

Hadronic decays of charmed hadron and CP violation at Belle (II)

Longke LI (李龙科)

On behalf of the Belle II Collaboration

Hunan Normal University



12th International Workshop on Charm Physics (CHARM 2025)
May 14, 2025 at Shanghai

Outline

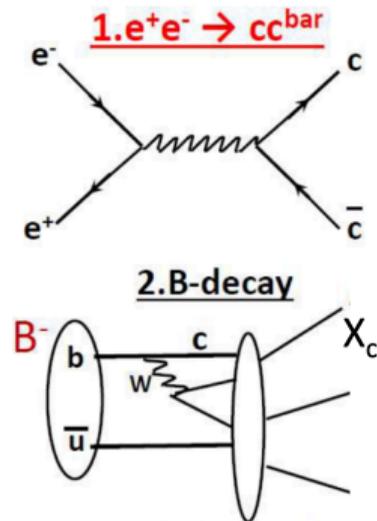
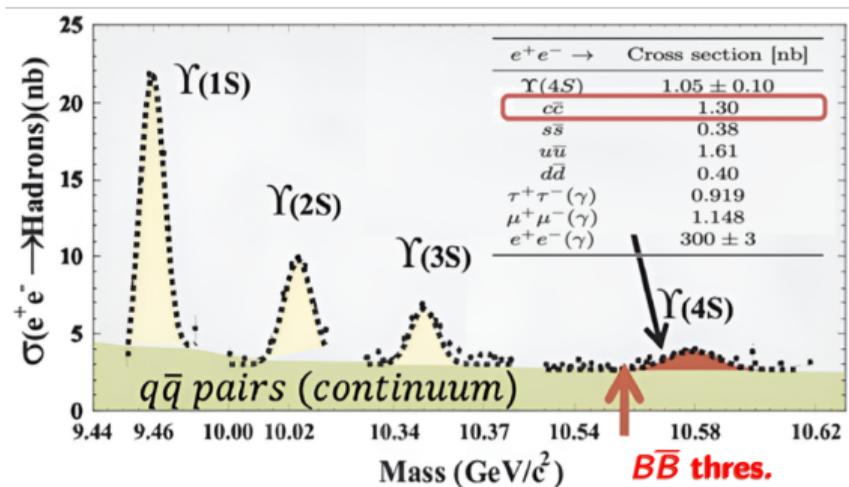
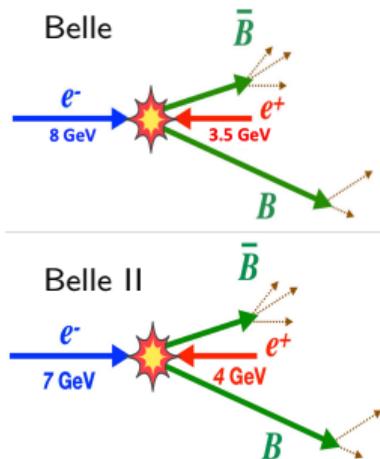
- 1 Charm sample at Belle (II)
- 2 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$
- 3 $A_{CP}(D^{0,+} \rightarrow \pi^{0,+} \pi^0)$
- 4 $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$
- 5 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
- 6 $\mathcal{B}(\Xi_c^+ \rightarrow BP)$
- 7 Summary

Outline

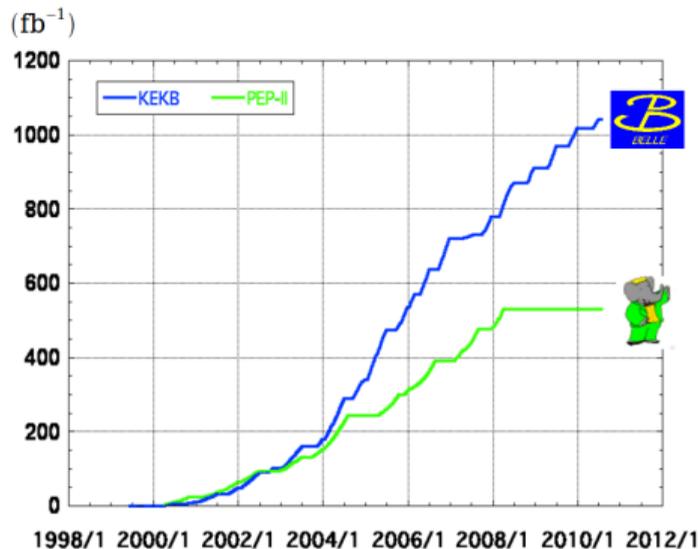
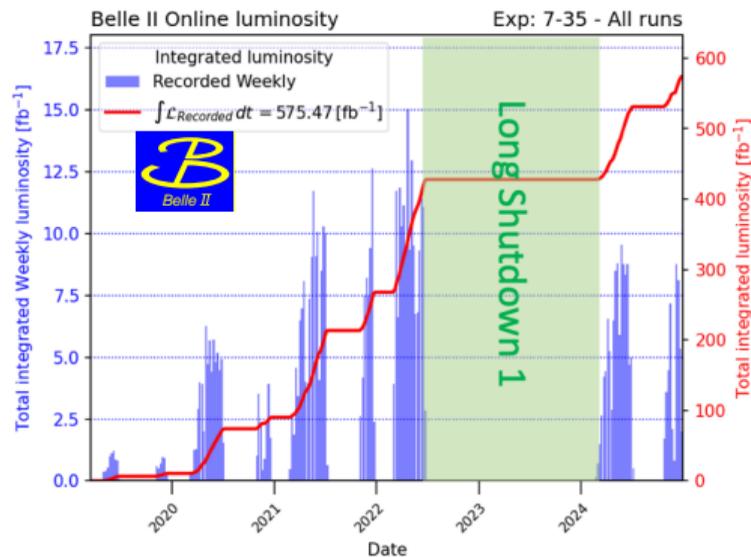
- 1 Charm sample at Belle (II)
- 2 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$
- 3 $A_{CP}(D^{0,+} \rightarrow \pi^{0,+} \pi^0)$
- 4 $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$
- 5 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
- 6 $\mathcal{B}(\Xi_c^+ \rightarrow BP)$
- 7 Summary

Charm production at Belle and Belle II

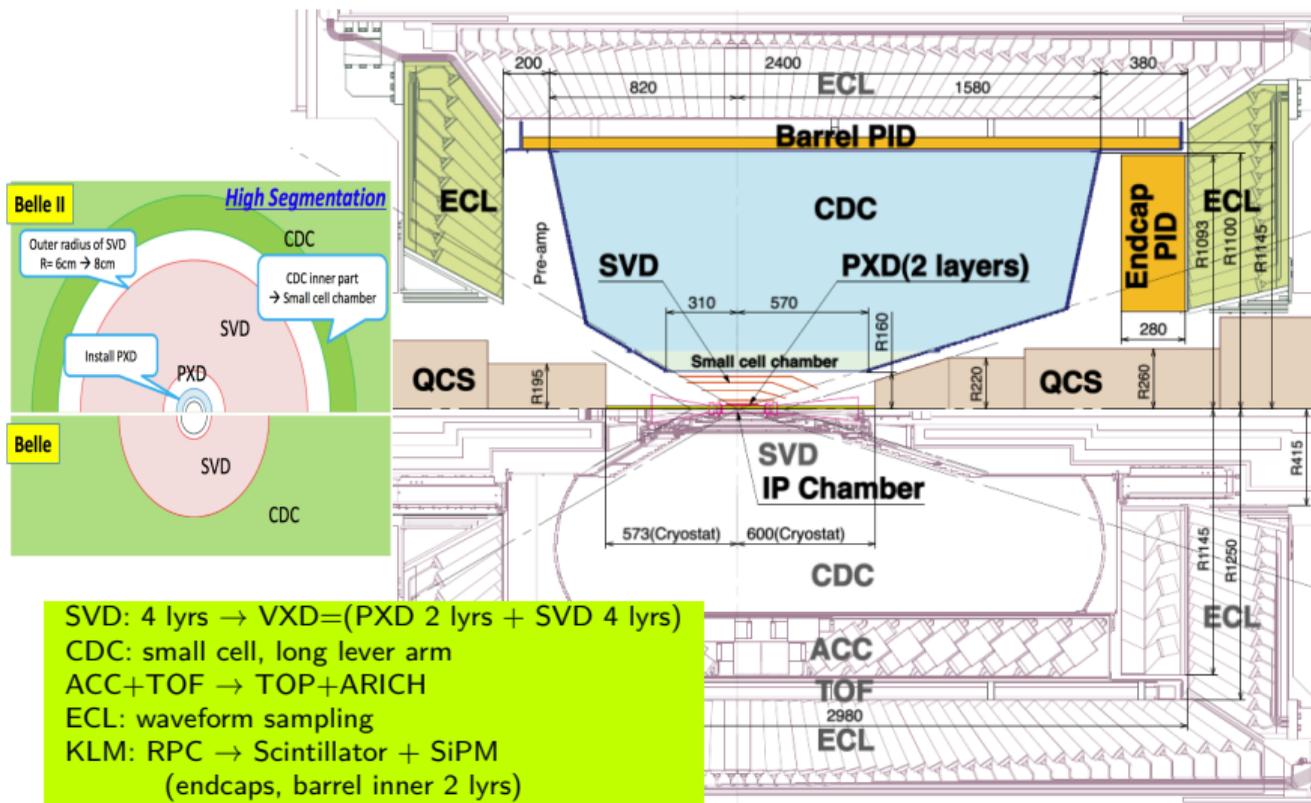
- At Belle (II), e^+e^- mainly collide at 10.58 GeV to make $\Upsilon(4S)$ resonance decaying into $B\bar{B}$ in 96% of the time.
- Meanwhile, continuum processes $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) have large cross sections.
- Two ways to produce the charm sample: $e^+e^- \rightarrow c\bar{c}$ ($\sigma = 1.3$ nb), and $B \rightarrow$ charm decays.



Luminosity at Belle (II)

Integrated luminosity of B factories**> 1 ab⁻¹****On resonance:**Y(5S): 121 fb⁻¹Y(4S): 711 fb⁻¹Y(3S): 3 fb⁻¹Y(2S): 25 fb⁻¹Y(1S): 6 fb⁻¹**Off reson./scan:**~ 100 fb⁻¹**~ 550 fb⁻¹****On resonance:**Y(4S): 433 fb⁻¹Y(3S): 30 fb⁻¹Y(2S): 14 fb⁻¹**Off resonance:**~ 54 fb⁻¹In Dec. 2024, SuperKEKB made new W.R. $5.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ 

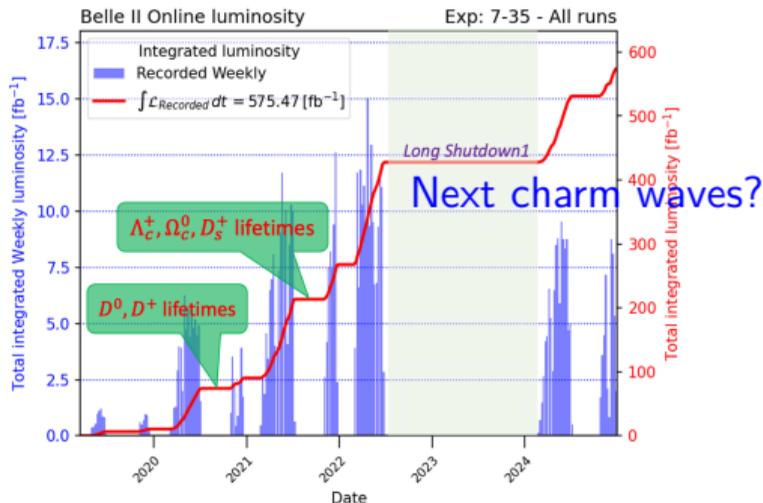
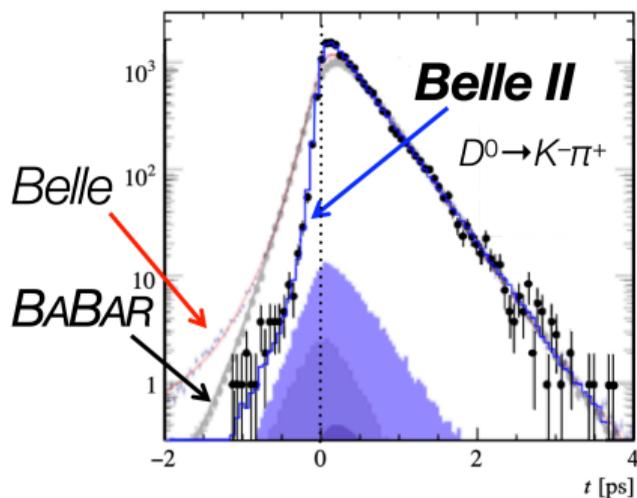
Detector: Belle II Vs. Belle



Charm lifetimes

PRL 127, 211801 (2021); PRL 130, 071802 (2023); PRD 107, L031103 (2023); PRL 131, 171803 (2023)

- Hadron lifetimes are difficult to calculate theoretically, as they depend on nonperturbative arising from QCD.
- Comparing calculated values with measured values improves our understanding of QCD. [(FLAG) EPJ C 82, 869 (2022)]
- Based on early datasets, Belle II **reported the most precise charm lifetimes**: $\tau(D^0) = 410.5 \pm 1.1 \pm 0.8$ fs, $\tau(D^+) = 1030.4 \pm 4.7 \pm 3.1$ fs, $\tau(D_s^+) = 499.5 \pm 1.7 \pm 0.9$ fs, and $\tau(\Lambda_c^+) = 203.20 \pm 0.89 \pm 0.77$ fs; and **confirmed the new charmed baryon lifetime hierarchy** found by LHCb $\tau(\Omega_c^0)$ result.



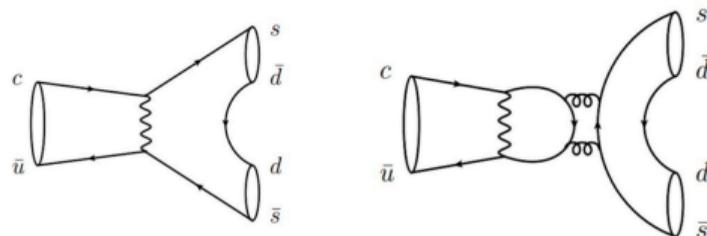
Outline

- 1 Charm sample at Belle (II)
- 2 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$
- 3 $A_{CP}(D^{0,+} \rightarrow \pi^{0,+} \pi^0)$
- 4 $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$
- 5 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
- 6 $\mathcal{B}(\Xi_c^+ \rightarrow BP)$
- 7 Summary

$A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ measurement using D^{*+} -tagged sample

(B+B2) PRD 111, 012015 (2025)

- The time-integrated CP asymmetry $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = \frac{\Gamma(D^0 \rightarrow K_S^0 K_S^0) - \Gamma(\bar{D}^0 \rightarrow K_S^0 K_S^0)}{\Gamma(D^0 \rightarrow K_S^0 K_S^0) + \Gamma(\bar{D}^0 \rightarrow K_S^0 K_S^0)}$.
- It may be enhanced to be an observable level (the 1% level) within the Standard Model, due to the interference of $c \rightarrow us\bar{s}$ and $c \rightarrow ud\bar{d}$ amplitudes. [PRD 99, 113001 (2019), PRD 86, 014023 (2012), PRD 92, 054036 (2015)]

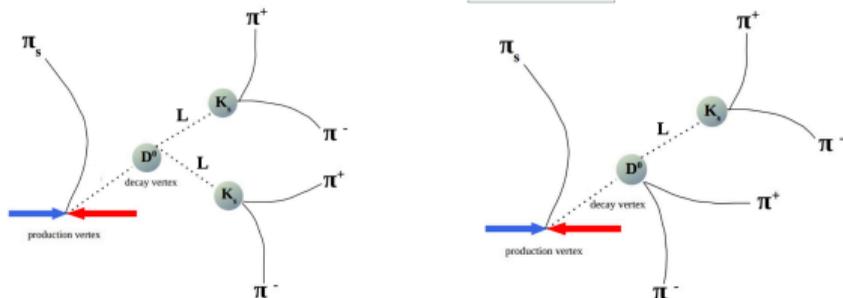


- World average: $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (-1.9 \pm 1.0)\%$ is dominated by
 - Belle (921 fb^{-1}): $A_{CP} = (-0.02 \pm 1.53 \pm 0.02 \pm 0.17)\%$ using $D^0 \rightarrow K_S^0 \pi^0$ as control mode [(Belle) PRL 119, 171801 (2017)]
 - LHCb (6 fb^{-1}): $A_{CP} = (-3.1 \pm 1.2 \pm 0.4 \pm 0.2)\%$ using $D^0 \rightarrow K^+ K^-$ as control mode [(LHCb) PRD 104, L031102 (2021)]
- $A_{CP}(D^0 \rightarrow K^+ K^-)$: recently improved by LHCb, uncertainty $< 0.1\%$ [(LHCb) PRL 131, 091802 (2023)]

$A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ measurement using D^{*+} -tagged sample

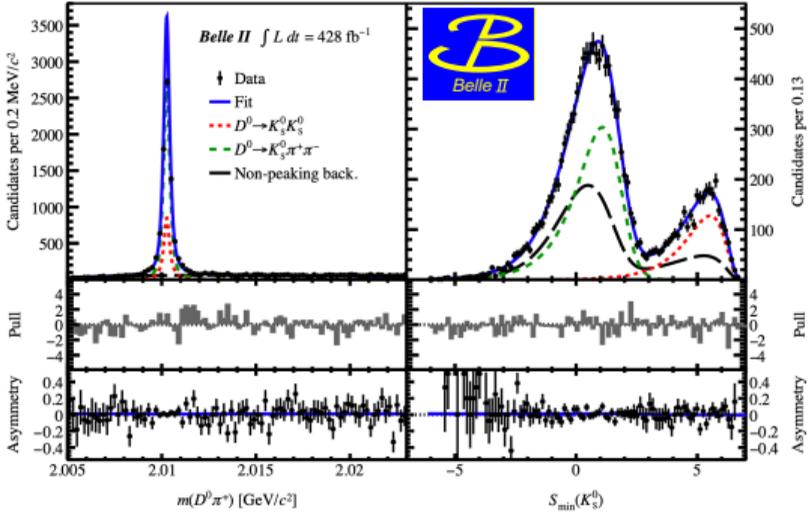
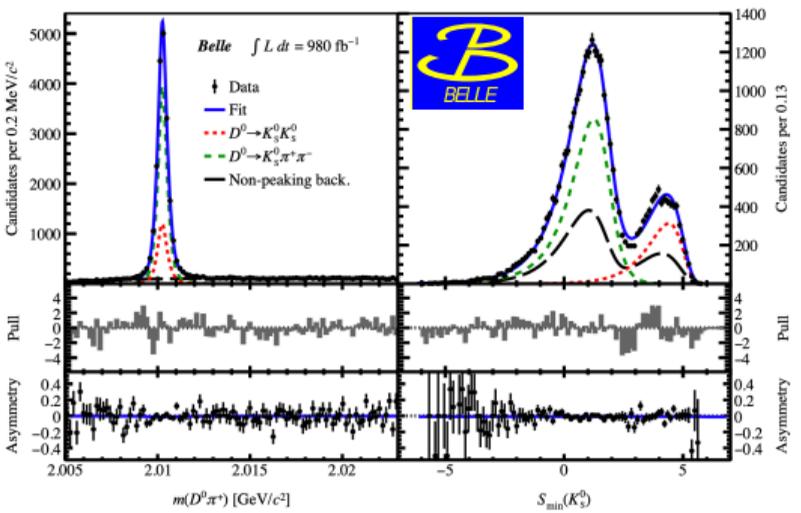
(B+B2) PRD 111, 012015 (2025)

- Measure $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ based on $D^{*+} \rightarrow D^0 \pi_s^+$ sample at B+B2 (totally 1.4 ab^{-1}).
- Raw asymmetry of $D^0 \rightarrow K \bar{K}$: $A_{\text{raw}}^{K \bar{K}} = \frac{N(D^0) - N(\bar{D}^0)}{N(D^0) + N(\bar{D}^0)} = A_{\text{FB}}^{D^{*+}} + A_{CP}^{K \bar{K}} + A_{\epsilon}^{\pi_s}$
- Use $D^0 \rightarrow K^+ K^-$ as control mode, and $A_{CP}^{K^+ K^-} = A_{CP}^{\text{dir}} + \Delta Y = (6.7 \pm 5.4) \times 10^{-4}$:
 - $A_{CP}^{\text{dir}}(D^0 \rightarrow K^+ K^-) = (7.7 \pm 5.7) \times 10^{-4}$: direct CP asymmetry [(LHCb) PRL 131, 091802 (2023)]
 - $\Delta Y = (-1.0 \pm 1.1) \times 10^{-4}$: CPV in mixing and in the interference between mixing and decay [(LHCb) PRD 104, 072010 (2021)]
- $A_{CP}^{K_S^0 K_S^0} = (A_{\text{raw}}^{K_S^0 K_S^0} - A_{\text{raw}}^{K^+ K^-}) + A_{CP}^{K^+ K^-}$ assuming that the nuisance asymmetries are identical between two decays, or that they can be made so by widening the control sample.
- Unbinned fit to $(m(D^0 \pi_s), S_{\text{min}})$ of D^0 and \bar{D}^0 candidates for $D^0 \rightarrow K_S^0 K_S^0$ decays.
 - Flight significance variable $S_{\text{min}} = \log(\min(L_i/\sigma_i))$: separate the peaking background $D^0 \rightarrow K_S^0 \pi^+ \pi^-$.



$A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ measurement using D^{*+} -tagged sample

(B+B2) PRD 111, 012015 (2025)



● Belle: $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (-1.1 \pm 1.6 \pm 0.1)\%$

Belle II: $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (-2.2 \pm 2.3 \pm 0.1)\%$

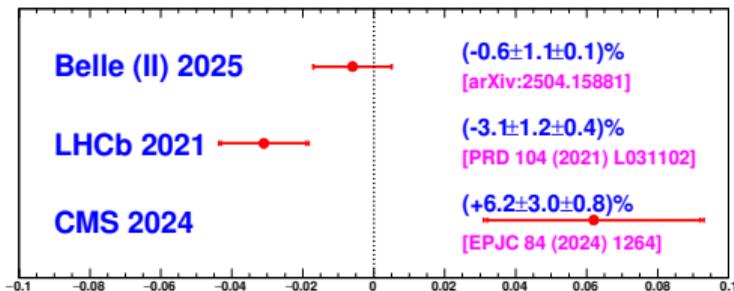
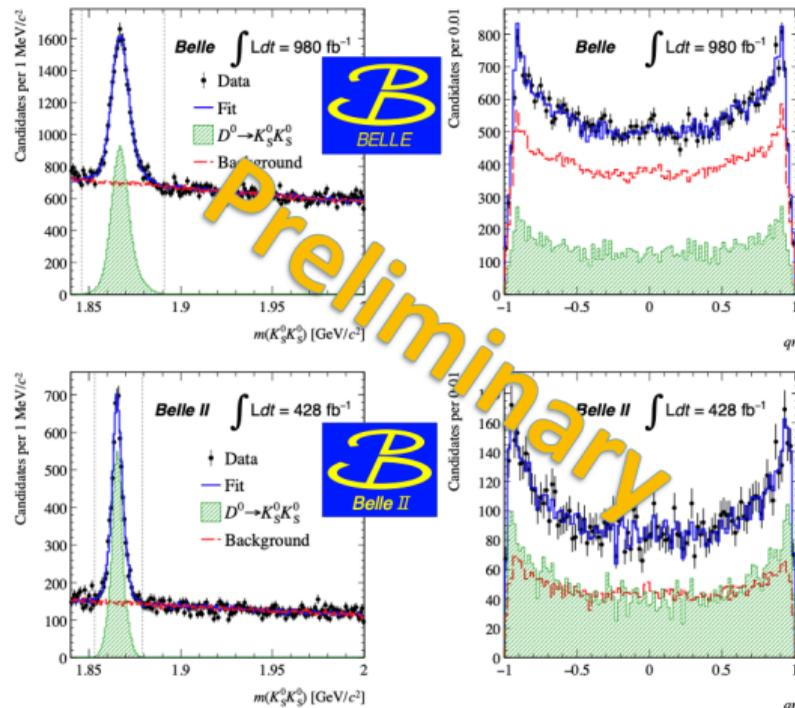
● Combined $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (-1.4 \pm 1.3 \pm 0.1)\%$: comparable to the world-best result: $\sigma_{\text{LHCb}} = 1.3\%$

● Belle(II)+LHCb average: $(-2.3 \pm 0.9)\%$ vs. CMS: $(6.2 \pm 3.1)\%$: 2.6σ diff. \Rightarrow preciser result needed



$A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ measurement using an independent sample (B+B2) arXiv:2504.15881 (preliminary)

- Using an independent sample tagged by opposite-side flavor tagging for $e^+e^- \rightarrow c\bar{c}$ events [(B2) PRD 107, 112010 (2023)]
- Candidates that are also reconstructed in the D^{*+} -tagged analysis in previous slide are removed.
- Belle sample (980 fb⁻¹):
 $N_{\text{sig}} = 14490 \pm 340$ and $A_{CP} = (+2.5 \pm 2.7 \pm 0.4)\%$
- Belle II sample (428 fb⁻¹):
 $N_{\text{sig}} = 5180 \pm 120$ and $A_{CP} = (-0.1 \pm 3.0 \pm 0.3)\%$
- Their combined results based on such independent sample:
 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (+1.3 \pm 2.0 \pm 0.2)\%$
- Combining it with previous result from D^{*+} -tagged sample:
 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (-0.6 \pm 1.1 \pm 0.1)\%$ **most precise**



Outline

- 1 Charm sample at Belle (II)
- 2 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$
- 3 $A_{CP}(D^{0,+} \rightarrow \pi^{0,+} \pi^0)$
- 4 $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$
- 5 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
- 6 $\mathcal{B}(\Xi_c^+ \rightarrow BP)$
- 7 Summary

CPV searches in isospin-related $D^{0,+} \rightarrow \pi^{0,+} \pi^0$ modes

- The following sum-rule for CPV in $D \rightarrow \pi\pi$ decays; it helps to determine the source of CPV:

$$R = \frac{A_{CP}^{\text{dir}}(D^0 \rightarrow \pi^+ \pi^-)}{1 + \frac{\tau_{D^0}}{\mathcal{B}_{+-}} \left(\frac{\mathcal{B}_{00}}{\tau_{D^0}} - \frac{2}{3} \frac{\mathcal{B}_{+0}}{\tau_{D^+}} \right)} + \frac{A_{CP}^{\text{dir}}(D^0 \rightarrow \pi^0 \pi^0)}{1 + \frac{\tau_{D^0}}{\mathcal{B}_{00}} \left(\frac{\mathcal{B}_{+-}}{\tau_{D^0}} - \frac{2}{3} \frac{\mathcal{B}_{+0}}{\tau_{D^+}} \right)} + \frac{A_{CP}^{\text{dir}}(D^+ \rightarrow \pi^+ \pi^0)}{1 - \frac{3}{2} \frac{\tau_{D^+}}{\mathcal{B}_{+0}} \left(\frac{\mathcal{B}_{00}}{\tau_{D^0}} + \frac{\mathcal{B}_{+-}}{\tau_{D^0}} \right)}$$

- if $R \neq 0$, CPV from $\Delta I = 1/2$ amplitude; if $R = 0$ and at least one $A_{CP}^{\text{dir}} \neq 0$, CPV from a beyond-SM $\Delta I = 3/2$ amplitude.
 - the \mathcal{B} 's and τ have been well-measured (by BESIII/Belle II/etc.)
 - $A_{CP}^{\text{dir}}(D^0 \rightarrow \pi^+ \pi^-)$: precise; first evidence of direct CPV in a specific D decay (by LHCb).
- Raw asymmetry of $D^0 \rightarrow \pi^0 \pi^0$ from the $D^{*+} \rightarrow D^0 \pi_s^+$ sample:

$$A_{\text{raw}}(D^0 \rightarrow \pi^0 \pi^0) = A_{CP}(D^0 \rightarrow \pi^0 \pi^0) + A_{\text{prod}}^{D^{*+}} + A_{\epsilon}^{\pi_s}$$

- $A_{\text{prod}}^{D^{*+}}$: being an odd function of $\cos \theta^*$, i.e. the cosine of the charmed-meson polar angle in $e^+ e^-$ c.m.s
 - $A_{\epsilon}^{\pi_s}$: using tagged and untagged $D^0 \rightarrow K^- \pi^+$ samples.
- Time-integrated CP asymmetry: $A_{CP}(D^0 \rightarrow \pi^0 \pi^0) = A_{\text{avg}}^{\pi^0 \pi^0} - A_{\text{avg}}^{K\pi} + A_{\text{avg}}^{K\pi, \text{untag}}$

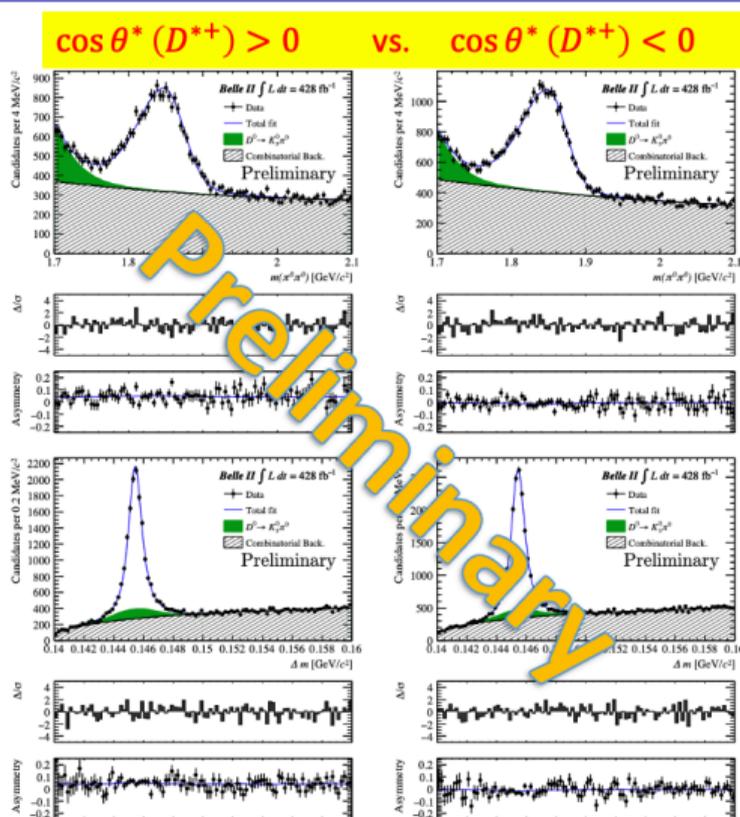
here $A_{\text{avg}}^f = (A^f(\cos \theta^* < 0) + A^f(\cos \theta^* > 0)) / 2$ where $f = \pi^0 \pi^0; K\pi; \text{untag}$.



$A_{CP}(D^0 \rightarrow \pi^0 \pi^0)$ at Belle II

(B2) arXiv:2505.02912 (preliminary)

- Utilizing data split in the forward and backward bins:
 $N_{\text{sig}} = 14\,100 \pm 130$ and $11\,550 \pm 110$.
- Result at Belle II (428 fb^{-1})
 $A_{CP}(D^0 \rightarrow \pi^0 \pi^0) = (+0.30 \pm 0.72 \pm 0.20)\%$
consistent with CP symmetry and with Belle (980 fb^{-1}):
 $(-0.03 \pm 0.64 \pm 0.10)\%$ [PRL 112 (2014) 211601]
- It's 15% less precision than Belle result; an improved precision per luminosity which leverages Belle II's superior capabilities in the reconstruction of neutral pions.
- Using our result, $A_{CP}^{\pi^+ \pi^-}$ and ΔY from LHCb, W.A. $A_{CP}^{\pi^+ \pi^0}$ and B 's and $\tau(D^{0,+})$, we have $R = (1.5 \pm 2.5) \times 10^{-3}$.
It shows that this measurement improves the precision of the sum rule by $\sim 20\%$ compared to the current determination by HFLAV [PRD 107 (2023) 052008].



$A_{CP}(D^+ \rightarrow \pi^+ \pi^0)$ at Belle II

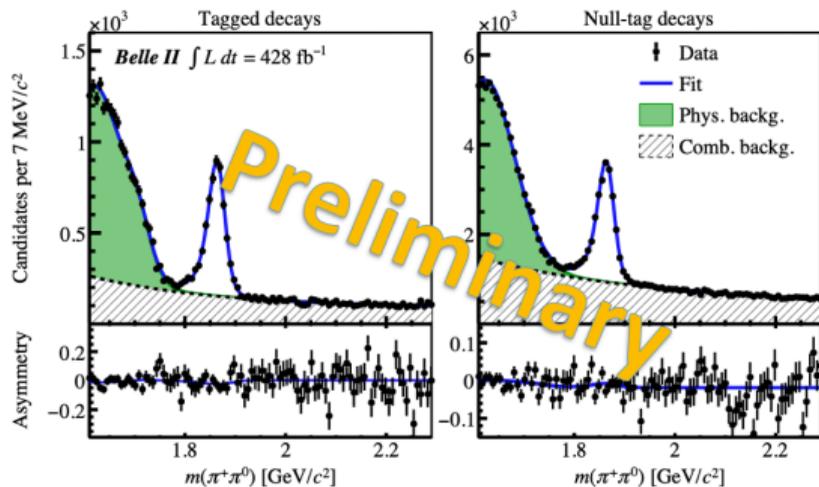
Preliminary result

- Utilizing a sample of $e^+e^- \rightarrow c\bar{c}$ data collected by Belle II (with high momentum requirement).
- Using $D^+ \rightarrow K_S^0 \pi^+$ to eliminate common asymmetry sources: A_{prod}^D and $A_{\varepsilon}^{\pi^+}$, thus CP asymmetry of interest:

$$A_{CP}^{\pi^+ \pi^0} = A_{\text{raw}}^{\pi^+ \pi^0} - A_{\text{raw}}^{K_S^0 \pi^+} + A_{\bar{K}^0}$$

- Combined result at Belle II (428 fb⁻¹):
 $A_{CP}(D^+ \rightarrow \pi^+ \pi^0) = (-1.8 \pm 0.9 \pm 0.1)\%$ (most precise)
- 30% improved precision compared to Belle (921 fb⁻¹):
 $(+2.31 \pm 1.24 \pm 0.23)\%$ [PRD 97 (2018) 011101]
- due to the substantially better purity achieved through an improved event selection, which exploits Belle II's superior performance in the reconstruction of neutral pions and displaced charged particles.

- Split sample: D^+ from $D^{*+} \rightarrow D^+ \pi^0$ decay or not.



$$N_{\text{sig}} = 5130 \pm 110$$

$$A_{CP} = (-3.9 \pm 1.8 \pm 0.2)\%$$

$$N_{\text{sig}} = 18510 \pm 240$$

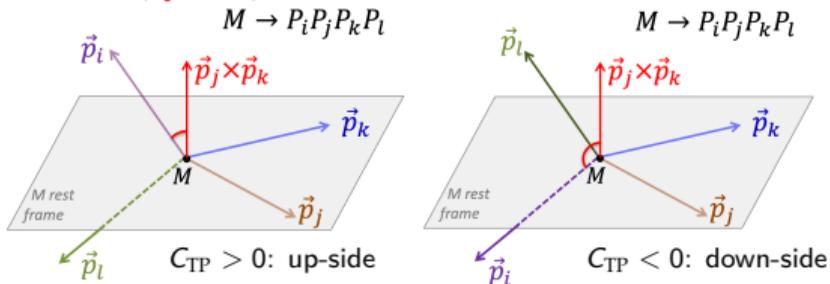
$$A_{CP} = (-1.1 \pm 1.0 \pm 0.1)\%$$

Outline

- 1 Charm sample at Belle (II)
- 2 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$
- 3 $A_{CP}(D^{0,+} \rightarrow \pi^{0,+} \pi^0)$
- 4 $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$
- 5 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
- 6 $\mathcal{B}(\Xi_c^+ \rightarrow BP)$
- 7 Summary

CPV searches in $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$ using triple-product correlations

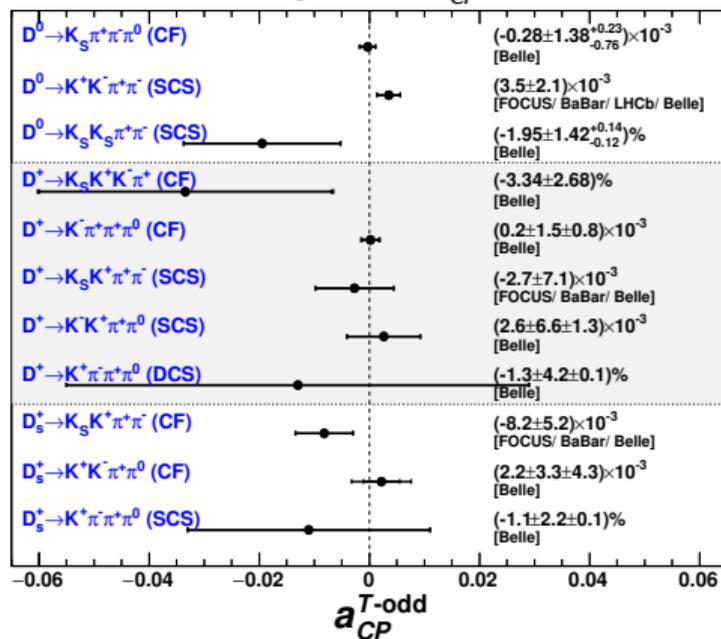
- CPV searches in several four-body D -decays at FOCUS, BABAR, LHCb and Belle using the **triple-product (TP)**:
 $C_{TP} = \vec{p}_i \cdot (\vec{p}_j \times \vec{p}_k)$.



C_{TP} asymmetry: so-called '**up-down asymmetry**'

- CPV in $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$: never been searched.
 They have large branching fractions $\mathcal{B} = 0.23\% (1.53\%)$
 $\Rightarrow \mathcal{O}(10^5)$ signals expected, inspiring us to obtain their precise $a_{CP}^{T\text{-odd}}$ results for the first time.

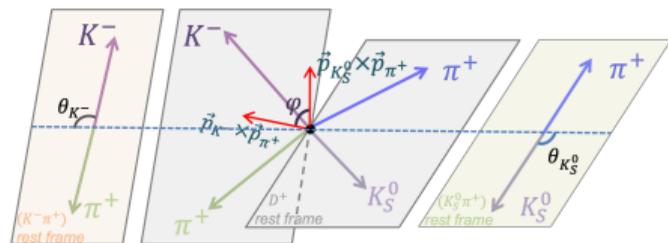
Current world averages of all $a_{CP}^{T\text{-odd}}$ measurements:



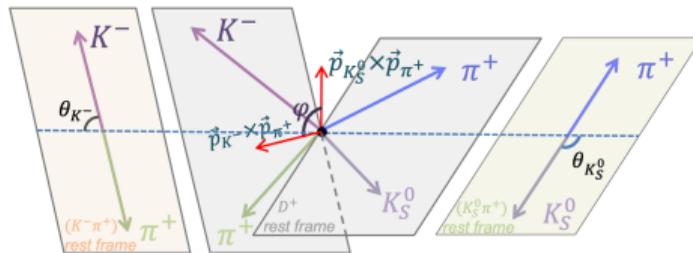
CPV searches in $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$ using quadruple-product correlations

- We do the first CPV search with the quadruple-product (QP): in $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$: $C_{QP} = (\vec{p}_{K^-} \times \vec{p}_{\pi_h^+}) \cdot (\vec{p}_{K_S^0} \times \vec{p}_{\pi_l^+})$, where the subscripts ('h' and 'l') denote the π^+ with higher and lower momentum, respectively, of two identical π^+ in the final state.
- $\cos \theta_{K_S^0} \cos \theta_{K^-}$ is used for charm CPV searches; its asymmetry is the so-called 'two-fold forward-backward asymmetry'^a.
- $D \rightarrow V_a V_b$ (e.g. $D_{(s)}^+ \rightarrow \bar{K}^{*0} K^{*+}$ is a dominant process) amplitude involves terms of
 - $d_{1,0}^2(\theta_a) d_{1,0}^2(\theta_b) \sin \varphi \propto \sin(2\theta_a) \sin(2\theta_b) \sin \varphi$,
 - $d_{1,0}^2(\theta_a) d_{1,0}^2(\theta_b) \cos \varphi \propto \sin(2\theta_a) \sin(2\theta_b) \cos \varphi$.
- two more observables for CPV searches^b:
 - $\cos \theta_{K_S^0} \cos \theta_{K^-} C_{TP}$: same sign as $\cos \theta_{K_S^0} \cos \theta_{K^-} \sin \varphi$,
 - $\cos \theta_{K_S^0} \cos \theta_{K^-} C_{QP}$: same sign as $\cos \theta_{K_S^0} \cos \theta_{K^-} \cos \varphi$.

$C_{QP} > 0$: \vec{p}_{K^-} at left-side of $\vec{p}_{K_S^0} \pi^+$ ($\vec{p}_{K_S^0} \times \vec{p}_{\pi^+}$) plane



$C_{QP} < 0$: \vec{p}_{K^-} at right-side of $\vec{p}_{K_S^0} \pi^+$ ($\vec{p}_{K_S^0} \times \vec{p}_{\pi^+}$) plane



C_{QP} asymmetry: so-called 'left-right asymmetry'.

^aZ.-H. Zhang, *Phys. Rev. D* **107**, L011301 (2023)

^bG. Durieux and Y. Grossman, *Phys. Rev. D* **92**, 076013 (2015)

Motivation: first CPV searches for $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$

(B+B2) JHEP 04 (2025) 036

- We search for CPV with a set of six kinematic observables (X) linked to various decay amplitude terms.
- For $D_{(s)}^+$ decays:
 - 1) $X = C_{TP} = \vec{p}_{K^-} \cdot (\vec{p}_{K_S^0} \times \vec{p}_{\pi_1^+})$: same sign as $\sin \varphi$.
 - 2) $X = C_{QP} = (\vec{p}_{K^-} \times \vec{p}_{\pi_h^+}) \cdot (\vec{p}_{K_S^0} \times \vec{p}_{\pi_l^+})$: same sign as $\cos \varphi$.
 - 3) $X = C_{TP} C_{QP}$: same sign as $\sin(2\varphi)$.
 - 4) $X = \cos \theta_{K_S^0} \cos \theta_{K^-}$.
 - 5) $X = \cos \theta_{K_S^0} \cos \theta_{K^-} C_{TP}$: same sign as $\cos \theta_{K_S^0} \cos \theta_{K^-} \sin \varphi$,
 - 6) $X = \cos \theta_{K_S^0} \cos \theta_{K^-} C_{QP}$: same sign as $\cos \theta_{K_S^0} \cos \theta_{K^-} \cos \varphi$.
- For $D_{(s)}^-$ decays: $\bar{X} = \eta_X^{CP} X$, where $\eta_X^{CP} = -1$ for (C_{TP} , $C_{TP} C_{QP}$ and $\cos \theta_{K_S^0} \cos \theta_{K^-} C_{TP}$); while $\eta_X^{CP} = +1$ for others.

- The kinematic asymmetries for $D_{(s)}^+$ and $D_{(s)}^-$ decays:

$$A_X(D_{(s)}^+) = \frac{N(X > 0) - N(X < 0)}{N(X > 0) + N(X < 0)} \quad \bar{A}_{\bar{X}}(D_{(s)}^-) = \frac{\bar{N}(\bar{X} > 0) - \bar{N}(\bar{X} < 0)}{\bar{N}(\bar{X} > 0) + \bar{N}(\bar{X} < 0)}$$

- CP-violating parameter: $a_{CP}^X = \frac{1}{2}(A_X - \bar{A}_{\bar{X}})$ (the factor 1/2 is required for normalization) to avoid a fake signal of CPV arising from the final state interaction (FSI) effects.



Signal yield extraction of $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$

(B+B2) JHEP 04 (2025) 036

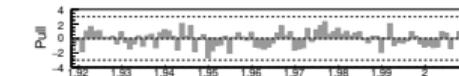
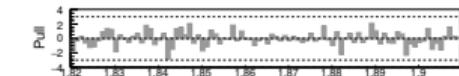
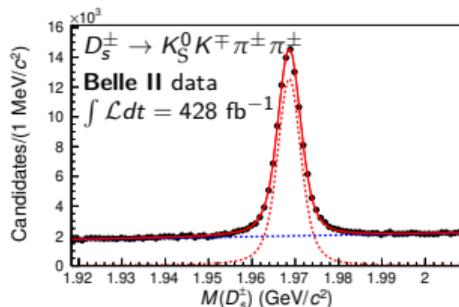
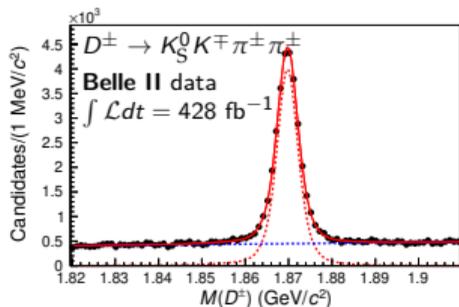
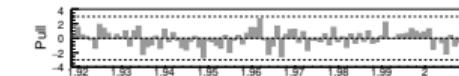
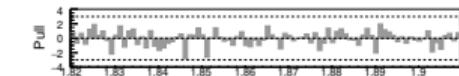
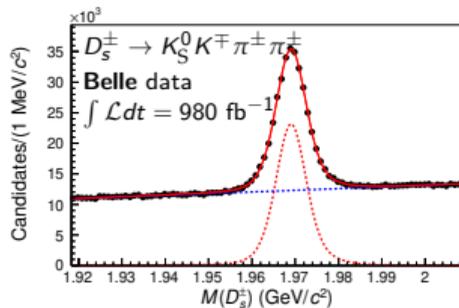
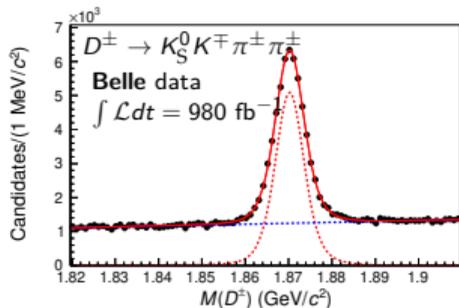


Table: Fitted signal and background yields in a window $\pm 10 \text{ MeV}/c^2$ around the nominal $D_{(s)}^+$ mass.

Component	$D^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$	
	Belle	Belle II
Signal (N_{sig})	44048 ± 288	26738 ± 199
Background (N_{bkg})	24844 ± 88	8964 ± 53
Ratio ($N_{\text{sig}}/N_{\text{bkg}}$)	1.8	3.0
Component	$D_s^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$	
	Belle	Belle II
Signal (N_{sig})	210743 ± 780	92000 ± 393
Background (N_{bkg})	245285 ± 280	39997 ± 114
Ratio ($N_{\text{sig}}/N_{\text{bkg}}$)	0.9	2.3



Measurement of $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$

(B+B2) JHEP 04 (2025) 036

► C_{TP} and C_{QP} at Belle II ($\int \mathcal{L} dt = 428 \text{ fb}^{-1}$):

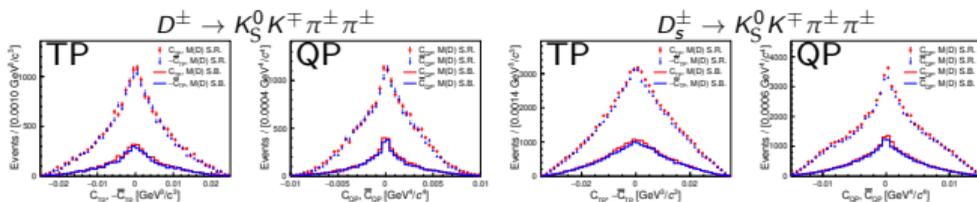


Table 2: Results for A_{CP}^X in $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$ decays, where $X = C_{TP}$ (1), C_{QP} (2), $C_{TP}C_{QP}$ (3), $\cos\theta_{K_S^0} \cos\theta_{K^-}$ (4), $C_{TP} \cos\theta_{K_S^0} \cos\theta_{K^-}$ (5), and $C_{QP} \cos\theta_{K_S^0} \cos\theta_{K^-}$ (6). The significance of the combined A_{CP}^X result from $A_{CP}^X = 0$ is listed in the last column.

Decay	X	A_{CP}^X (10^{-3}) at Belle	A_{CP}^X (10^{-3}) at Belle II	Combined A_{CP}^X (10^{-3})	Significance
D^+	(1)	$-4.0 \pm 5.9 \pm 3.0$	$-0.2 \pm 7.0 \pm 1.8$	$-2.3 \pm 4.5 \pm 1.5$	0.5σ
	(2)	$-1.0 \pm 5.9 \pm 2.5$	$-0.4 \pm 7.0 \pm 2.4$	$-0.7 \pm 4.5 \pm 1.7$	0.2σ
	(3)	$+6.4 \pm 5.9 \pm 2.2$	$+0.6 \pm 7.0 \pm 1.3$	$+3.9 \pm 4.5 \pm 1.1$	0.8σ
	(4)	$-4.7 \pm 5.9 \pm 3.0$	$-0.6 \pm 6.9 \pm 3.0$	$-2.9 \pm 4.5 \pm 2.1$	0.6σ
	(5)	$+1.9 \pm 5.9 \pm 2.0$	$-0.2 \pm 7.0 \pm 1.9$	$+1.0 \pm 4.5 \pm 1.4$	0.2σ
	(6)	$+14.9 \pm 5.9 \pm 1.4$	$+7.0 \pm 7.0 \pm 1.6$	$+11.6 \pm 4.5 \pm 1.1$	2.5σ
D_s^+	(1)	$-0.3 \pm 3.1 \pm 1.3$	$+1.0 \pm 3.9 \pm 1.1$	$+0.2 \pm 2.4 \pm 0.8$	0.1σ
	(2)	$+0.6 \pm 3.1 \pm 1.2$	$+2.0 \pm 3.9 \pm 1.4$	$+1.1 \pm 2.4 \pm 0.9$	0.4σ
	(3)	$+1.5 \pm 3.2 \pm 1.4$	$-2.7 \pm 3.9 \pm 1.7$	$-0.2 \pm 2.5 \pm 1.1$	0.1σ
	(4)	$-3.7 \pm 3.1 \pm 1.1$	$-6.3 \pm 3.9 \pm 1.2$	$-4.7 \pm 2.4 \pm 0.8$	1.8σ
	(5)	$-4.4 \pm 3.2 \pm 1.4$	$+0.8 \pm 3.9 \pm 1.4$	$-2.2 \pm 2.5 \pm 1.0$	0.8σ
	(6)	$-1.6 \pm 3.1 \pm 1.3$	$-0.0 \pm 3.9 \pm 1.7$	$-1.0 \pm 2.4 \pm 1.0$	0.4σ

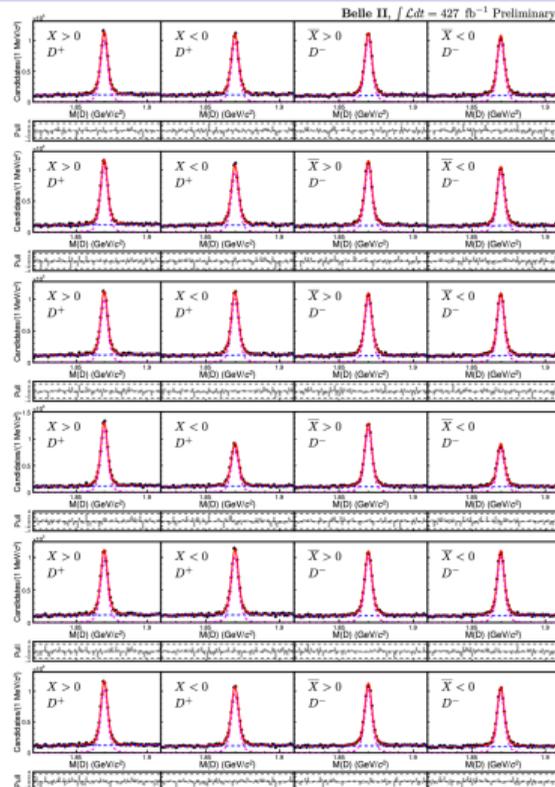
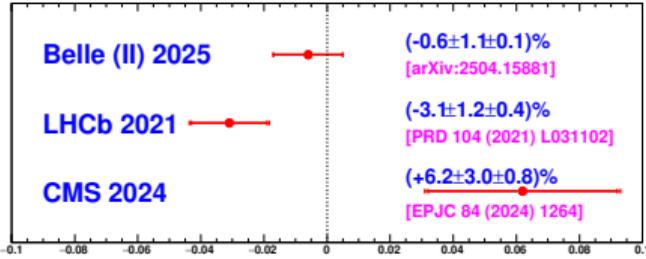


Figure 7: Fitted distributions for Belle II $D^{\pm} \rightarrow K_S^0 K^{\mp} \pi^{\pm} \pi^{\pm}$ data, for (top to bottom) $X = C_{TP}$, C_{QP} , $C_{TP}C_{QP}$, $\cos\theta_{K_S^0} \cos\theta_{K^-}$, $C_{TP} \cos\theta_{K_S^0} \cos\theta_{K^-}$, and $C_{QP} \cos\theta_{K_S^0} \cos\theta_{K^-}$.



Summary: charm CPV searches at Belle (II)

- $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ using D^{*+} and non- D^{*+} tagged samples at Belle (II):

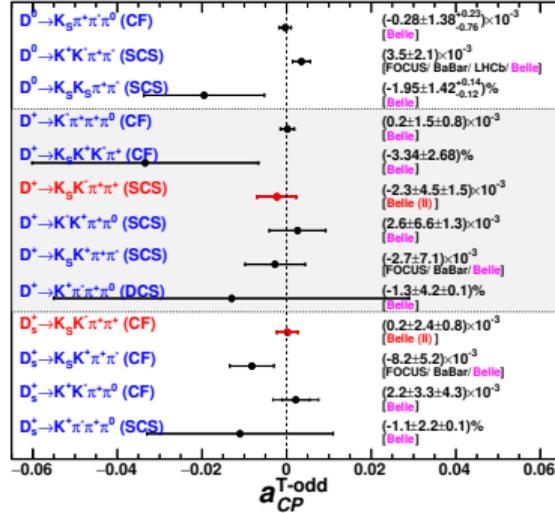


- $A_{CP}(D^{0,+} \rightarrow \pi^+, 0 \pi^0)$ at Belle II (428 fb^{-1}):
 $A_{CP}^{\pi^0 \pi^0} = (+0.30 \pm 0.72 \pm 0.20)\%$ (vs. $\sigma_{B1} = 0.65\%$)
 $A_{CP}^{\pi^+ \pi^0} = (-1.9 \pm 0.9 \pm 0.1)\%$ (vs. $\sigma_{B1} = 1.3\%$)

An improved precision per luminosity at Belle II, because of superior performance in the reconstruction of neutral pions and displaced charged particles.

- Working on more charm decays. Please stay tuned.

- $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$: first search for this mode.
 - $X = C_{TP/QP}, C_{TP} C_{QP}, \cos \theta_{K_S^0} \cos \theta_{K^-} (C_{TP/QP})$.
 - most precise $a_{CP}^{T\text{-odd}}$ for D^+ SCS decays and D_s^+ decays; and the other A_{CP}^X results: the first such measurements.



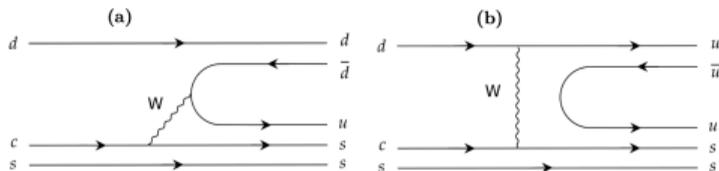
Outline

- 1 Charm sample at Belle (II)
- 2 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$
- 3 $A_{CP}(D^{0,+} \rightarrow \pi^{0,+} \pi^0)$
- 4 $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$
- 5 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
- 6 $\mathcal{B}(\Xi_c^+ \rightarrow BP)$
- 7 Summary

$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0) (P^0 = \pi^0 / \eta / \eta')$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$

(B+B2) JHEP 10 (2024) 045

- In hadronic weak decays of charmed baryons, **nonfactorizable contributions** from W -emission and W -exchange diagrams play an essential role and cannot be neglected; leading to **difficulties for theoretical predictions**.
- For $\Xi_c^0 \rightarrow \Xi^0 h^0$ decays, only the nonfactorizable amplitude contributes to the internal W -emission and W -exchange amplitudes.



- Parity violation study in charmed baryon decays via $1/2^+ \rightarrow 1/2^+ + 0^-$: decay asymmetry parameter α is related to interference between parity-violating S -wave and parity-conserving P -wave amplitudes.

$$\alpha \equiv 2 \cdot \text{Re}(S^* P) / (|S|^2 + |P|^2)$$

- It leads to an asymmetry in the angular decay distribution:

$$\frac{dN}{d \cos \theta_{\Xi_c^0}} \propto 1 + \alpha(\Xi_c^0 \rightarrow \Xi^0 h^0) \alpha(\Xi^0 \rightarrow \Lambda \pi^0) \cos \theta_{\Xi^0}$$

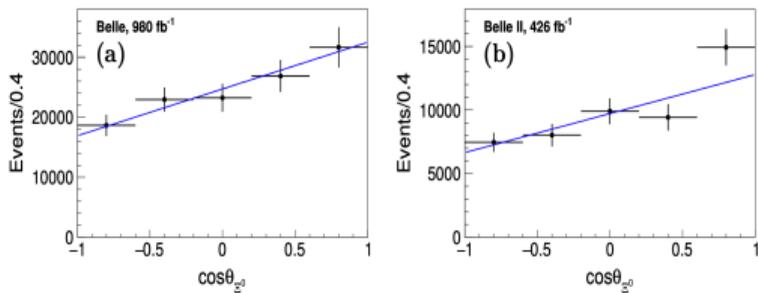
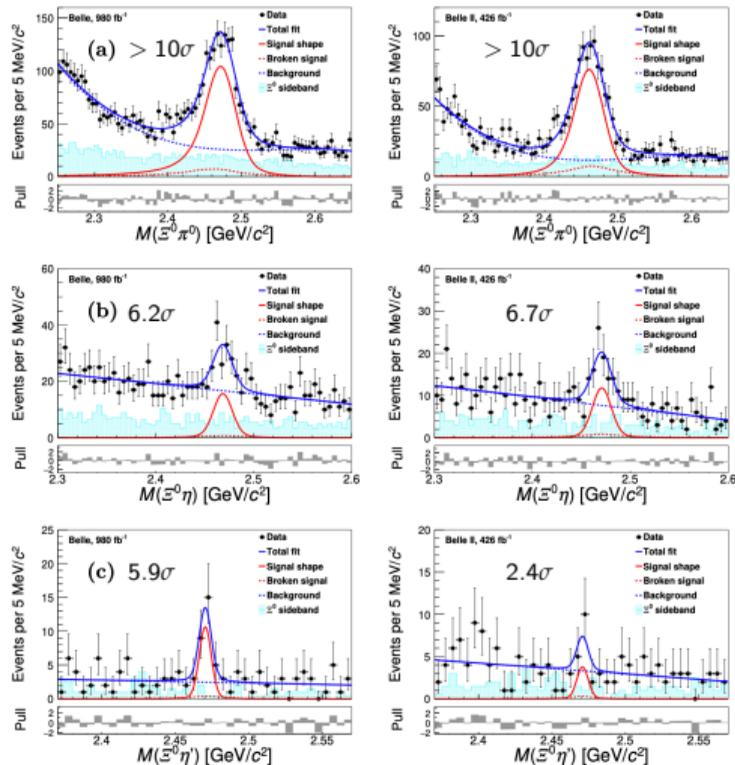
where $\theta_{\Xi^0} = \langle \vec{p}_\Lambda, -\vec{p}_{\Xi^0} \rangle$ in the Ξ^0 rest frame.

- Measurements of \mathcal{B} and α** : clarify the theoretical picture.

$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0) (P^0 = \pi^0 / \eta / \eta')$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$

(B+B2) JHEP 10 (2024) 045

- Based on 1.4 ab^{-1} dataset from Belle and Belle II.
- Using $\Xi_c^0 \rightarrow \Xi^- \pi^+$ as reference mode (obtained yields $N = 5.0 \times 10^4$)
- Combining \mathcal{B} -results from Belle/Belle II samples:
 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \pi^0) / \mathcal{B}_{\text{ref}} = 0.48 \pm 0.02 \pm 0.03$
 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta) / \mathcal{B}_{\text{ref}} = 0.11 \pm 0.01 \pm 0.01$
 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta') / \mathcal{B}_{\text{ref}} = 0.08 \pm 0.02 \pm 0.01$
- Simultaneous fit on efficiency-corrected yields in helicity angle bins for Belle and Belle II samples:
 $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0) = -0.90 \pm 0.15 \pm 0.23$



Outline

- 1 Charm sample at Belle (II)
- 2 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$
- 3 $A_{CP}(D^{0,+} \rightarrow \pi^{0,+} \pi^0)$
- 4 $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$
- 5 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
- 6 $\mathcal{B}(\Xi_c^+ \rightarrow BP)$
- 7 Summary

Measurement of $\mathcal{B}(\Xi_c^+ \rightarrow BP)$

(B+B2) arXiv:2503.17643, JHEP 03 (2025) 061

- \mathcal{B} -measurement for six hadronic weak decays of Ξ_c^+ baryon

- Using $\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$ as reference mode

- Two CF decays:

$$\mathcal{B}(\Xi_c^+ \rightarrow \Sigma^+ K_S^0) / \mathcal{B}_{\text{ref}} = (6.7 \pm 0.7 \pm 0.3)\%$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+) / \mathcal{B}_{\text{ref}} = (24.8 \pm 0.5 \pm 0.9)\%$$

- Four SCS decays:

$$\mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 K^+) / \mathcal{B}_{\text{ref}} = (1.7 \pm 0.3 \pm 0.1)\%$$

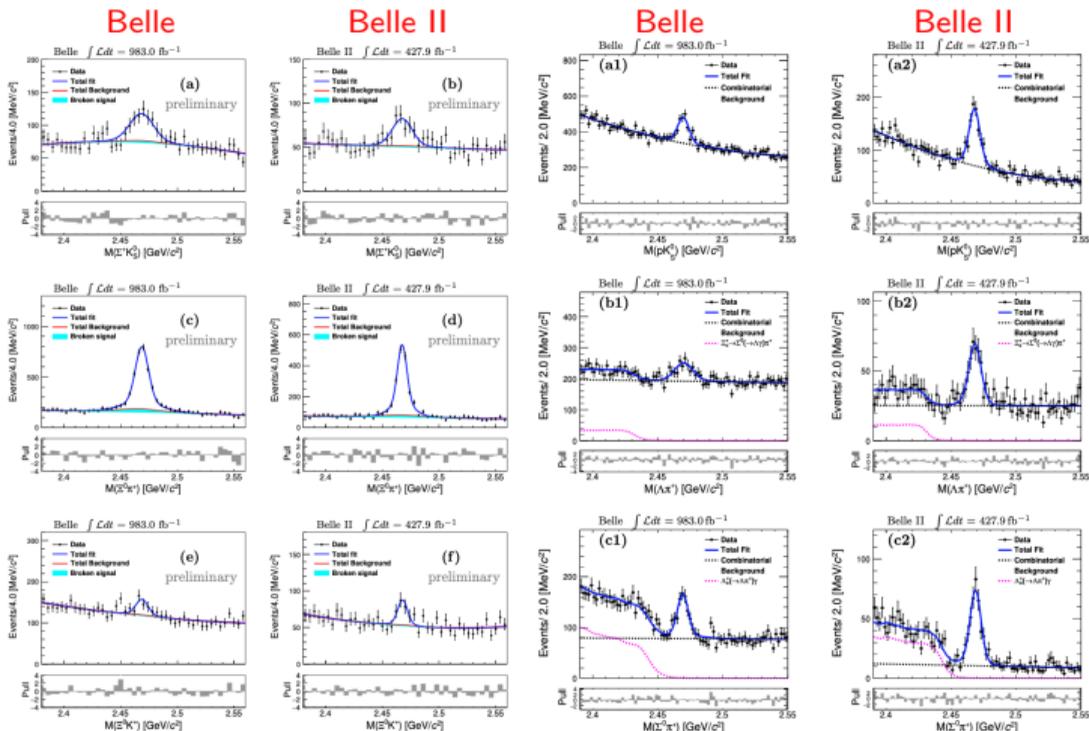
$$\mathcal{B}(\Xi_c^+ \rightarrow \rho K_S^0) / \mathcal{B}_{\text{ref}} = (2.47 \pm 0.16 \pm 0.07)\%$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Lambda \pi^+) / \mathcal{B}_{\text{ref}} = (1.56 \pm 0.14 \pm 0.09)\%$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Sigma^0 \pi^+) / \mathcal{B}_{\text{ref}} = (4.13 \pm 0.26 \pm 0.22)\%$$

- Belle II has better resolution and mostly has higher significance than Belle.

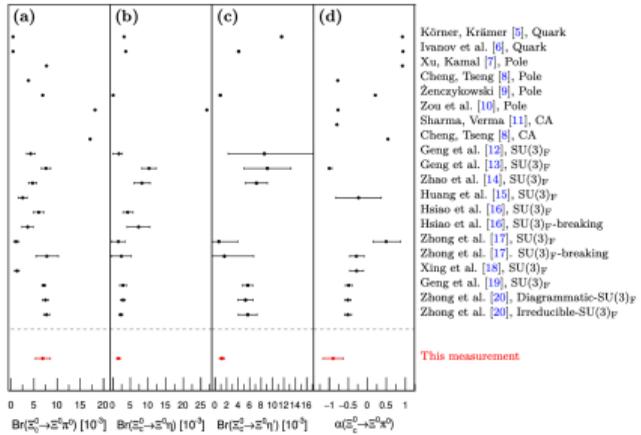
- These **SCS decays: first observed**, and may provide samples for CPV searches in charmed baryon in the future.



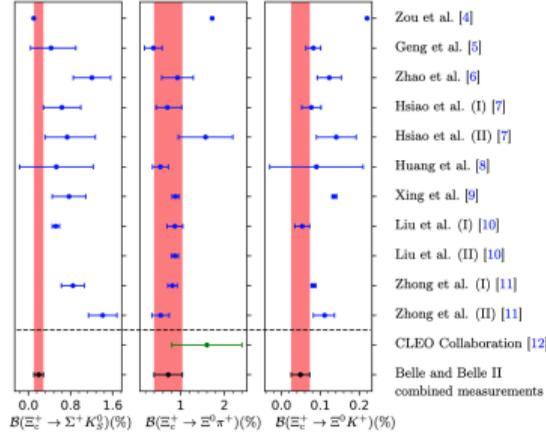
Summary of charmed baryon studies

● Based on B+B2 (1.4 ab^{-1}), we reported studies of 5 CF and 4 SCS decays of $\Xi_c^{0,+}$ baryons:

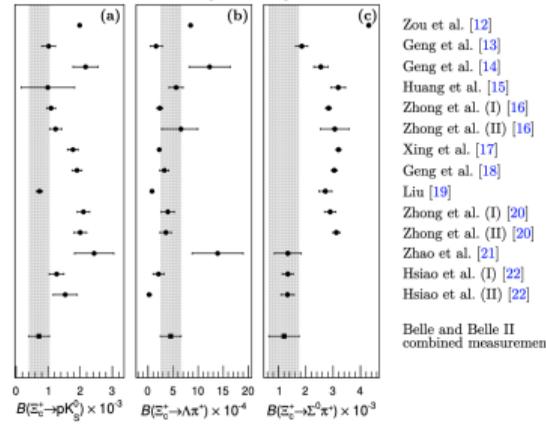
JHEP 10 (2024) 045



arXiv:2503.17643



JHEP 03 (2025) 061



- These **relative \mathcal{B} 's** are almost the **first or most precise** results, providing important inputs for theoretical studies.
- **Top priority** for Ξ_c physics: precise measurement of **absolute $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)$ and $\mathcal{B}(\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+)$** .

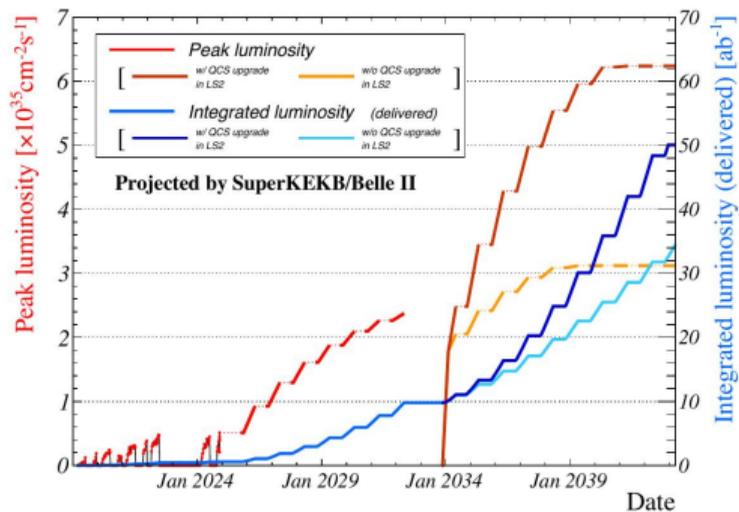


Outline

- 1 Charm sample at Belle (II)
- 2 $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$
- 3 $A_{CP}(D^{0,+} \rightarrow \pi^{0,+} \pi^0)$
- 4 $A_{CP}^X(D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+)$
- 5 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
- 6 $\mathcal{B}(\Xi_c^+ \rightarrow BP)$
- 7 **Summary**

Summary

- Belle II has collected dataset of 575 fb^{-1} and SuperKEKB made a W.R. luminosity: $5.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- After the first charm wave: precise charm lifetimes based on early dataset, we welcome new charm waves at Belle (II):
- Charm CPV in charmed meson decays:
 $D^0 \rightarrow K_S^0 K_S^0$, $D^{0,+} \rightarrow \pi^{0,+} \pi^0$, and $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$.
 new flavor-tagging method; new reference mode; new variables (C_{QP}); etc.
- Study of hadronic decays of charmed baryons:
 $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 P^0)$ and $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$, six Ξ_c^+ decays.
 Belle II has better purity/resolution and higher signal-noise-ratio than Belle.
- More studies on hadronic decays of charmed hadron and CPV searches based on current available datasets at Belle (II), and the final dataset (Belle II target luminosity 50 ab^{-1}) in the future. Please stay tuned.



Thanks for your attention.

谢谢!



Dr. Longke LI (李龙科)
School of Physics and Electronics
Hunan Normal University
36 LuShan Road, YueLu District
Changsha, Hunan, 410081, P. R. China

☎ (+86)-159-5693-4447

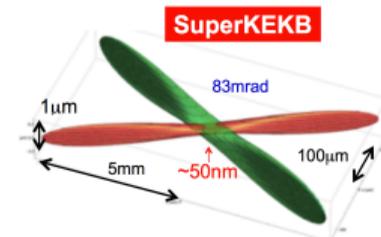
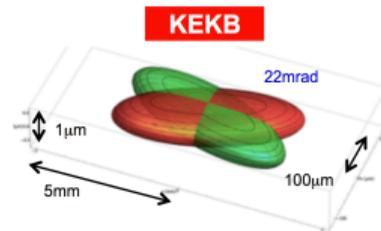
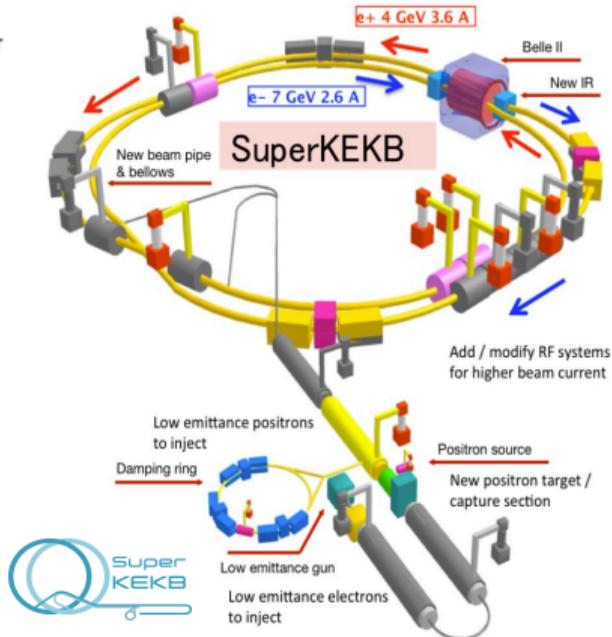
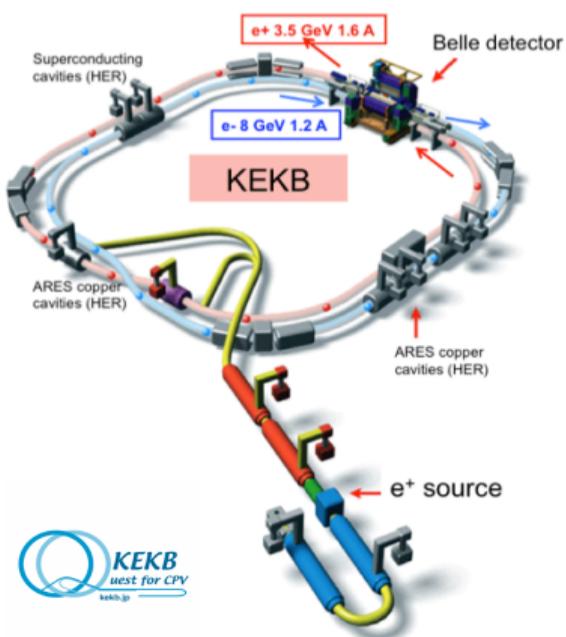
👤 lilongke_ustc

✉ lilongke@hunnu.edu.cn



from KEKB to SuperKEKB

- ▶ As 1st and 2nd generation B-factories, KEKB and SuperKEKB have many similarities, and more differences:
 - Damping ring added to have low emittance positrons / use 'Nano-beam' scheme by squeezing the beta function at the IP.
 - beam energy: admit lower asymmetry to mitigate Touschek effects / beam current: $\times 2$ to contribute to higher luminosity.
 - SuperKEKB achieved the luminosity record of $5.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$.



Comparison of available charm samples

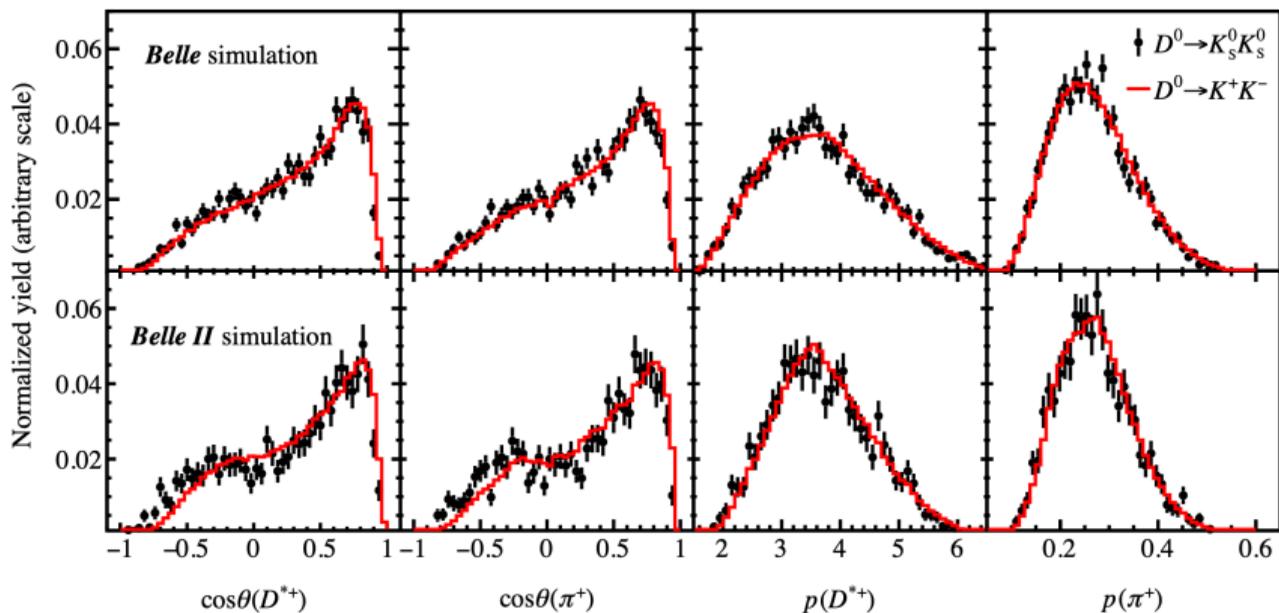
Experiment	Machine	C.M.	Luminosity(fb^{-1})	N_{prod}	Efficiency	Characters
	BEPC-II (e^+e^-)	3.77 GeV	20	$D^{0,+}: 10^8$	$\sim 10\text{-}30\%$	☺ extremely clean environment ☺ quantum coherence ☹ no boost, no time-dept analysis
		4.18-4.23 GeV 4.6-4.7 GeV	7.3 4.5	$D_s^+: 5 \times 10^6$ $\Lambda_c^+: 0.8 \times 10^6$		
	SuperKEKB (e^+e^-)	10.58 GeV	600 ($\rightarrow 50000$)	$D^0: 10^9 (\rightarrow 10^{11})$ $D_{(s)}^+: 10^8 (\rightarrow 10^{10})$ $\Lambda_c^+: 10^7 (\rightarrow 10^9)$	$\mathcal{O}(1\text{-}10\%)$	☺ high-efficiency detection of neutrals ☺ good trigger efficiency ☺ time-dependent analysis ☹ smaller cross-section than LHCb
			KEKB (e^+e^-)	10.58 GeV		
	LHC (pp)	7+8 TeV	1+2	5×10^{12}	$\mathcal{O}(0.1\%)$	☺ very large production cross-section ☺ large boost, excellent time resolution ☹ dedicated trigger required
		13 TeV	6+9 ($\rightarrow 23 \rightarrow 50$)	10^{13}		

Here uses $\sigma(D^0\bar{D}^0@3.77\text{ GeV})=3.61\text{ nb}$, $\sigma(D^+D^-@3.77\text{ GeV})=2.88\text{ nb}$, $\sigma(D_s^+D_s^-@4.17\text{ GeV})=0.967\text{ nb}$; $\sigma(c\bar{c}@10.58\text{ GeV})=1.3\text{ nb}$ where each $c\bar{c}$ event averagely has 1.1/0.6/0.3 $D^0/D^+/D_s^+$ yields; $\sigma(D^0@CDF)=13.3\text{ }\mu\text{b}$, and $\sigma(D^0@LHCb)=1661\text{ }\mu\text{b}$, mainly from *Int. J. Mod. Phys. A* **29**(2014)24,14300518.

- BESIII, Belle II, and LHCb experiments, with their advantages, are all ideal platforms for charm studies.
- They all are continuously collecting more datasets with increased luminosity in the foreseeable future.



Equalization of kinematic-parameter distributions of $D^0 \rightarrow K_S^0 K_S^0, K^+ K^-$



X-dependent efficiency in $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$

