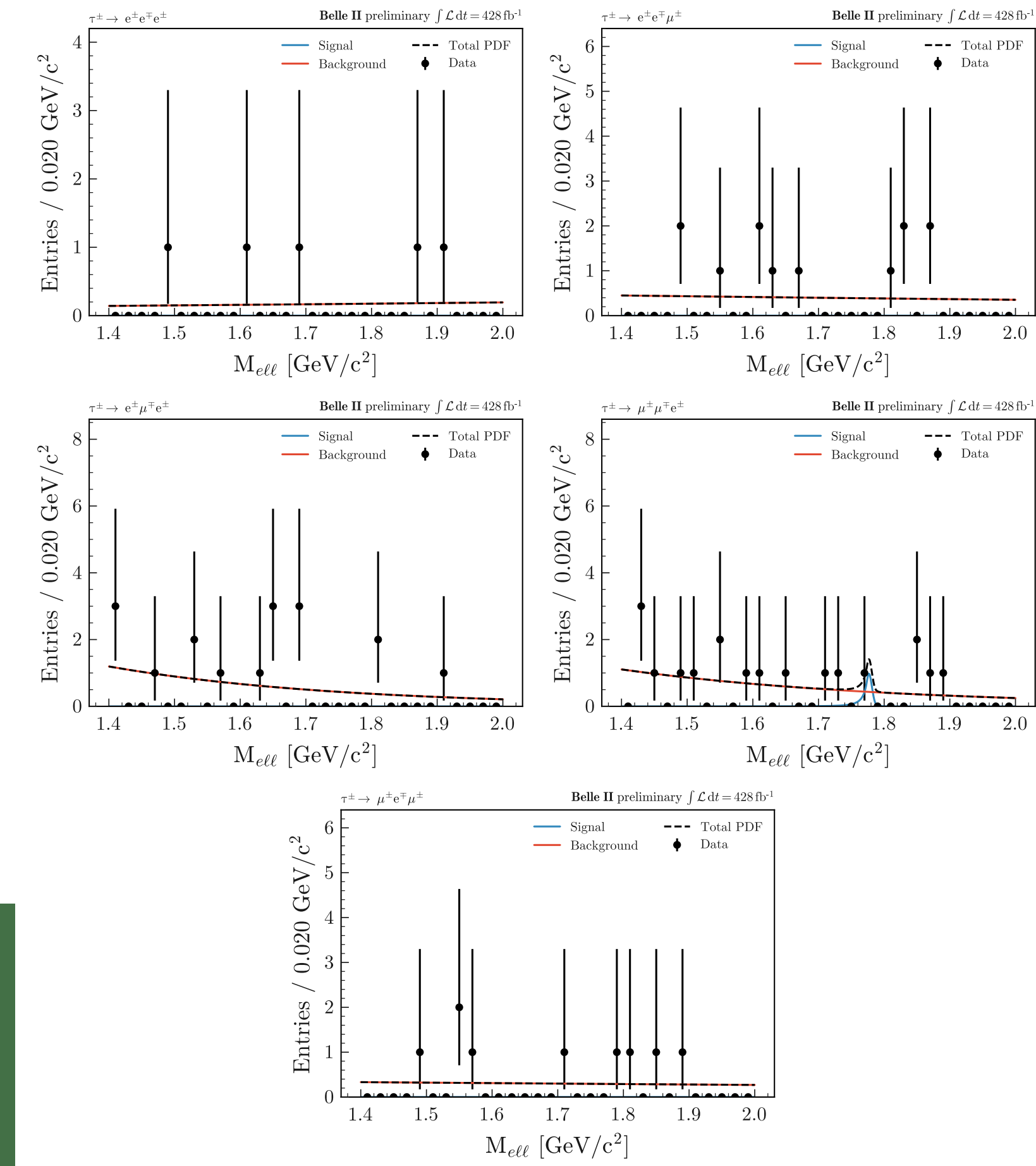
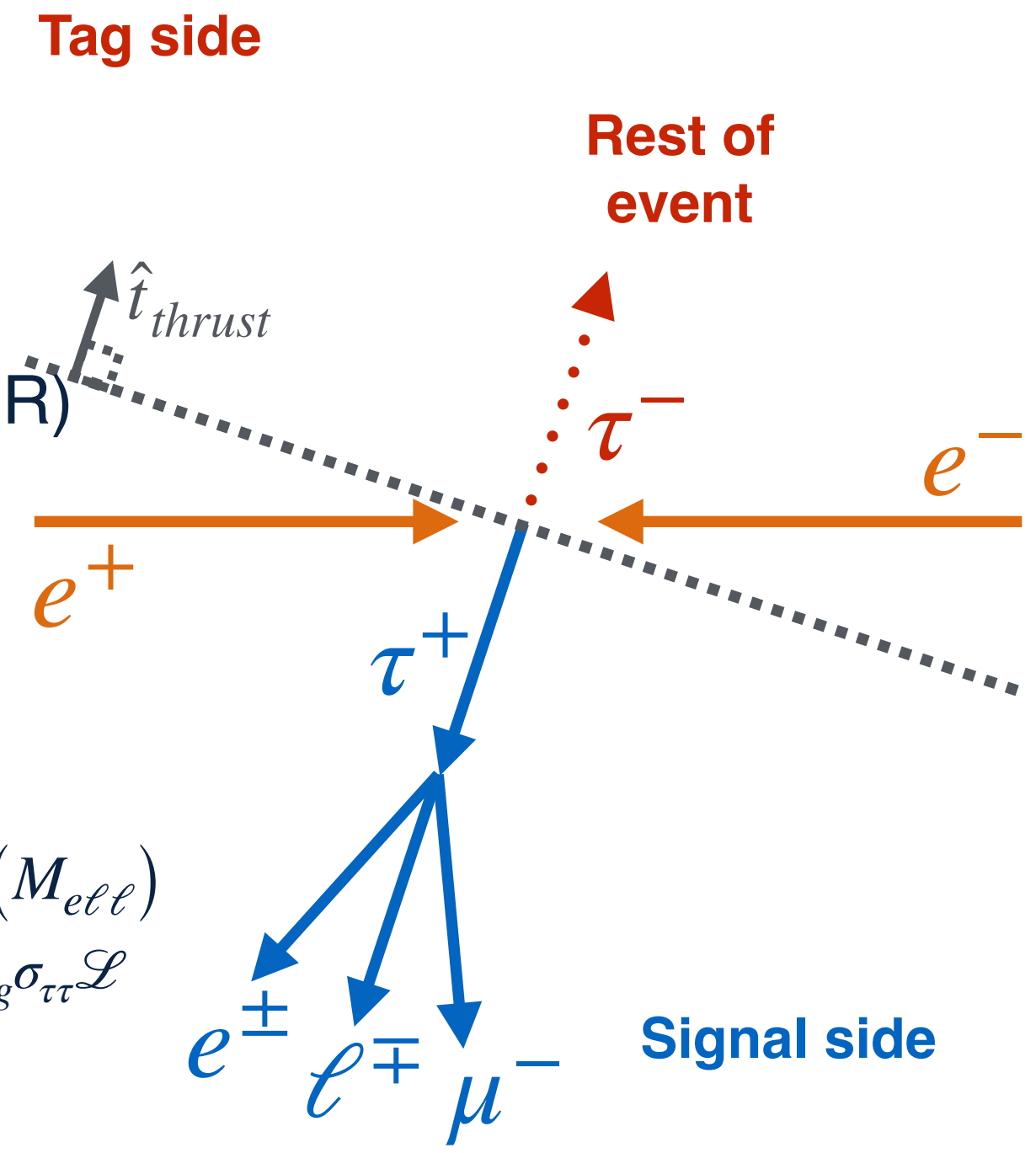
Belle II - $\tau^- \rightarrow e^\pm \ell^\mp \ell^-$ Lepton Flavour Violation

Preliminary

- Extend $\tau^- \rightarrow \mu^- \mu^+ \mu^-$ study to 5 modes:
 $e^- e^+ e^-$, $e^- e^+ \mu^-$, $e^- \mu^+ e^-$, $\mu^- \mu^+ e^-$, $\mu^- e^+ \mu^-$
- Higher background contamination from $\ell^- \ell^+ (\gamma)$ and $\ell^- \ell^+ \ell^- \ell^+$
- Existing measurements: $1.5 - 2.7 \times 10^{-8}$ by Belle

Signal efficiency challenge:

- **Untagged τ reconstruction** to cover more final states
- Preselection rectangular cuts
- **Data (blind) driven BDT classifier:**
 - reject main backgrounds $\ell^- \ell^+ \ell^- \ell^+$ (mismodeled ISR/FSR)
 - training sample away from the fitted region
 - rely on signal, ROE and kinematic variables
- Resulting final $\epsilon_{sig} \simeq 15 - 24 \%$
- **Extract expected by fitting M_{ell} :**
 $PDF_{tot}(M_{ell}) = \mathcal{B}(\tau^- \rightarrow e^\mp \ell^\pm \ell^-) \cdot \mu \cdot PDF_{sig}(M_{ell}) + N_{bg} \cdot PDF_{bg}(M_{ell})$
 PDF_{sig} is a double-sided Crystal Ball
 PDF_{bg} is an exponential
 $\mu = 2\epsilon_{sig}\sigma_{\tau\tau}\mathcal{L}$



- **No significant signal was observed in $424fb^{-1}$**
- **Set 90% CL upper limit on the branching fraction**
- **The most stringent upper limit on all modes**

	$\mathcal{B}_{exp}^{UL} \times 10^{-8}$	$\mathcal{B}_{obs}^{UL} \times 10^{-8}$
$e^- e^+ e^-$	2.50	2.18
$e^- e^+ \mu^-$	2.00	1.38
$e^- \mu^+ e^-$	1.54	1.36
$\mu^- \mu^+ e^-$	1.80	2.36
$\mu^- e^+ \mu^-$	1.54	1.46

Belle and Belle II - $\tau^- \rightarrow \ell^- K_S^0$ Lepton Flavour Violation



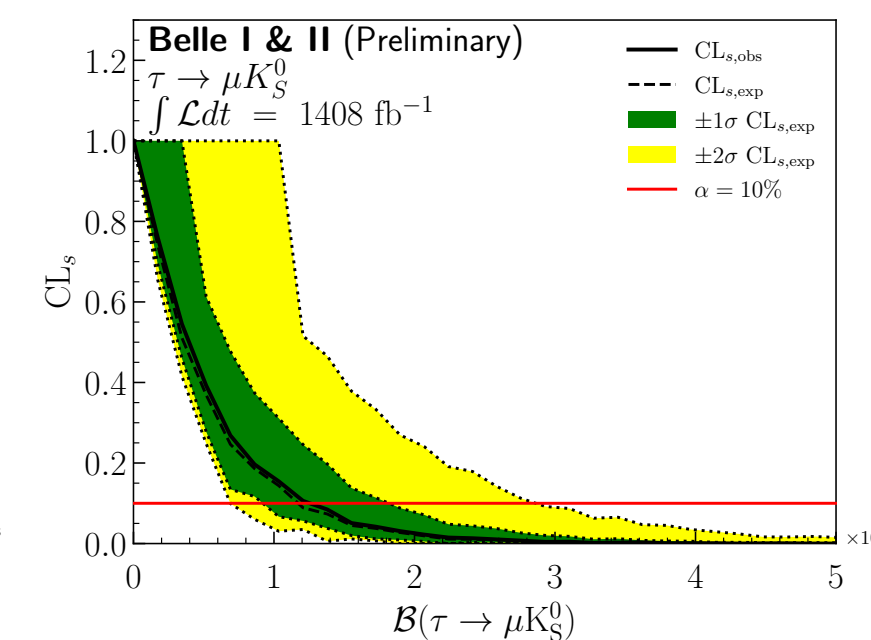
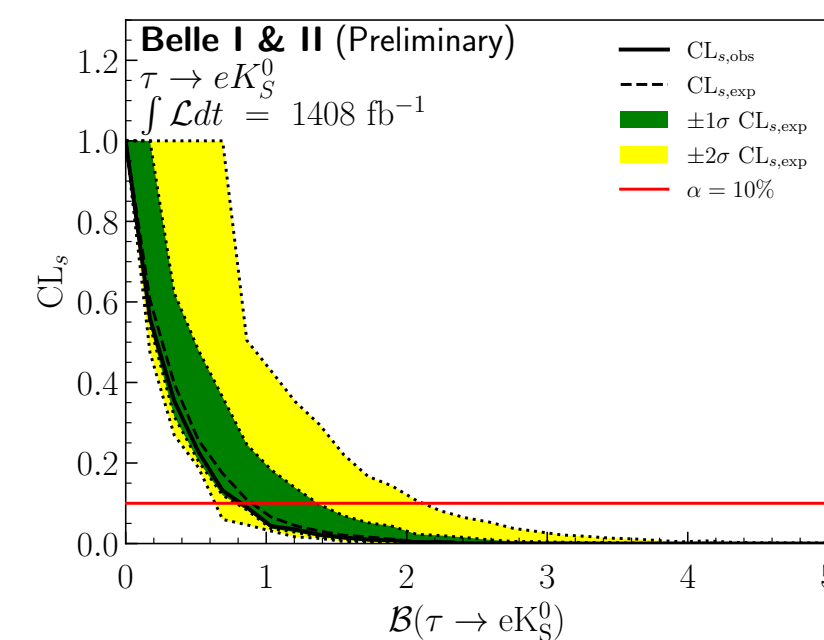
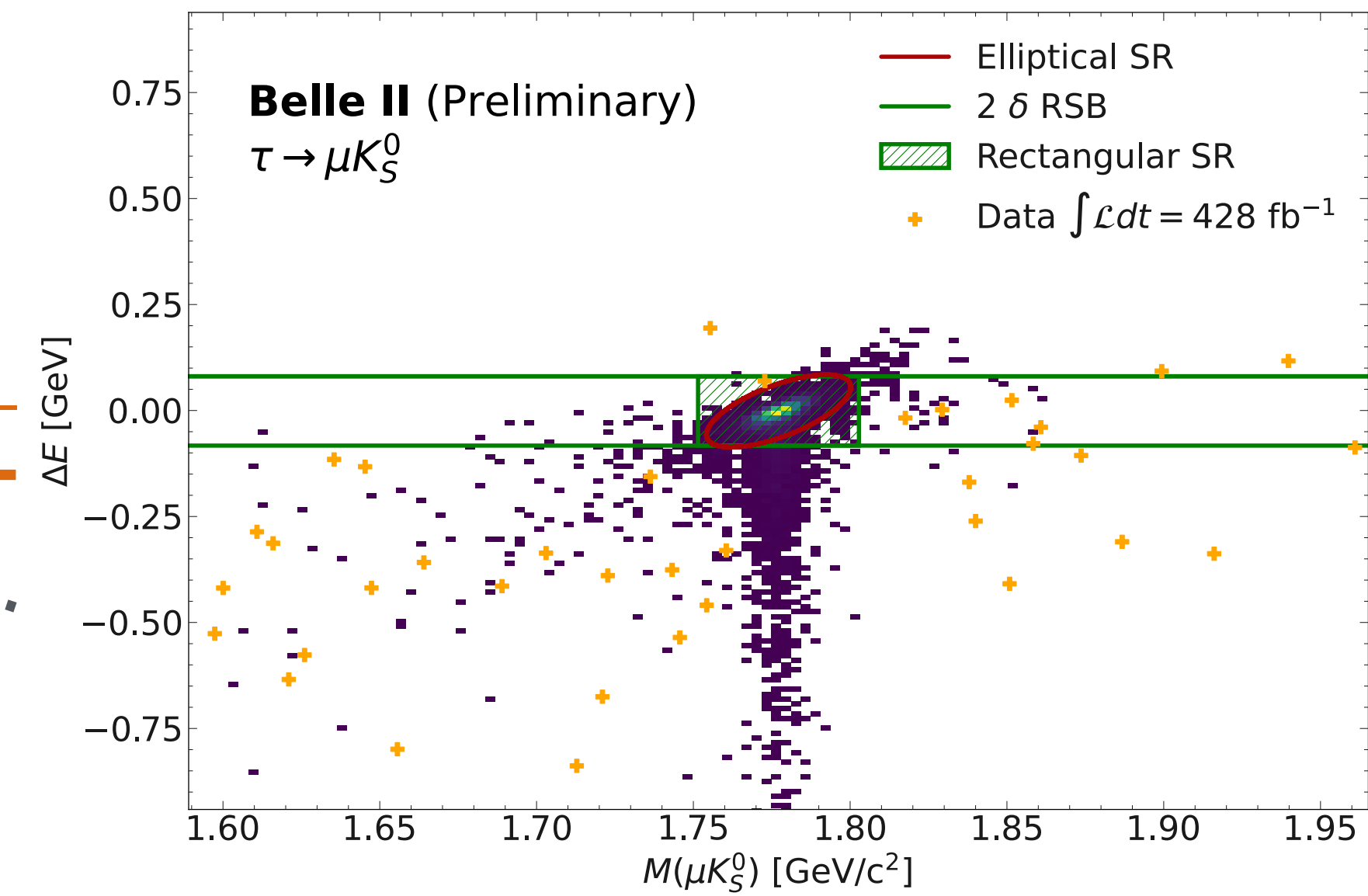
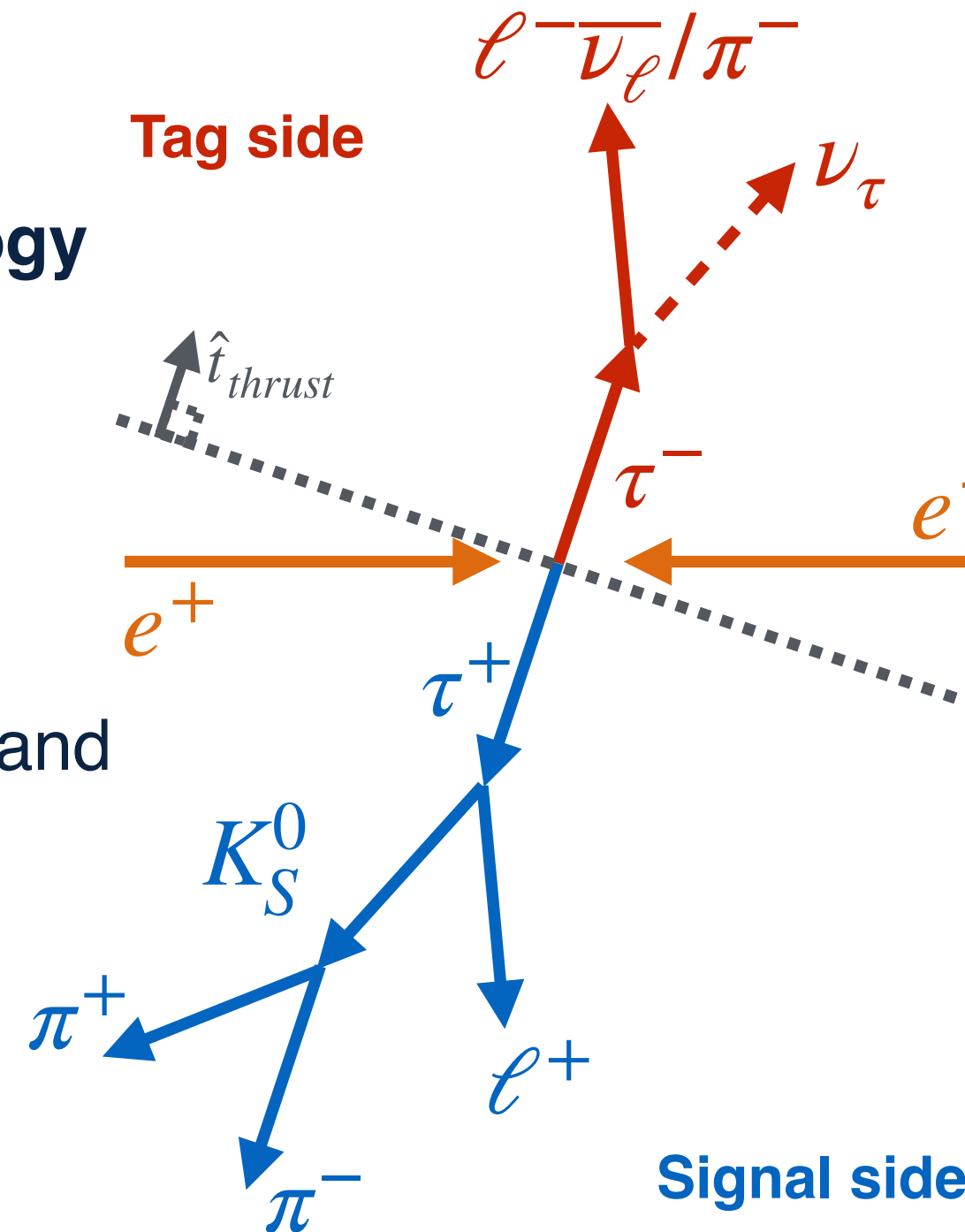
Preliminary

- In EFT, it can constrain different types of operators (e.g two-lepton and two-quark-operators in leptoquark models)
- Existing measurements: $2.3(2.6) \times 10^{-8}$ by Belle for $e^-(\mu^-)$ mode

Signal efficiency challenge:

- Reconstruct 4 charged particles (0 net charge) in **1x3 topology**
- K_S^0 reconstructed from $\pi^-\pi^+$
- Preselection rectangular cuts
- BDT classifier:**
 - different training on each Belle and Belle II samples
 - use signal (tag) τ^- , K_S^0 and track kinematics, event shape and neutrals variables
- Resulting final $\epsilon_{sig} \simeq 10\%$
- Extract expected background by fitting $M_{\ell K_S^0}$:**

PDF_{bg} is an exponential



- No significant signal was observed in $424fb^{-1}$ Belle II and $980fb^{-1}$ Belle
- Set a combined 90% CL upper limit on the branching fraction

$$\mathcal{B}(\tau^- \rightarrow e^-(\mu^-)K_S^0) = 0.8(1.2) \times 10^{-8}$$
- Most stringent limit on all modes