









### Detector Alignment at Belle II

Tadeáš Bilka<sup>1\*</sup>

<sup>1</sup>DESY, Hamburg

Belle II Collaboration

**Belle II Germany Meeting 2025** 

Sep 8 – 10, 2025

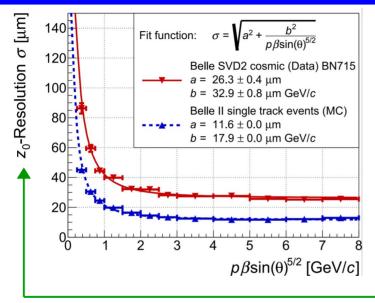
**Bonn** 

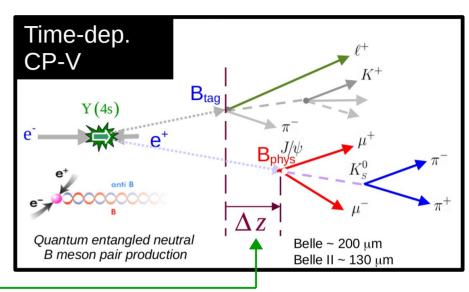
\* tadeas.bilka@desy.de tadeas.bilka@gmail.com (always online :-)



### Precision @ Belle II

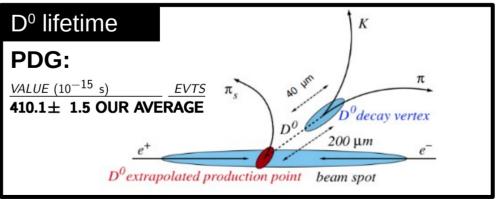
Just two examples...





Alignment precision at level of micrometers needed

Advanced track-based (time-dependent) alignment

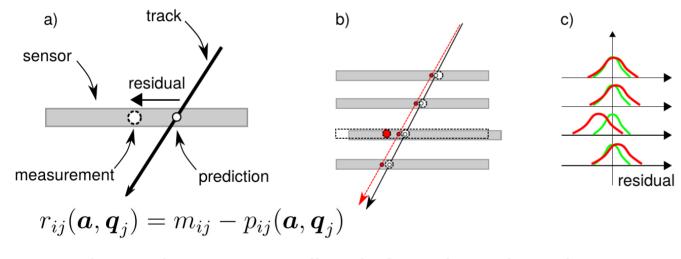




### Track-based alignment

Detection elements not in assumed positions/orientations/...

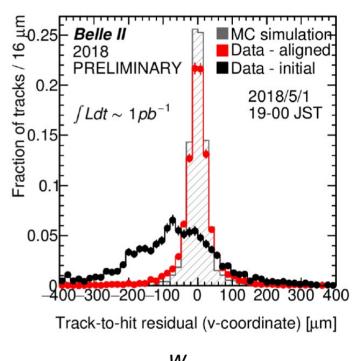
→ biased measurements & sub-optimal residuals

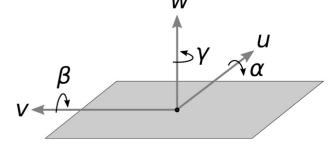


Estimate the geometry directly from the trajectories

→ minimize many millions of residuals!

$$\chi^2(oldsymbol{a},oldsymbol{q}) = oldsymbol{r}^\intercal(oldsymbol{a},oldsymbol{q})oldsymbol{V}^{-1}oldsymbol{r}(oldsymbol{a},oldsymbol{q}) \quad o \mathsf{min}$$

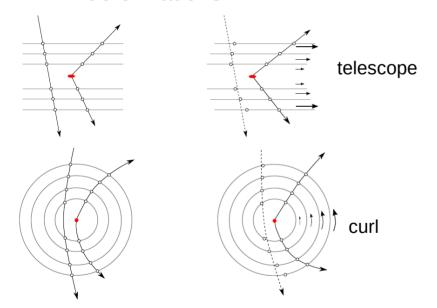






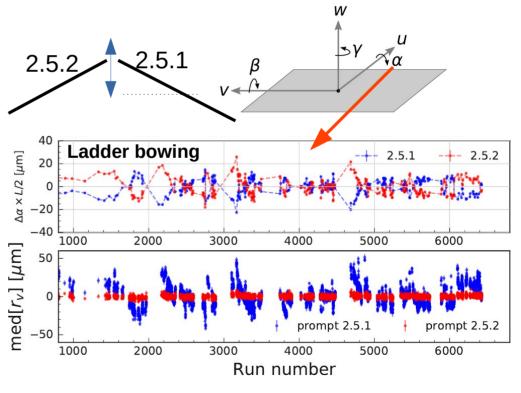
### Alignment Challenges

- Weak Modes
  - (some) data not sensitive to (some) deformations



- Detector&reco model issues
  - e.g. imperfect magnetic field description

- Time-dependence
  - Detector not stable, many effects at play





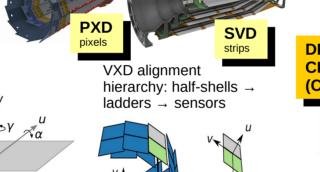
### Belle II Alignment "Constants"

Belle II

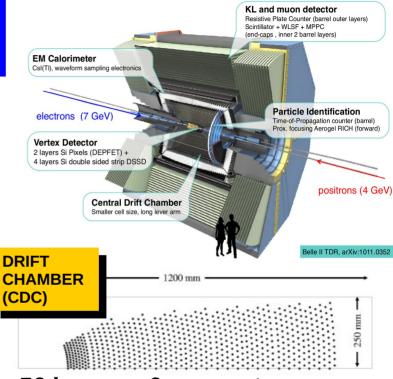


with help of J. Kandra

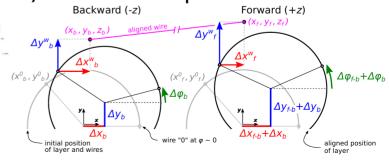
212 sensorsx 18 parameters



More than 60,000 parameters to be determined

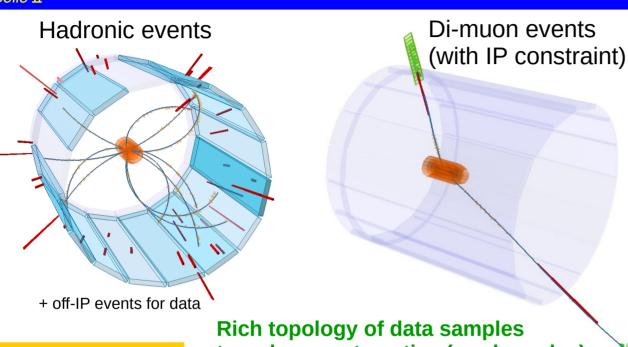


**56 layers x 6 parameters 14,336** wires x 4 parameters





### Data Samples for alignment

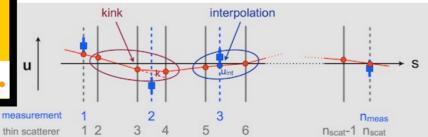


#### **General Broken** Lines (GBL)

Track model with proper description of multiple scattering

Belle II = low mom. particles relative to CMS

to reduce systematics (weak modes)



Recorded during collisions

Cosmic events

(merged tracks)

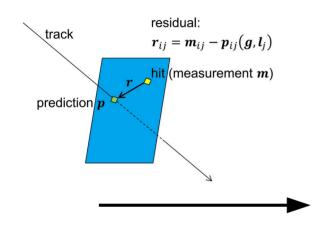
Also works for cosmics without magnetic field, implemented massconstrained decays ...



#### Alignment Algorithm: Millepede II





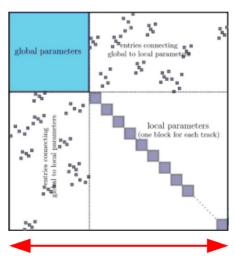


#### Minimize over all parameters:

$$\chi^{2}(\boldsymbol{g},\boldsymbol{l}) = \sum_{j}^{\text{tracks hits}} \boldsymbol{r}_{ij}^{T}(\boldsymbol{g},\boldsymbol{l}_{j}) V_{ij}^{-1} \boldsymbol{r}_{ij}(\boldsymbol{g},\boldsymbol{l}_{j})$$

g ... alignment parameters (global)  $l_i$  ... track parameters (local)

Millepede II



~ 100's of millions of track parameters for typical alignment

Block matrix algebra

→ no approximation
except linearization
(→ iterations)

All correlations kept
in the solution!

@ Belle II

Matrix for global par.

Diagonalization, Inversion, MINRES, Decomposition ...

New: LAPACK for solution

| Method            | Factorisation | Calc. inverse | QtAQ, QA-1Qt | Total time |
|-------------------|---------------|---------------|--------------|------------|
| Decomposition     | 331           | -             | no A·1 9.7   | 361        |
| Inversion         | -             | 852           | 20.0         | 898        |
| MKL, packed       | 6.3           | 1338          | 18.4         | 1377       |
| MKL, unpacked     | 4.2           | 19.8          | 2.1          | 40         |
| OpenBlas, unpack. | 4.8           | 10.0          | 15.9         | 45         |

Time in minutes. Table from C. Kleinwort

up to ~ 60k

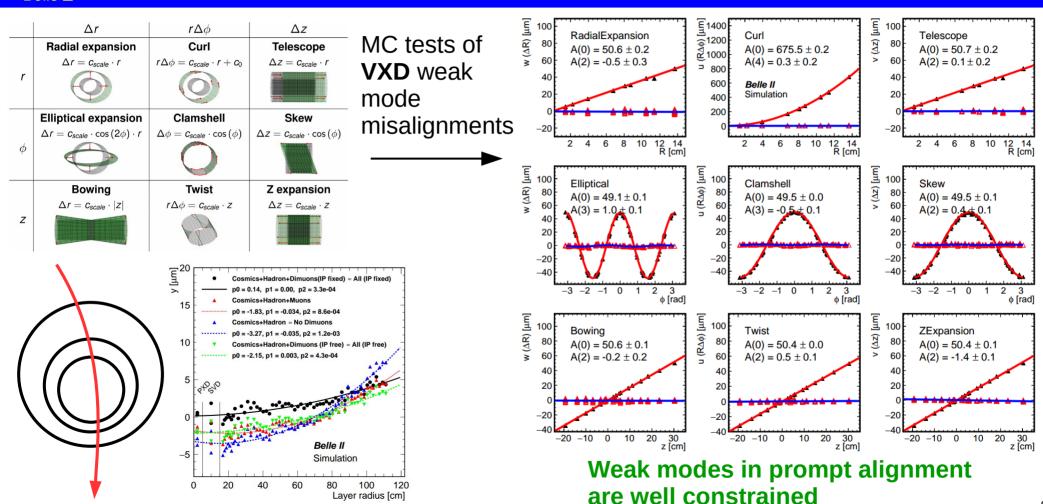
With recent speed-ups, an exact solution for 60k parameters can be obtained in about 30 min\*!

https://www.terascale.de/wiki/millepede\_ii/ https://helmholtz.software/software/millepede-ii

\*Using 10 cores @ Xeon(R) CPU E5-2640 v3 @ 2.60GHz. 20GB of memory required.



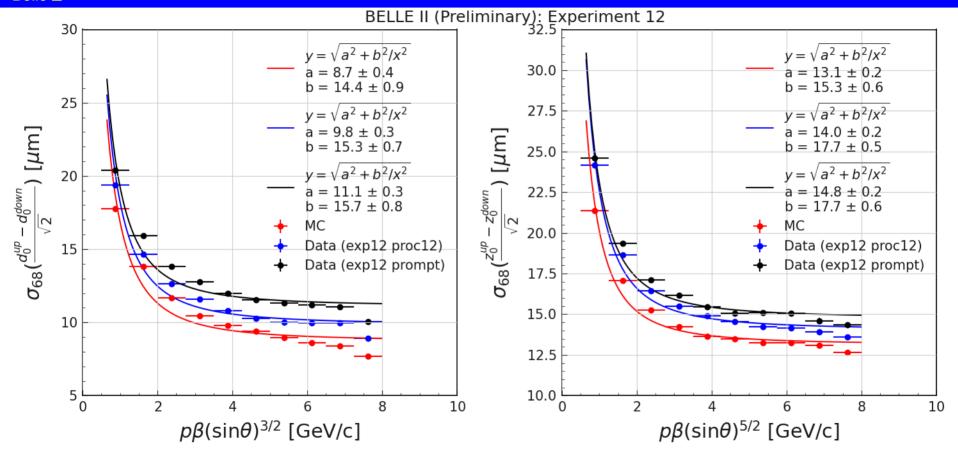
# Weak Modes in Prompt Alignment (without wires and IPdimuons)





### Impact Parameter Resolutions

selection="abs(Z01)>0.3&&
abs(Z02)>0.3"

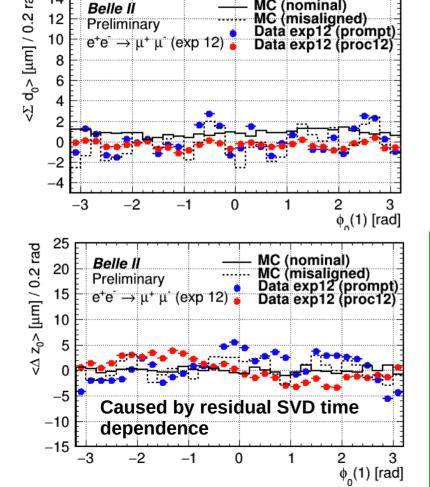


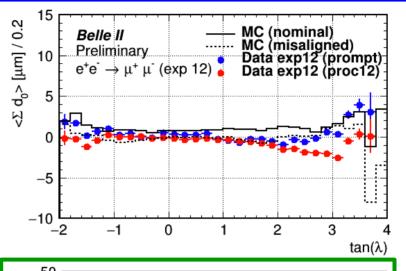
Reprocessing-like alignment deployed already at prompt calibration stage since 2021 → no waiting for reprocessing for publication-level alignment quality!



### Vertexing systematics for dimuons

MC (nominal)





Belle II

Preliminary

 $\rightarrow \mu^+ \mu^- \text{ (exp 12)}$ 

Ö

[mm]

 $z_0$ >

-10

-20

-30

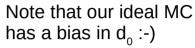
-40

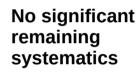
MC (nominal)

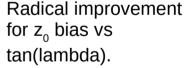
MC (misaligned)
Data exp12 (prompt)

tan(λ)

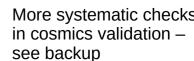
Data exp12 (proc1







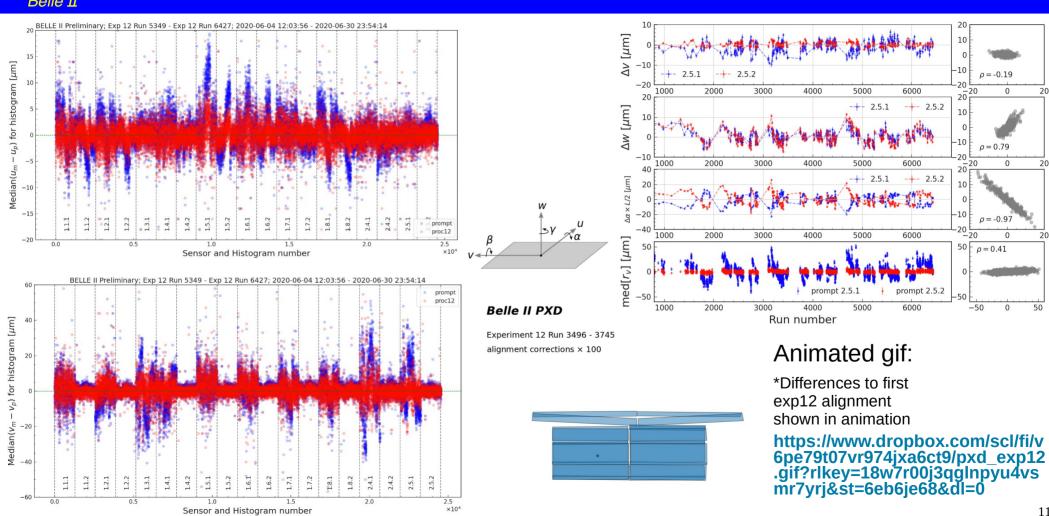
#### **Systematics can be** well reproduced on MC



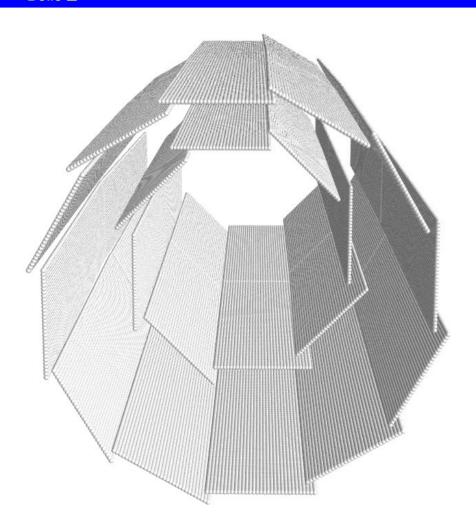
More systematic checks



# PXD Alignment evolution example





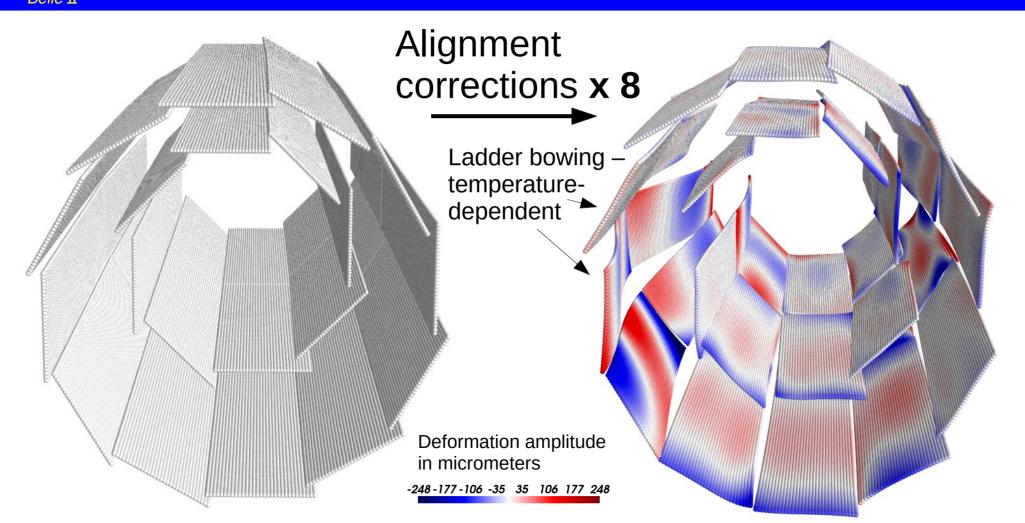


# Real shape of the PXD2 (sensitive areas)

as determined by the alignment during commissioning (B=0T cosmics)

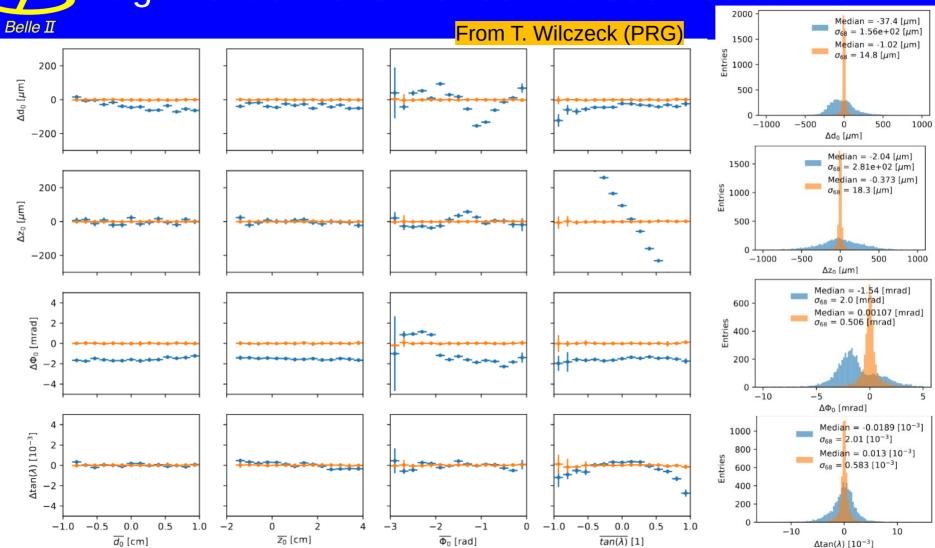


# Rew PXD & Alignment x 8



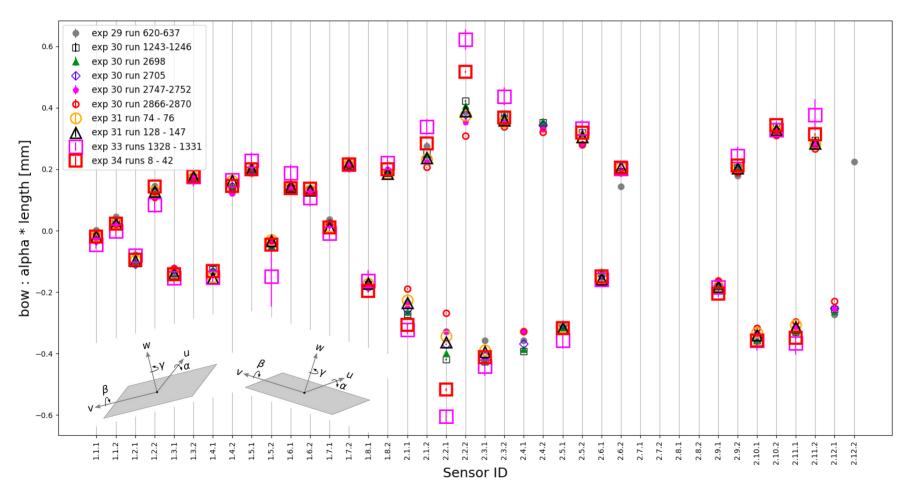


### Alignment & Performance with cosmics & B=0T





# PXD2 ladder bowing amplitude in different 2024 periods



Max bowing for operated ladders between 300-650 um.

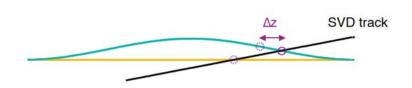
Depends on beam currents (and which sensors are turned on)

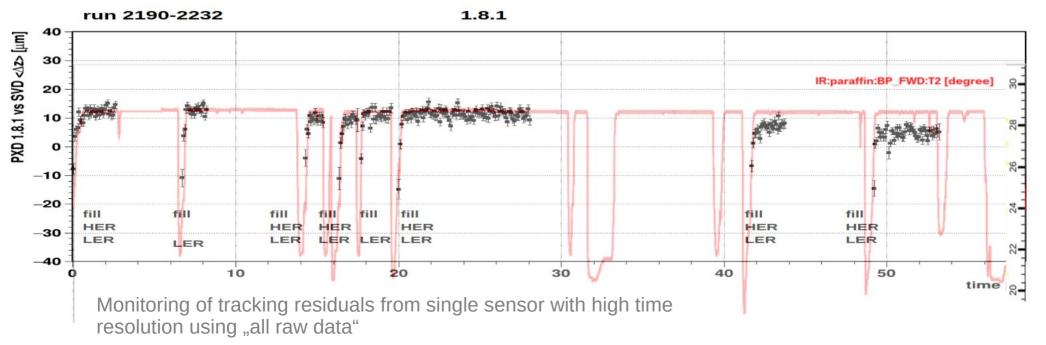
Two ladders with largest bowing turned off in beam operations :-(



## PXD2 & New Alignment Challenges

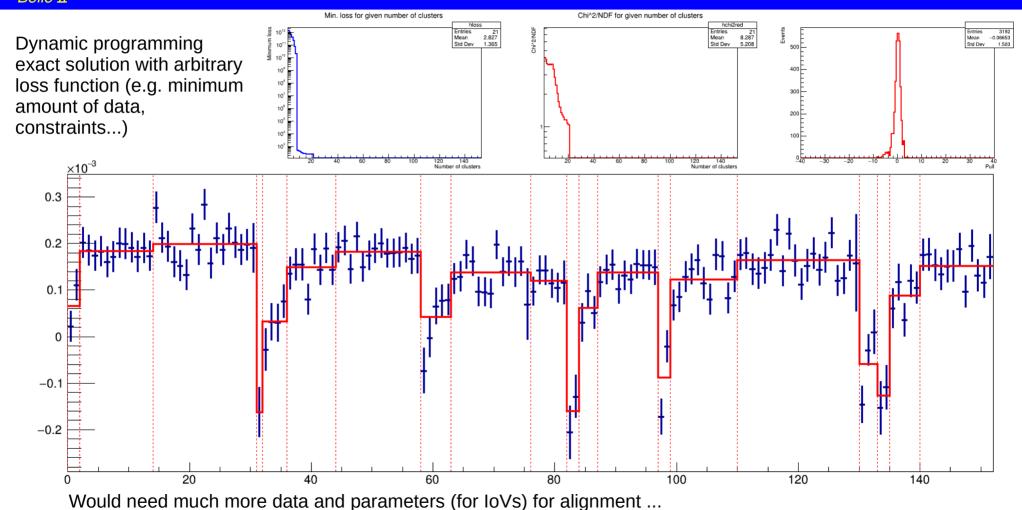
Observed (also) very fast bowing-like deformations correlated to beampipe temperature ← depends on beam currents





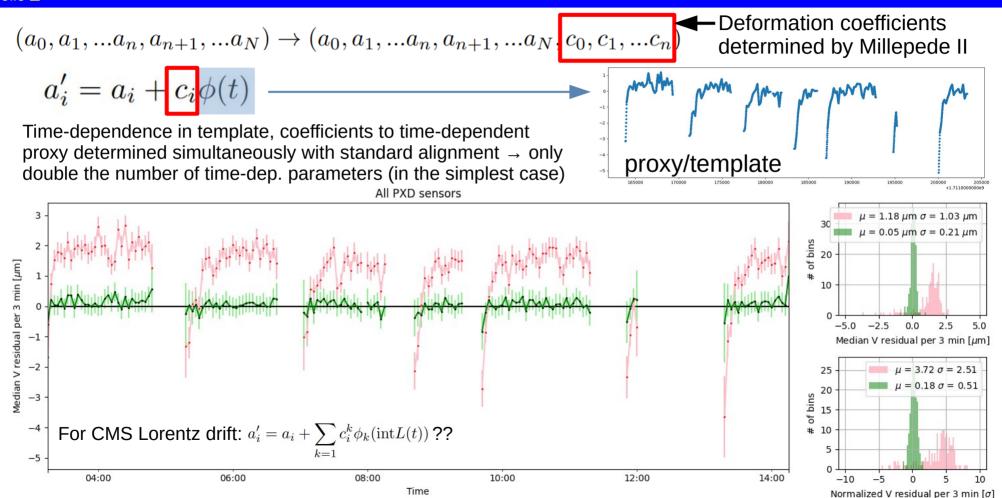


### Automatic loVs from clustering with loss function?





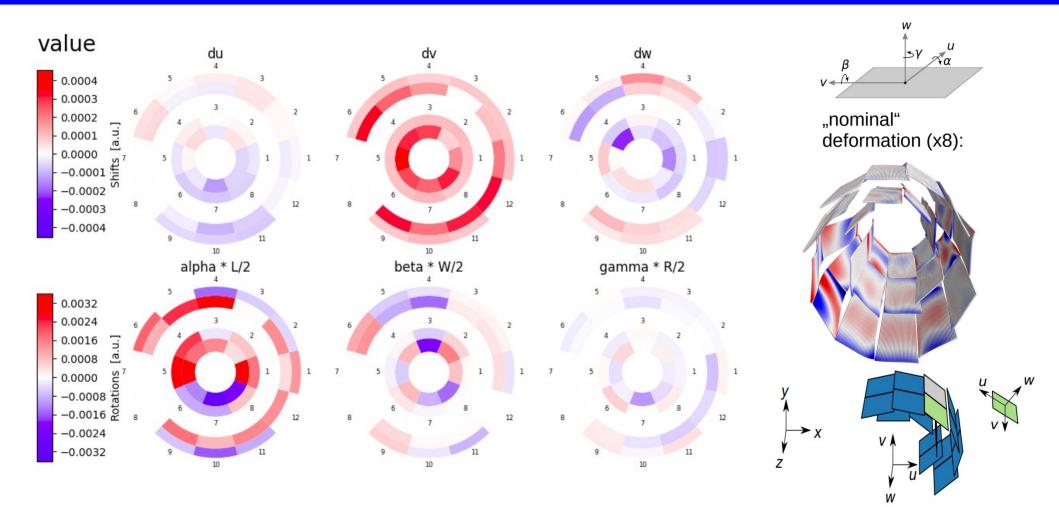
### Alignment with Time-Dependent Template(s) ?



Or, if you "know" deformation coefficients, determine instead single amplitude in many IoVs...



### PXD deformation coefficients (rigid body)



# Conclusion & Outlook

- Precise alignment required for precision physics
- Belle II alignment determines about 60k parameters for pixel and strip detectors and the drift chamber promptly after data-taking
  - CDC layers and PXD&SVD hafl-shells and individual PXD sensors are aligned about every 50k di-muon events (+some cosmics) → once in several hours (depending on lumi)
- Alignment performance pretty good in MC simulations and data validations
  - Some remaining discrepancies related residual time dependence and to imperfect magnetic field description or other detector modelling defficiencies
  - Data-driven conservative misalignment scenario available for systematics estimation in physics analyses
    - + one more data-driven (from day-to-day alignment differences) + 2 MC-based (residual misalignments)
- New challenges with new PXD
  - Need much "faster" alignment if the beam conditions keep changing frequently
  - But not all data available at the calibration site
  - Alignment already takes ¼ to ½ a day (multiple passes over data needed)
  - Possible solutions
    - Much more data for alignment → expensive
      - Alignment on GRID? (Need high-performance high-memory machine processing data after each collection step)
    - "Parametrize" deformations with less degrees of freedom → maybe not feasible (work in progress)
    - Ignore (flag bad quality vertex data ...)

. . .



### Thank you for your attention!



### **BACKUP**



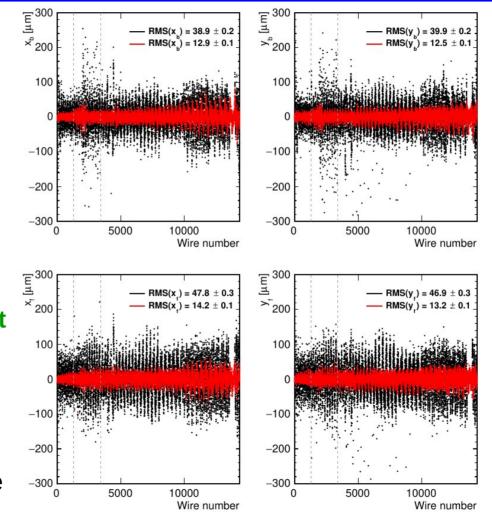
### Full scale MC tests with misaligned wires

**Black**: initial realistic misalignment

**Red**: remaining residual misalignment

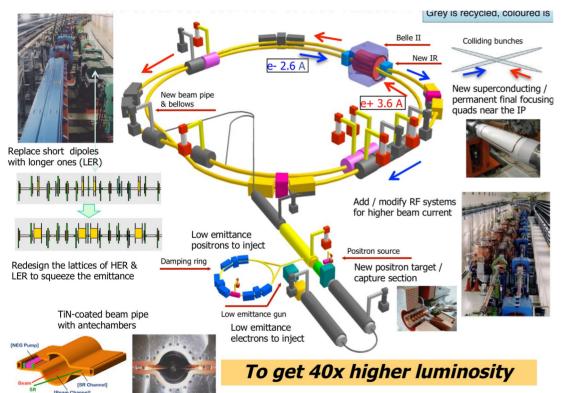
Can recover from a realistic wire misalignment to negligible residual misalignment in a single iteration!

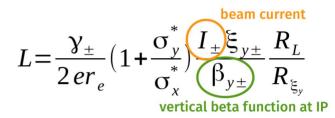
First use of decomposition solution method in Millepede

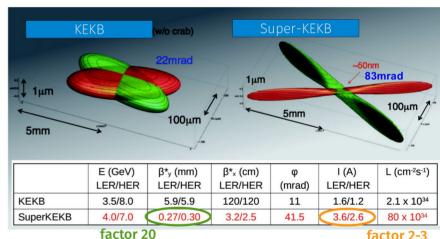




### KEKB → SuperKEKB



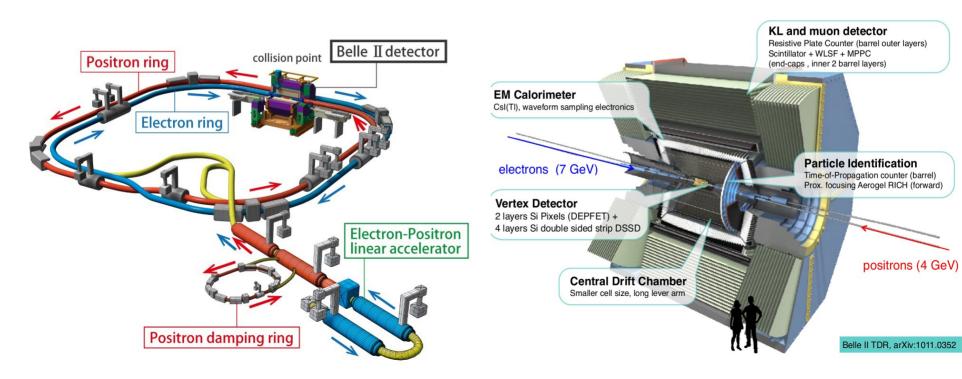






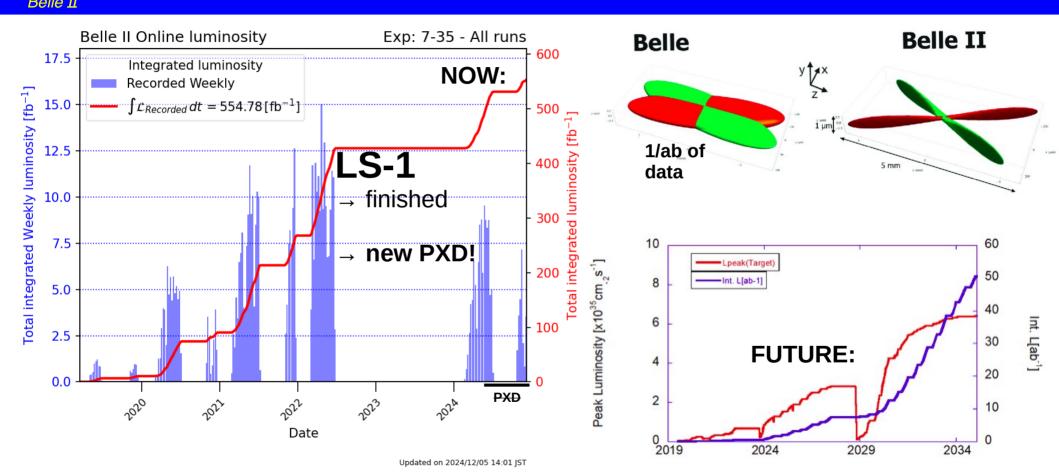
### SuperKEKB & Belle II

- Upgrade of KEKB & Belle, taking physics data since 2019
- Worlds' highest luminosity electron-positron collider (KEK, Tsukuba, Japan) at Upsilon(4S) resonance → B physics, D physics, tau physics ...





#### Past, Present, and Future

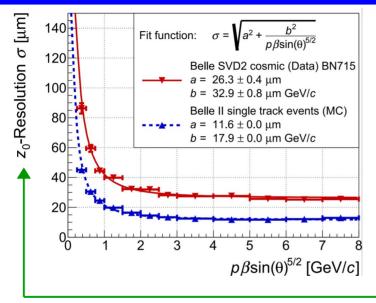


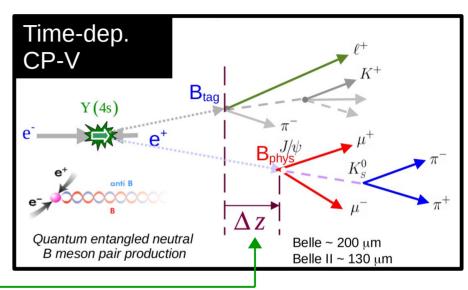
Systematic errors will start to dominate measurement precisions for many analyses



### Precision @ Belle II: low-momentum compared to CMS

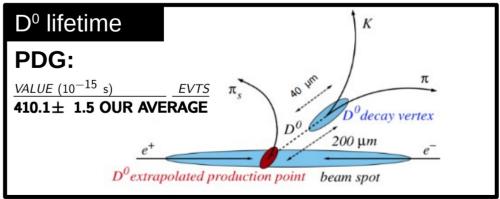
Just two examples...





Alignment precision at level of micrometers needed

Advanced track-based (time-dependent) alignment

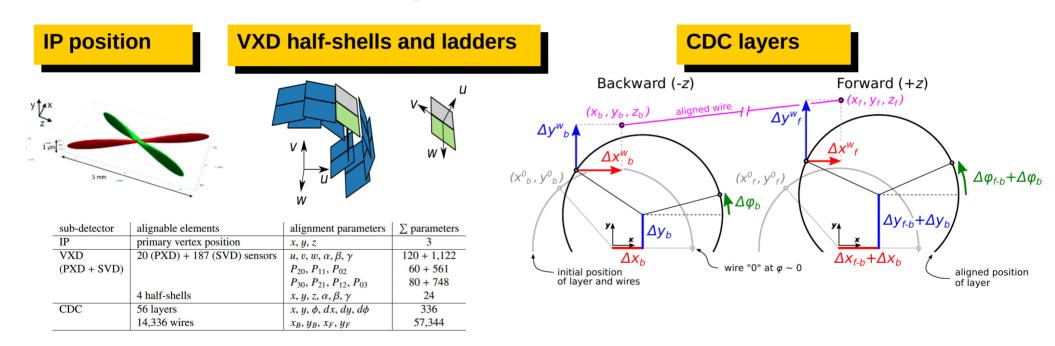




### Belle II Alignment Parameters: 2/2

Relative positions of sub-detectors and larger structures\*

**Problem**: Correlations with local alignment and correlations of different sub-detectors!



Alignment of all degrees of freedom should be done simultaneously → Millepede II !!!

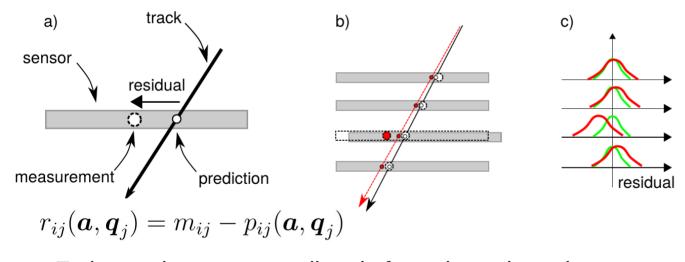
\*Redundant DoFs removed by linear equality constraints



### Track-based alignment

Detection elements not in assumed positions/orientations/...

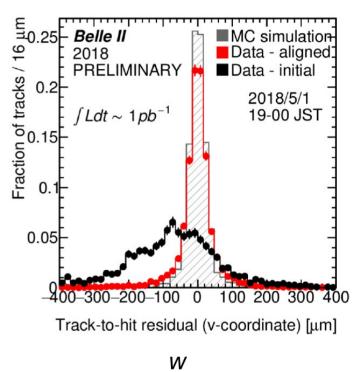
→ biased measurements & sub-optimal **residuals** 

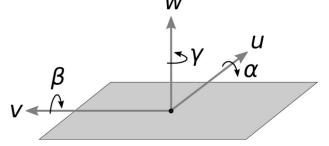


Estimate the geometry directly from the trajectories

→ minimize many millions of residuals!

$$\chi^2(oldsymbol{a},oldsymbol{q}) = oldsymbol{r}^\intercal(oldsymbol{a},oldsymbol{q}) V^{-1}oldsymbol{r}(oldsymbol{a},oldsymbol{q}) 
ightarrow ext{min}$$

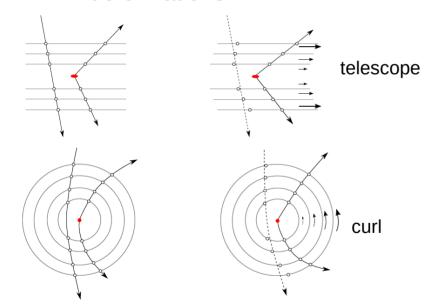






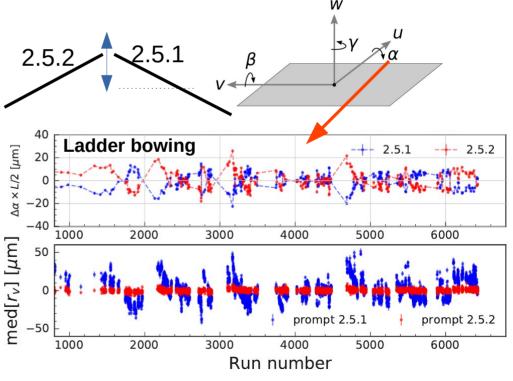
### Alignment Challenges

- Weak Modes
  - (some) data not sensitive to (some) deformations



- Detector&reco model issues
  - e.g. imperfect magnetic field description

- Time-dependence
  - Detector not stable, many effects at play

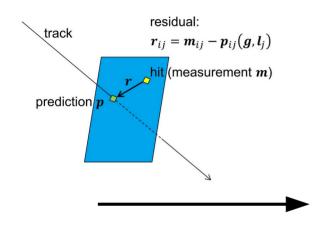




#### Alignment Algorithm: Millepede II





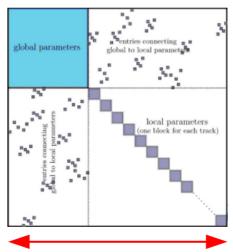


#### Minimize over all parameters:

$$\chi^{2}(\boldsymbol{g},\boldsymbol{l}) = \sum_{j}^{\text{tracks hits}} \boldsymbol{r}_{ij}^{T}(\boldsymbol{g},\boldsymbol{l}_{j}) V_{ij}^{-1} \boldsymbol{r}_{ij}(\boldsymbol{g},\boldsymbol{l}_{j})$$

g ... alignment parameters (global)  $l_i$  ... track parameters (local)

#### Millepede II



~ 100's of millions of track parameters for typical alignment

@ Belle II Block matrix algebra → no approximation Matrix for except linearization global par. iterations) Diagonalization. All correlations kept Inversion MINRES. in the solution! Decomposition ...

#### New: LAPACK for solution

| Method            | Factorisation | Calc. inverse | QtAQ, QA-1Qt | Total time |
|-------------------|---------------|---------------|--------------|------------|
| Decomposition     | 331           | •             | no A-1 9.7   | 361        |
| Inversion         | -             | 852           | 20.0         | 898        |
| MKL, packed       | 6.3           | 1338          | 18.4         | 1377       |
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Time in minutes, Table from C. Kleinwort

up to ~ 60k

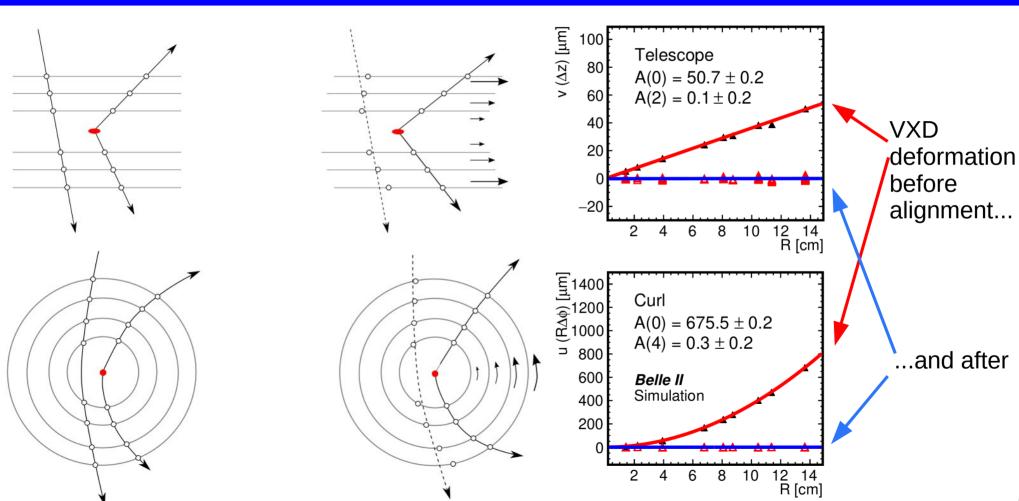
With recent speed-ups, an exact solution for 60k parameters can be obtained in about 30 min\*!

https://www.terascale.de/wiki/millepede\_ii/ https://helmholtz.software/software/millepede-ii

\*Using 10 cores @ Xeon(R) CPU E5-2640 v3 @ 2.60GHz. 20GB of memory required.

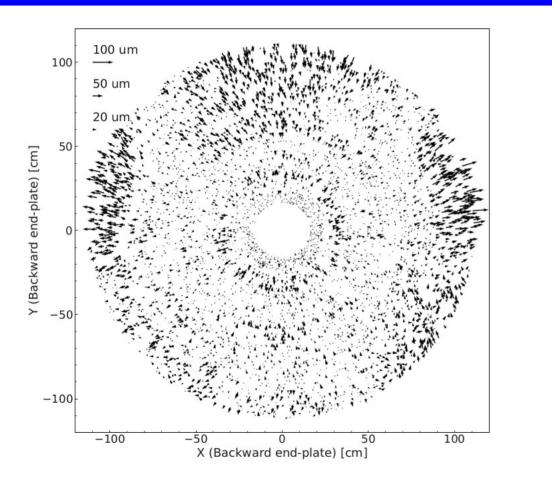


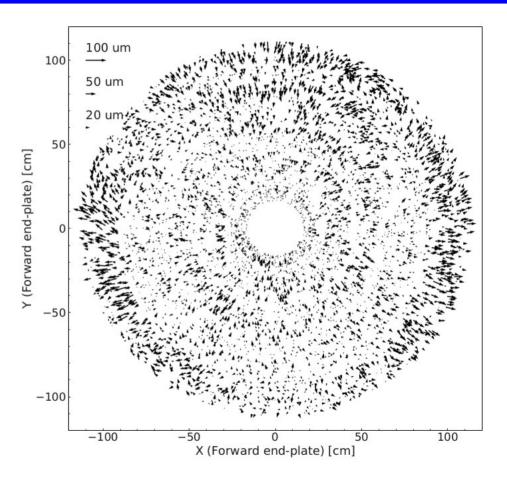
### Reducing weak modes with rich track topology





### Residual wire misalignment in MC

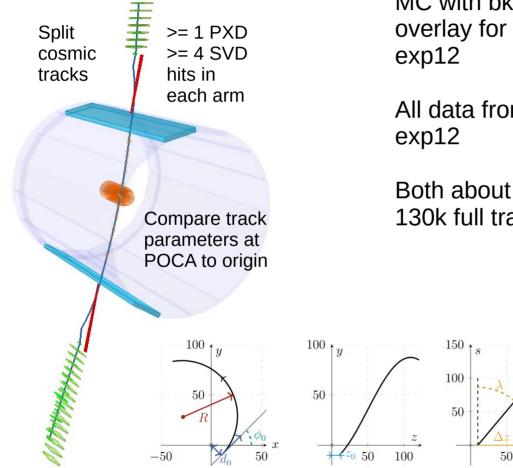


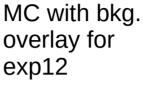


Only 20% randomly selected wires shown



### Cosmic Validation with PXD+SVD+CDC

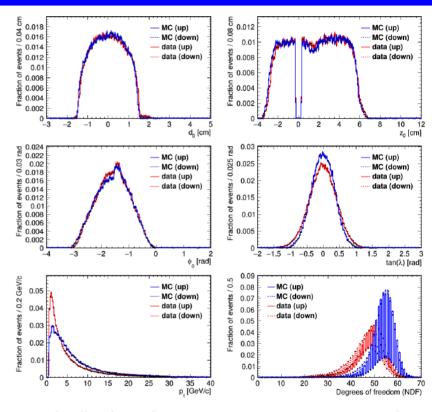




All data from

Both about 130k full tracks

100



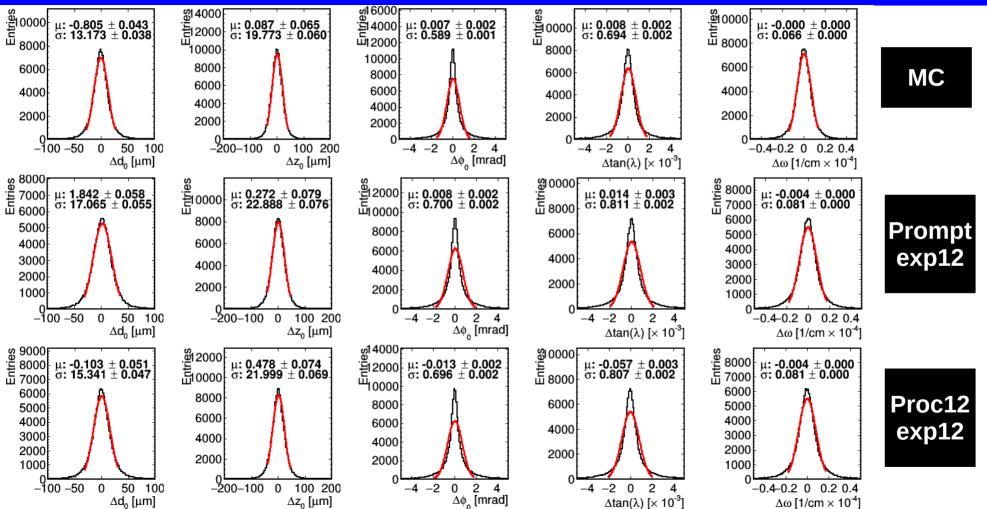
Distributions for transverse momentum and number of CDC hits are slightly different



#### Helix Parameter Resolutions

selection="abs(Z01)>0.5 && abs(Z02)>0.5 && Pt1>0.6 &&Pt2>0.6"

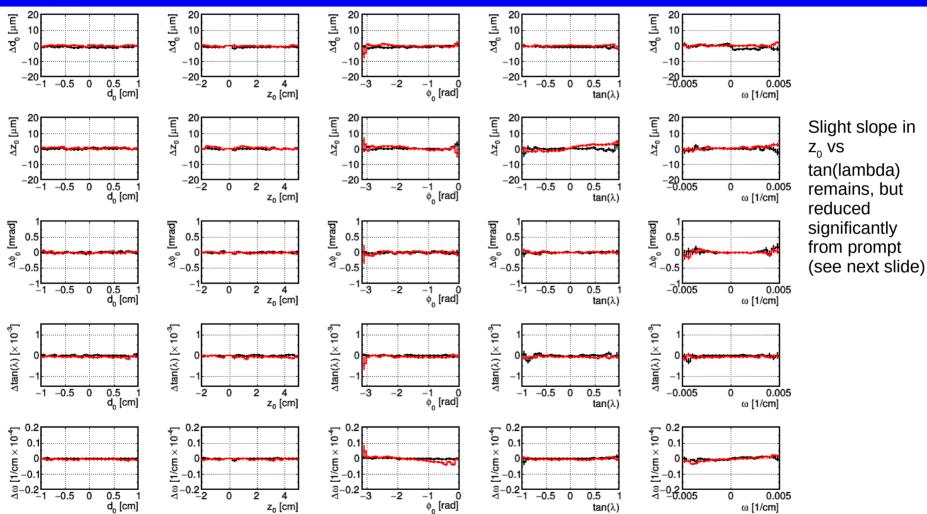






# Correlation of helix parameter biases: MC vs proc12





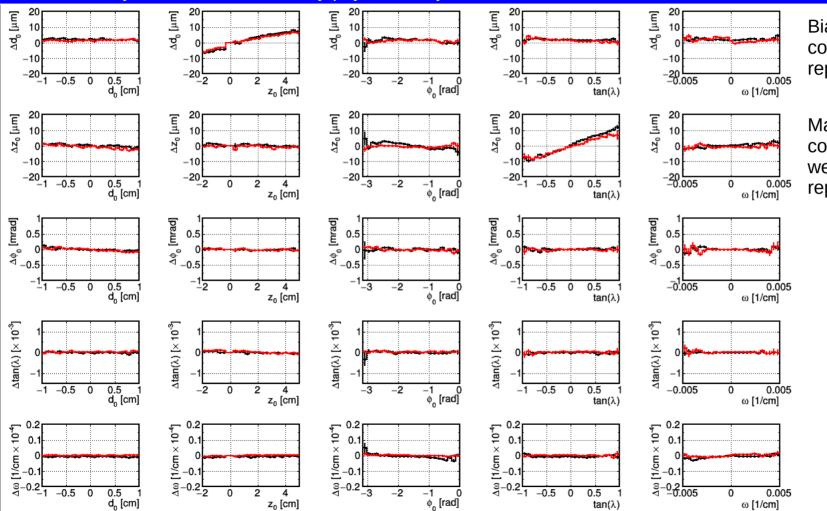
MC

Proc12 exp12



### Correlation of helix parameter biases: Conservative misalignment

Old prompt alignment vs MC with misalignment = largest misalignment scenario (of 4) used for alignment systematics estimation by physics analyses



Bias and correlation reproduced

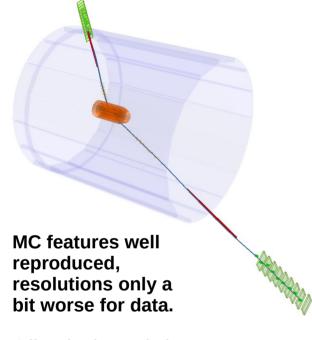
Main correlation well reproduced



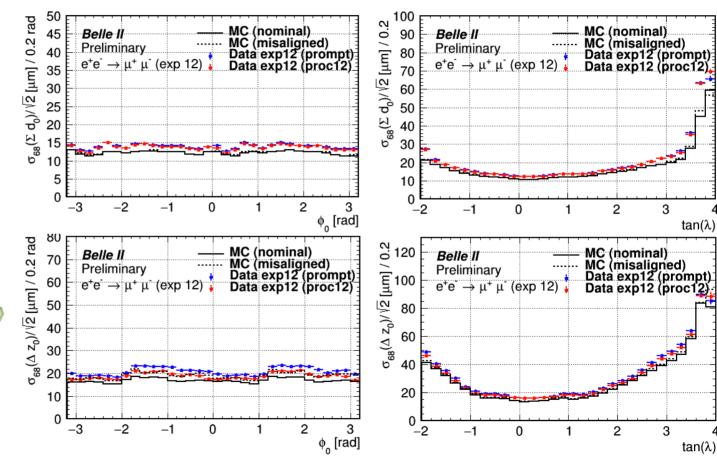
MC With Misal.



### Validation with Dimuons: Angular dep. of vertex resolutions



Offset in d<sub>0</sub> resolution related to (old) optimistic SVD simulation



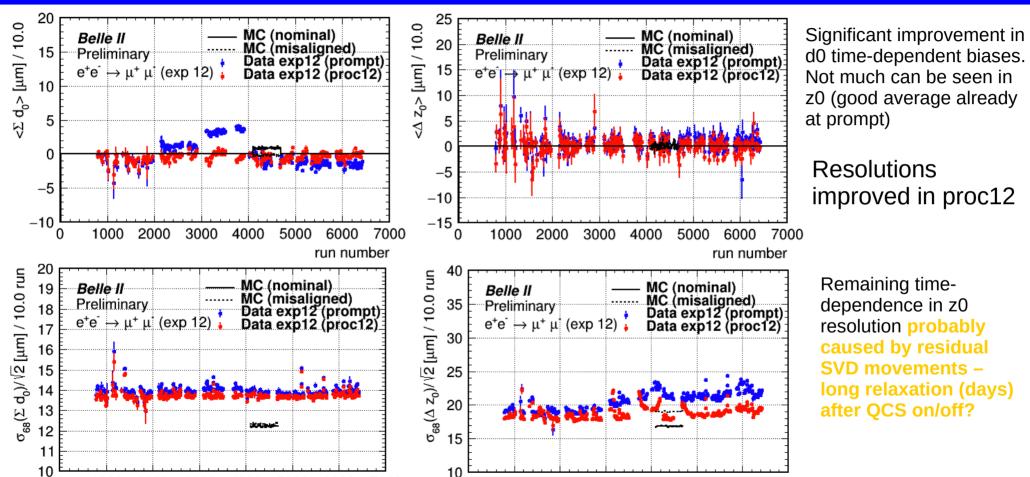
Angles for positive-charge muon candidate



run number

## Run dependence of vertex parameter biases and resolutions with dimuons

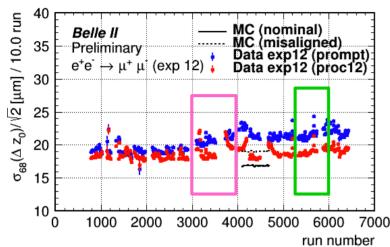


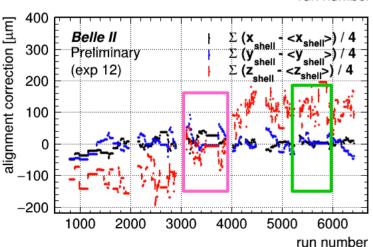


run number



### Residual SVD time-dependence after major events



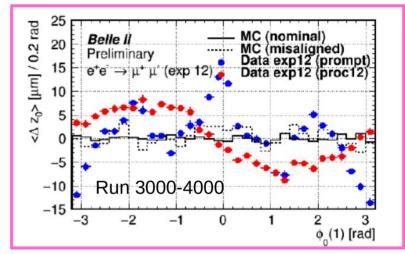


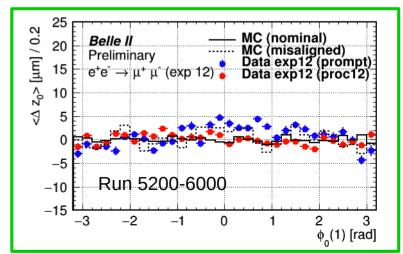
It seems the major remaining bias comes from a "typical" deformation in SVD: Not corrected, because SVD sensors are aligned once per bucket (shells each run)

Big step upwards in CDC deformation – VXD follows, but something more happens for SVD.

This is followed by continuous relaxation over several days... bad!!

Looks a bit like ladders shifting in z (5-10um in L3, maybe 20um in L4+, but not consistently







## Alignment basics: residuals



0.16

0.14

0.08

0.06

0.04

0.02

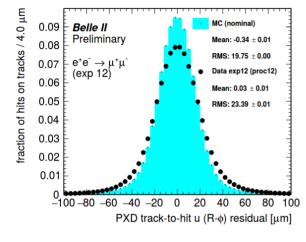
Belle II

Preliminary

 $e^+e^- \rightarrow \mu^+\mu^-$ 

(exp 12)

-100 -80 -60



Mean: 0.07 + 0.00

RMS: 14.78 ± 0.00

Data exp12 (proc12)

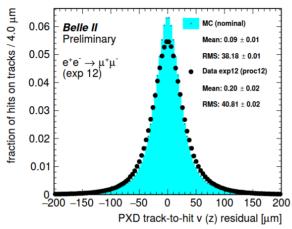
Mean: -0.17 ± 0.01

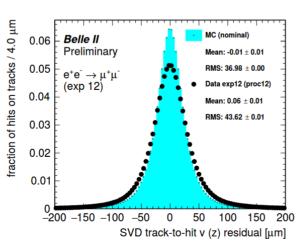
RMS: 21.14 + 0.00

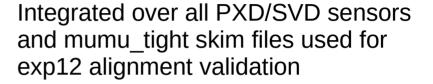
60 80 100

20

SVD track-to-hit u (R-φ) residual [μm]







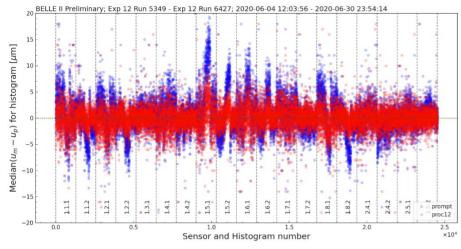
Much larger discrepancy for "u" probably comes from SVD

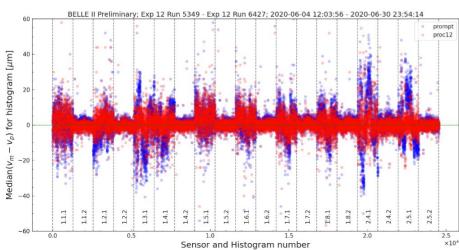
Intrinsic SVD sensor resolutions too optimistic on older MC – new MC simulation will address this

Cannot be caused by any kind of misalignment (confirmed)



# PXD Alignment evolution in exp12 reprocessing



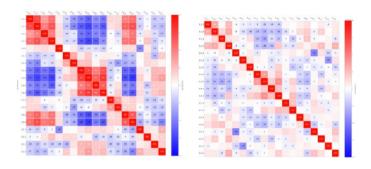


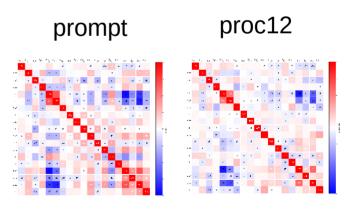
Even with this granularity (about 0.1/fb), alignment sometimes not fast enough to follow all movements

In U-direction. the remaining effects seem negligible

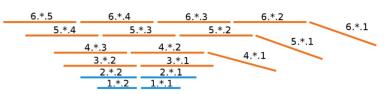
V-direction is worse and forward sensor more affected (due to track&detector topology)

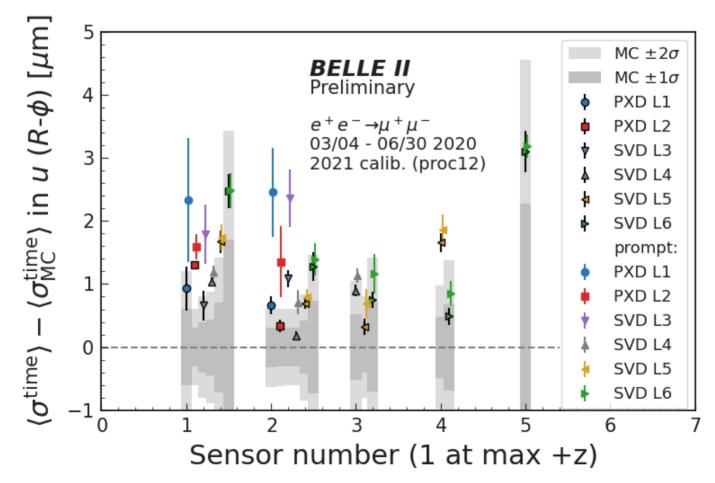
#### Correlations of residuals



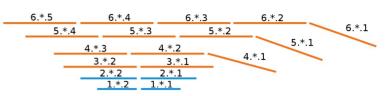


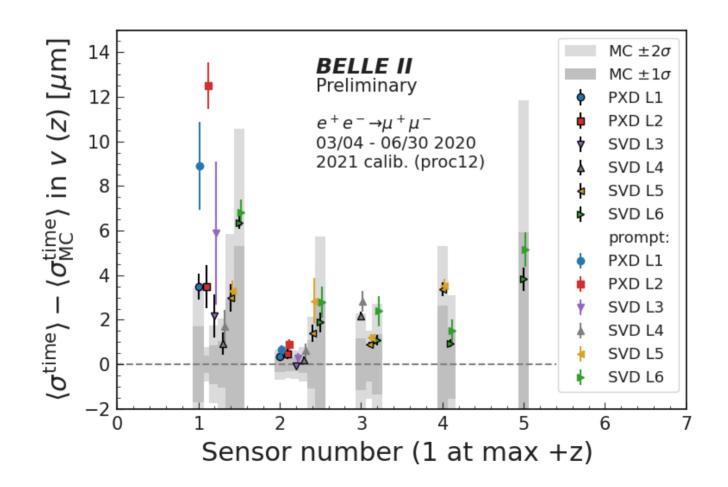






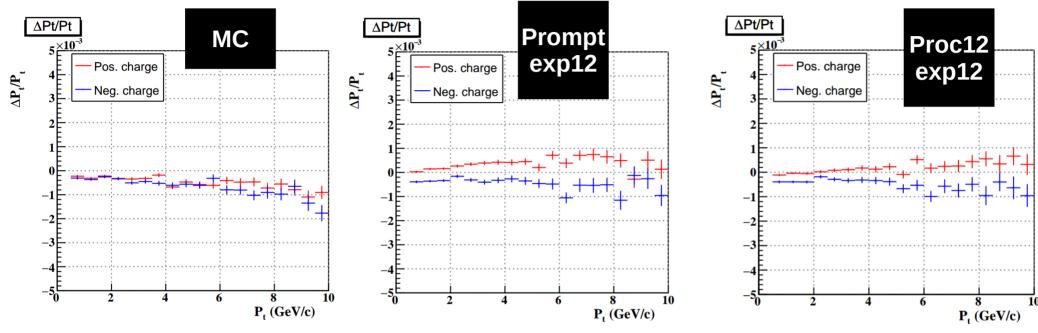








### Charge-dependent momentum biases for cosmics



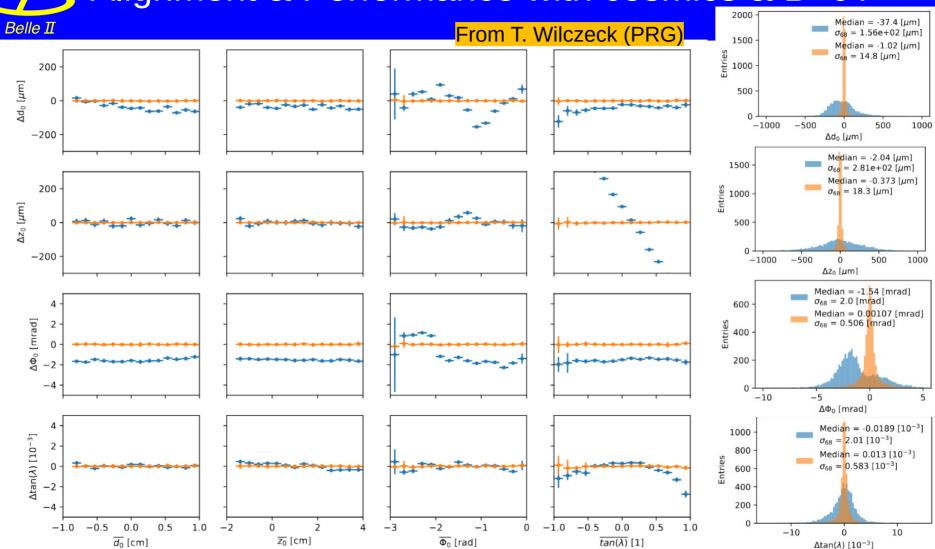
MC does have a larger bias, but not charge-dependent

General small (<10<sup>-3</sup>) problems with momentum biases (also vs. phi) might be related to compensation of problems beyond alignment (magnetic field / deformed CDC endplates / ...). Difficult to fix at alignment level (need better detector model). Solution: cos(theta) but also phi- and charge-dependent (sagitta) momentum corrections at analysis level.

It seems there is a residual twist caused by compensation of some inconsistencies (deformed CDC-endplates/ magnetic field description/?)

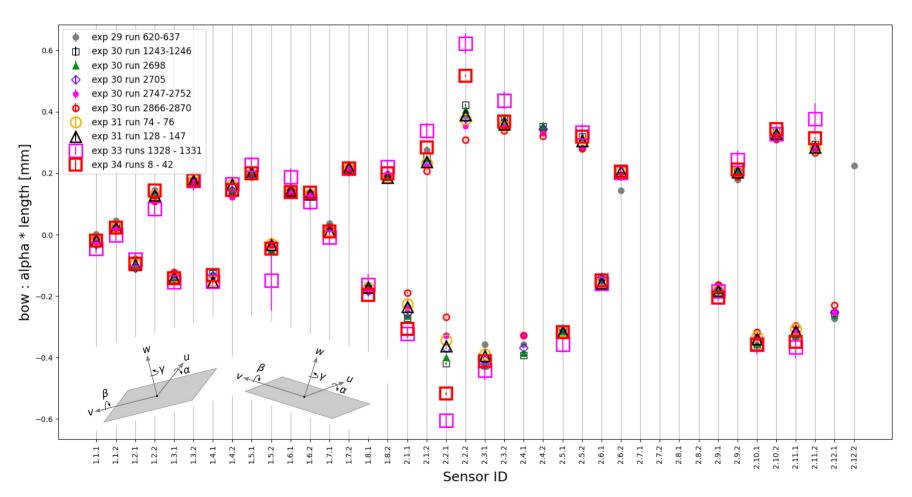


### Alignment & Performance with cosmics & B=0T





# PXD2 ladder bowing amplitude in different 2024 periods



Max bowing for operated ladders between 300-650 um.

Depends on beam currents (and which sensors are turned on)

Two ladders with largest bowing turned off in beam operations :-(



#### Belle II Calibration and Data Production

- Physics data calibrated in prompt calibration loop every bucket
  - Done at BNL
  - About a month after data
- Recalibration
  - KEKCC or NAF
  - After a year or two, all data when needed
  - Fix issues, improve...

**PROMPT Calibration** -Read-Uploadcalibrations Local runs u/mDST CDC tracking cal Upload-PXD masking Upload -Upload Download Readfraction of Download ARICH masking calibration HLT skims (RAW) u/mdst SVD CoG production TOP post-tracking Read -Alianment Final validation ARICH cDST production IP position Beam energy -Read-Raw data fraction of (grid) calibration HLT skims (cDST)

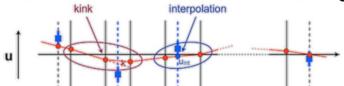
Bucket = several weeks of datataking (scaled to about 10/fb) Alignment: aim to provide the best possible performance for physics already in prompt calibration



#### **General Broken Lines**



- Track model with proper describtion of multiple scattering
- Track constructed from measurement and scattering points

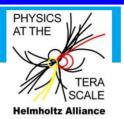


- > User has to provide at each point:
  - Residuals, measurement errors, projections from track coords. → measurement coords.
  - Jacobians of propagation between adjacent points
  - Scattering errors at scatterers; derivatives of residuals w.r.t. align. params (for MP2)
- > Track described by change of curvature and kinks at scattering points

$$x = (\Delta q/p, \mathbf{u}_1, ..., \mathbf{u}_{\text{# of scatterers}})$$

- > Track fit by minimization of:  $\chi^2(x) =$
- Interface to MP2

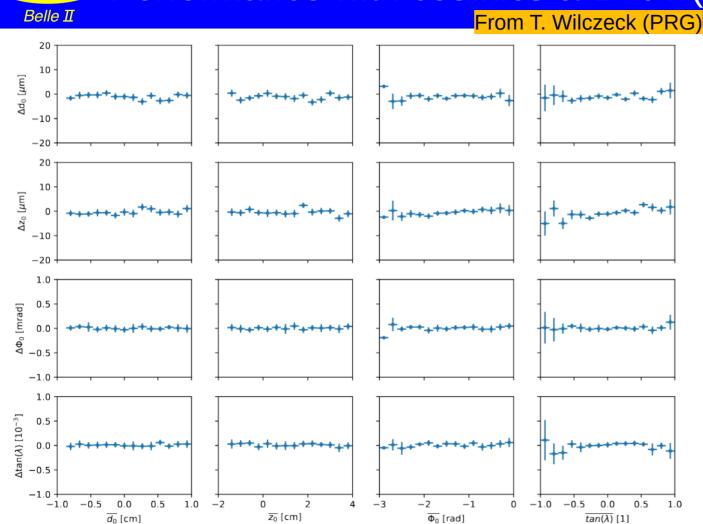
from measurements  $= \sum_{i=1}^{n_{\text{# meas}}} (\boldsymbol{H}_{m,i}\boldsymbol{x} - \boldsymbol{m}_i)^T \boldsymbol{V}_{m,i}^{-1} (\boldsymbol{H}_{m,i}\boldsymbol{x} - \boldsymbol{m}_i)^T$   $+ \sum_{i=1}^{n_{\text{# scat}}} (\boldsymbol{H}_{k,i}\boldsymbol{x})^T \boldsymbol{V}_{k,i}^{-1} (\boldsymbol{H}_{k,i}\boldsymbol{x})$ 



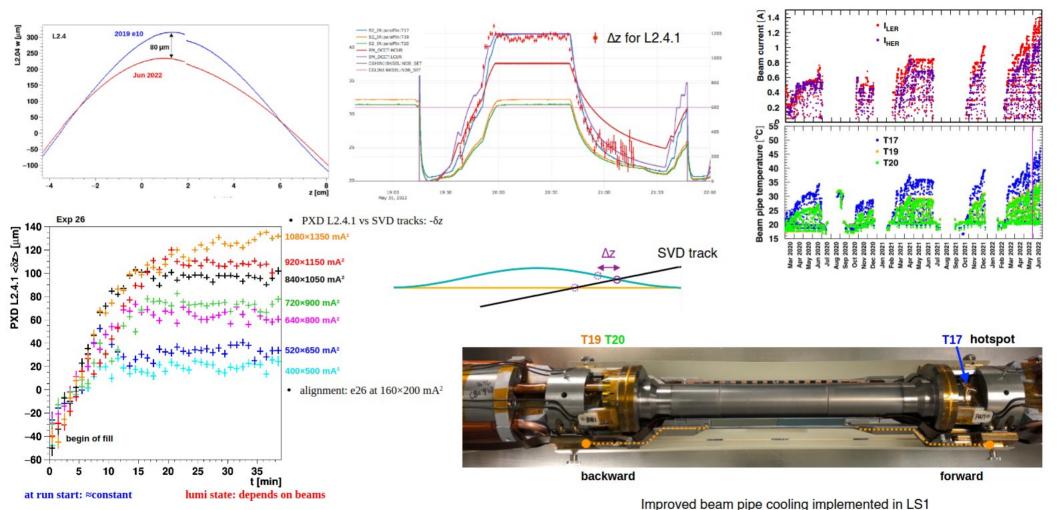
- → Integrated into GENFIT2 package
- → Profits from generic treatment of many different measurement types
- → Advanced treatment of material for multiple scattering estimation (thick scatterers)



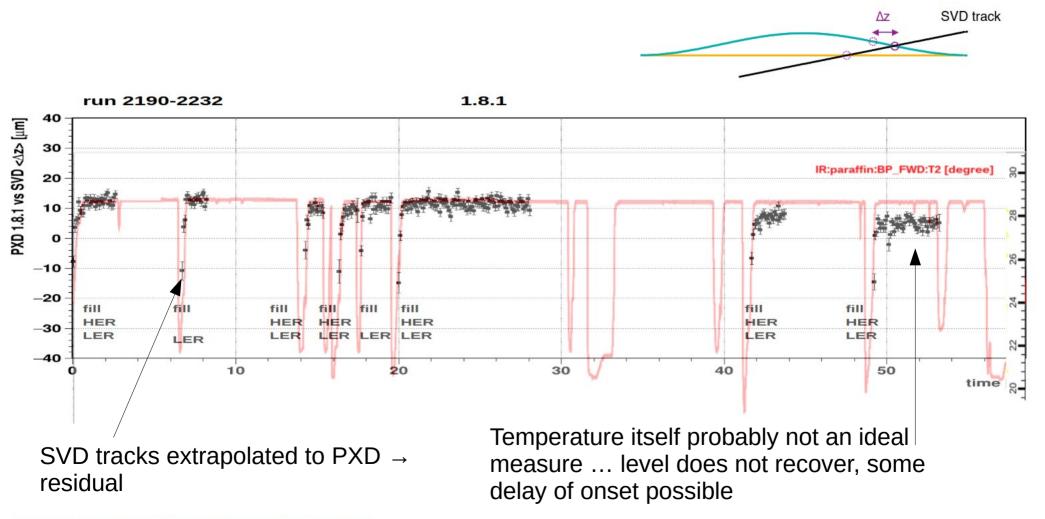
### Performance with cosmics & B=0T (PXD2)



### Reminder: Ladder Bowing in PXD1 L2 due to Beam Pipe Heating



#### L1 Ladder Bowing in March 2024



# Can the deformation be described (in first approximation) by a single time-dependent parameter?

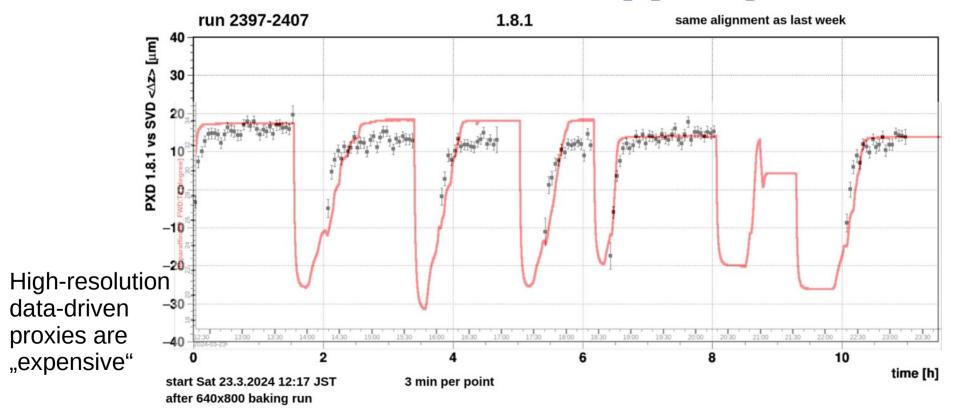
- All non-linearity in the time-dependence + each sensor parameter can have different (but constant) correlation to the temperature
  - Effects have to be reproducible (same temp → same deformation), relative behavior of sensors have to be constant (sliding starts at the same time)
- ... at least in the first approximation

Assume such a parameter exists and we can extract it from the data. Can we correct for these effects now?



### All charged tracks from IP: SVD to PXD extrapolation

### L1 residual trend and beam pipe temperature

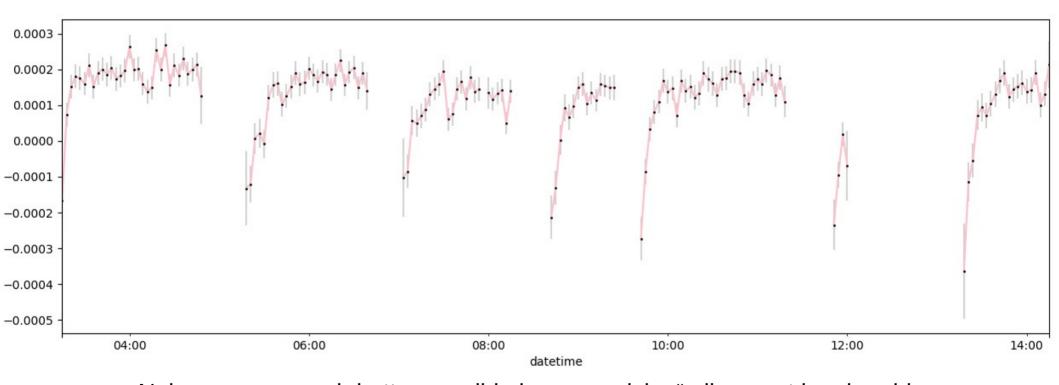


correlation not perfect (time lag): other influencers?



### Median V residual over all PXD sensors

Only di-muons, SVD to PXD extrapolation

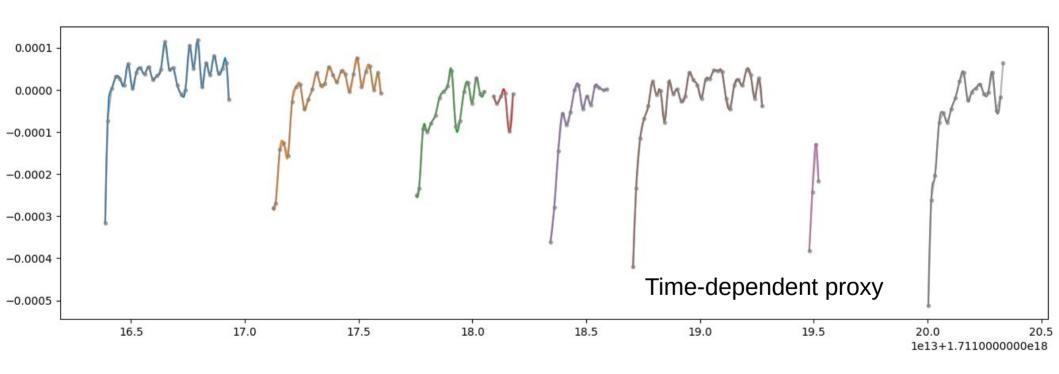


Naive proxy – much better possible by "pre-solving" alignment by absorbing residuals in u,v shifts for each sensor individually (higher-order residual proxies?)

# Belle II

### Fit with splines for up-sampling

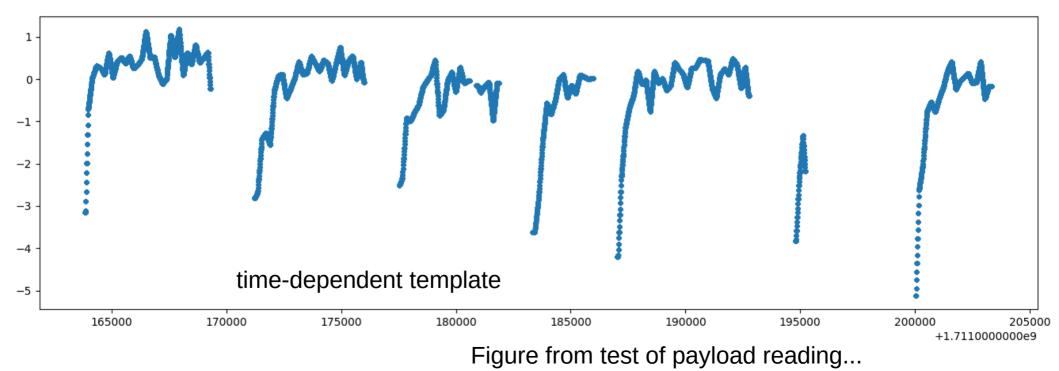
Subtract average and fit with splines for upsampling





### VXD deformation amplitude every 10 seconds

- Uploaded into database (IntraRunDependencies)
  - Our condition database has no notion of time need to fabricate it expost and parameterize by event numbers (due to variations in luminosity)

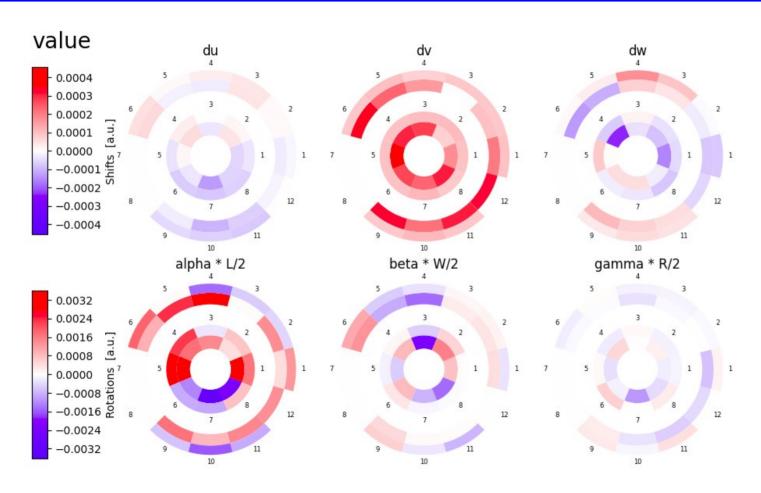


### Alignment with deformation parameters extraction

- Define for each PXD sensor alignment parameter a new alignment parameter
  - Same derivative as original, but multiplied by the (time-dependent) bowing amplitude (taken from GT)
  - $40 (-5) \times (6 + 3 + 4) = 520 (455)$  new parameters, constant over alignment period
- Determine complete VXD+CDC alignment + parameters of the deformation with Millepede II
  - Adjust the average and can absorb part of time-dependence which is coherent among sensors and proportional to the input bowing amplitude

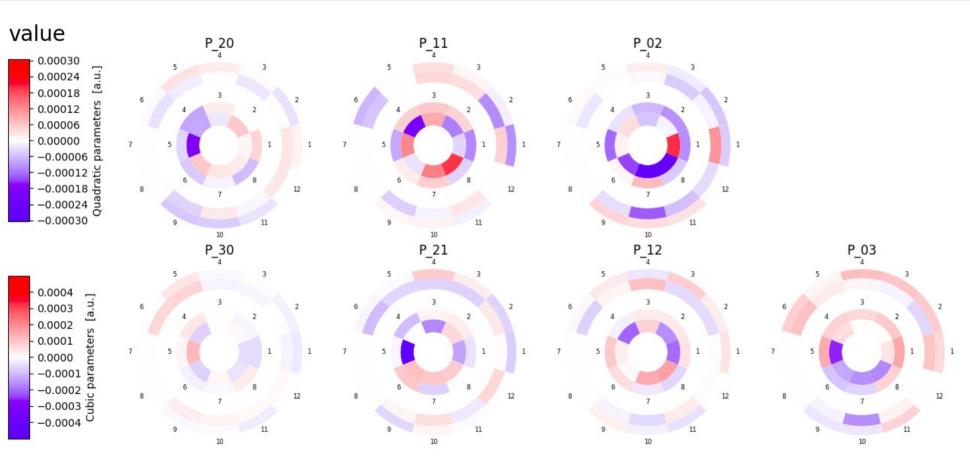


### PXD deformation coefficients (rigid body)



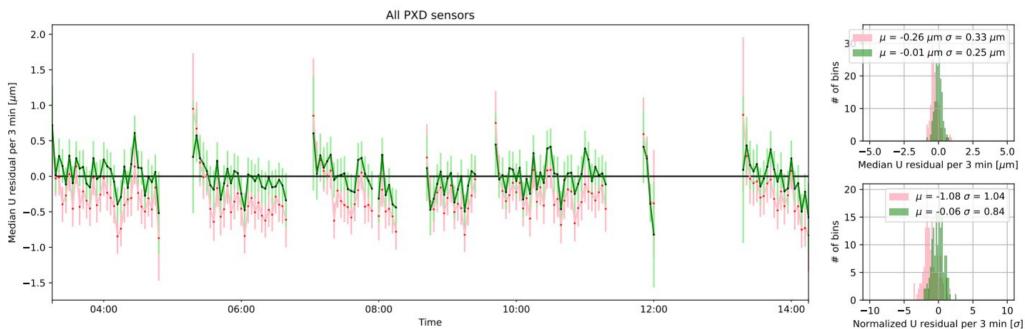


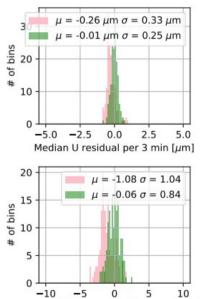
## PXD deformation coefficients (surface)

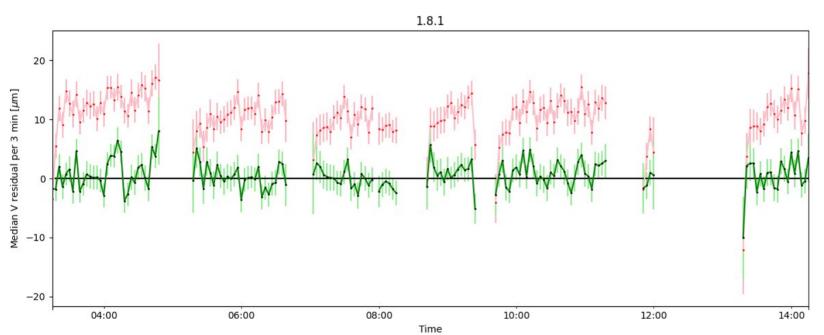


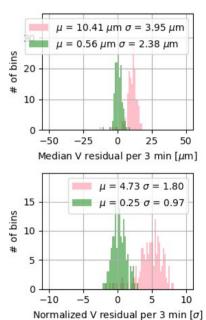
- Compare residuals versus time before and after
- U / V
- All sensors vs. individual sensors

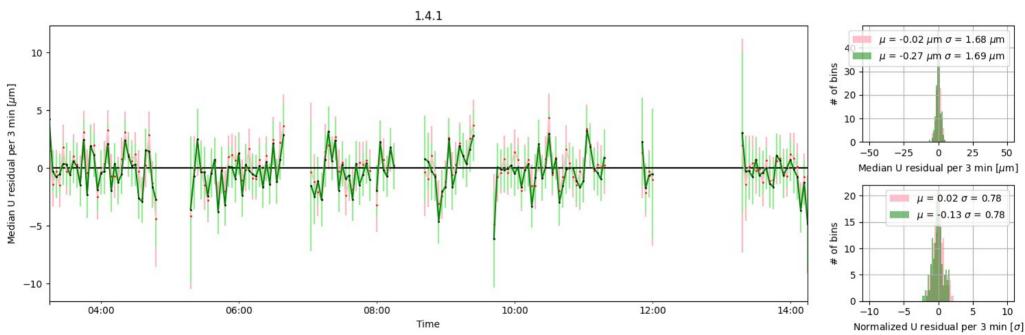


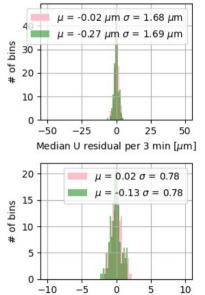


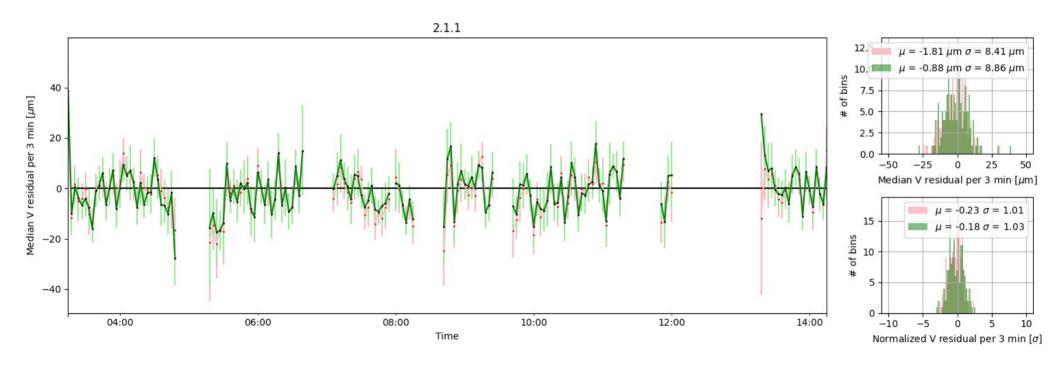








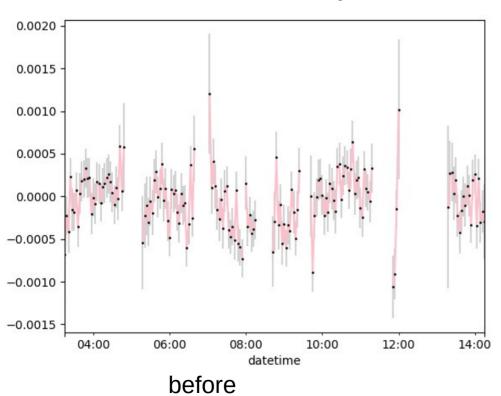


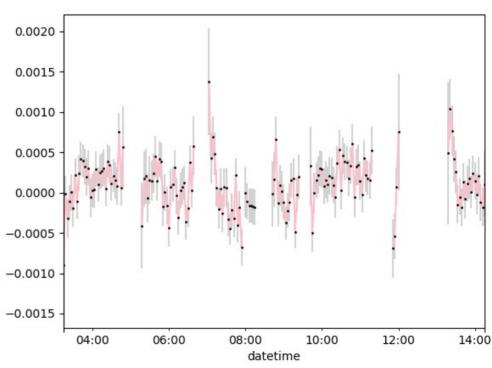


For L2 sensors, pulls usually not reduced

# All L2 V residuals

 Probably should add indepedent proxy and coefficients for layer 2





after

# Belle II

### Many open questions and work

- Really "safe" method?
  - Proxy does not match? → "zero" coefficients… still global minimum, should not get worse (really?)
- How much can we describe real detectors like this?
  - How many parameters can we reduce? Could describe slow evolution of high granularity structures at fine level? Needs already some knowledge of time dependence (L1+L2+... or separately? ...)
- Templates from residual validation vs. template basis
  - Physics-informed: continuous versus step movements
- Interaction with existing IoV methods, pixel detector recalibration (CMS), iterations, integration into existing workflows...
- Derivation of proxies
  - Machine learning? Learn from high-frequency proxies → better proxies for lower statistical resolution
- So far only "proof-of-concept" on 10 hours of Belle II data
  - Possibly years of work (also for students)