



The 21st International Conference  
on Hadron Spectroscopy and Structure

Measurement of Branching Fraction of

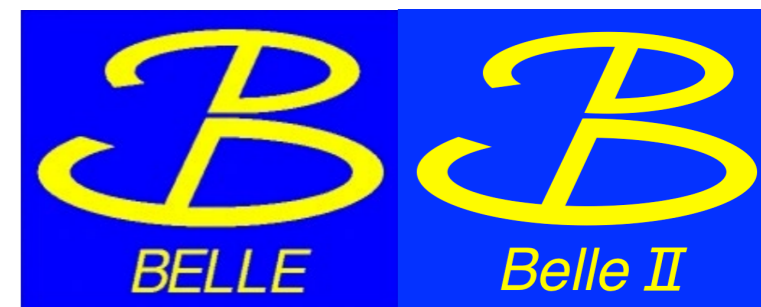
$$\Lambda_c^+ \rightarrow p K_S^0 \pi^0 \text{ at Belle}$$

YoungJun Kim (Korea University)

On behalf of Belle & Belle II Collaborations



March 27, 2025

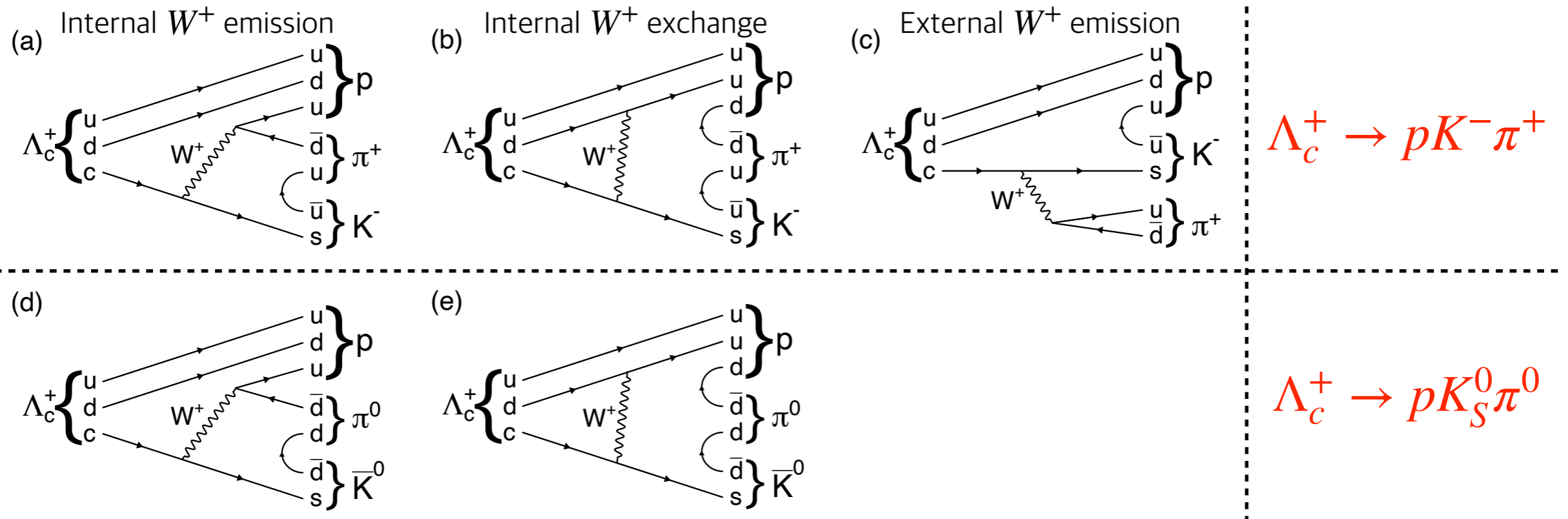


# Overview

Presentation about paper (submitted to PRD)  
Please find [arXiv:2503.04371](https://arxiv.org/abs/2503.04371)

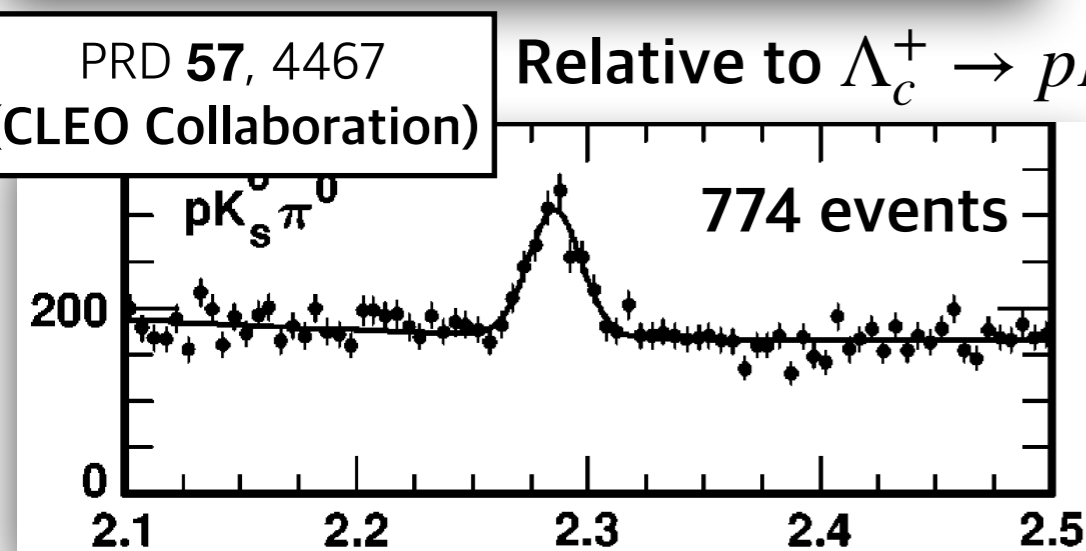
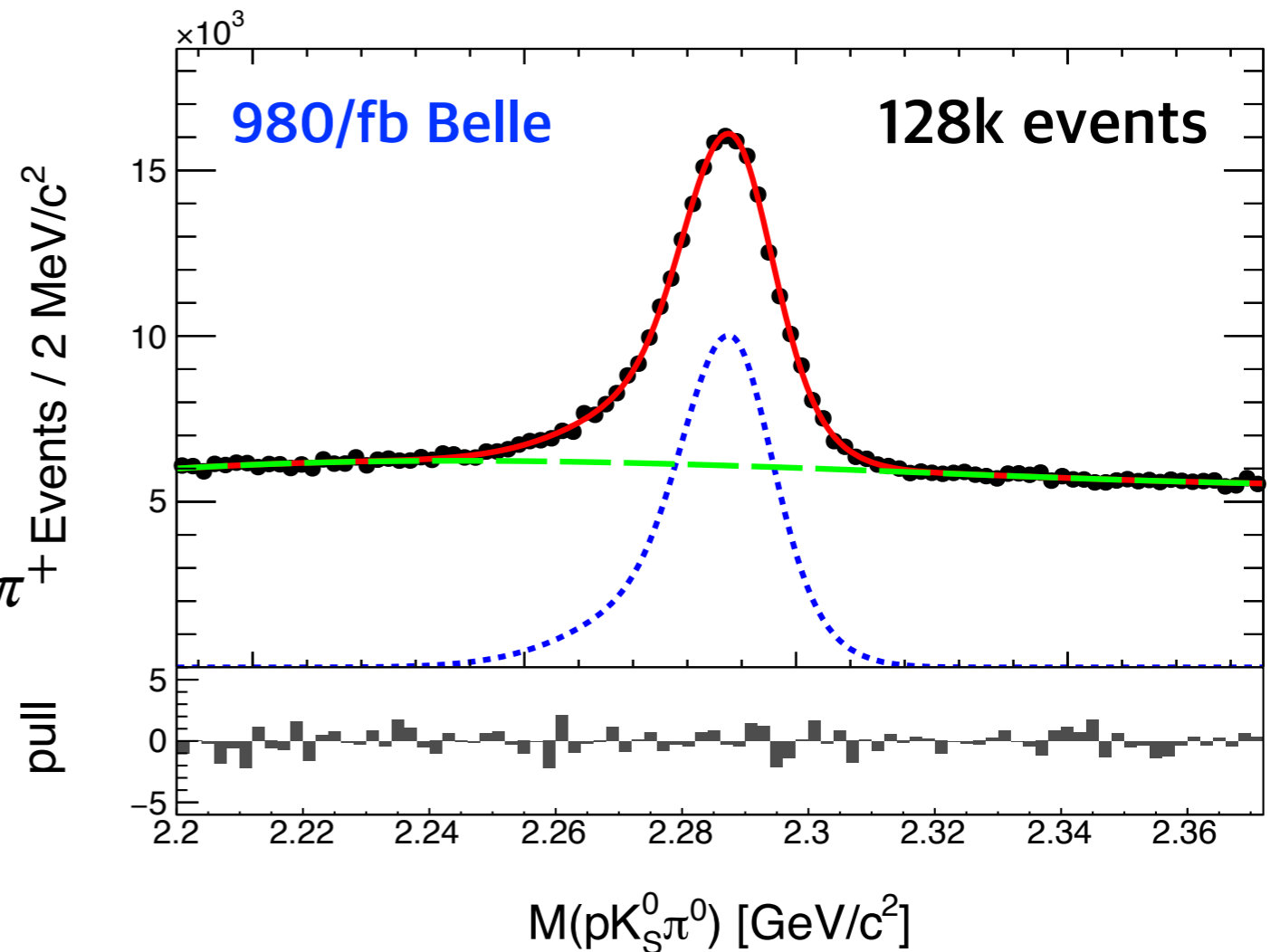
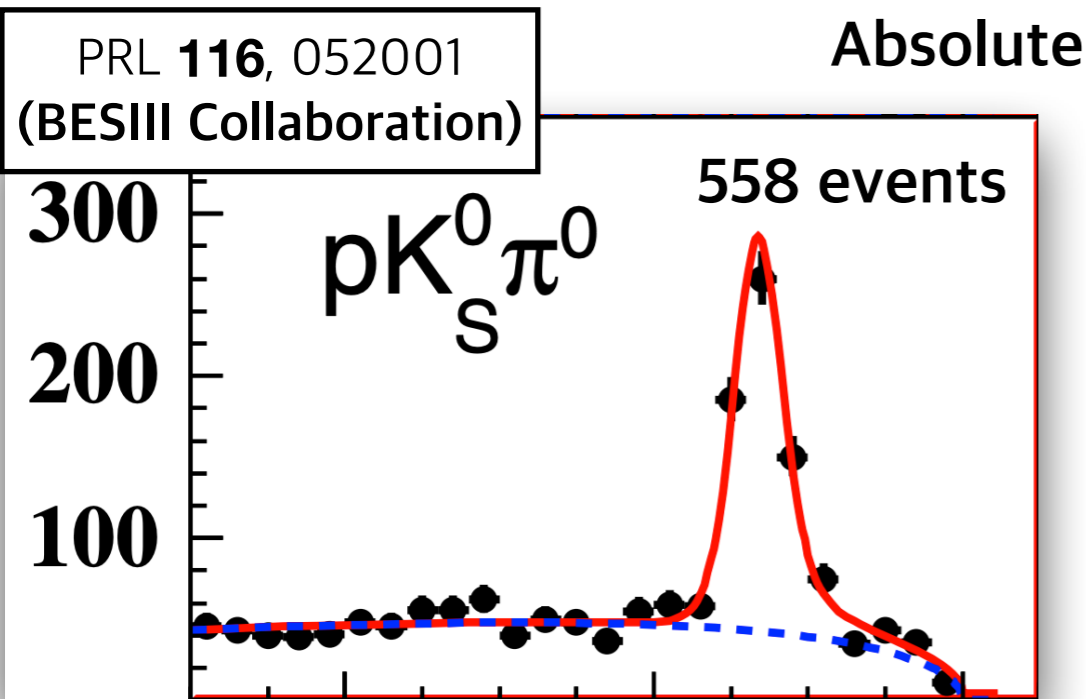
- Motivation
- Branching ratio measurement
  - ➔ Reconstruction and Efficiency
  - ➔ Yield Extraction
  - ➔ Relative and absolute Branching Ratios
- Intermediate structures
  - ➔ Dalitz plots
  - ➔ Two particle mass projections

# Physics analysis motivation



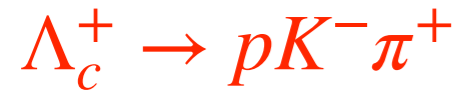
- $\Lambda_c^+ \rightarrow N\bar{K}\pi$  decays are good playground testing the isospin properties.
- $\Lambda_c^+$  decays result in a final state with  $I_3 = 1$  ( $c \rightarrow sud$  transition,  $\Delta S = 1$ )
  - ➔ Isospin symmetry:  $\sqrt{2}\mathcal{A}(p\bar{K}^0\pi^0) + \mathcal{A}(pK^-\pi^+) + \mathcal{A}(n\bar{K}^0\pi^+) = 0 \rightarrow$  amplitude and phase
- (a), (b), (d), (e) are color-suppressed, (c) is color-allowed
  - ➔ Direct  $\pi^+$  emission leaves the  $ud$  in the  $\Lambda_c^+$  as a spectator,  $uds$  cluster is pure  $I = 0$ .
  - ➔ If direct  $\pi^+$  emission(c) is dominant,  $\Lambda_c^+ \rightarrow \Lambda\pi^+$  is favored over  $\Lambda_c^+ \rightarrow \Sigma^0\pi^+$ .  
However, in experiment results, they are comparable. How about  $\Lambda^*$  and  $\Sigma^*$ ?

# Physics analysis motivation

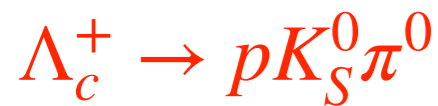


- Update of the  $\Gamma(\Lambda_c^+ \rightarrow pK_S^0\pi^0)/\Gamma(\Lambda_c^+ \rightarrow pK^- \pi^+)$  with **x100** statistics than previous reports
- First investigation of intermediate resonances in the  $\Lambda_c^+ \rightarrow pK_S^0\pi^0$  decay

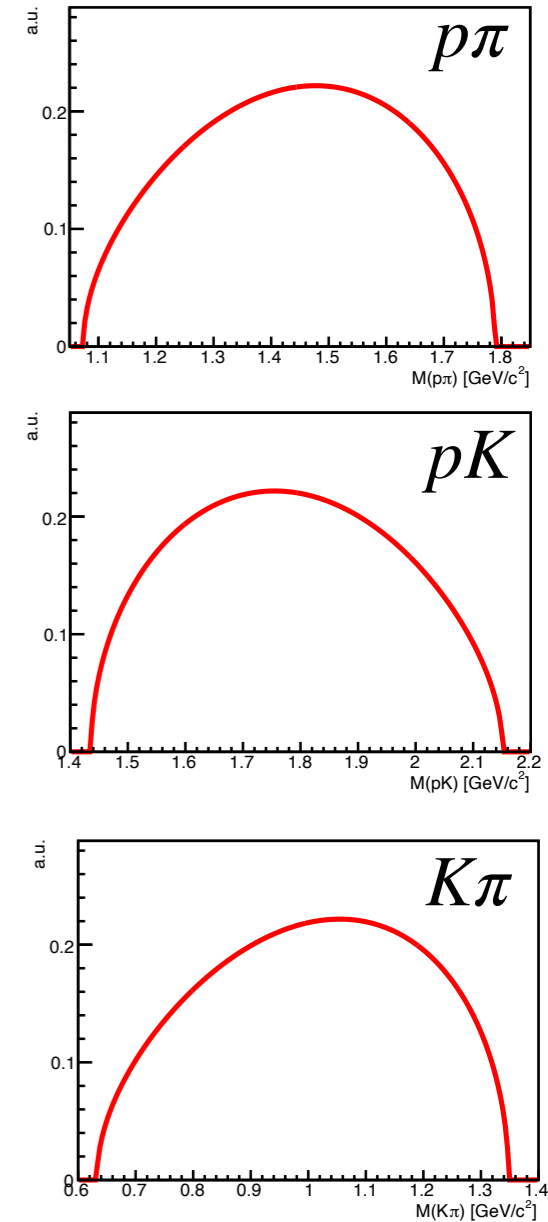
# Physics analysis motivation



$\Gamma_2$	$pK^- \pi^+$		$(6.24 \pm 0.28)\%$
$\Gamma_3$	$p\bar{K}_0^*(700)^0$		$(1.9 \pm 0.6) \times 10^{-3}$
$\Gamma_4$	$p\bar{K}^*(892)^0$	[1]	$(1.39 \pm 0.07)\%$
$\Gamma_5$	$p\bar{K}_0^*(1430)$		$(9.2 \pm 1.8) \times 10^{-3}$
$\Gamma_6$	$\Delta(1232)^{++} K^-$		$(1.76 \pm 0.09)\%$
$\Gamma_7$	$\Delta(1600)^{++} K^-$		$(2.8 \pm 1.0) \times 10^{-3}$
$\Gamma_8$	$\Delta(1700)^{++} K^-$		$(2.4 \pm 0.6) \times 10^{-3}$
$\Gamma_9$	$\Lambda(1405)^0 \pi^+$		$(4.8 \pm 1.9) \times 10^{-3}$
$\Gamma_{10}$	$\Lambda(1520) \pi^+$	[1]	$(1.16 \pm 0.16) \times 10^{-3}$
$\Gamma_{11}$	$\Lambda(1600) \pi^+$		$(3.2 \pm 1.2) \times 10^{-3}$
$\Gamma_{12}$	$\Lambda(1670) \pi^+$		$(7.4 \pm 2.1) \times 10^{-4}$
$\Gamma_{13}$	$\Lambda(1690) \pi^+$		$(7.4 \pm 2.2) \times 10^{-4}$
$\Gamma_{14}$	$\Lambda(2000) \pi^+$		$(6.0 \pm 0.7) \times 10^{-3}$
$\Gamma_{15}$	$pK^- \pi^+$ nonresonant		$(3.5 \pm 0.4)\%$

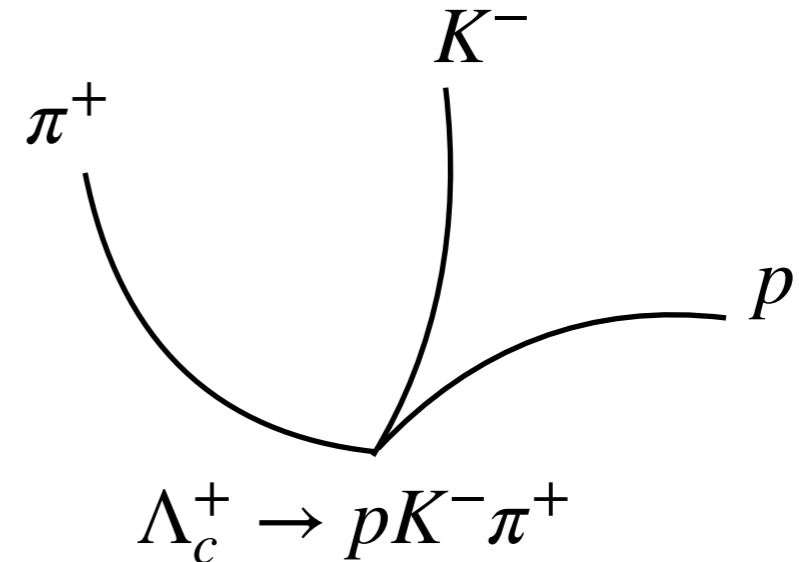
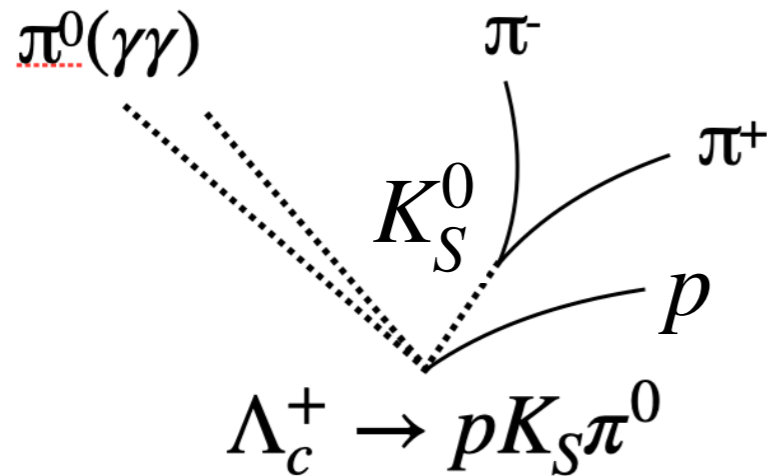


$\Gamma_{16}$	$pK_S^0 \pi^0$		$(1.96 \pm 0.12)\%$
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- Update of the  $\Gamma(\Lambda_c^+ \rightarrow pK_S^0 \pi^0)/\Gamma(\Lambda_c^+ \rightarrow pK^- \pi^+)$  with **x100** statistics than previous reports
- First investigation of intermediate resonances in the  $\Lambda_c^+ \rightarrow pK_S^0 \pi^0$  decay

# $\Lambda_c^+$ Reconstruction

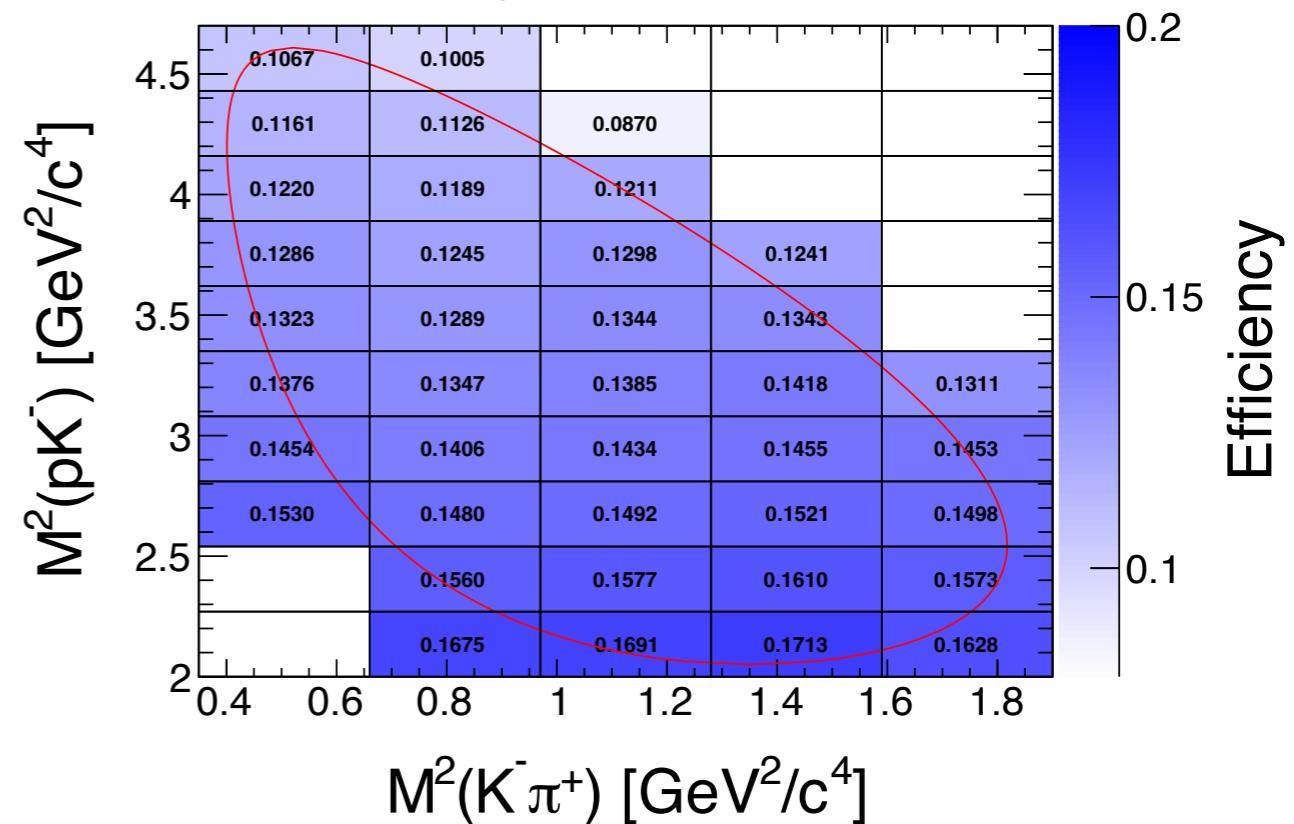
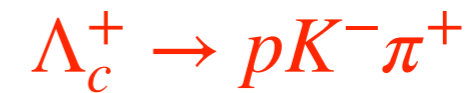
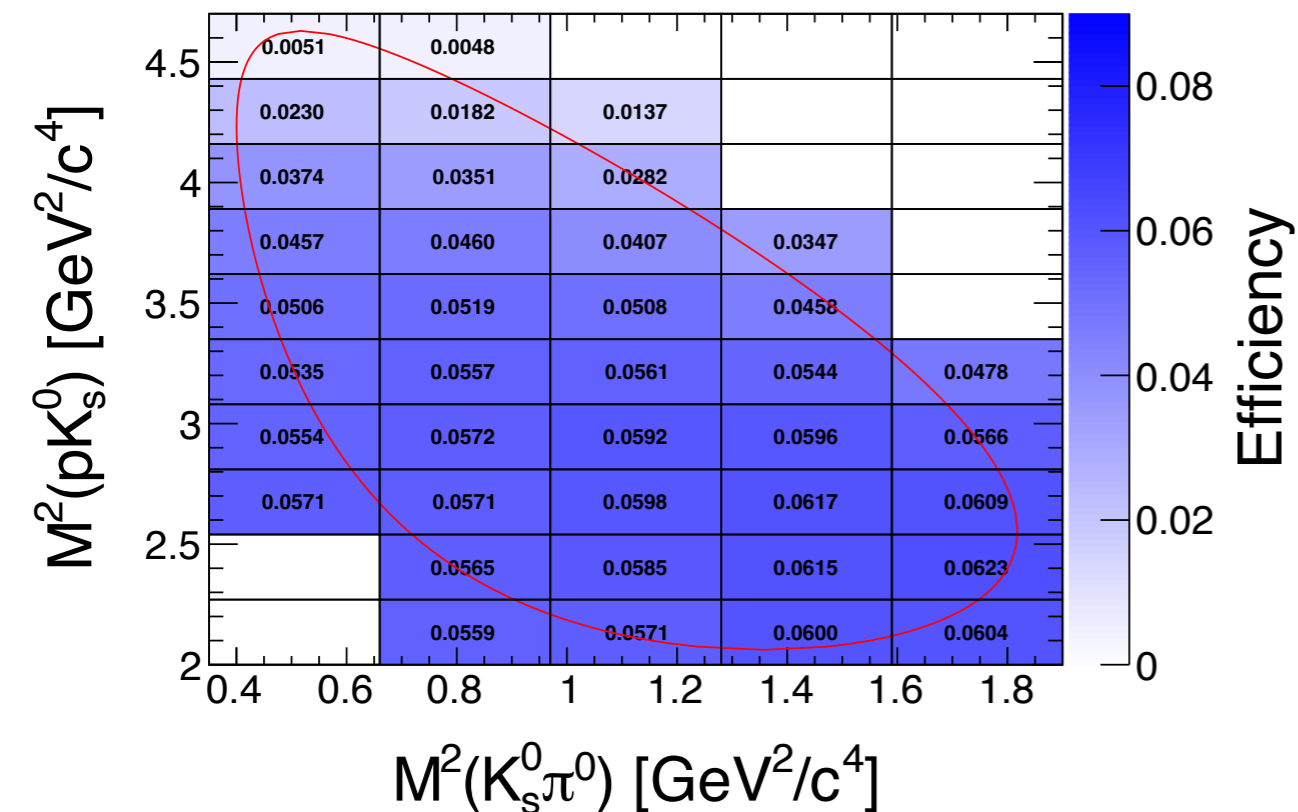
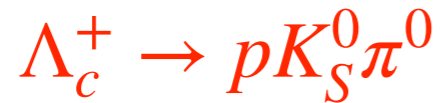


- $\Lambda_c^+ \rightarrow p K_S^0 \pi^0$  (Signal mode)
  - $\Lambda_c^+$ : Scaled momentum  $x_p$ , vertex fit  $\chi^2$
  - $p$ : PID, Impact parameters
  - $\pi^0(\gamma\gamma)$ : mass, momentum,  $E_\gamma$
  - $K_S^0(\pi^+\pi^-)$ : Belle standard  $K_S^0$ , vertex fit  $\chi^2$
- $\Lambda_c^+ \rightarrow p K^- \pi^+$  (Normalization mode)
  - $\Lambda_c^+$ : Scaled momentum  $x_p$ , vertex fit  $\chi^2$
  - $p, K^-, \pi^+$ : PID, Impact parameters

→ Selection criteria are optimized to maximize

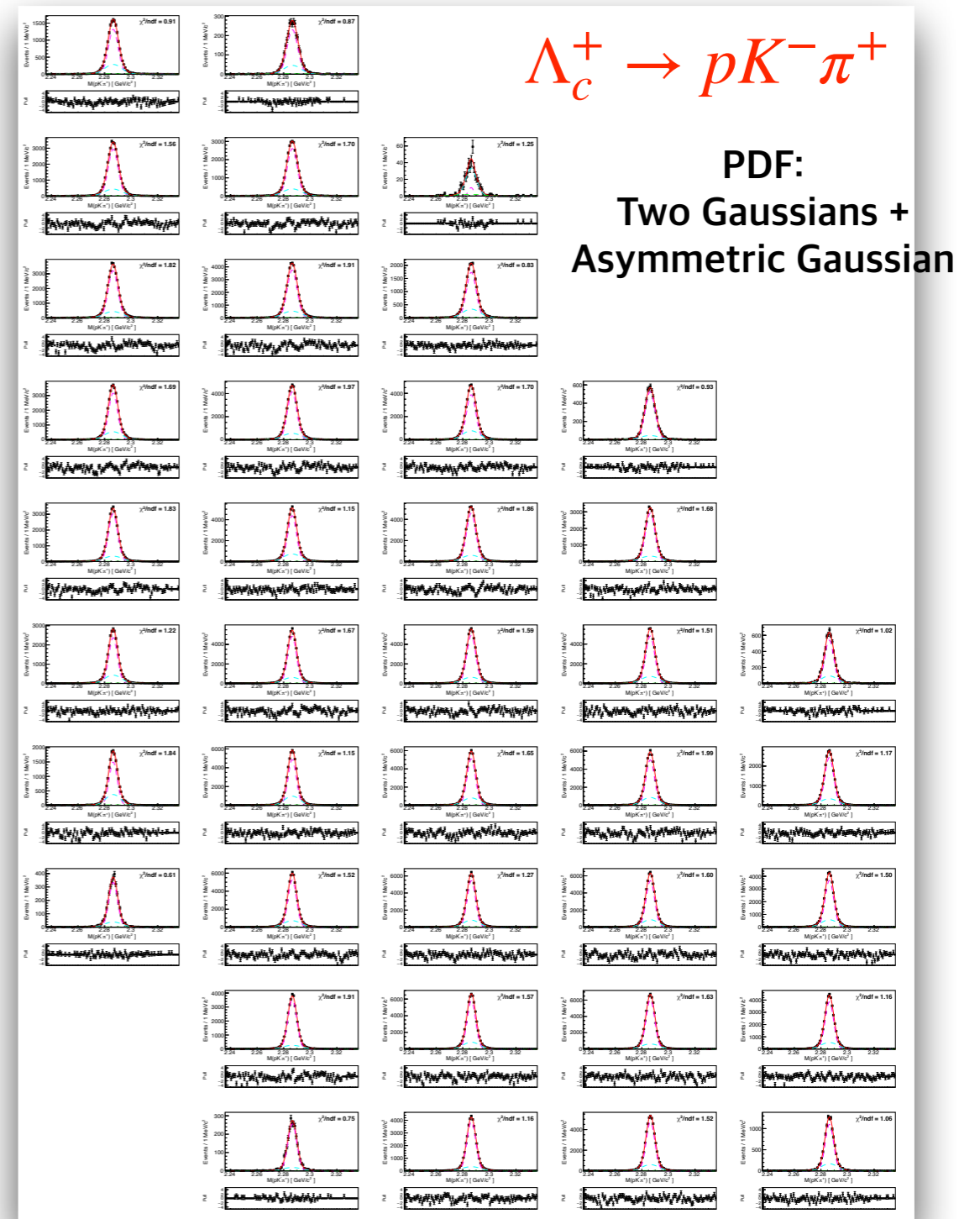
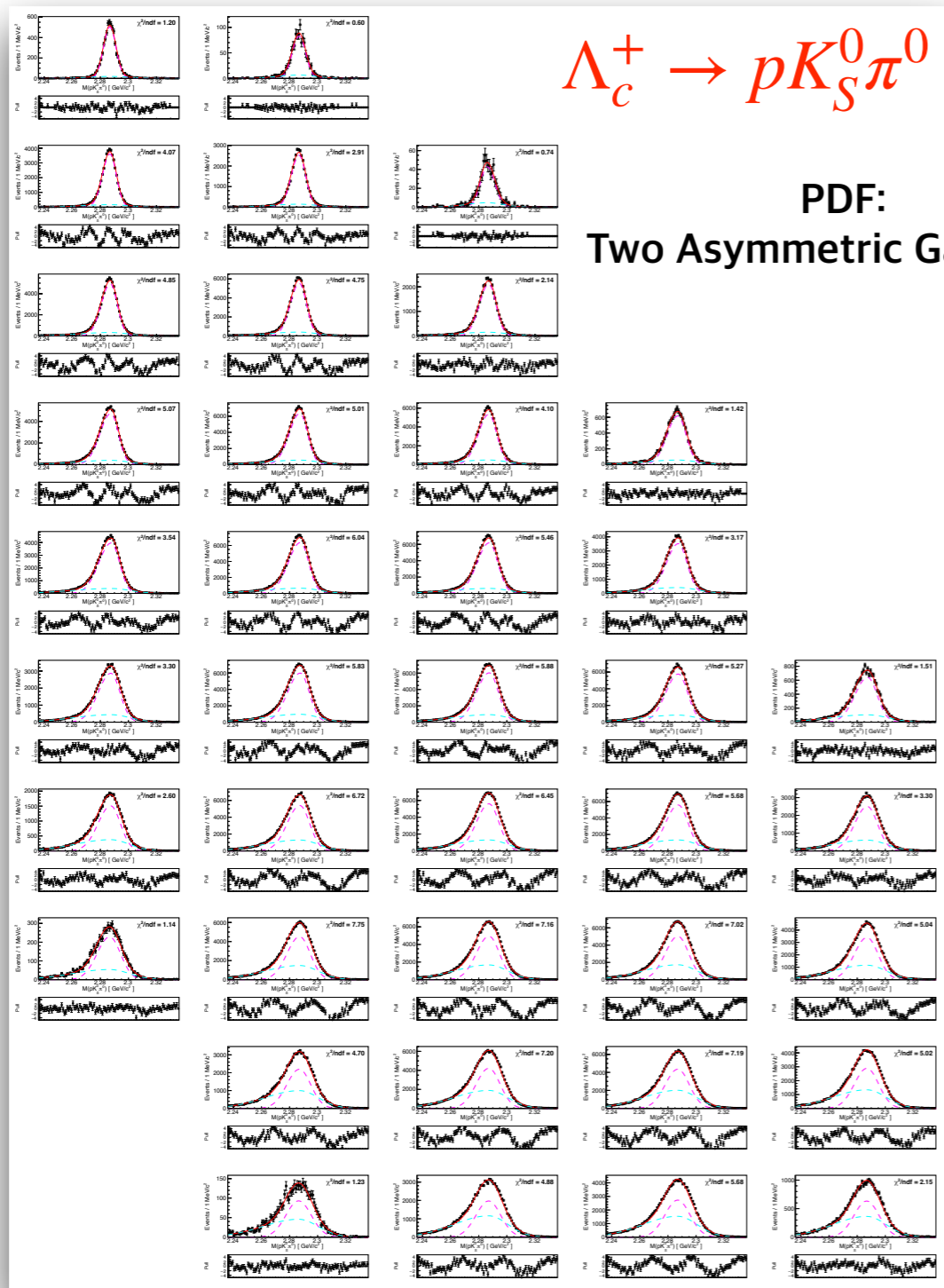
$$FoM = N_{sig} / \sqrt{N_{sig} + N_{bkg}} \text{ (Statistical significance)}$$

# Detection Efficiency



- In order to perform a **resonance model-independent efficiency correction**
  - ➔ Intermediate resonances are shown in Dalitz plot. (horizontal, vertical, diagonal)
  - ➔ Yield extraction and efficiency correction are performed on **5 × 10 Dalitz bins**

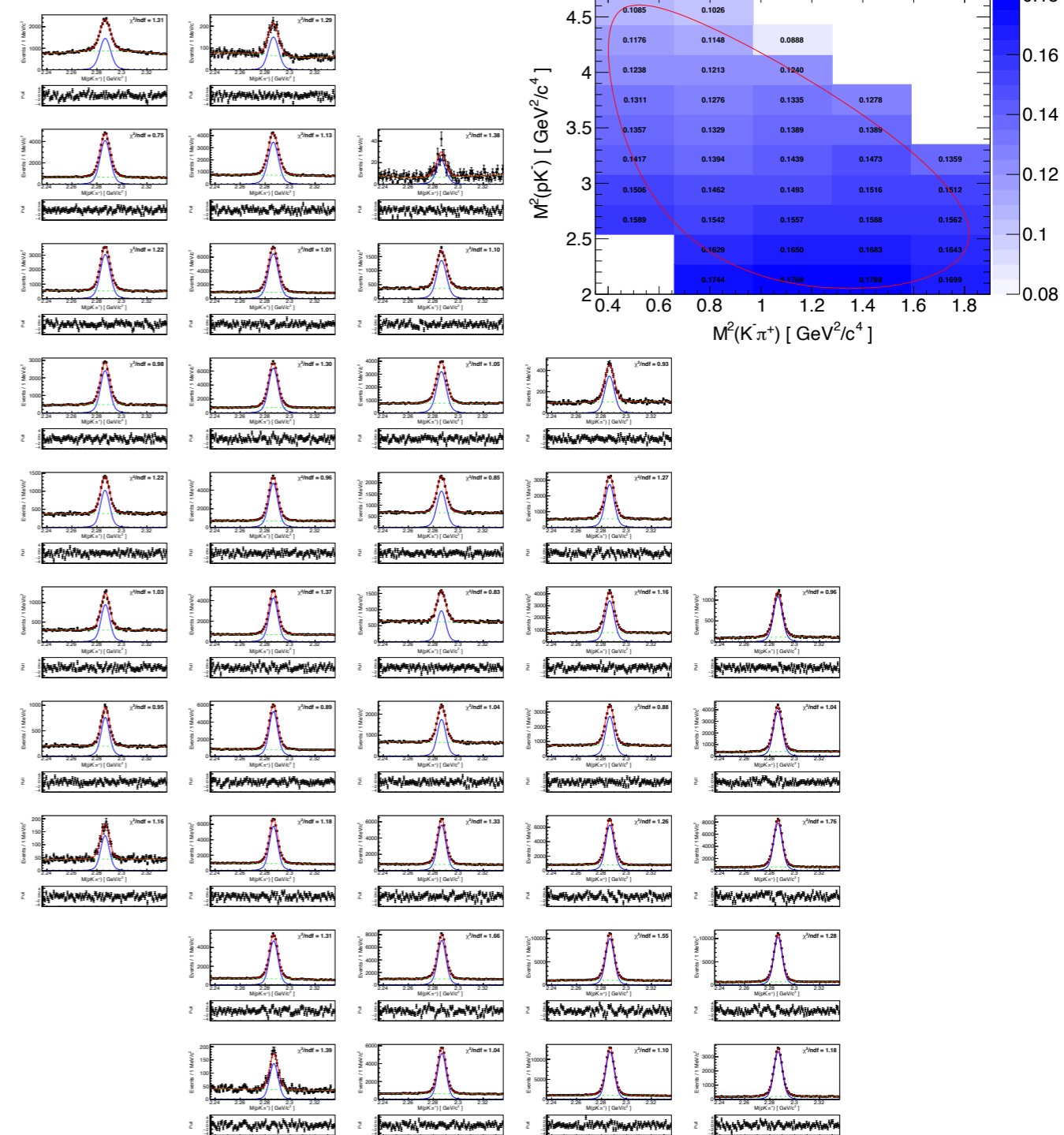
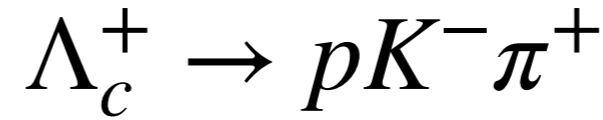
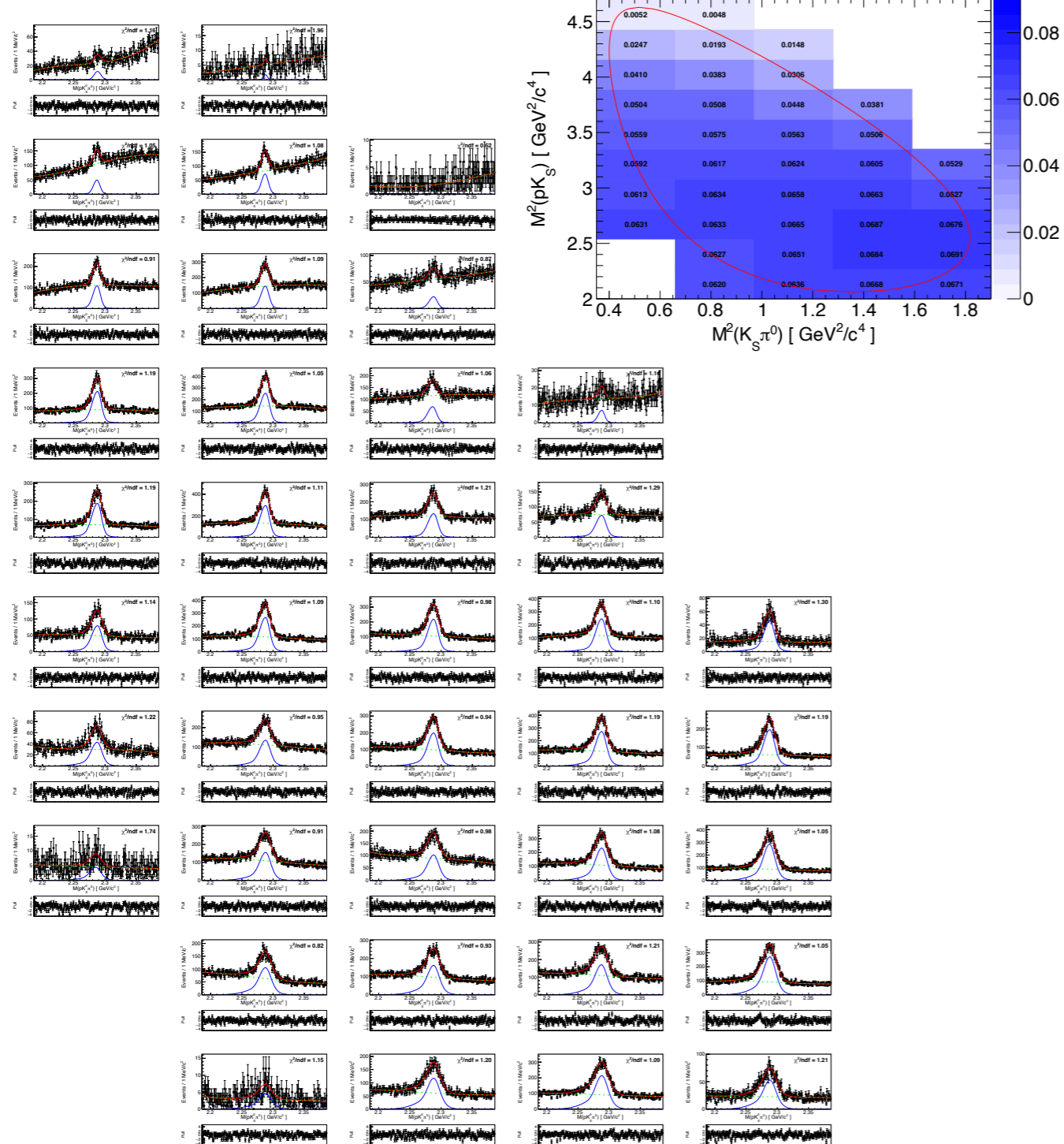
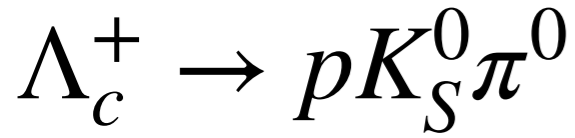
# Signal PDF



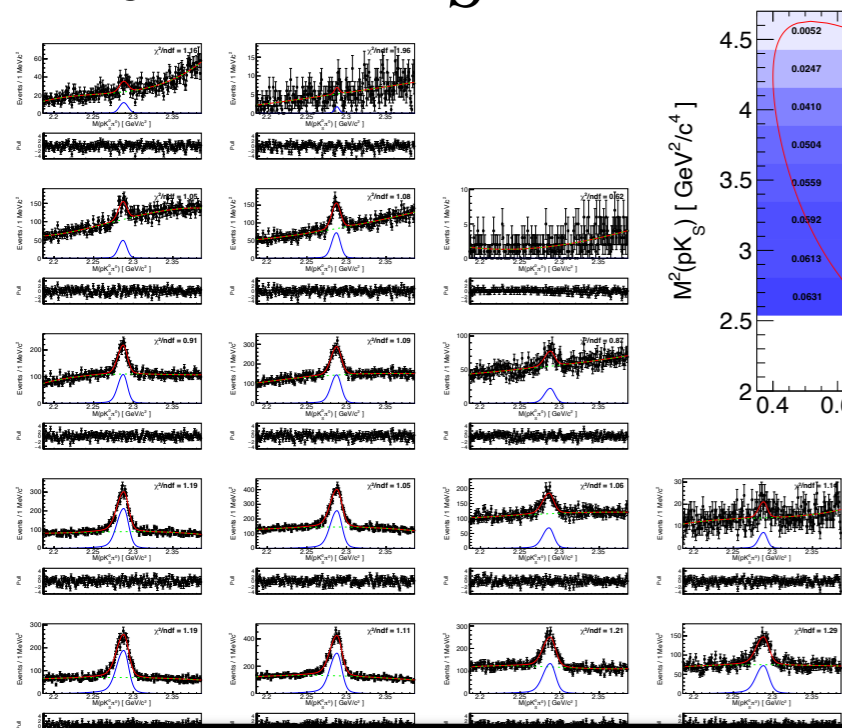
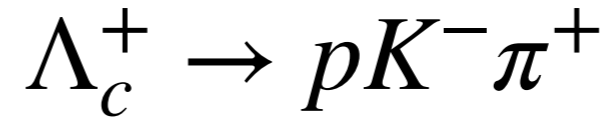
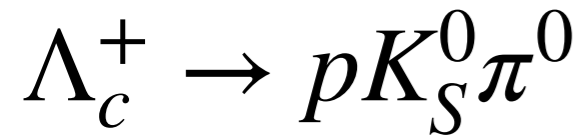
- Signal line shapes are constrained for each bin. Only  $m_0$  and scale parameter  $\sigma$  are floated



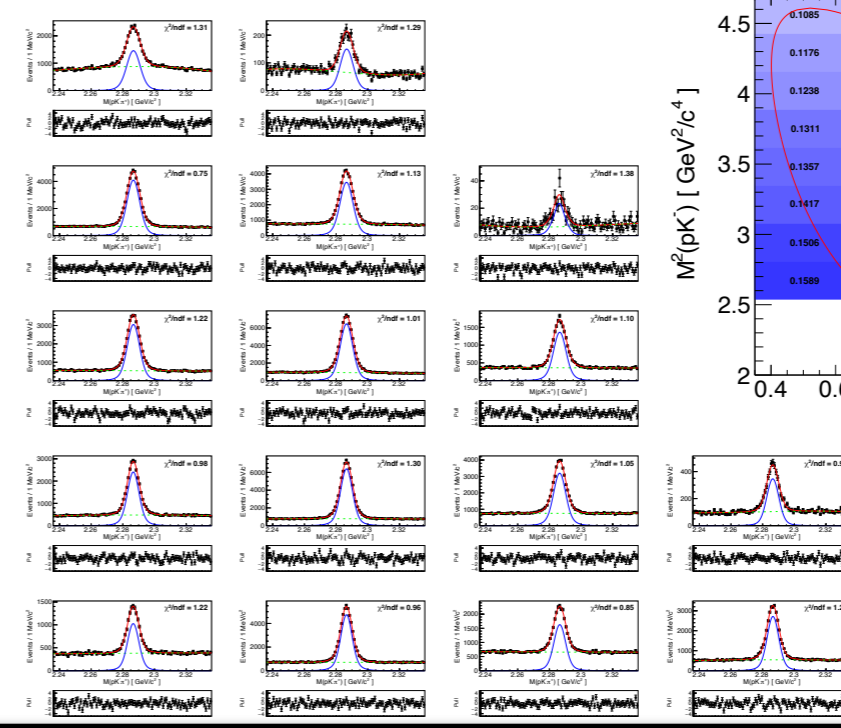
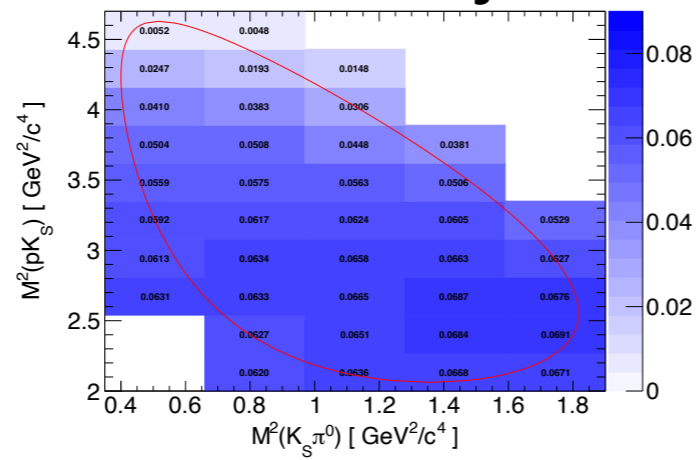
# $N(\Lambda_c^+ \rightarrow pK_S^0\pi^0)$ and $N(\Lambda_c^+ \rightarrow pK^-\pi^+)$ extraction



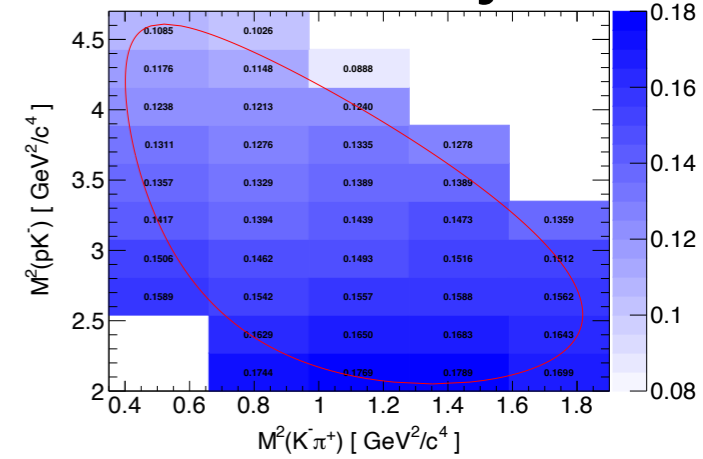
# Relative and Absolute BFs



Efficiency



Efficiency



$$\frac{\Gamma(\Lambda_c^+ \rightarrow p K_S^0 \pi^0)}{\Gamma(\Lambda_c^+ \rightarrow p K^- \pi^+)} = \frac{y^{corr}(\Lambda_c^+ \rightarrow p K_S^0 \pi^0)}{y^{corr}(\Lambda_c^+ \rightarrow p K^- \pi^+) \times B(\pi^0 \rightarrow \gamma\gamma) \times B(K_S^0 \rightarrow \pi^+ \pi^-)}$$

**This Work**

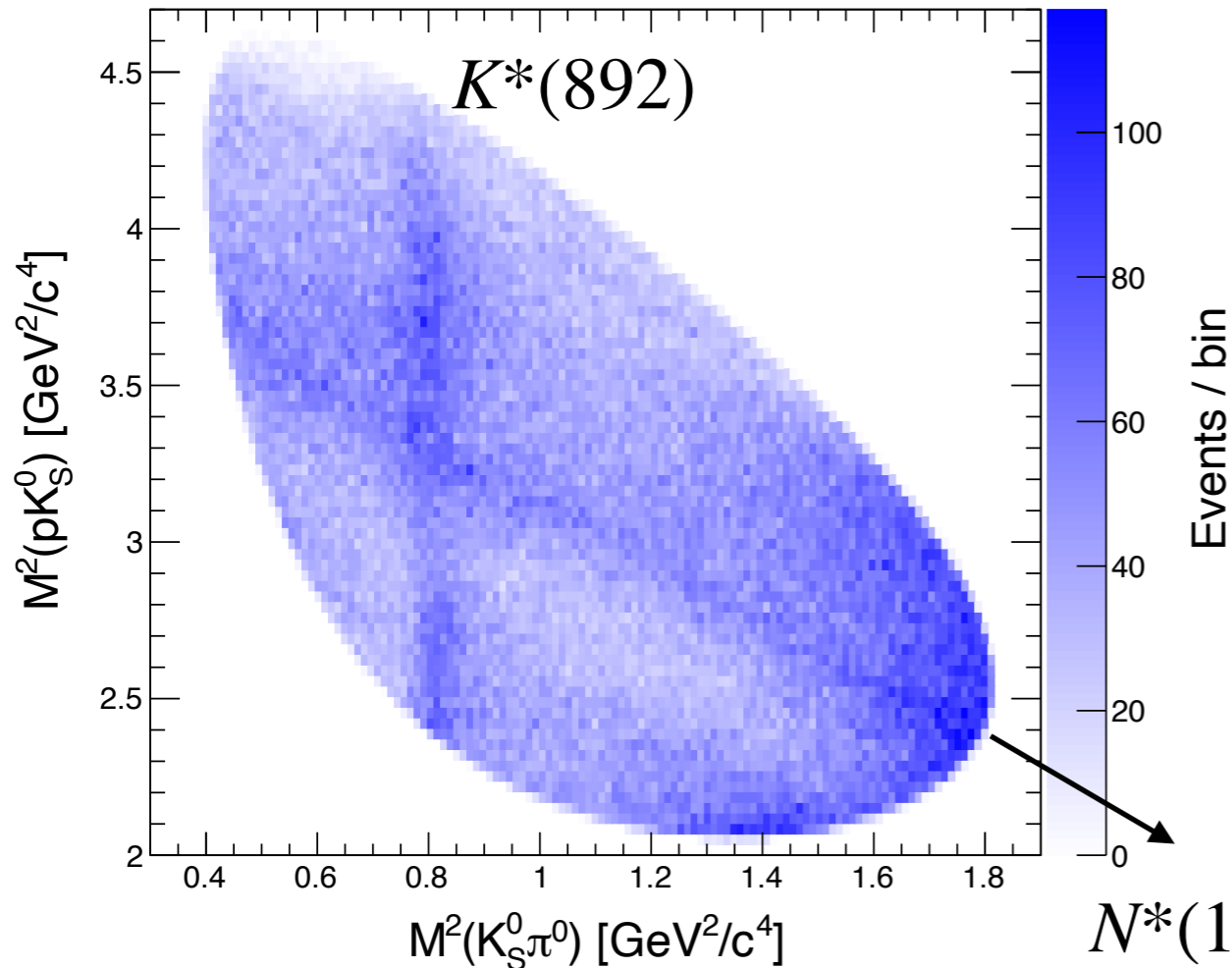
$$\Gamma(\Lambda_c^+ \rightarrow p K_S^0 \pi^0) / \Gamma(\Lambda_c^+ \rightarrow p K^- \pi^+) = 0.339 \pm 0.002(\text{stat.}) \pm 0.009(\text{syst.})$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow p K_S^0 \pi^0) = 2.12 \pm 0.01(\text{stat.}) \pm 0.05(\text{syst.}) \pm 0.10(\text{norm PDG2024}) (\%)$$

**Fivefold improvement than previous measurements (CLEO)**

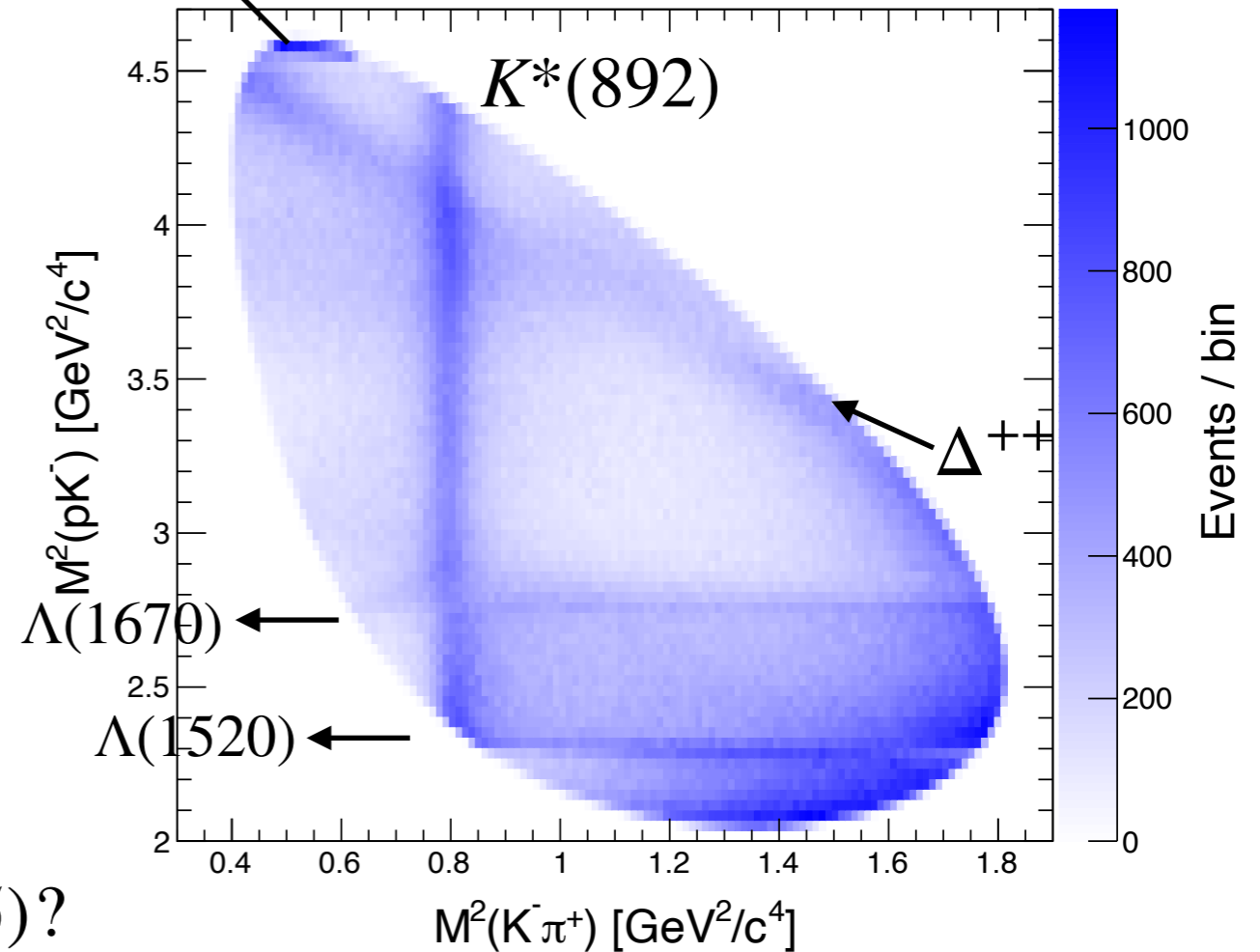
# Dalitz plots

$$\Lambda_c^+ \rightarrow pK_S^0\pi^0$$



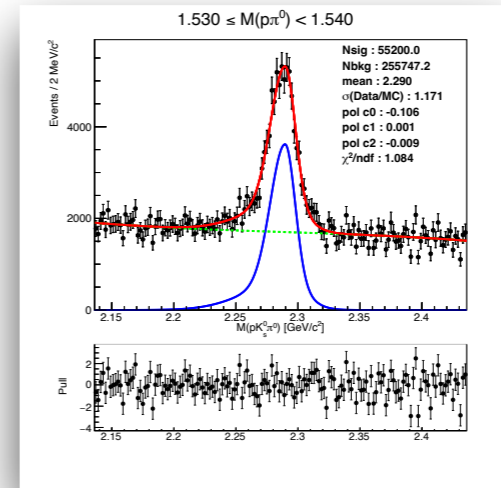
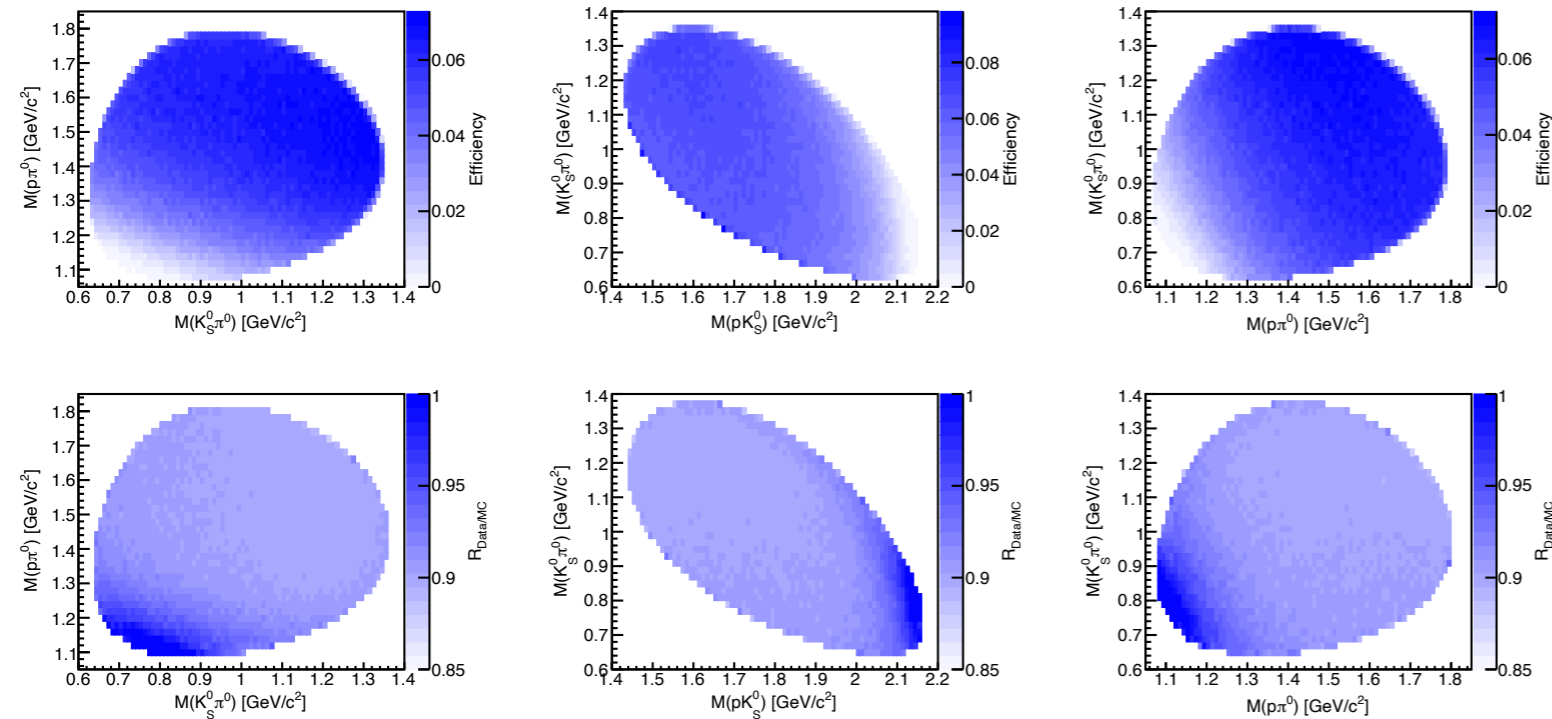
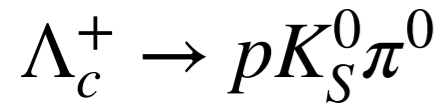
$D \rightarrow K\pi$  mis identification

$$\Lambda_c^+ \rightarrow pK^-\pi^+$$



- There is no clear peak structure in the  $pK_S^0$  system (horizontal axis)
- $K^*(892)$  clearly seen and, in the  $p\pi^0$  system, a peak appears at 1.5 GeV
- Enhancements are seen in the boundary of the bottom and right side

# One dimensional mass projections



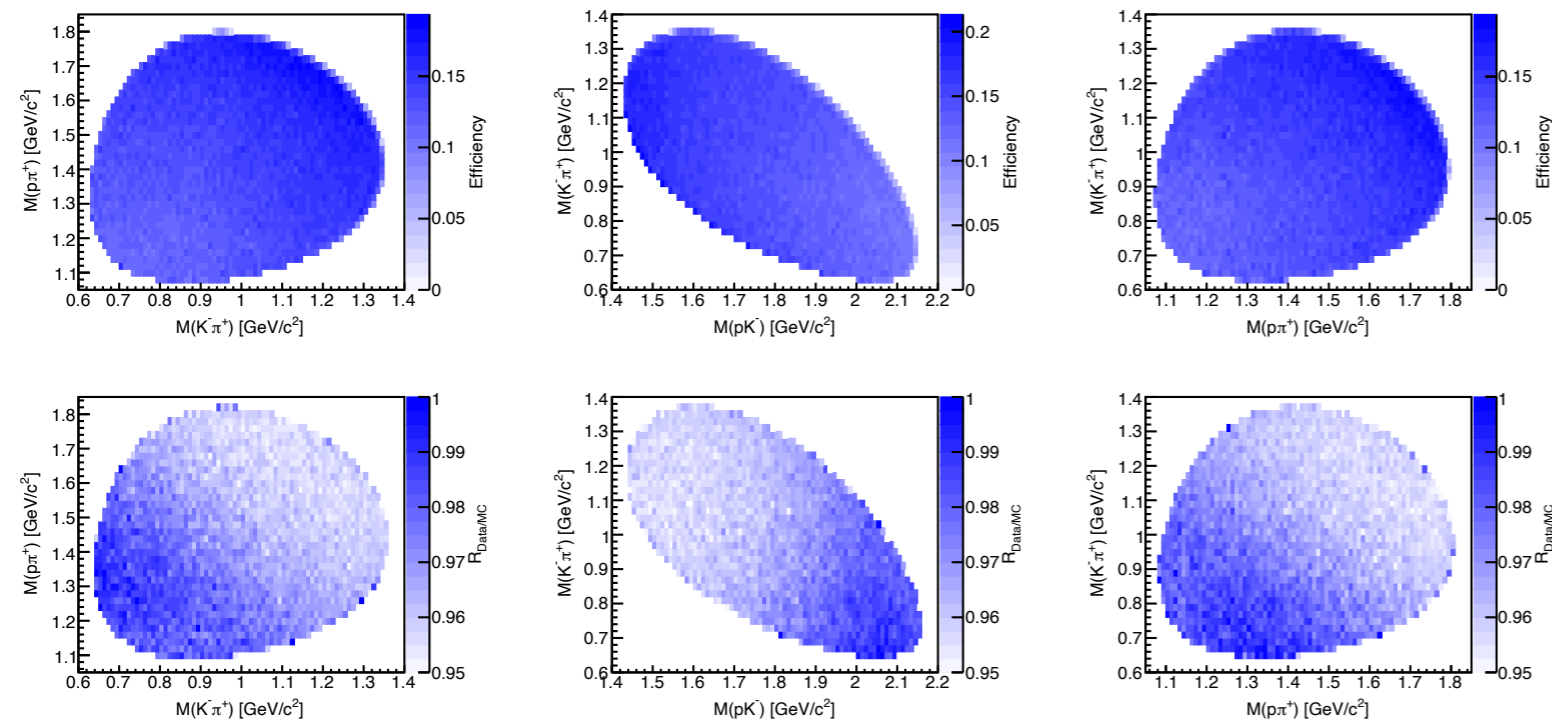
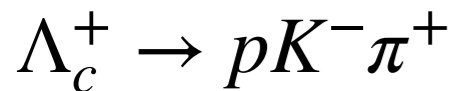
1. We constructed event-by-event efficiency-corrected  $M(\Lambda_c^+)$  histograms

$$\left( \text{weighted by } \frac{1}{\epsilon_{i,j} \cdot R_{i,j}(\text{Data}/\text{MC})} \right)$$

for each mass bin  $m_{ab,i}$ ,  $a, b$  for daughter particle,  $i$  for mass bin of  $m_{ab}$

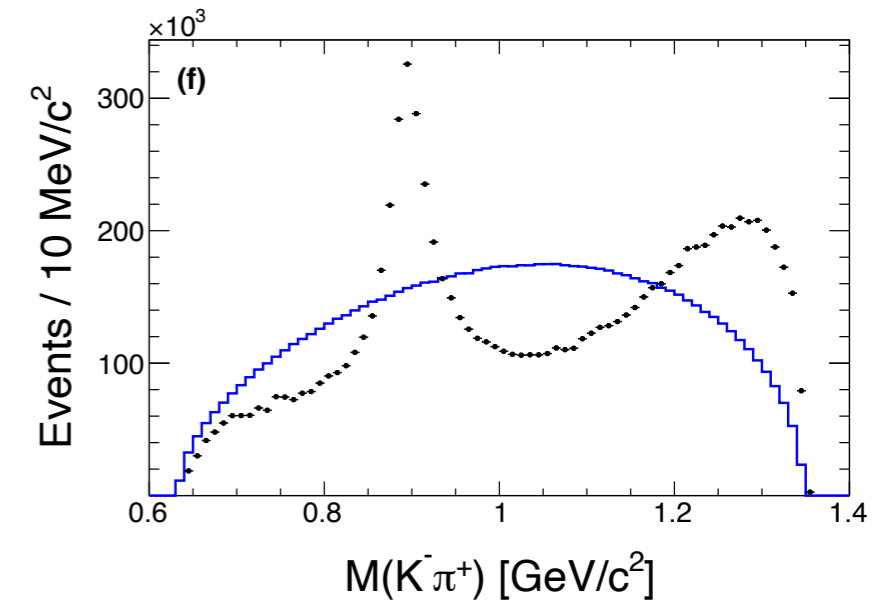
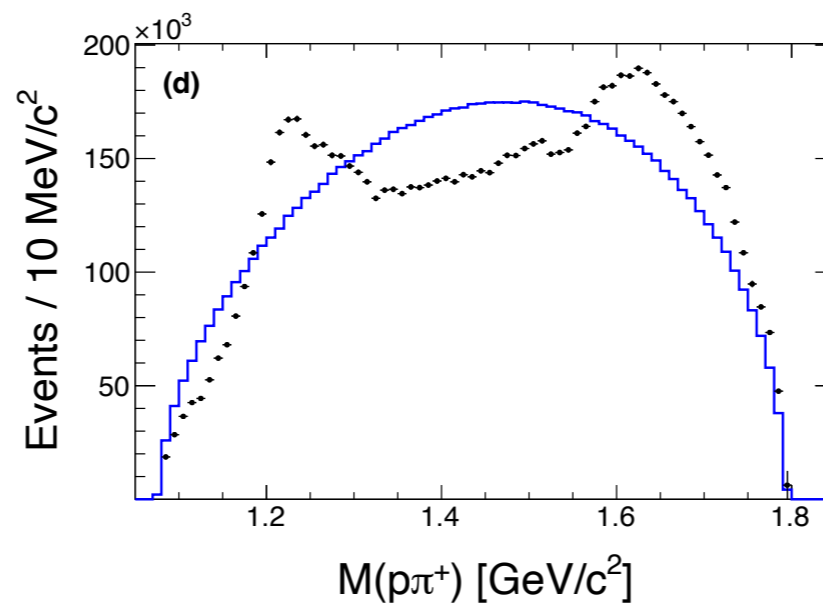
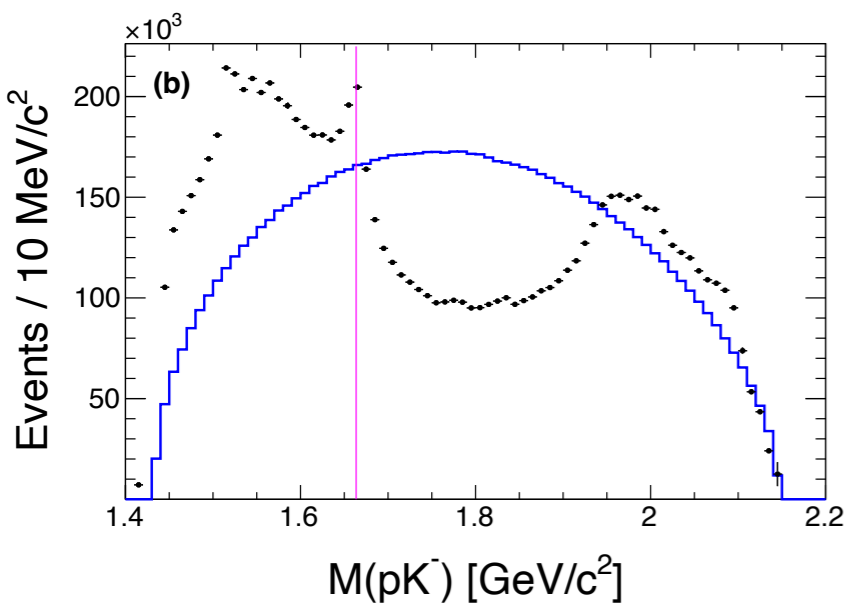
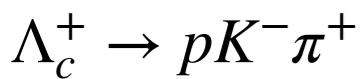
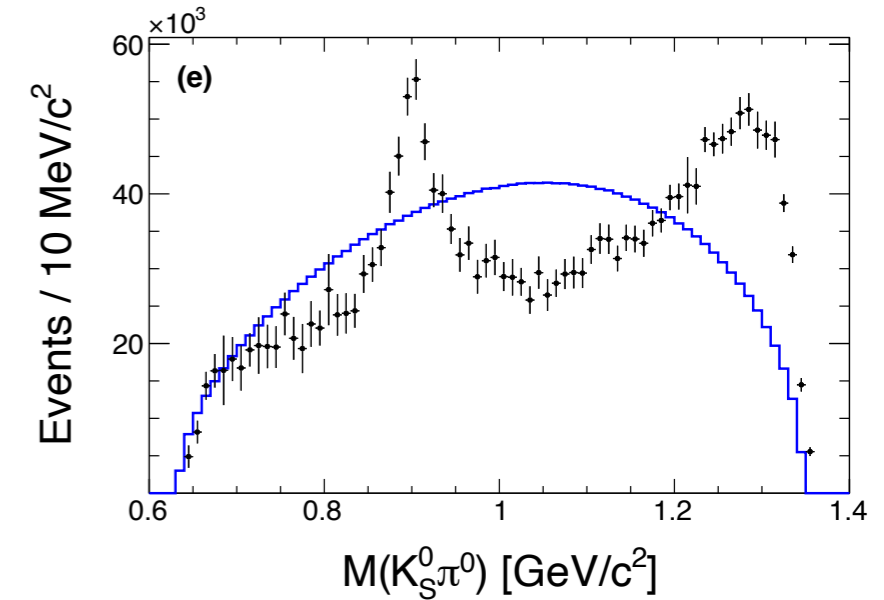
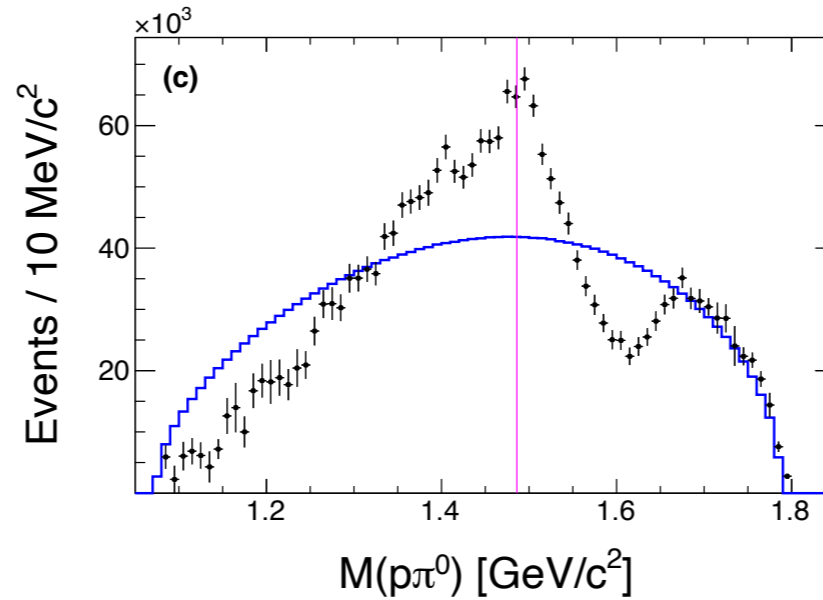
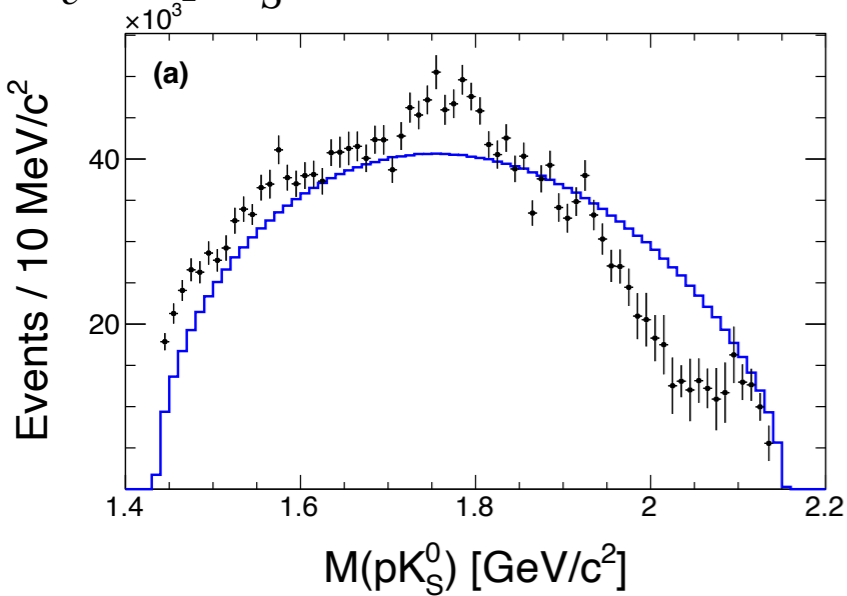
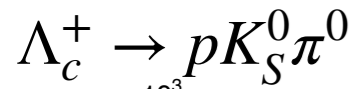
2. Fit and extract yield for each mass bin  $m_{ab,i}$

3. Similar with BR measurement, Data/MC has been corrected, the same signal PDFs are used, and shape parameters are fixed. For background PDFs, 3rd order polynomial and Argus function are used depending on mass bin.



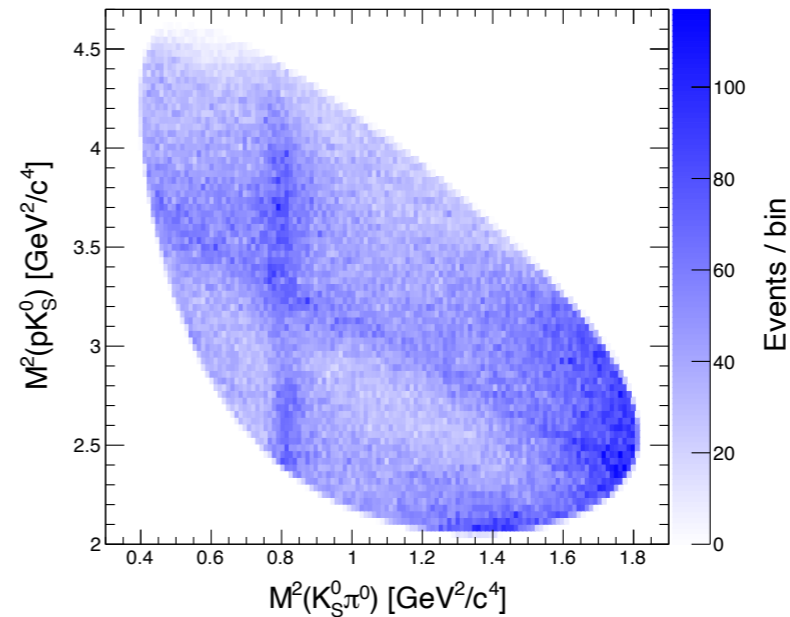
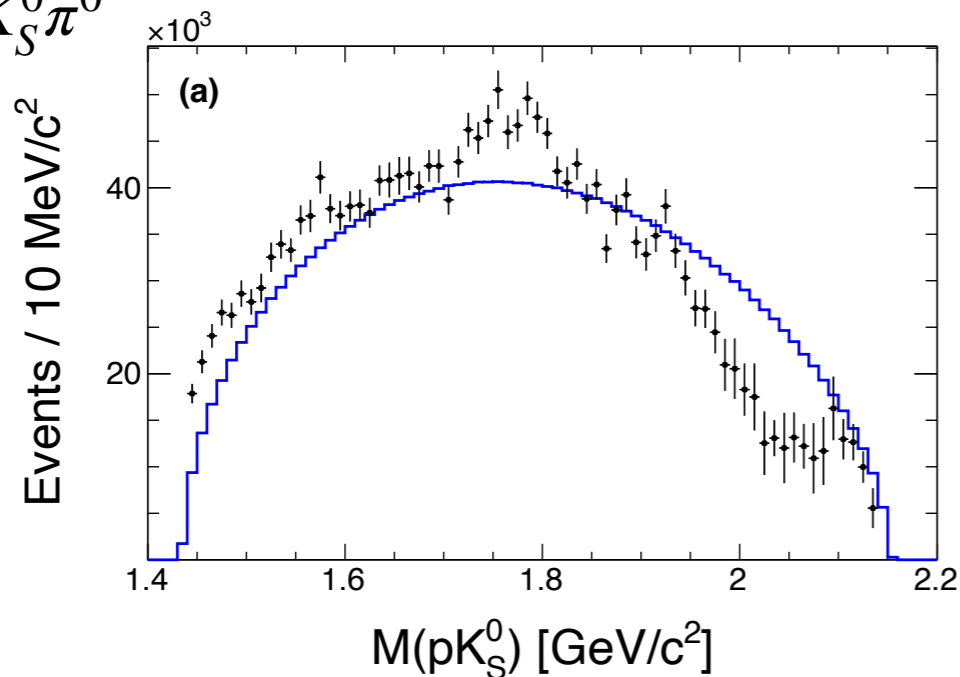
# Efficiency corrected mass spectra

Blue histograms represent PHSP line shapes

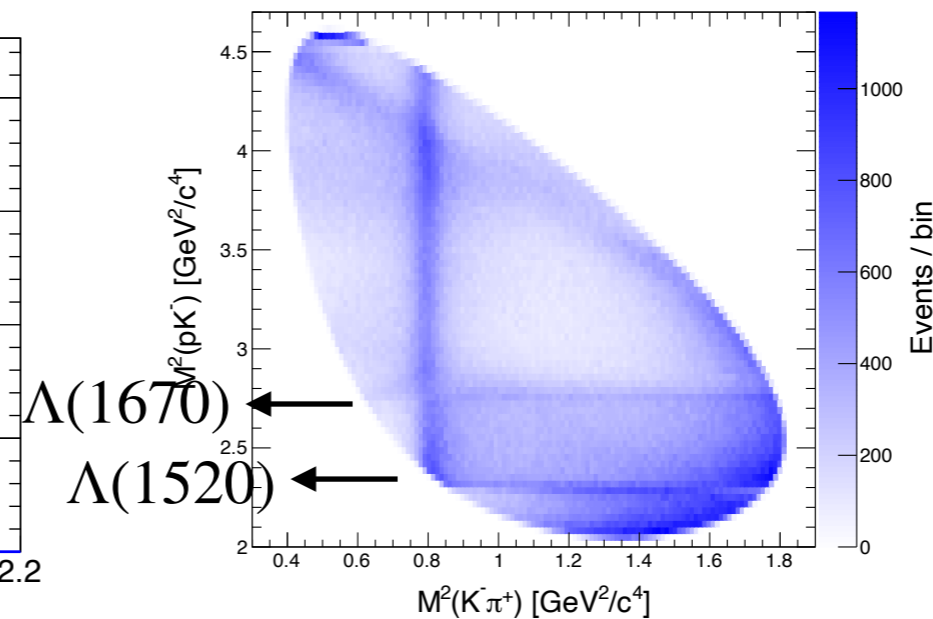
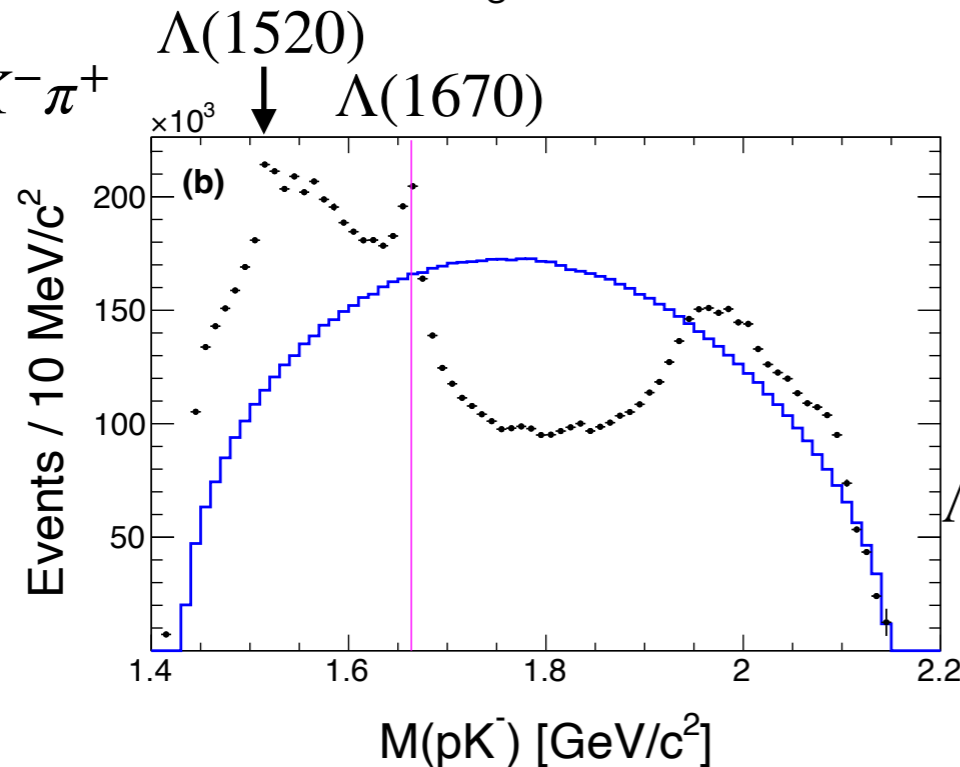


# Absence of peak structure in the $M(pK_S^0)$

$$\Lambda_c^+ \rightarrow pK_S^0\pi^0$$



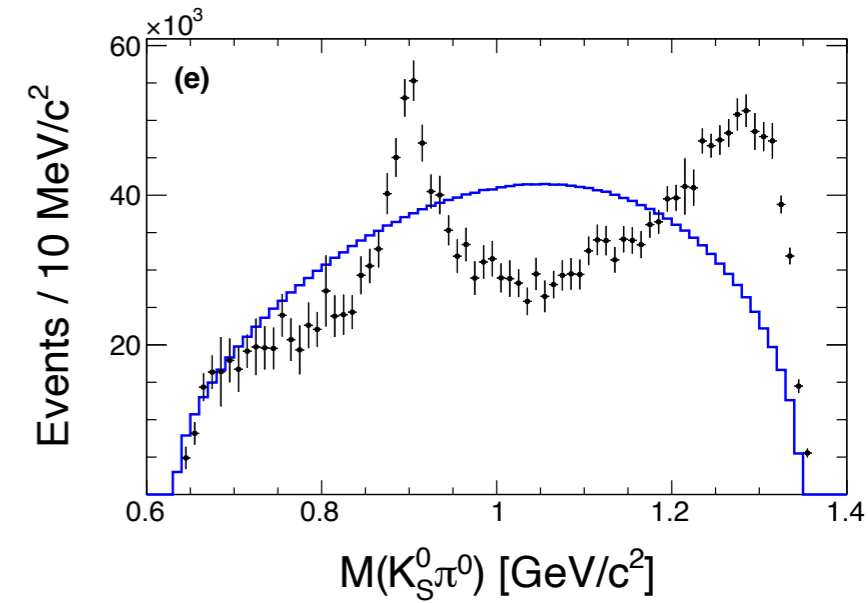
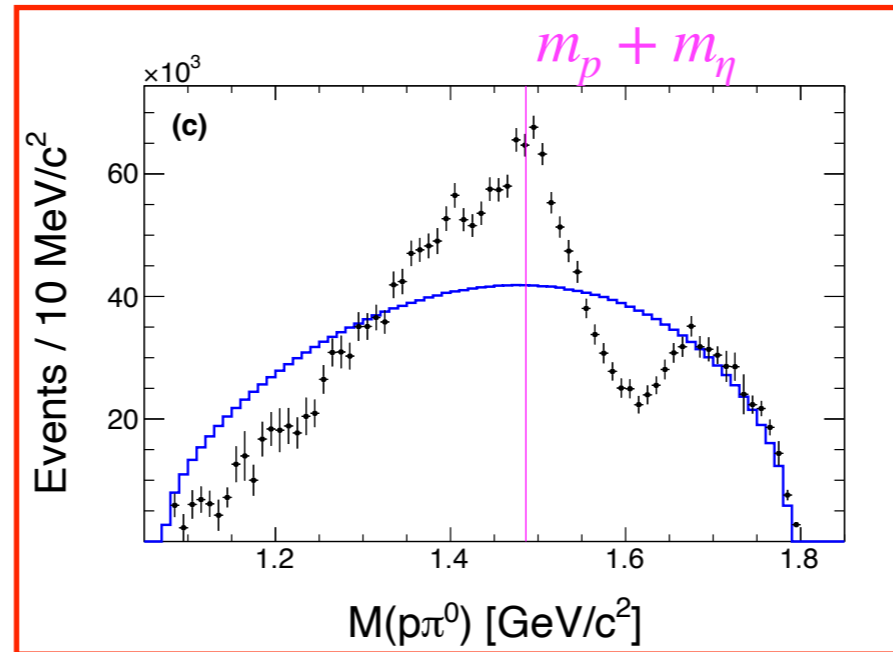
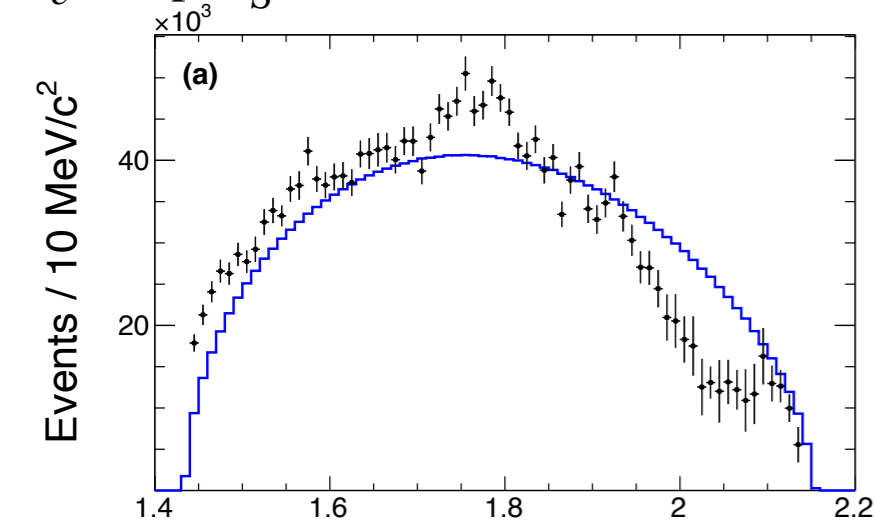
$$\Lambda_c^+ \rightarrow pK^-\pi^+$$



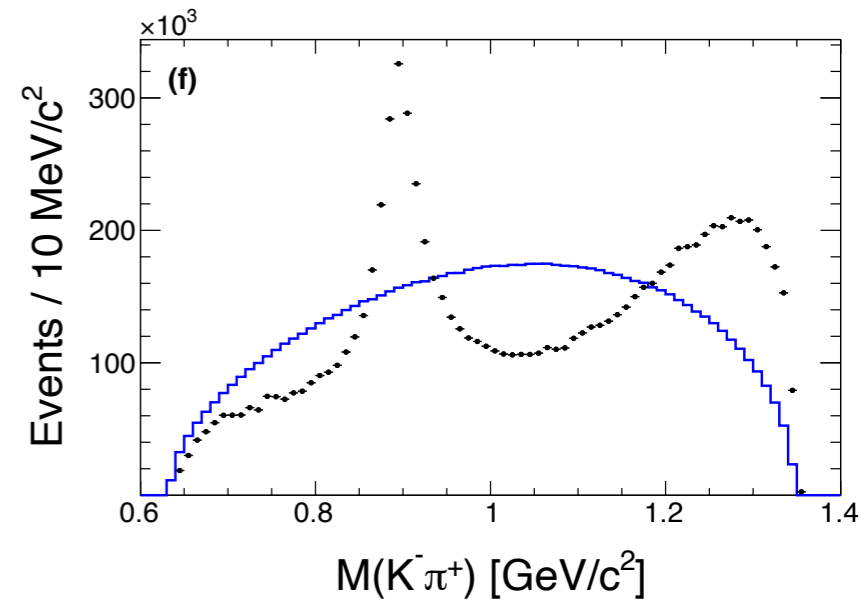
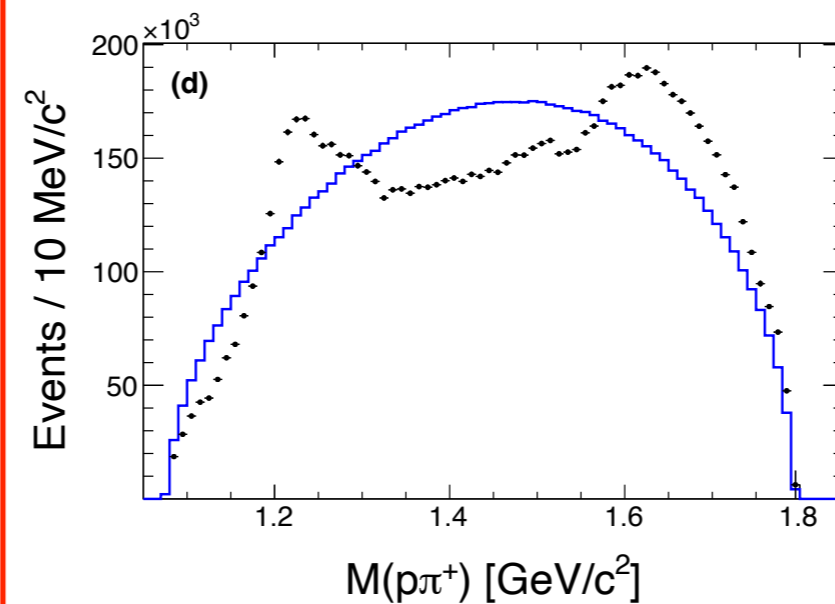
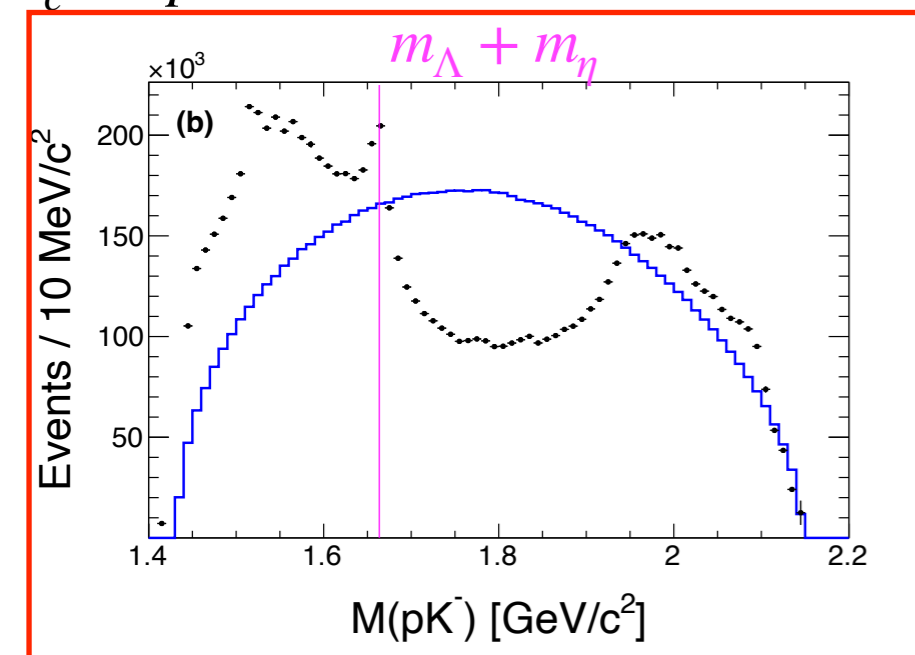
- Compared with Dalitz plots, there is no narrow peak structure ( $\Sigma^{*+}$ ) in the  $M(pK_S^0)$ , while  $\Lambda^*$ s are clearly seen in the  $M(pK^-)$

# Threshold cusp in $M(p\pi^0)$

$$\Lambda_c^+ \rightarrow p K_S^0 \pi^0$$



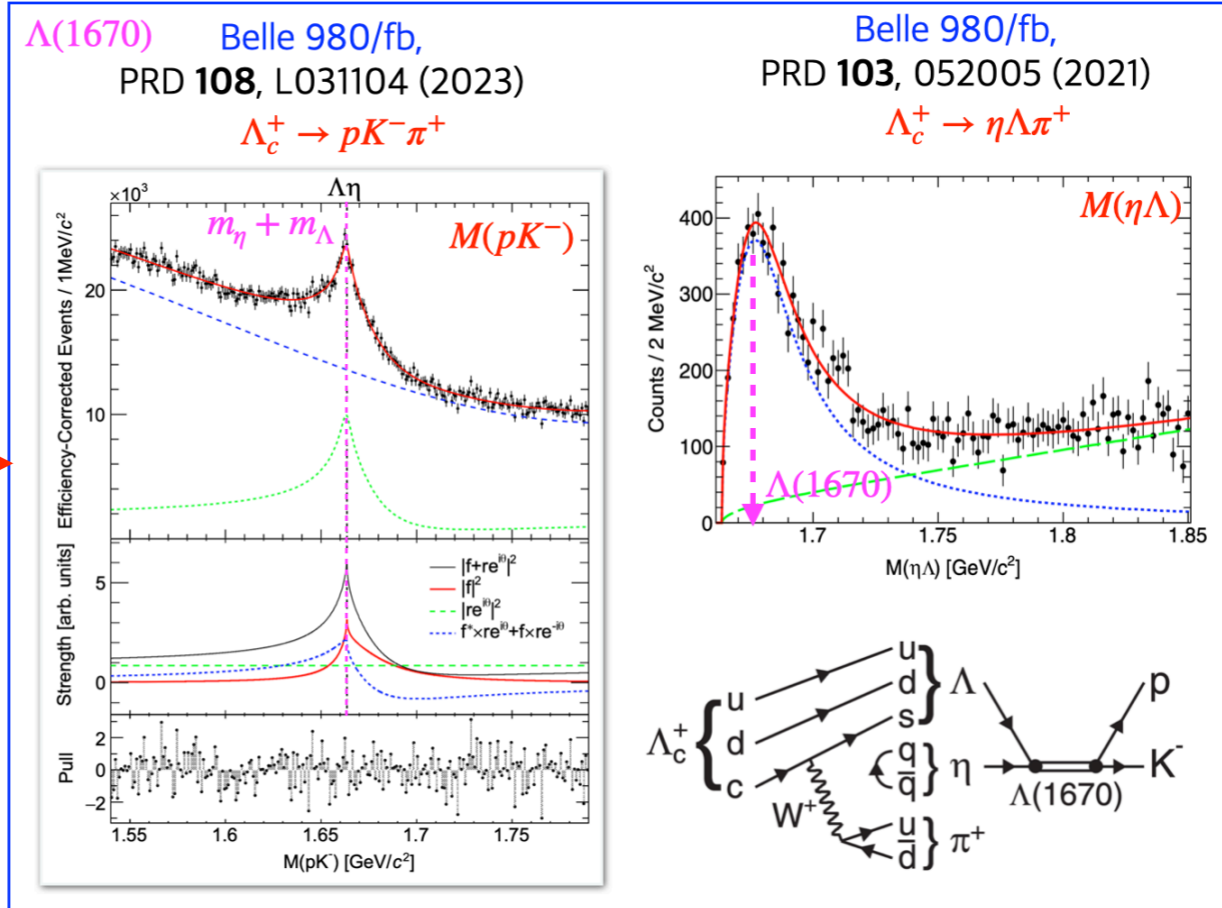
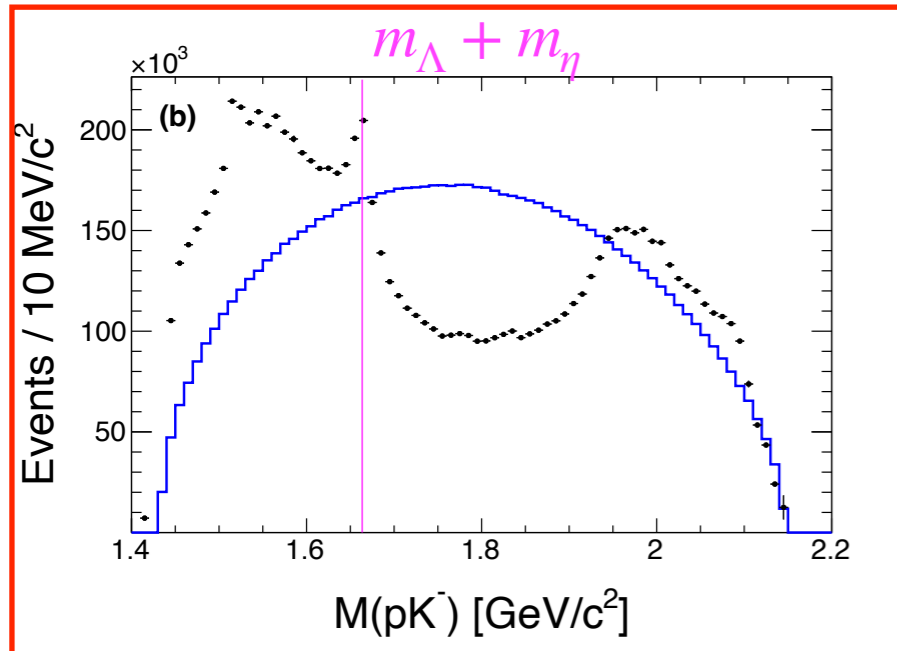
$$\Lambda_c^+ \rightarrow p K^- \pi^+ M(pK_S^0) [\text{GeV}/c^2]$$



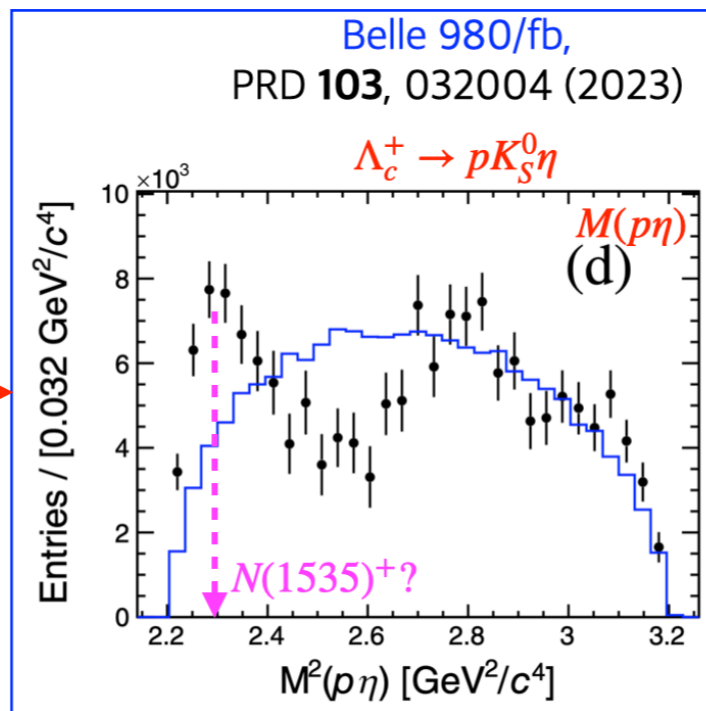
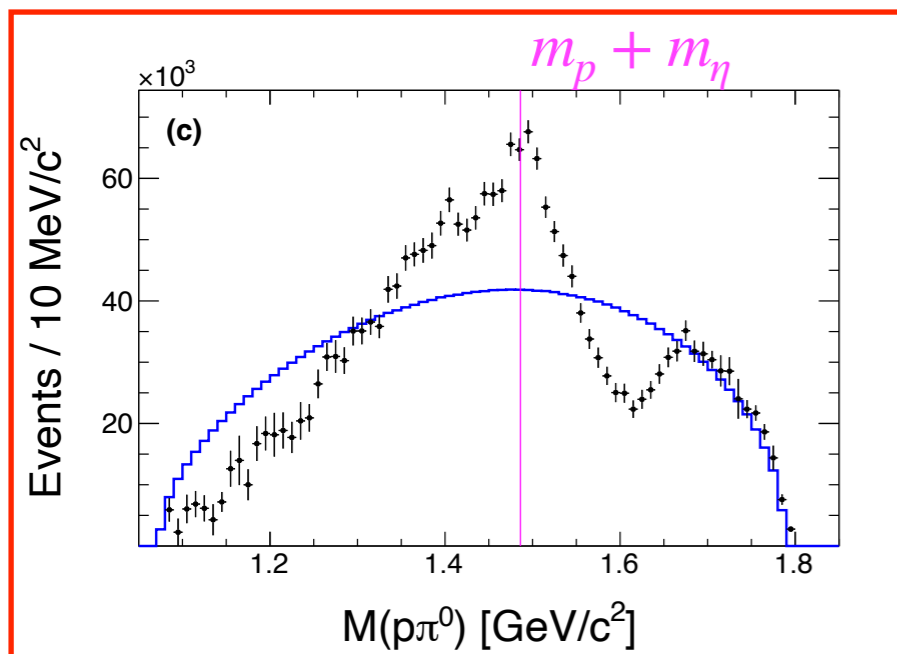
- The threshold cusps near the  $p\eta$  mass threshold enhanced by  $N(1535)^+$ .
- The same situation with the  $\Lambda\eta$  threshold cusp enhanced by  $\Lambda(1670)$

# Threshold cusp in $M(p\pi^0)$

$$\Lambda_c^+ \rightarrow pK^-\pi^+$$



$$\Lambda_c^+ \rightarrow pK_S^0\pi^0$$

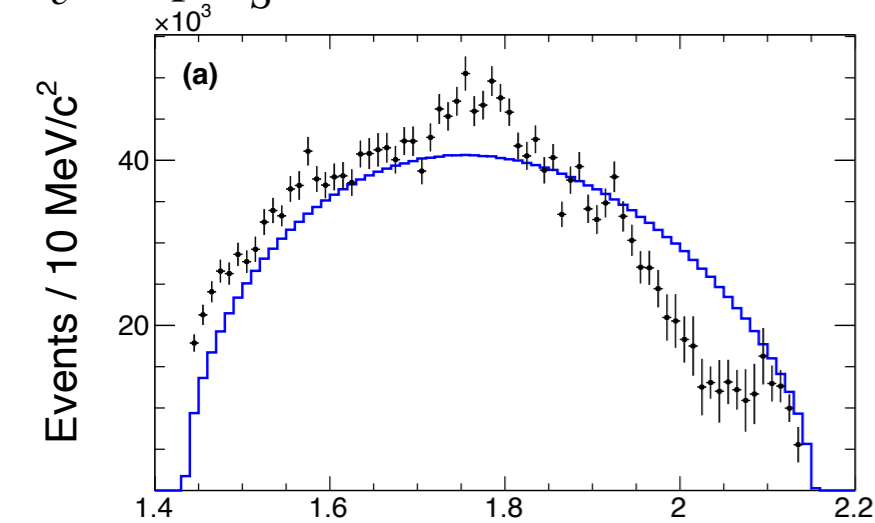


- $\Lambda(1670)$  observed in  $M(\eta\Lambda)$ , threshold cusp observed in  $M(pK^-)$
- $N^*$  seen in  $M(p\eta)$ , threshold cusp observed in  $M(p\pi^0)$

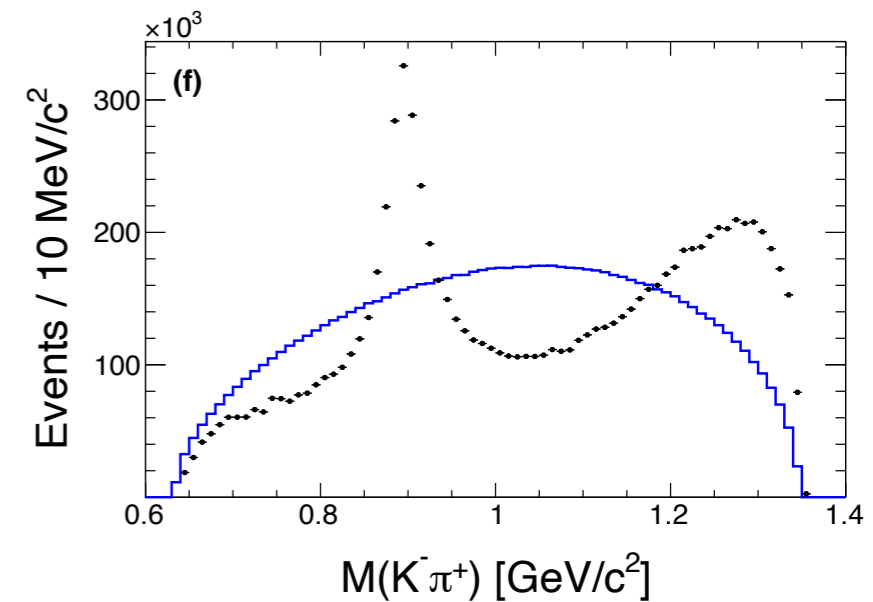
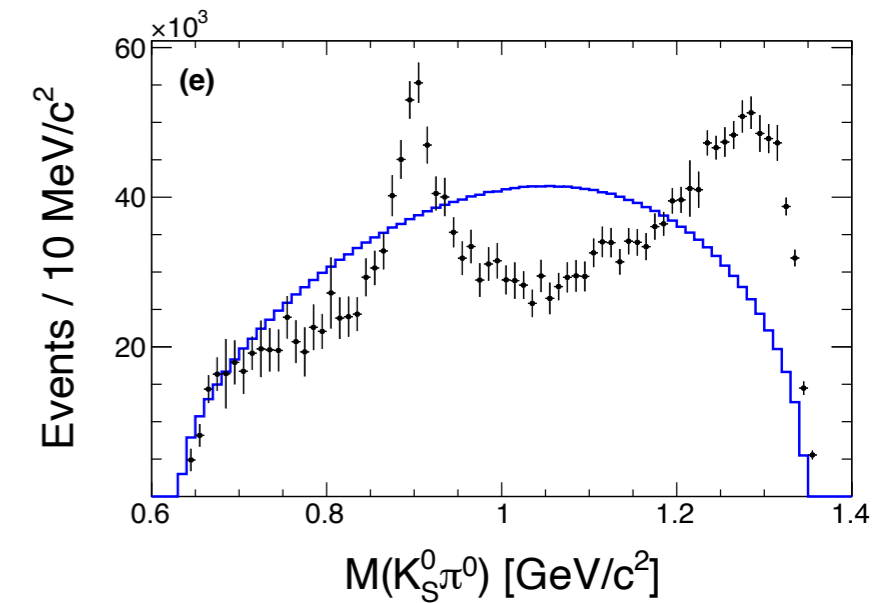
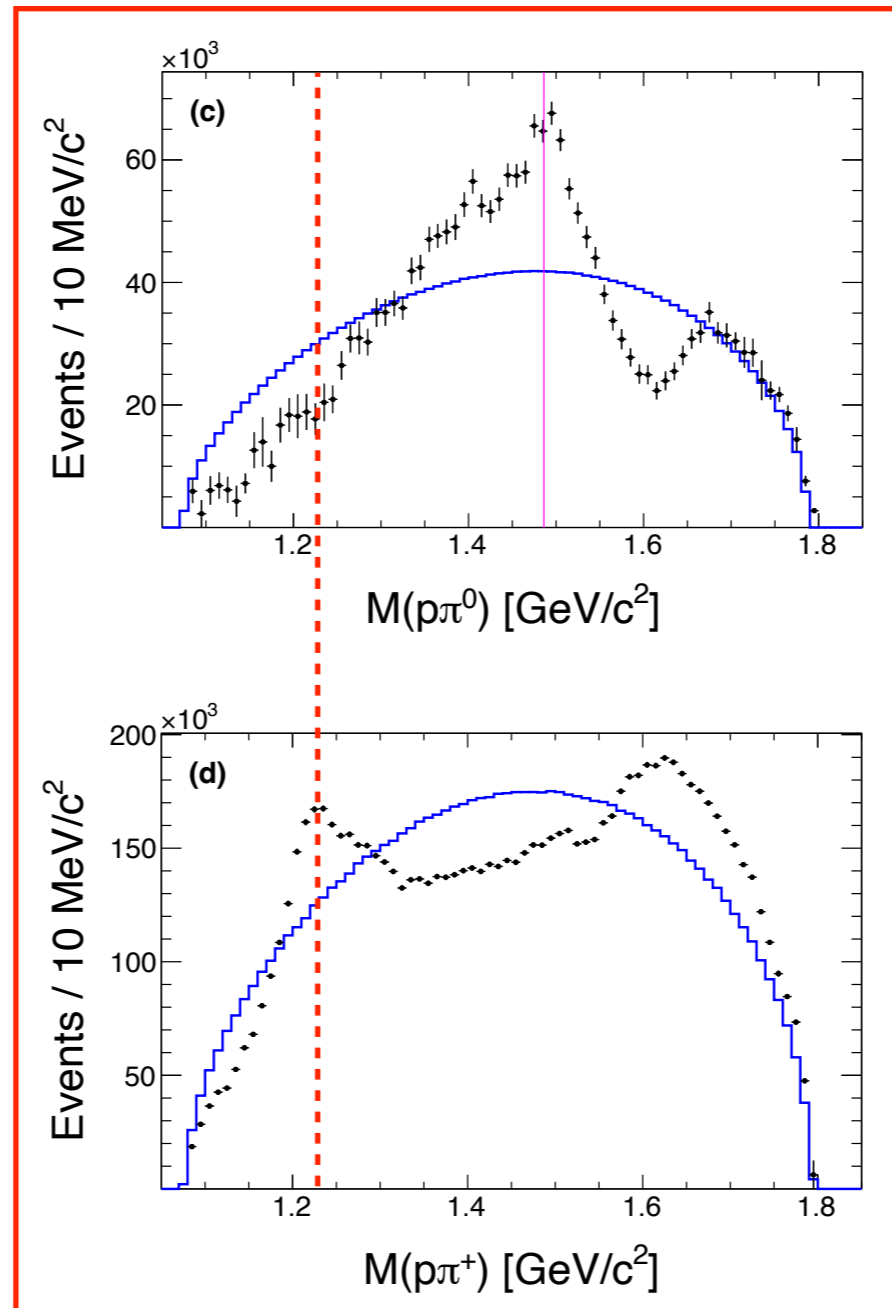
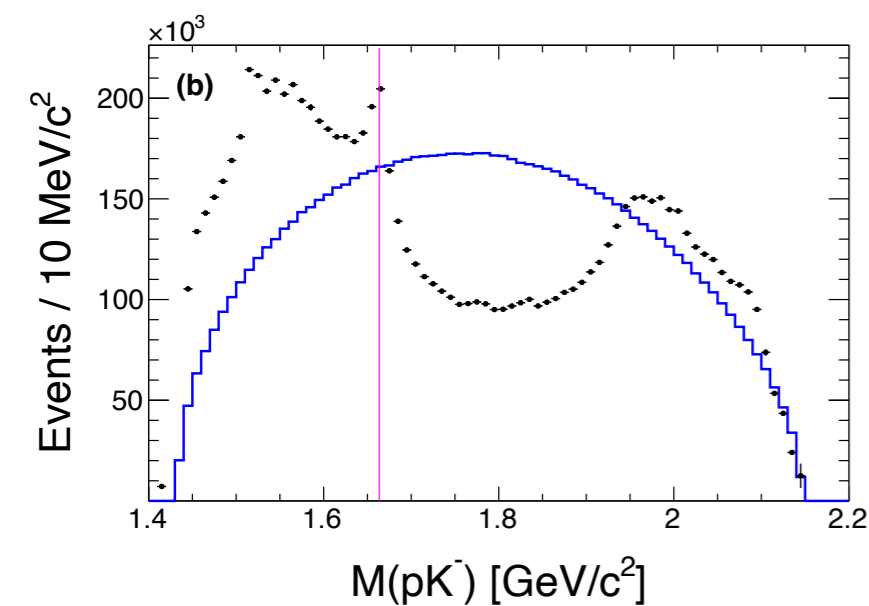


# $\Delta(1232)$ suppression in $M(p\pi^0)$

$$\Lambda_c^+ \rightarrow pK_S^0\pi^0$$



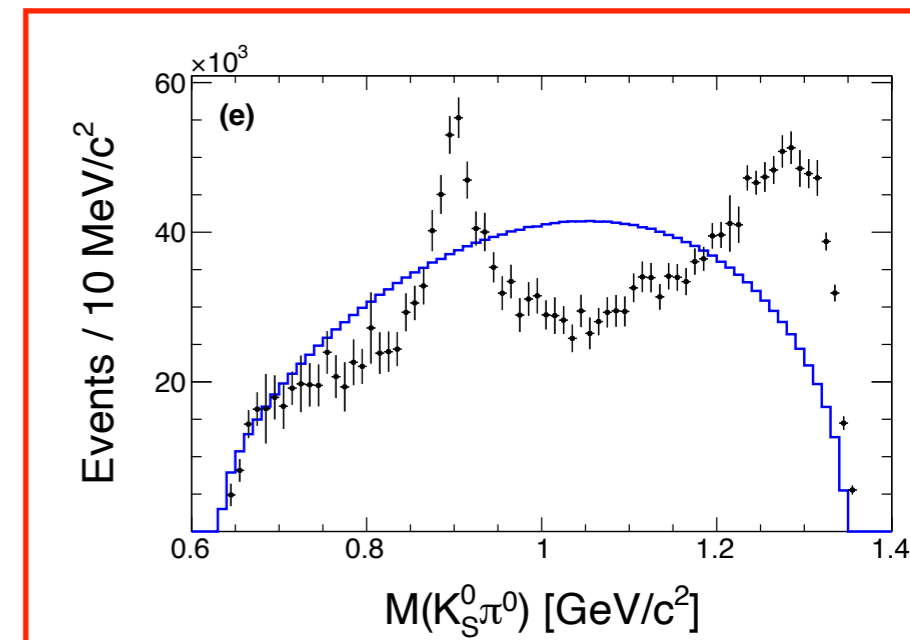
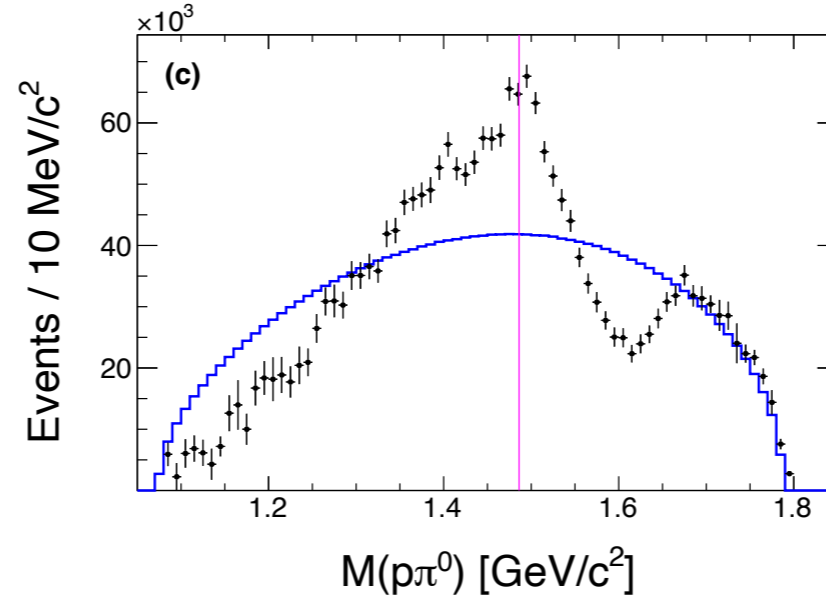
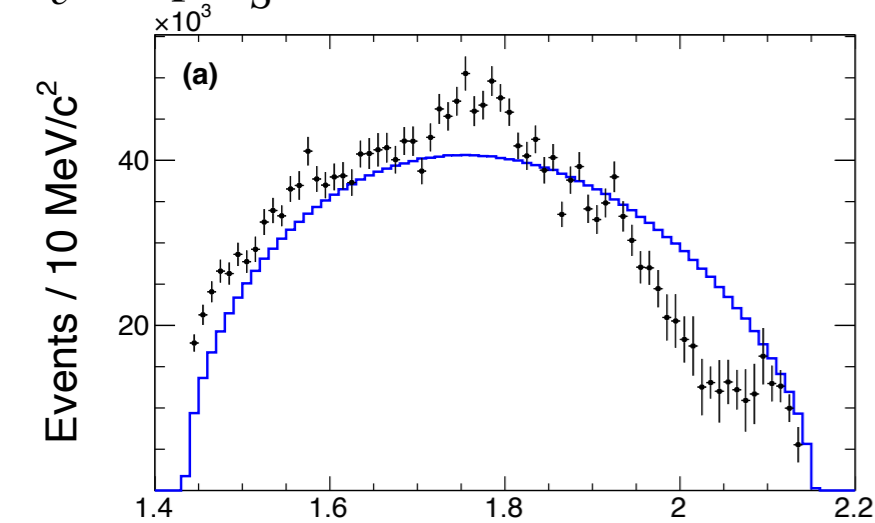
$$\Lambda_c^+ \rightarrow pK^-\pi^+$$



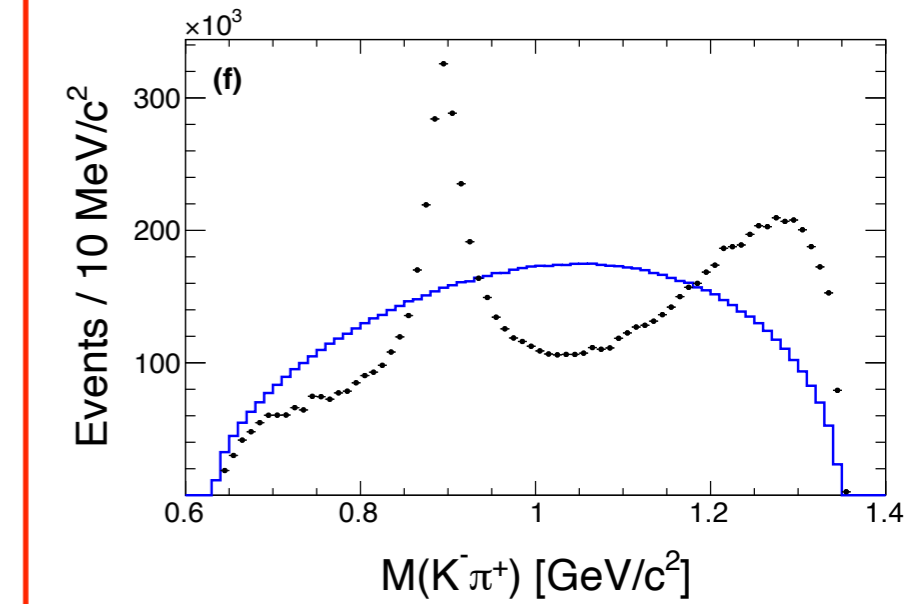
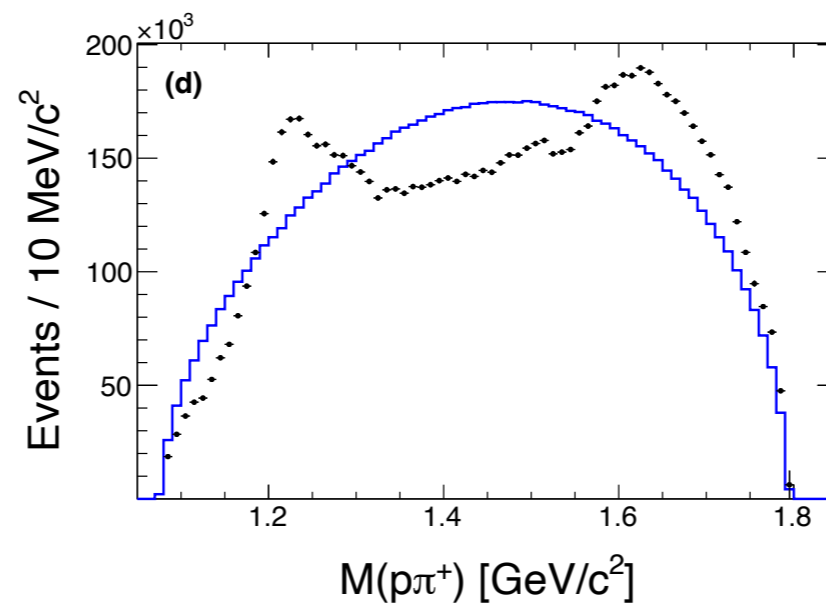
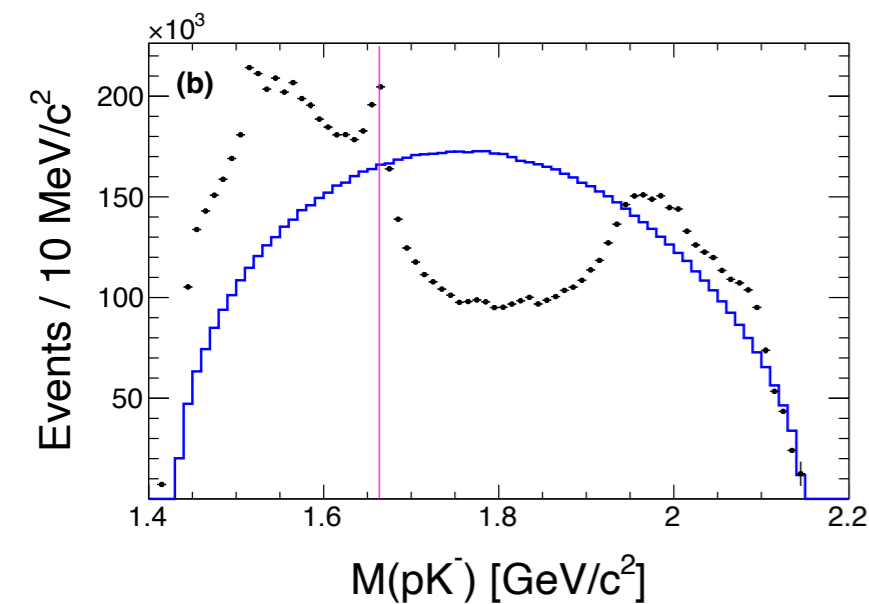
- The  $\Delta(1232)$  is not clearly seen in the  $M(p\pi^0)$ 
  - Isospin sum rule  $-\mathcal{A}(\Lambda_c^+ \rightarrow K^- \Delta^{++}) + \sqrt{3}\mathcal{A}(\Lambda_c^+ \rightarrow \bar{K}^0 \Delta^+) = 0$  indicates suppression of  $\Delta^+$  in the  $M(p\pi^0)$

# Same line shapes in $K\pi$ systems

$$\Lambda_c^+ \rightarrow p K_S^0 \pi^0$$



$$\Lambda_c^+ \rightarrow p K^- \pi^+ M(p K_S^0) [\text{GeV}/c^2]$$



- $K^*(892)$  and high mass  $M(K\pi)$  enhancements are clearly seen
- Same line shapes.  $\Lambda_c^+ \rightarrow p \bar{K}^{*0}$ ;  $\bar{K}^{*0} \rightarrow K^- \pi^+ / K_S^0 \pi^0$

# Summary

- We have been analyzing  $\Lambda_c^+ \rightarrow pK_S^0\pi^0$  using the Belle 980/fb data sample.
  - ➔ 130k signal candidates (100 times larger statistics than current PDG)
- We report
  - $\Gamma(\Lambda_c^+ \rightarrow pK_S^0\pi^0)/\Gamma(\Lambda_c^+ \rightarrow pK^-\pi^+) = 0.339 \pm 0.002(\text{stat.}) \pm 0.009(\text{syst.})$
  - $\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0) = 2.12 \pm 0.01(\text{stat.}) \pm 0.05(\text{syst.}) \pm 0.10(\text{norm.})$
- Mass projection spectra (Intermediate resonances)
  - ➔ Absence of  $\Sigma^*$
  - ➔ Possible  $p\eta$  threshold cusp
- Paper has been submitted to PRD.
  - ➔ You can find the paper at [arXiv:2503.04371](https://arxiv.org/abs/2503.04371)

**Thank you**