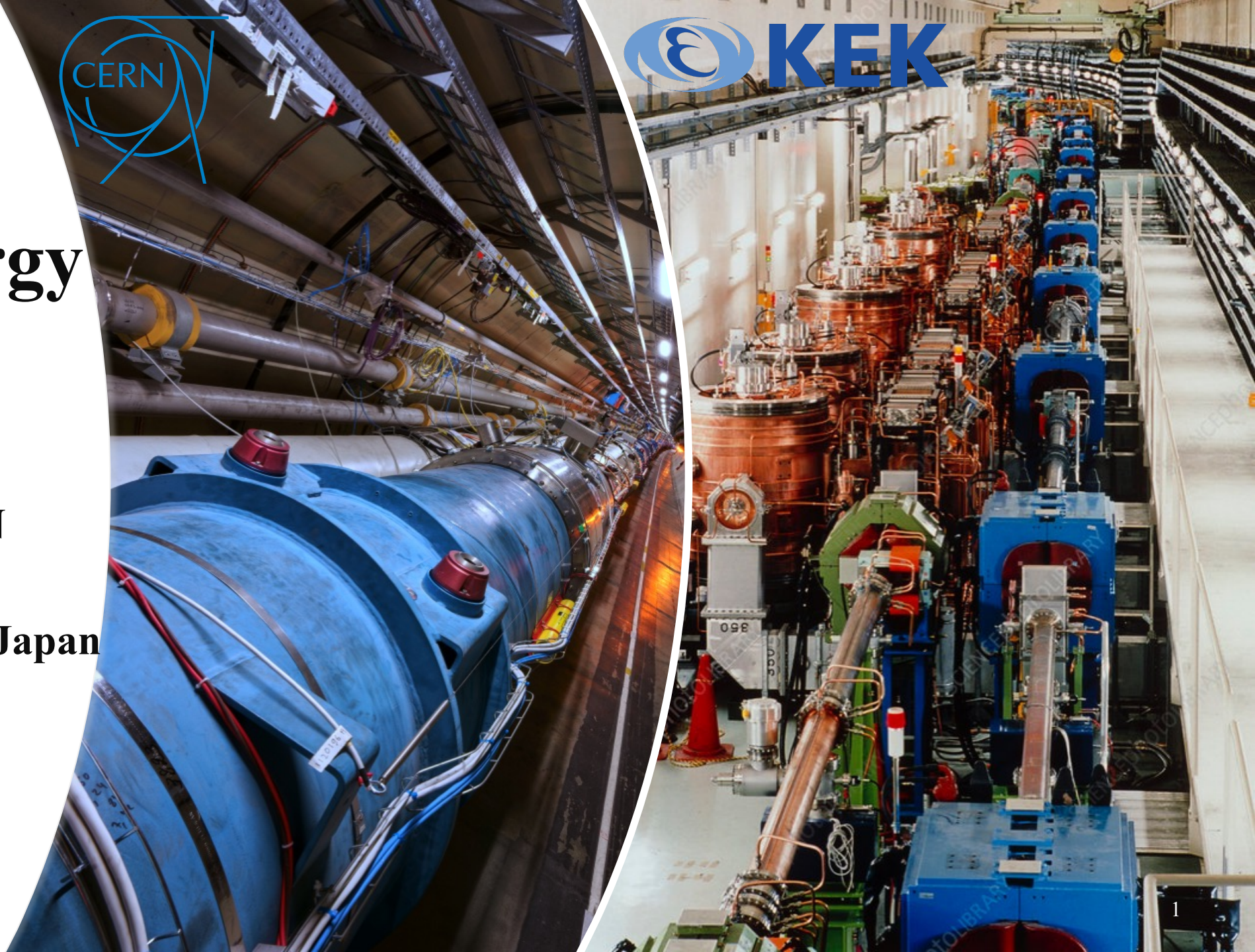
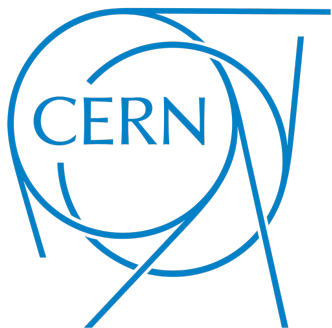
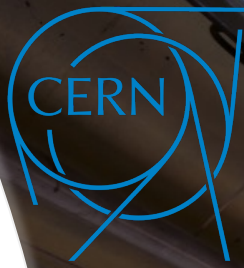


Missing energy B decays @ LHCb

Abhijit Mathad, CERN

On behalf of LHCb

Belle II Physics Week, Japan



Talk content

➤ Common techniques in missing energy decays.

➤ Analyses this year (newest to oldest):

➤ (Rare) Searches for $B^0 \rightarrow h^+ h^- \tau^+ \tau^-$.

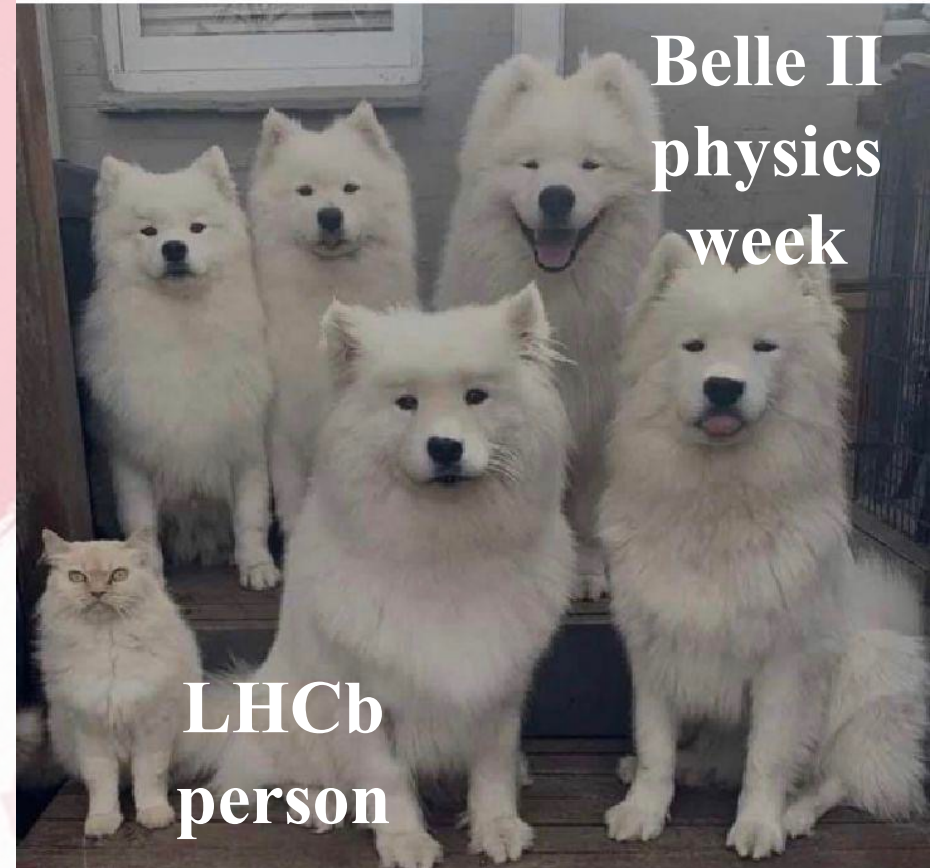
➤ (Very rare) LFV search: $B^0 \rightarrow K^{*0} \tau^\pm e^\mp$.

➤ (Abundant) Evidence of $B^- \rightarrow D^{**0} \tau^- \bar{\nu}$.

➤ Conclusions

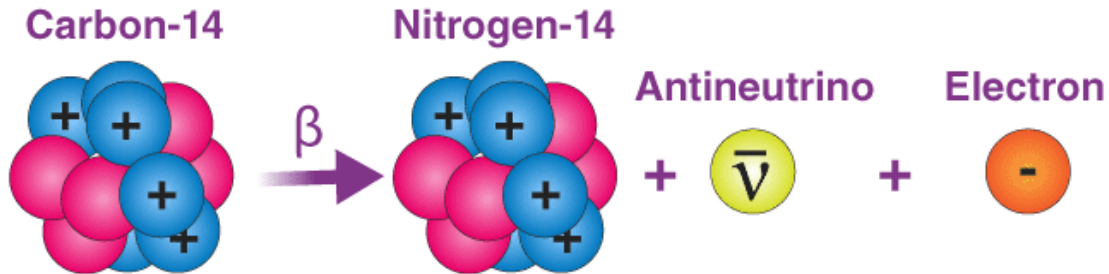
Day 2 :

They haven't noticed a thing

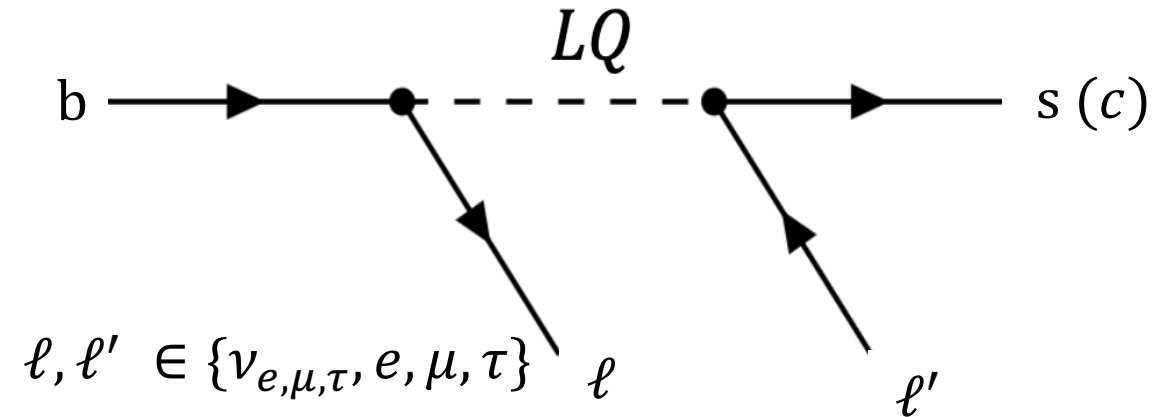


Missing energy decays have evolved

First missing-energy β decays: **neutrino discovery, parity violation, weak theory**, and still a BSM probe (e.g. KATRIN).



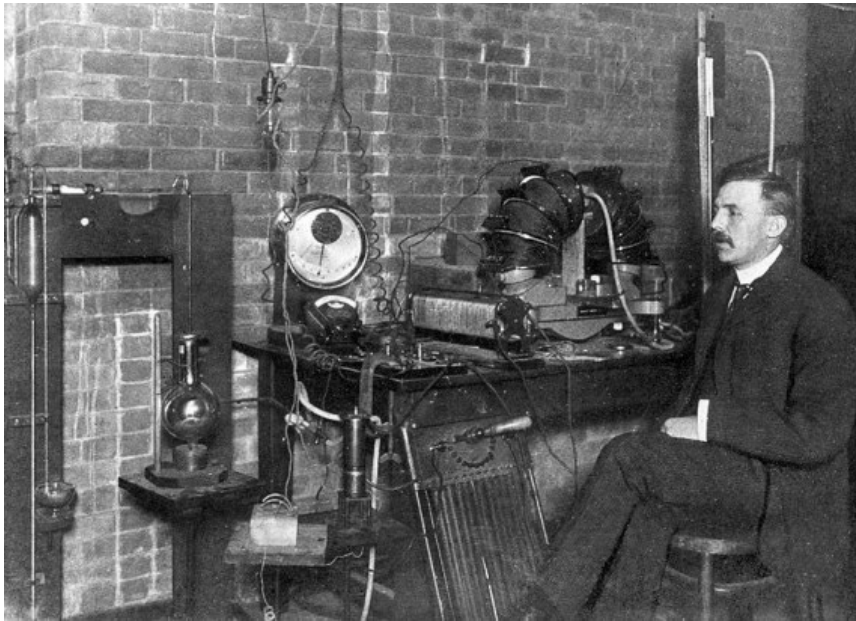
Can **heavy flavour missing energy** decays reveal new physics?



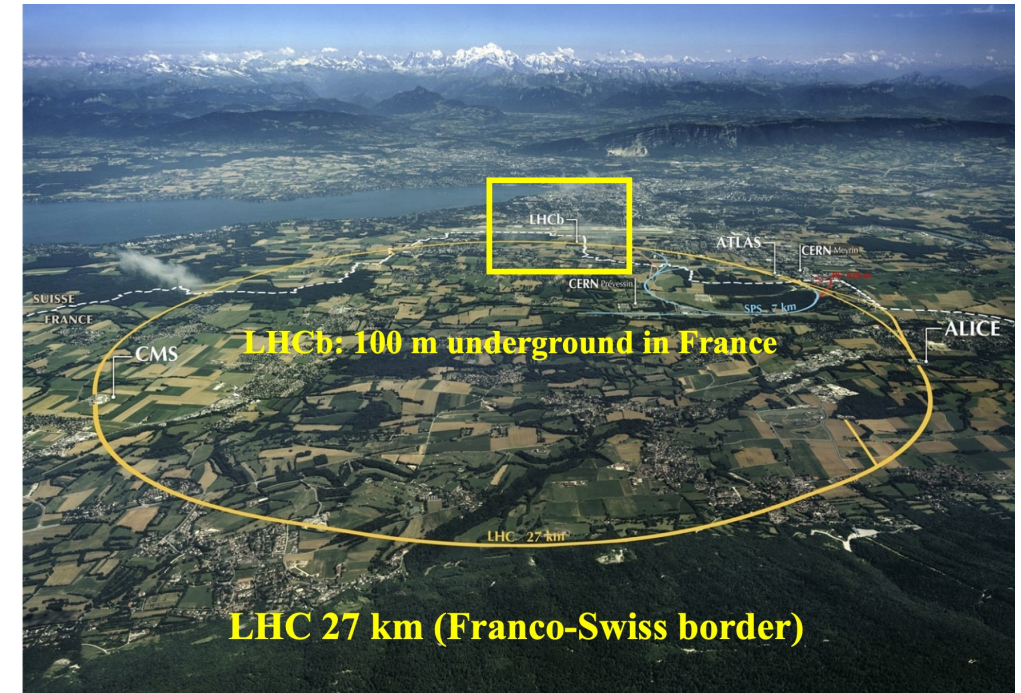
Current tensions: $R(D^{(*)})$ **3.8σ** , $\text{BF}(B^+ \rightarrow K^+ \nu \bar{\nu})$ **2.7σ** ,
 $\text{BF}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$ **1.7σ** !

Missing energy experiments have evolved

First missing energy, β
decay, experiments (1890s)



Facilities hosting heavy flavour
experiments (Now)



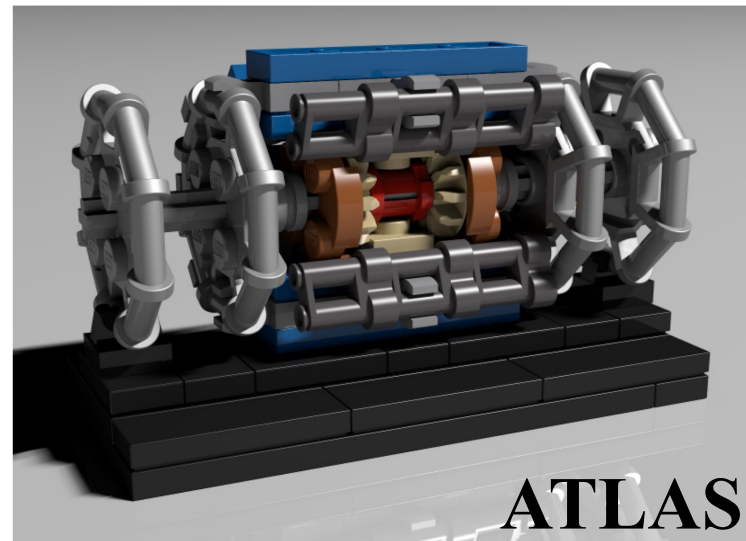
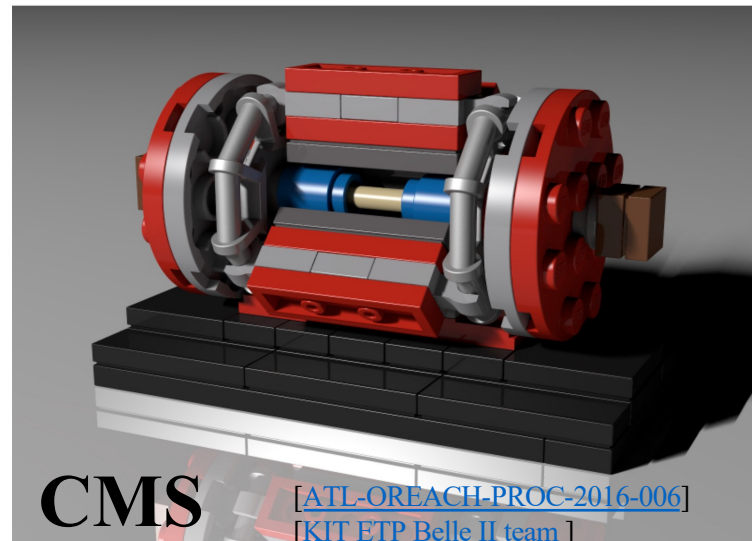
Up to 2,808 proton bunches per beam collide every
25 ns at four interaction points at $\sqrt{s} = 13.6$ TeV.



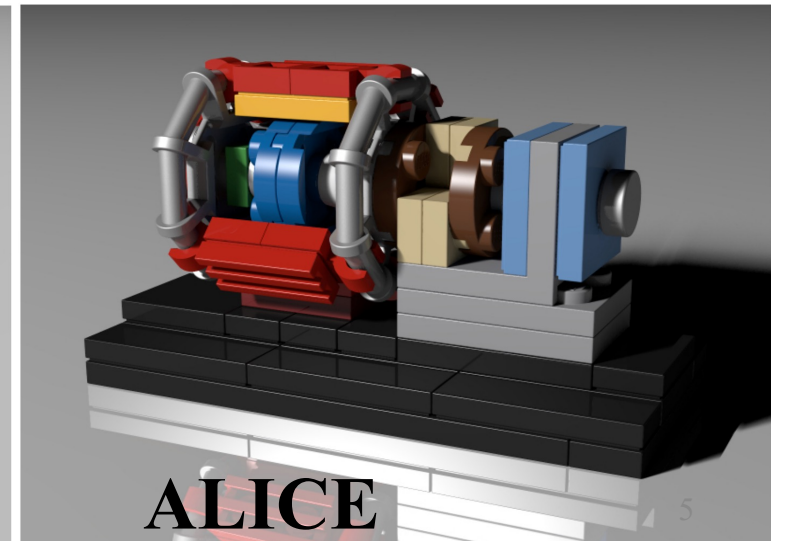
One such collision point is LHCb.

- Since its 1998 [proposal](#), LHCb has become a **general-purpose forward detector**.
- Has rich missing-energy B decay programme from abundant to rare decays.

High-pT signatures, but **also do missing-energy B decays (e.g. $R(J/\psi)$ @ CMS)**



Heavy ion physics



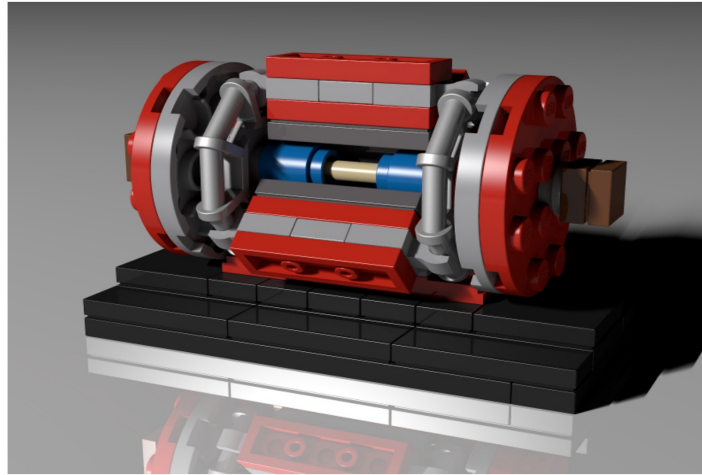
Best experiment for missing-energy B decays?

LHCb @ CERN



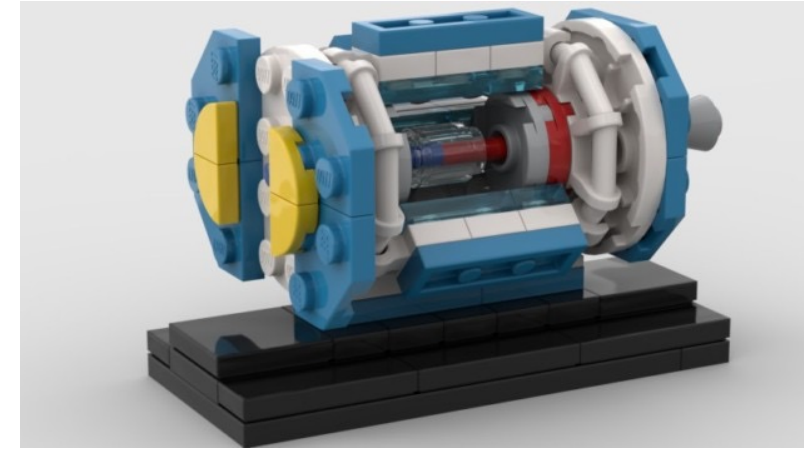
Vs

ATLAS/CMS @ CERN



Vs

Belle II @ KEK

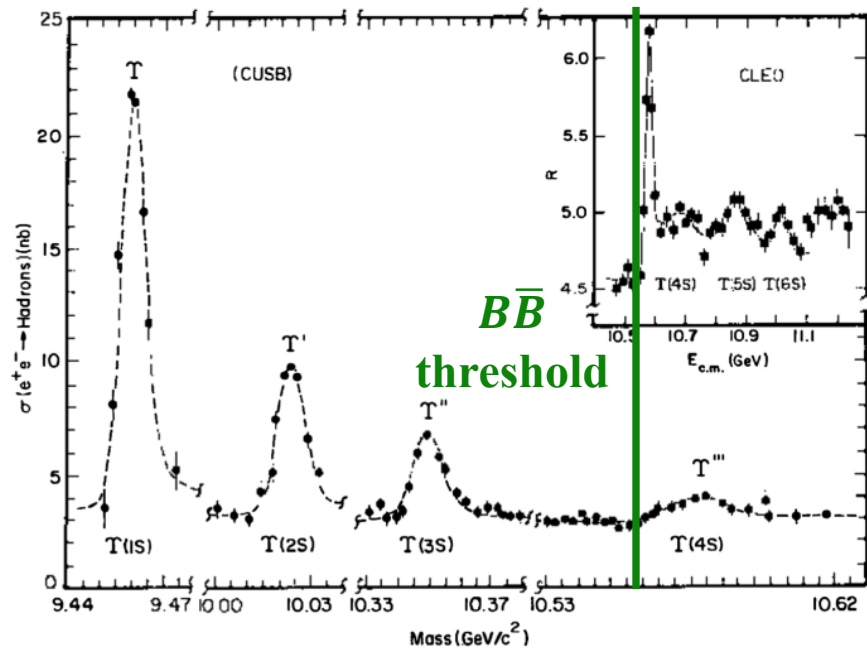


Who wins, you decide!

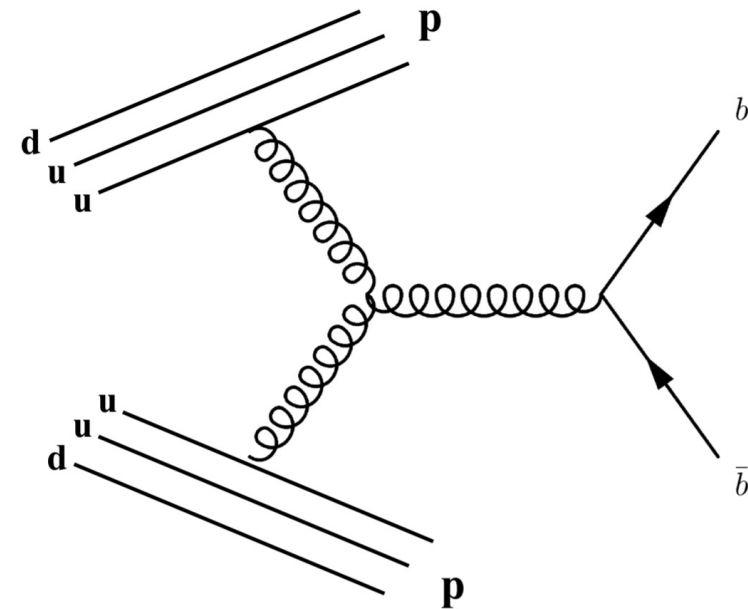
Ideal place is Belle II conditions

At Belle-II, $B\bar{B}$ produced via $e^+e^- \rightarrow \gamma(4S)$
($\sqrt{s} = 10.58$ GeV)

At LHC, **95% of $b\bar{b}$ via gluon fusion**
(pp collision @ $\sqrt{s} = 13.6$ TeV)

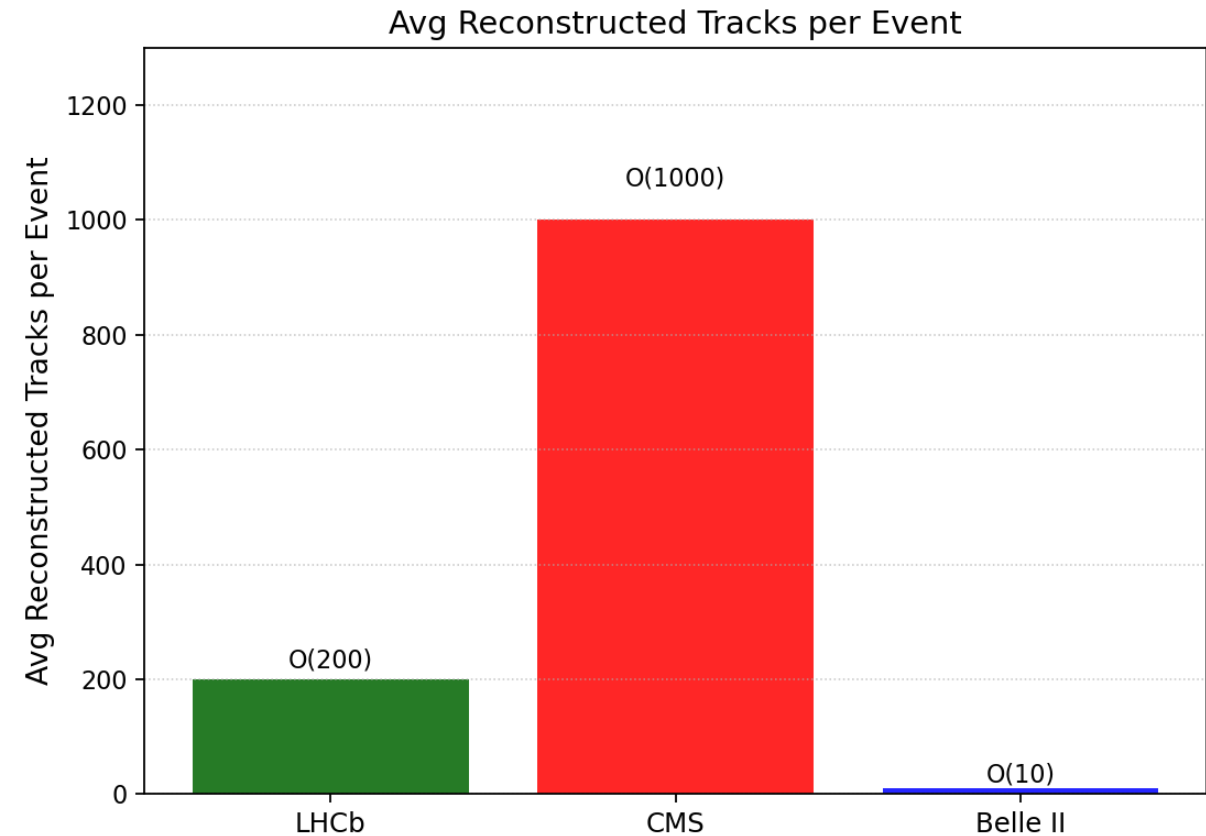
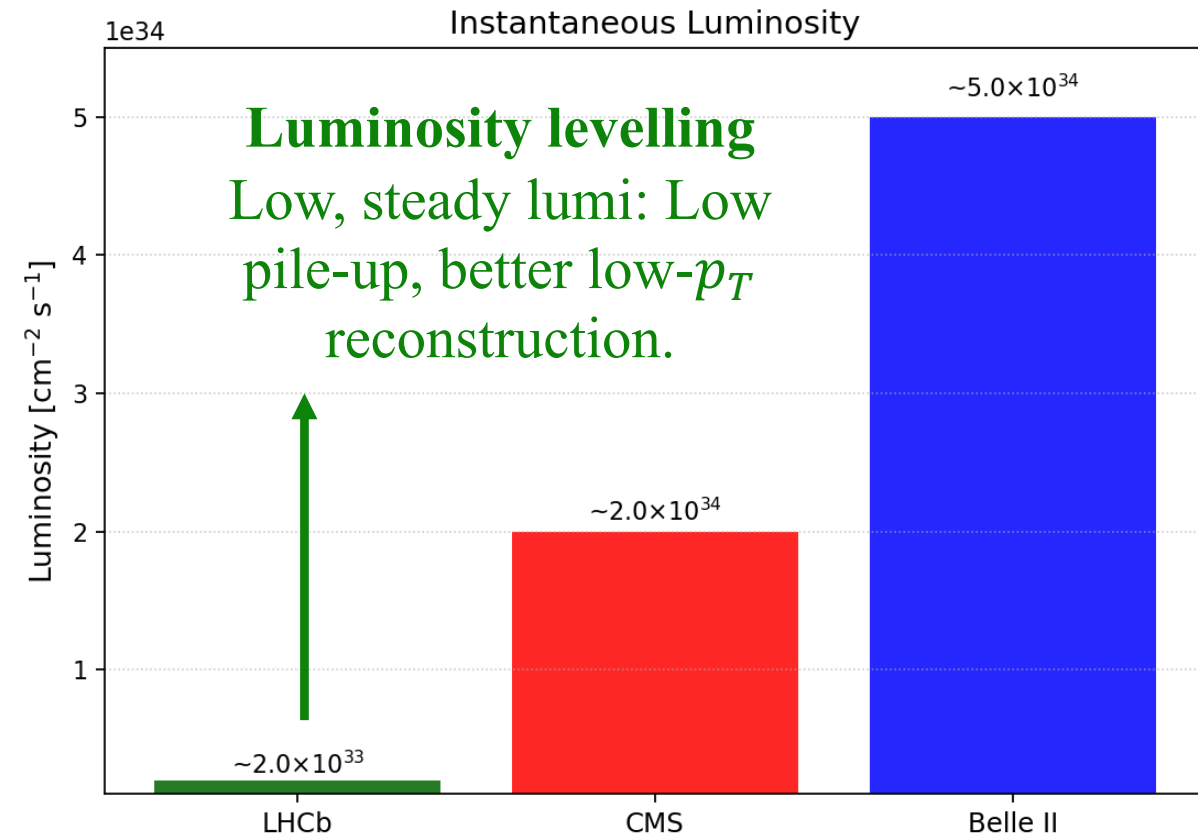


Fixed CoM energy!



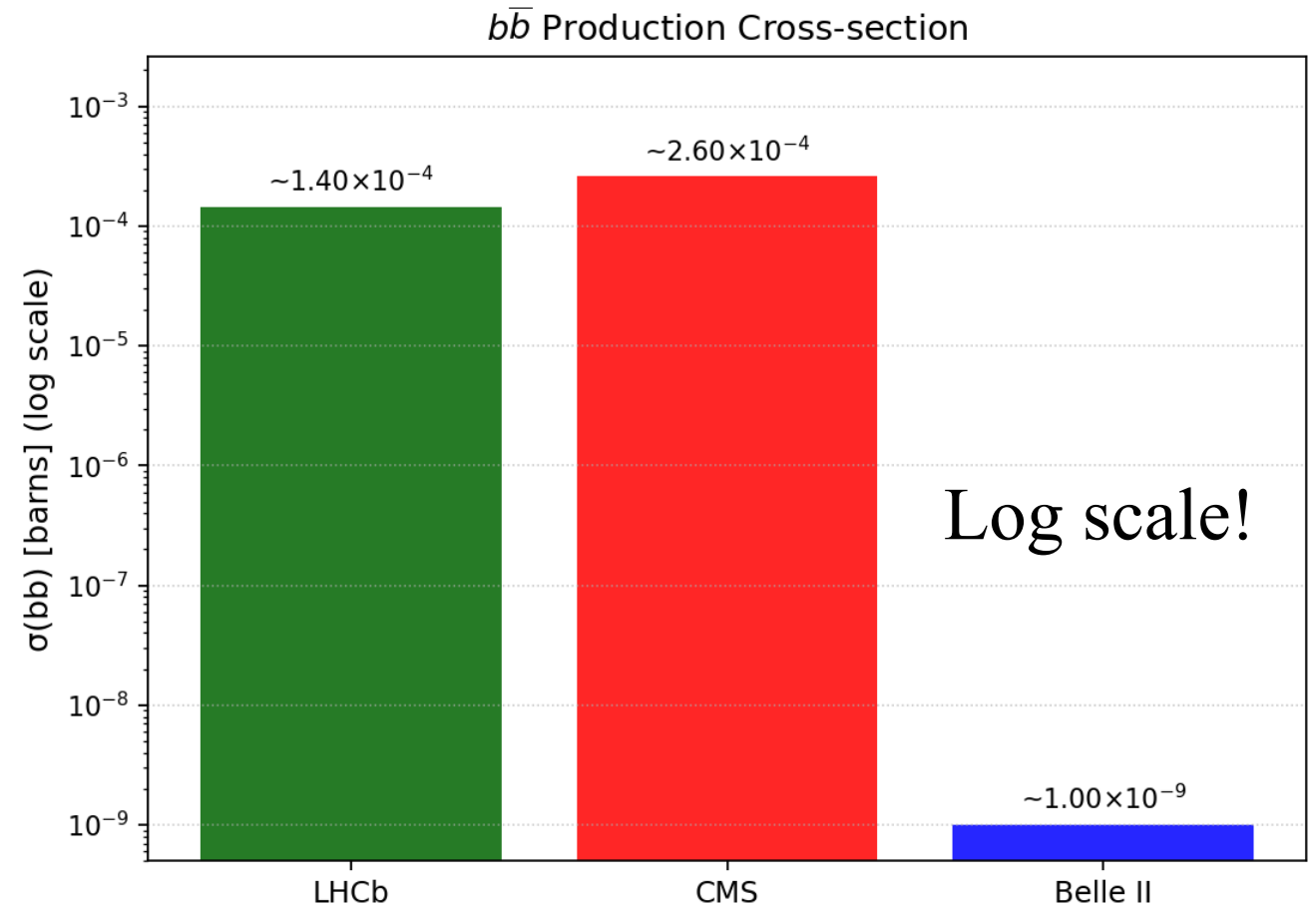
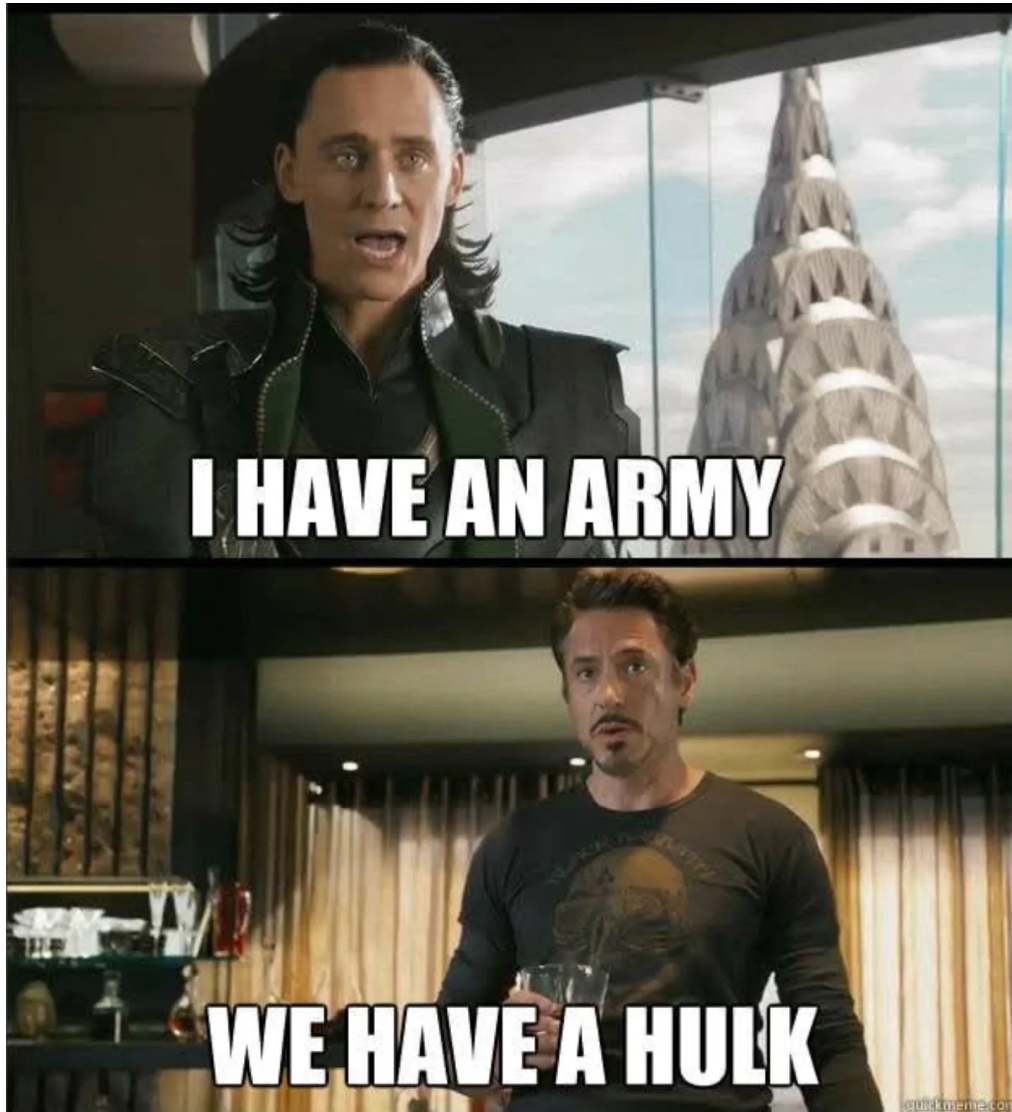
**How much proton momentum
carried by gluon?**

Ideal place is Belle II conditions



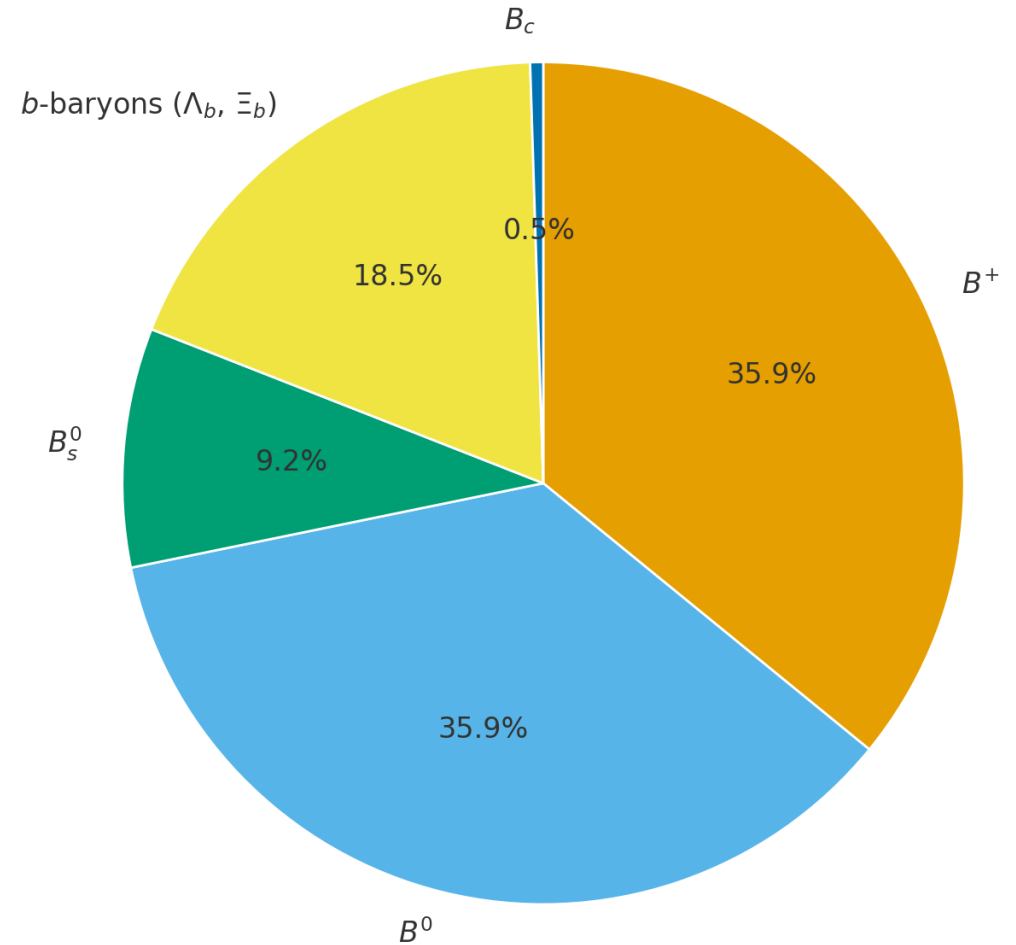
Belle II achieves large peak luminosities (**$25\times$ LHCb**), with clean reconstructed event (**factor 20 lower tracks per event than LHCb**).

But...



$b\bar{b}$ production 5 orders of magnitude higher at LHC!

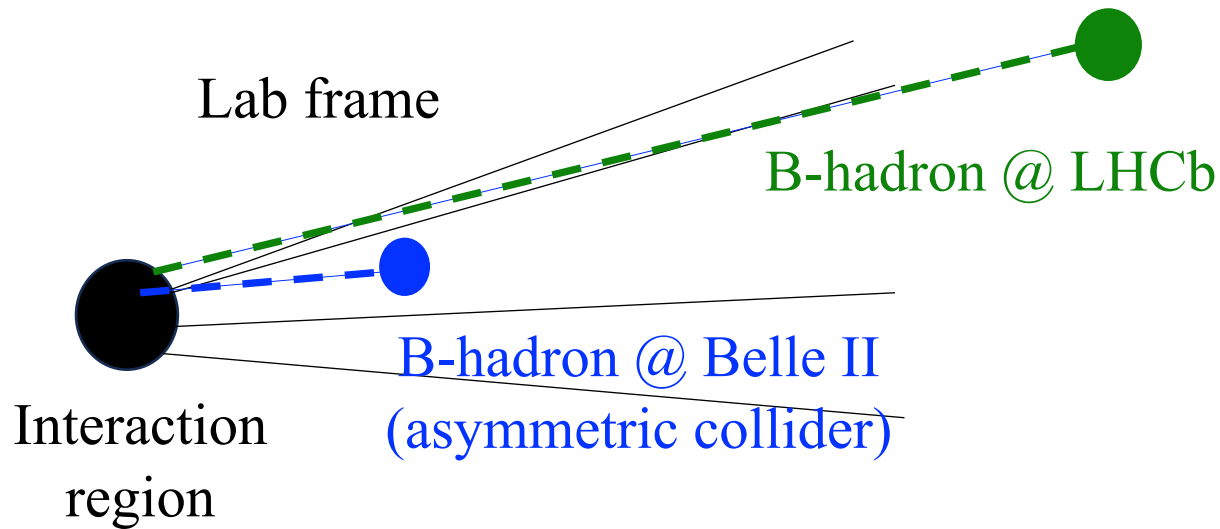
LHC produces different species of b-hadron



At Belle-II its $B^\pm$ or $B^0/\bar{B}^0$.

Large boost and excellent vertexing/tracking

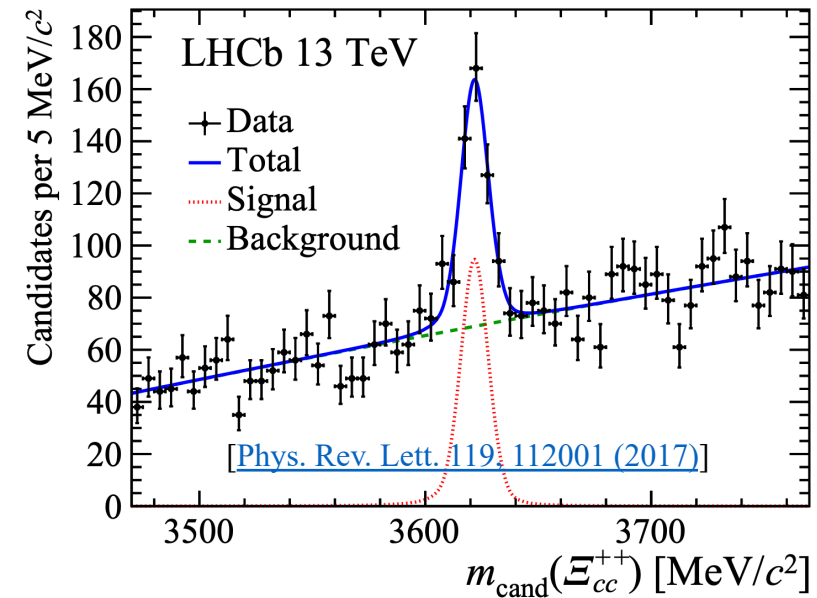
Large boosts @ LHC



Flight distance @ LHCb ~ 1 cm

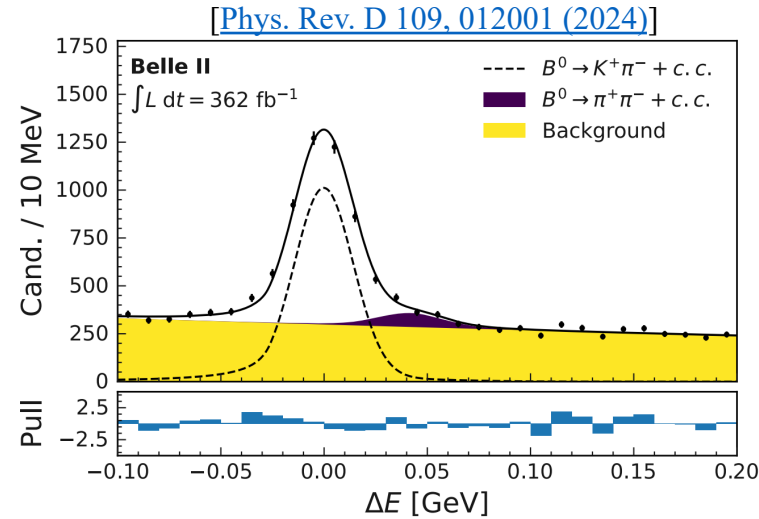
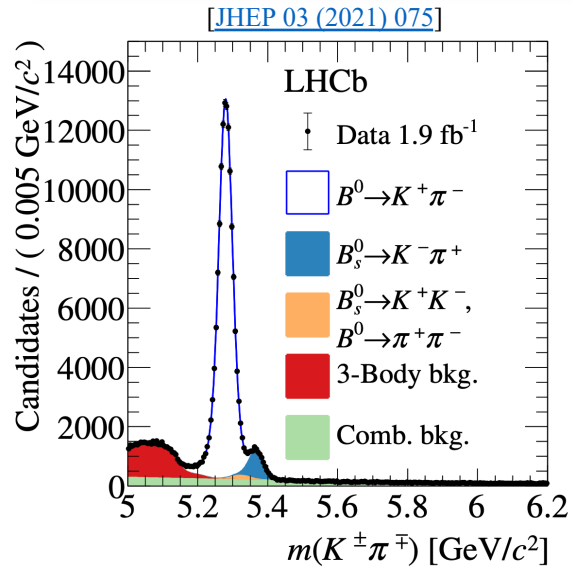
Flight distance @ Belle II ~ 130 μm

Power of vertexing and tracking

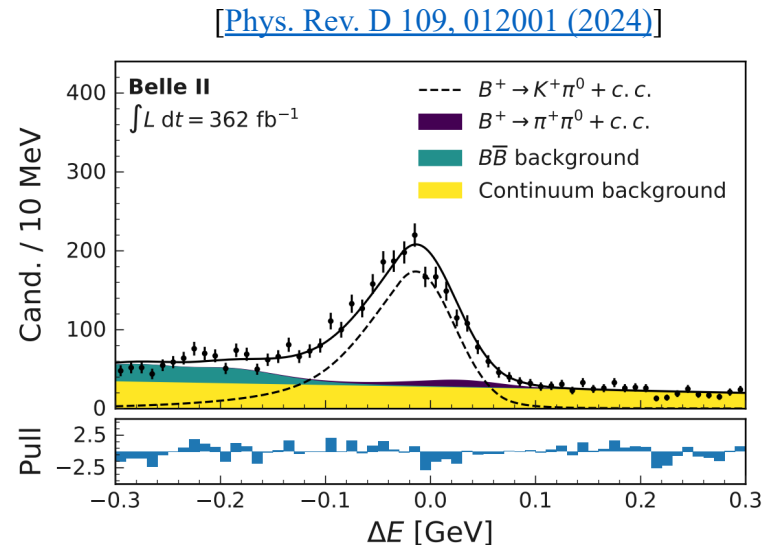
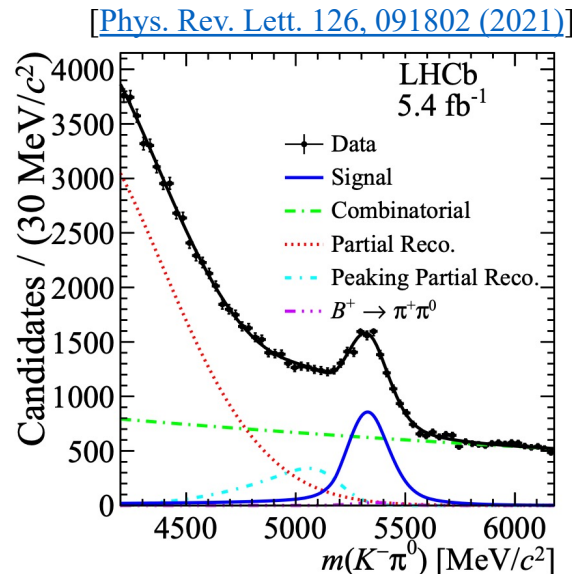


Allows to reconstruct particles (Ξ_c^{++}) with lifetimes $6 \times$ lower than **B** ($\tau_B \sim 1.5$ ps)!

Implications of large boosts + precise vertexing/tracking



Excellent S/B for **fully reconstructed** decays.

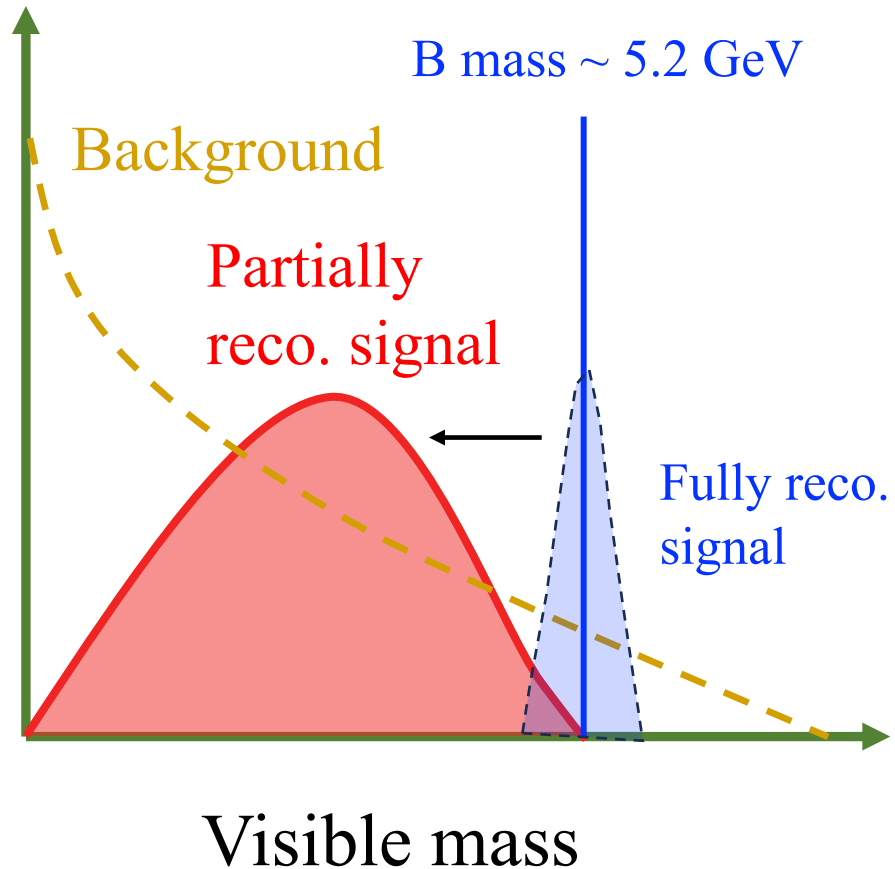


Still gives a good S/B for cases **without explicit B decay vertex**.

S/B much worse for missing energy decays

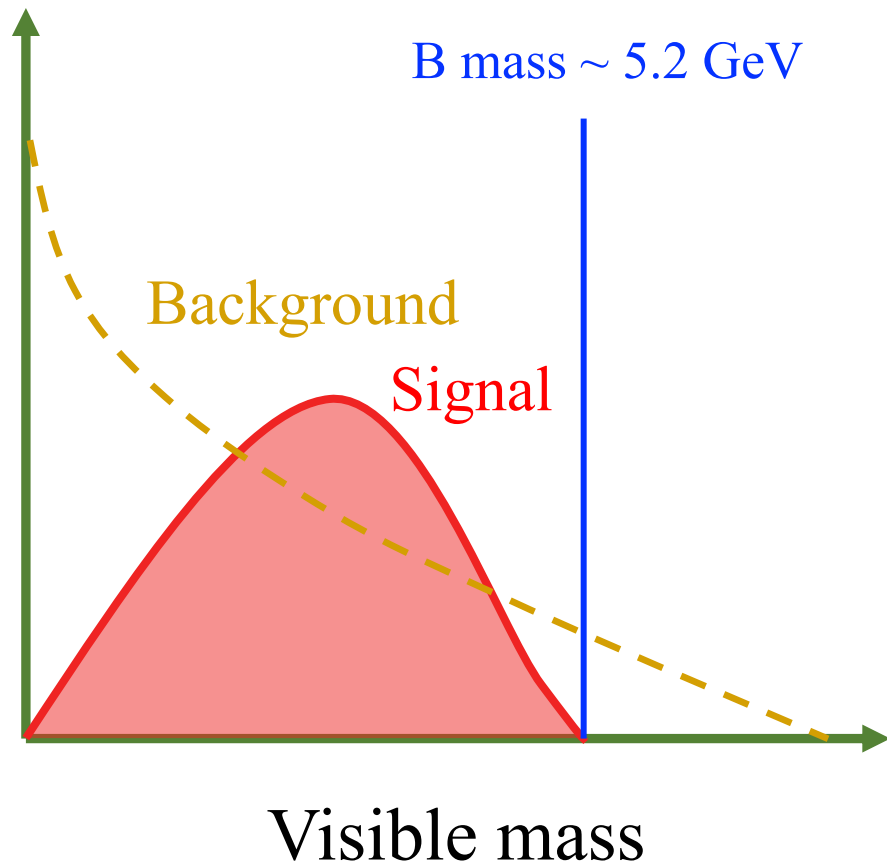
Missing particle: S/B very low.

How do we recover that lost energy?

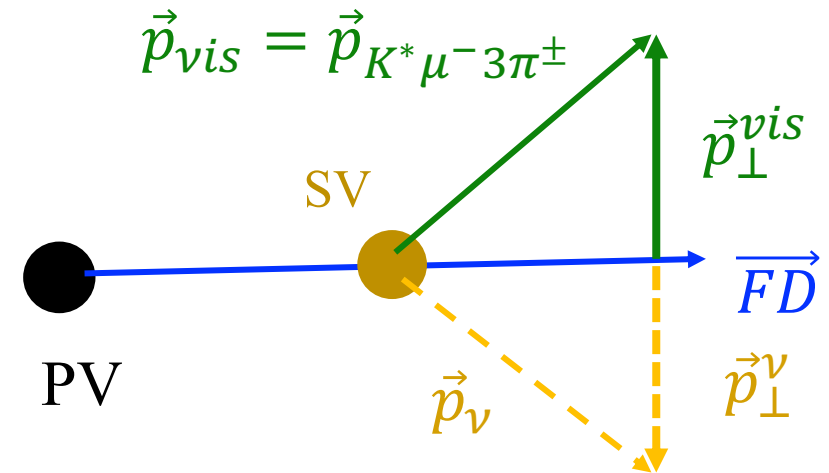


Technique 1: How do we recover a better S/B?

Missing particle: Peaks below B mass
How do we recover that low energy?



Define corrected mass



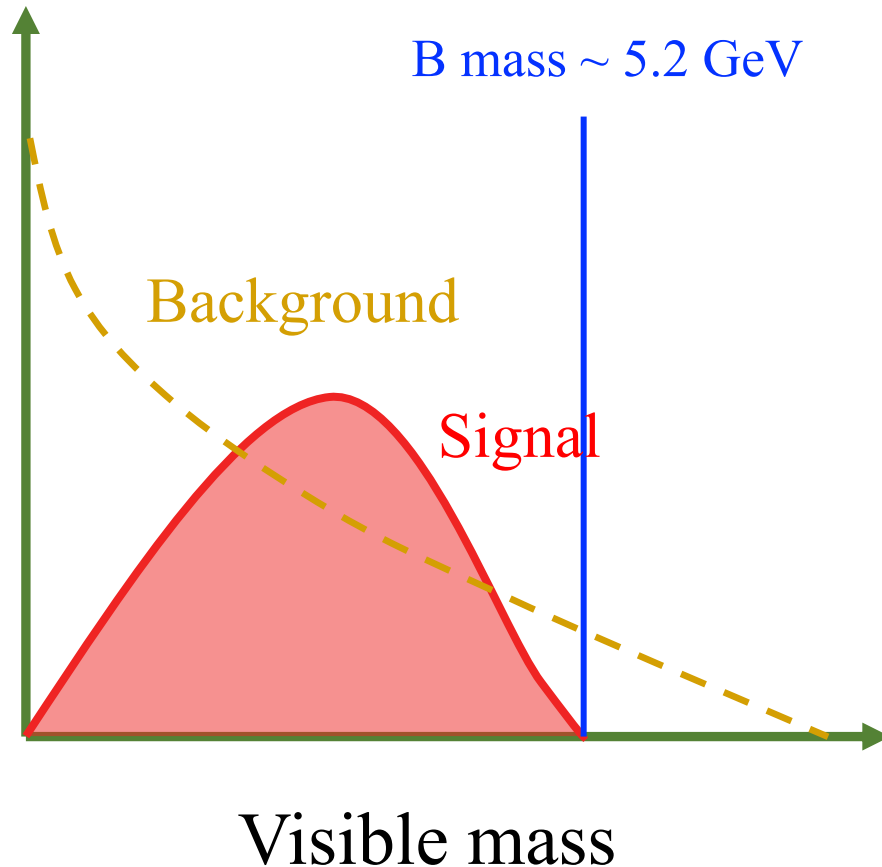
$$\vec{p}_\perp^{vis} = -\vec{p}_\perp^v$$

Assume $|\vec{p}_\parallel^v| = 0$

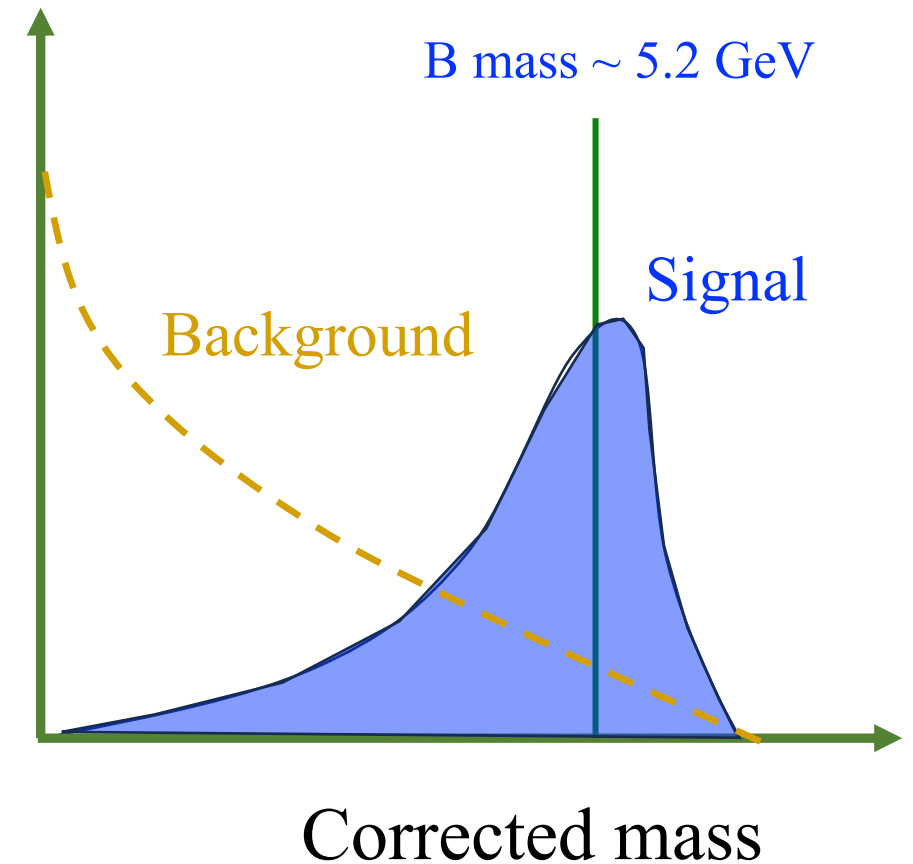
$$m_{corr} = \sqrt{M_{vis}^2 + |\vec{p}_\perp^{vis}|^2 + |\vec{p}_\perp^{vis}|^2}$$

How do we recover a better S/B?

Missing particle: Peaks below B mass
How do we recover that low energy?



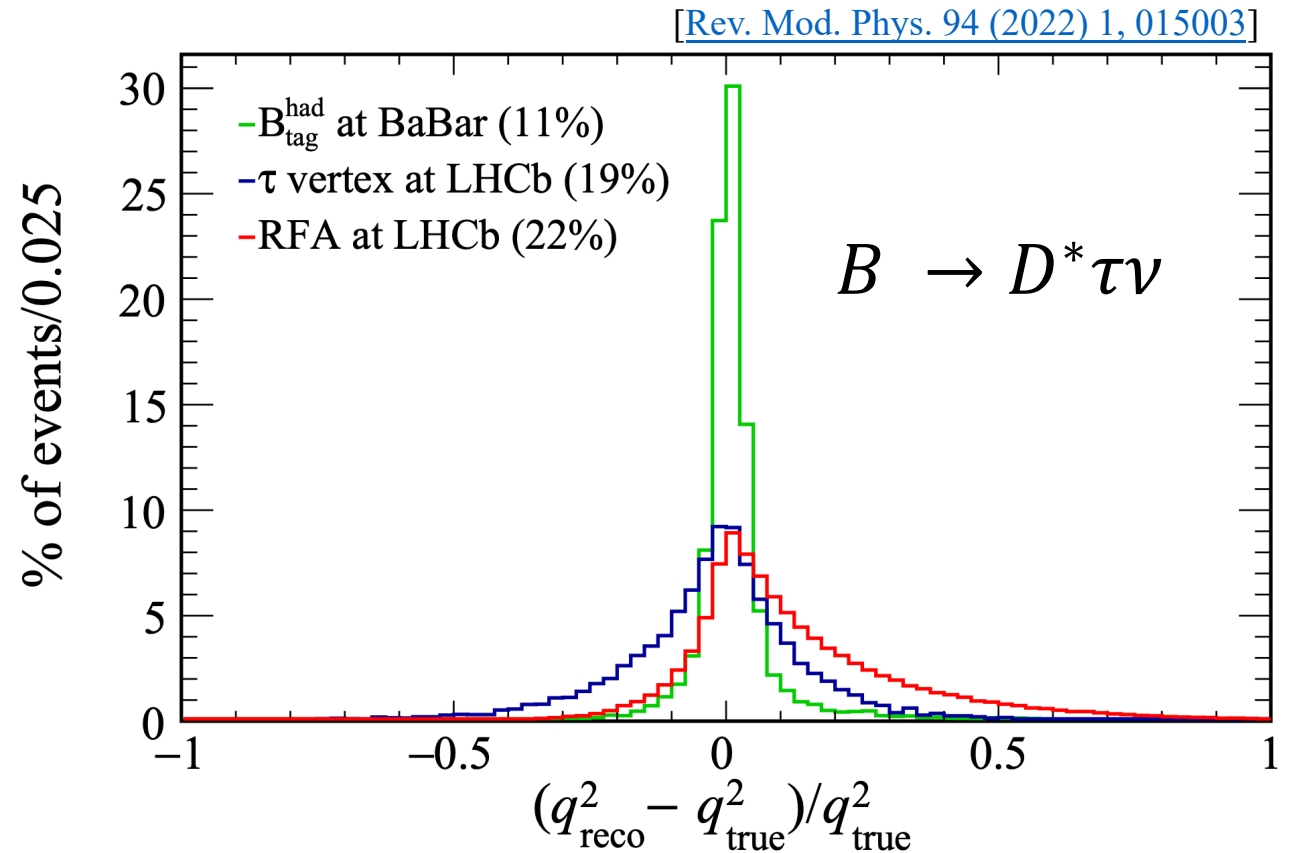
Corrected mass provides a much better S/B!
(used in LFV $B^0 \rightarrow K^{*0} \tau^+ \mu^-$)



Technique 2: Kinematic reconstruction

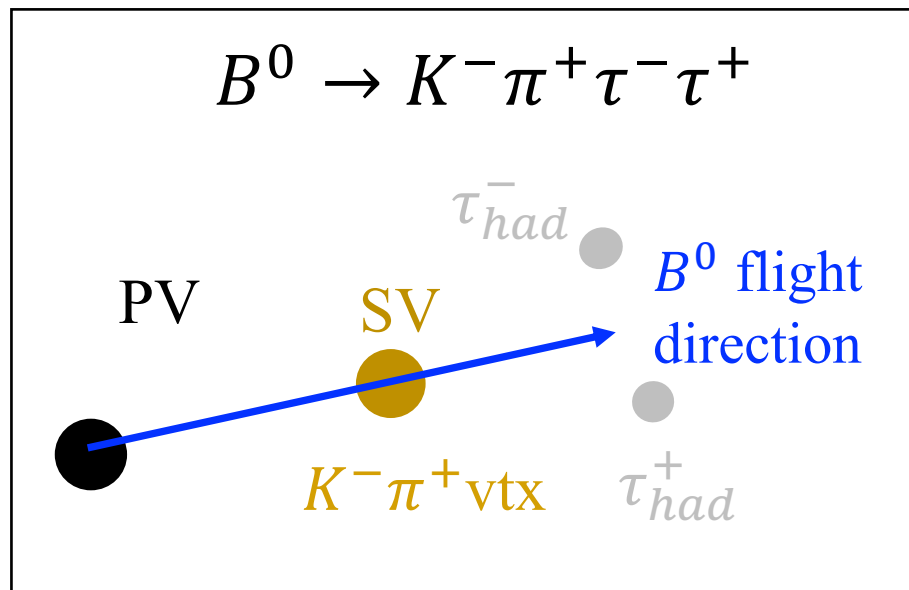
Reconstructing B momentum, q^2 , and angles depend on **decay-specific kinematic and geometric constraints**.

Different reconstruction methods lead to varying resolution. **Why?**

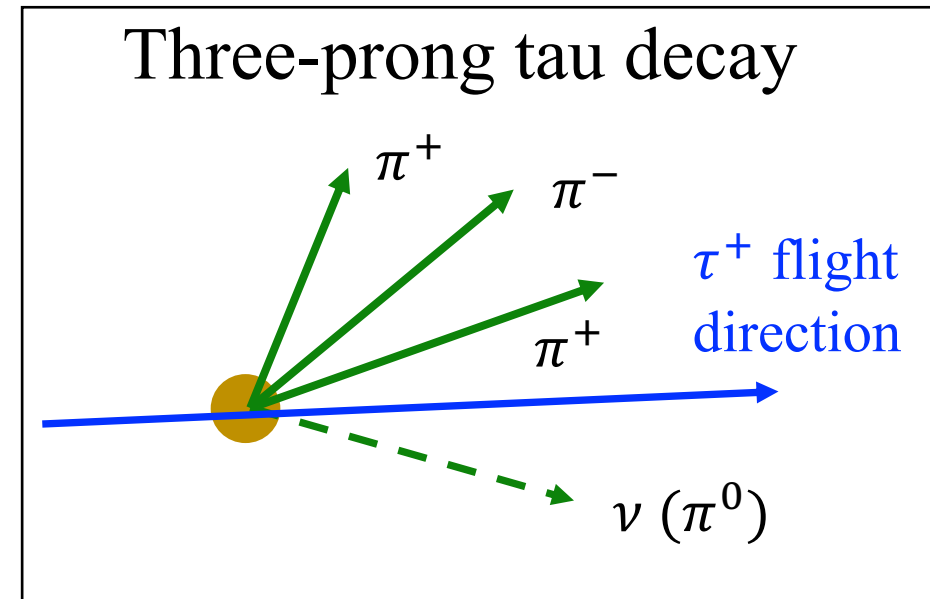


Kinematic reconstruction: Hadronic tau

Reconstructing B momentum, q^2 , and angles depend on **decay-specific kinematic and geometric constraints**.



+

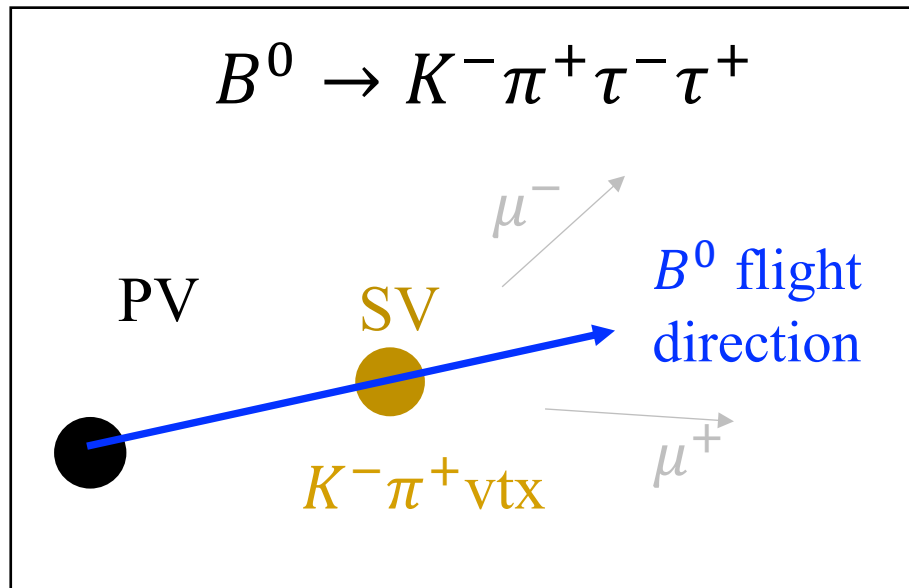


[[Thesis of Alessandro Mordá](#)]

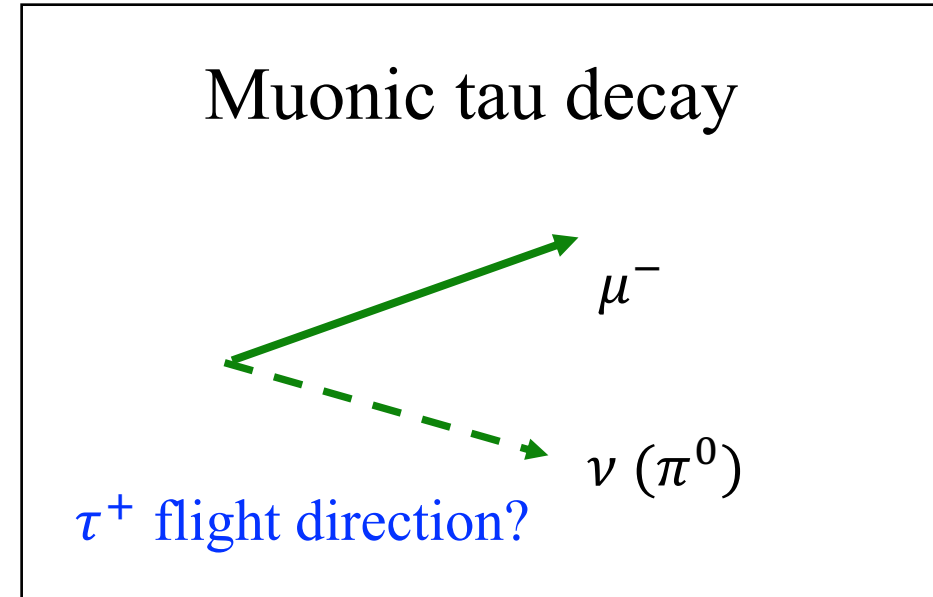
Combining τ and B flight vertex info $\rightarrow$ **Analytic B mom. $\rightarrow$ 2-fold ambiguity!**
But low statistics (low BF of τ & low eff.)

Kinematic reconstruction: Muonic tau

Reconstructing B momentum, q^2 , and angles depend on **decay-specific kinematic and geometric constraints**.



+



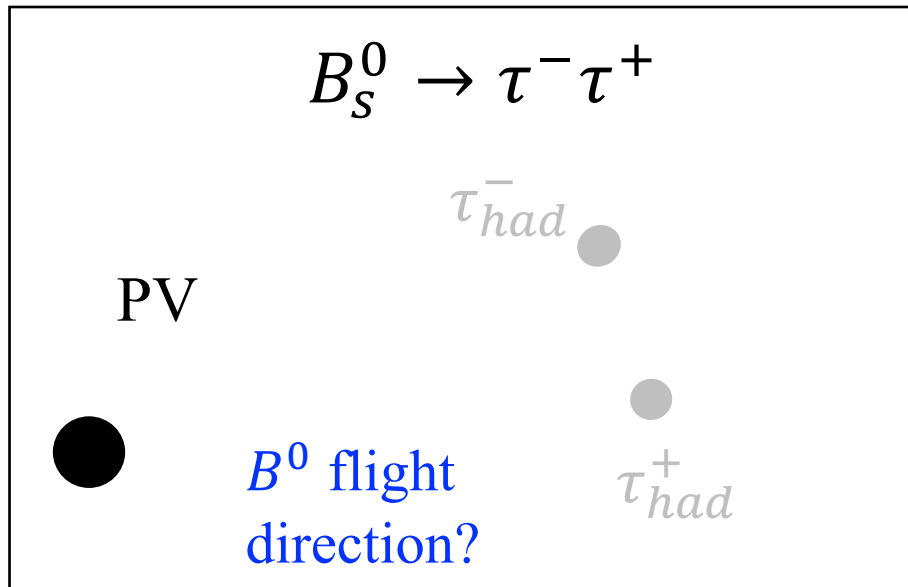
[RFA in $R(D^*)$ [analysis](#)].

Large statistics (high BF of τ & high eff.).

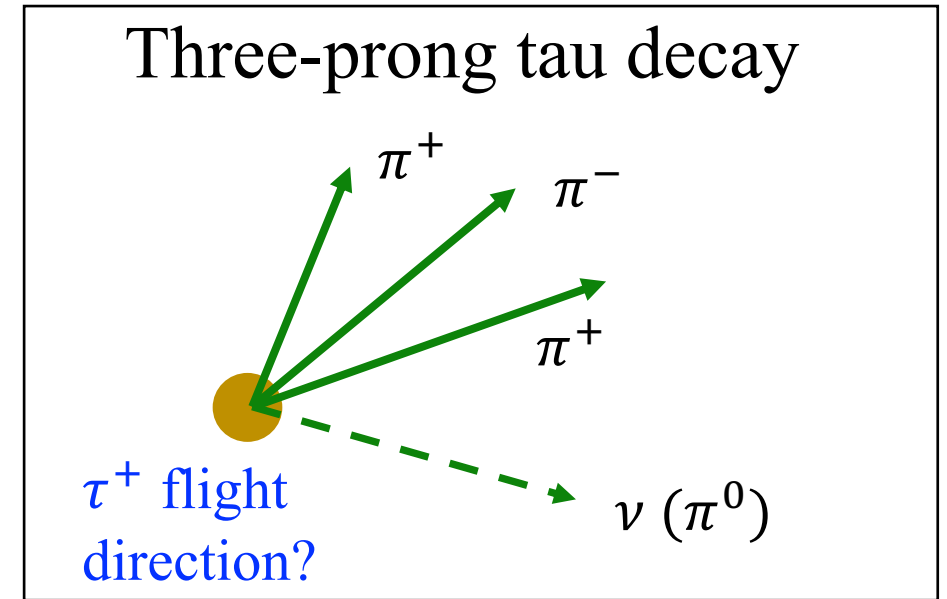
But no τ flight info (**rest frame approx.** $p_B^\parallel \propto p_{vis}^\parallel$), **worsens resolution**.

Situation not simple for kinematic reconstruction

Reconstructing B momentum, q^2 , and angles depend on **decay-specific kinematic and geometric constraints**.



+

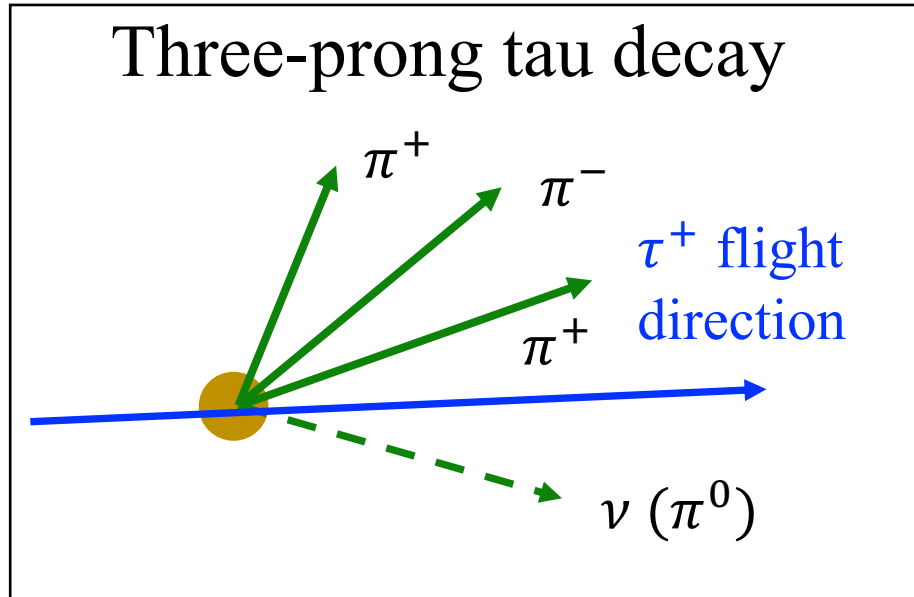


[[Thesis of Alessandro Mordá](#)]

No B flight info, but mass constraints $\rightarrow$ **Analytic B mom. $\rightarrow$ 2-fold ambiguity!**

Another advantage of hadronic τ

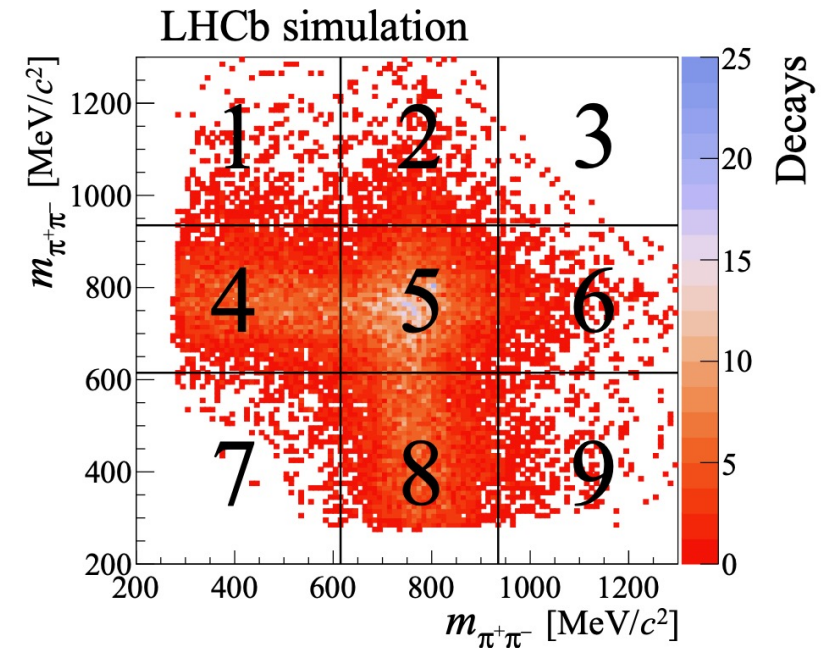
[[Phys. Rev. Lett. 118, 251802 \(2017\)](#)]



Proceeds mainly via

$$\tau^\pm \rightarrow a_1^\pm \bar{\nu}_\tau \rightarrow \rho^0 \pi^\pm \bar{\nu}_\tau \rightarrow \pi^+ \pi^- \pi^\pm \bar{\nu}_\tau.$$

Exploited in **search for $B_{(s)}^0 \rightarrow \tau^+ \tau^-$** : Dalitz plane used control bkg e.g. $B^0 \rightarrow D^- D_s^+$



Region 5 is signal-dominated; others regions define background or optimize selection.

Technique 3: Charged and neutral isolation

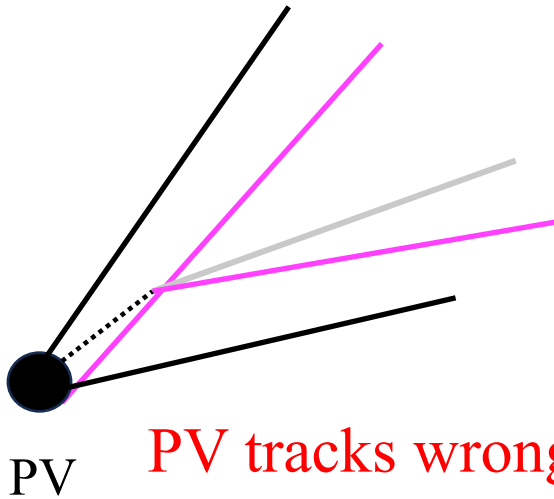
Signal tracks

PV



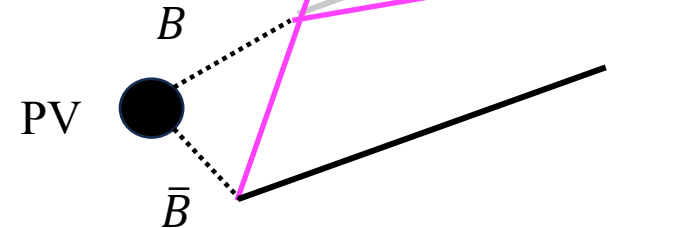
Feed-down: Extra tracks not reconstructed (e.g. $B \rightarrow K^* D \bar{D}$ feeding into $B_s \rightarrow K^* \tau \tau$)

PV



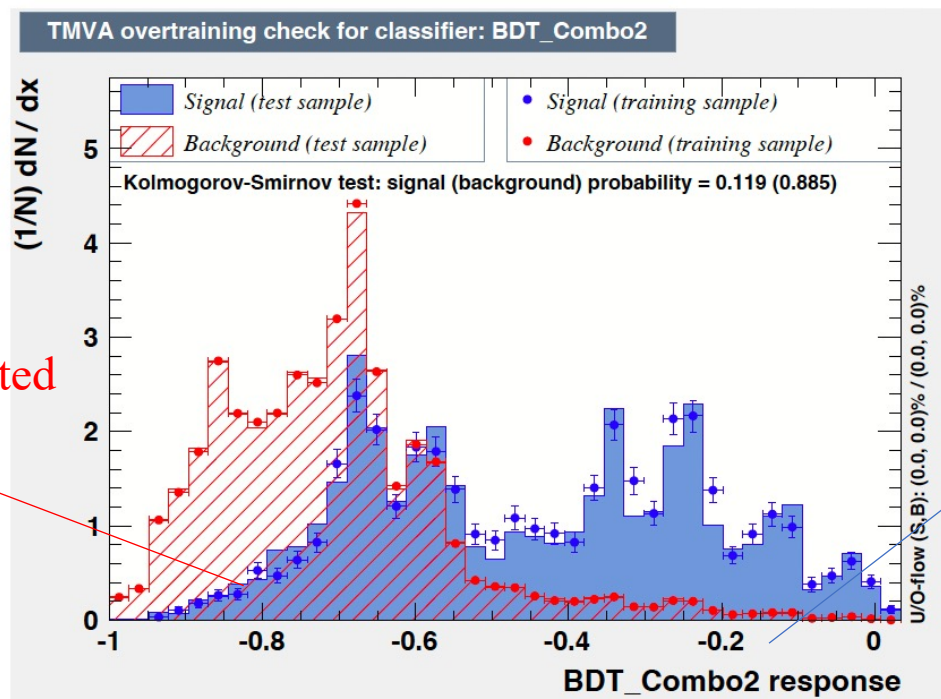
PV tracks wrongly associated as signal

Other B tracks wrongly associated as signal



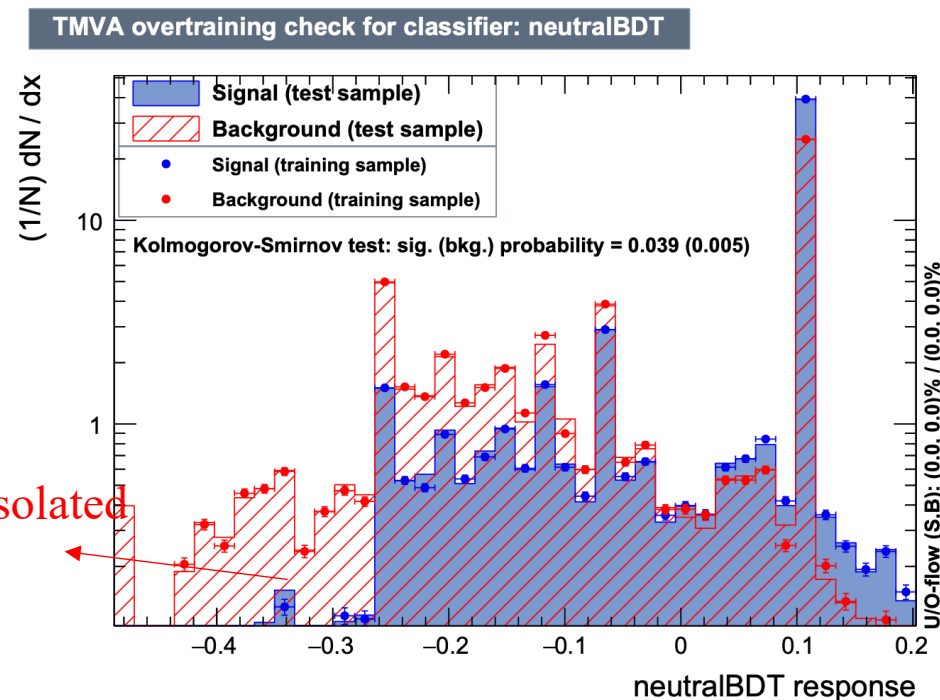
Charged and neutral isolation

Charge isolation techniques (e.g. $B \rightarrow D^+ \tau \nu$)



(d) IsoBDT_Combo2

Neutral isolation techniques (e.g. $B \rightarrow D^+ \tau \nu$ [analysis](#))

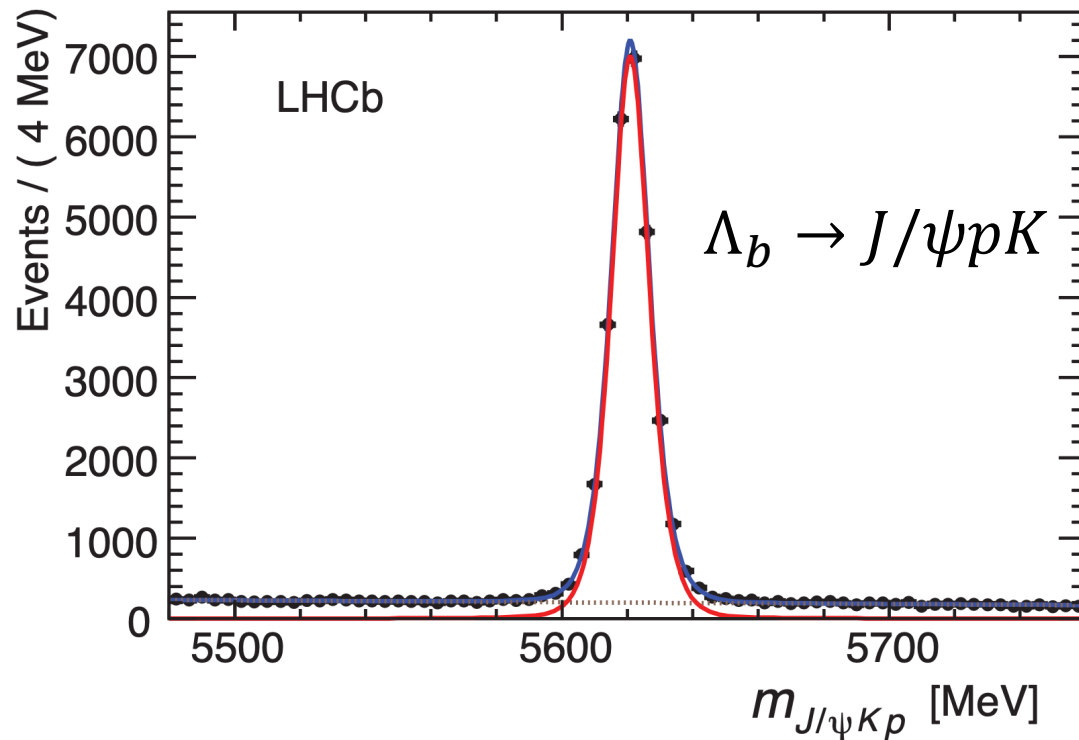


Reversing the cuts help define background enriched control regions!

MisID: Importance of PID at LHCb

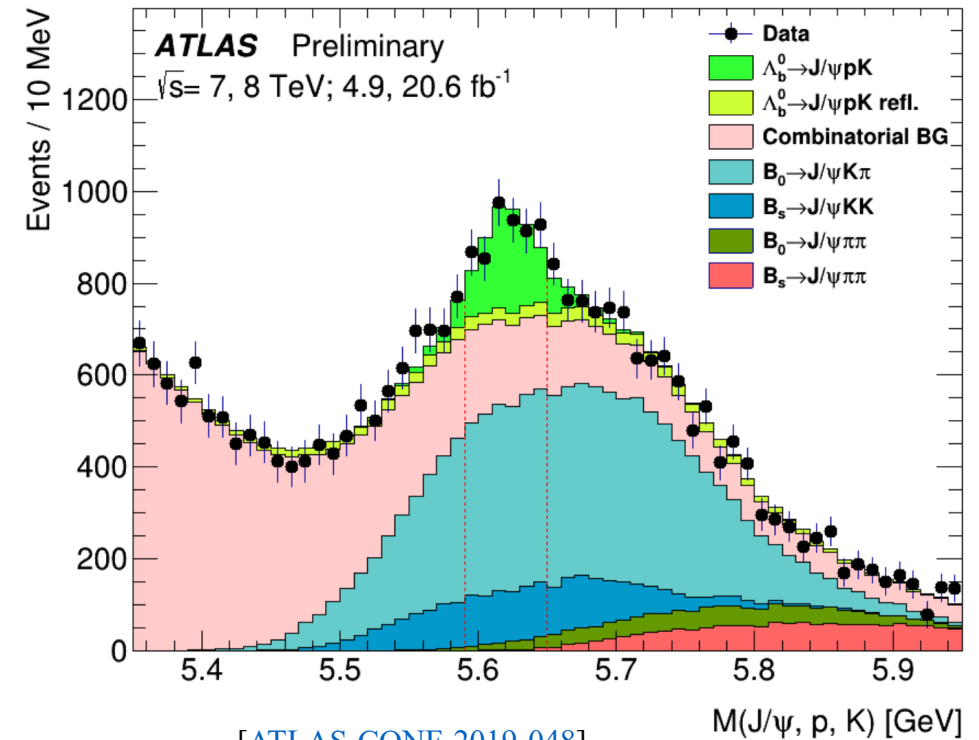
For more see Tim G's [talk](#)

LHCb pentaquark analysis



[[Phys. Rev. Lett. 115, 072001 \(2015\)](#)]

ATLAS pentaquark analysis

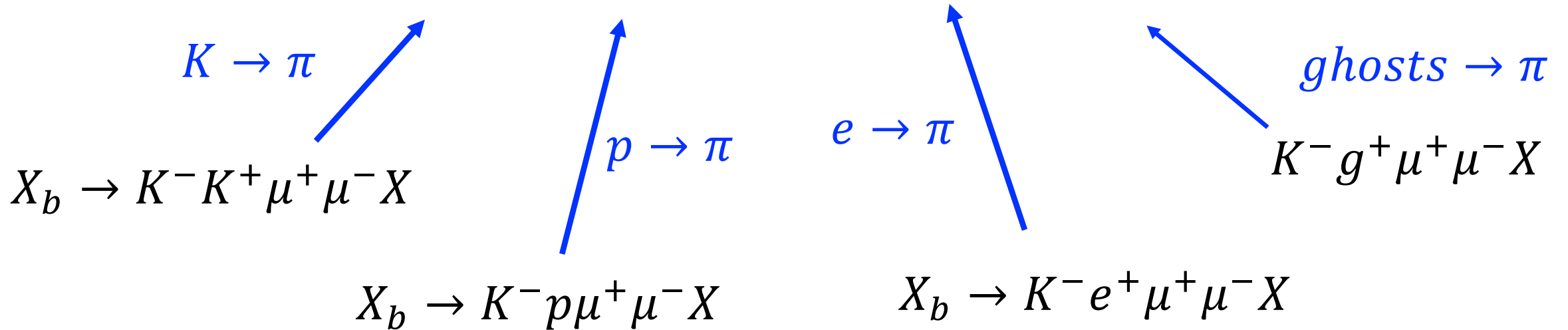


[[ATLAS-CONF-2019-048](#)]

MisID in missing energy decays

Large number of channels can be **misidentified** as signal.

Signal: $B^0 \rightarrow K^- \pi^+ \tau^+ (\rightarrow \mu^+ X) \tau^- (\rightarrow \mu^- X)$

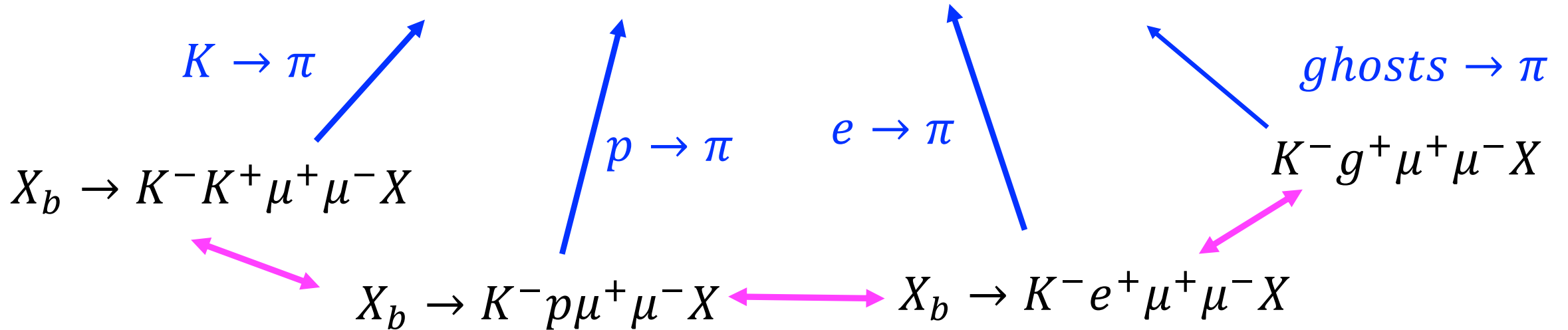


MisID in missing energy decays

Large number of channels can be **misidentified** as signal.

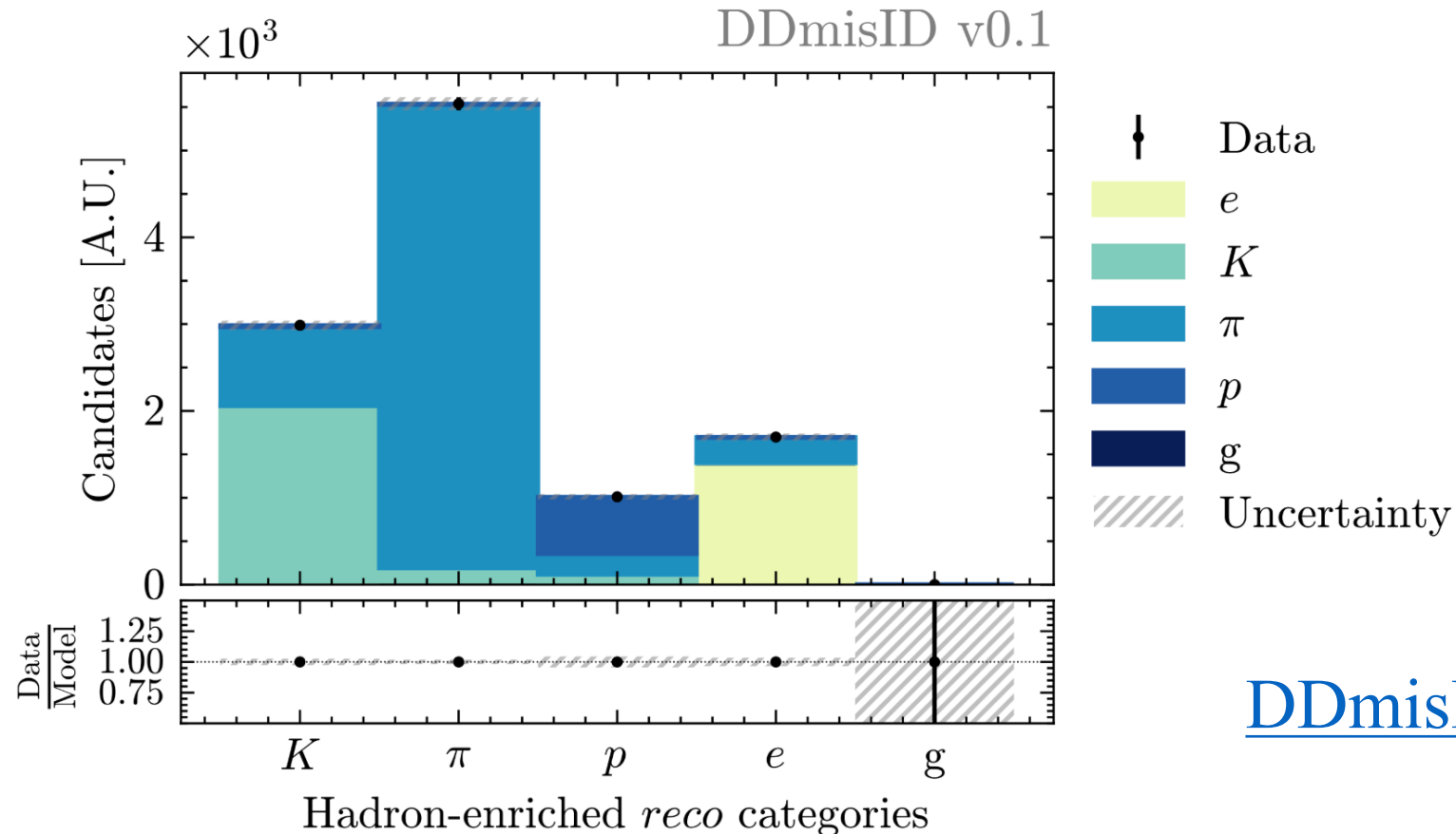
There could be **cross-contamination** between them.

Signal: $B^0 \rightarrow K^- \pi^+ \tau^+ (\rightarrow \mu^+ X) \tau^- (\rightarrow \mu^- X)$



MisID in missing energy decays

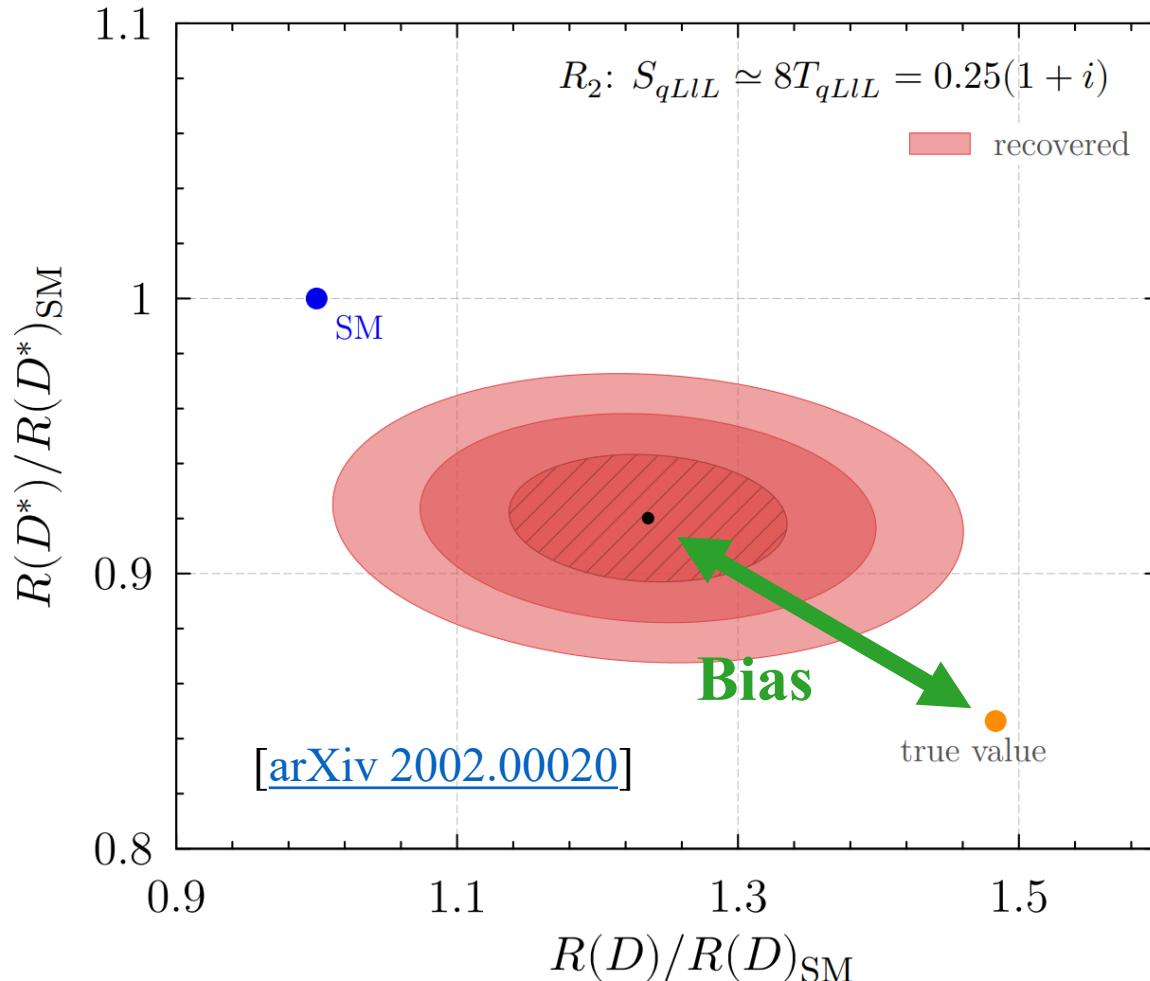
Define mis-ID enriched control regions and obtaining yield and shape from data.
Sophisticated folding/unfolding techniques (e.g. $B^0 \rightarrow D^+ \tau \nu$ analysis)



[DDmisID](#) package

Missing Energy: Model dependence

No variable that is fully independent of the signal model.



If data has NP and we fit with SM templates this leads to a bias. Not good for global fits!

How to solve the model dependence?

Correct thing to do is at **each fit iteration**:

Generate MC
according to model



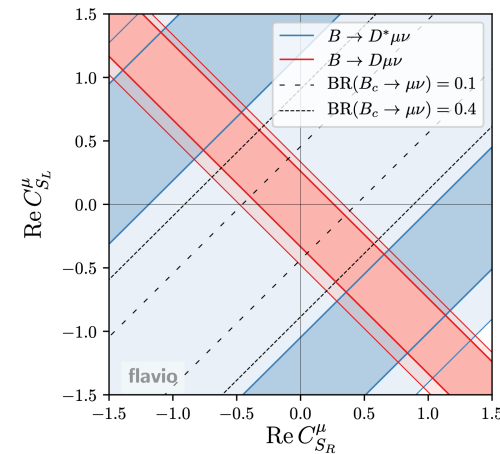
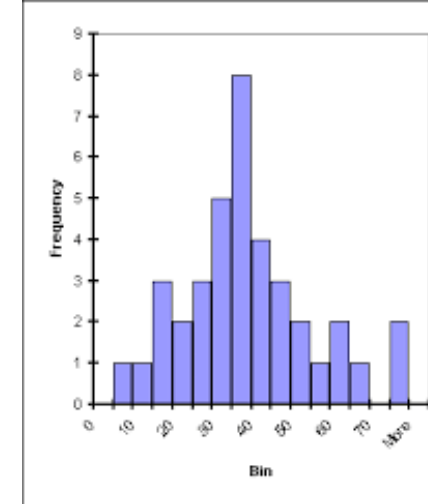
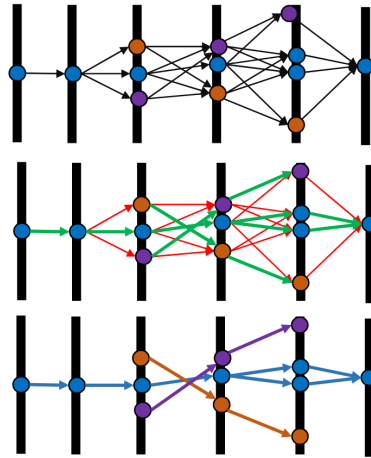
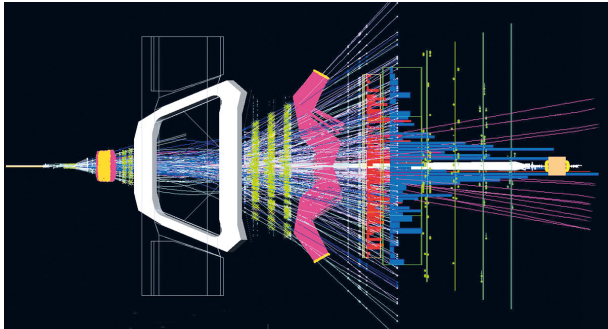
Reconstruct and
apply selection



Model signal/bkg
template



Extract
parameters



This is not pragmatic!

How to solve the model dependence?

Assume reconstruction and selection are not heavily model dependent



Techniques developed:

- RoHammerModel (see [paper](#))
- [ReDist](#) + [EOS](#) (See [paper](#))
- **ReDist + HAMMER**

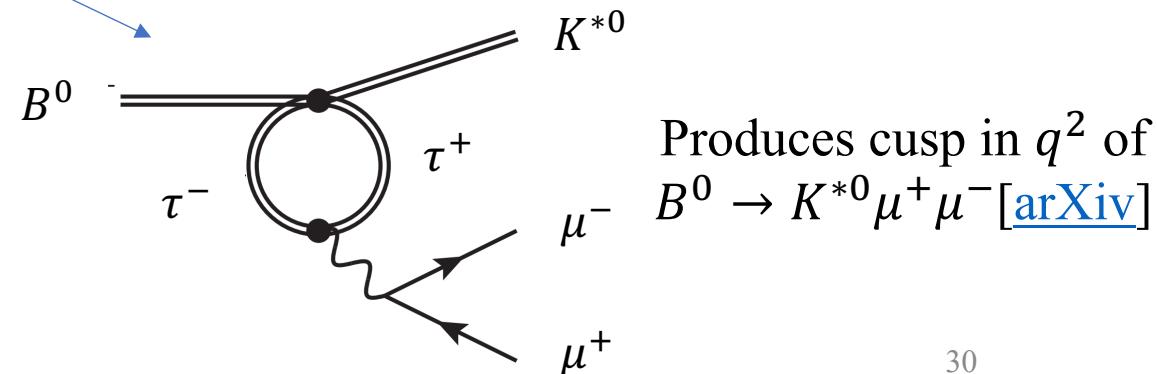
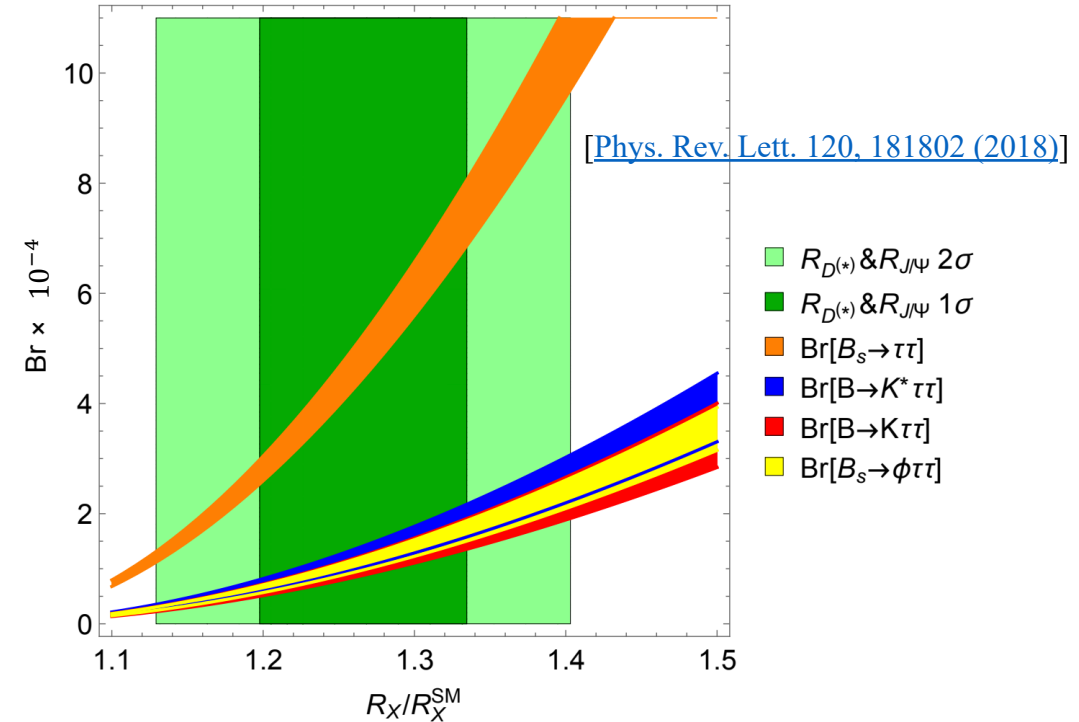
(Prospects for LHCb + Belle II combination, paper soon)

At each fit iteration, reweight truth information to a different NP model

A green box containing text, with two green arrows forming a loop between the 'Model signal/bkg template' and 'Extract parameters' boxes in the flowchart above.

Searches for $B^0 \rightarrow K^+ \pi^- \tau^+ \tau^-$ and $B_s^0 \rightarrow K^+ K^- \tau^+ \tau^-$

- BF of these channels $O(10^{-7})$.
- BSM models explaining $R(D^*)$ can enhance them by $O(100)$.
- [Previously Belle-II](#): $BF(B^0 \rightarrow K^{*0} \tau^+ \tau^-) < 1.8 \times 10^{-3}$ (90% CL)
- [Previously LHCb](#): Indirect Wilson coefficient $C_9^{\tau\tau} < 600$ (95% CL).
- Can we improve with Run 2 data (2016-2018)?

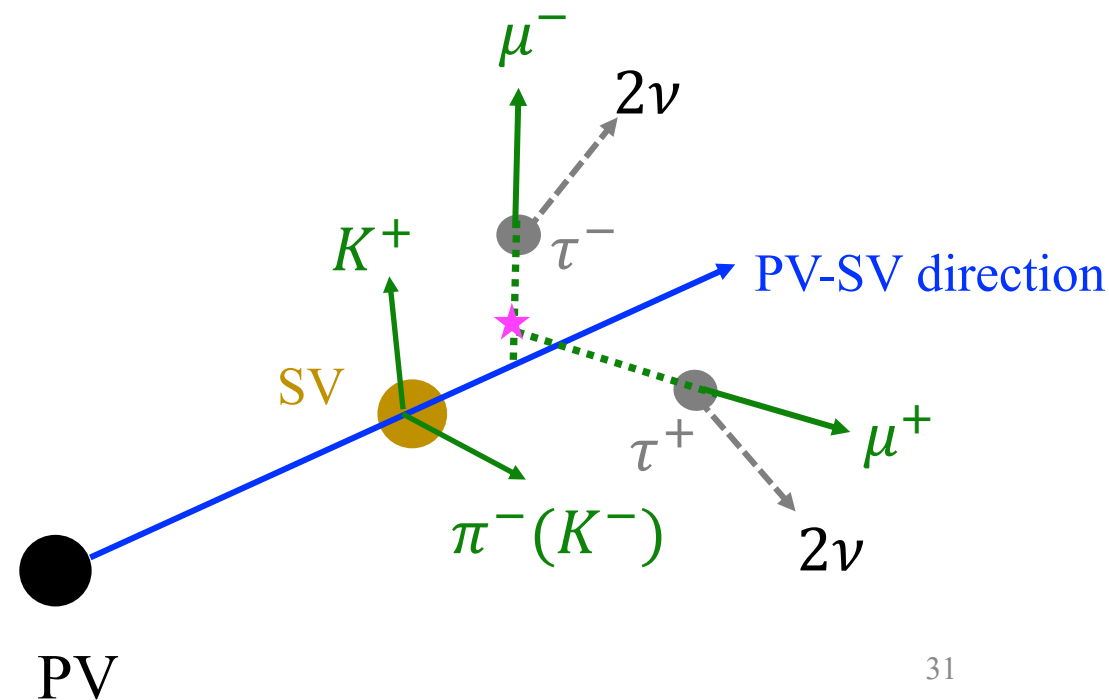


Topology and bins in di-hadron mass spectra

[LHCb-PAPER-2025-048]

- Search carried out in bins of $m(h^+ h^-)$ spectra taking resonant (e.g. $K^*(892)$, $\phi(1020)$) into account.
- Large PV-SV distance $\rightarrow$ beats combinatorial bkg.
- Muon **intersection** downstream of SV $\rightarrow$ beats $b \rightarrow s \mu^+ \mu^-$ bkg.

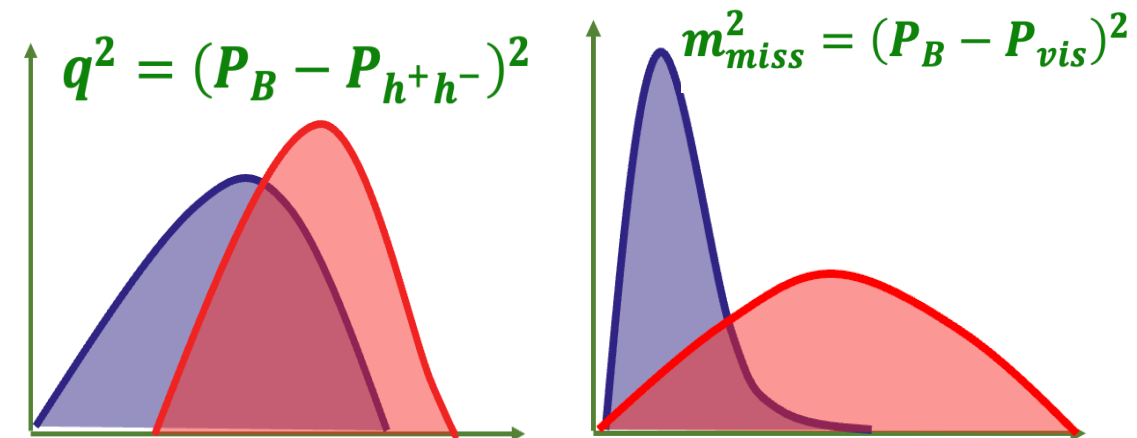
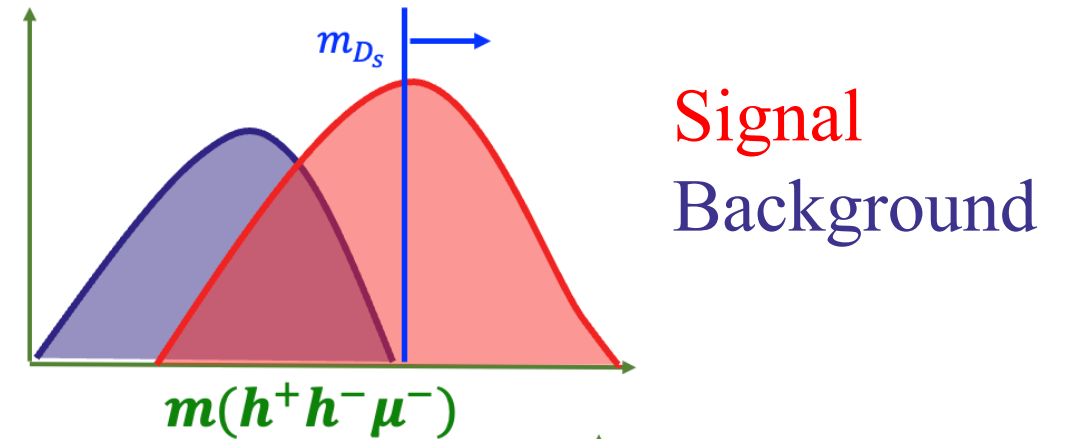
Mass range (MeV/ c^2)	Mass range (MeV/ c^2)
$792 \leq m_{K^+\pi^-} < 992$	$980 \leq m_{K^+K^-} < 1060$
$992 \leq m_{K^+\pi^-} < 1330$	$1060 \leq m_{K^+K^-} < 1200$
$1330 \leq m_{K^+\pi^-} < 1530$	$1200 \leq m_{K^+K^-} < 1400$
$1530 \leq m_{K^+\pi^-} < 1726$	$1400 \leq m_{K^+K^-} < 1600$
–	$1600 \leq m_{K^+K^-} < 1813$



Background rejection

[LHCb-PAPER-2025-048]

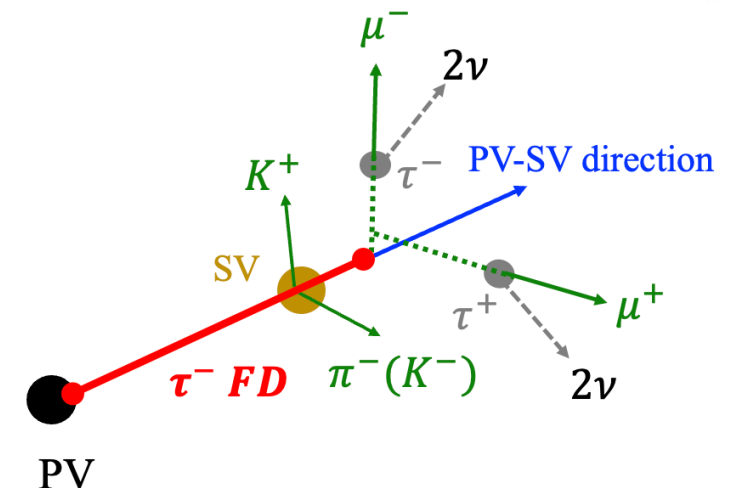
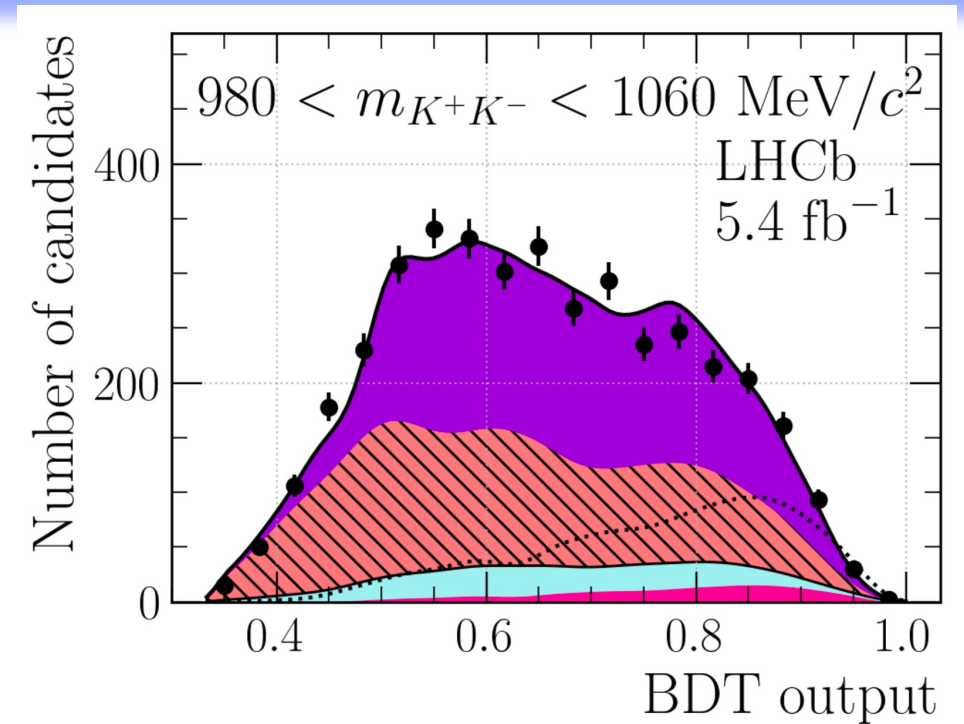
- Bkg $B \rightarrow D_s(\rightarrow h^+ h^- \mu^+ \nu) \mu^- \nu$ removed with $m(h^+ h^- \mu^+) > m_{D_s}$.
 - Halves the eff. but larger bkg. rej.
- Bkg $B \rightarrow D\bar{D}h^+h^-$ with each SL D decaying, apply 2D cut:
 - q^2 (used rest frame approximation)
 - m_{miss}^2 as signal has more missing particles.
- Feed down from higher K^* negligible.



BDT training

[LHCb-PAPER-2025-048]

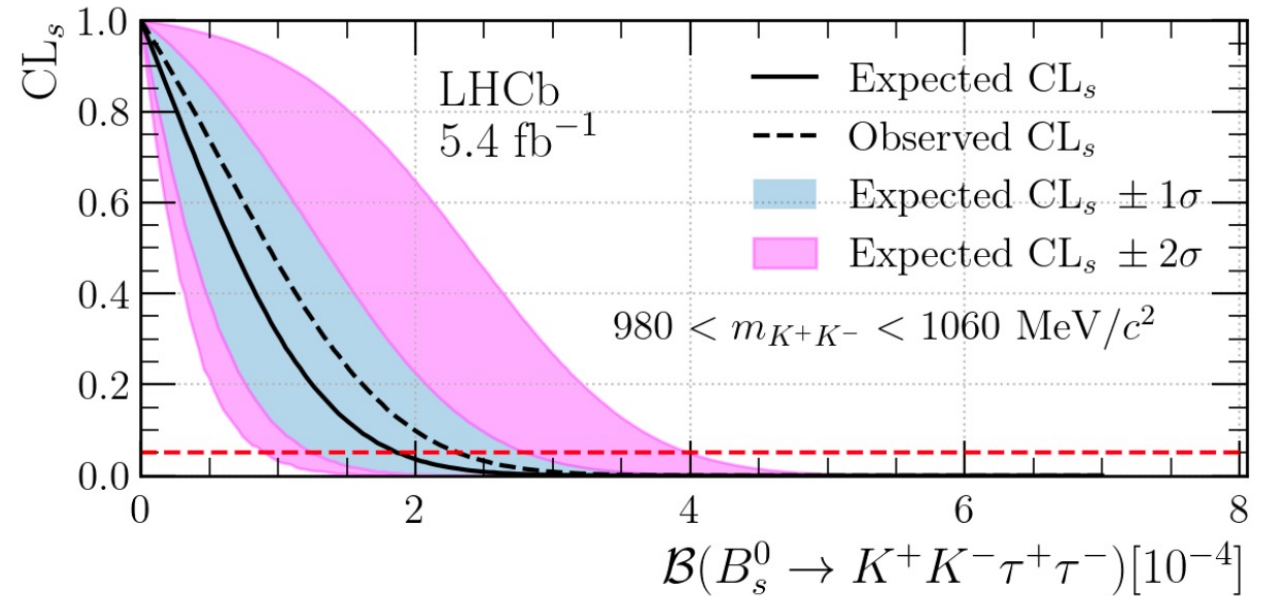
- Three-class BDT: **Combinatorial bkg.**, **Semileptonic $B \rightarrow D^0(\rightarrow h^- \mu^+ X) h^+ \mu^- X$** and **signal**.
- BDT features: $\tau^\pm$ FD and isolation vars.
- Candidate with highest BDT for the signal category retained and fitted.
- **MisID**: Four control regions used for yield and shape determination.
- **SL bkg** & **signal** modelled using MC, **comb. bkg.** via data (same muon sign).



Results

[LHCb-PAPER-2025-048]

- Normalisation channels: $B^0 \rightarrow J/\psi K^*$ and $B_s^0 \rightarrow J/\psi \phi$.
- Limits obtained in all bins of $m(K^+ K^-)$ and $m(K^+ \pi^-)$.
- **Dominant systematics: Modelling of the bkg shapes.**



$$\mathcal{B}(B^0 \rightarrow K^{*0} \tau^+ \tau^-) < 2.8 \times 10^{-4} \quad (2.5 \times 10^{-4}) \text{ at 95\% (90\%) CL,}$$

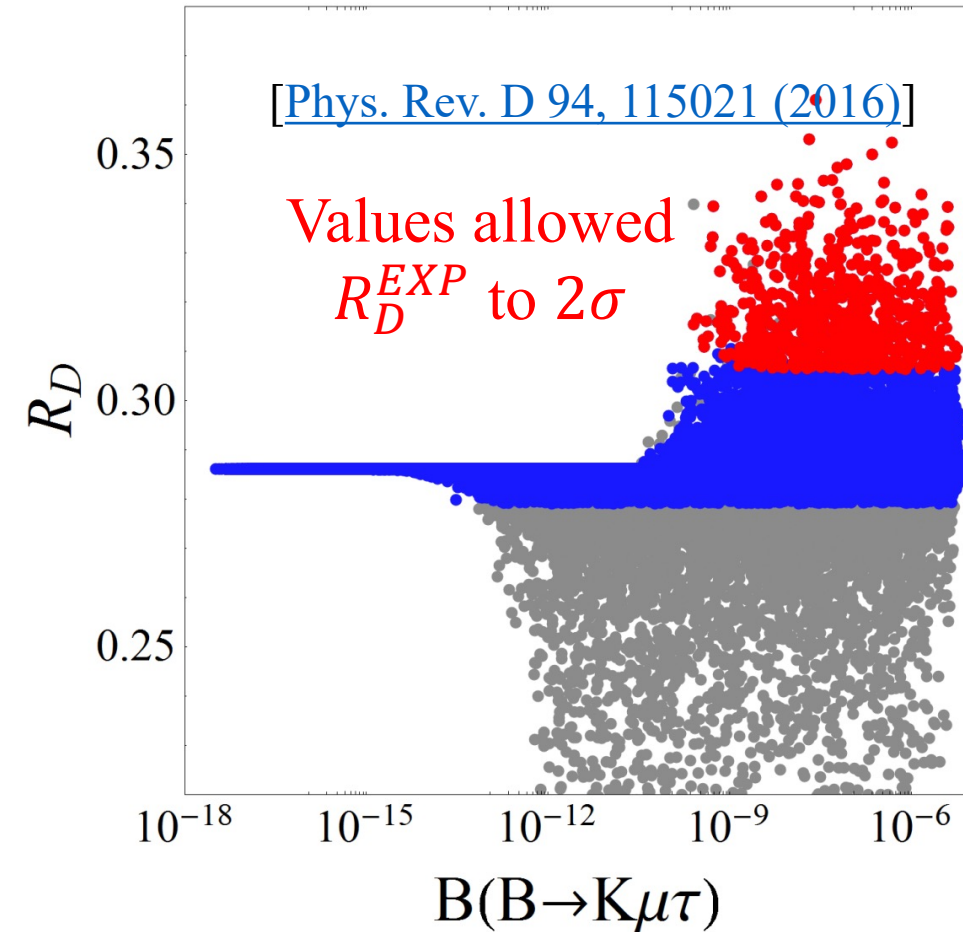
$$\mathcal{B}(B_s^0 \rightarrow \phi \tau^+ \tau^-) < 4.7 \times 10^{-4} \quad (4.1 \times 10^{-4}) \text{ at 95\% (90\%) CL.}$$

Limit 10x better than Belle-II!

Limits 3x better on $|C_9^{\tau\tau}|$ than prev. LHCb limit.

Search for Lepton Flavour Violation (LFV) in $B^0 \rightarrow K^{*0} \tau^\pm e^\mp$

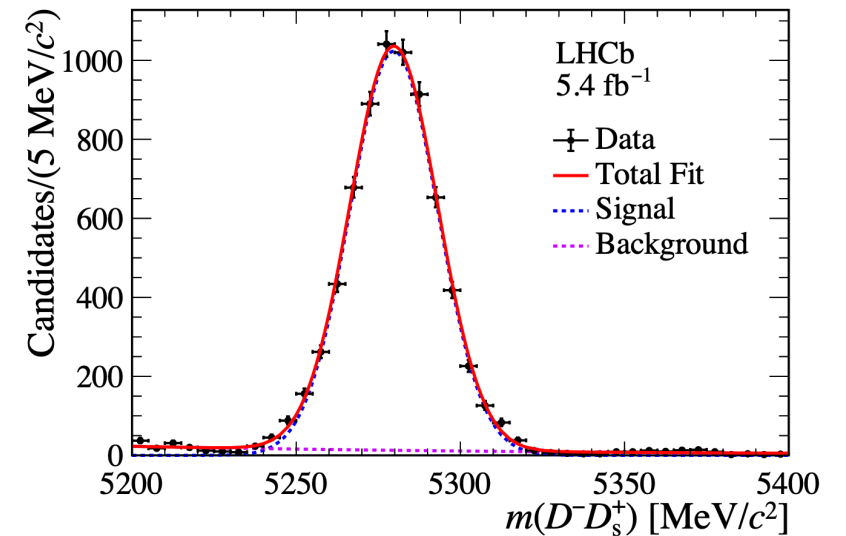
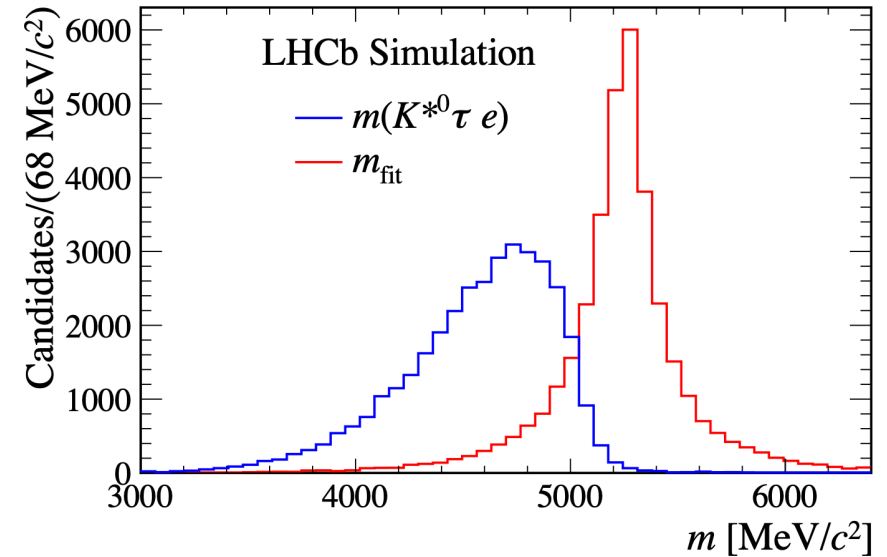
- Even with neutral LFV in SM, charged LFV (cLFV) highly suppressed $O(10^{-50})$.
- NP models of $R(D^*)$ can enhance them.
- Most stringent τe coupling [Belle](#):
 $BF(B^+ \rightarrow K^+ \tau e) < 1.5 \times 10^{-5}$ @ 90% CL.
- First τe probe by LHCb with Run 2 data ($\sim 5.4 fb^{-1}$).
- Both $\tau^+ e^-$ & $\tau^- e^+$ samples analyzed independently, with hadronic τ decay.



Event selection

[[LHCb-PAPER-2025-048](#)]

- Use vertex and mass constraints to reconstruct full decay chain.
- Normalisation: $B^0 \rightarrow D^-(\rightarrow K\pi\pi) D_s(\rightarrow KK\pi)$.
- **Event selection:**
 - Multiple L0 triggers to offset low e^- L0 eff.
 - MVA to reject comb. bkg, partially reco., and mis-ID charm bkg.
 - Optimized PID selection.
 - D-meson vetoes to suppress physics backgrounds.

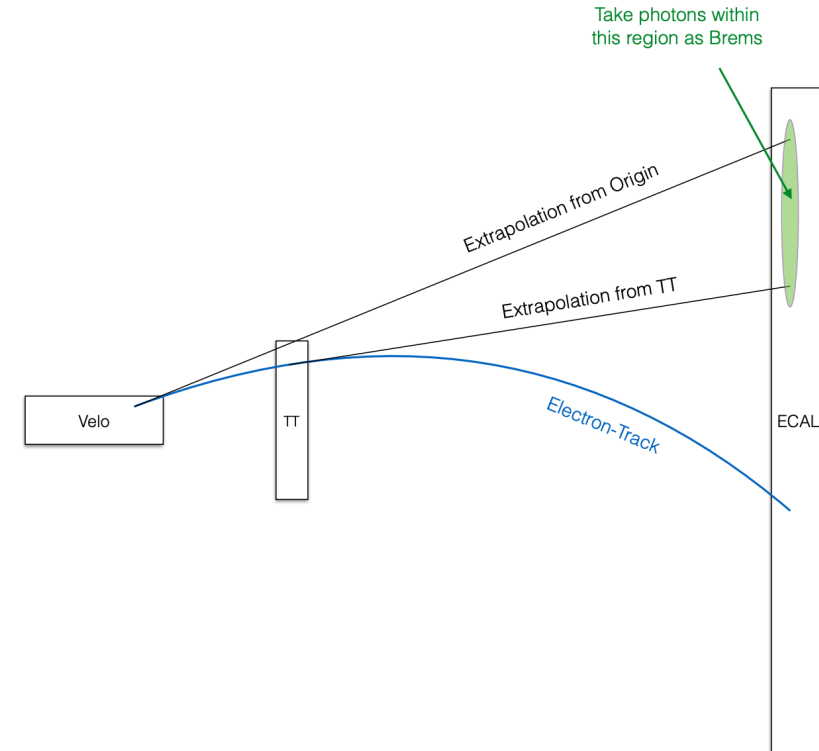
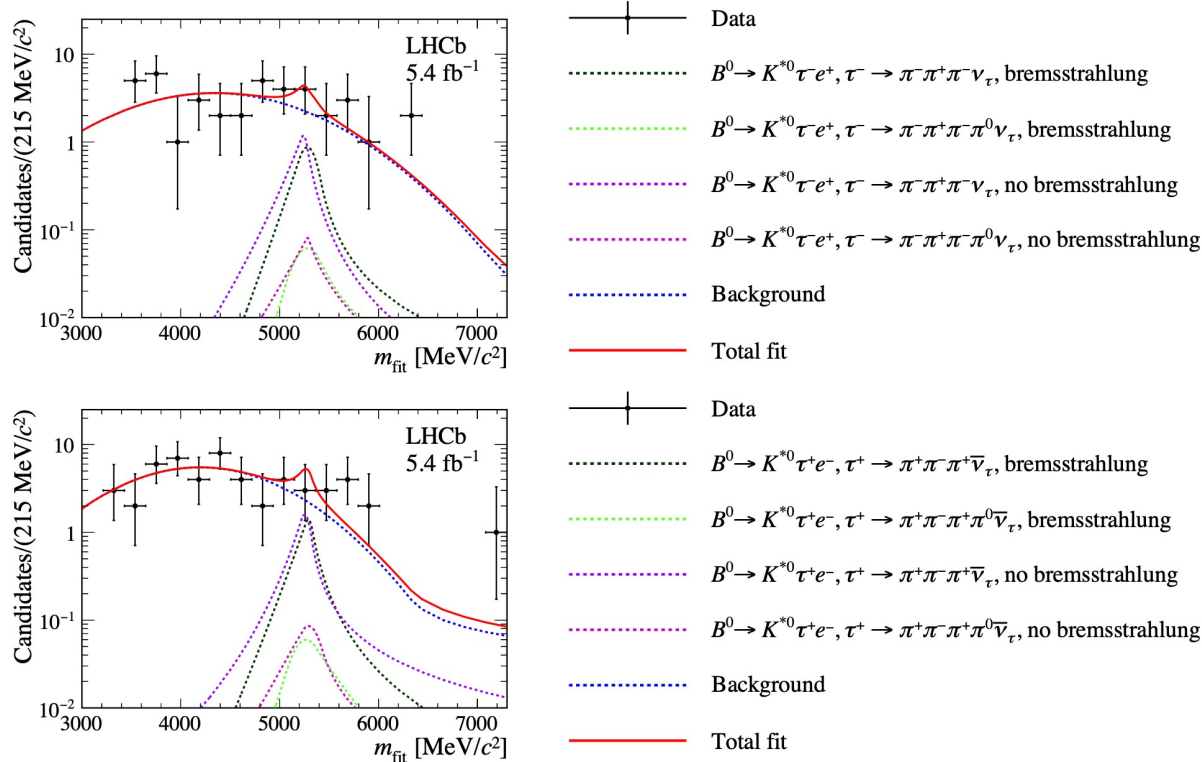


Backgrounds and fit

[[LHCb-PAPER-2025-048](#)]

- Main backgrounds: combinatorial and $b \rightarrow cl\nu$ decays.
- Electrons with and without bremsstrahlung considered.

$$B^0 \rightarrow K^{*0} \tau^- e^+$$



$$B^0 \rightarrow K^{*0} \tau^+ e^-$$

Results

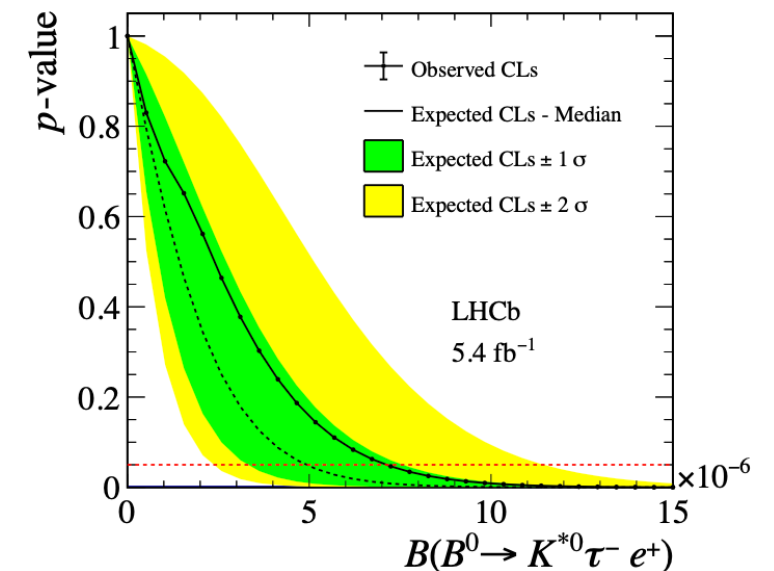
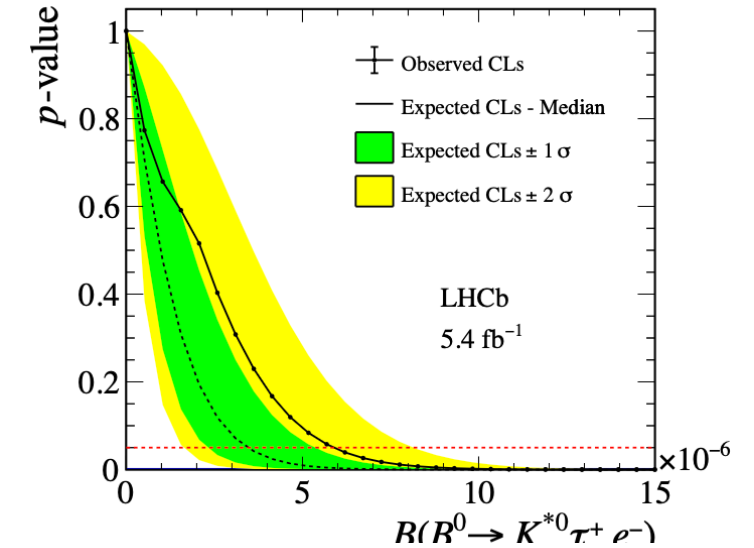
[LHCb-PAPER-2025-048]

- **Most stringent limits to date on $b \rightarrow s\tau l$.**
- Upper limits on NP scenarios: accounting for variation selection efficiency.

Model	Upper limit [10^{-6}]	
	$B^0 \rightarrow K^{*0} \tau^- e^+$	$B^0 \rightarrow K^{*0} \tau^+ e^-$
Phase space (PHSP)	5.9 (7.1)	4.9 (5.9)
Left-handed ($C_9^{\tau e} = -C_{10}^{\tau e} \neq 0$)	6.3 (7.7)	5.4 (6.4)
Scalar ($C_S^{\tau e} \neq 0$)	6.6 (8.0)	5.7 (6.8)

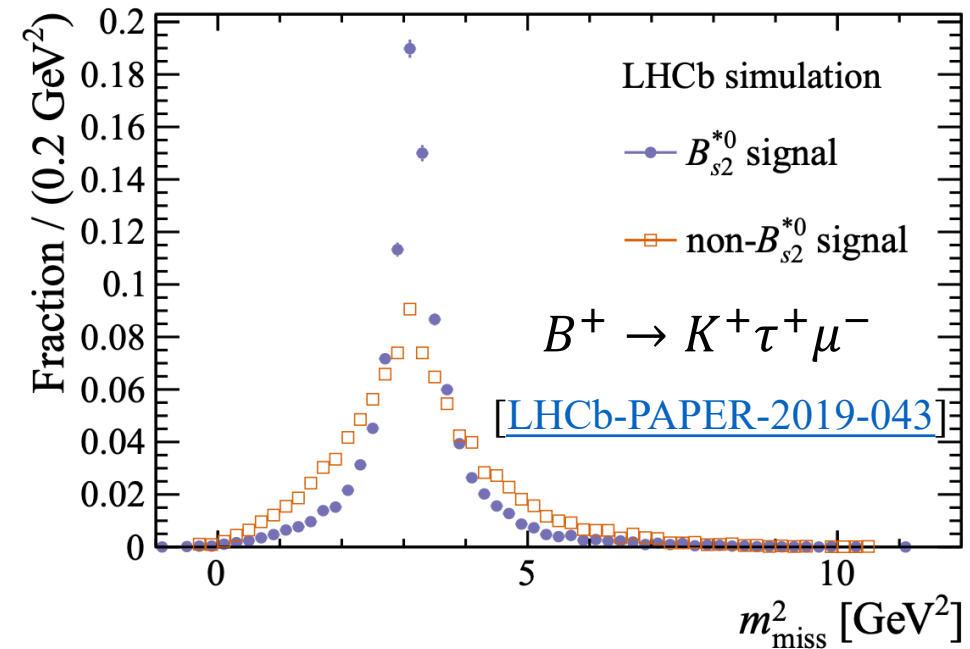
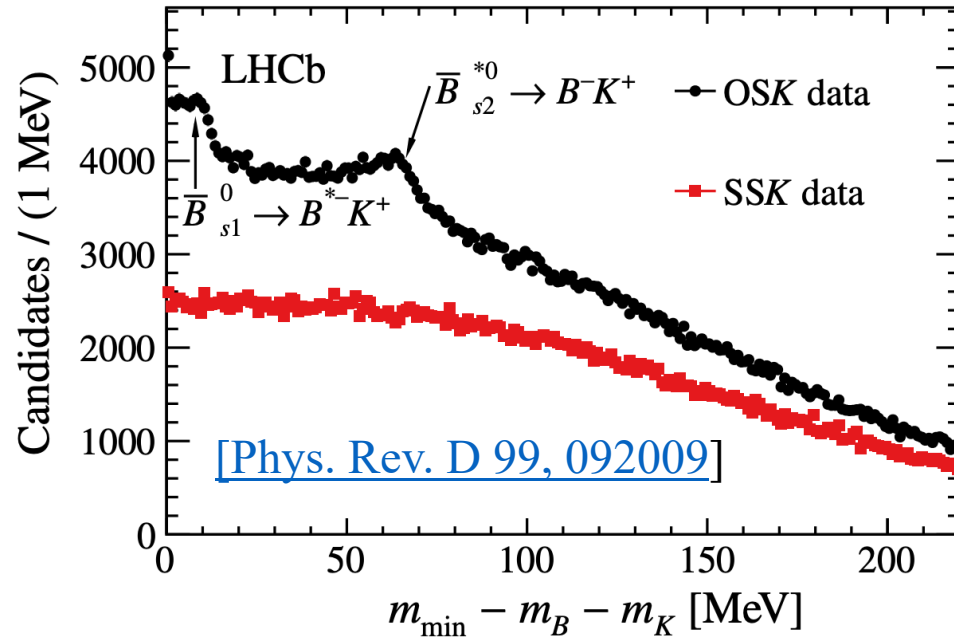
90 (95) % CL

Systematic effect	Upper limit increase [%]	
	$B^0 \rightarrow K^{*0} \tau^+ e^-$	$B^0 \rightarrow K^{*0} \tau^- e^+$
Input branching fractions	2.3	2.5
Normalisation yields	<0.1	<0.1
Efficiencies	1.2	1.0
Background model	4.7	5.2
Signal model	1.2	0.5
Total	9.7	9.5



Other tricks with missing energy decays at LHCb

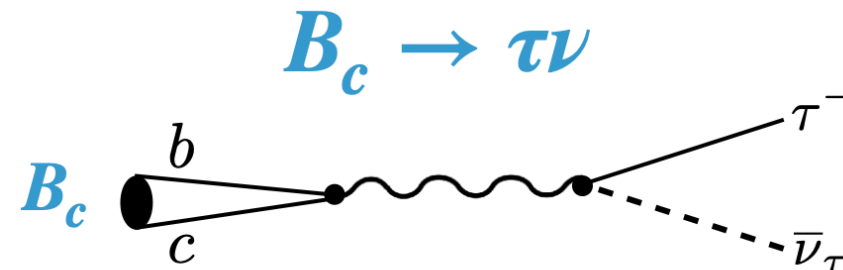
Exploit the fact that B_{s2}^* is narrow and decays to $B_{s2}^* \rightarrow B^- K^+$ to constrain the missing momentum.



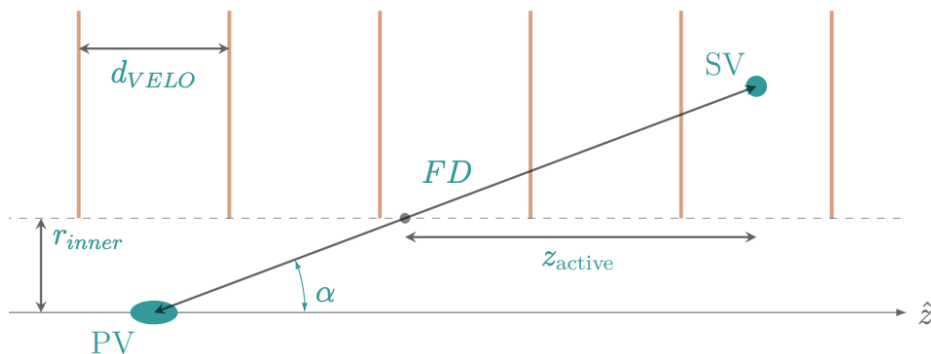
Used in BF analysis of $B^- \rightarrow D^{*,**,0} \mu^- \nu$ and LFV in $B^+ \rightarrow K^+ \tau^+ \mu^-$.

FCC-ee decays @ LHCb?

Probe $B_c^- \rightarrow \tau^- \nu$ @ LHCb?
A clean probe of NP in $b \rightarrow c \tau \nu$

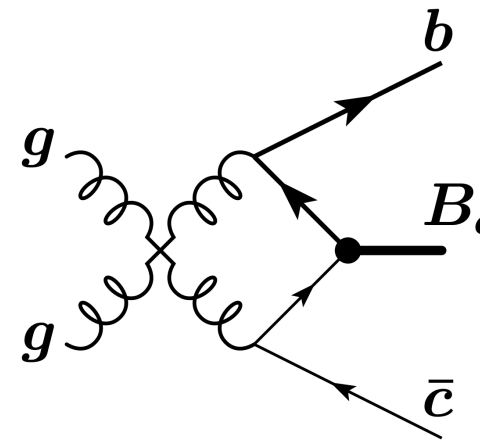


Idea I: Exploit B_c^+ hits in VELO



[[Master's Thesis](#)]

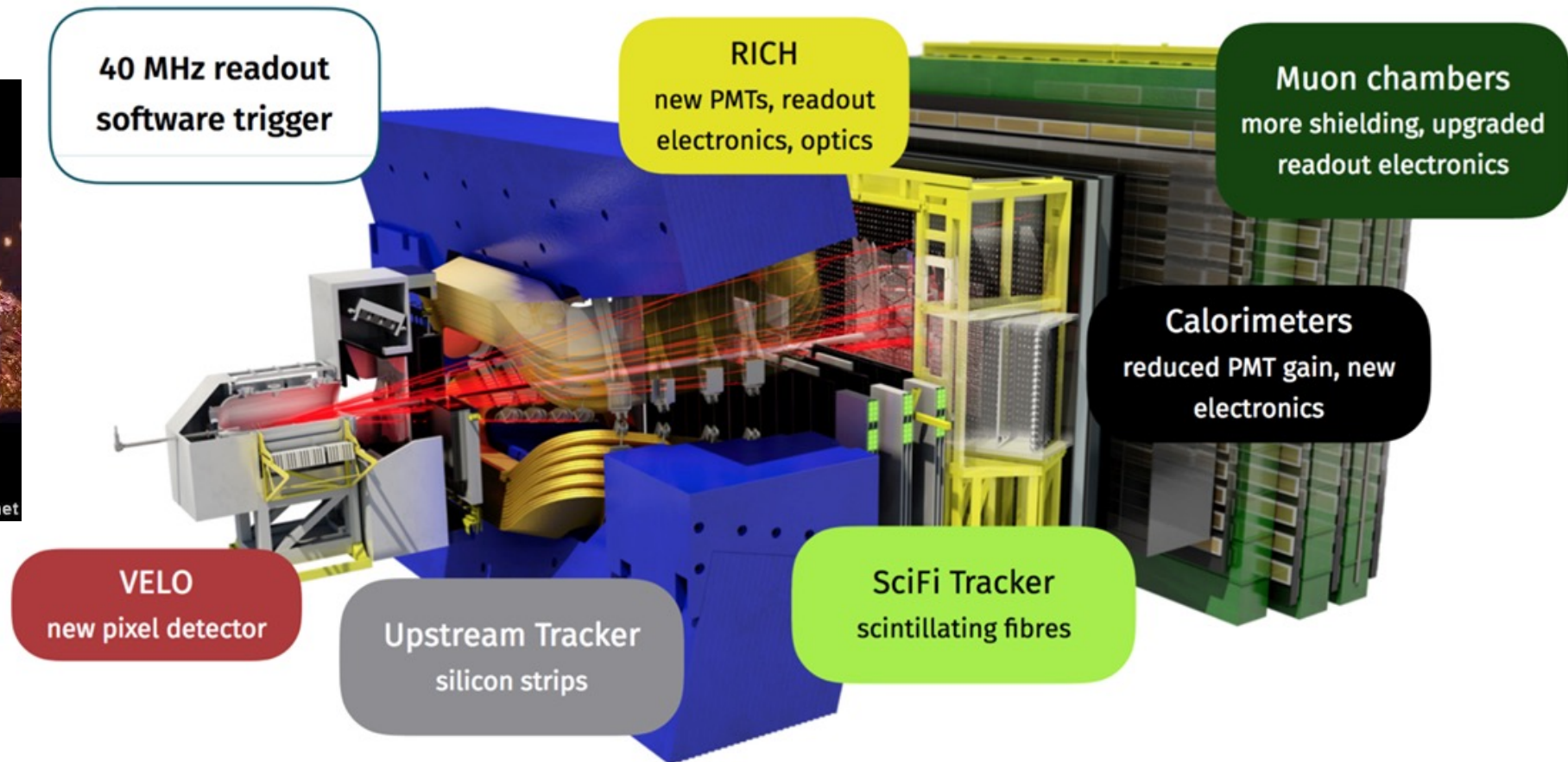
Idea II: Exploit Bc-D associated production



Production property measurement
ongoing...

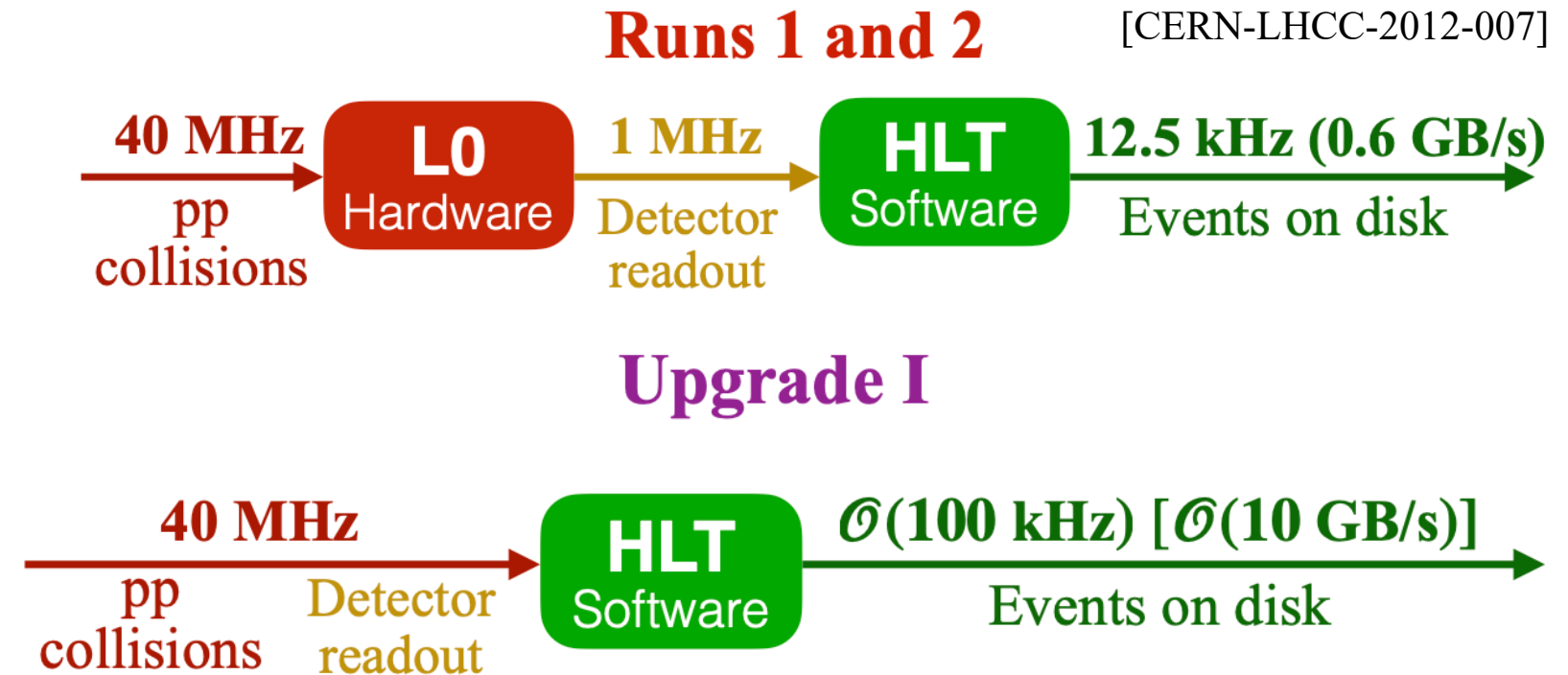
Brand new detector for Run 3

Luminosity increased by a factor 5. New tracking system: VELO, UT, SciFi



Brand new software for Run 3

For more Manuel's [talk](#)



First hadron detector with no hardware trigger!

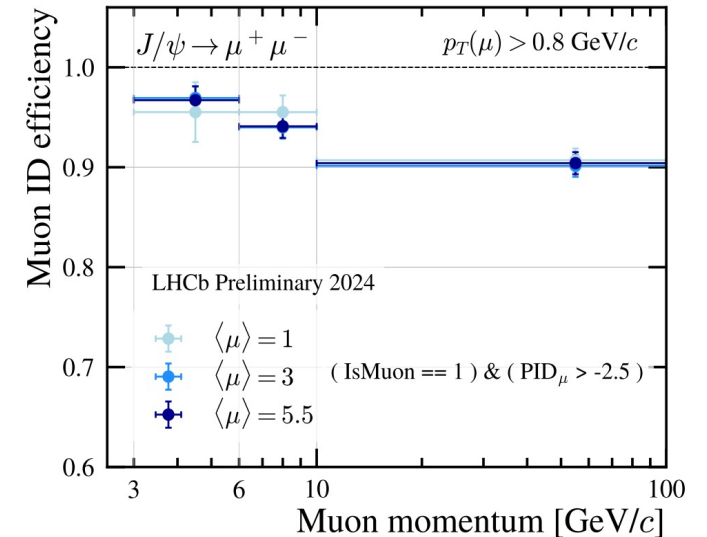
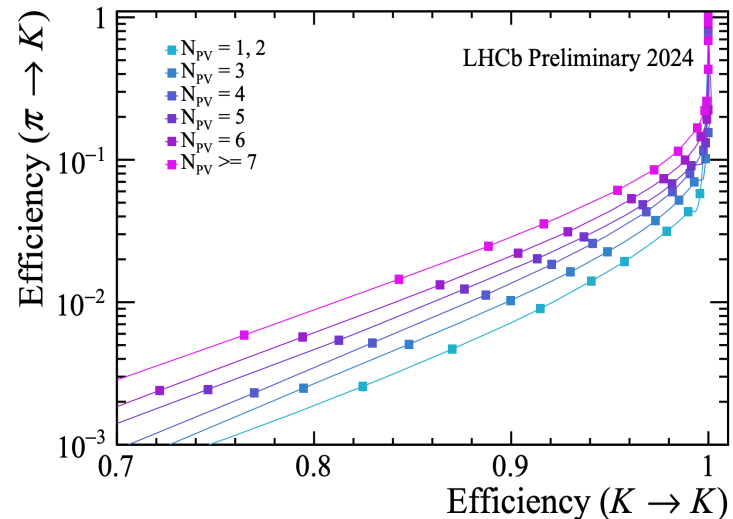
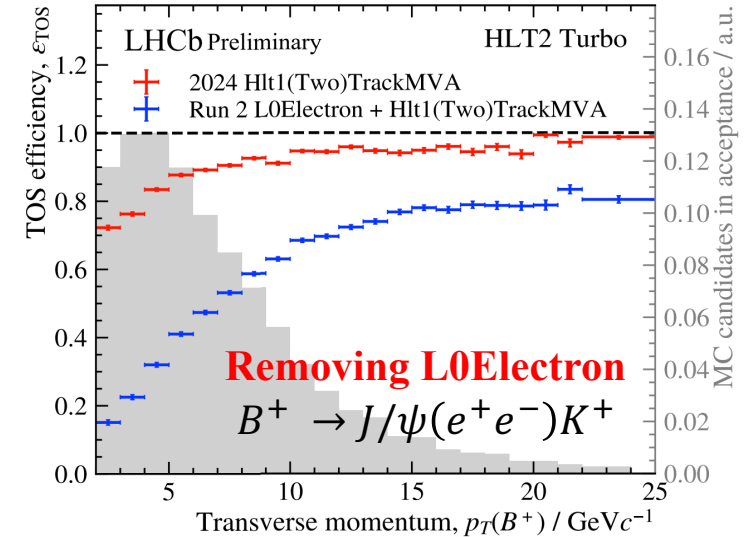
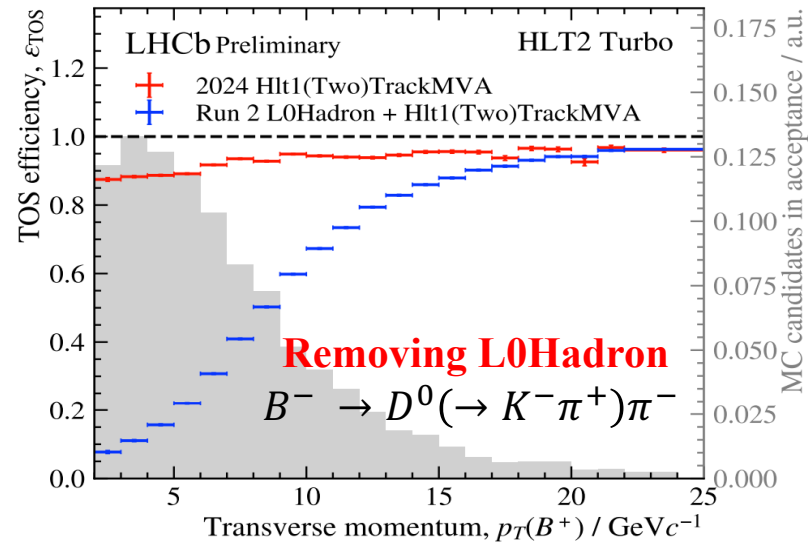
Run 3 Performance and new physics results

**Much higher efficiency
for “soft” B decays!**

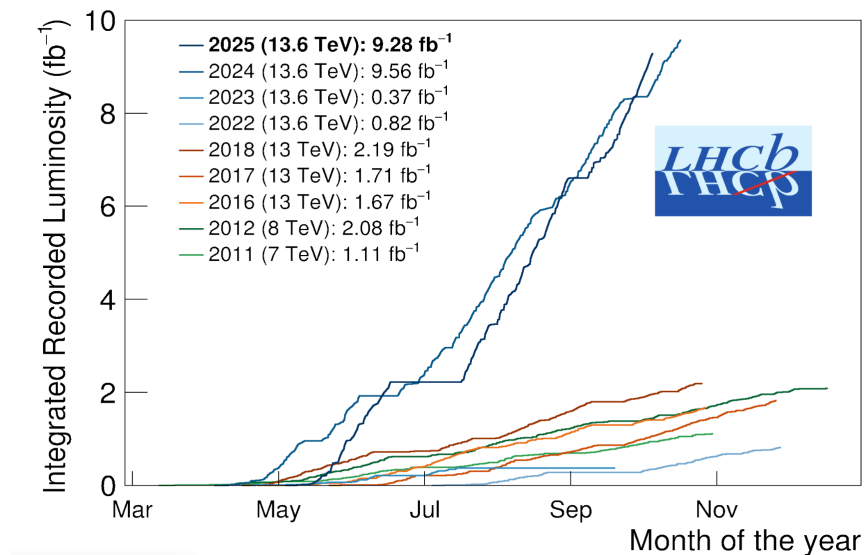
**Particle ID performing
well in harsher Run 3
environment!**

**Two charm physics
results: Production asym.
and $A_{CP}(D^0 \rightarrow K_S K_S)$**

**[[LHCb-PAPER-2024-052](#),
[CERN Seminar](#)]**



Incredible Run 3 data taking!



More than 20 fb^{-1} Run 3 pp data collected.
More than twice that Run 1-2 (pp)!

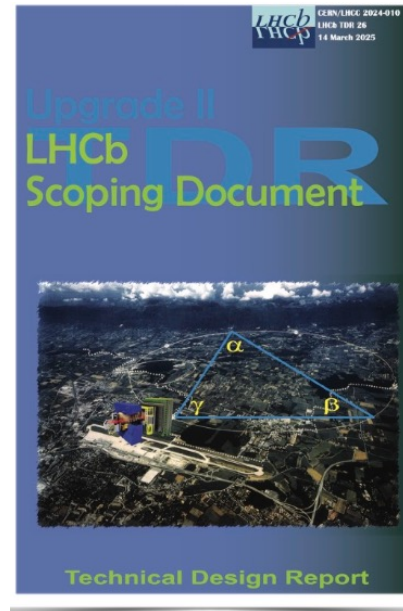
More to collect in 2026...



LHCb Future (Upgrade II)



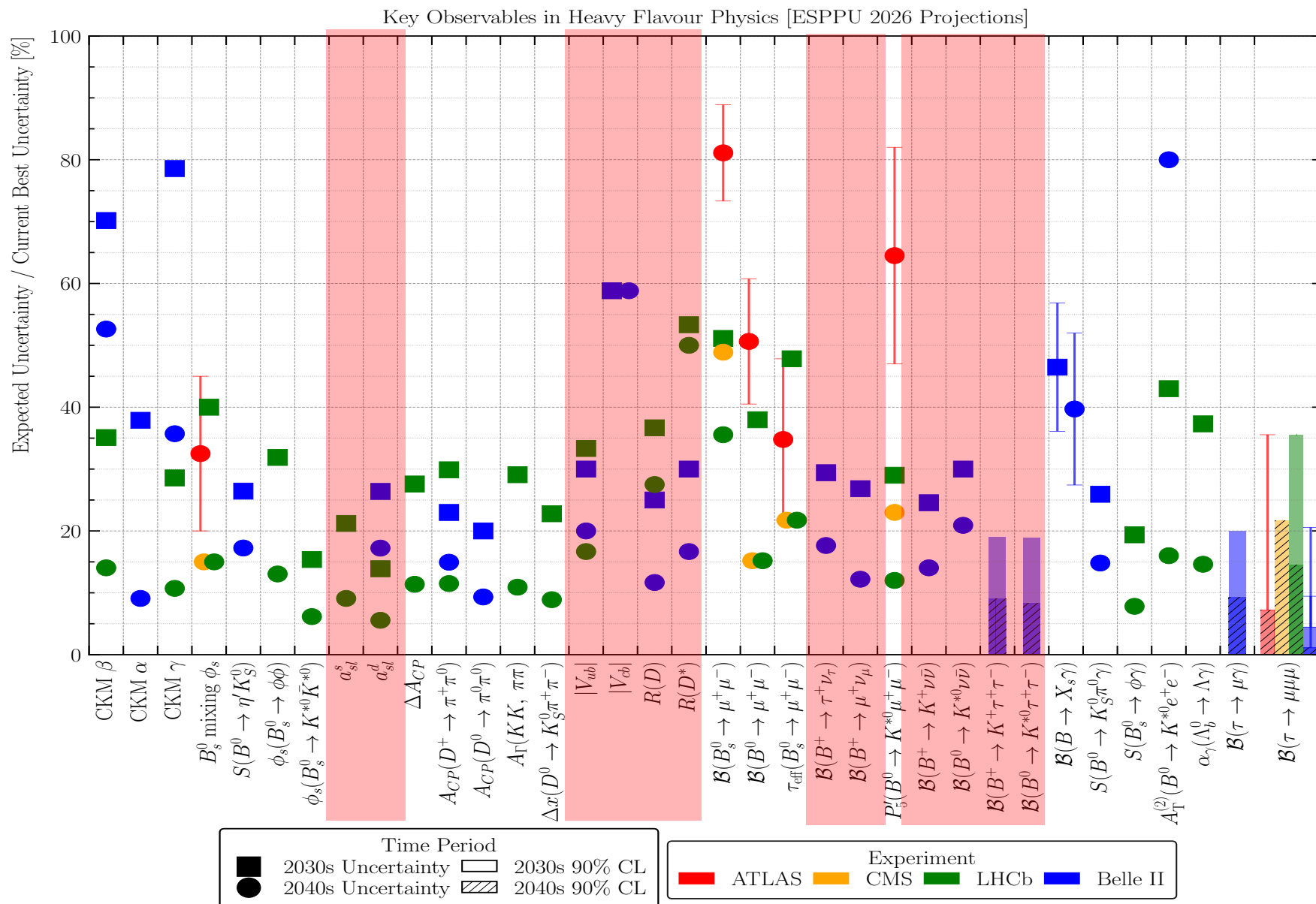
- bridge to future accelerators
- Starting R&D phase of new technologies
 - precision timing for tracking and PID
 - extreme radiation hardness
 - low-cost monolithic pixels
 - cryogenic cooling (for SiPMs)



Endorsed by CERN Research board (April 2025)!

Towards the TDR in one year!

Future of missing energy decays



LHCb will strive to deliver competitive results to Belle II's missing-energy programme well into the 2040s.

Conclusions

Best experiment (for missing-energy decays)?



For a dynamic heavy-flavour programme,
LHCb needs Belle II and Belle II needs LHCb.

ありがとうございました

Back-up

Need for speed: Simulation

- Tree-level missing-energy decays are abundant → form background to rare modes.
 - Need equally large simulated samples.
 - **Data vs. MC**
 - Signal $B \rightarrow D^* \tau \nu$: once every 1.7×10^7 bunch crossings (or every 0.6 s at LHC).
 - Simulation: ~ 1 min per event → 1M events $\approx$ **2 years** (sequential, but in really production parallel).
- **Fast simulation is essential!**

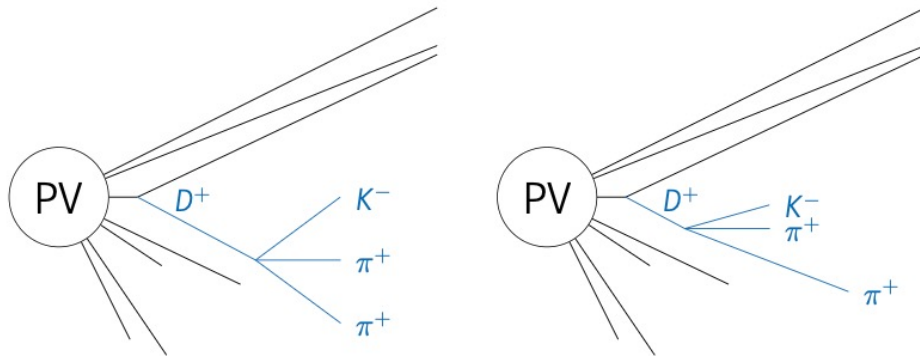


Need for speed: Simulation

Redecay

Reuse underlying event for different decays.

[arXiv:1810.10362](https://arxiv.org/abs/1810.10362)

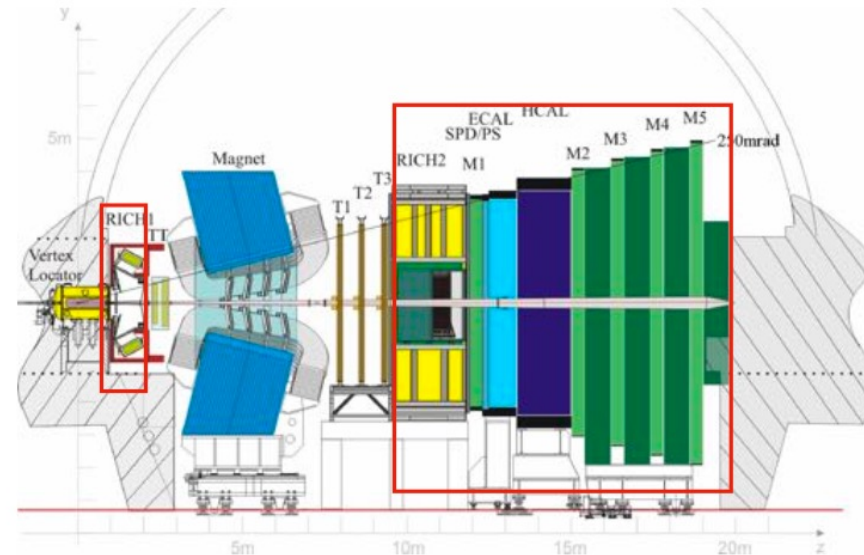


Speed up 10-100, same disk space.

Tracker only simulation

See Patrick O's [talk](#)

Turn off parts of the detector response (shower development, photon propagation in RICH).



Speed up by factor 8, disk space down by 40%

Systematics relative to statistical uncertainty

[LHCb-PAPER-2025-048]

Source of uncertainty	Percentage uncertainty for $\mathcal{B}(B^0 \rightarrow K^+ \pi^- \tau^+ \tau^-)$			
$m_{K^+ \pi^-}$ (MeV/ c^2)	[792, 992]	[992, 1330]	[1330, 1530]	[1530, 1726]
Combinatorial shape	74%	128%	125%	124%
Misidentified shape	39%	85%	78%	116%
Semileptonic shape	45%	42%	28%	19%
Signal shape	15%	12%	9%	11%
Reweighting	21%	11%	6%	4%
Known quantities	11%	5%	5%	4%
Efficiency	11%	4%	5%	4%

Source of uncertainty	Percentage uncertainty for $\mathcal{B}(B_s^0 \rightarrow K^+ K^- \tau^+ \tau^-)$				
$m_{K^+ K^-}$ (MeV/ c^2)	[980, 1060]	[1060, 1200]	[1200, 1400]	[1400, 1600]	[1600, 1813]
Combinatorial shape	111%	140%	160%	141%	175%
Misidentified shape	44%	33%	40%	44%	35%
Semileptonic shape	69%	64%	53%	33%	17%
Signal shape	25%	13%	11%	10%	19%
Reweighting	15%	16%	14%	11%	12%
Known quantities	11%	5%	9%	18%	25%
Efficiency	9%	4%	8%	15%	21%

Dominant due to low background statistics for modelling!

Limits in all $m(K^+K^-)$ and $m(\pi^+\pi^-)$ bins

[LHCb-PAPER-2025-048]

Confidence level	Upper limit on $\mathcal{B}(B^0 \rightarrow K^+\pi^-\tau^+\tau^-)$			
$m_{K^+\pi^-}$ (MeV/ c^2)	[792, 992]	[992, 1330]	[1330, 1530]	[1530, 1726]
90%	1.4×10^{-4}	2.7×10^{-5}	1.0×10^{-5}	2.7×10^{-6}
95%	1.6×10^{-4}	3.4×10^{-5}	1.1×10^{-5}	3.3×10^{-6}

Confidence level	Upper limit on $\mathcal{B}(B_s^0 \rightarrow K^+K^-\tau^+\tau^-)$				
$m_{K^+K^-}$ (MeV/ c^2)	[980, 1060]	[1060, 1200]	[1200, 1400]	[1400, 1600]	[1600, 1813]
90%	2.0×10^{-4}	1.3×10^{-4}	1.2×10^{-4}	6.8×10^{-5}	3.2×10^{-5}
95%	2.3×10^{-4}	1.5×10^{-4}	1.4×10^{-4}	7.6×10^{-5}	3.6×10^{-5}

Confidence level	Upper limit on $\mathcal{B}(B_s^0 \rightarrow K^-\pi^+\tau^+\tau^-)$			
$m_{K^+\pi^-}$ (MeV/ c^2)	[792, 992]	[992, 1330]	[1330, 1530]	[1530, 1726]
90%	6.5×10^{-4}	1.2×10^{-4}	5.1×10^{-5}	1.7×10^{-5}
95%	7.3×10^{-4}	1.5×10^{-4}	6.2×10^{-5}	2.1×10^{-5}

Limits of $|C_9^{\tau\tau}|$

[LHCb-PAPER-2025-048]

the-SM effects may be introduced via a shift, Δ , in the Wilson coefficients $C_9^{\tau\tau} = C_9^{\text{SM}} - \Delta$ and $C_{10}^{\tau\tau} = C_{10}^{\text{SM}} + \Delta$ where C_9^{SM} is 4.1 and C_{10}^{SM} is -4.3 [23]. If $\Delta \gg C_9^{\text{SM}}$ the branching

In this particular case four unknowns must be fixed, which are the components of the τ momentum p_τ^μ . This can be done by exploiting the information on the τ flight direction $\hat{p}_\tau$ (which fixes two unknowns), the mass shell condition for the τ $p_\tau^2 = M_\tau^2$ (one unknown) as well as the momentum conservation in the $\tau \rightarrow 3\pi + \nu$ decay, *i.e.* $(p_\tau - p_{3\pi})^2 = p_\nu^2 = 0$ (one unknown), where $p_{3\pi} \equiv (E_{3\pi}, \vec{p}_{3\pi})$ and p_ν are the four-momenta of the 3π system and the ν respectively. With these constraints the modulus p of the τ space momentum is defined up to a twofold ambiguity, being the solution of the following second degree equation (see *e.g.* Ref.[112]):

$$p^2 \left(1 - \frac{|\vec{p}_{3\pi}|^2}{E_{3\pi}^2} \right) - p \left(\frac{\vec{p}_{3\pi}}{E_{3\pi}} \cdot \hat{p}_\tau \right) \frac{M_\tau^2 + p_{3\pi}^2}{E_{3\pi}} + M_\tau^2 + \left(\frac{M_\tau^2 + p_{3\pi}^2}{2E_{3\pi}} \right)^2 = 0. \quad (4.12)$$

Confidence level	$B^0 \rightarrow K^+ \pi^- \tau^+ \tau^-$	$B_s^0 \rightarrow K^+ K^- \tau^+ \tau^-$
90%	2.5×10^4	4.5×10^4
95%	2.9×10^4	5.2×10^4

Ambiguities in B momentum reconstruction

[LHCb-INT-2011-039](#)

The B_s^0 decay vertex must lie within the plane spanned by the three vertices pV , dV_1 and dV_2 . The vectors between the primary vertex and the first or second decay vertex are denoted by $\vec{v}$ and $\vec{w}$ respectively. The B_s^0 and τ momentum vectors are colinear with the spacial vectors between their origin and decay vertices. Scale factors, $L_{1\tau}$, $L_{2\tau}$ and L_B , are used to relate the topological direction vectors to the particle momenta. The basic geometry of the plane in which the B_s^0 and τ momenta lie is depicted in Figure 1.

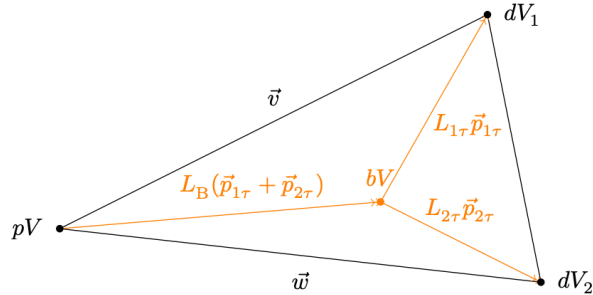


Figure 1 Geometry of the plane containing the B_s^0 and both τ momentum vectors.

L1, L2 and LB are parameters that are found empirically!

The three relations linking the directional vectors to the momenta using scale factors are

$$dV_1 - bV = L_{1\tau}\vec{p}_{1\tau} \quad (1)$$

$$dV_2 - bV = L_{2\tau}\vec{p}_{2\tau} \quad (2)$$

$$bV - pV = L_B(\vec{p}_{1\tau} + \vec{p}_{2\tau}) \quad (3)$$

These relations can be rewritten to a single formula, eliminating the factors $L_{1\tau}$, $L_{2\tau}$ and L_B , as

$$\vec{v} \times \vec{p}_{1\tau} = -\vec{w} \times \vec{p}_{2\tau} \quad (4)$$

The second relation occurs through the fixing of the B_s^0 mass: $(p_{1\tau} + p_{2\tau})^2 = m_B^2$

$$E_{1\tau}E_{2\tau} - \vec{p}_{1\tau} \cdot \vec{p}_{2\tau} = \frac{1}{2}m_B^2 - m_\tau^2 \quad (5)$$

And finally two relations due to the fixing of the neutrino mass

$$(p_{1\tau} - p_{13\pi})^2 = (p_{2\tau} - p_{23\pi})^2 = 0 \quad (6)$$

and two from fixing the τ mass

$$p_{1\tau}^2 = p_{2\tau}^2 = m_\tau^2 \quad (7)$$

The system to be solved thus consists of 8 equations and 8 unknowns, which are the two τ 4-momenta $\{p_{1\tau}, p_{2\tau}\}$. To simplify the algebra, the plane is rotated such that its norm aligns with the z -axis. By doing this the z -components of the two τ momenta as well as the vectors $\vec{v}$ and $\vec{w}$ are set to 0. From this point onwards this will be assumed to be the case.

The $B_s^0 \rightarrow \tau^\pm \tau^\mp$ decay with $\tau^\pm \rightarrow \pi^\pm \pi^\pm \pi^\mp \nu_\tau$ is theoretically reconstructable up to an 8th order polynomial. In order to find the B_s^0 and τ momenta solutions, the roots of this polynomial need to be determined. These roots are limited to a specified interval and can be calculated by scanning this interval in a certain number of steps.

Ambiguities in B momentum reconstruction

$B^0 \rightarrow K^- \pi^+ \tau^+ \tau^-$ Case

<https://repository.cern/records/k8s3d-gf870>

In this particular case four unknowns must be fixed, which are the components of the τ momentum p_τ^μ . This can be done by exploiting the information on the τ flight direction $\hat{p}_\tau$ (which fixes two unknowns), the mass shell condition for the τ $p_\tau^2 = M_\tau^2$ (one unknown) as well as the momentum conservation in the $\tau \rightarrow 3\pi + \nu$ decay, *i.e.* $(p_\tau - p_{3\pi})^2 = p_\nu^2 = 0$ (one unknown), where $p_{3\pi} \equiv (E_{3\pi}, \vec{p}_{3\pi})$ and p_ν are the four-momenta of the 3π system and the ν respectively. With these constraints the modulus p of the τ space momentum is defined up to a twofold ambiguity, being the solution of the following second degree equation (see *e.g.* Ref.[112]):

$$p^2 \left(1 - \frac{|\vec{p}_{3\pi}|^2}{E_{3\pi}^2} \right) - p \left(\frac{\vec{p}_{3\pi}}{E_{3\pi}} \cdot \hat{p}_\tau \right) \frac{M_\tau^2 + p_{3\pi}^2}{E_{3\pi}} + M_\tau^2 + \left(\frac{M_\tau^2 + p_{3\pi}^2}{2E_{3\pi}} \right)^2 = 0. \quad (4.12)$$

[LHCb-INT-2011-039](#)

$B_s^0 \rightarrow \tau^+ \tau^-$ Case

<https://arxiv.org/pdf/1703.02508>

The unknown quantities are

- the decay vertex of the B_s^0 meson: bV ,
- the momentum of the B_s^0 meson: $\vec{p}_B$,
- the momenta of the two τ leptons: $\vec{p}_{1\tau}$ and $\vec{p}_{2\tau}$,
- the momenta of the two neutrinos: $\vec{p}_{1\nu}$ and $\vec{p}_{2\nu}$.

of the $B \rightarrow \tau^+ \tau^-$ decay chain, described in detail in Refs. [35,36], has been developed. It combines geometrical information about the decay and mass constraints on the particles (B , τ and ν) in the decay chain to calculate the τ momenta analytically. The possible solutions for the two τ momenta are found as solutions of a system of two coupled equations of second degree with two unknowns. The finite detector resolution and approximations made in the calculation prevent real solutions being found for a substantial fraction of the signal events. However, several intermediate quantities associated with the method are exploited to discriminate signal from background.

Track and Vertex reconstruction [\[LHCb-DP-2014-002\]](#)

Vertex locator

- 42 silicon modules provide r and ϕ coord.
 - Retractable halves
 - 8mm from beam in data taking

Tracking stations

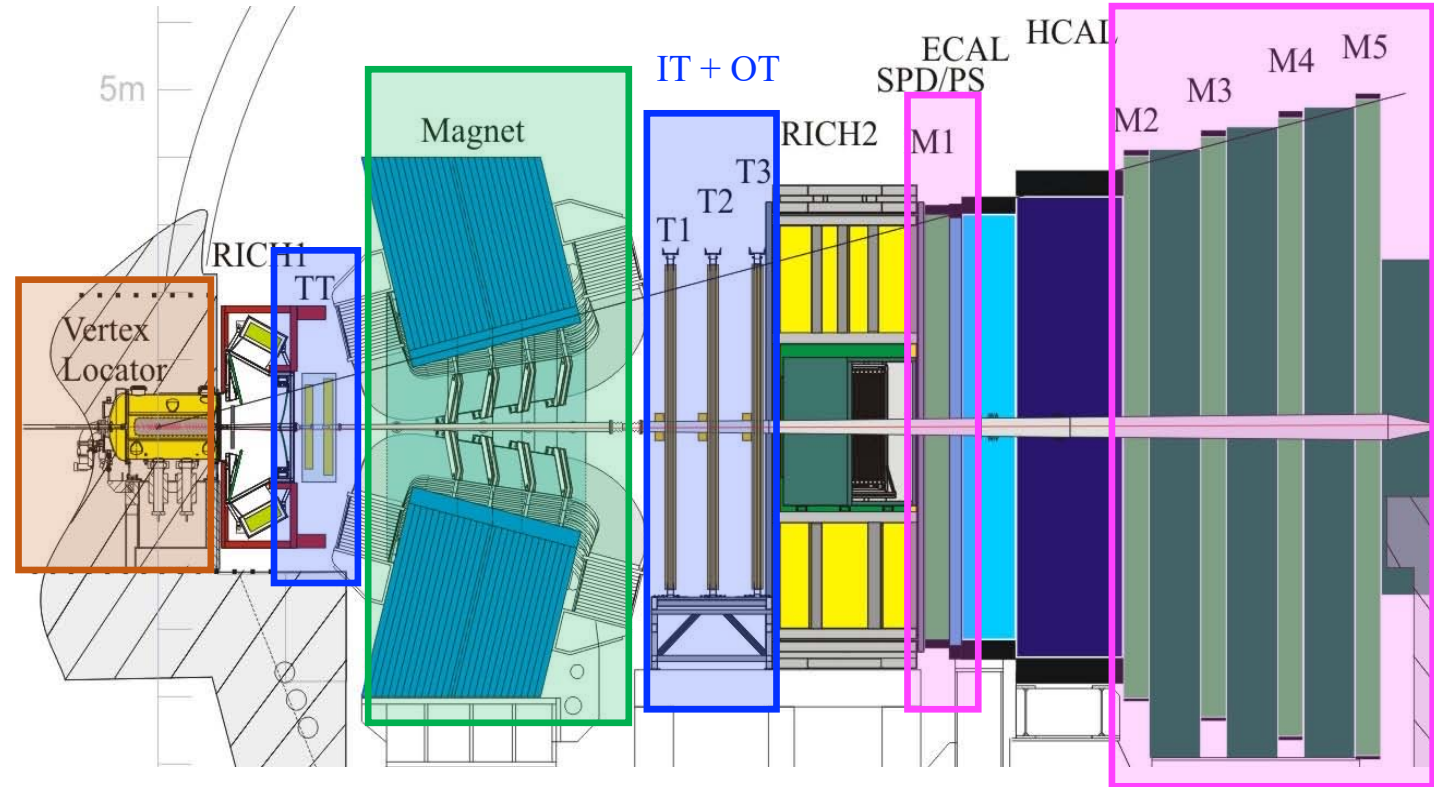
- TT and IT: silicon microstrips
- OT: Straw-tube modules

Dipole magnet

- 4 Tm magnetic field
- Polarity inverted every few weeks

Muon stations

- Consists of 5 stations (M1-M5)
 - MWPCs + triple GEM



- Good decay time res. $\sigma_\tau \sim 45 \text{ fs}$ wrt $\tau_B \sim 1.5 \text{ ps}$
- Good momentum res. $\frac{\delta p}{p} \sim 0.5\% - 1\%$ (5 – 200 GeV)

Particle identification (PID)

[LHCb-DP-2014-002]

Ring imaging Cherenkov detectors

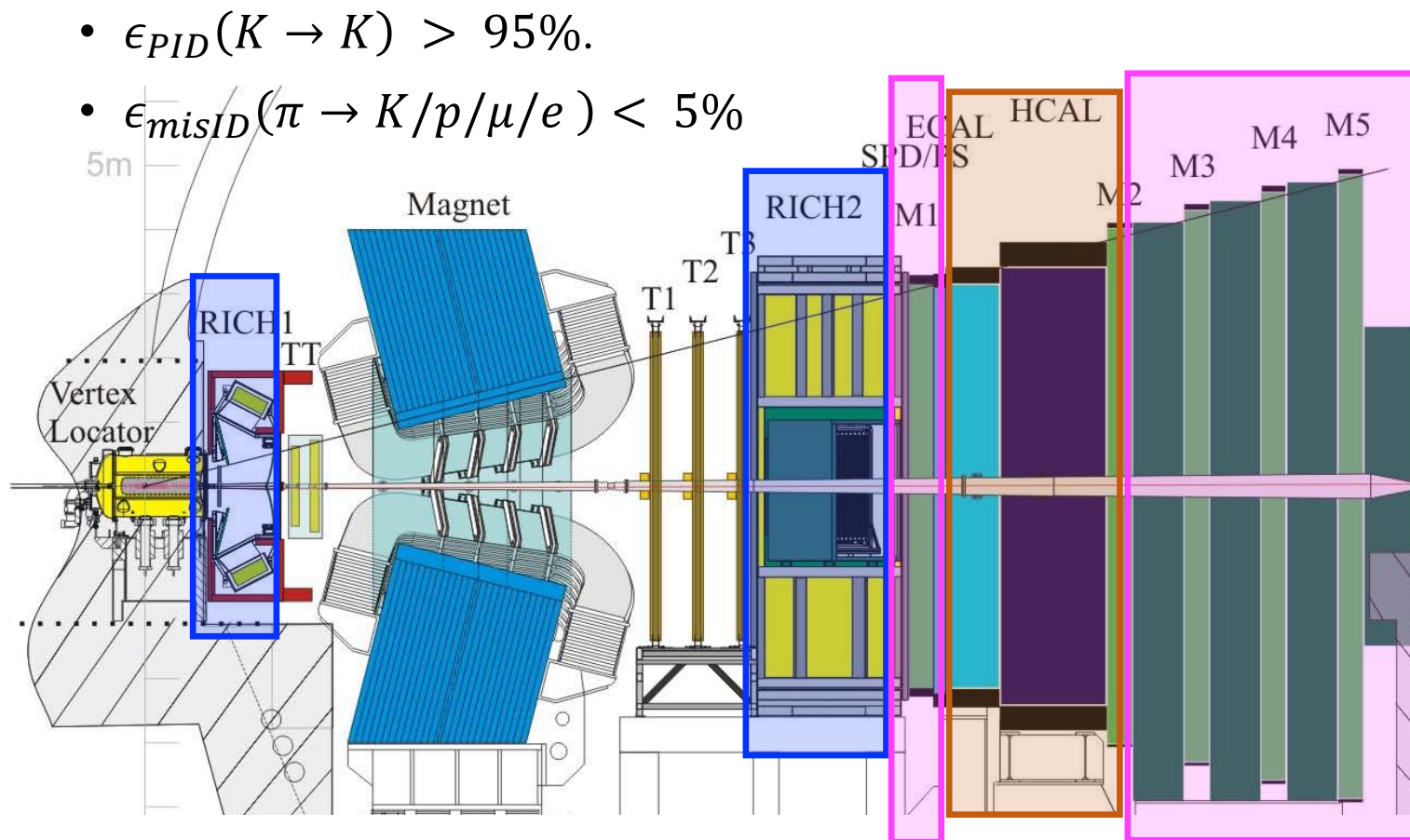
- PID for kaons, pion and protons
- Covers a wide momentum range

Calorimeters

- SPD,PS,ECAL,HCAL
 - PID for e, γ, π^0
- Energy and position for neutral objects and trigger for e, γ

Muon stations

- 5 stations (M1-M5) have high purity PID for muons



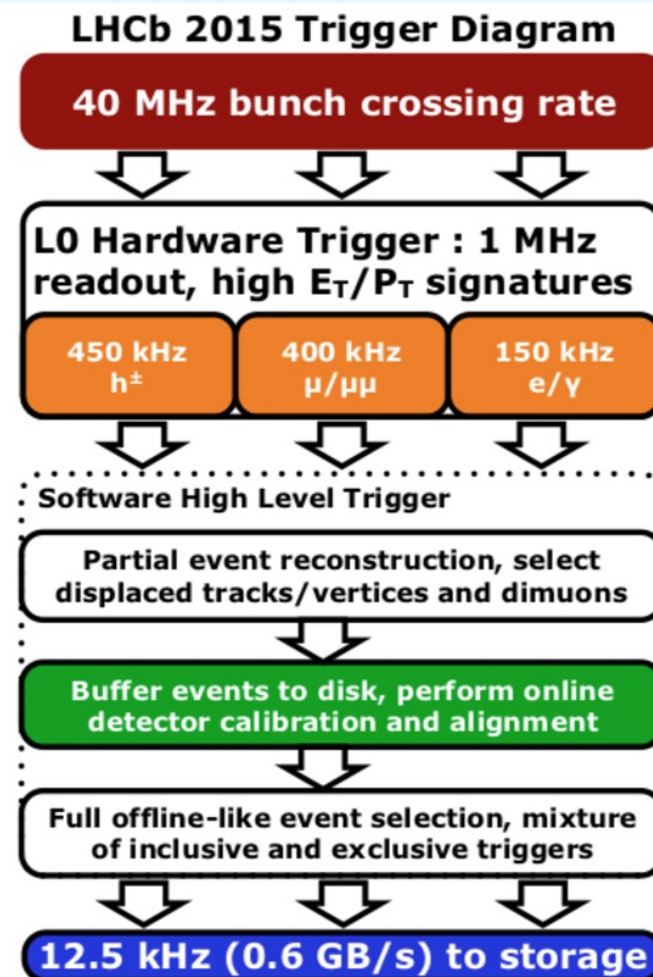
SPD: Scintillating pad detector
PS: Preshower

LHCb trigger (2015-2018)

[[2019 JINST 14 P04006](#), [Comput.Phys.Commun. 208 \(2016\) 35-42](#)]

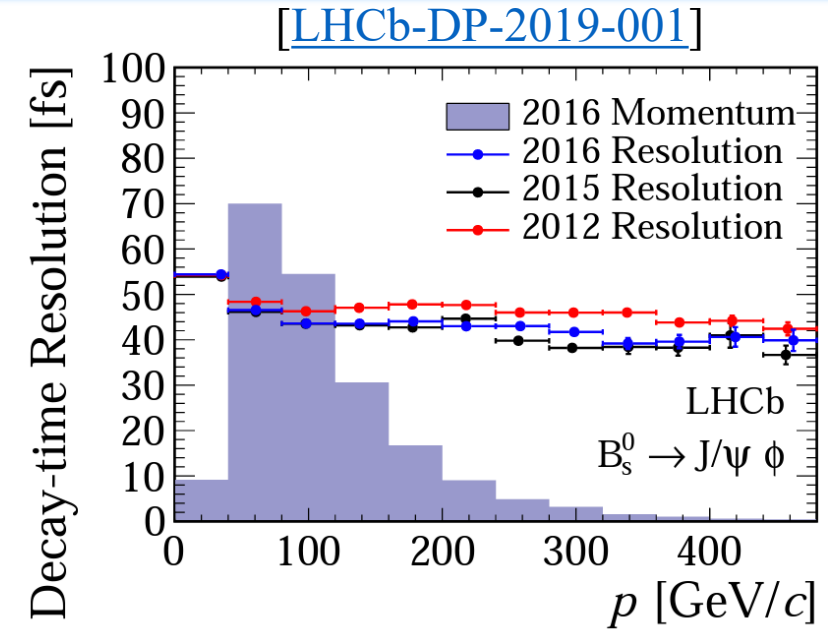
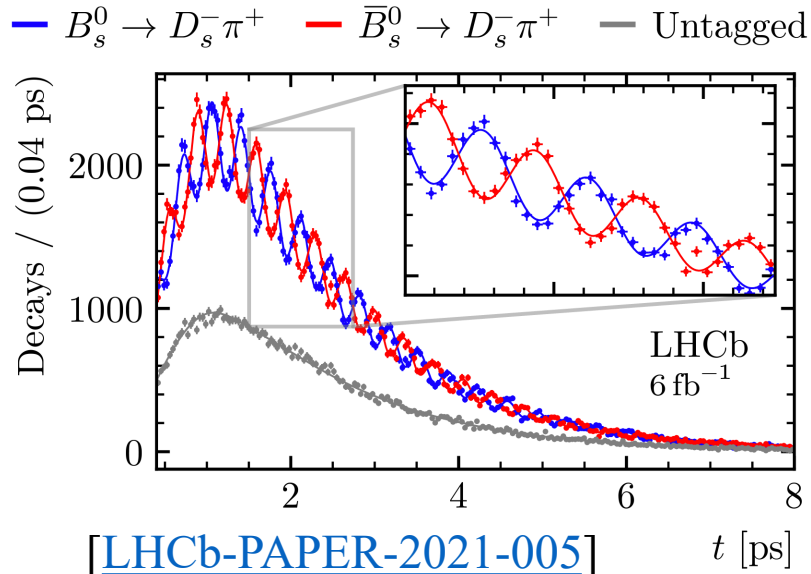
- Trigger needed to **reduce storage and readout costs with good signal to background ratio.**
- Consists of three stages:
 - **L0**: Hardware, E_T/p_T thresholds.
40 MHz $\rightarrow$ 1 MHz.
 - **HLT1**: Software, partial reconstruction,
1 MHz $\rightarrow$ 150 kHz.
 - **HLT2**: Full event reconstruction,
100 kHz $\rightarrow$ 12.5 kHz.

L0: Level 0 trigger
HLT: High level trigger



Vertex reconstruction

Excellent vertexing in VELO! Can still reconstruct downstream decays (K_S , Λ).

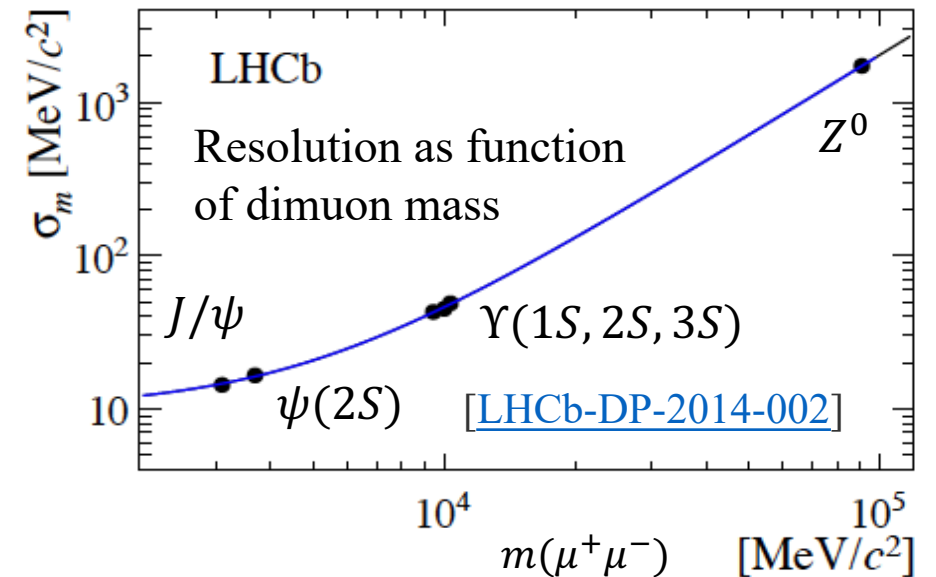
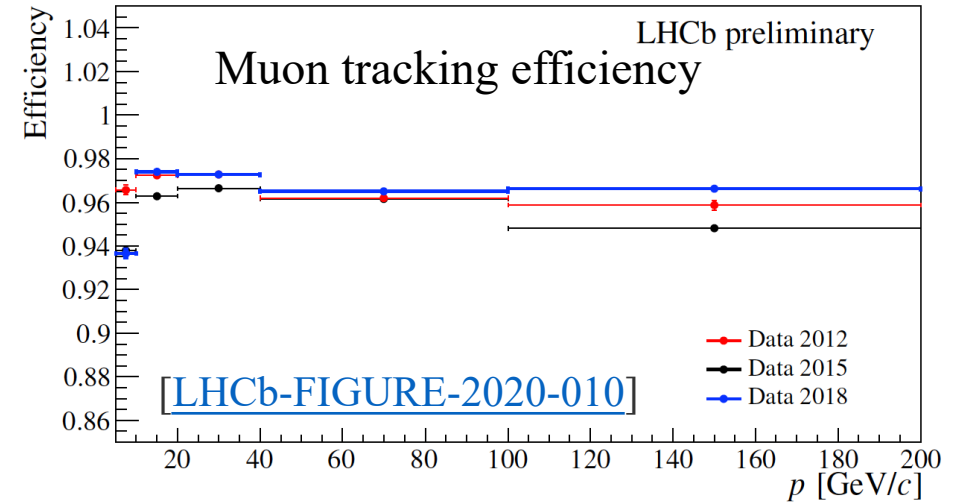
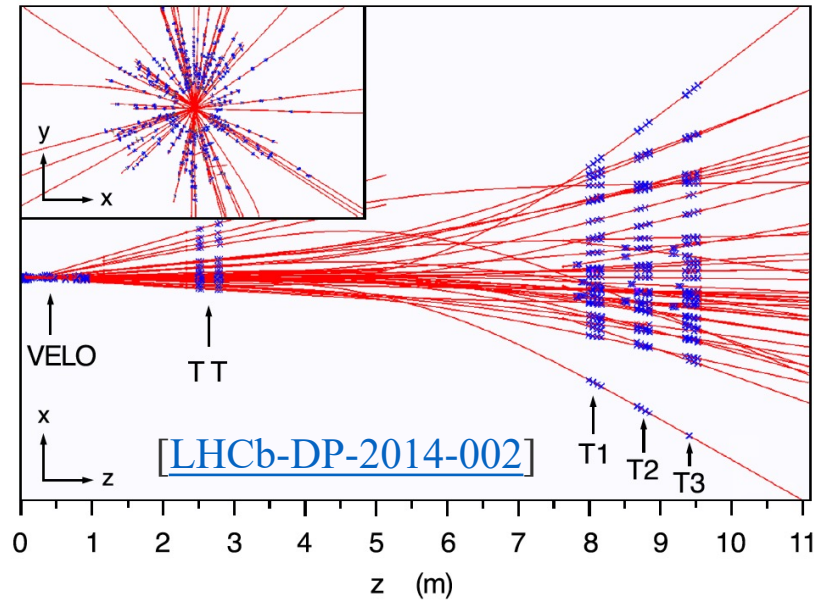


- Good resolution on **Impact Parameter (IP)** required for efficiently selecting B decays:
 $\sigma_{IP} \sim 20 \mu m$ for high p_T tracks.
- Good resolution on **decay time** crucial for time-dependent CP violation analyses:
 $\sigma_\tau \sim 45 fs$ wrt $\tau_B \sim 1.5 ps$

Track reconstruction

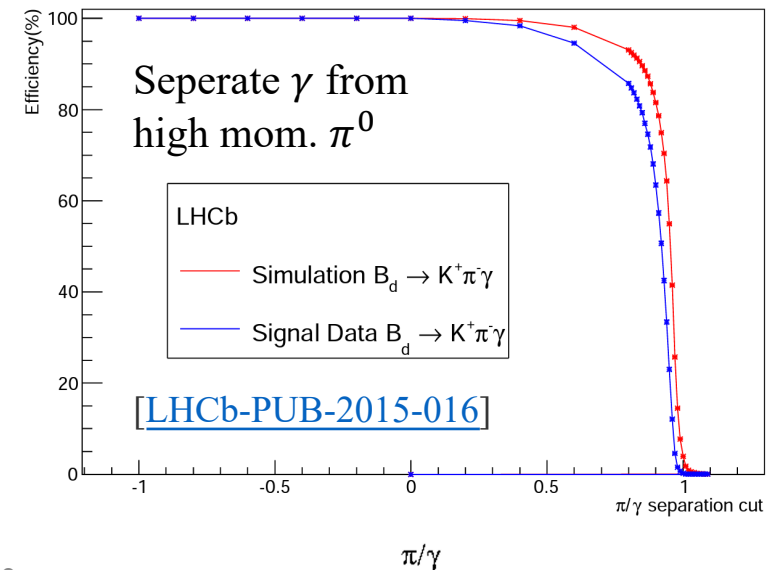
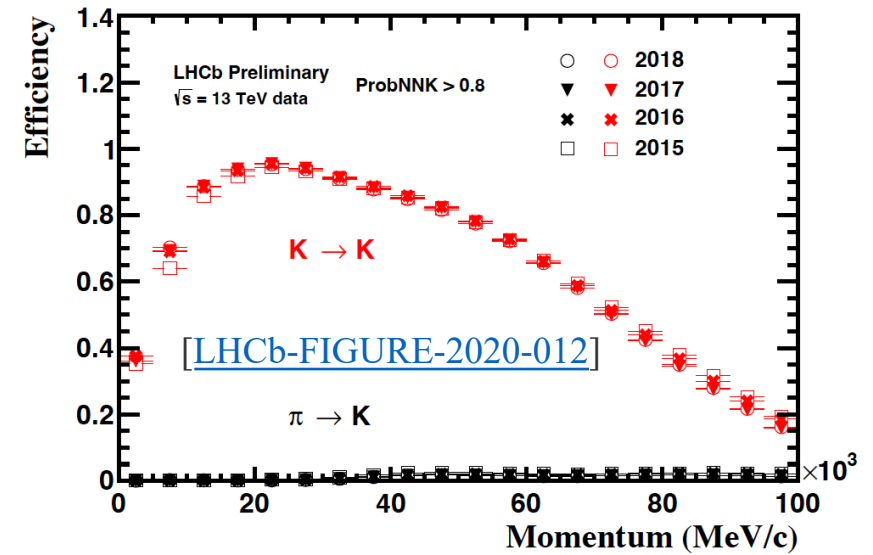
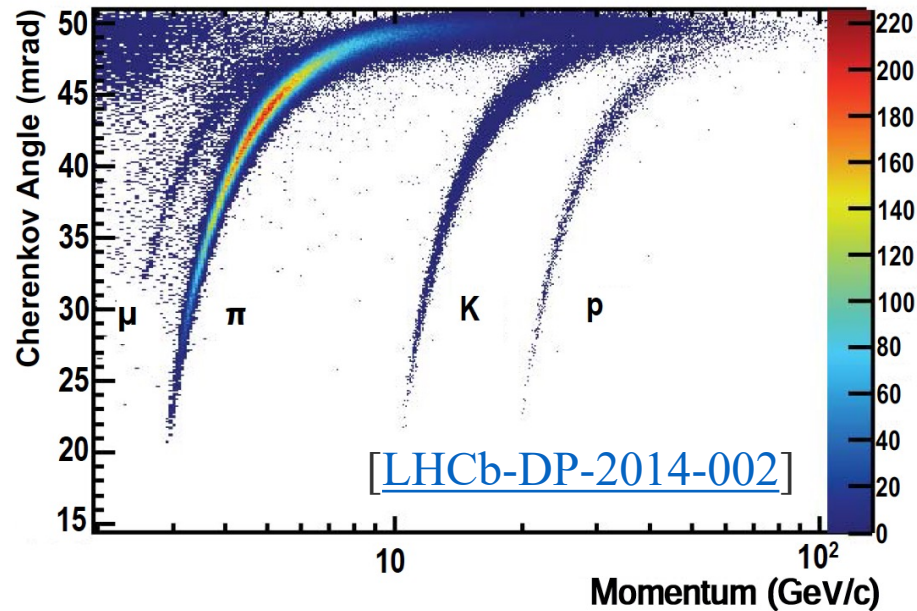
Excellent track reconstruction!

- $\epsilon(\text{tracking}) \sim 96\%$
- $\frac{\delta p}{p} \sim 0.5\% - 1\% \text{ (5 - 200 GeV)}$
- $\sigma(m_{J/\psi}) \sim 15 \text{ MeV}$



Particle identification performance

- Charged: Combine info from RICH, CALO, MUON.
 - $\epsilon_{PID}(K \rightarrow K) > 95\%$ (same for μ and lower for e)
 - $\epsilon_{misID}(\pi \rightarrow K/p/\mu/e) < 5\%$
- Neutral: Dedicated NN for identifying deuterons and separating γ from hadrons, $e^\pm$ and high-energy π^0 s.



Upgrade II

