

Inclusive $\bar{B} \rightarrow X_s \nu \bar{\nu}$ Standard Model update



Jack Jenkins
08 October 2025

In collaboration with
M. Fael, E. Lunghi, Z. Polonsky



TP1
CPPS
Theoretical
Particle Physics
Center for Particle
Physics Siegen

Collaborative Research Center TRR 257



Particle Physics Phenomenology after the Higgs Discovery

Scope of semileptonic FCNC decays:

- $\bar{B} \rightarrow X_s \nu \bar{\nu}$ — top loop dominated, very clean theoretically
- $\bar{B} \rightarrow X_s \ell^+ \ell^-$ — complementary channel with LD effects and angular observables

Phenomenology of $b \rightarrow s \nu \bar{\nu}$ will be limited by experimental precision (Belle/II) for the foreseeable future
The inclusive rate has x10 higher statistics of $B \rightarrow K$, may be possible to leverage against systematic effects

Outline: Refine SM prediction from 10+ years ago

$$\begin{aligned} \text{Br}(\bar{B} \rightarrow X_s \nu \bar{\nu}) &= (3.48 \pm 0.12) \times 10^{-5} && \text{(this work, preliminary)} \\ &= (2.9 \pm 0.3) \times 10^{-5} && \text{Buras, Noe, Niehoff, Straub [1409.4557]} \\ &&& \text{Altmannshofer, Buras, Straub, Wick [0902.0160]} \end{aligned}$$

Various theoretical developments:

- Updated Wilson coefficients and QCD corrections in the heavy quark limit
- Heavy quark expansion including corrections up to $1/m_b^3$
- Analysis of the neutrino pair invariant mass spectrum
- Comparison with experimental prospects / thoughts on leveraging the M_X distribution

Scope of semileptonic FCNC decays:

- $\bar{B} \rightarrow X_s \nu \bar{\nu}$ — top loop dominated, very clean theoretically
- $\bar{B} \rightarrow X_s \ell^+ \ell^-$ — complementary channel with LD effects and angular observables

Phenomenology of $b \rightarrow s \nu \bar{\nu}$ will be limited by experimental precision (Belle/II) for the foreseeable future
The inclusive rate has x10 higher statistics of $B \rightarrow K$, may be possible to leverage against systematic effects

Outline: Refine SM prediction from 10+ years ago

$$\begin{aligned} \text{Br}(\bar{B} \rightarrow X_s \nu \bar{\nu}) &= (3.48 \pm 0.12) \times 10^{-5} && \text{(this work, preliminary)} \\ &= (2.9 \pm 0.3) \times 10^{-5} && \text{Buras, Noe, Niehoff, Straub [1409.4557]} \\ &&& \text{Altmannshofer, Buras, Straub, Wick [0902.0160]} \end{aligned}$$

Various theoretical developments:

- Updated Wilson coefficients and QCD corrections in the heavy quark limit
- Heavy quark expansion including corrections up to $1/m_b^3$
- Analysis of the neutrino pair invariant mass spectrum
- Comparison with experimental prospects / thoughts on leveraging the M_X distribution

Scope of semileptonic FCNC decays:

- $\bar{B} \rightarrow X_s \nu \bar{\nu}$ — top loop dominated, very clean theoretically
- $\bar{B} \rightarrow X_s \ell^+ \ell^-$ — complementary channel with LD effects and angular observables

Phenomenology of $b \rightarrow s \nu \bar{\nu}$ will be limited by experimental precision (Belle/II) for the foreseeable future
The inclusive rate has x10 higher statistics of $B \rightarrow K$, may be possible to leverage against systematic effects

Outline: Refine SM prediction from 10+ years ago

$$\begin{aligned} \text{Br}(\bar{B} \rightarrow X_s \nu \bar{\nu}) &= (3.48 \pm 0.12) \times 10^{-5} && \text{(this work, preliminary)} \\ &= (2.9 \pm 0.3) \times 10^{-5} && \text{Buras, Noe, Niehoff, Straub [1409.4557]} \\ &&& \text{Altmannshofer, Buras, Straub, Wick [0902.0160]} \end{aligned}$$

Various theoretical developments:

- Updated Wilson coefficients and QCD corrections in the heavy quark limit
- Heavy quark expansion including corrections up to $1/m_b^3$
- Analysis of the neutrino pair invariant mass spectrum
- Comparison with experimental prospects / thoughts on leveraging the M_X distribution

Standard model matches to the $V - A$ operator only

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} [C_\nu Q_\nu + \text{h.c.}] ,$$

$$C_\nu = \frac{\alpha(M_Z)}{2 \sin^2 \theta_W(M_Z)} X_t , \quad Q_\nu = \bar{b}_L \gamma_\mu s_L \sum_\nu \bar{\nu}_L \gamma^\mu \nu_L$$

At NLO QCD: [Misiak, Urban \[9901278\]](#) [Buchalla, Buras \[9901288\]](#) and NLO EW: [Brod, Gorbahn, Stamou \[1009.0947\]](#)

$$X_t = 1.462(9)_{\text{QCD}}(2)_{\text{EW}}(5)_{\text{par}} = 1.462(10) \quad (\text{this work})$$

$$= 1.462(17) \quad \text{Brod, Gorbahn, Stamou [2105.02868]}$$

- We include higher order running of the top mass $\bar{m}_t(\mu)$
- Perturbative uncertainty will be clarified when complete NNLO is available
- The NLO corrections are small, but are likely not accidentally so, since the NNLO QCD corrections are under control for the perturbative series in $\bar{B}_s \rightarrow \mu^+ \mu^-$ [Hermann, Misiak, Steinhauser \[1311.1347\]](#)

Standard model matches to the $V - A$ operator only

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} [C_\nu Q_\nu + \text{h.c.}] ,$$

$$C_\nu = \frac{\alpha(M_Z)}{2 \sin^2 \theta_W(M_Z)} X_t , \quad Q_\nu = \bar{b}_L \gamma_\mu s_L \sum_\nu \bar{\nu}_L \gamma^\mu \nu_L$$

At NLO QCD: [Misiak, Urban \[9901278\]](#) and [Buchalla, Buras \[9901288\]](#) and NLO EW: [Brod, Gorbahn, Stamou \[1009.0947\]](#)

$$X_t = 1.462(9)_{\text{QCD}}(2)_{\text{EW}}(5)_{\text{par}} = 1.462(10) \quad (\text{this work})$$

$$= 1.462(17) \quad \text{Brod, Gorbahn, Stamou [2105.02868]}$$

- We include higher order running of the top mass $\bar{m}_t(\mu)$
- Perturbative uncertainty will be clarified when complete NNLO is available
- The NLO corrections are small, but are likely not accidentally so, since the NNLO QCD corrections are under control for the perturbative series in $\bar{B}_s \rightarrow \mu^+ \mu^-$ [Hermann, Misiak, Steinhauser \[1311.1347\]](#)

Standard model matches to the $V - A$ operator only

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} [C_\nu Q_\nu + \text{h.c.}] ,$$

$$C_\nu = \frac{\alpha(M_Z)}{2 \sin^2 \theta_W(M_Z)} X_t , \quad Q_\nu = \bar{b}_L \gamma_\mu s_L \sum_\nu \bar{\nu}_L \gamma^\mu \nu_L$$

At NLO QCD: [Misiak, Urban \[9901278\]](#) [Buchalla, Buras \[9901288\]](#) and NLO EW: [Brod, Gorbahn, Stamou \[1009.0947\]](#)

$$X_t = 1.462(9)_{\text{QCD}}(2)_{\text{EW}}(5)_{\text{par}} = 1.462(10) \quad (\text{this work})$$

$$= 1.462(17) \quad \text{Brod, Gorbahn, Stamou [2105.02868]}$$

- We include higher order running of the top mass $\overline{m}_t(\mu)$
- Perturbative uncertainty will be clarified when complete NNLO is available
- The NLO corrections are small, but are likely not accidentally so, since the NNLO QCD corrections are under control for the perturbative series in $\bar{B}_s \rightarrow \mu^+ \mu^-$ [Hermann, Misiak, Steinhauser \[1311.1347\]](#)

Standard model matches to the $V - A$ operator only

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} [C_\nu Q_\nu + \text{h.c.}] ,$$

$$C_\nu = \frac{\alpha(M_Z)}{2 \sin^2 \theta_W(M_Z)} X_t , \quad Q_\nu = \bar{b}_L \gamma_\mu s_L \sum_\nu \bar{\nu}_L \gamma^\mu \nu_L$$

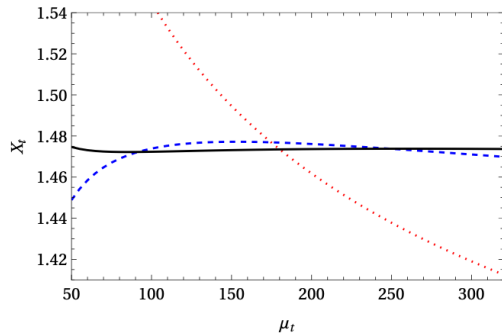
At NLO QCD: [Misiak, Urban \[9901278\]](#) and [Buchalla, Buras \[9901288\]](#) and NLO EW: [Brod, Gorbahn, Stamou \[1009.0947\]](#)

$$X_t = 1.462(9)_{\text{QCD}}(2)_{\text{EW}}(5)_{\text{par}} = 1.462(10) \quad (\text{this work})$$

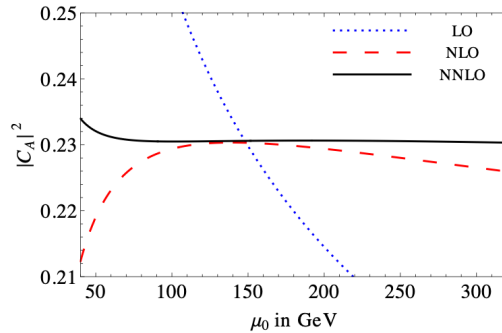
$$= 1.462(17) \quad \text{Brod, Gorbahn, Stamou [2105.02868]}$$

- We include higher order running of the top mass $\bar{m}_t(\mu)$
- Perturbative uncertainty will be clarified when complete NNLO is available
- The NLO corrections are small, but are likely not accidentally so, since the NNLO QCD corrections are under control for the perturbative series in $\bar{B}_s \rightarrow \mu^+ \mu^-$ [Hermann, Misiak, Steinhauser \[1311.1347\]](#)

$b \rightarrow s \nu \bar{\nu}$ (V-A) Preliminary, from E. Stamou's talk at Kaon25



$b \rightarrow s \mu^+ \mu^-$ (A) Hermann, Misiak, Steinhauser [1311.1347]



The heavy quark masses are critical parametric inputs

$$\text{Br}(\bar{B} \rightarrow X_s \nu \bar{\nu}) \sim (m_t^2)^2 (m_b^5)$$

Top quark mass

Top mass from direct determinations at the LHC

$$m_t^{\text{OS}} = 172.56(31) \text{ GeV} \\ \implies \overline{m}_t(\overline{m}_t) = 162.98(30)_{\text{par}}(25)_{\text{had}}^* \text{ GeV}$$

Hadronic uncertainty from analysis of asymptotic series for m_t^{OS} in the $\overline{\text{MS}}$ scheme at N4LO

Hoang, Lepenik, Preisser [1706.08526]

Beneke, Marquard, Nason, Steinhauser [1605.03609]

*Errors should be combined linearly since the hadronic uncertainty has no statistical interpretation

Bottom quark mass

In principle one can take $\overline{m}_b(\overline{m}_b)$ from lattice QCD / spectroscopy and convert to kinetic scheme at N3LO

Fael, Schönwald, Steinhauser [2005.06487]

$$\overline{m}_b(\overline{m}_b) = 4.200(14) \text{ GeV}, N_f = 2 + 1 + 1 \\ \implies m_b^{\text{kin}}(1 \text{ GeV}) = 4.562(18) \text{ GeV}$$

In practice the kinetic mass determined in this way is treated as a prior entering in a fit to $\bar{B} \rightarrow X_c \ell \nu$ decay rate and distributions

$$\implies m_b^{\text{kin}}(1 \text{ GeV}) = 4.573(12) \text{ GeV}$$

Finauri, Gambino [2310.20324]

The heavy quark masses are critical parametric inputs

$$\text{Br}(\bar{B} \rightarrow X_s \nu \bar{\nu}) \sim (m_t^2)^2 (m_b^5)$$

Top quark mass

Top mass from direct determinations at the LHC

$$m_t^{\text{OS}} = 172.56(31) \text{ GeV}$$

$$\implies \bar{m}_t(\bar{m}_t) = 162.98(30)_{\text{par}}(25)_{\text{had}}^* \text{ GeV}$$

Hadronic uncertainty from analysis of asymptotic series for m_t^{OS} in the $\overline{\text{MS}}$ scheme at N4LO

Hoang, Lepenik, Preisser [1706.08526]

Beneke, Marquard, Nason, Steinhauser [1605.03609]

*Errors should be combined linearly since the hadronic uncertainty has no statistical interpretation

Bottom quark mass

In principle one can take $\overline{m}_b(\overline{m}_b)$ from lattice QCD / spectroscopy and convert to kinetic scheme at N3LO

Fael, Schönwald, Steinhauser [2005.06487]

$$\overline{m}_b(\overline{m}_b) = 4.200(14) \text{ GeV}, N_f = 2 + 1 + 1$$

$$\implies m_b^{\text{kin}}(1 \text{ GeV}) = 4.562(18) \text{ GeV}$$

In practice the kinetic mass determined in this way is treated as a prior entering in a fit to $\bar{B} \rightarrow X_c \ell \nu$ decay rate and distributions

$$\implies m_b^{\text{kin}}(1 \text{ GeV}) = 4.573(12) \text{ GeV}$$

Finauri, Gambino [2310.20324]

Factorization of leptonic current and optical theorem:

$$\Gamma(\bar{B} \rightarrow X_s \nu \bar{\nu}) = \frac{1}{2M_B} \text{Im} \left[i \int d^4x \langle \bar{B} | T \{ \mathcal{L}_{\text{eff}}^\dagger(x) \mathcal{L}_{\text{eff}}(0) \} | \bar{B} \rangle \right]$$

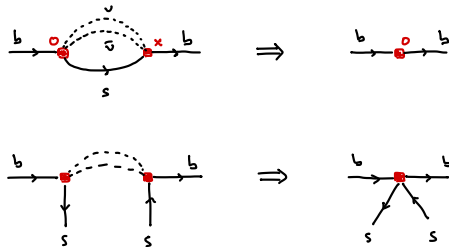
$$\frac{d\Gamma(\bar{B} \rightarrow X_s \nu \bar{\nu})}{dq^2} = \frac{1}{2M_B} \text{Im} \left[i \int d^4x e^{iqx} \langle \bar{B} | T J_\mu^\dagger(x) J_\nu(0) | \bar{B} \rangle \right] L^{\mu\nu}$$

Operator product expansion of QCD currents

$$J_\mu = \bar{b}_L \gamma_\mu s_L$$

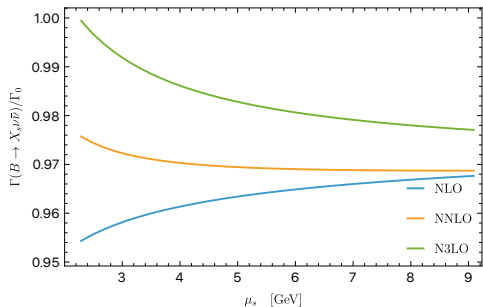
$$T J_\mu^\dagger(x) J^\mu(0) = \sum_k C_k(x) Q_k(0),$$

$$Q_k = \{ \bar{b}b, \bar{b}(iD)^2 b, \bar{b}\sigma^{\mu\nu} [iD_\mu, iD_\nu] b \dots \}$$



We take $m_s/m_b \sim 0$, then the structure of the QCD corrections is equivalent to $B \rightarrow X_u \ell \nu$

$$\Gamma(\bar{B} \rightarrow X_s \nu \bar{\nu}) = N_\nu \frac{G_F^2 m_b^5}{192 \pi^3} |V_{ts} V_{tb}|^2 |C_\nu|^2 \left\{ 1 + C_F \sum_{n=1} X_n \left(\frac{\alpha_s}{\pi} \right)^n - \frac{\mu_\pi^2}{2m_b^2} - \frac{3\mu_G^2}{2m_b^2} + \frac{3\rho_{LS}^3}{2m_b^3} + \frac{77\rho_D^3}{6m_b^3} + \frac{\tau_0}{m_b^3} \right\}$$



pQCD: Kinetic scheme optimized for $b \rightarrow c$ decays, some indication of a divergent series for $b \rightarrow u(s)$ at the percent level

Matrix elements: $\langle .. \rangle = \langle \bar{B} | ... | \bar{B} \rangle / (2M_B)$

$$\mu_\pi^2 = - \langle \bar{b}_v (iD)^2 b_v \rangle ,$$

$$\mu_G^2 = \frac{1}{2} \langle \bar{b}_v (-i\sigma^{\mu\nu}) [iD_\mu, iD_\nu] b_v \rangle ,$$

$$\rho_{LS}^3 = \frac{1}{2} \langle \bar{b}_v (-i\sigma^{\mu\nu}) \{ iD_\mu, [iv \cdot D, iD_\nu] \} b_v \rangle ,$$

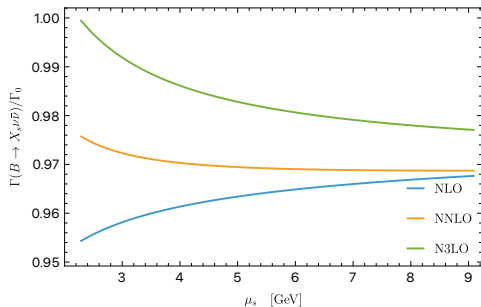
$$\rho_D^3 = \frac{1}{2} \langle \bar{b}_v [iD_\mu, [iv \cdot D, iD^\mu]] \bar{b}_v \rangle$$

Stability of HQE

$$\frac{\Gamma}{\Gamma_0} \simeq 1 - 0.0360 \alpha_s + (0.0216 - 0.00020 n_c) \alpha_s^2 + 0.0237 \alpha_s^3 - 0.0097 \mu_{i,\rho_i}$$

We take $m_s/m_b \sim 0$, then the structure of the QCD corrections is equivalent to $B \rightarrow X_u \ell \nu$

$$\Gamma(\bar{B} \rightarrow X_s \nu \bar{\nu}) = N_\nu \frac{G_F^2 m_b^5}{192 \pi^3} |V_{ts} V_{tb}|^2 |C_\nu|^2 \left\{ 1 + C_F \sum_{n=1} X_n \left(\frac{\alpha_s}{\pi} \right)^n - \frac{\mu_\pi^2}{2m_b^2} - \frac{3\mu_G^2}{2m_b^2} + \frac{3\rho_{LS}^3}{2m_b^3} + \frac{77\rho_D^3}{6m_b^3} + \frac{\tau_0}{m_b^3} \right\}$$



pQCD: Kinetic scheme optimized for $b \rightarrow c$ decays,
some indication of a divergent series for $b \rightarrow u(s)$ at
the percent level

Matrix elements: $\langle .. \rangle = \langle \bar{B} | ... | \bar{B} \rangle / (2M_B)$

$$\mu_\pi^2 = - \langle \bar{b}_v (iD)^2 b_v \rangle ,$$

$$\mu_G^2 = \frac{1}{2} \langle \bar{b}_v (-i\sigma^{\mu\nu}) [iD_\mu, iD_\nu] b_v \rangle ,$$

$$\rho_{LS}^3 = \frac{1}{2} \langle \bar{b}_v (-i\sigma^{\mu\nu}) \{ iD_\mu, [iv \cdot D, iD_\nu] \} b_v \rangle ,$$

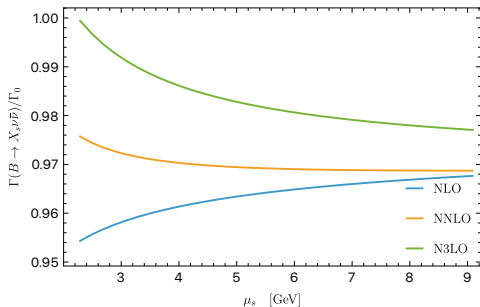
$$\rho_D^3 = \frac{1}{2} \langle \bar{b}_v [iD_\mu, [iv \cdot D, iD^\mu]] \bar{b}_v \rangle$$

Stability of HQE

$$\frac{\Gamma}{\Gamma_0} \simeq 1 - 0.0360 \alpha_s + (0.0216 - 0.00020 n_c) \alpha_s^2 \\ + 0.0237 \alpha_s^3 - 0.0097 \mu_i, \rho_i$$

We take $m_s/m_b \sim 0$, then the structure of the QCD corrections is equivalent to $B \rightarrow X_u \ell \nu$

$$\Gamma(\bar{B} \rightarrow X_s \nu \bar{\nu}) = N_\nu \frac{G_F^2 m_b^5}{192 \pi^3} |V_{ts} V_{tb}|^2 |C_\nu|^2 \left\{ 1 + C_F \sum_{n=1} X_n \left(\frac{\alpha_s}{\pi} \right)^n - \frac{\mu_\pi^2}{2m_b^2} - \frac{3\mu_G^2}{2m_b^2} + \frac{3\rho_{LS}^3}{2m_b^3} + \frac{77\rho_D^3}{6m_b^3} + \frac{\tau_0}{m_b^3} \right\}$$



pQCD: Kinetic scheme optimized for $b \rightarrow c$ decays, some indication of a divergent series for $b \rightarrow u(s)$ at the percent level

Matrix elements: $\langle .. \rangle = \langle \bar{B} | ... | \bar{B} \rangle / (2M_B)$

$$\mu_\pi^2 = - \langle \bar{b}_v (iD)^2 b_v \rangle ,$$

$$\mu_G^2 = \frac{1}{2} \langle \bar{b}_v (-i\sigma^{\mu\nu}) [iD_\mu, iD_\nu] b_v \rangle ,$$

$$\rho_{LS}^3 = \frac{1}{2} \langle \bar{b}_v (-i\sigma^{\mu\nu}) \{ iD_\mu, [iv \cdot D, iD_\nu] \} b_v \rangle ,$$

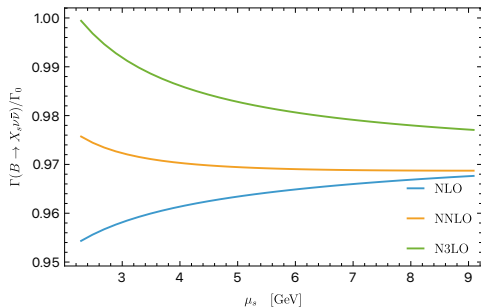
$$\rho_D^3 = \frac{1}{2} \langle \bar{b}_v [iD_\mu, [iv \cdot D, iD^\mu]] \bar{b}_v \rangle$$

Stability of HQE

$$\frac{\Gamma}{\Gamma_0} \simeq 1 - 0.0360 \alpha_s + (0.0216 - 0.00020 n_c) \alpha_s^2 + 0.0237 \alpha_s^3 - 0.0097 \mu_{i,\rho_i}$$

We take $m_s/m_b \sim 0$, then the structure of the QCD corrections is equivalent to $B \rightarrow X_u \ell \nu$

$$\Gamma(\bar{B} \rightarrow X_s \nu \bar{\nu}) = N_\nu \frac{G_F^2 m_b^5}{192 \pi^3} |V_{ts} V_{tb}|^2 |C_\nu|^2 \left\{ 1 + C_F \sum_{n=1} X_n \left(\frac{\alpha_s}{\pi} \right)^n - \frac{\mu_\pi^2}{2m_b^2} - \frac{3\mu_G^2}{2m_b^2} + \frac{3\rho_{LS}^3}{2m_b^3} + \frac{77\rho_D^3}{6m_b^3} + \frac{\tau_0}{m_b^3} \right\}$$



pQCD: Kinetic scheme optimized for $b \rightarrow c$ decays,
some indication of a divergent series for $b \rightarrow u(s)$ at
the percent level

Matrix elements: $\langle \dots \rangle = \langle \bar{B} | \dots | \bar{B} \rangle / (2M_B)$

$$\mu_\pi^2 = - \langle \bar{b}_v (iD)^2 b_v \rangle ,$$

$$\mu_G^2 = \frac{1}{2} \langle \bar{b}_v (-i\sigma^{\mu\nu}) [iD_\mu, iD_\nu] b_v \rangle ,$$

$$\rho_{LS}^3 = \frac{1}{2} \langle \bar{b}_v (-i\sigma^{\mu\nu}) \{ iD_\mu, [iv \cdot D, iD_\nu] \} b_v \rangle ,$$

$$\rho_D^3 = \frac{1}{2} \langle \bar{b}_v [iD_\mu, [iv \cdot D, iD^\mu]] \bar{b}_v \rangle$$

Stability of HQE

$$\frac{\Gamma}{\Gamma_0} \simeq 1 - 0.0360 \alpha_s + (0.0216 - 0.00020 n_c) \alpha_s^2 \\ + 0.0237 \alpha_s^3 - 0.0097 \mu_{i,\rho_i}$$

Weak annihilation is suppressed since the valence quark ($q = u, d$) is not involved in the weak transition

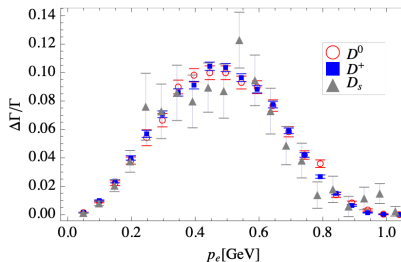
$$O_1 = 4(\bar{b}_v \gamma_\mu s_L)(\bar{s}_L \gamma^\mu b_v), \quad O_2 = 4(\bar{b}_v s_L)(\bar{s}_L b_v)$$

$$\langle \bar{B}_q | O_2 - O_1 | \bar{B}_q \rangle = F_B^2 M_B (\tilde{\delta}_2 - \tilde{\delta}_1)$$

Four-quark operators mix with ρ_D at $O(\alpha_s^0)$. We identify the scale independent quantity at this order with input from HQET sum rules [King, Lenz, Rauh \[2112.03691\]](#)

$$\begin{aligned} \tau_0 &= 8\rho_D \ln \frac{\mu^2}{m_b^2} + 16\pi^2 F_B^2 (\tilde{\delta}_2 - \tilde{\delta}_1) \\ &= -3_{-0.6}^{+1.4} \text{ GeV}^3, \quad (\mu = 1.5 \text{ GeV}) \end{aligned}$$

WA can be constrained by $\Delta\text{Br}(D_{(s)} \rightarrow X_d \ell \nu)$
(exploiting HQ and $SU(3)$ flavor-symmetry)



Using $|V_{cb}|_{\text{inc}} = 41.97(48) \times 10^{-3}$ and including correlation with m_b (-0.428)

$$\begin{aligned} \text{Br}(B^+ \rightarrow X_s \nu \bar{\nu}) &= 3.342(40)_{\mu_0} (40)_{\mu_b} (35)_{\mu_k} (27)_{\text{par}} (\textcolor{red}{68})_{\text{HQE}} (\textcolor{red}{58})_{\text{CKM}} \times 10^{-5} \\ &= 3.342(112) \times 10^{-5} \quad (3.4\%) \quad \hookrightarrow (\textcolor{red}{76})_{\text{CKM}} \text{ without accounting for} \\ &\quad \text{correlations with HQE} \end{aligned}$$

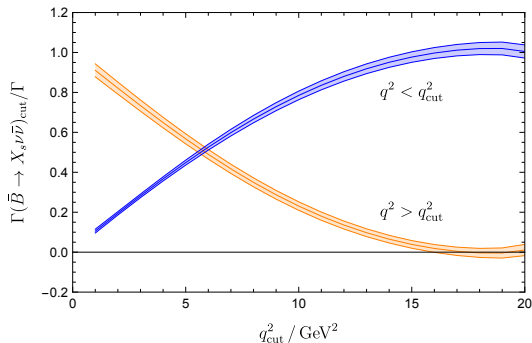
$$\text{Br}(\bar{B}^0 \rightarrow X_s \nu \bar{\nu}) = 3.609(121) \times 10^{-5}$$

$$\text{Br}(\bar{B} \rightarrow X_s \nu \bar{\nu})_{\text{inc } V_{cb}} = (3.48 \pm 0.12) \times 10^{-5} \quad (3.4\%)$$

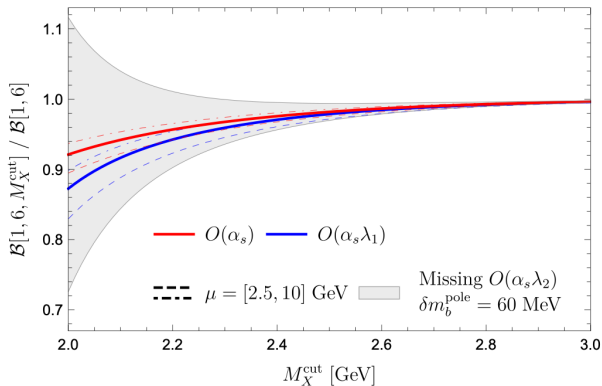
Using $|V_{cb}|_{\text{excl}} = 39.46(53) \times 10^{-3}$ (uncorrelated with m_b^5)

$$\text{Br}(\bar{B} \rightarrow X_s \nu \bar{\nu})_{\text{excl } V_{cb}} = (3.07 \pm 0.12) \times 10^{-5} \quad (4.0\%)$$

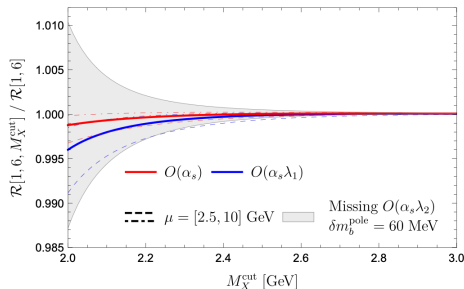
- Similar precision is achieved for the decay rate with a cut $q^2 < q_{\text{max}}^2$
- The complementary cut $q^2 > q_{\text{min}}^2$ is divergent as q_{min}^2 approaches the kinematical endpoint $\sim M_B^2$



- There is no photon pole at $q^2 = 0$, but the rate is still large at low q^2 due to phase space
- Point of discussion: what is the q^2 -dependent sensitivity for $B \rightarrow X_s \nu \bar{\nu}$?

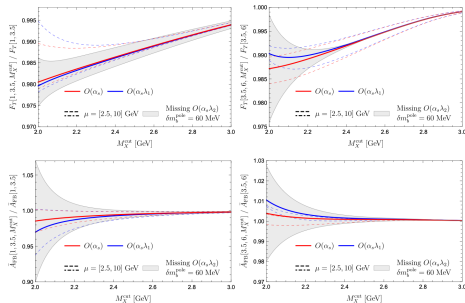


- Hadronic mass distribution can be studied in the OPE for $M_X \gtrsim \sqrt{\Lambda m_b}$
- The spectrum is known at partial α_s/m_b^2 including all penguin interference effects in $\bar{B} \rightarrow X_s \ell^+ \ell^-$
[Huber, Hurth, JJ, Lunghi \[2306.03134\]](#)
- $\bar{B} \rightarrow X_s \nu \bar{\nu}$ a small subset of the more general result
- Also possible to leverage measured $\bar{B} \rightarrow X_s \gamma$ spectrum and QCD factorization to study the shape function region $M_X \simeq \sqrt{\Lambda m_b}$



Hadronic mass cut effects at low- q^2 should be suppressed by forming the ratio (also for the neutrino mode)

$$R = \text{Br}(\bar{B} \rightarrow X_s \ell^+ \ell^-) / \text{Br}(\bar{B} \rightarrow X_u \ell \nu)$$

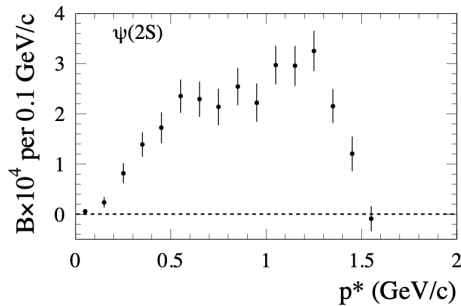
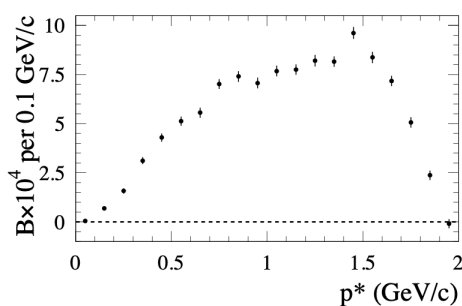


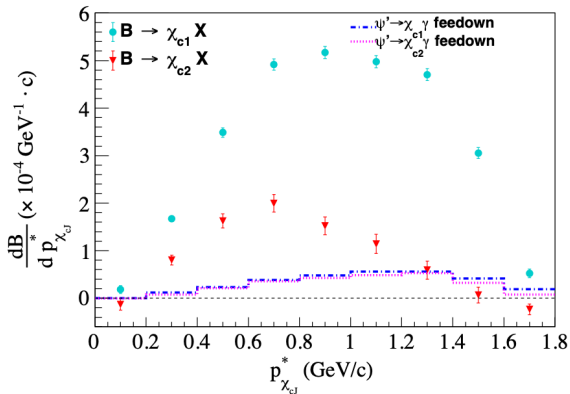
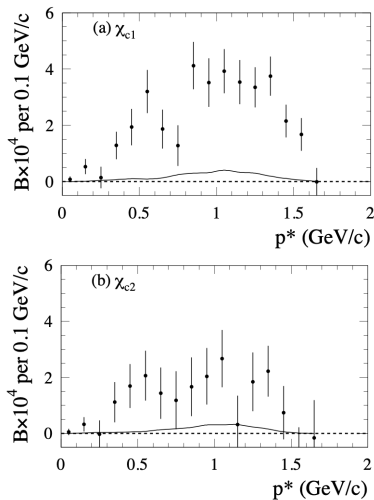
Similar suppression of M_X cut dependence for normalized angular observables A_{FB} , F_T

- BaBar measured the differential branching fractions of $B \rightarrow \{J/\psi, \psi', \chi_{c1}, \chi_{c2}\} X_s$ with feed-down to $\psi \rightarrow \ell^+ \ell^-$ and hadronic tagging of the X_s system

BaBar [0207097]

- The charmonium energy in the B frame is directly related to M_X since q^2 is fixed to a resonance, but results were presented in the laboratory frame (Could Belle/II improve on this?)





Belle [1512.02672]

- An update of $\text{Br}(B \rightarrow X_s \nu \bar{\nu})$ in the Standard Model is timely on the theory side:
 - Leading power upgraded from NLO $\rightarrow$ N³LO QCD ($\rightarrow$ NNLO for spectrum)
 - Power corrections are much better known including now $1/m_b^3$
- Result for the total rate is larger and more precise than previous estimates
Several sources of scale and parametric uncertainty at the 2-3% level remain
- $\sim 30\%$ of the spectrum survives a cut $q^2 < 4 \text{ GeV}^2$, so it may be useful (with enough statistics) to measure the cut rate
- Predictions with cuts on M_X in principle do-able with larger uncertainties
- Measurements of inclusive charmonium production $B \rightarrow (c\bar{c})X_s$ may be useful to test/train hadronization models (important also for $\bar{B} \rightarrow X_s \ell^+ \ell^-$)