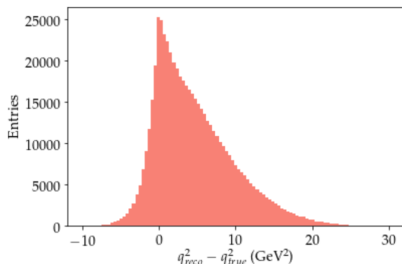
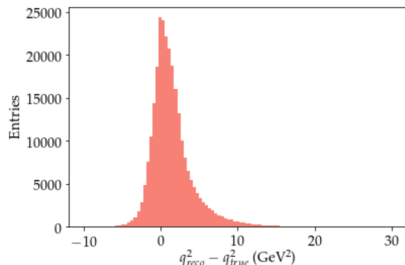


The  $|E_{miss} - p_{miss}| < 0.5$  GeV selection requirement greatly improves the resolution:



Resolution before cut



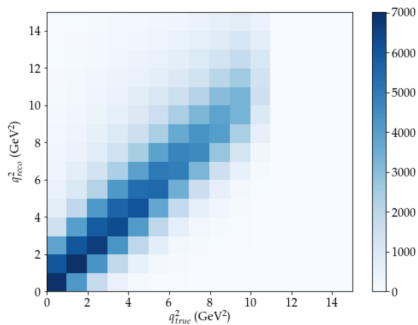
Resolution after cut

Me: the resolution looks so much better now!

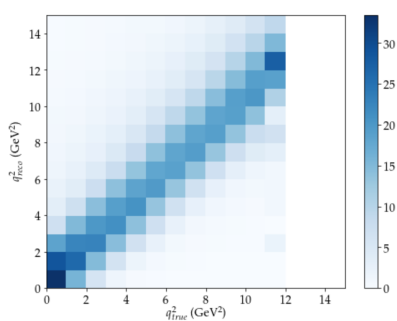
Christoph: still looks really bad.

Me: oh. :-(

# Migration matrix



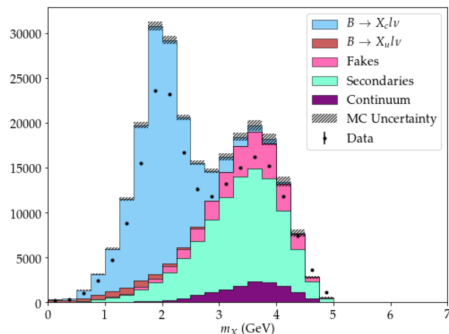
Before normalizing



Normalized to percentage

# Secondary correction

Use a secondary enriched region to estimate a secondary shape correction function:

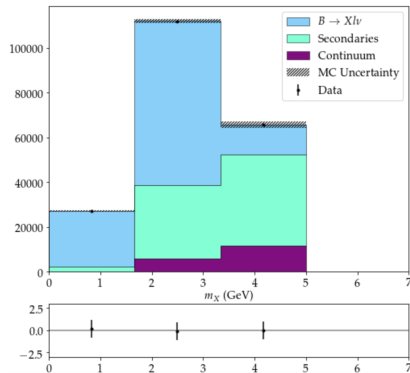


## Secondary selection

- $m_{bc} > 5.27 \text{ GeV}$
- $\log(\text{NB}) > -4$
- $\log(\text{contNB}) > -4$
- $p_e > 0.3$
- $p_\mu > 0.6$
- $Q_{tag} \times Q_{lep} > 0$
- $|E_{miss} - p_{miss}| < 0.5$

# Secondary correction

Use a secondary enriched region to estimate a secondary shape correction function:

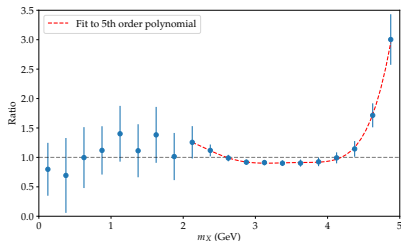
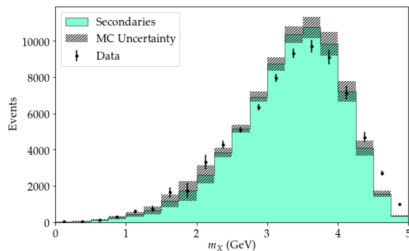


- Fit  $m_X$  in coarse bins to determine  $B \rightarrow Xl\nu$  component
- Use these normalizations to subtract the  $m_X$  distribution in fine bins
- Derive a correction function from the secondary versus subtracted shape

Christoph: why are you doing something so complicated?

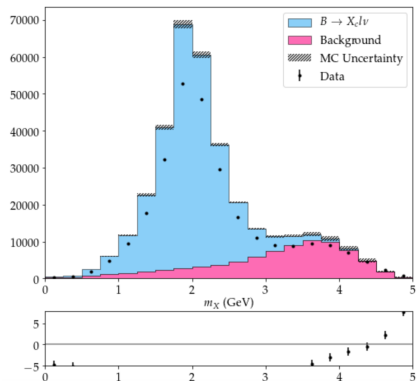
# Secondary correction

Use a secondary enriched region to estimate a secondary shape correction function:

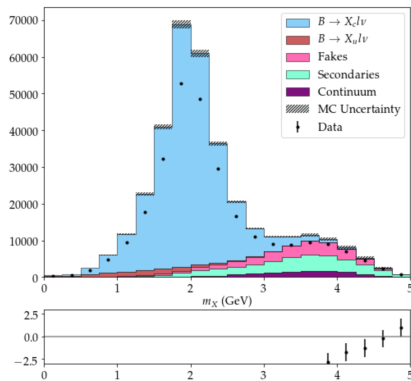


- Derive a correction function from the ratio between the secondary shape and subtracted data.

# Corrected $m_X$ distribution



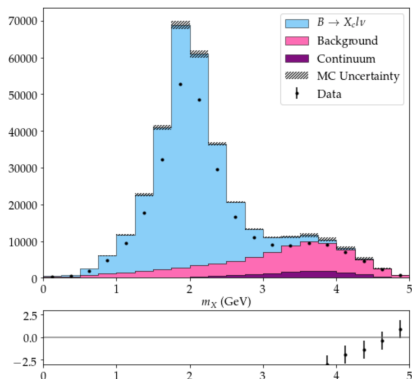
Before



After

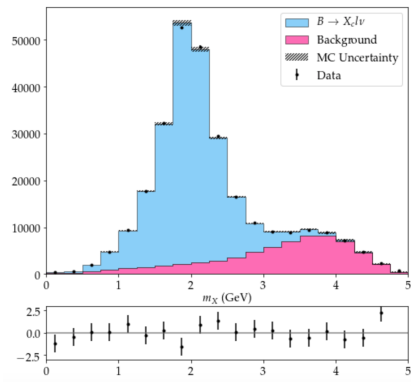
# Fit with corrected $m_X$ distribution

Estimate background component from a three component template fit to  $m_X$

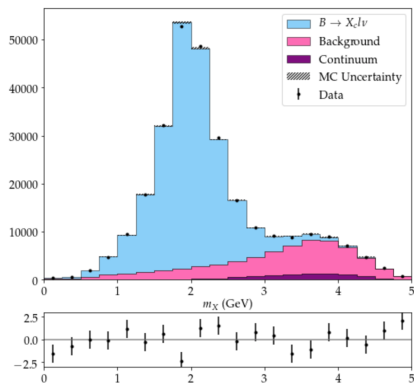


- Templates constrained to  $X_c l \nu$  BF errors (PDG 2020)
- All MC correction errors included as nuisance parameters
- 100% uncertainty assigned to the Gap modes
- Continuum constrained to off-resonance expectation

# Fit results



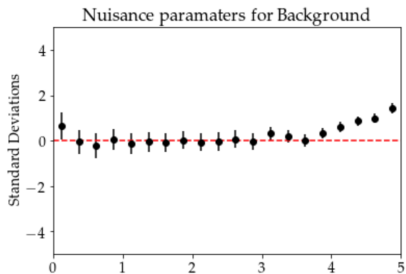
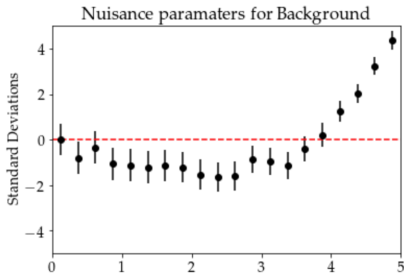
Old



New

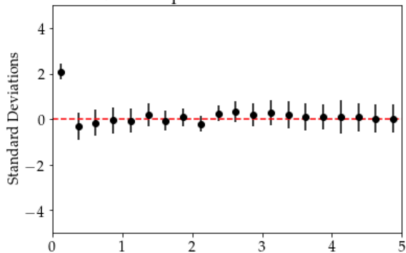


# Nuisance parameters

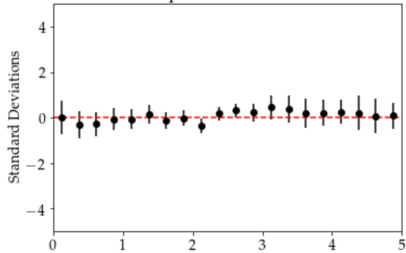


# Nuisance parameters

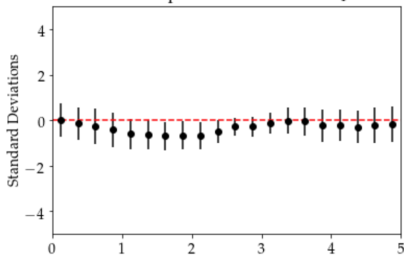
Nuisance parameters for  $B \rightarrow D l \nu$



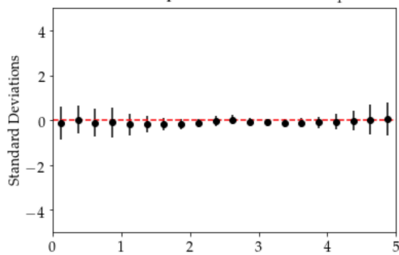
Nuisance parameters for  $B \rightarrow D^* l \nu$



Nuisance parameters for  $B \rightarrow D_1 l \nu$

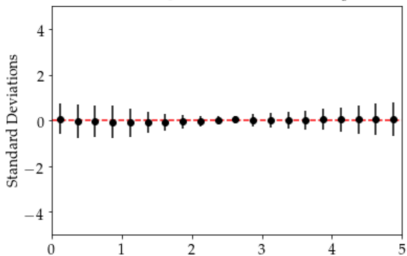


Nuisance parameters for  $B \rightarrow D'_1 l \nu$

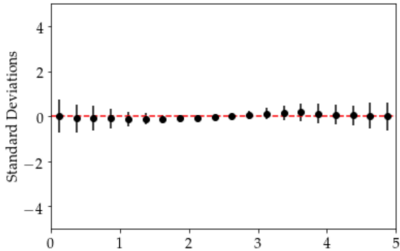


# Nuisance parameters

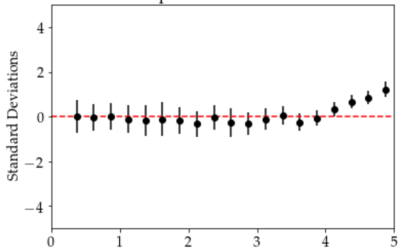
Nuisance parameters for  $B \rightarrow D_0^* l \nu$



Nuisance parameters for  $B \rightarrow D_2^* l \nu$

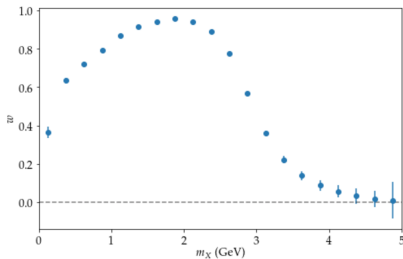
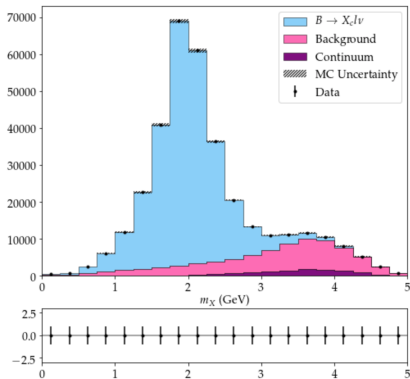


Nuisance parameters for Continuum



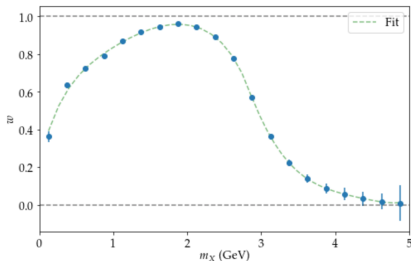
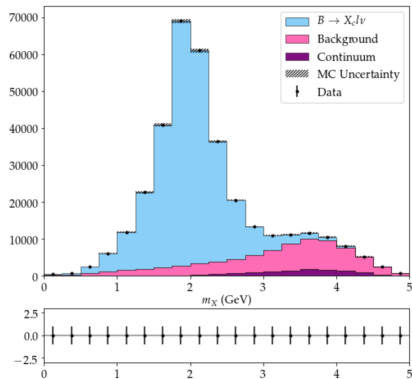
# Calculating $w_i$

Calculate  $w(m_X) = 1 - N_{bkg}/N_{tot}$  for each bin (only with MC for now):



# Calculating $w_i$

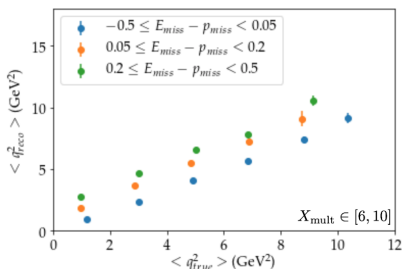
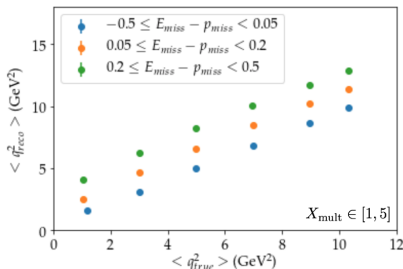
Calculate  $w(m_X) = 1 - N_{bkg}/N_{tot}$  for each bin (only with MC for now):



- Here, I fitted 2 polynomials over different ranges

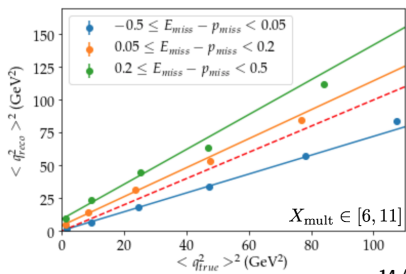
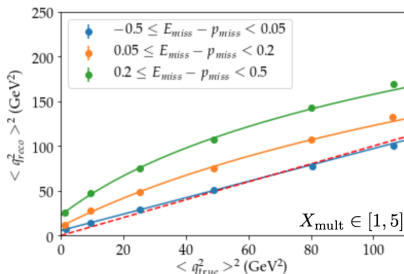
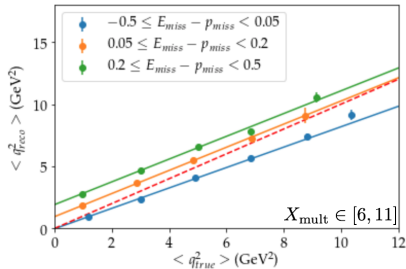
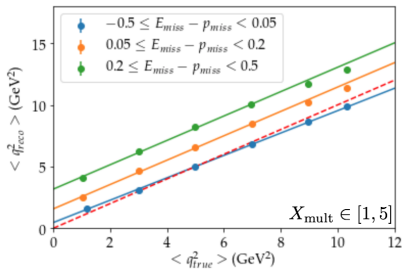
# Calibration

- Determine  $\langle q_{\text{reco}}^2 \rangle$  and  $\langle q_{\text{true}}^2 \rangle$  in bins of  $q_{\text{true}}^2$
- We see a linear behaviour between  $\langle q_{\text{reco}}^2 \rangle$  and  $\langle q_{\text{true}}^2 \rangle$
- Fit in bins of  $X_{\text{mult}}$  and  $E_{\text{miss}} - p_{\text{miss}}$ 
  - Three bins in  $E_{\text{miss}} - p_{\text{miss}}$ :  $[-0.5, 0.05, 0.2, 0.5]$  GeV
  - Two bins in  $X_{\text{mult}}$ :  $[1, 5]$  and  $[6, 10]$
- Calculate  $q_{\text{calib}}^2 = (q_{\text{reco}}^2 - c)/m$



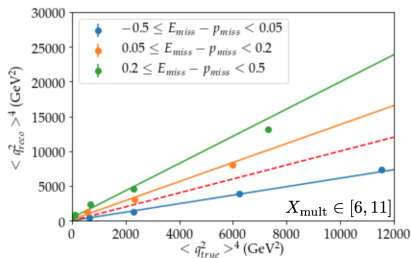
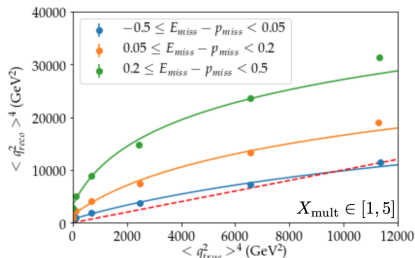
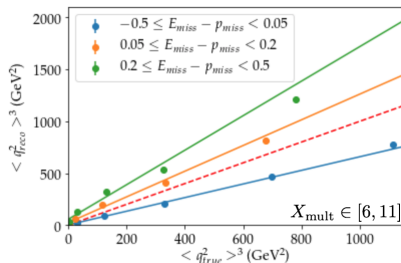
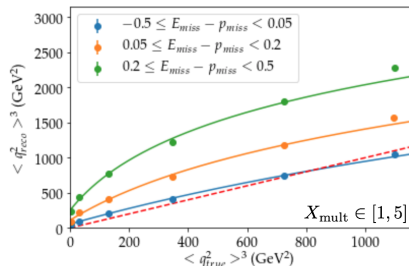
# Fit to extract the calibration

Fit linear curves to each of the scatter plots:



# Fit to extract the calibration

Fit linear curves to each of the scatter plots:



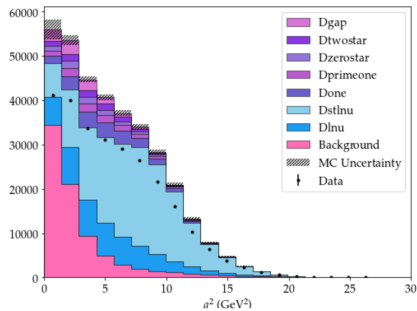
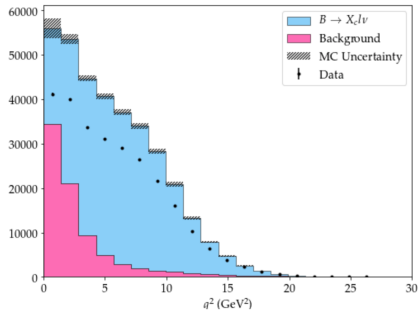


- Finish deriving the correction function for the secondaries (check!)
- Redo the  $m_X$  fit with the shape correction factors from the secondary enriched sample (check!)
- Determine the event-wise signal probability as a function of  $m_X$  (check!)
- Study and refine the calibration steps a bit more (check!)
- Investigate the additional bias correction,  $\mathcal{C}_{\text{calib}}$  (Working on it!)
- Bonus Round: Get MC closure (Almost done!)

## Next steps, questions, discussion points

- Finish getting MC closure
- Investigate the additional bias correction,  $\mathcal{C}_{\text{calib}}$
- Propagate uncertainties through all the analysis steps
- Decide the width that we will use to present the final results
- Write my Belle Note (/thesis) when I'm bored (FYI: already started)

# $q^2$ distribution after selection and corrections



# How to calculate moments

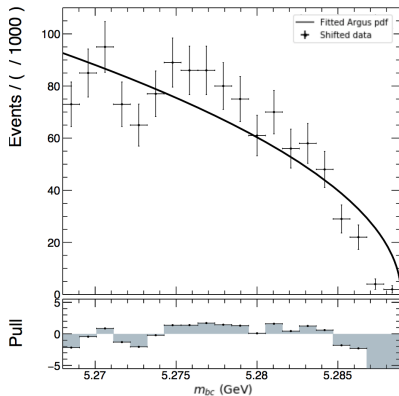
Moments calculated as a weighted mean:

$$\langle q^2 \rangle_n = \frac{\sum w_i(q^2) (q_{\text{calib},i}^2)^n}{\sum_i w_i(q^2)} \times \mathcal{C}_{\text{calib}}$$

- $w_i(q^2)$ : Event-wise signal probability as a function of  $q^2$
- $q_{\text{calib},i}^2$ : Calibrated  $q_{\text{reco}}^2$
- $\mathcal{C}_{\text{calib}}$ : Additional bias correction

# Continuum correction

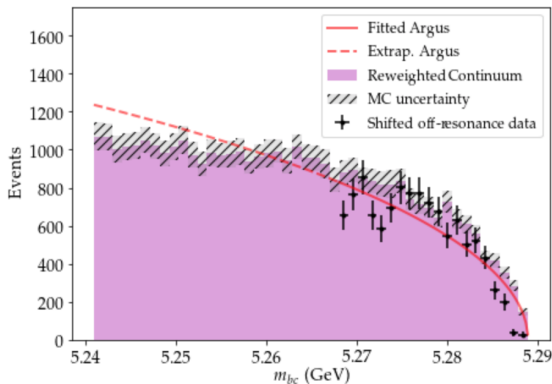
Use off-resonance data to derive a correction factor for Continuum MC



- Apply nominal selection cuts
- Shift data to end point of the distribution
- Fit Argus function to data points
- Extrapolate to full  $m_{bc}$  range

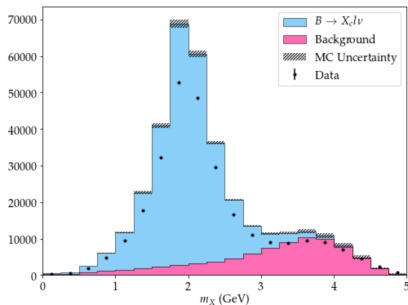
# Continuum correction

Weight the number of MC to the number of expected events from the fit result:



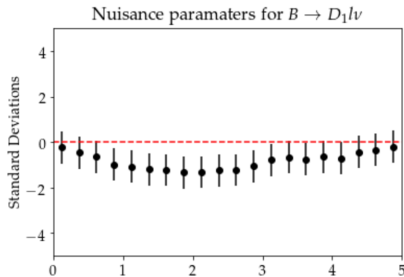
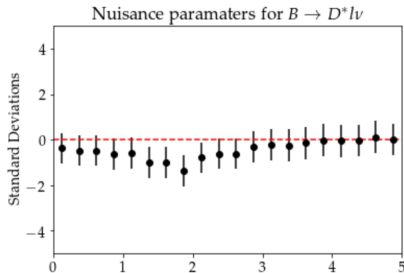
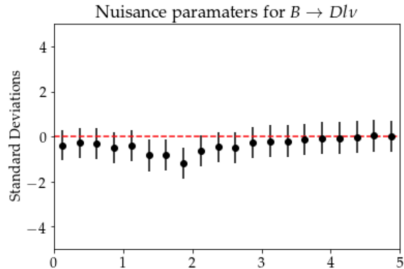
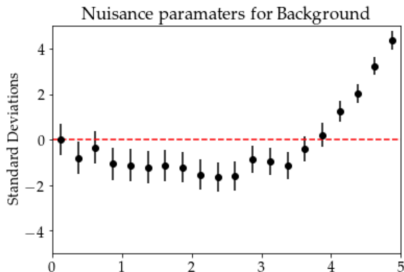
# Old background subtraction

Estimate background component from a two component template fit to  $m_X$



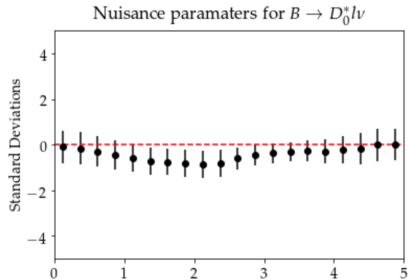
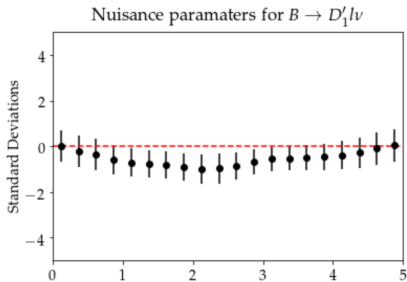
- Templates constrained to  $X_c l \nu$  BF errors (PDG 2020)
- All MC correction errors included as nuisance parameters
- Tracking error
- 100% uncertainty assigned to the Gap modes

# Old nuisance parameters





# Old nuisance parameters



# Old nuisance parameters

