

Status of Lepton Flavour Universality

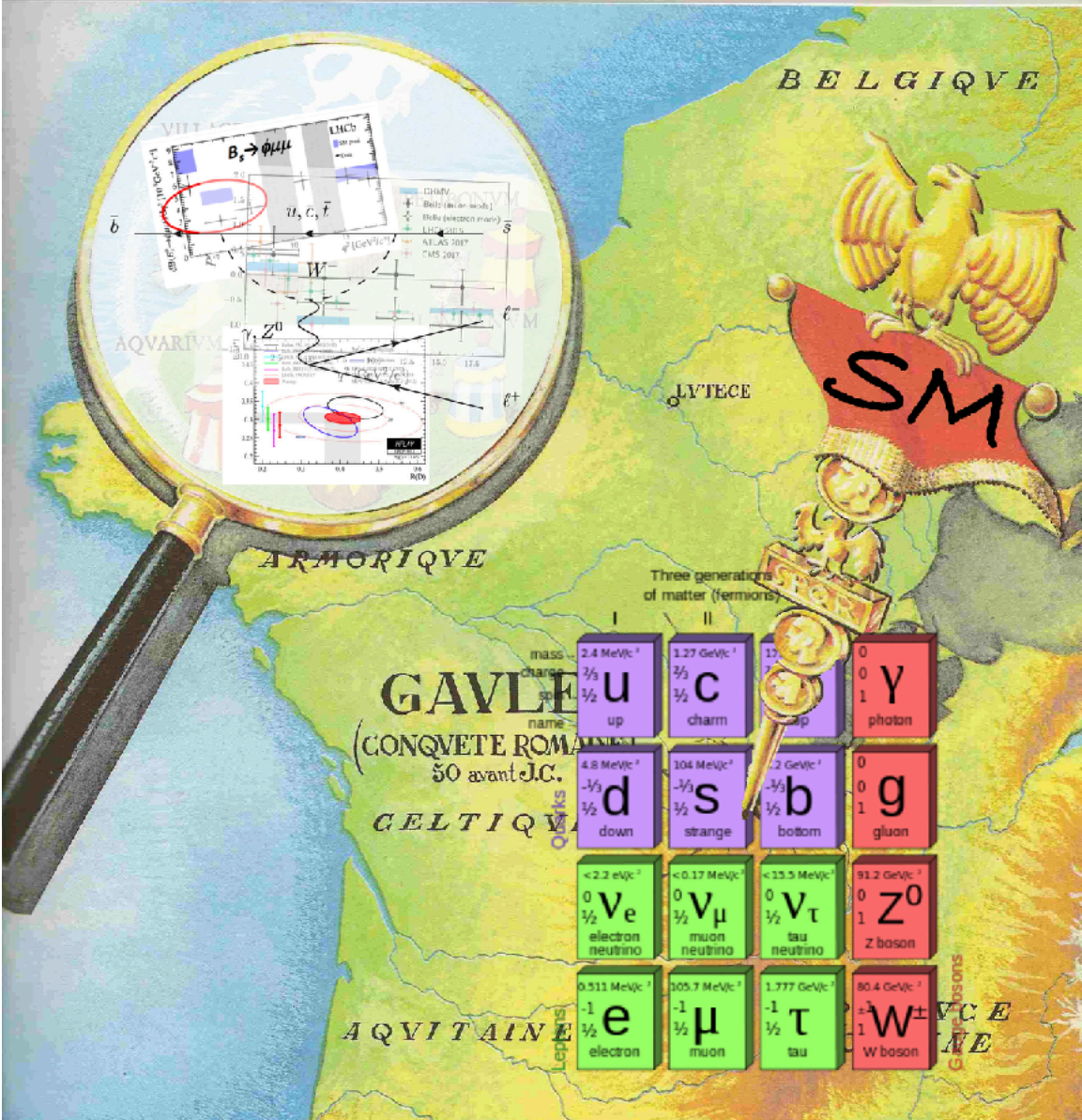
Virtual FSP Belle II Germany Meeting

Simon Wehle
14.09.2020 Hamburg



Motivation

- The **Standard Model (SM)** is very successful in describing the world at particle level
- Almost all SM predictions seem to fit experimental data precisely... **Almost?**



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- Almost all SM predictions seem to fit experimental data precisely... *Almost?*

The Flavour Anomalies



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(maybe only “local” anomalies...)

> 3.5σ enhanced $B \rightarrow D^{(*)}\tau\nu$ rates

3.3σ suppressed branching ratio of $B_s \rightarrow \phi\mu^+\mu^-$

$\sim 3\sigma$ tension between inclusive and exclusive determination of $|V_{ub}|$

$\sim 3\sigma$ tension between inclusive and exclusive determination of $|V_{cb}|$

> 3σ anomalies in angular distributions of $B \rightarrow K^*\ell\ell$

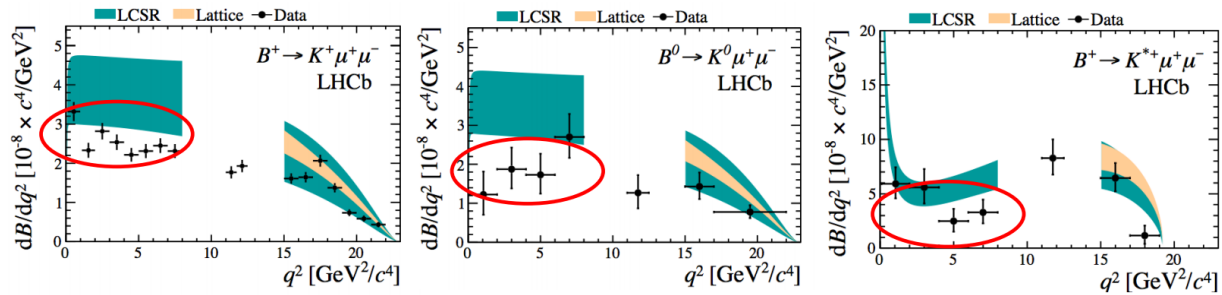
2.6σ lepton flavor non-universality in $B \rightarrow K^{(*)}\mu^+\mu^-$ vs. $B \rightarrow K^{(*)}e^+e^-$



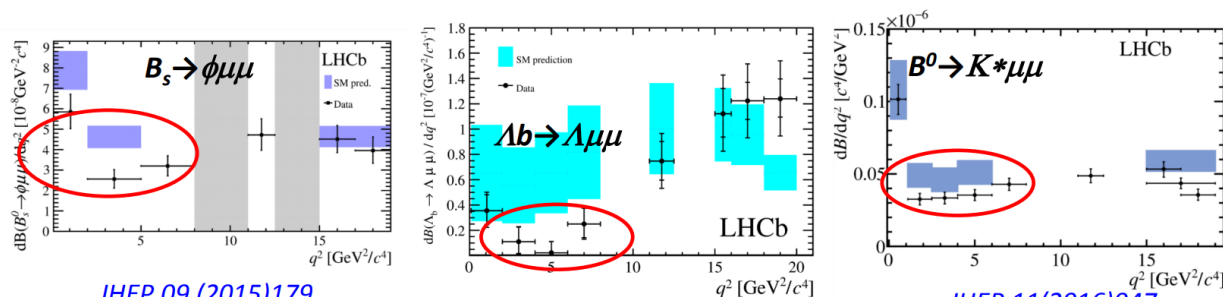
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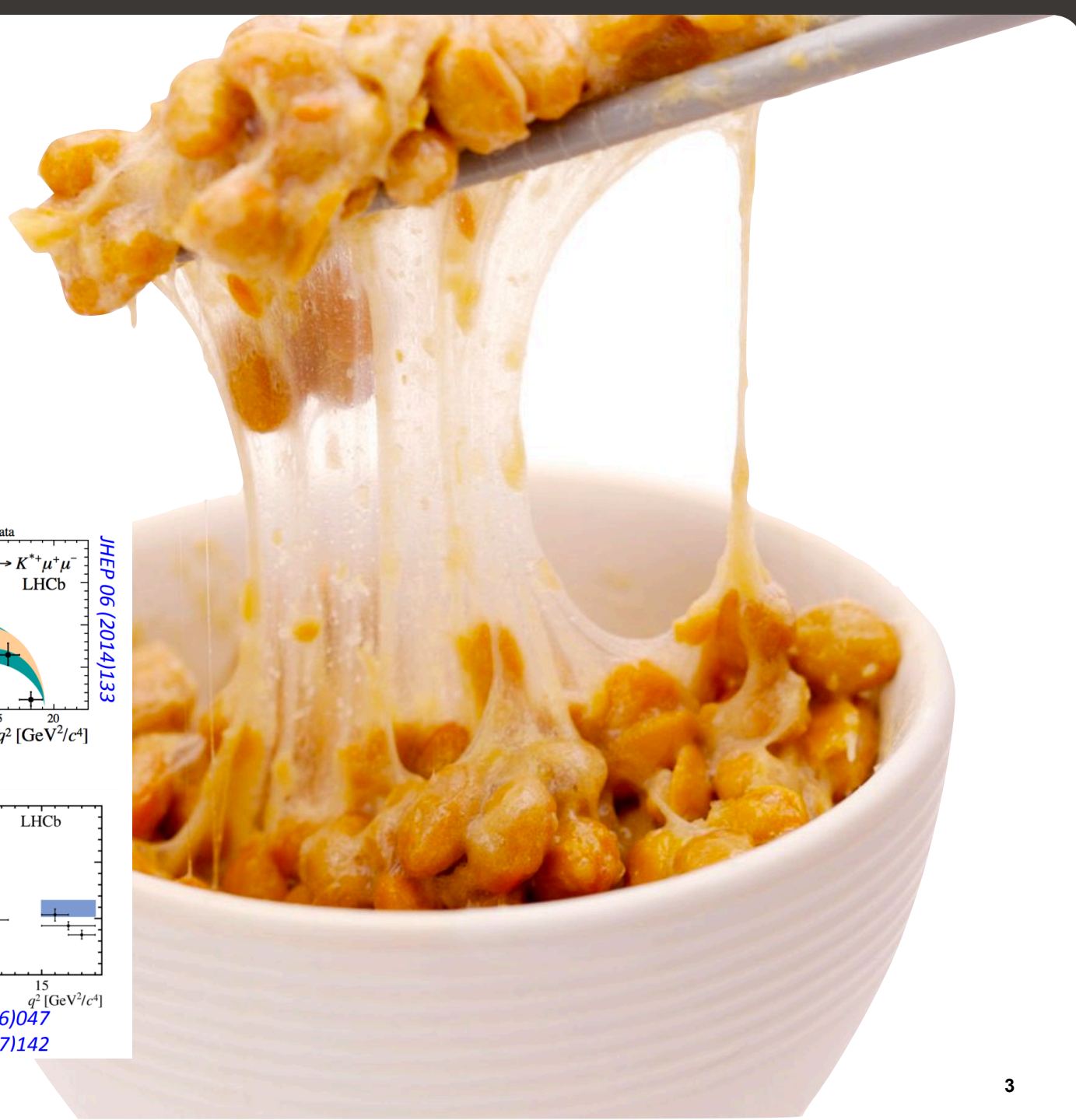
JHEP 06 (2014)133



JHEP 09 (2015)179

JHEP 06 (2015) 115

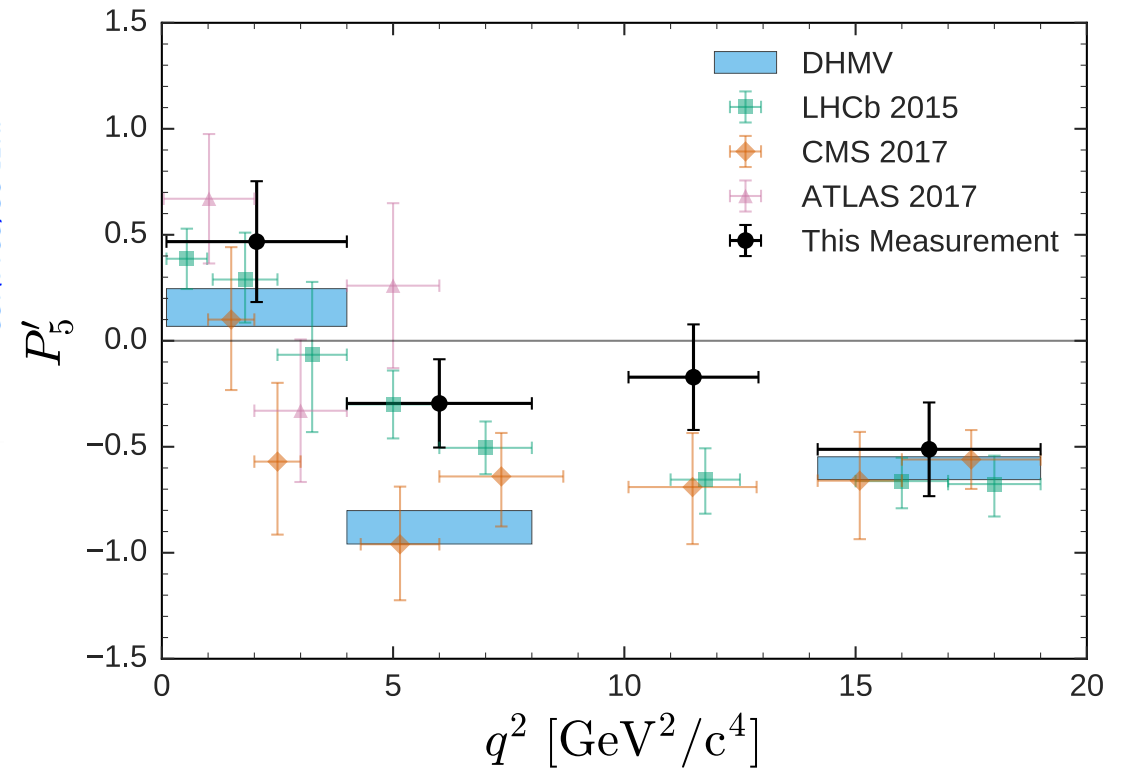
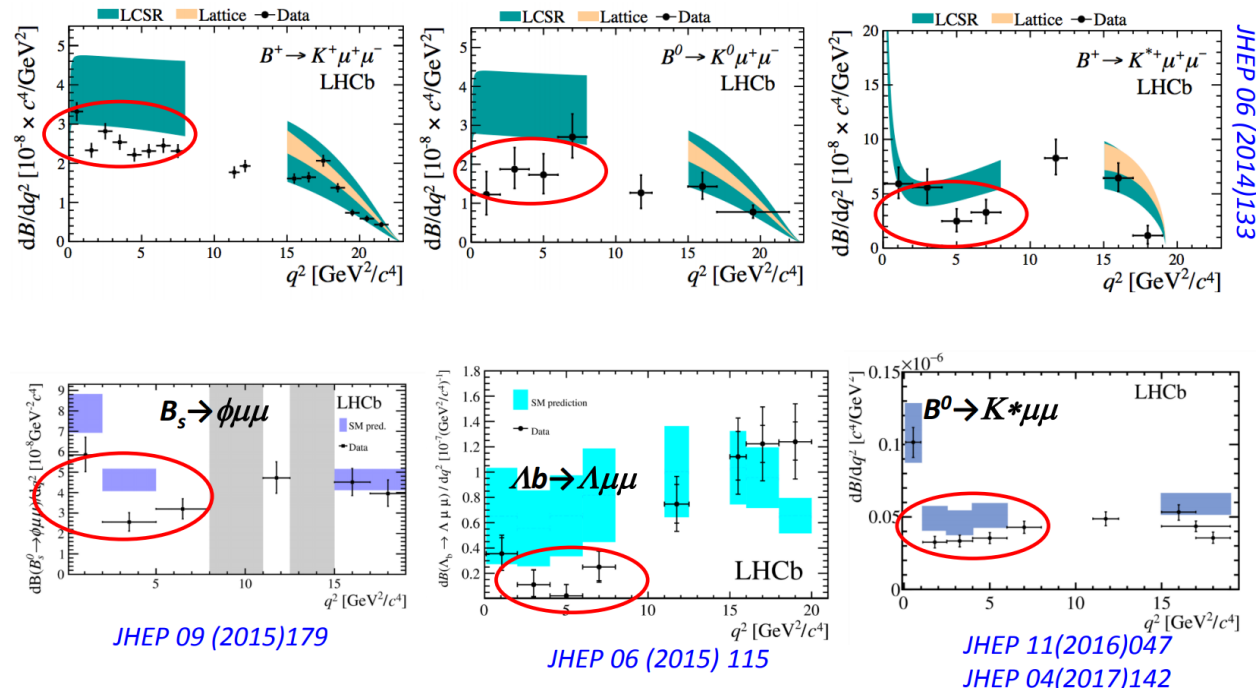
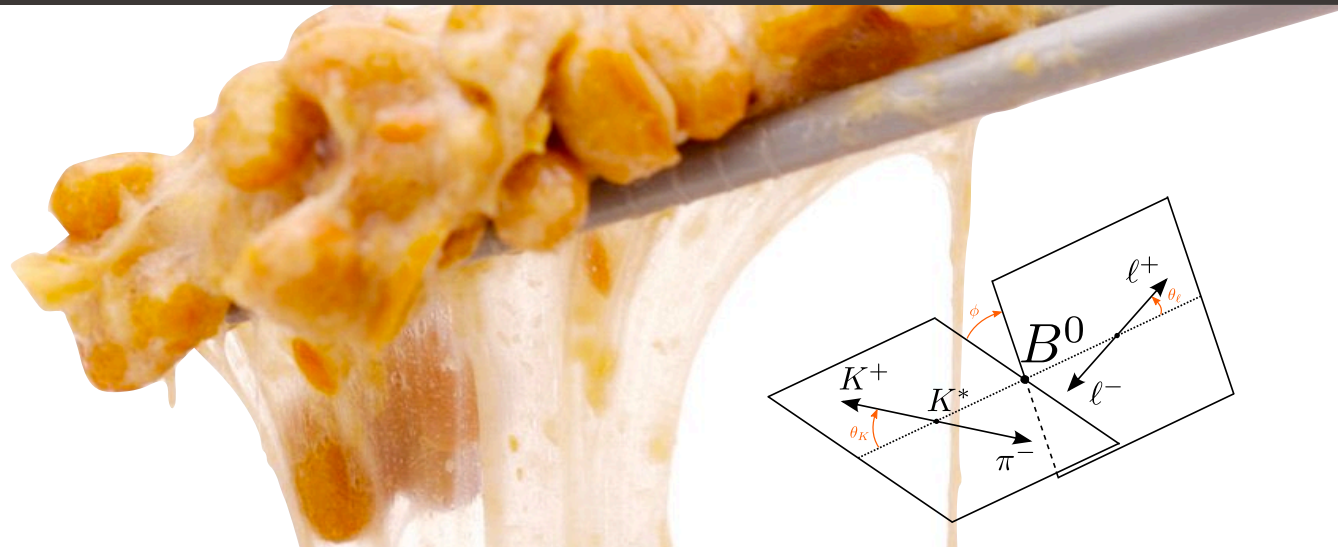
JHEP 11(2016)047
JHEP 04(2017)142



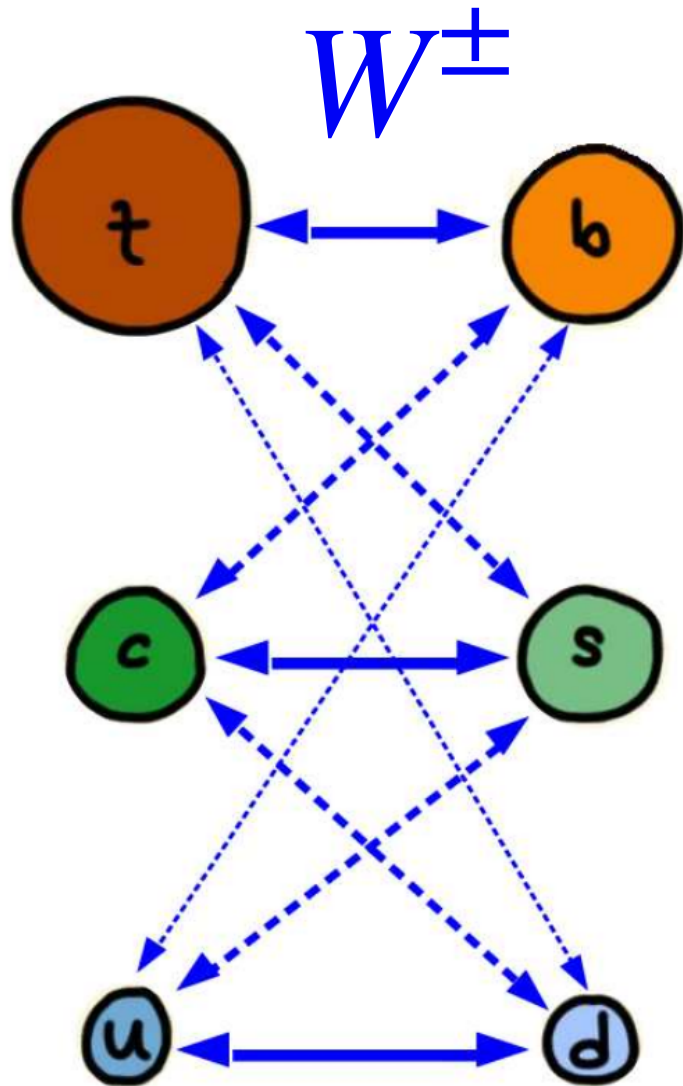
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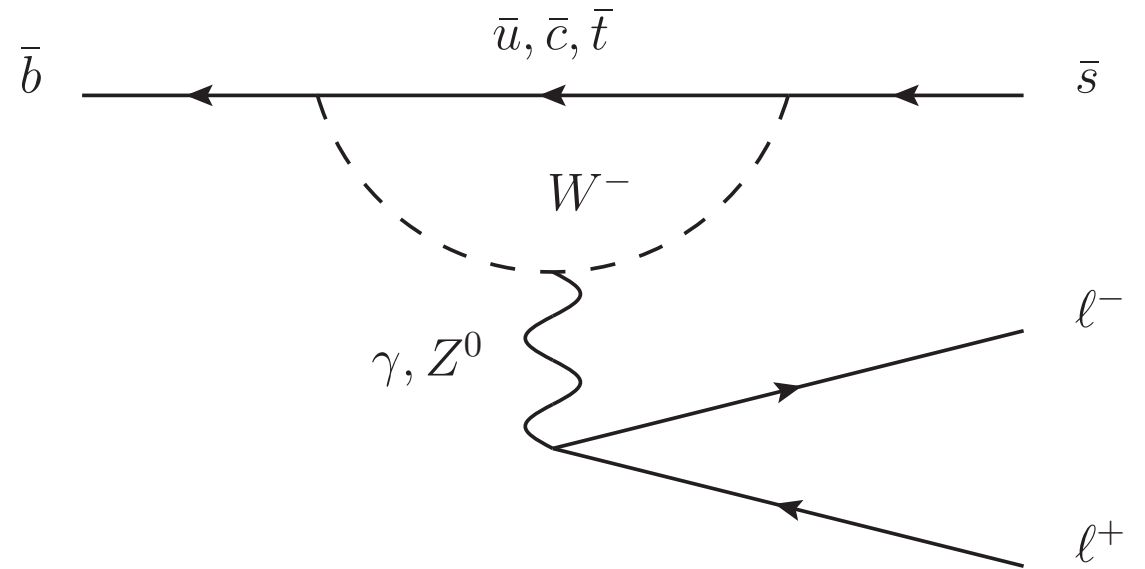
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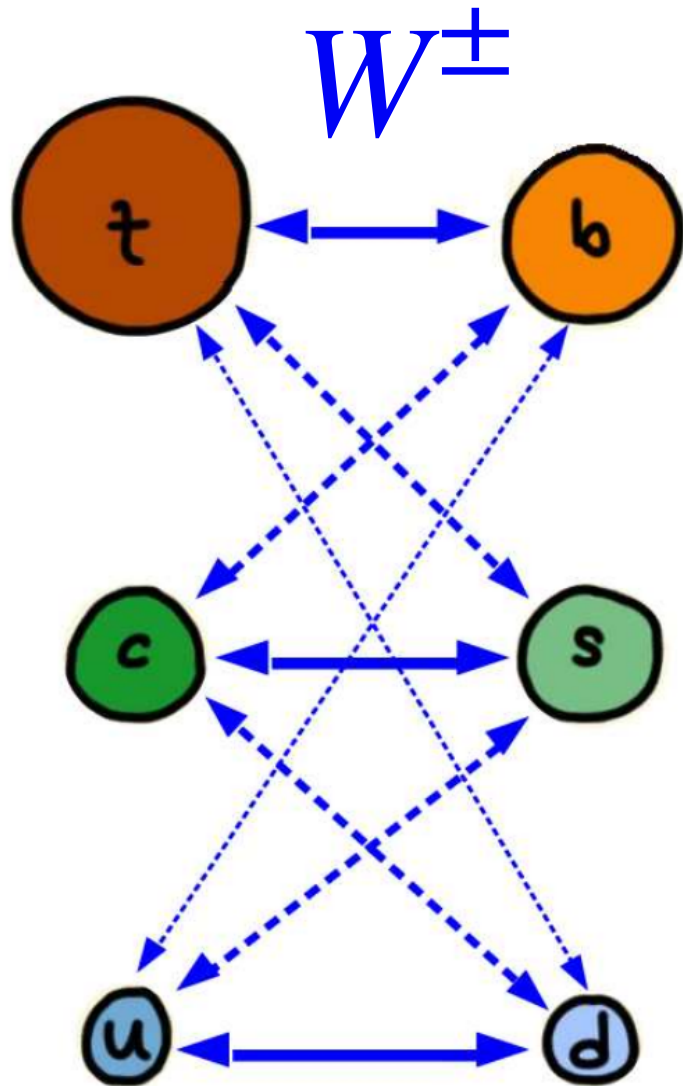
The $b \rightarrow s$ transition



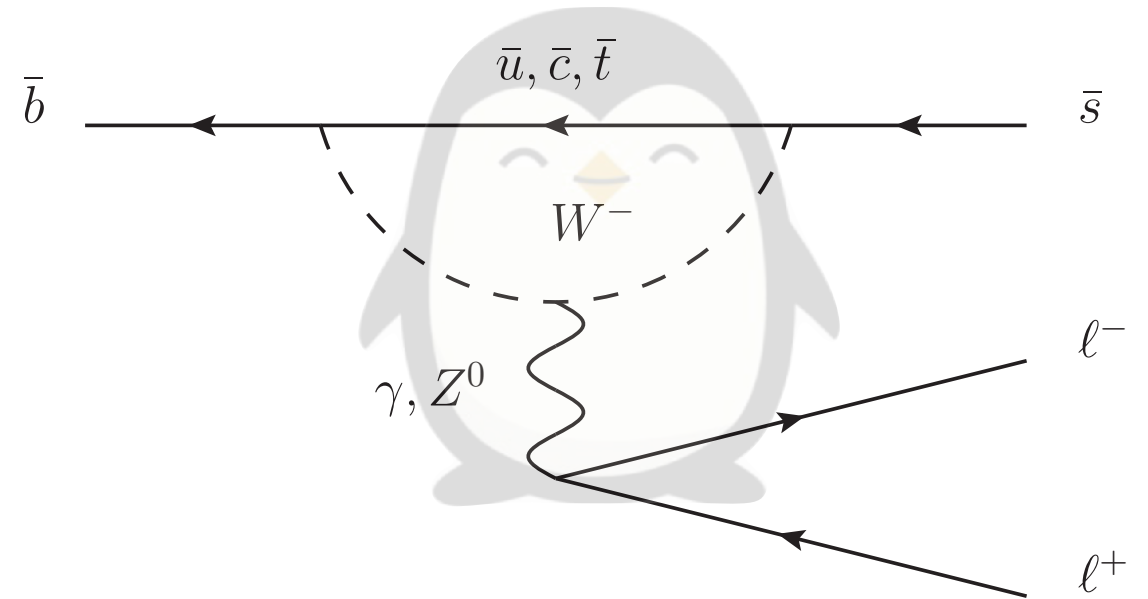
$Z'?$



The $b \rightarrow s$ transition



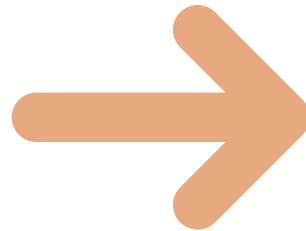
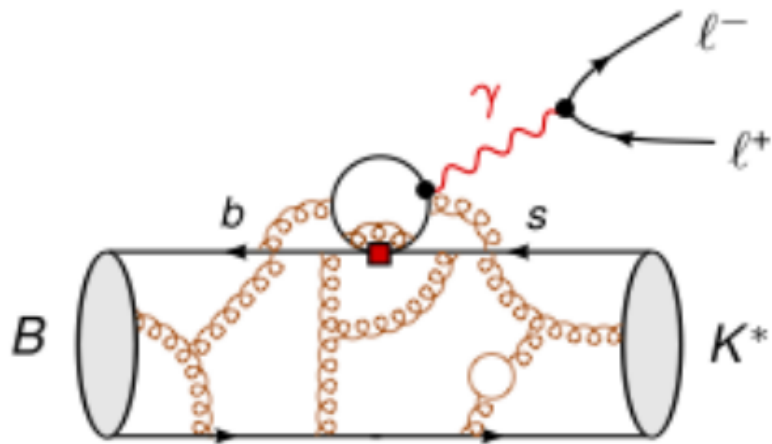
$Z'?$



Testing for Lepton Flavour Universality

Smoking gun to overcome theory uncertainties

- Angular observables might have residual uncertainties from form-factors

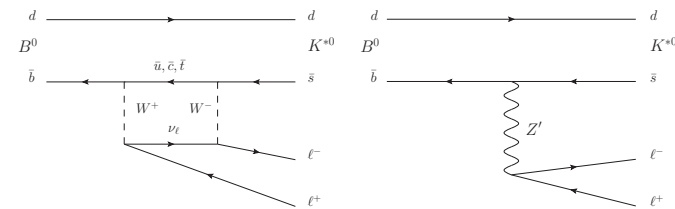
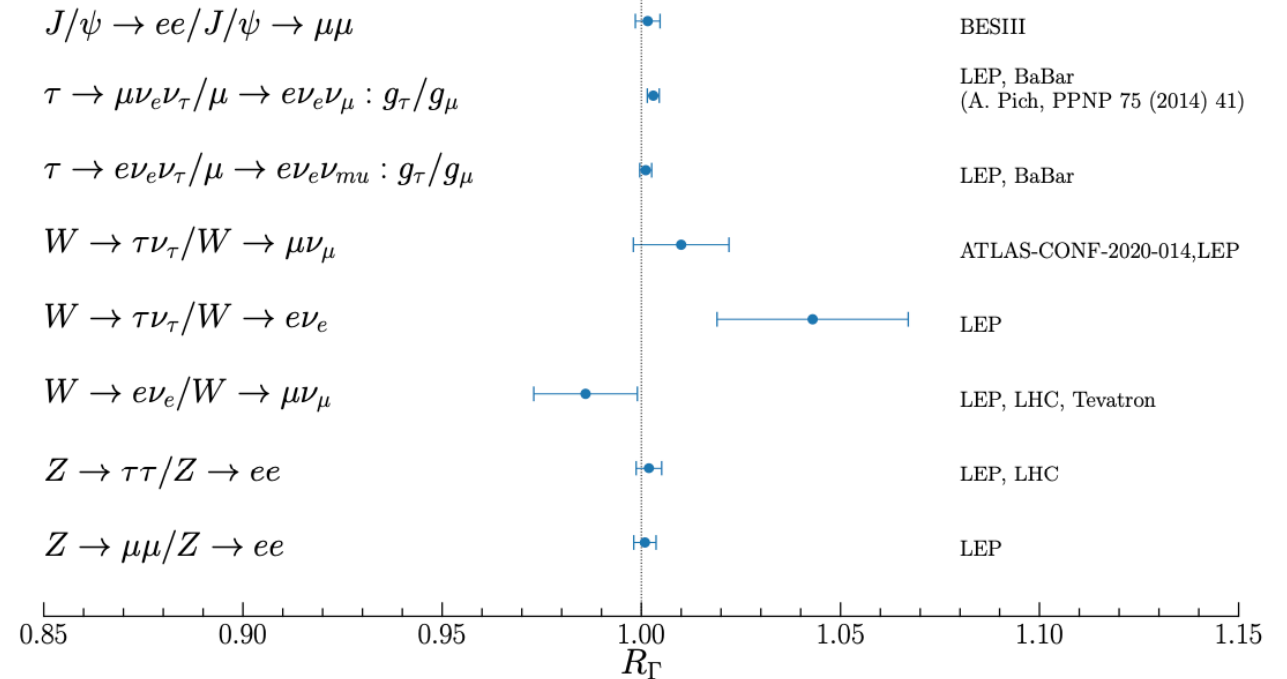


Testing for Lepton Flavour Universality

Smoking gun to overcome theory uncertainties

- All SM forces couple **universal** to the lepton flavour
- Only differences from mass/phase-space
- Most data seems to support the SM
- NP models can introduce flavour dependent couplings
- Non-universal flavour coupling would be a strong sign for physics beyond the SM

[PDG2020, Prog. Theor. Exp. Phys. 2020, 083C01 (2020)]



(c) SM example

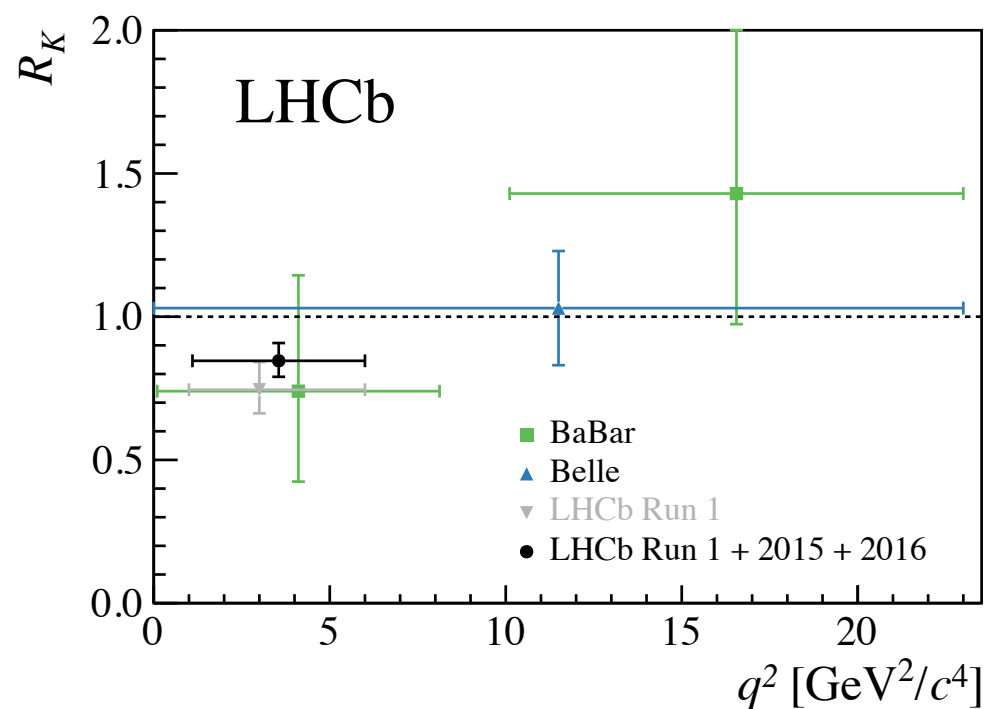
(d) NP example

Most simple approach: Ratio of Branching Ratios

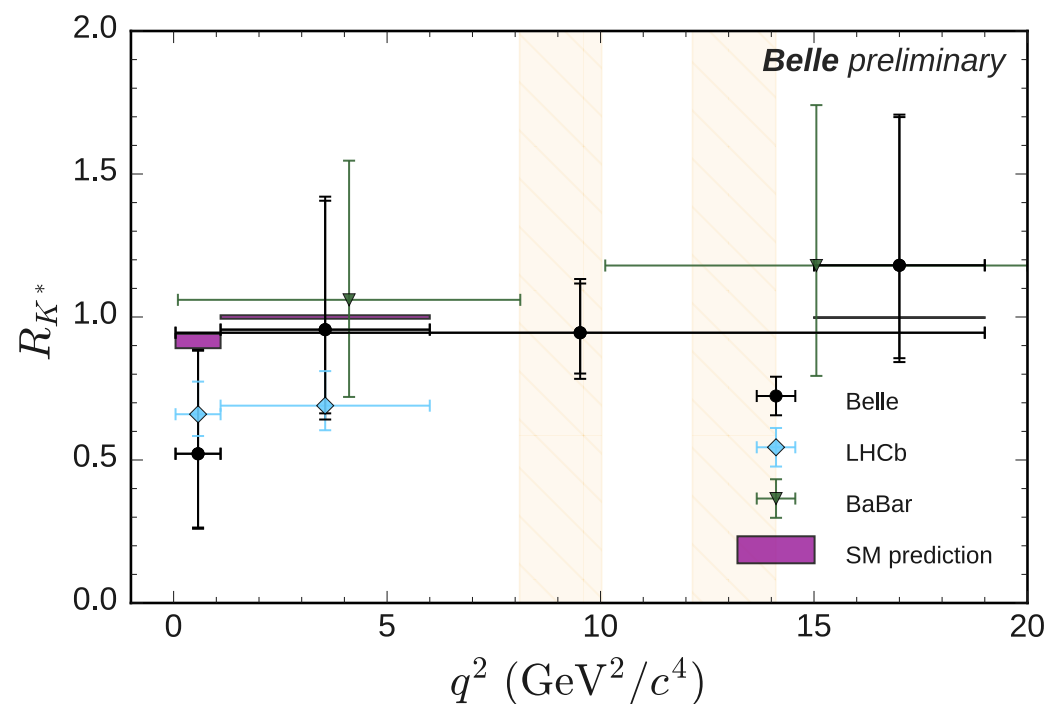
After Moriond

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}$$

$$R_K^* = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{*0} e^+ e^-)}$$



[arXiv:1903.09252](https://arxiv.org/abs/1903.09252)



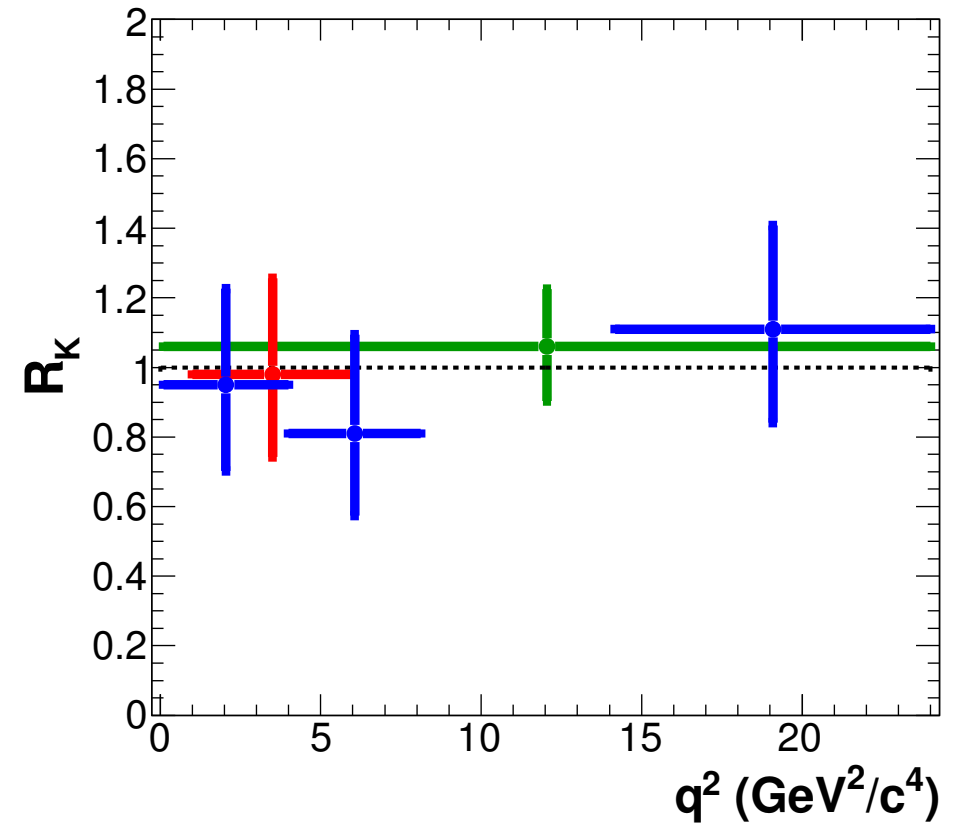
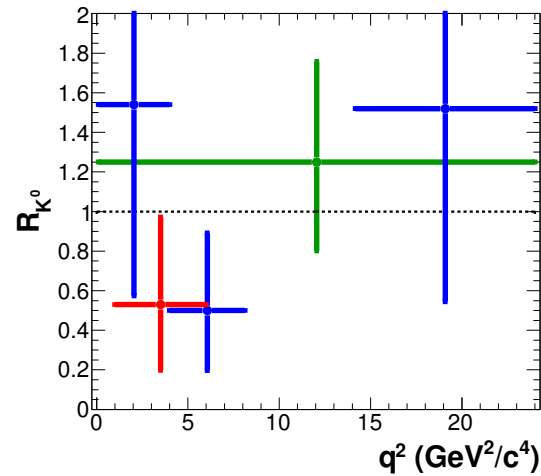
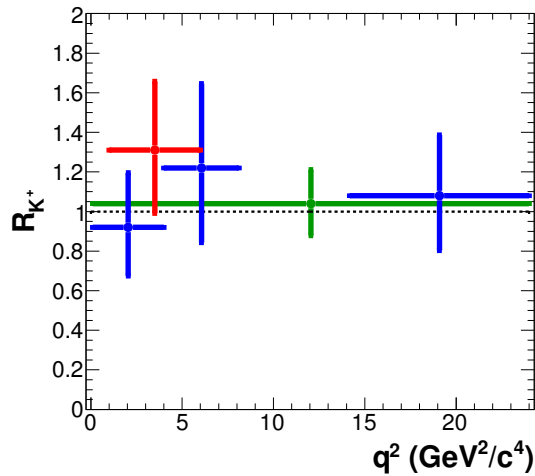
[arXiv:1904.02440](https://arxiv.org/abs/1904.02440)

R_K analysis

Results for R_K

- All measurements in agreement with recent results and SM
- The combined result is the weighted average of the B^+ and B^0 modes

[arXiv:1908.01848](https://arxiv.org/abs/1908.01848)

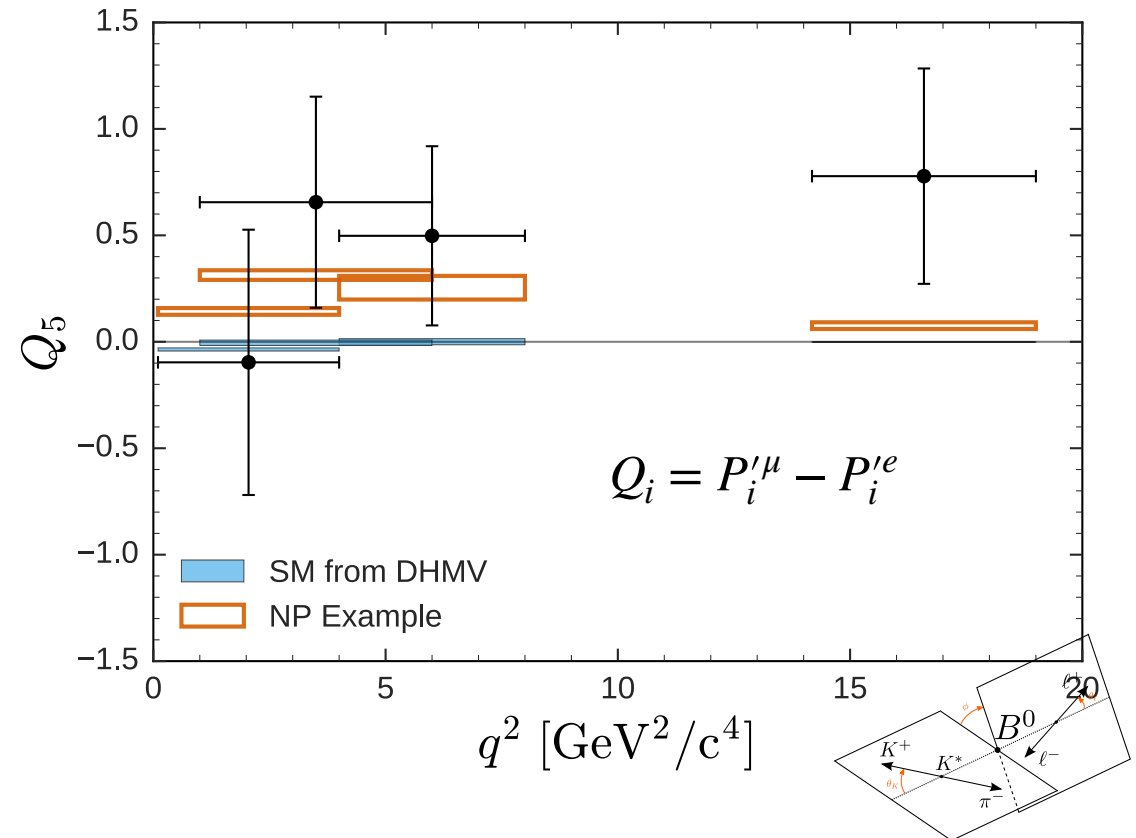
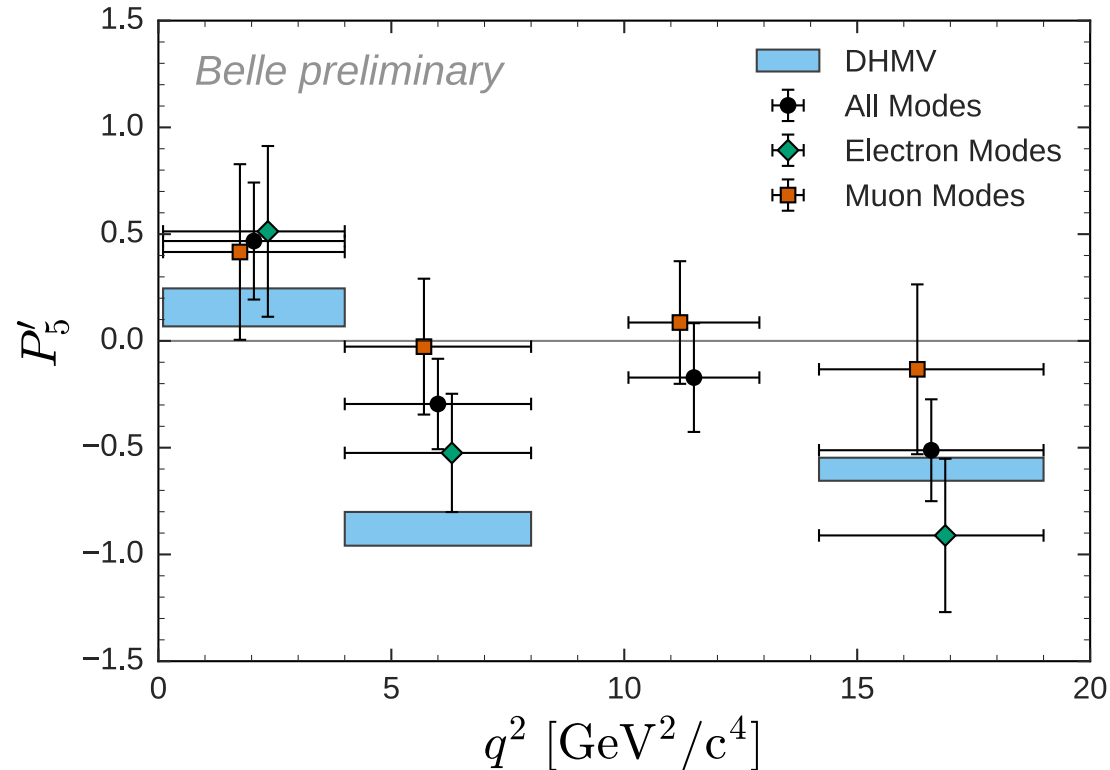


[0.1 , 4.0], [4.0 , 8.12], [1.0 , 6.0], > 14.18 and > 0.1 q^2 bins

Testing for lepton flavour universality in angular observables

Smoking gun to overcome theory uncertainties

- Performing the angular analysis separately for electron and muon modes
- Largest discrepancy in muons mode with 2.6σ while 1.1σ in the electron mode



Overview of the $b \rightarrow sll$ Puzzle

Combining the results

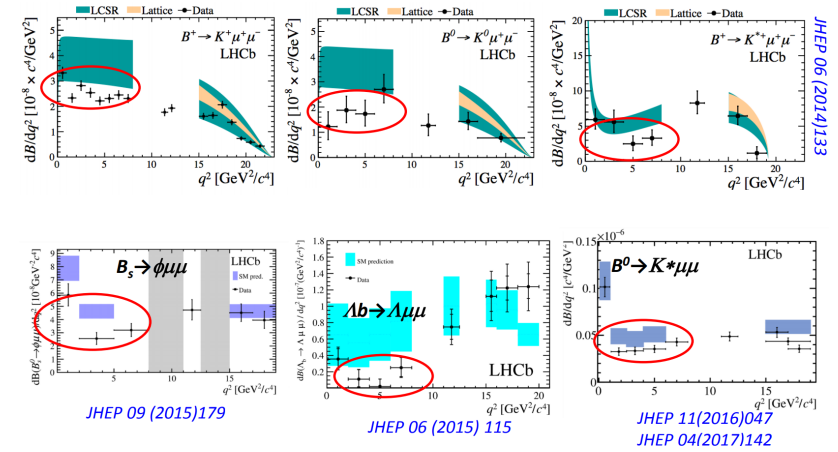
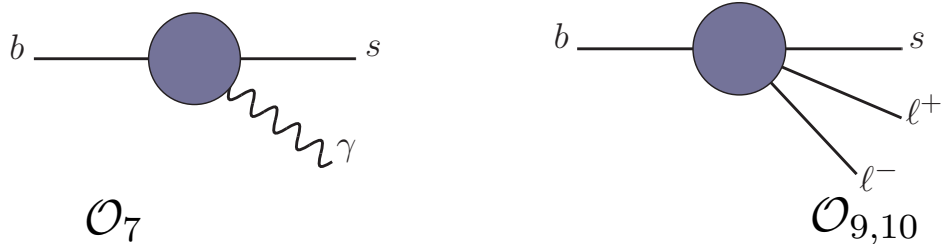
- Effective Hamiltonian approach

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i)$$

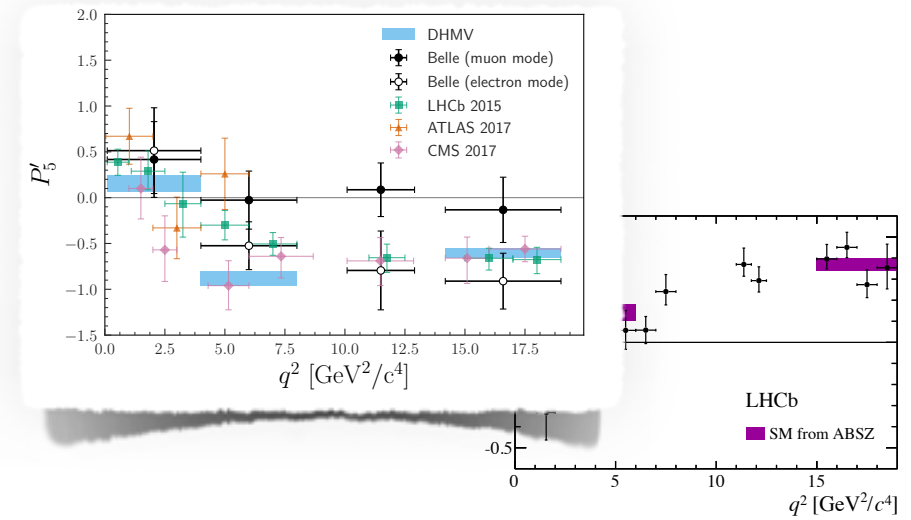
↑ left-handed part ↑ right-handed part
 suppressed in SM

- Effective Operators \mathcal{O}_i
- Effective Couplings C_i
- Combine measurements and fit for

$$C_9 = C_9^{\text{SM}} + C_9^{\text{NP}}$$

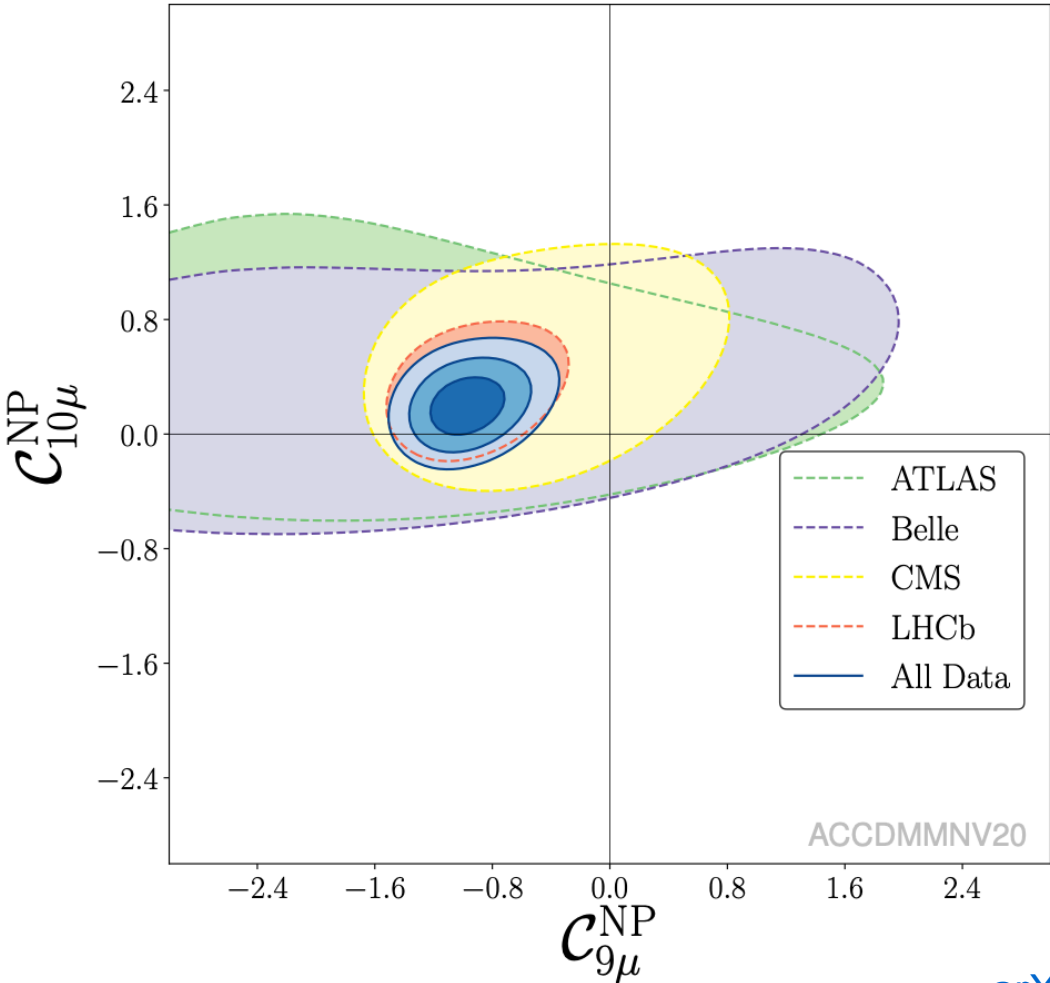


+

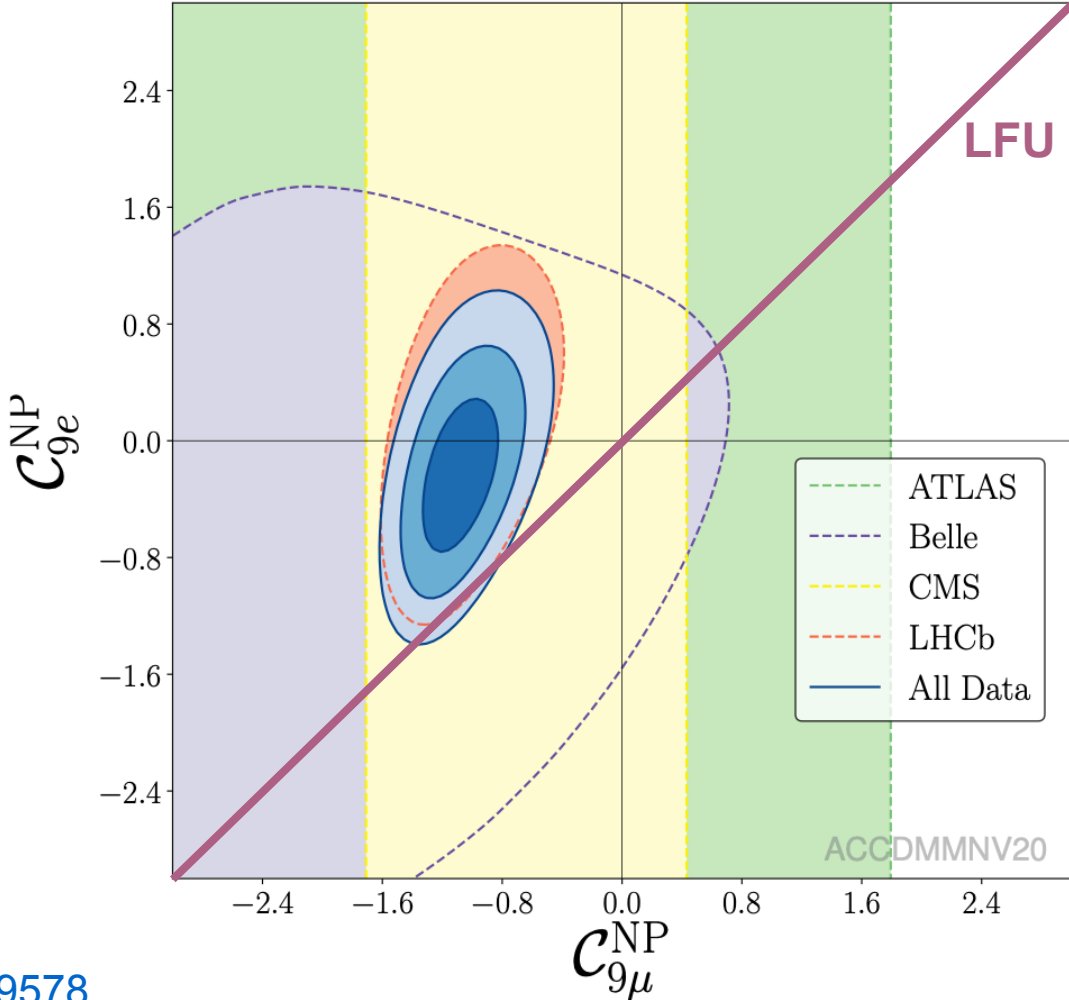


Combined Fit for New Physics

Fit for New Physics



LFU $\sim 3\sigma$ pull from SM

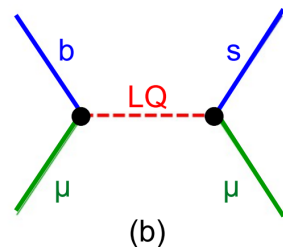
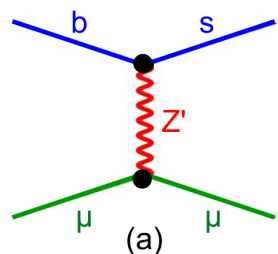


[arXiv:1903.09578](https://arxiv.org/abs/1903.09578)

LFU in tau decays

Discussion

- Most new physics models imply large contributions to the tau modes



- ▶ New Physics may couple to mass of the τ
→ enhance sensitivity by $|m_\tau/m_\mu|^2 \simeq 286$
- ▶ Both Z' and leptoquark models predict large enhancements [1704.05340]



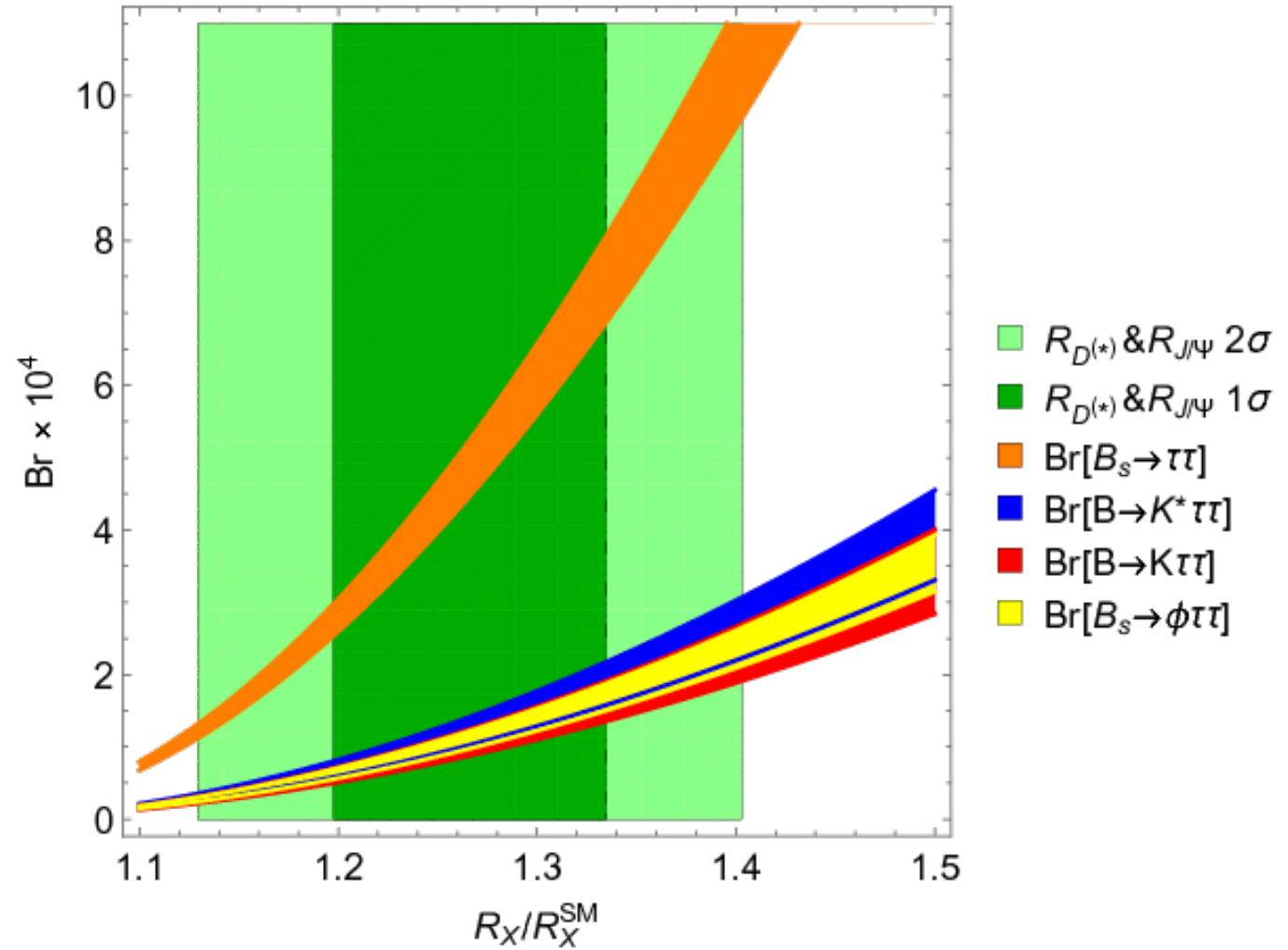
LFU in tau decays

Motivation for $B \rightarrow K^+ \tau \tau$

- Strong hints for new physics in $b \rightarrow sll$ decays
- Deviations occur dominantly in muon modes
 - NP couples to mass?
 - **tau modes could be dominant**

- ▶ $\mathcal{B}(B^+ \rightarrow K^+ \tau \tau)^{SM} < 1.44(15) \times 10^{-7}$
- ▶ Some models may lead to a strong enhancement
- ▶ $\mathcal{B}(B \rightarrow K \tau^- \tau^+)^{MLFV} < 2 \times 10^{-4}$
- ▶ Only experimental constraints by BaBar with $\mathcal{B}(B^+ \rightarrow K^+ \tau^+ \tau^-) < 2.25 \times 10^{-3}$ at 90% C.L..

Prediction of the $b \rightarrow s \tau \tau$ branching fraction

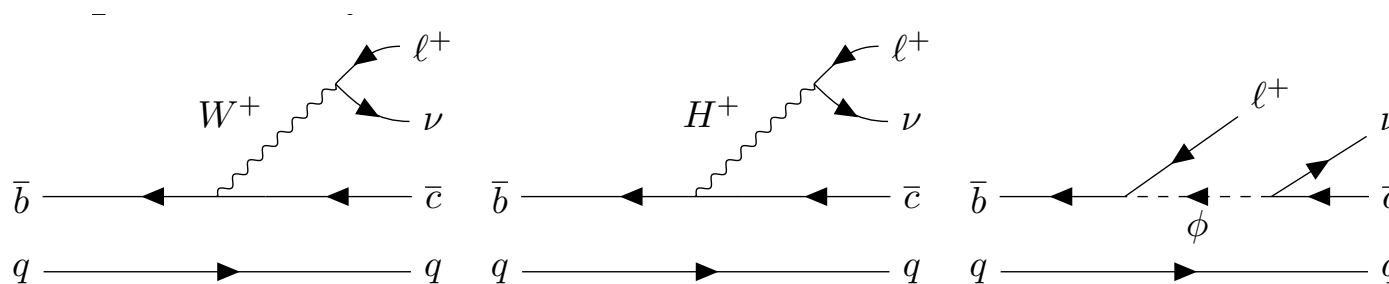


10.1103/PhysRevLett.120.181802

Lepton Flavour Universality in R_D^*

$$R_D^{(*)} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \mu \nu)}$$

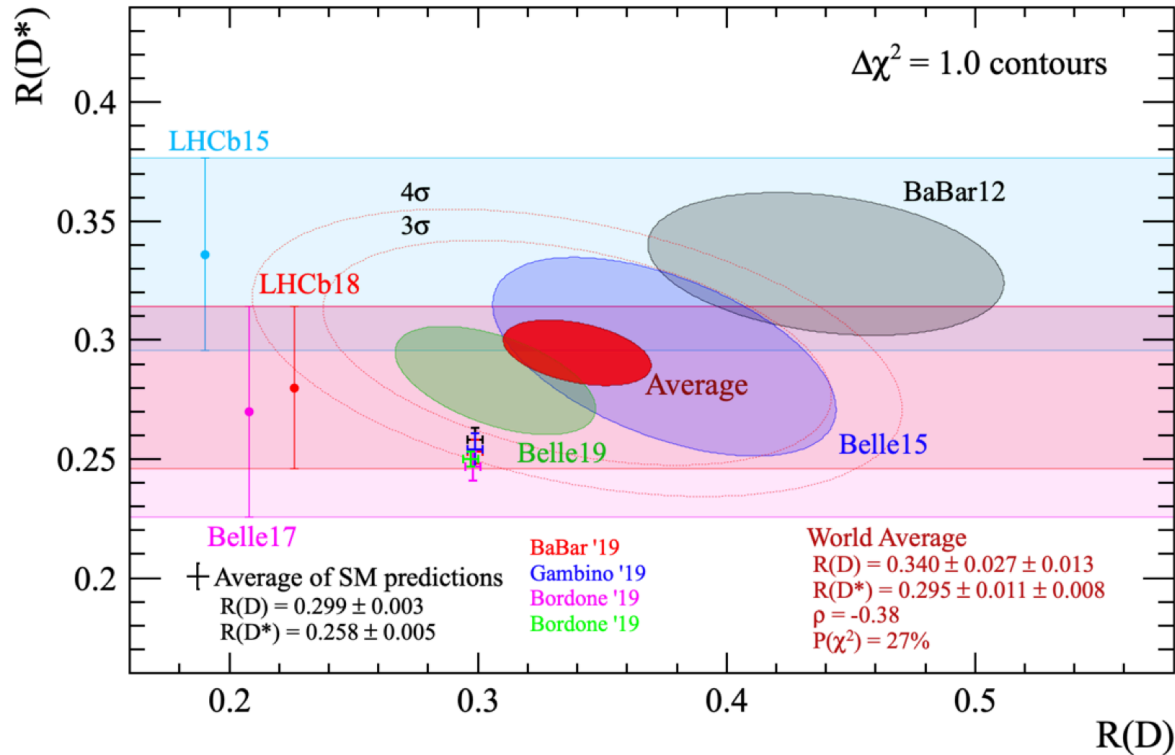
- Tree level decay
- Clean theoretical observable
- Neutrinos in the final state



Lepton Flavour Universality in R_D^*

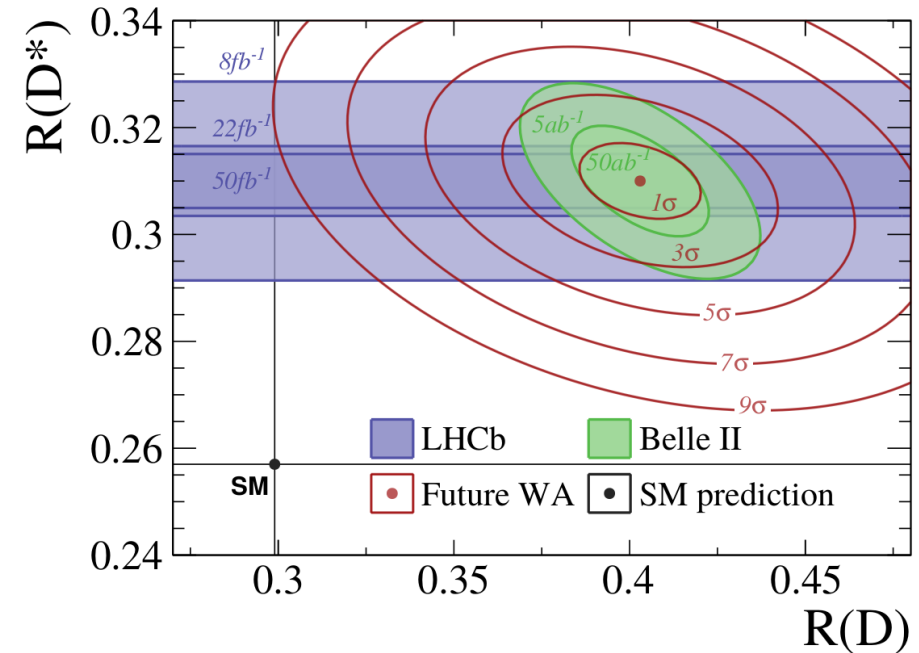
Present and Future

Now



- $\sim 3.1\sigma$ tension with SM
- $\sim 30\%$ effect against SM for taus in tree level decays

Soon



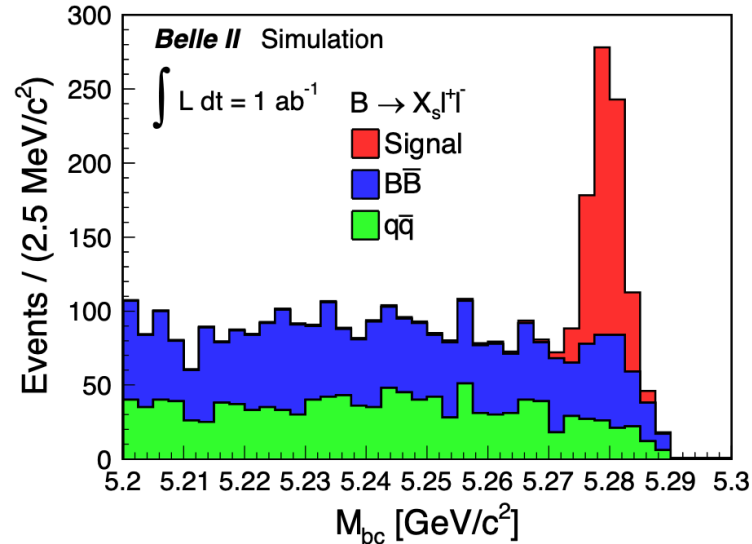
	$\Delta R(D)$ [%]			$\Delta R(D^*)$ [%]		
	Stat	Sys	Total	Stat	Sys	Total
Belle 0.7 ab^{-1}	14	6	16	6	3	7
Belle II 5 ab^{-1}	5	3	6	2	2	3
Belle II 50 ab^{-1}	2	3	3	1	2	2

Projections based on Belle SL tag measurement (before 2019)

Belle II Early Physics program

Rediscovery and performance studies

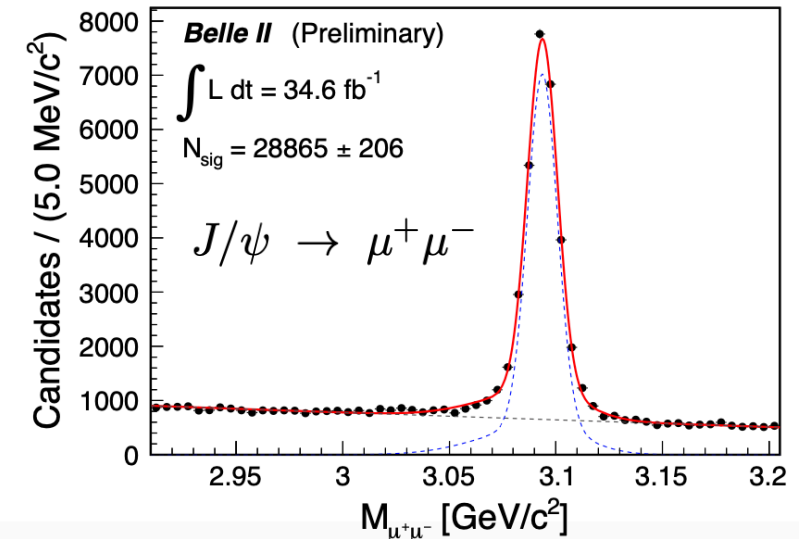
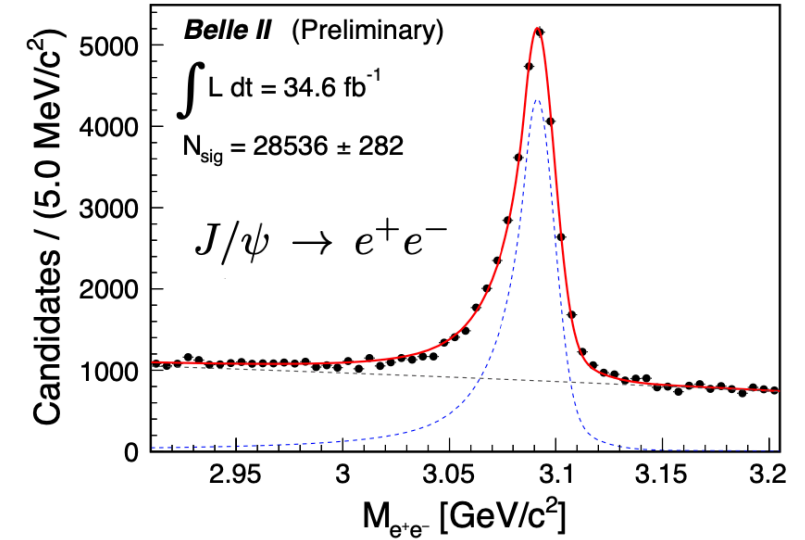
- Validation and performance studies
- Rediscovery for $B \rightarrow X_s \ell \ell$ and $B \rightarrow K \ell \ell$ soon



BELLE2-NOTE-
PL-2020-007

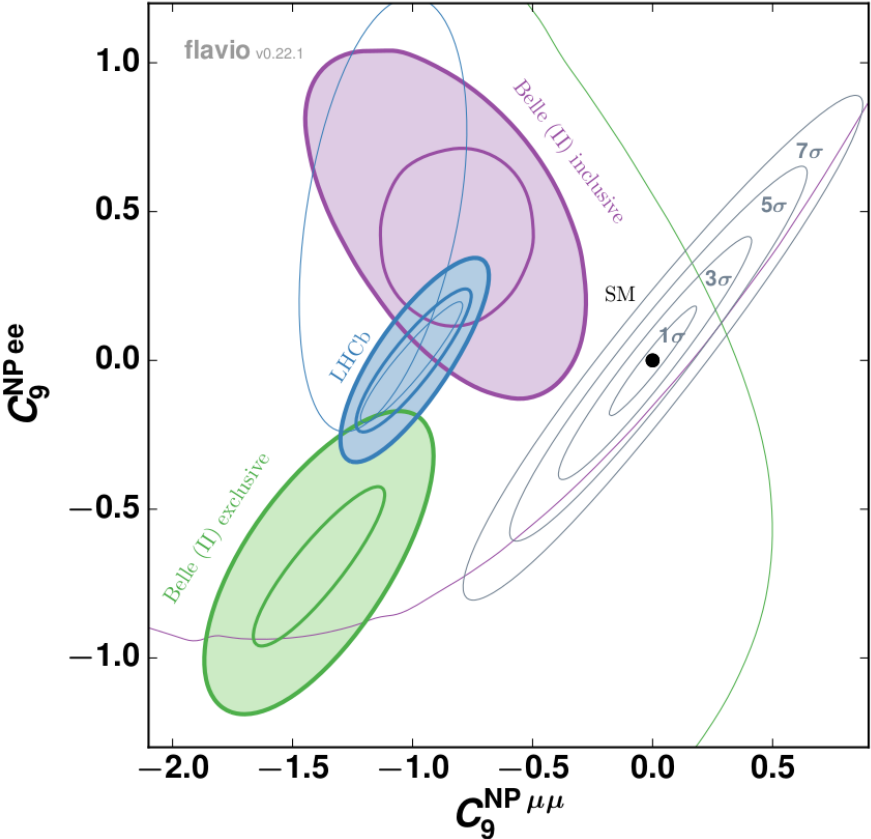
Observables	Belle 0.71 ab^{-1}	Belle II 5 ab^{-1}	Belle II 50 ab^{-1}
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-)$ ([1.0, 3.5] GeV^2)	29%	13%	6.6%
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-)$ ([3.5, 6.0] GeV^2)	24%	11%	6.4%
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-)$ ($> 14.4 \text{ GeV}^2$)	23%	10%	4.7%
$A_{\text{FB}}(B \rightarrow X_s \ell^+ \ell^-)$ ([1.0, 3.5] GeV^2)	26%	9.7%	3.1%
$A_{\text{FB}}(B \rightarrow X_s \ell^+ \ell^-)$ ([3.5, 6.0] GeV^2)	21%	7.9%	2.6%
$A_{\text{FB}}(B \rightarrow X_s \ell^+ \ell^-)$ ($> 14.4 \text{ GeV}^2$)	19%	7.3%	2.4%

B2TiP

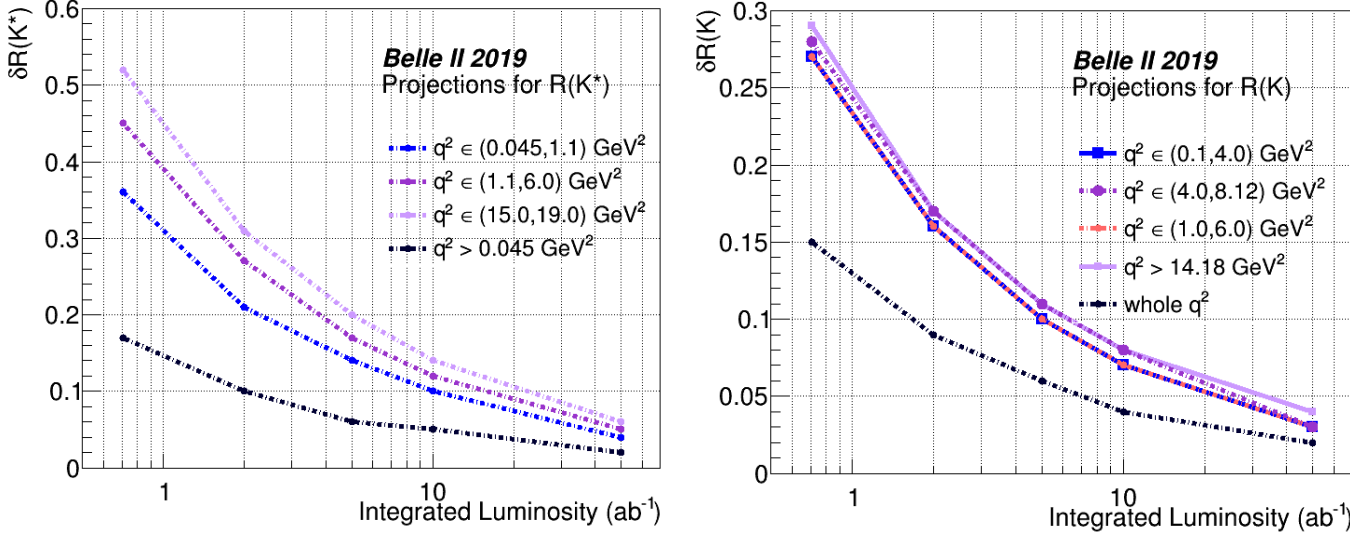


Belle II and LHCb Projections for $b \rightarrow sll$

Combined Analysis



Individual Measurements



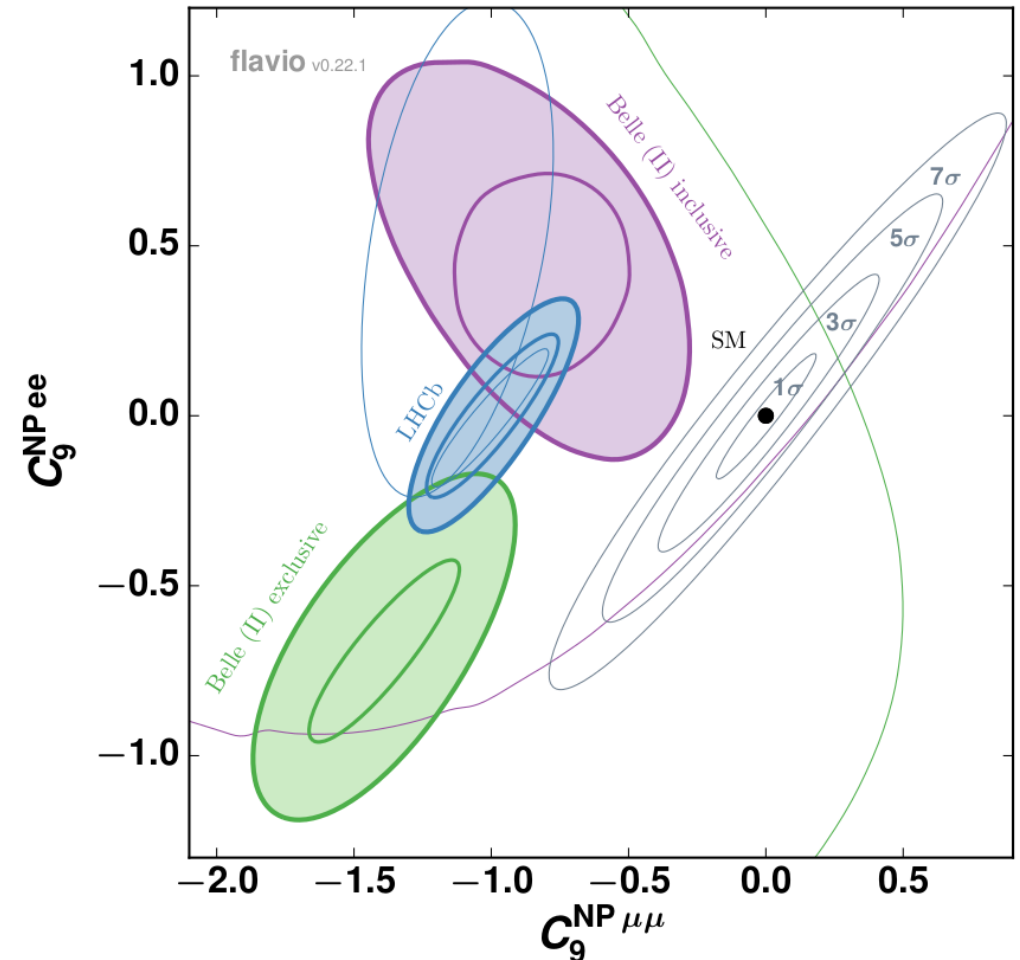
- Already with a few ab^{-1} Belle II might be able to confirm the $b \rightarrow s$ anomalies
- Belle II has excellent electron momentum resolution and neutrals performance

J. Albrecht et al., Future prospects for exploring present day anomalies in flavour physics measurements with Belle II and LHCb

Summary and Conclusion

Prospects for $b \rightarrow s \ell \ell$ decays at Belle II

- LFU tests in rare decays provide excellent tests for new physics
- Belle II can probe unique channels and provide an independent validation of the current anomalies
 - Inclusive analyses, full event interpretation, very good electron and neutral particle efficiency
- Discovery of $b \rightarrow s \tau \tau$ could be in reach of Belle II if anomalies persist
- But not only Belle II also the LHC experiments will be able to shed more light upon the anomalies



Appendix

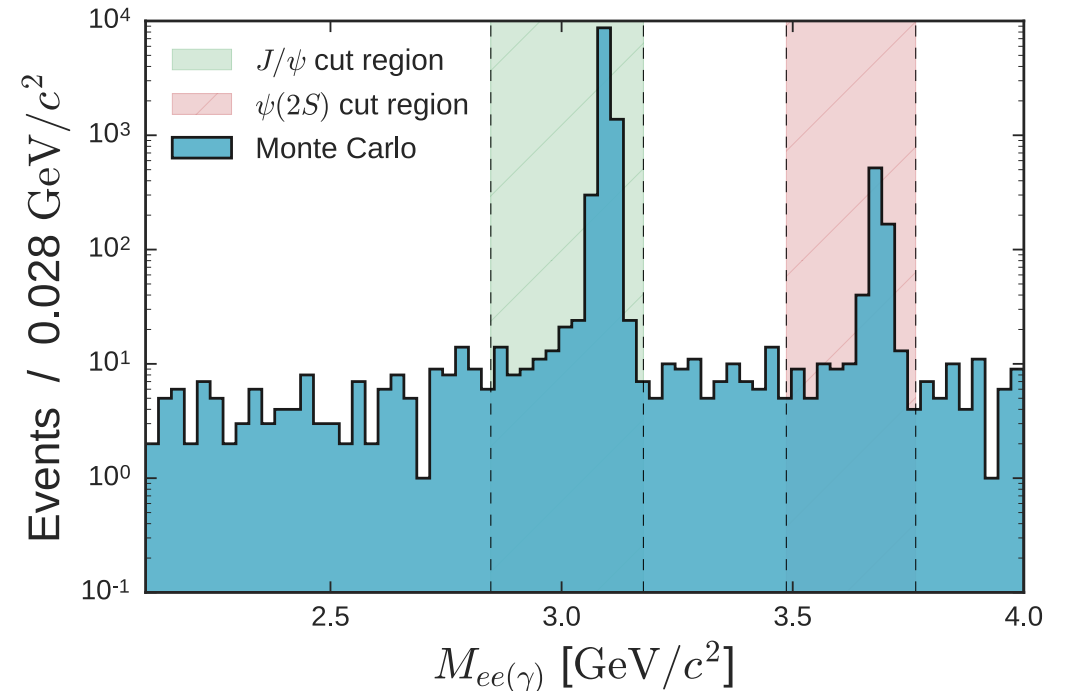
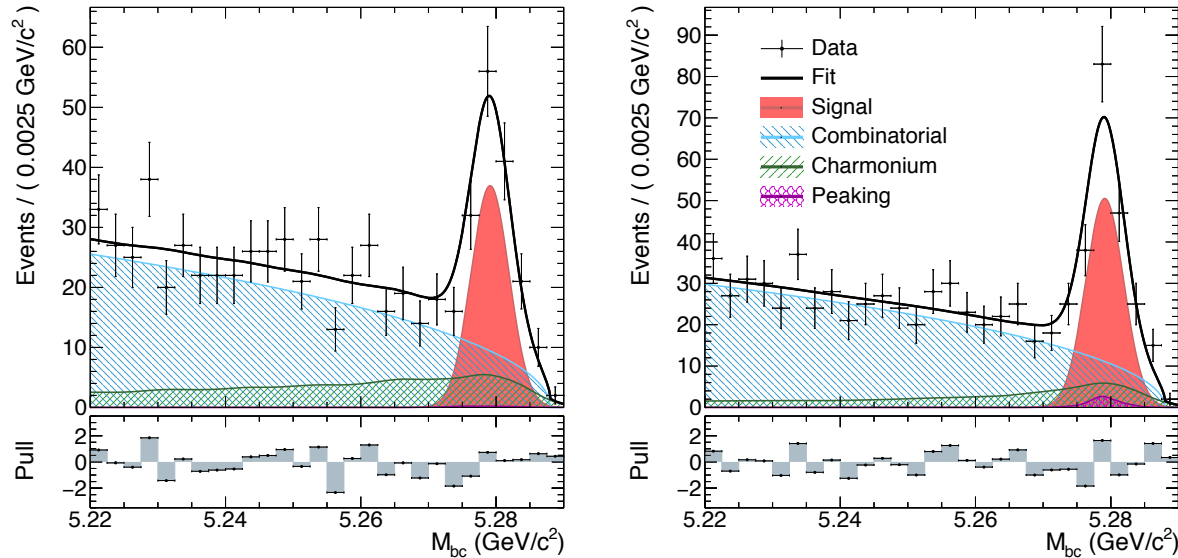
B → K*ll Analysis at Belle

Belle Analysis

- Similar electron and muon performance
- limited statistics
- Neural network based reconstruction in order to maximise efficiency

$$B^+ \rightarrow K^{*+}(K^+\pi^0)l^+l^-$$
$$B^+ \rightarrow K^{*+}(K_S\pi^+)l^+l^-$$

$$B^0 \rightarrow K^{*0}(K_S\pi^0)l^+l^-$$
$$B^0 \rightarrow K^{*0}(K^+\pi^-)l^+l^-$$



Angular Analysis

Parametrisation of the differential decay rate

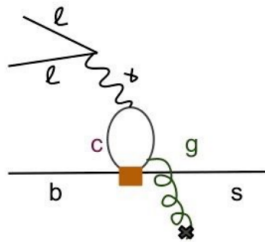
$$\frac{d^4(\Gamma + \bar{\Gamma})}{d \cos \theta_\ell d \cos \theta_K d\phi dq^2} = \frac{9}{32\pi} \sum_{i=1}^9 (I_i + \bar{I}_i) f_i(\cos \theta_\ell, \cos \theta_K, \phi)$$

► $I_i =$ short distance + long distance

Wilson coefficients:
perturbatively calculable

Form-factors:
non-perturbative estimates
from LCSR, HQET, Lattice ...
tremendous effort since past

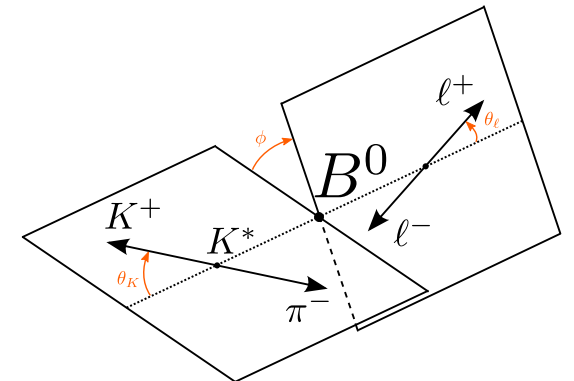
Non-factorizable
contributions:



no quantitative computation

$$S_i^{(a)} = \frac{I_i^{(a)} + \bar{I}_i^{(a)}}{d(\Gamma + \bar{\Gamma}) / dq^2}$$

$$A_i^{(a)} = \frac{I_i^{(a)} - \bar{I}_i^{(a)}}{d(\Gamma + \bar{\Gamma}) / dq^2}$$



Credit: R. Mandal, ICHEP 2016

Angular Analysis

Full expansion of the differential decay rate

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_L d\cos\theta_K d\phi dq^2} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ \left. + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_L \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_L + S_3 \sin^2 \theta_K \sin^2 \theta_L \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_L \cos \phi + S_5 \sin 2\theta_K \sin \theta_L \cos \phi \right. \\ \left. + S_6 \sin^2 \theta_K \cos \theta_L + S_7 \sin 2\theta_K \sin \theta_L \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_L \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_L \sin 2\phi \right]$$

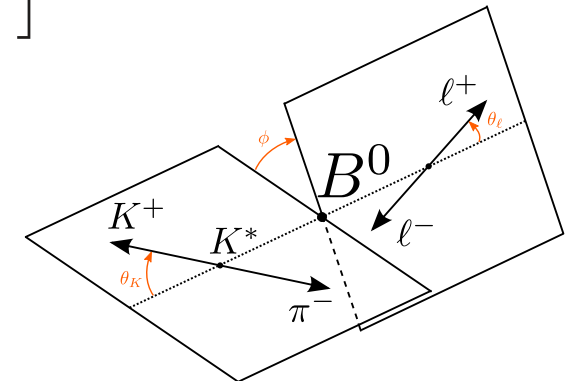
using definitions of [J. High Energy Phys. 01 \(2009\) 019](#).

$$S_i^{\text{obs}} = S_i - A_i(\mathcal{A}_{CP} + \kappa\mathcal{A}_P + A_D)$$

“clean” observables

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$$

cancel form-factor uncertainties

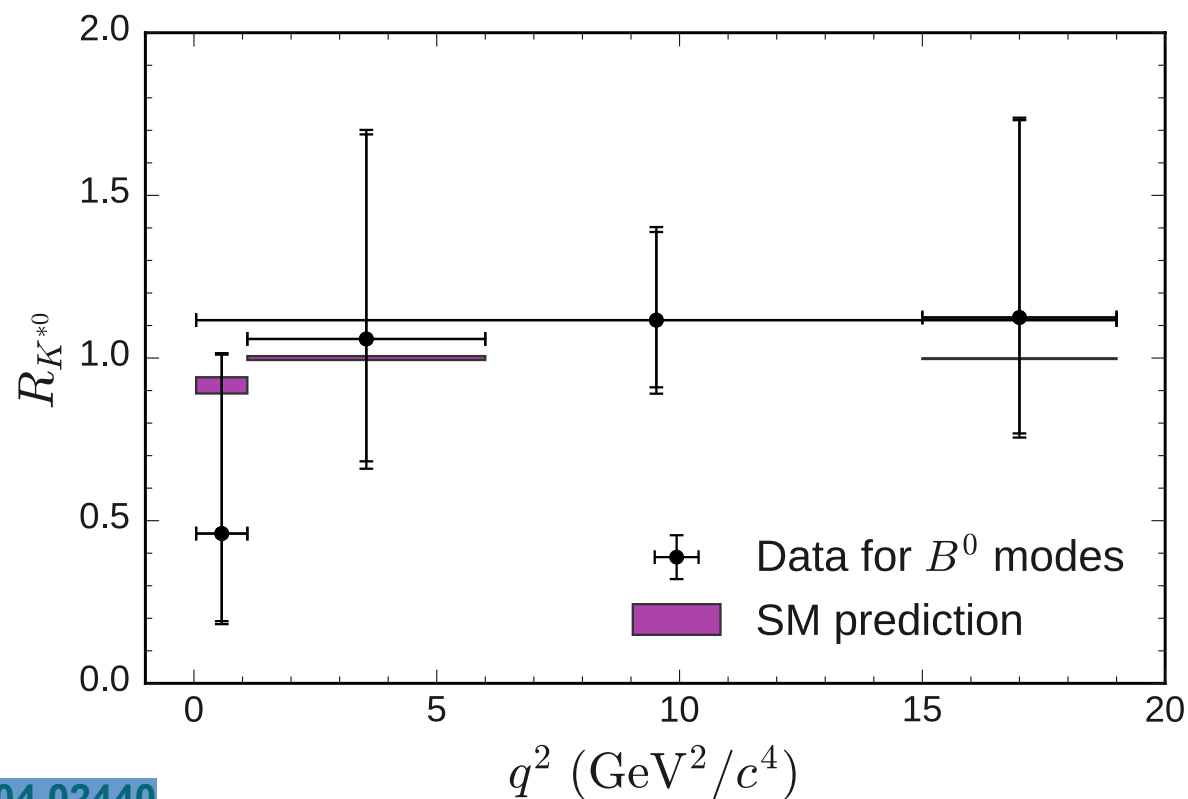
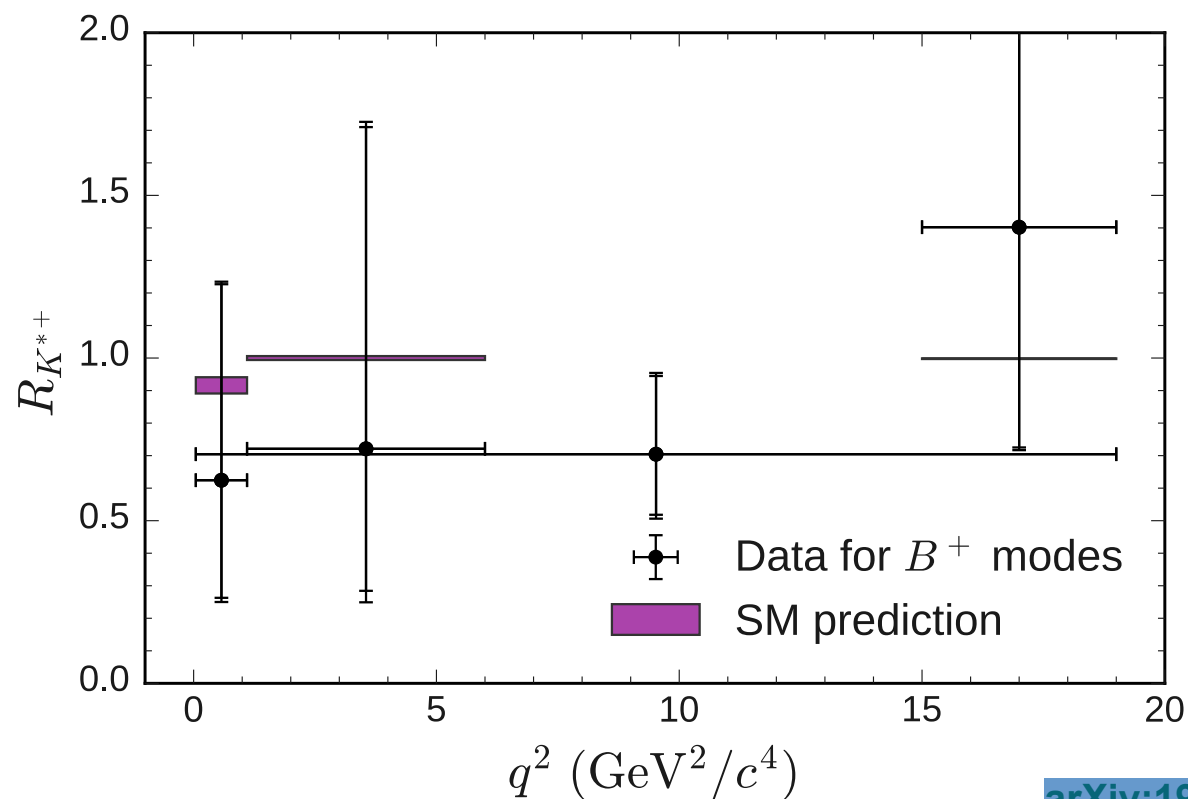


Most simple approach: Ratio of Branching Ratios

The new Belle result

- Separate results B^0 and B^+

SM prediction by: [10.1007/JHEP10\(2016\)075](https://arxiv.org/abs/10.1007/JHEP10(2016)075)



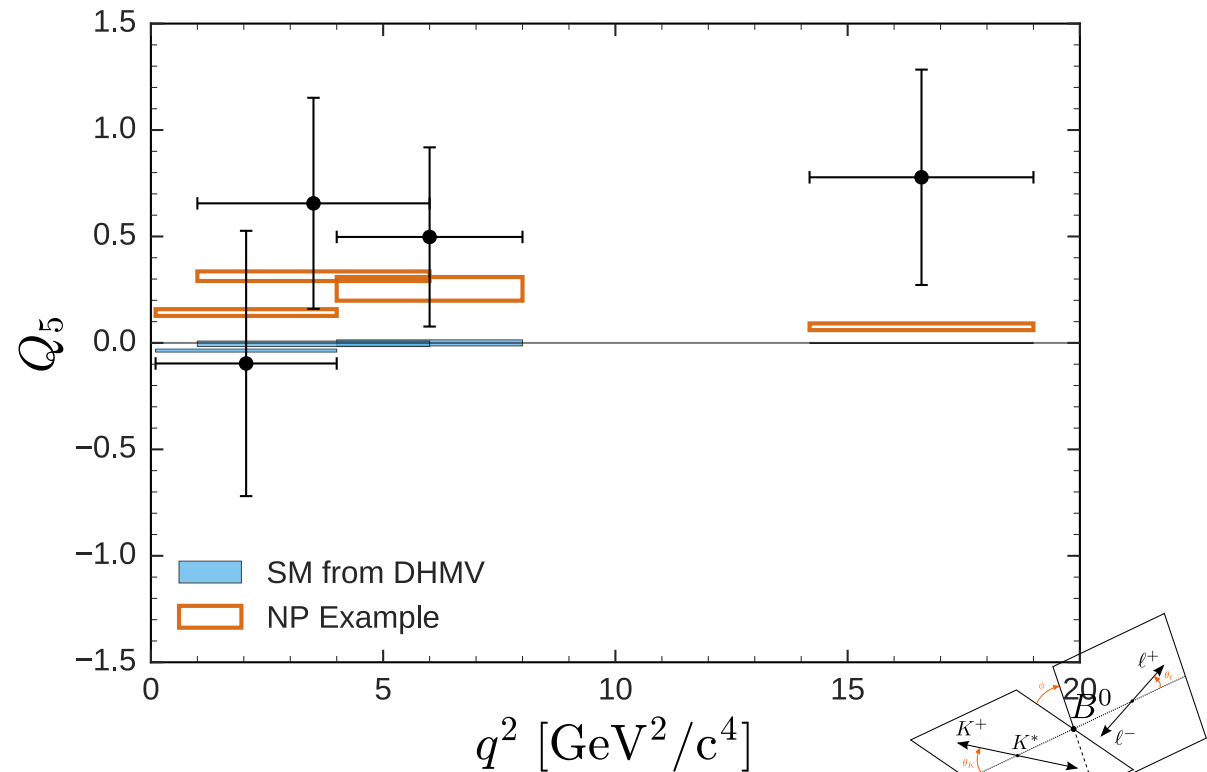
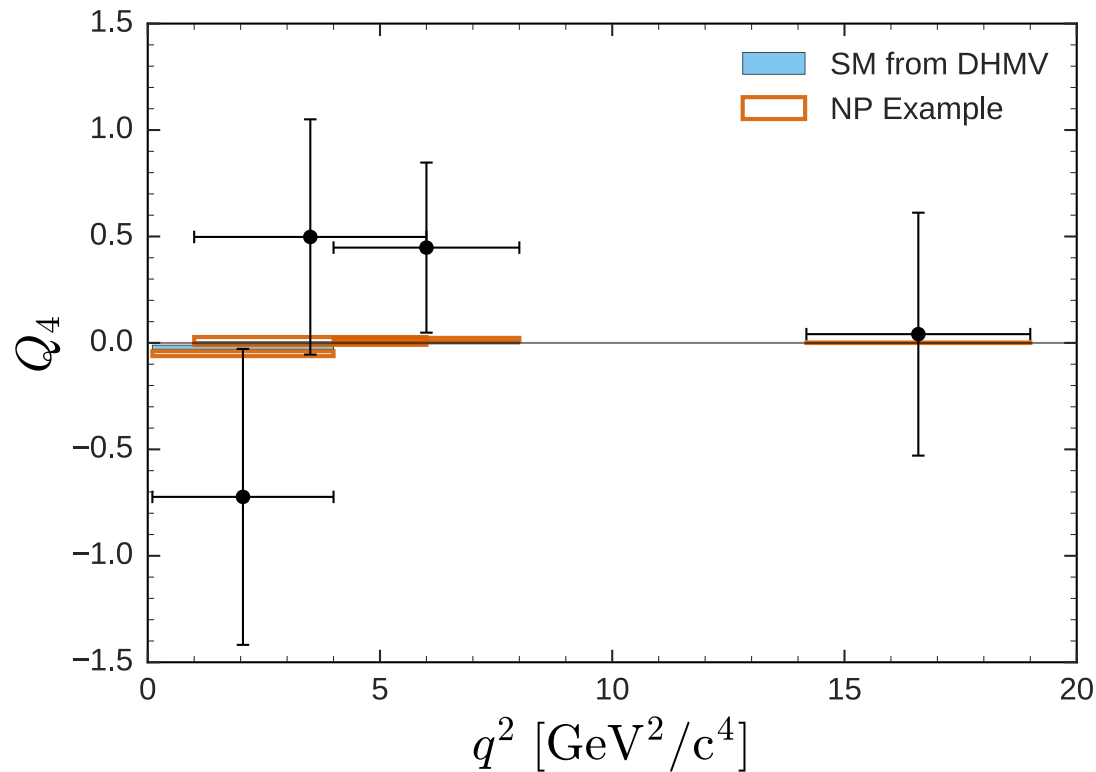
[arXiv:1904.02440](https://arxiv.org/abs/1904.02440)

Testing for lepton flavour universality in angular observables

Smoking gun to overcome theory uncertainties

- Testing for LFU can overcome this with very clean observables

$$Q_i = P_i^{\prime\mu} - P_i^{\prime e}$$



Phys. Rev. Lett. 118, 111801 (2017)

