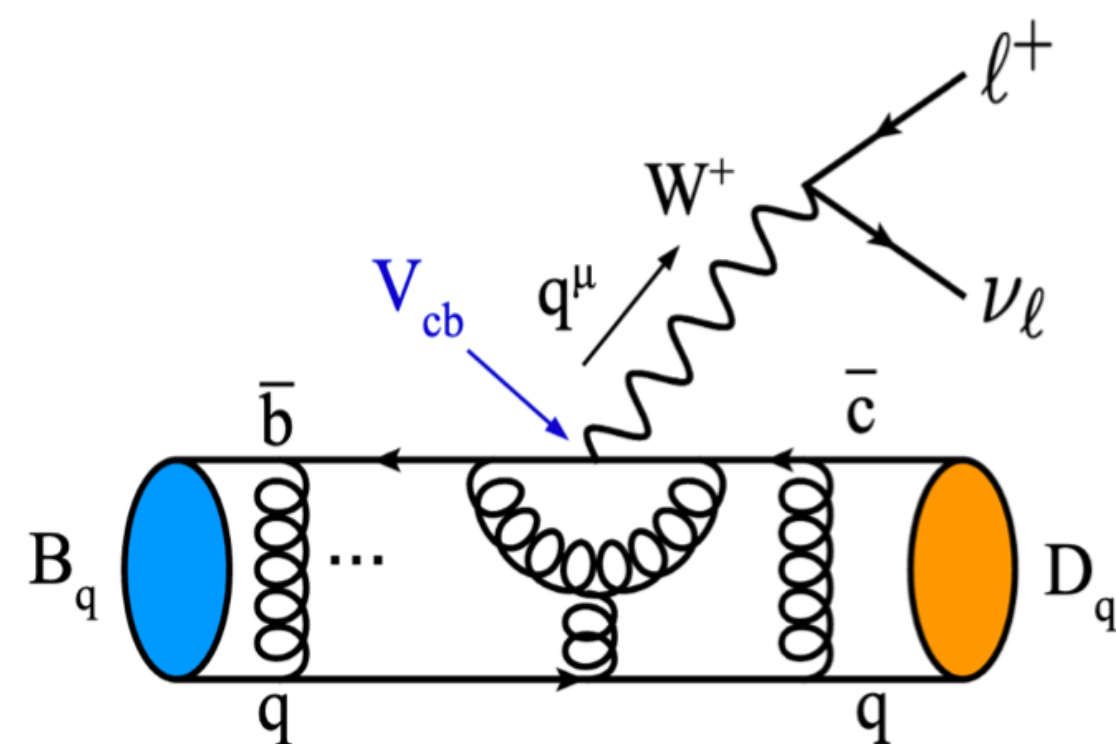
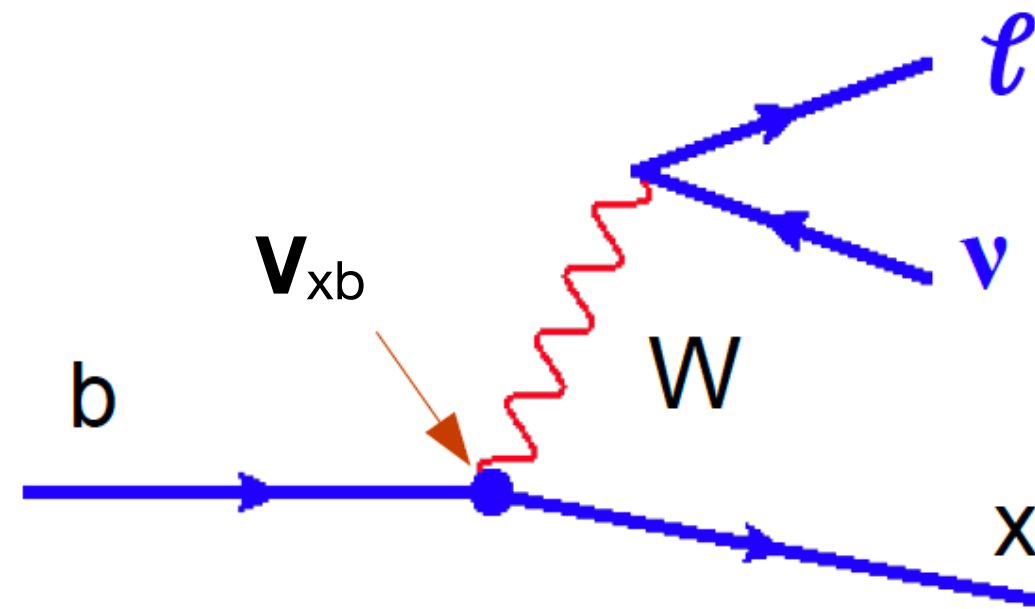


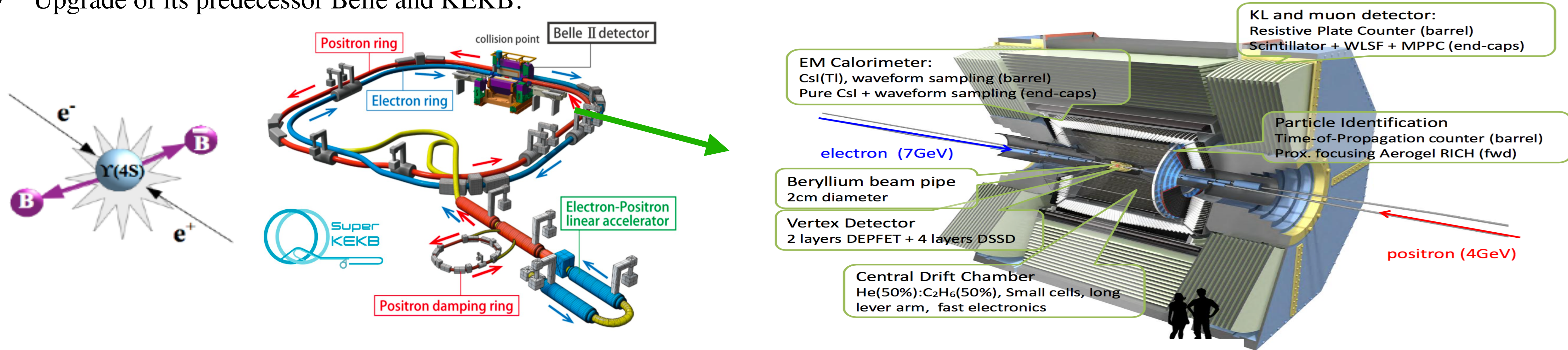
Semi-leptonic B decays at Belle II

Racha Cheaib
 DESY
 July 5th, 2021

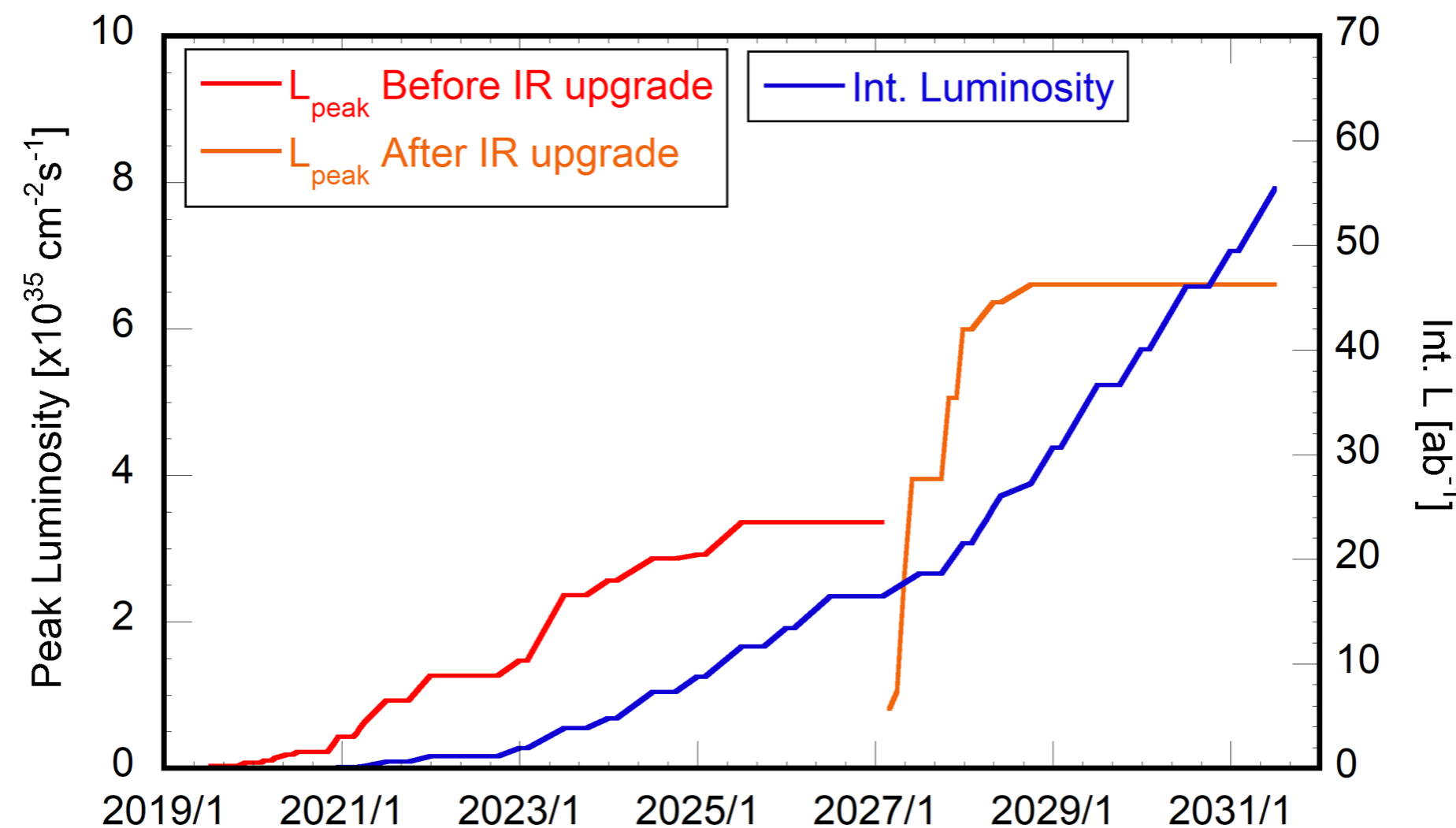


Belle II experiment

- A B meson factory in Tsukuba, Japan based on the SuperKEKB accelerator complex.
- Upgrade of its predecessor Belle and KEKB.



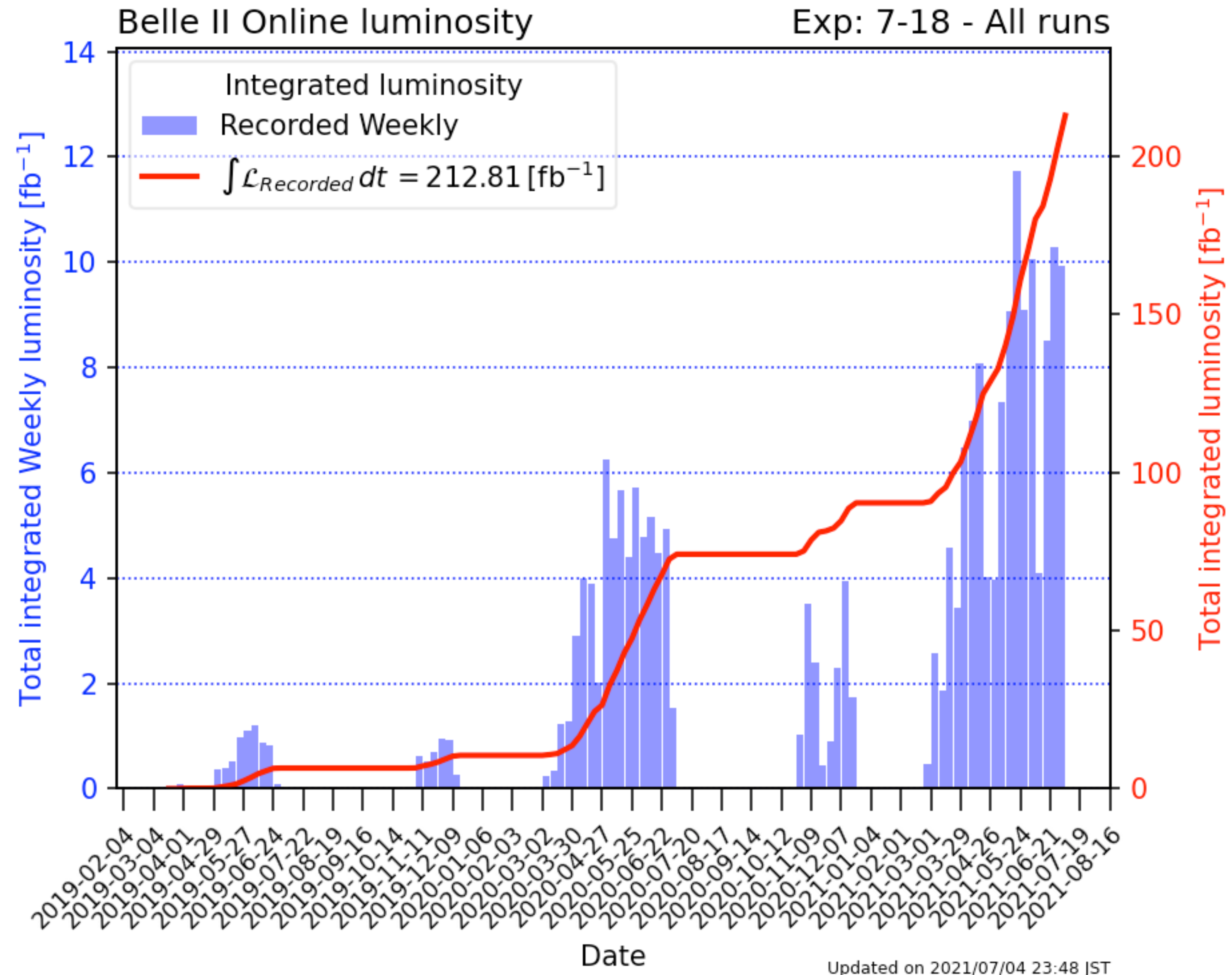
- Target luminosity: 50 ab^{-1} , 50x the Belle dataset.
- a (Super) B-factory ($\sim 1.1 \times 10^9 \text{ } B\bar{B}$ pairs per ab^{-1})
- a (Super) charm factory ($\sim 1.3 \times 10^9 \text{ } c\bar{c}$ pairs per ab^{-1})
- a (Super) τ factory ($\sim 0.9 \times 10^9 \text{ } \tau\bar{\tau}$ pairs per ab^{-1})



- B-physics:
 - CPV: $B \rightarrow J/\psi K_S^0, \phi K^0$
 - Rare B decays: $B \rightarrow K \nu \nu, K \tau^+ \tau^-$
 - Semi-leptonic B decays
- Lepton flavour violation:
 - $\tau \rightarrow \mu \gamma$
- Charm Physics: D-mixing

Current Belle II dataset

Many results
presented today
with 34.6 or 68.2
 fb^{-1} of reprocessed
data.

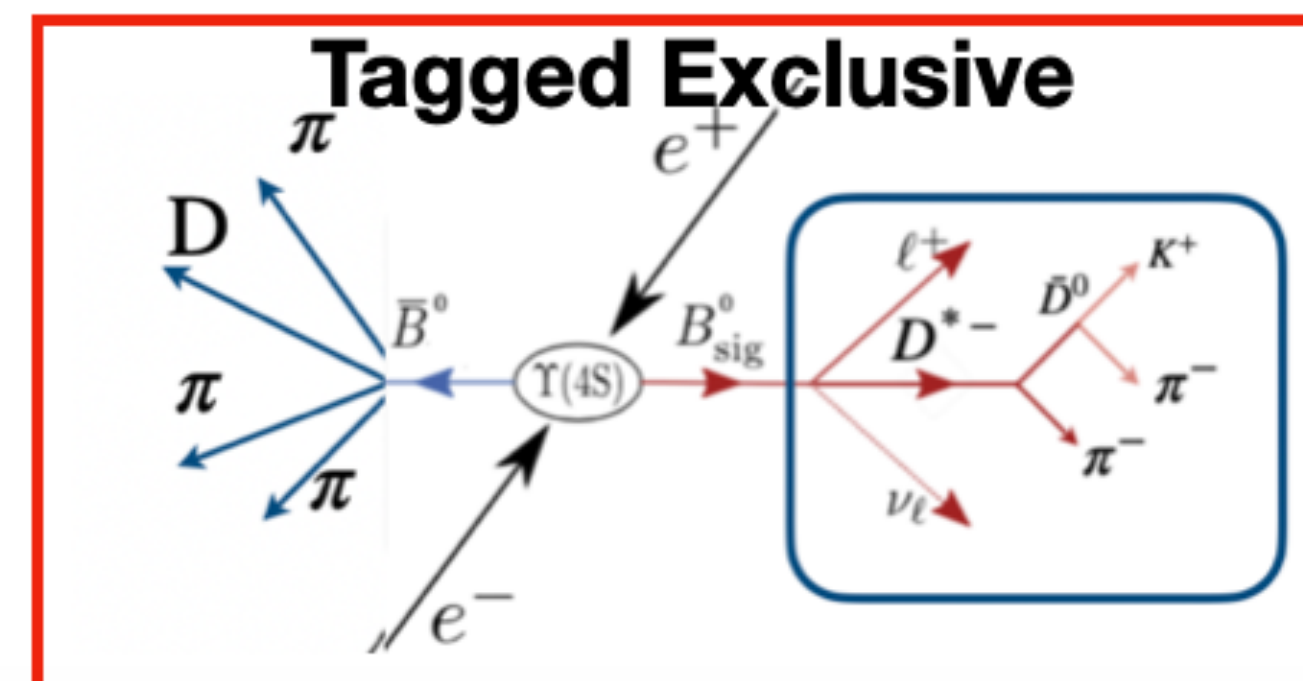
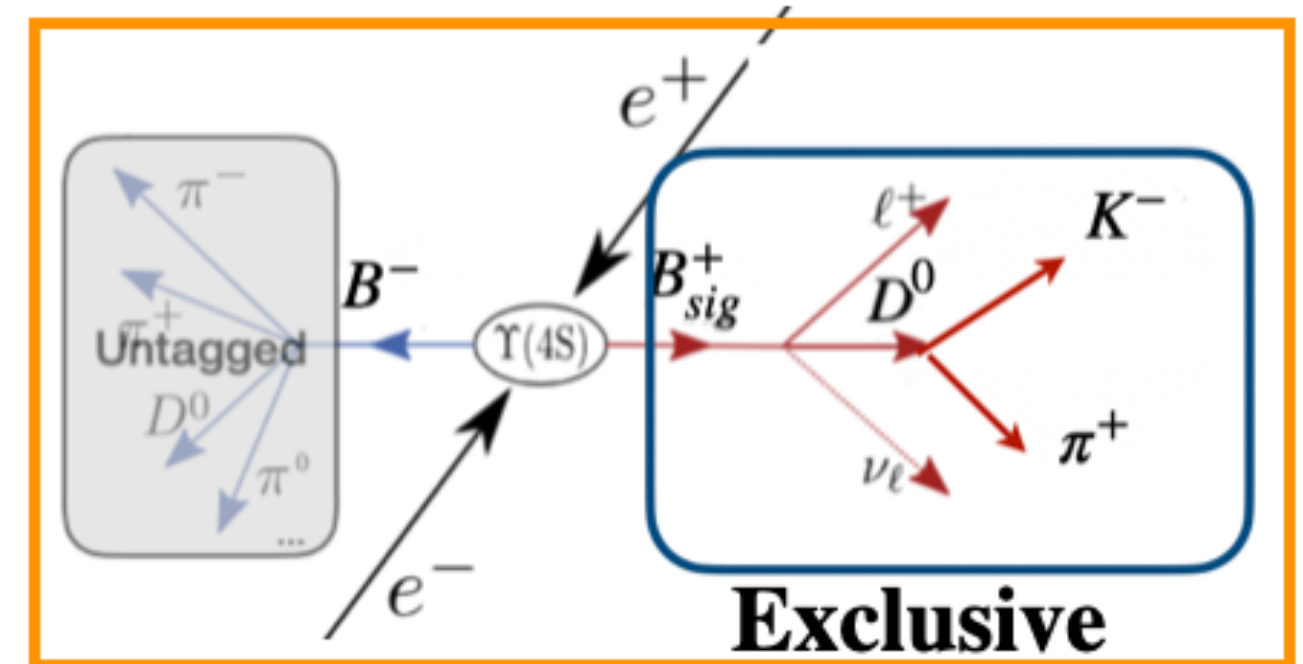
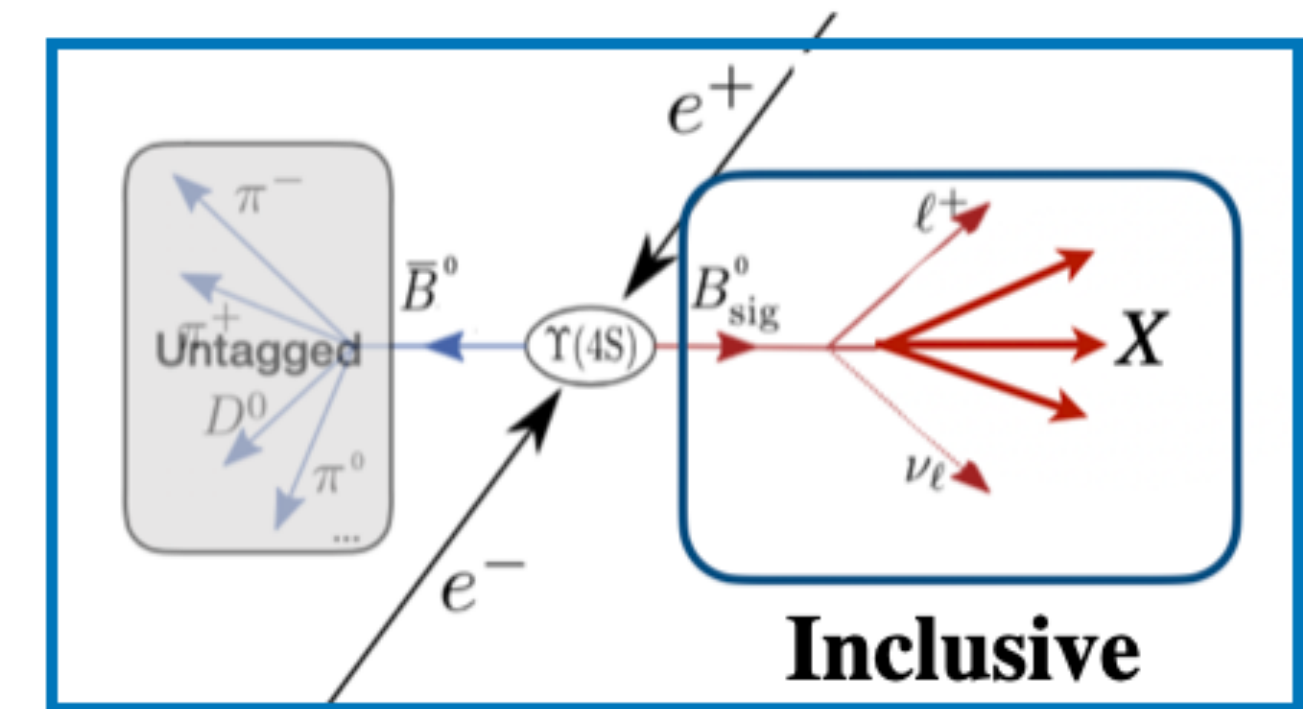
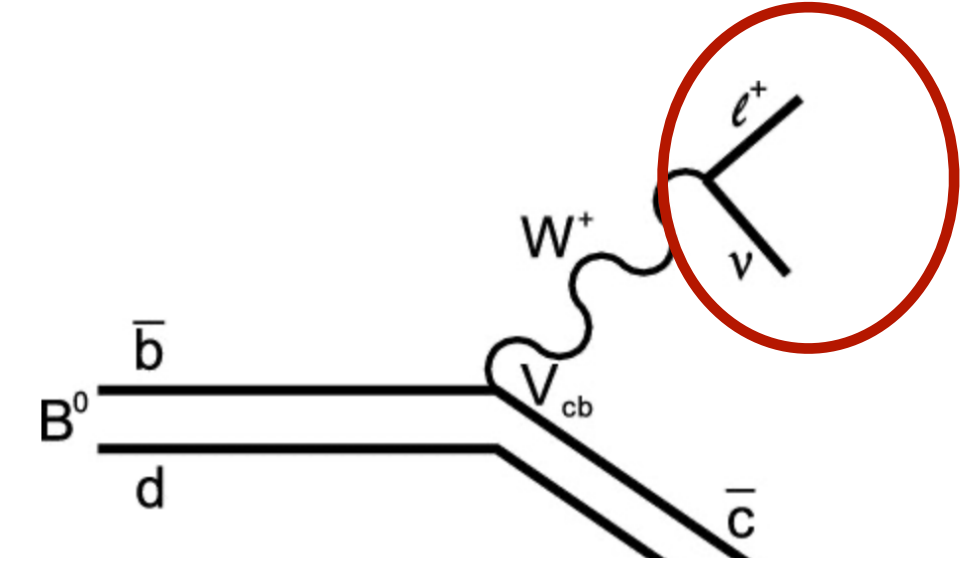
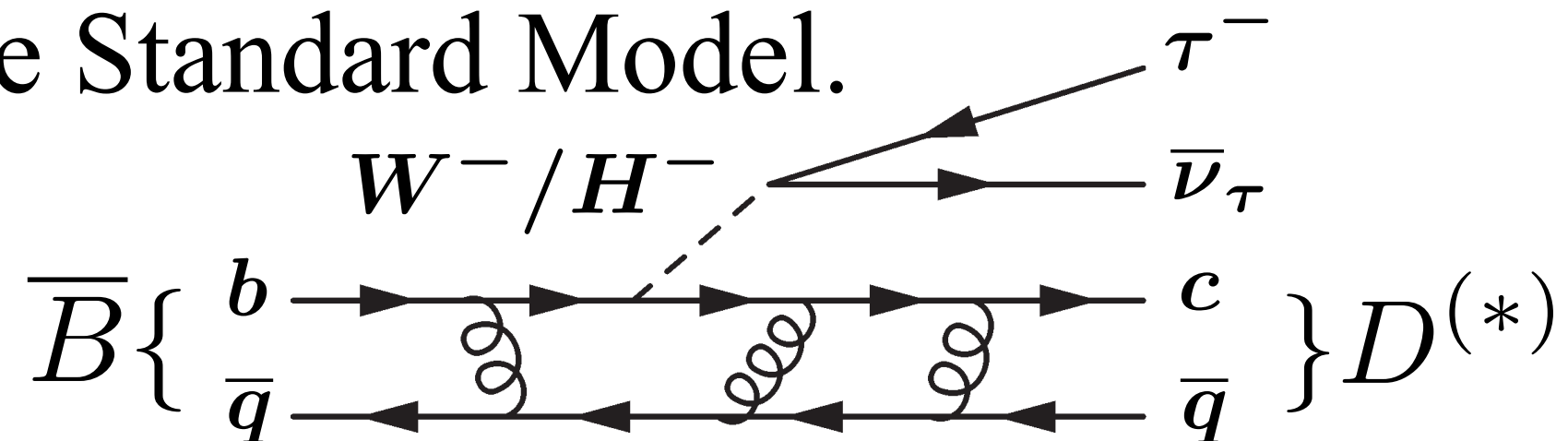


Semi-leptonic decays

- Semi-leptonic decays involve neutrinos, which is inferred as missing energy in our detector.
- Inclusive and exclusive $b \rightarrow u\ell\nu$ and $b \rightarrow c\ell\nu$ transitions are crucial for the determination of the CKM matrix elements $|V_{ub}|$ and $|V_{cb}|$.

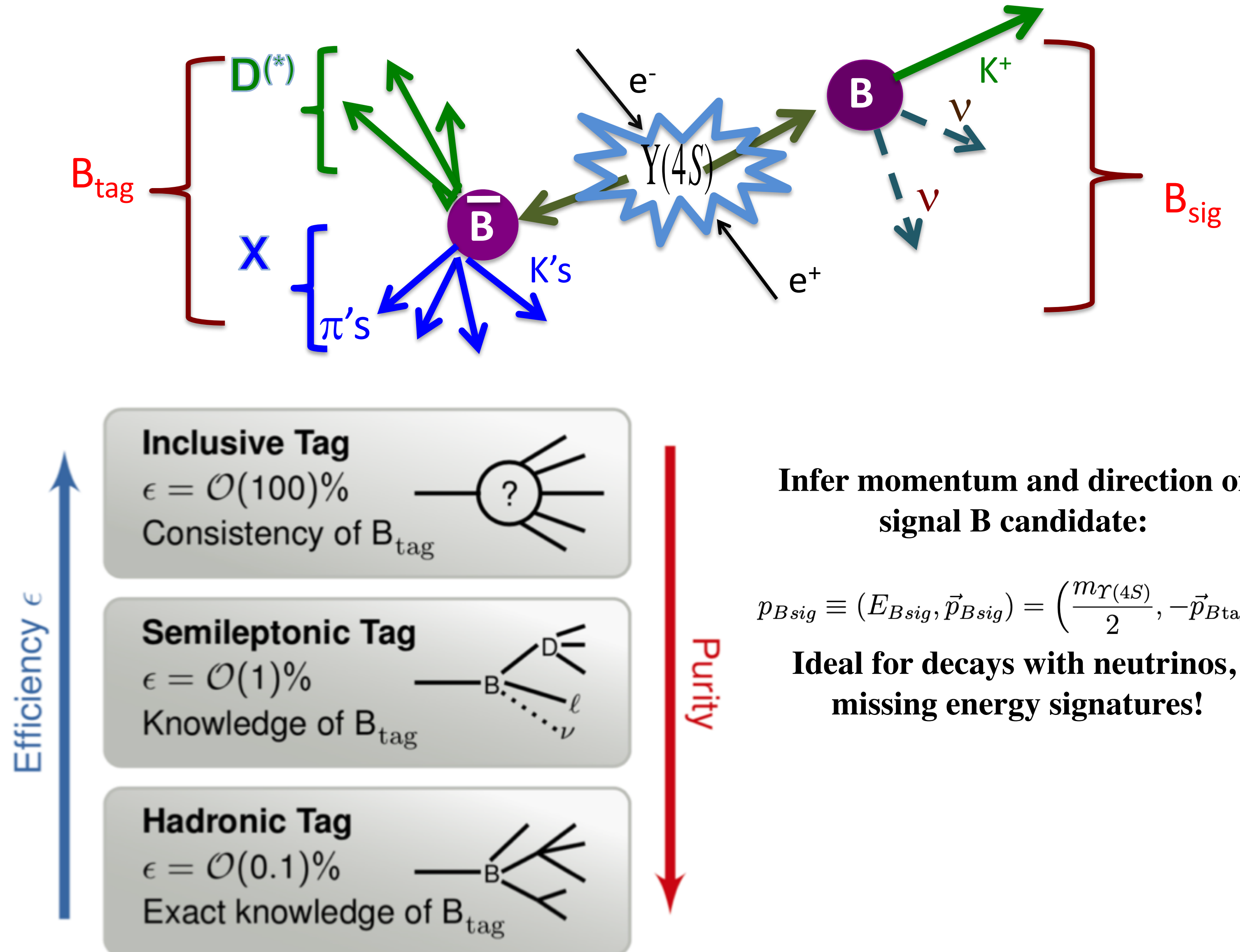
$$V = \begin{pmatrix} \begin{array}{c|c|c} d & s & b \\ \hline u & \begin{array}{c} n \\ \text{---} \end{array} \begin{array}{c} e^- \\ \bar{\nu} \end{array} \begin{array}{c} p \\ \pi \end{array} & \begin{array}{c} K \\ \text{---} \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \end{array} \begin{array}{c} \pi \end{array} & \begin{array}{c} B \\ \text{---} \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \end{array} \begin{array}{c} \pi \end{array} \\ \hline c & \begin{array}{c} D \\ \text{---} \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \end{array} \begin{array}{c} \pi \end{array} & \begin{array}{c} D \\ \text{---} \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \end{array} \begin{array}{c} K \end{array} & \begin{array}{c} B \\ \text{---} \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \end{array} \begin{array}{c} D \end{array} \\ \hline t & \begin{array}{c} B^0 \\ \text{---} \end{array} \begin{array}{c} \bar{B}^0 \end{array} & \begin{array}{c} B_s \\ \text{---} \end{array} \begin{array}{c} \bar{B}_s \end{array} & \begin{array}{c} t \\ \text{---} \end{array} \begin{array}{c} W \\ \text{---} \end{array} \begin{array}{c} b \end{array} \end{array} \end{pmatrix}$$

- Lepton Flavour Violation studies are an important probe for physics beyond the Standard Model.



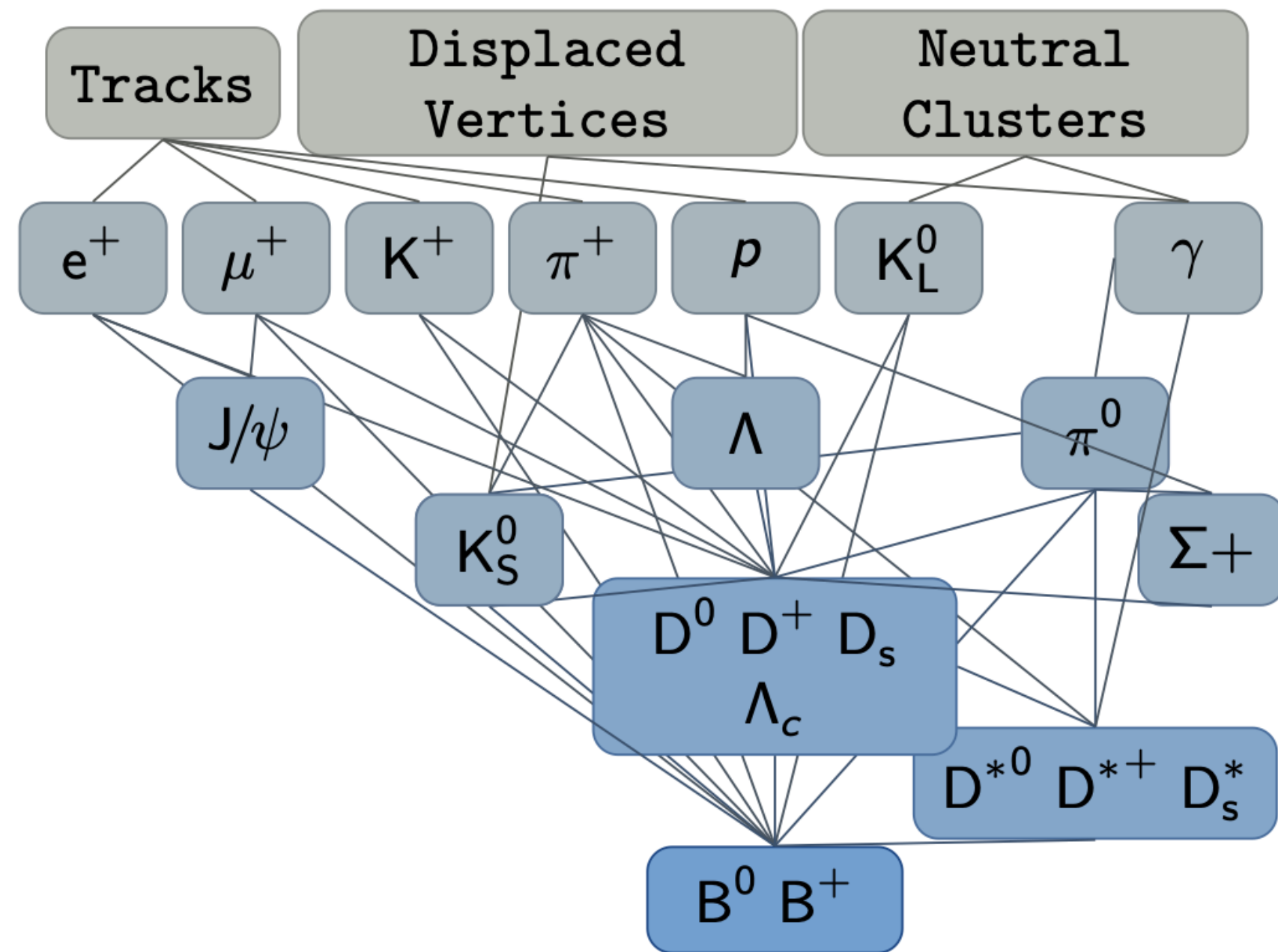
Full Event Interpretation

- Implement tagging, where one B referred to as B_{tag} is exclusively reconstructed using hadronic or semi-leptonic modes.
- The remaining tracks and clusters are then attributed to the signal B , B_{sig} , on which the search or measurement of a particular decay is done.
- Any missing energy is attributed to the B_{sig} .

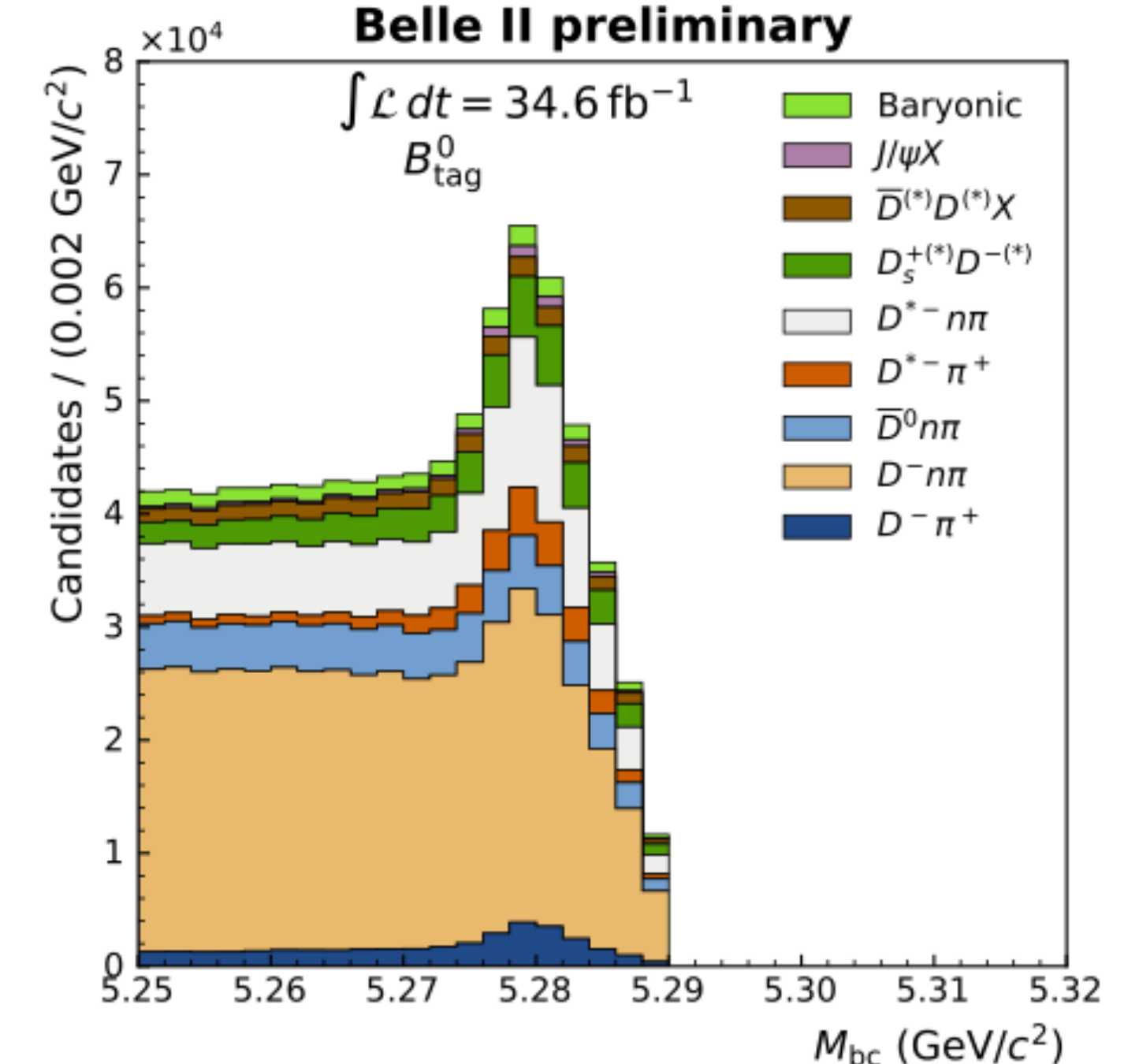
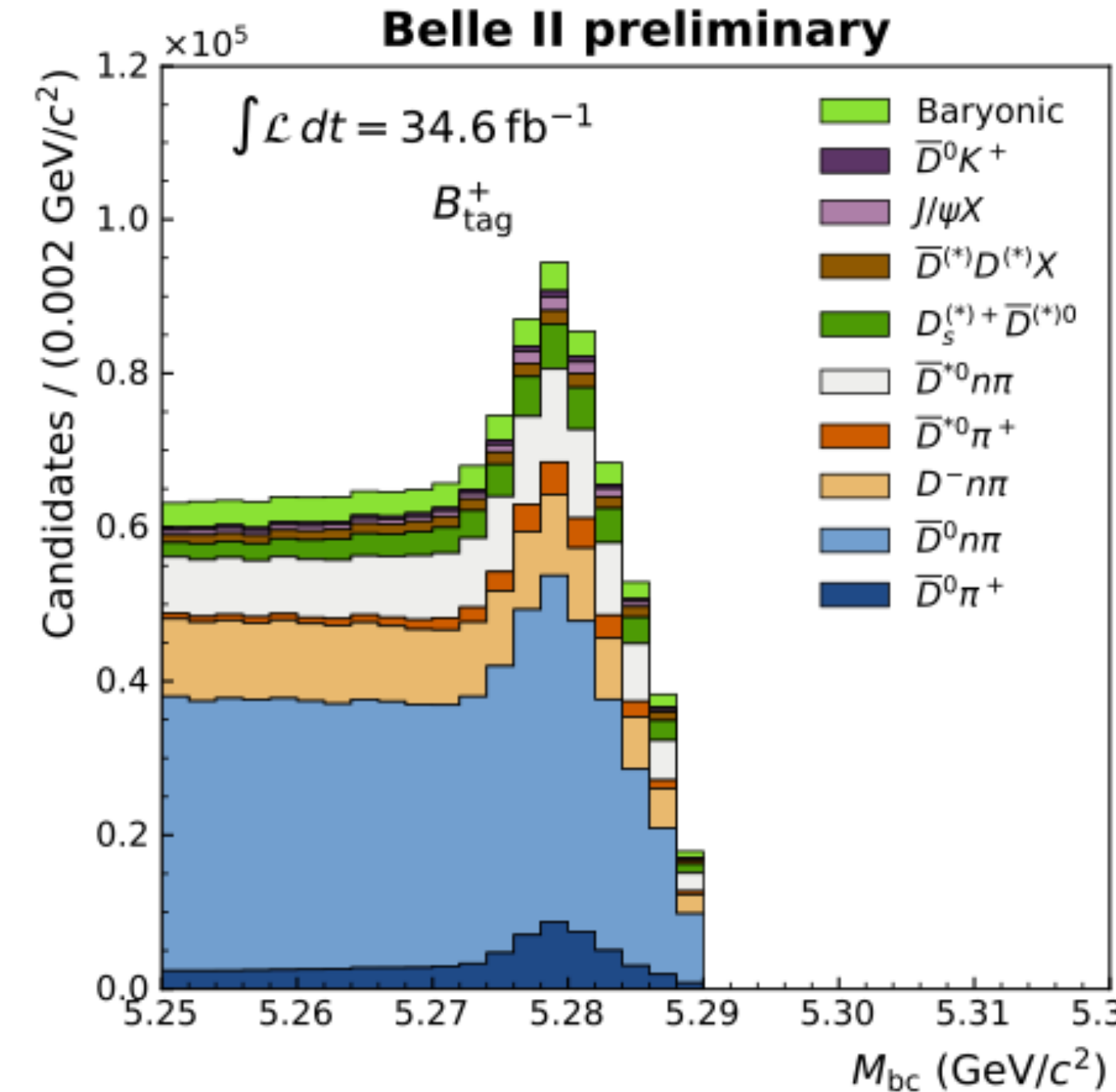


Full Event Interpretation

- Multivariate algorithm with hierarchal approach



- Employs over 200 Boosted Decision Trees to reconstruct more than 10000 B decay modes.



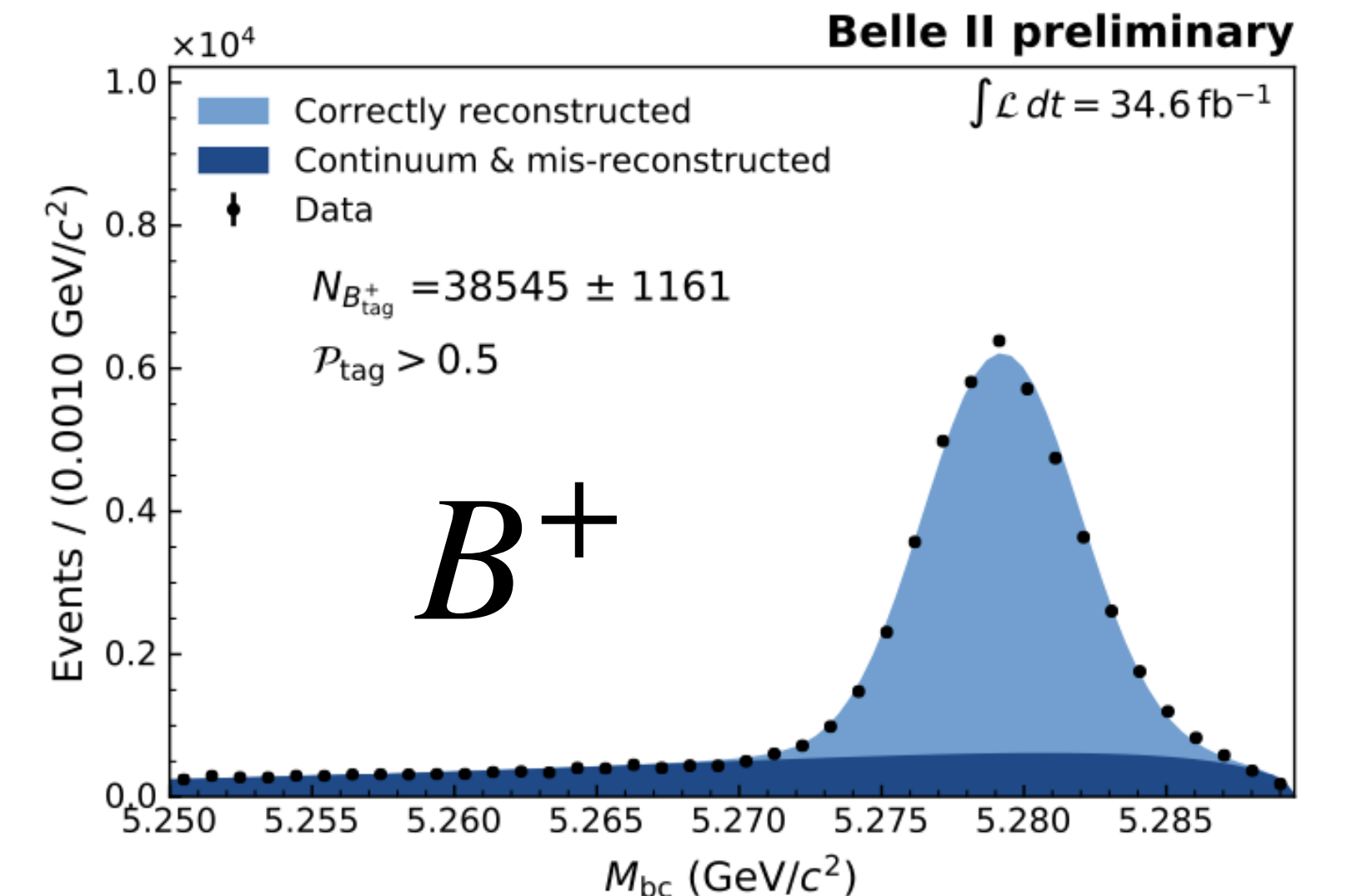
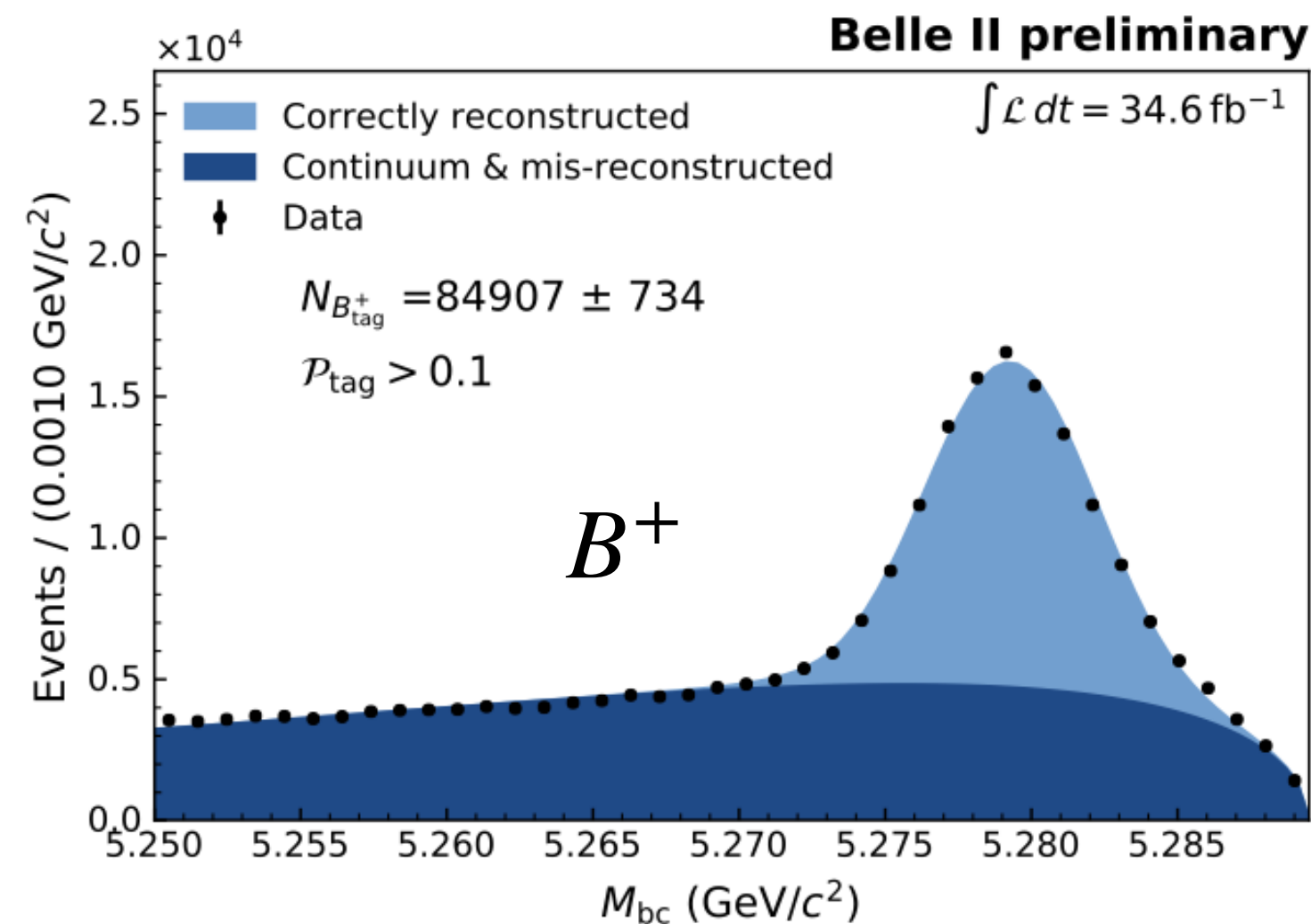
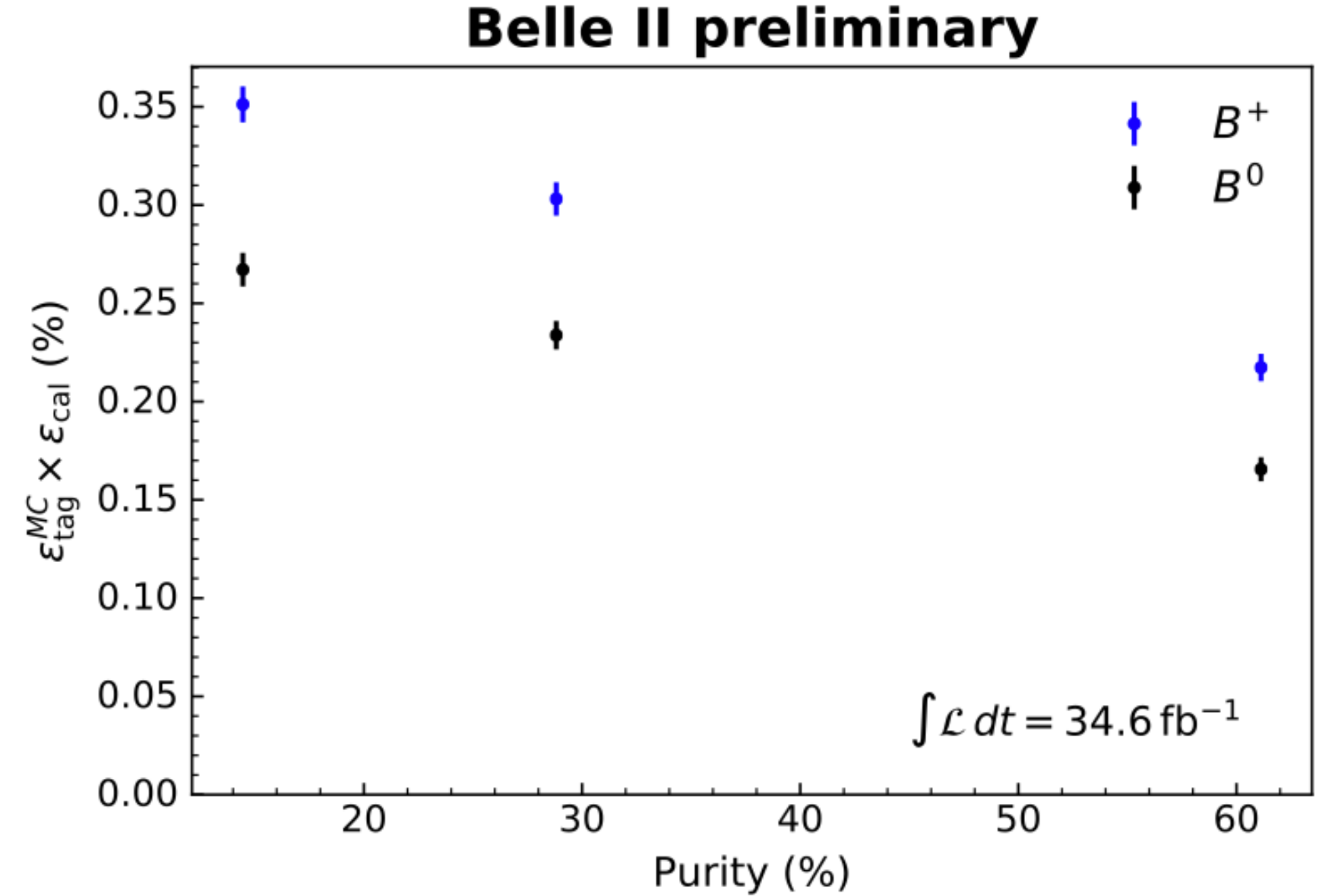
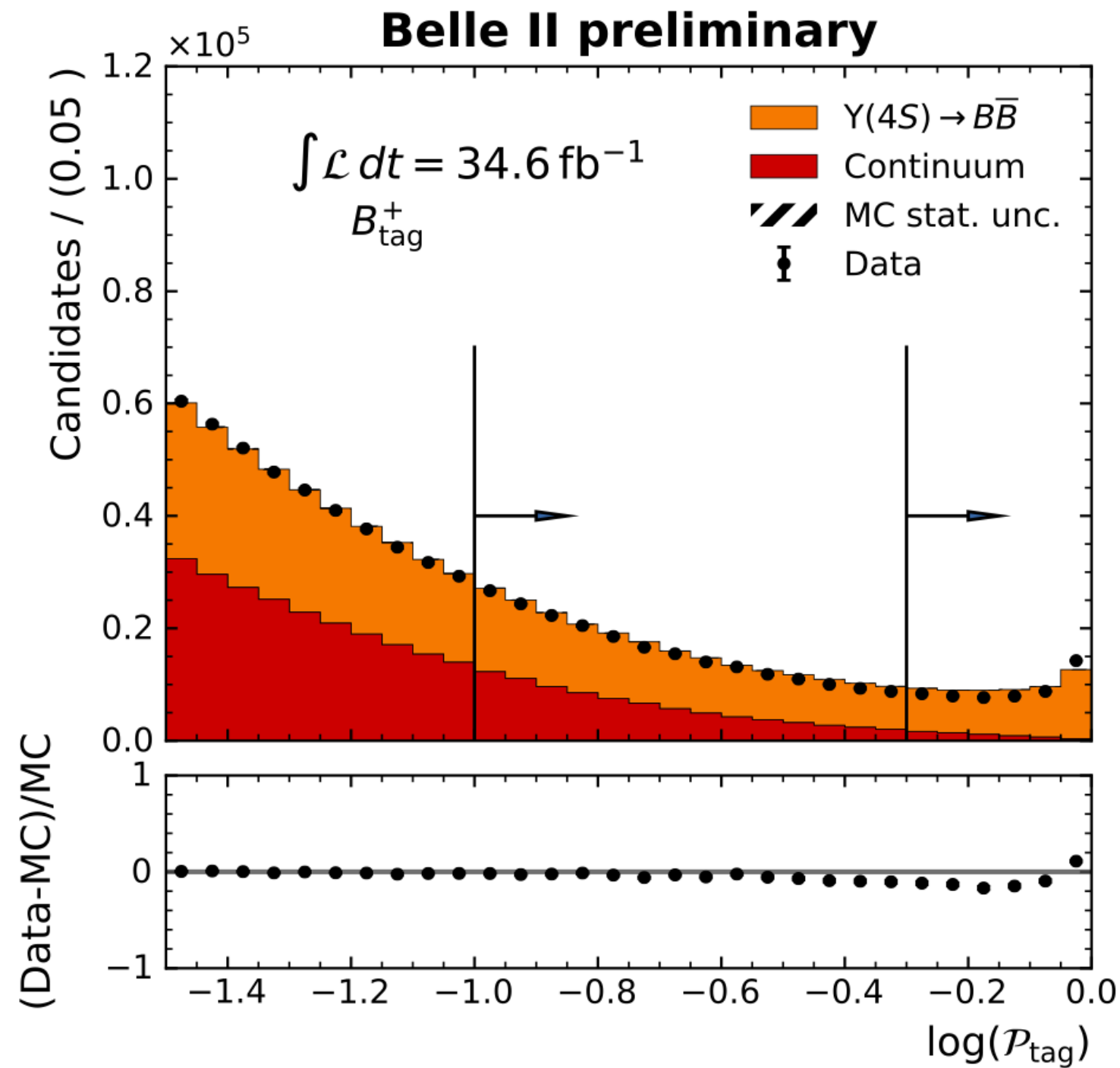
$$M_{bc} = \sqrt{E_{\text{beam}}^2/4 - (p_{B_{\text{tag}}}^{\text{cm}})^2}$$

Tagging Algorithm	Had B ⁺ /B ⁰	SL B ⁺ /B ⁰
Full Reconstruction Belle	0.28/0.18	0.67/0.63
FEI Belle	0.78/0.46	1.80/2.04

MC Tagging efficiency at
10% purity!

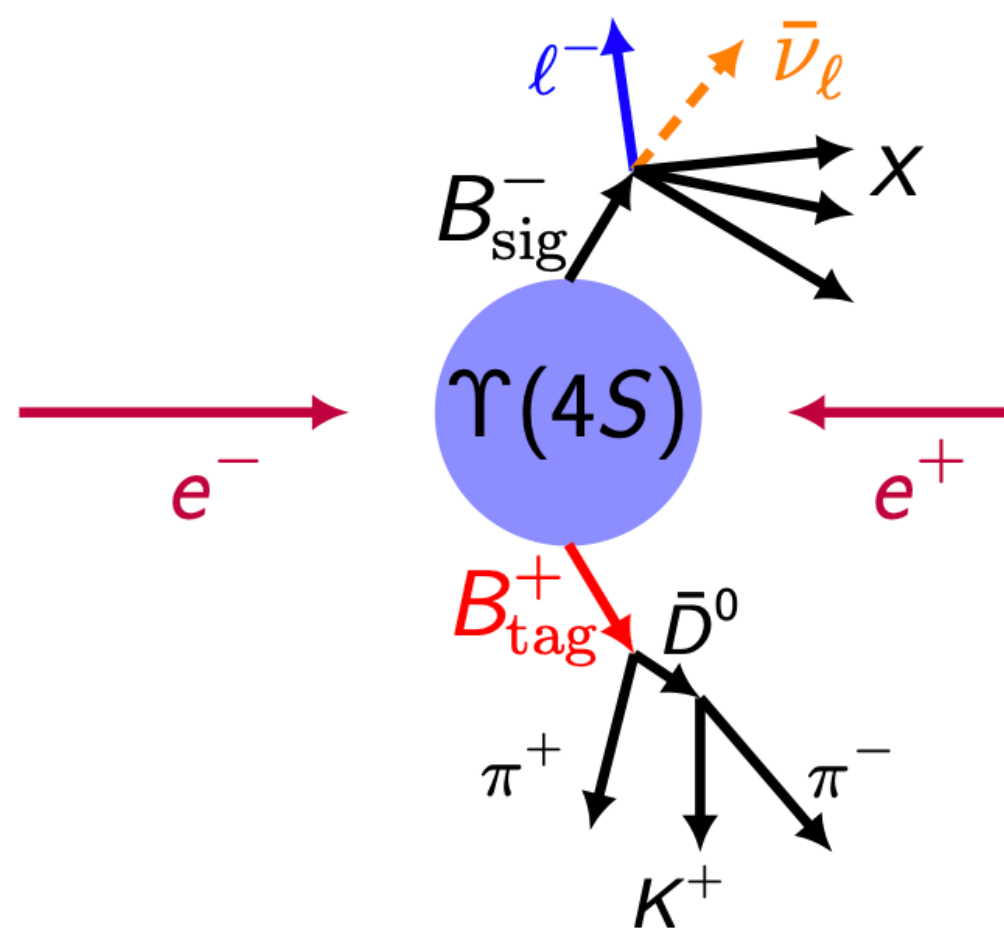
FEI signal probability

- Output of the FEI is a signal probability between 0 (mis-reconstructed) and 1 (properly reconstructed) B_{tag} candidate.
- Purity and efficiency of B_{tag} sample varies with FEI signal probability cut.



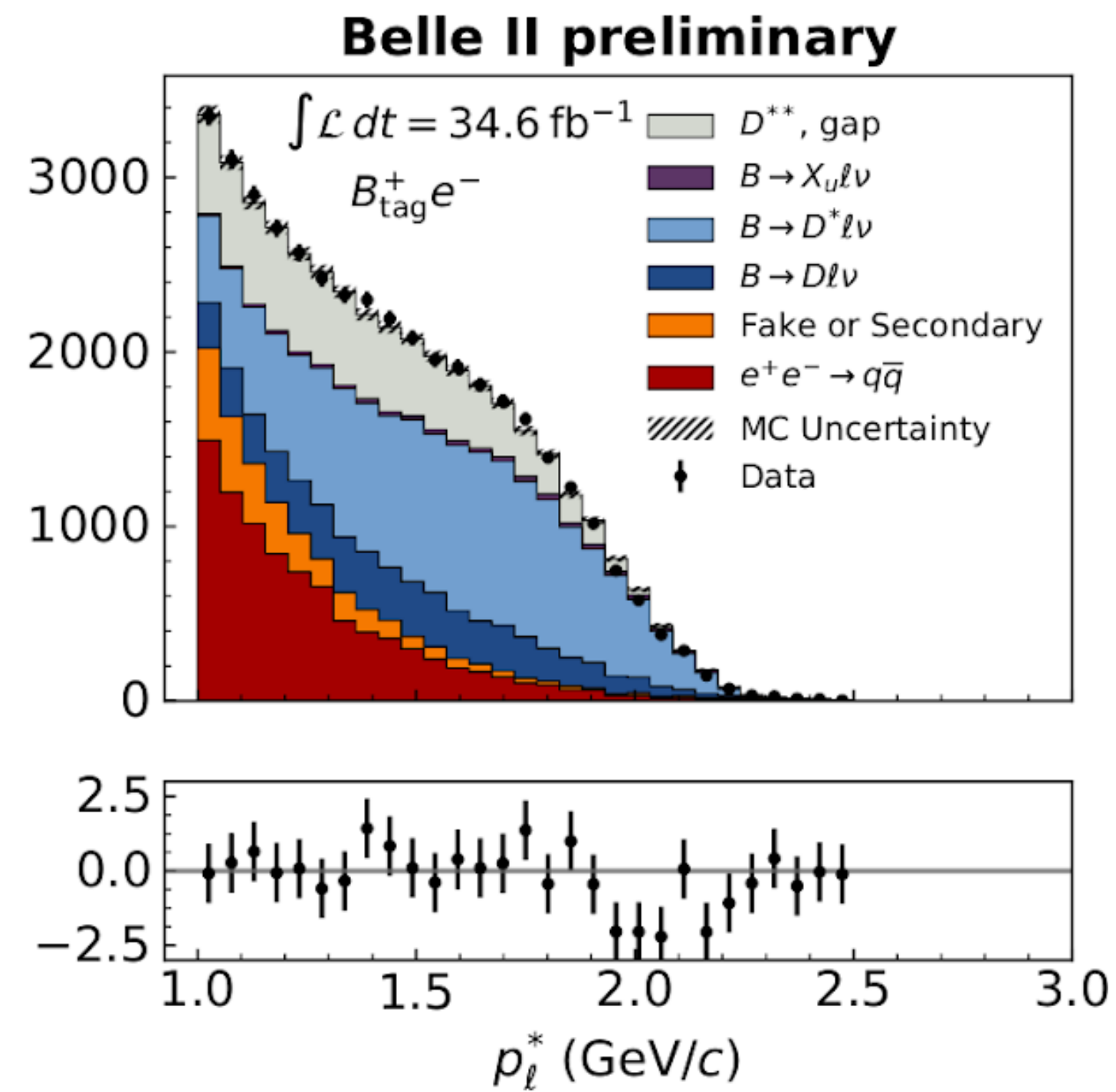
Hadronic FEI calibration

- calibration is required to account for data MC differences in the FEI algorithm.
- Using a signal side decay with a large branching fraction $B \rightarrow X\ell\nu$ ($\sim 20\%$), the efficiency of the FEI is compared between data and MC.

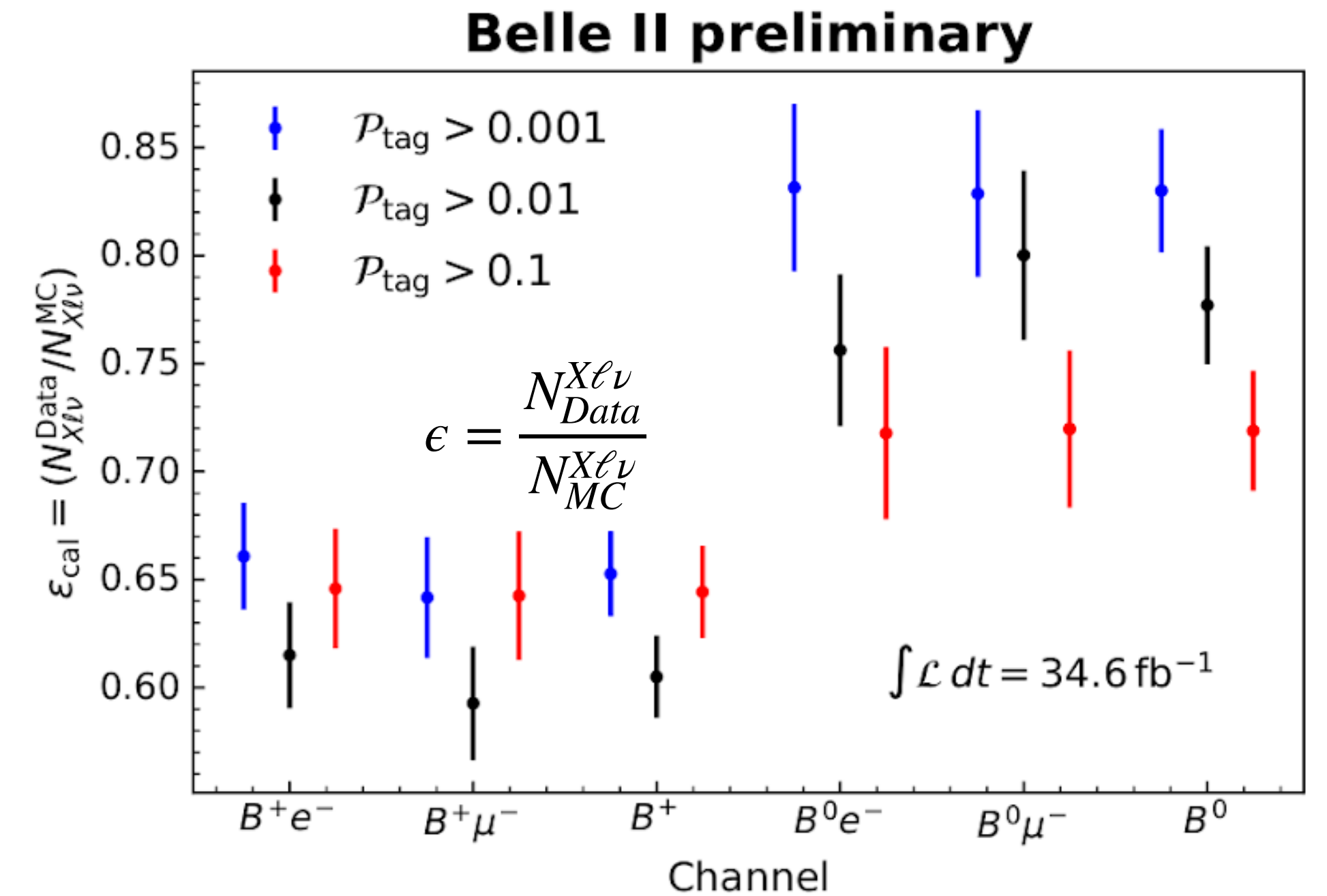


Require B_{tag} candidate with
 $M_{\text{bc}} > 5.27 \text{ GeV}/c^2$ and
 $-0.15 < \Delta E < 0.1 \text{ GeV}$.

Look for signal side lepton
 with momentum (in B_{sig} rest
 frame) $> 1 \text{ GeV}/c$.



$\mathcal{P}_{B^+} >$	ϵ	% uncertainty
0.001	0.653 ± 0.020	3.02
0.01	0.605 ± 0.019	3.13
0.1	0.644 ± 0.021	3.30



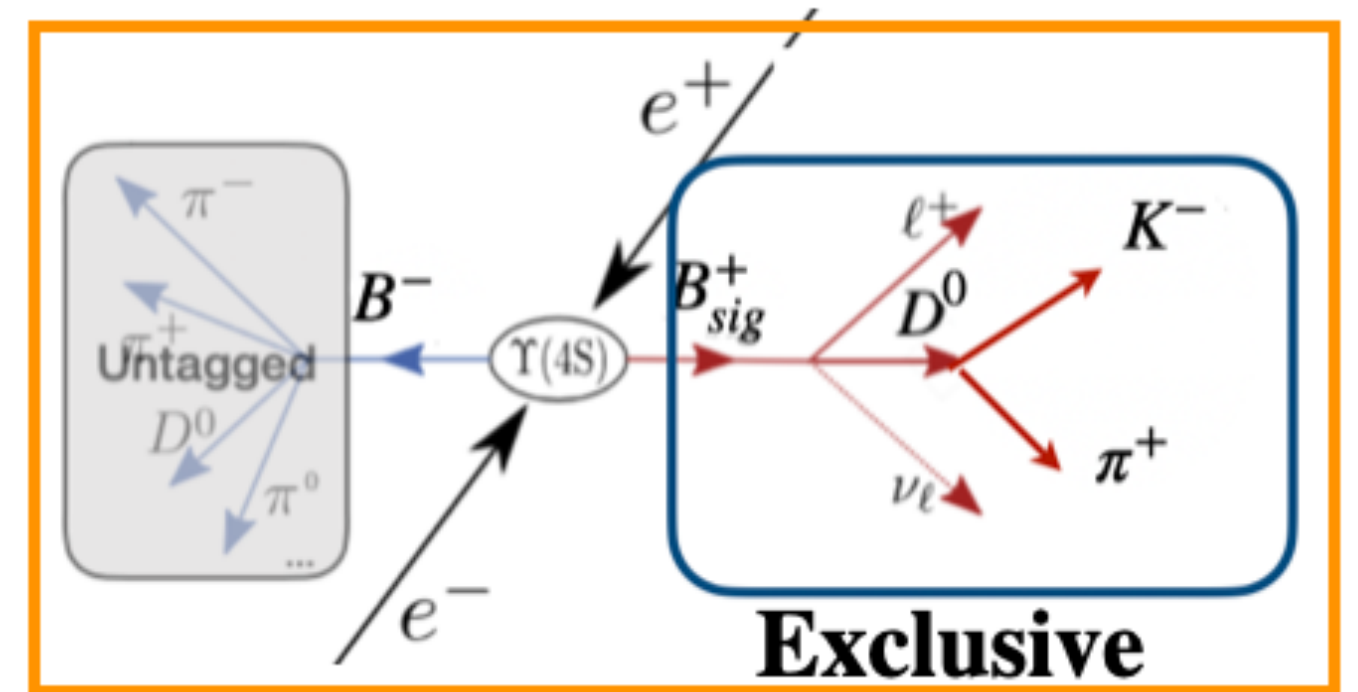
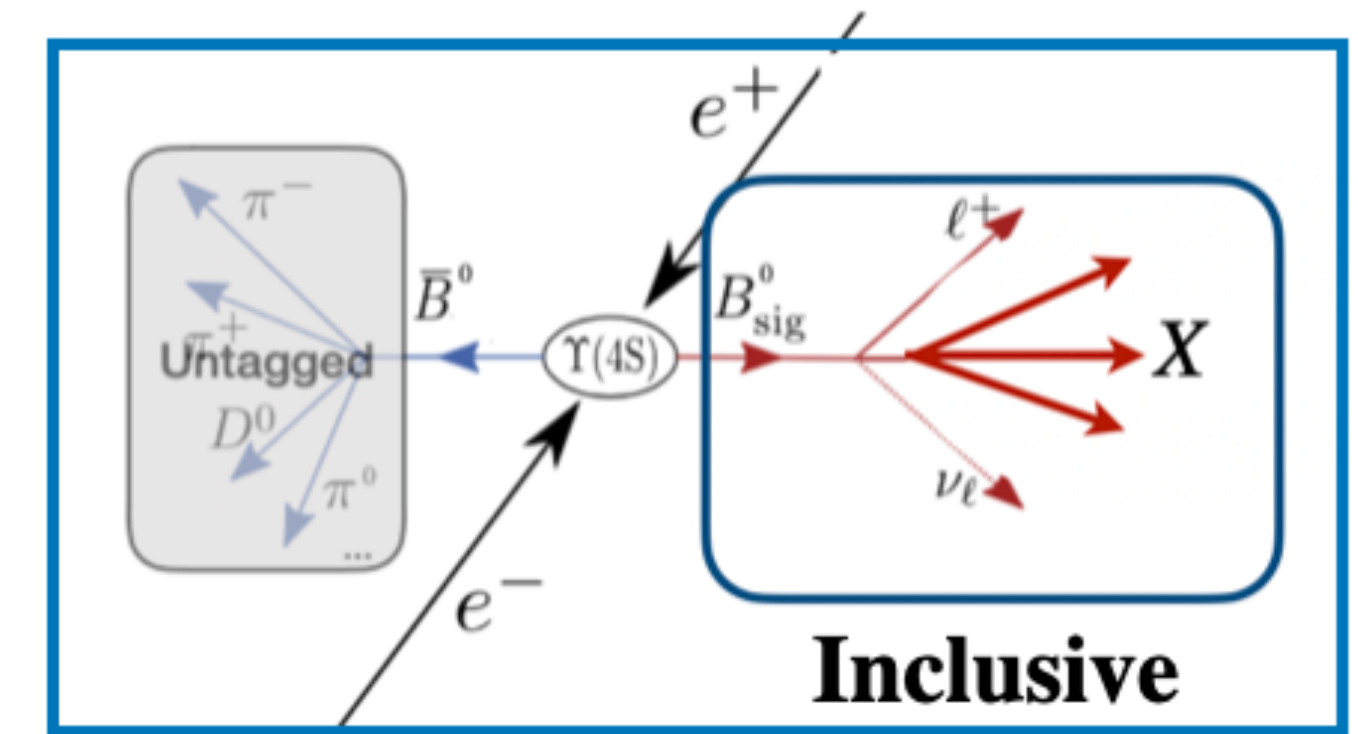
$\mathcal{P}_{B^0} >$	ϵ	% uncertainty
0.001	0.830 ± 0.029	3.44
0.01	0.777 ± 0.027	3.51
0.1	0.719 ± 0.028	3.87

$b \rightarrow c \ell \nu$

- $B \rightarrow X_c \ell \nu$: main channel for inclusive $|V_{cb}|$ determination.

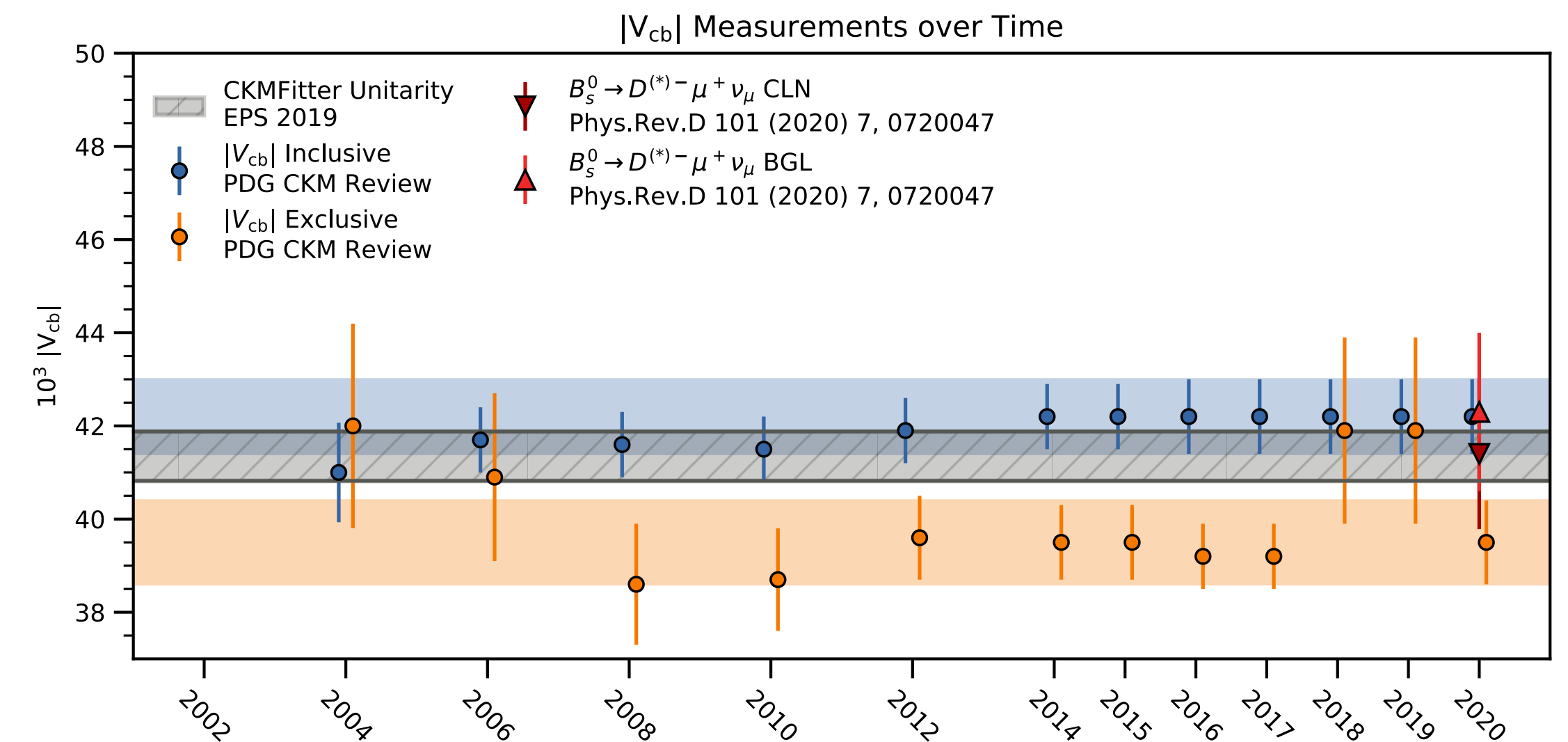
$$\Gamma = \frac{G_F^2 m_b^5}{192 \pi^3} |V_{cb}|^2 \left(1 + \frac{c_5(\mu) \langle O_5 \rangle(\mu)}{m_b^2} + \frac{c_6(\mu) \langle O_6 \rangle(\mu)}{m_b^3} + \mathcal{O}\left(\frac{1}{m_b^4}\right) \right)$$

- Heavy Quark expansion of decay rate with non-perturbative matrix elements and perturbative coefficients.
- Non-perturbative parameters determined using the lepton energy or hadronic mass moments of $B \rightarrow X_c \ell \nu$
- $B \rightarrow D^{(*)} \ell \nu$: main channel for exclusive $|V_{cb}|$ determination:
 - Clean experimental modes with low background.
 - Decay rate requires input on the form factor parametrization.



$$|V_{cb}| = (42.2 \pm 0.8) \times 10^{-3} \text{ (inclusive) PDG value}$$

$$|V_{cb}| = (39.5 \pm 0.9) \times 10^{-3} \text{ (exclusive) PDG value}$$



Tension between exclusive and inclusive determinations.

Tagged Exclusive $B^0 \rightarrow D^{*+} \ell \nu$

- Clean mode for testing FEI calibration and Belle II analysis chain.
- Identify B_{tag} candidate with $M_{\text{bc}} > 5.27 \text{ GeV}/c^2$
 $-0.15 < \Delta E < 0.1$ and FEI signal probability > 0.001 .
- Reconstruct D^0 meson from oppositely charged tracks and form D^{*+} with $0.143 < \Delta M < 0.148 \text{ GeV}/c^2$
- Identify high momentum lepton with $p_l^* > 1.0 \text{ GeV}$ and determine M_{miss}^2

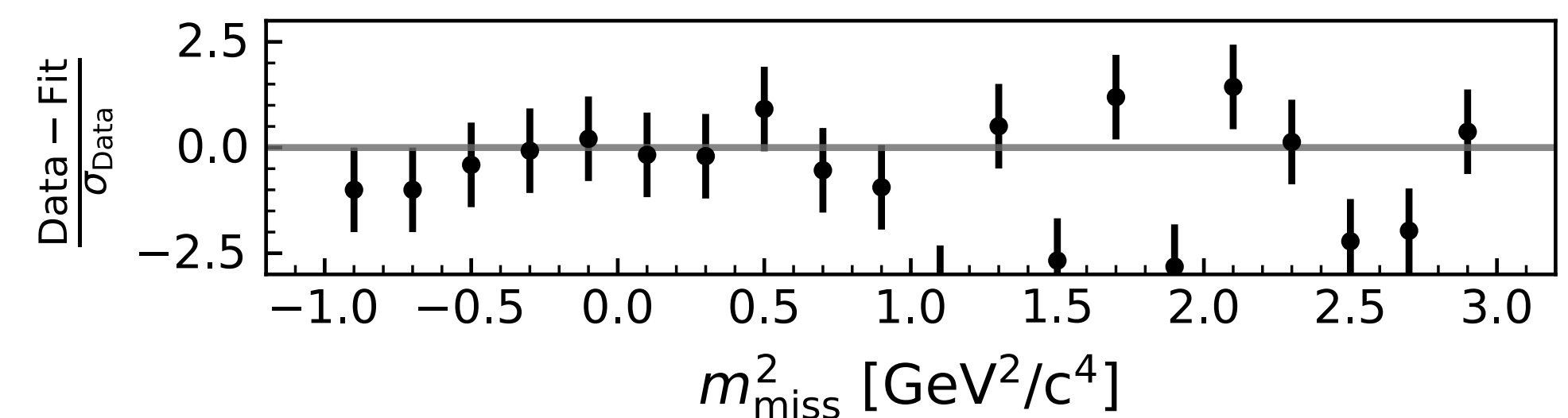
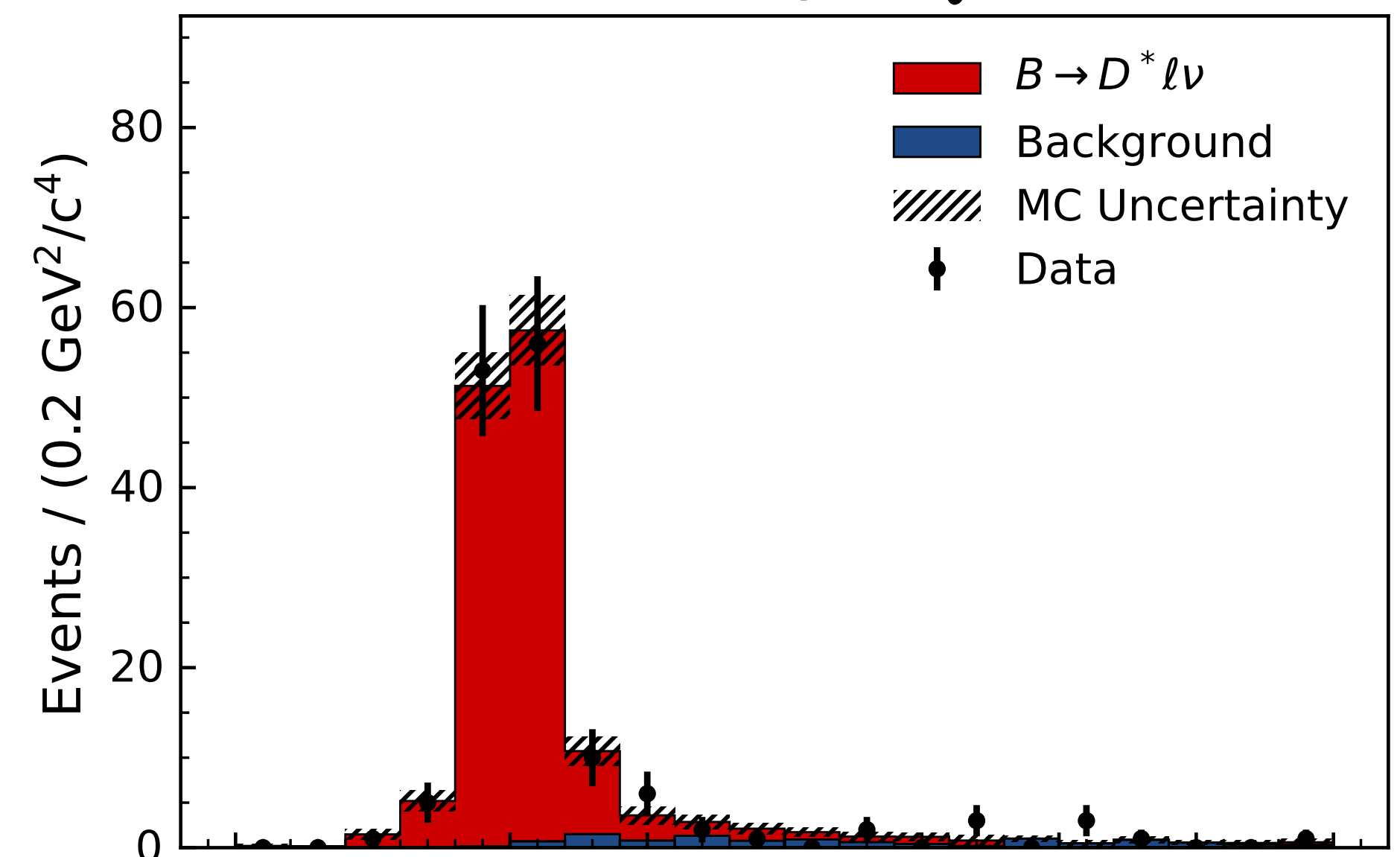
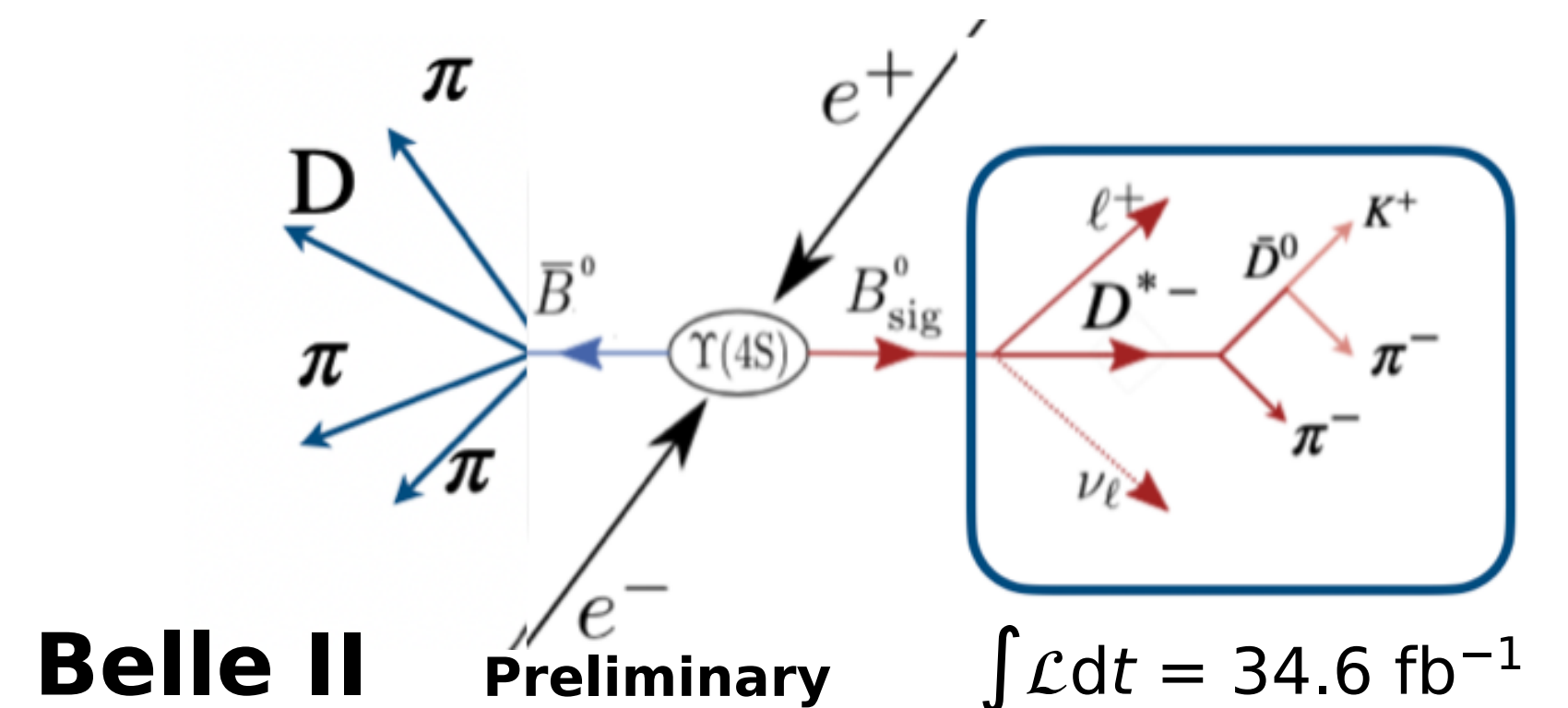
$$m_{\text{miss}}^2 = \left(p_{e^+ e^-} - p_{B_{\text{tag}}} - p_{D^*} - p_{\ell} \right)^2$$

- Extract signal yield using a fit to signal + background:

$$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \ell \nu_{\ell}) = (4.51 \pm 0.41_{\text{stat}} \pm 0.27_{\text{syst}} \pm 0.45_{\pi_s}) \%$$

In agreement with world average

$$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \ell \nu_{\ell}) = (5.05 \pm 0.14) \%$$



Untagged Exclusive $B \rightarrow D^{*+} \ell \nu$

Flagship decay for exclusive $|V_{cb}|$ measurements!

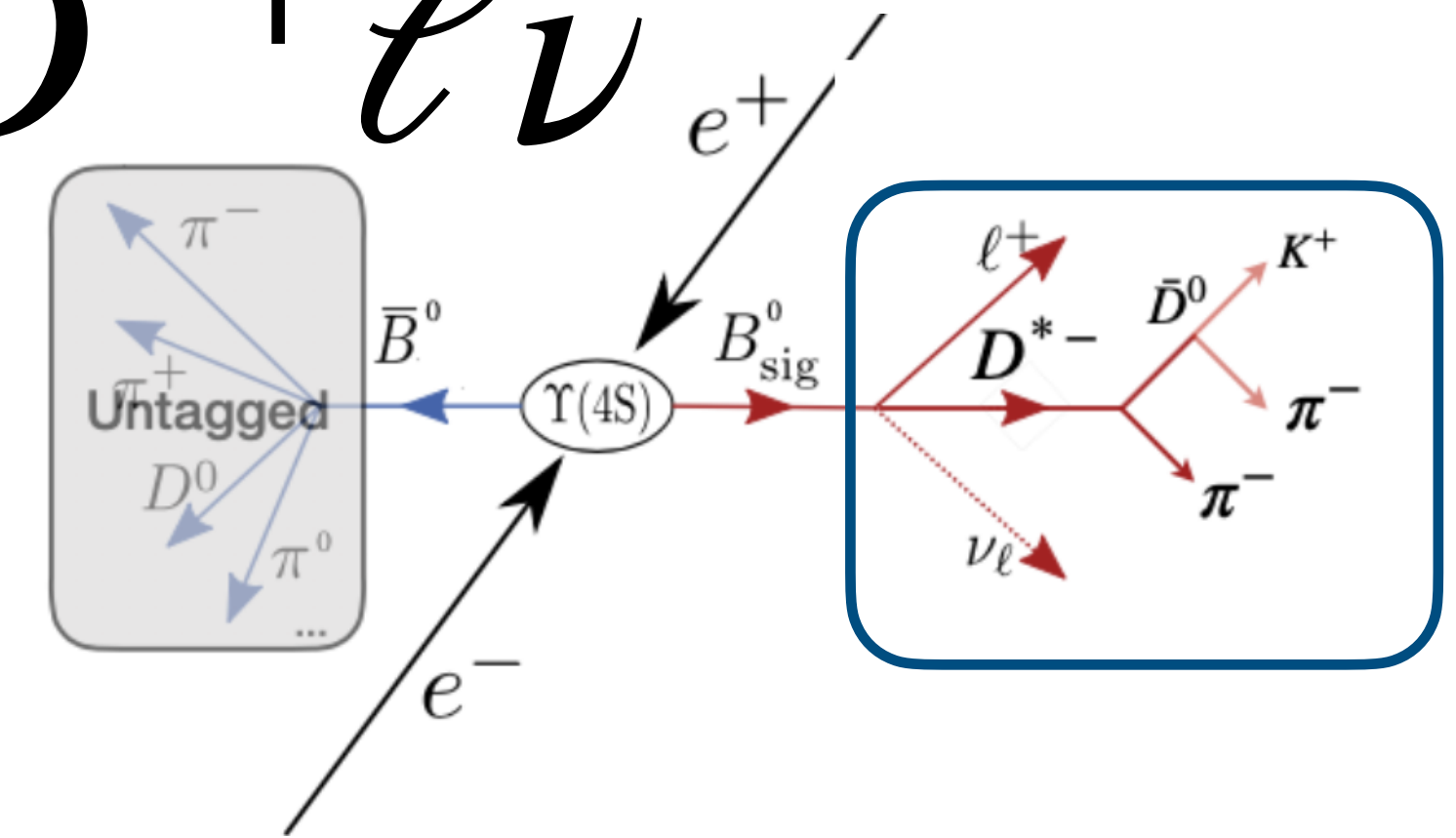
Reconstruct $D^0 \rightarrow K^- \pi^+$ and $D^{*+} \rightarrow D^0 \pi_s$.

Identify lepton using PID algorithms.

Suppress $e^+ e^- \rightarrow q \bar{q}$ events using $p_{D^*} < 2.4 \text{ GeV}/c$ and $R_2 < 0.3$.

Extract signal yield with a fit to $\cos \theta_{BY}$, where $Y = D^* \ell$.

$$\cos \theta_{BY} = \frac{2E_B^* E_Y^* - m_B^2 - m_Y^2}{2|p_B^*||p_Y^*|}$$

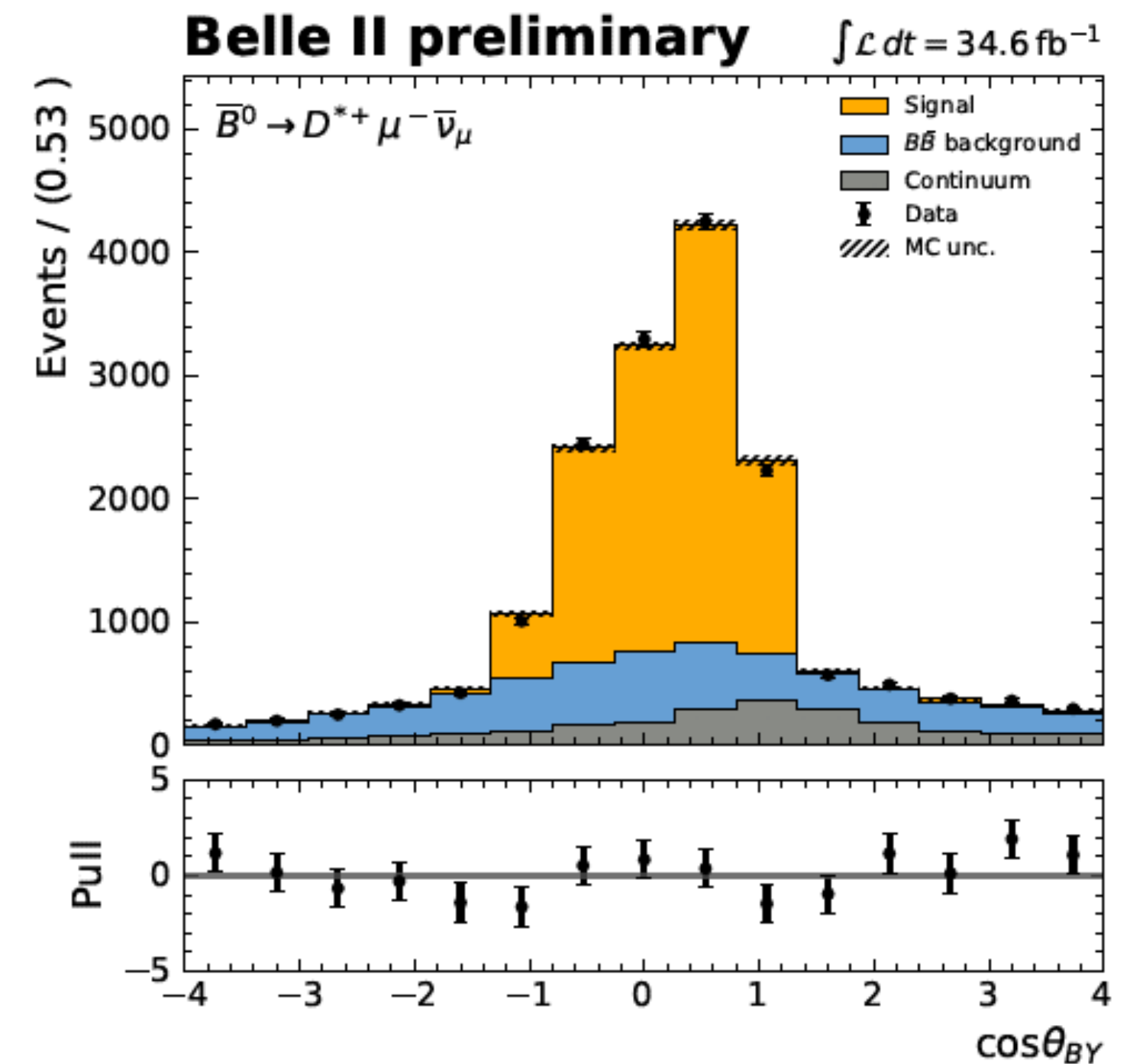
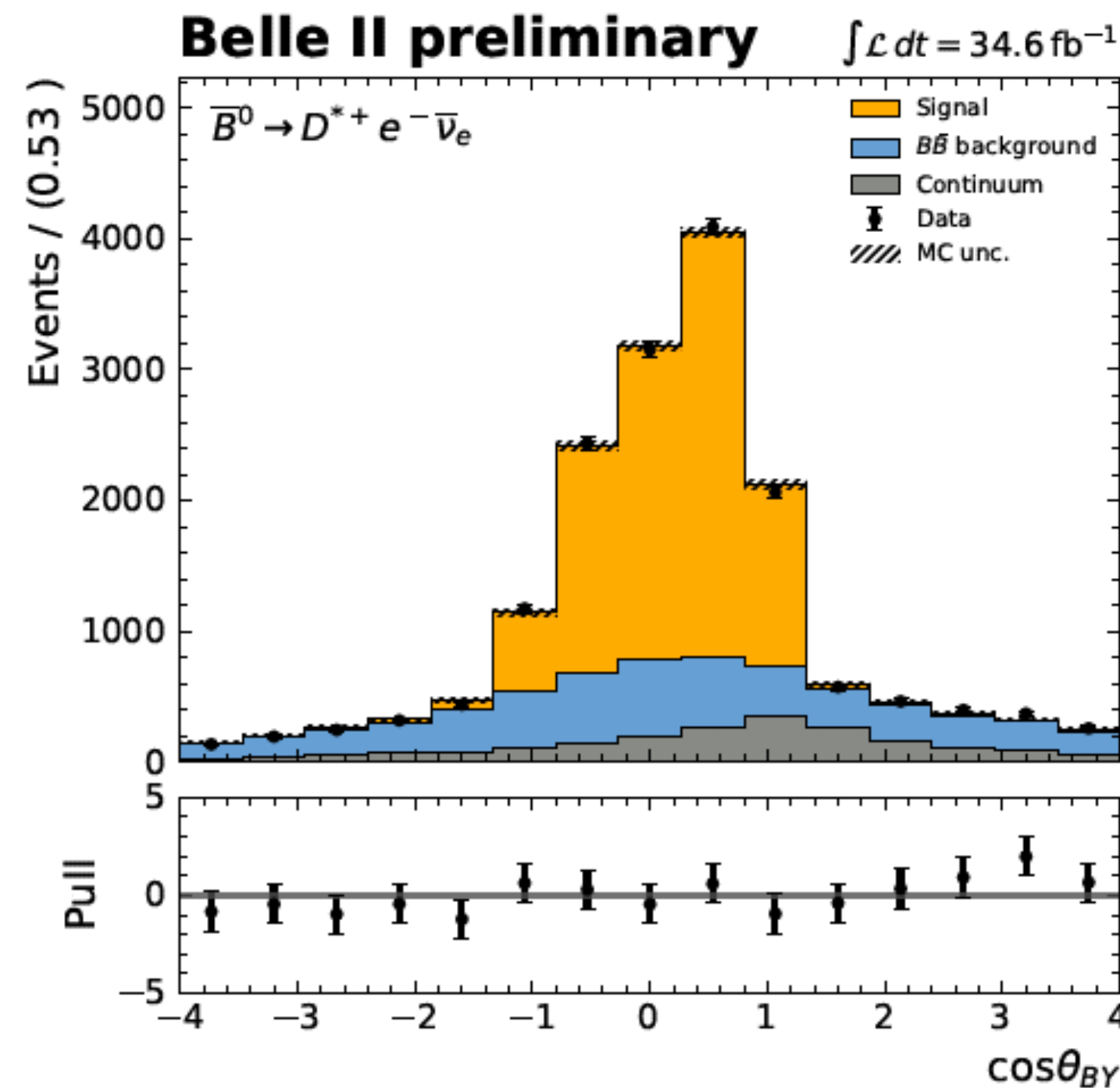


$$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \ell \bar{\nu}) = (4.60 \pm 0.05(stat) \pm 0.18(sys) \pm 0.45\pi_s) \%$$

Compatible with current world average.

$$R_{e\mu} = \frac{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} e^- \bar{\nu}_e)}{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu)} = 0.99 \pm 0.03$$

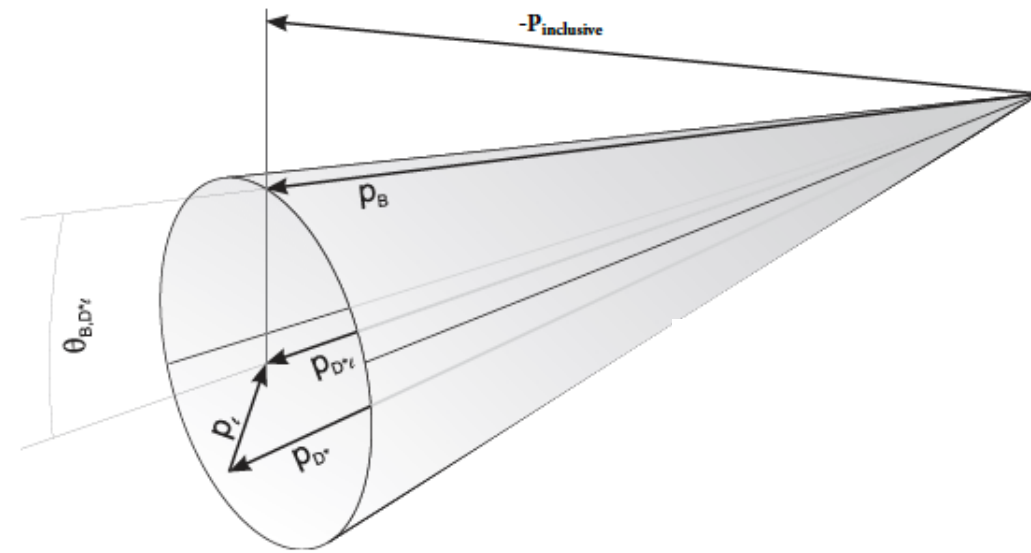
Expecting updated results with the full available Belle II dataset very soon.



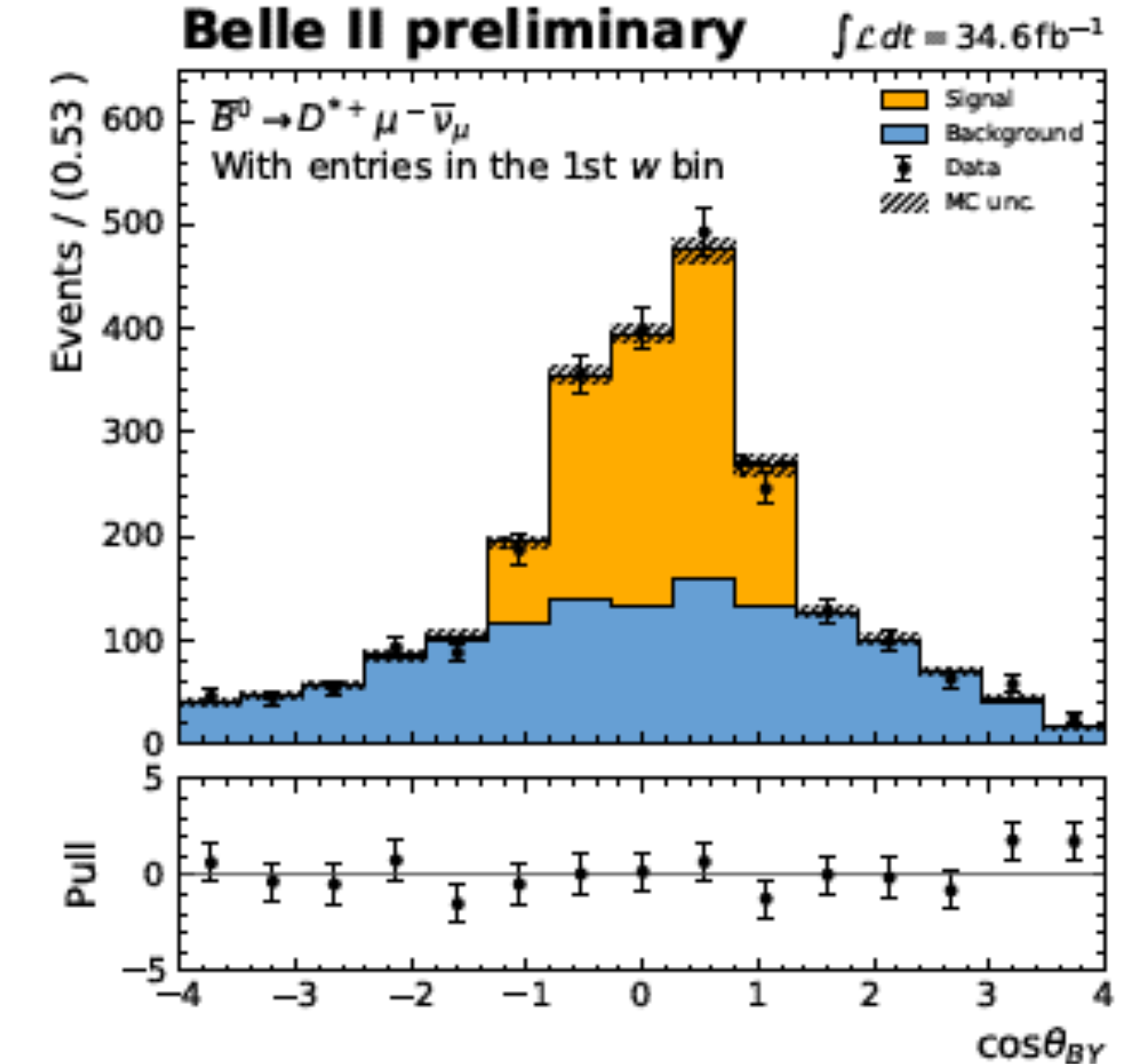
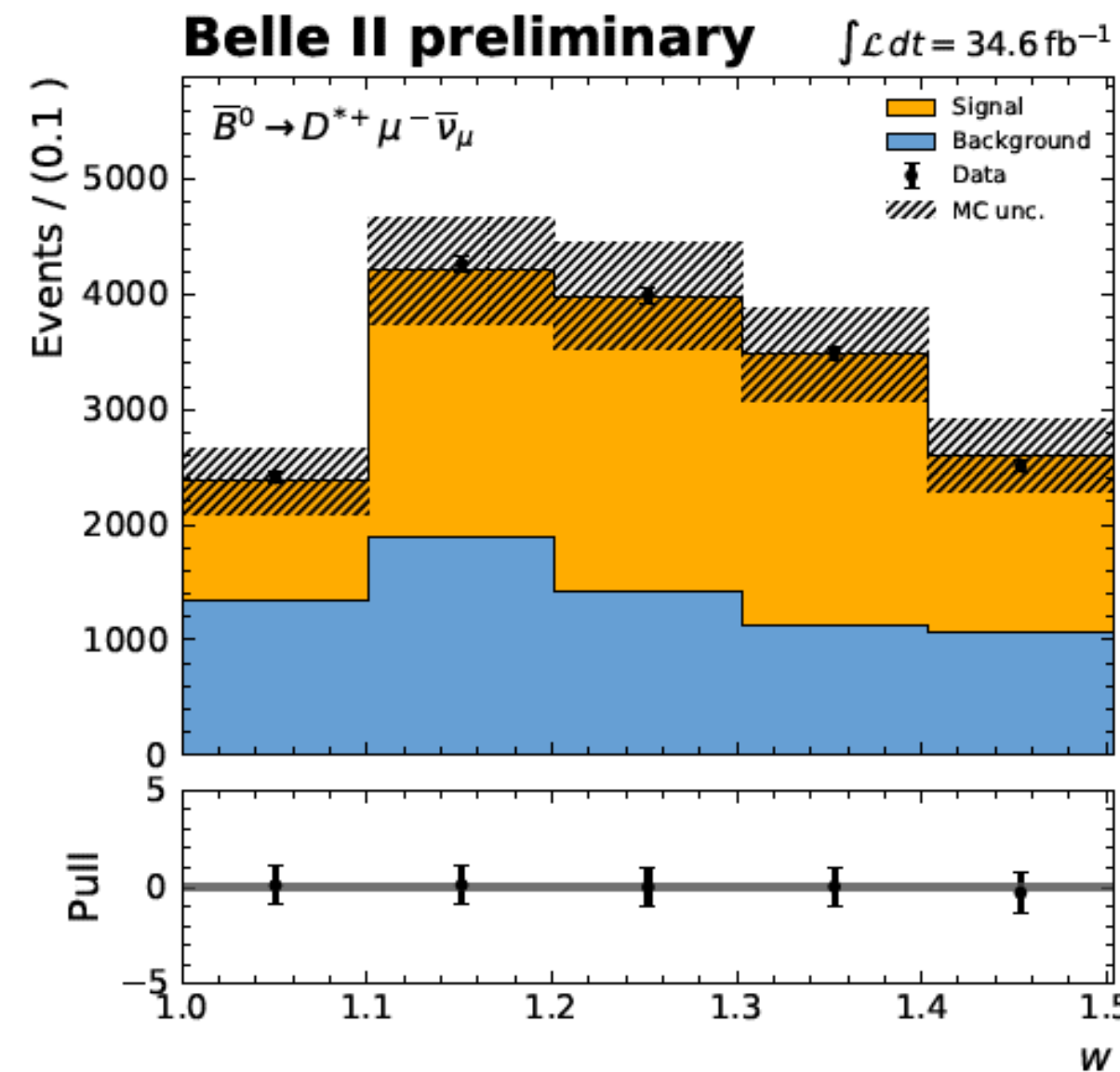
Untagged Exclusive $B \rightarrow D^{*+} \ell \nu$

Examine hadronic recoil parameter spectrum

$$w = \frac{m_B^2 - m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

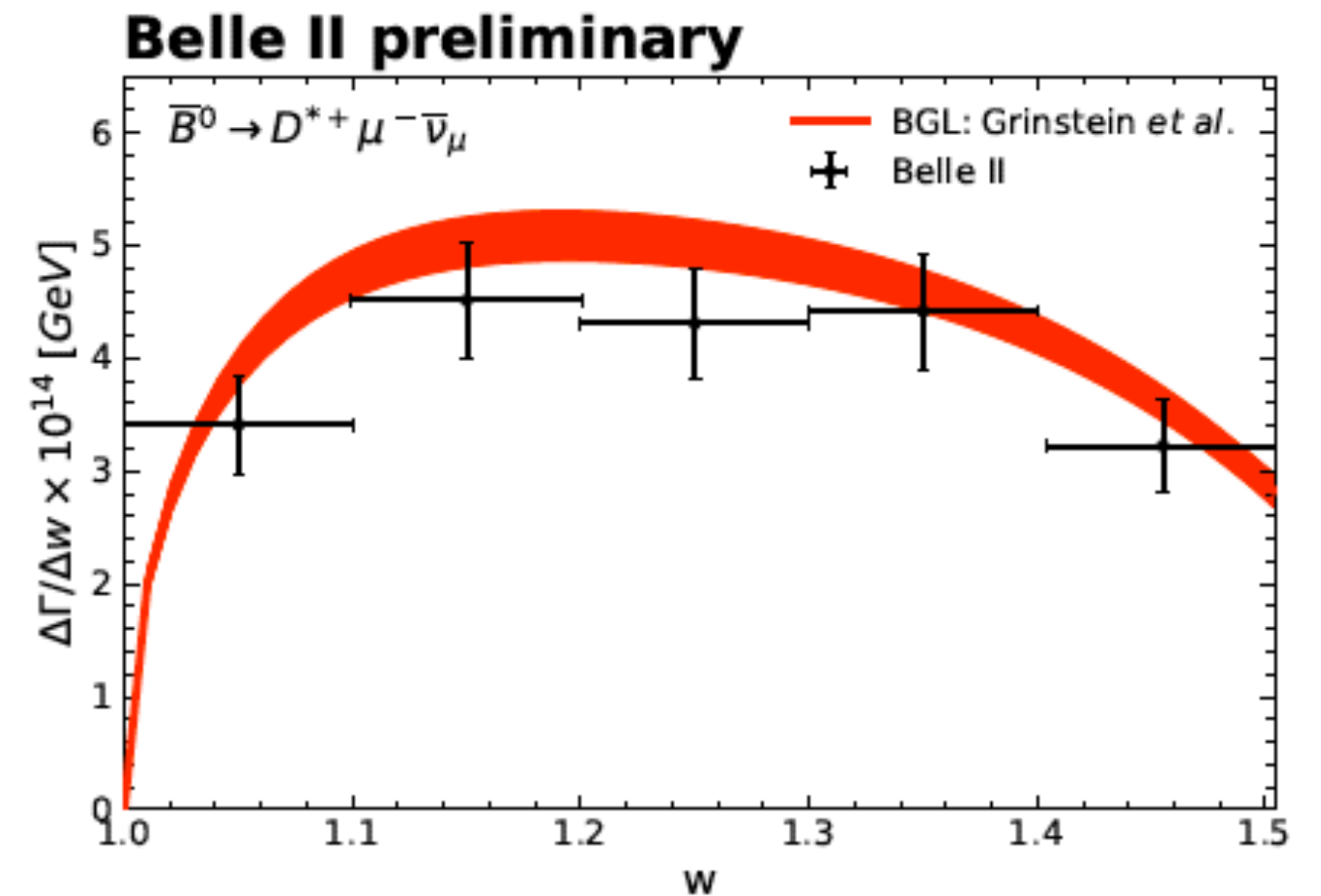
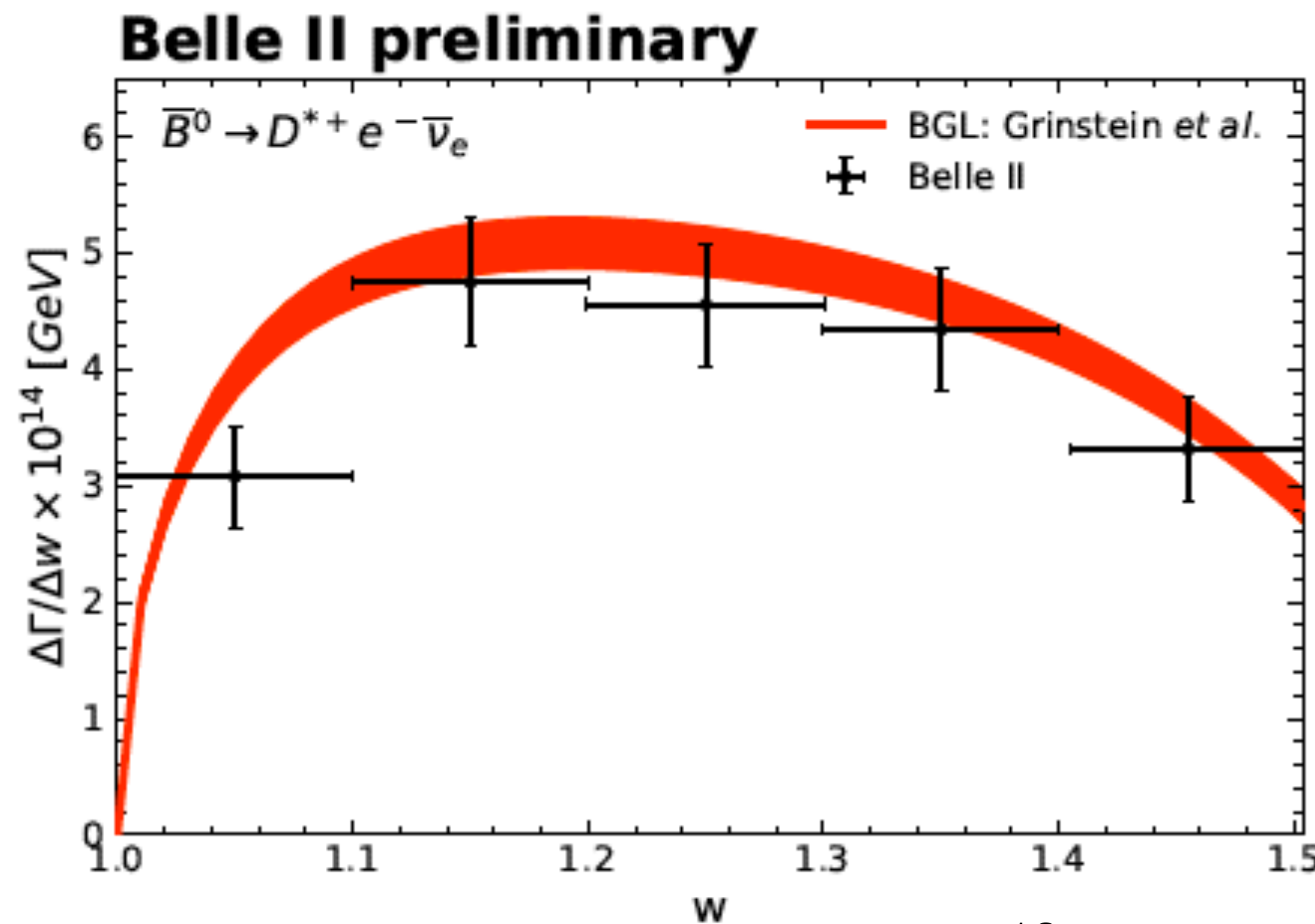


Divide spectrum into 5 equal bins of 0.1008 between $w=1$ and $w_{\max}=1.504$.



Unfold the w spectrum to compare with BGL.

Partial branching fractions in bins of w are a key step to determine $|V_{cb}|$.



$$B^- \rightarrow D^0 \ell \nu$$

Flagship decay for exclusive V_{cb} measurements!

Reconstruct $D^0 \rightarrow K^- \pi^+$.

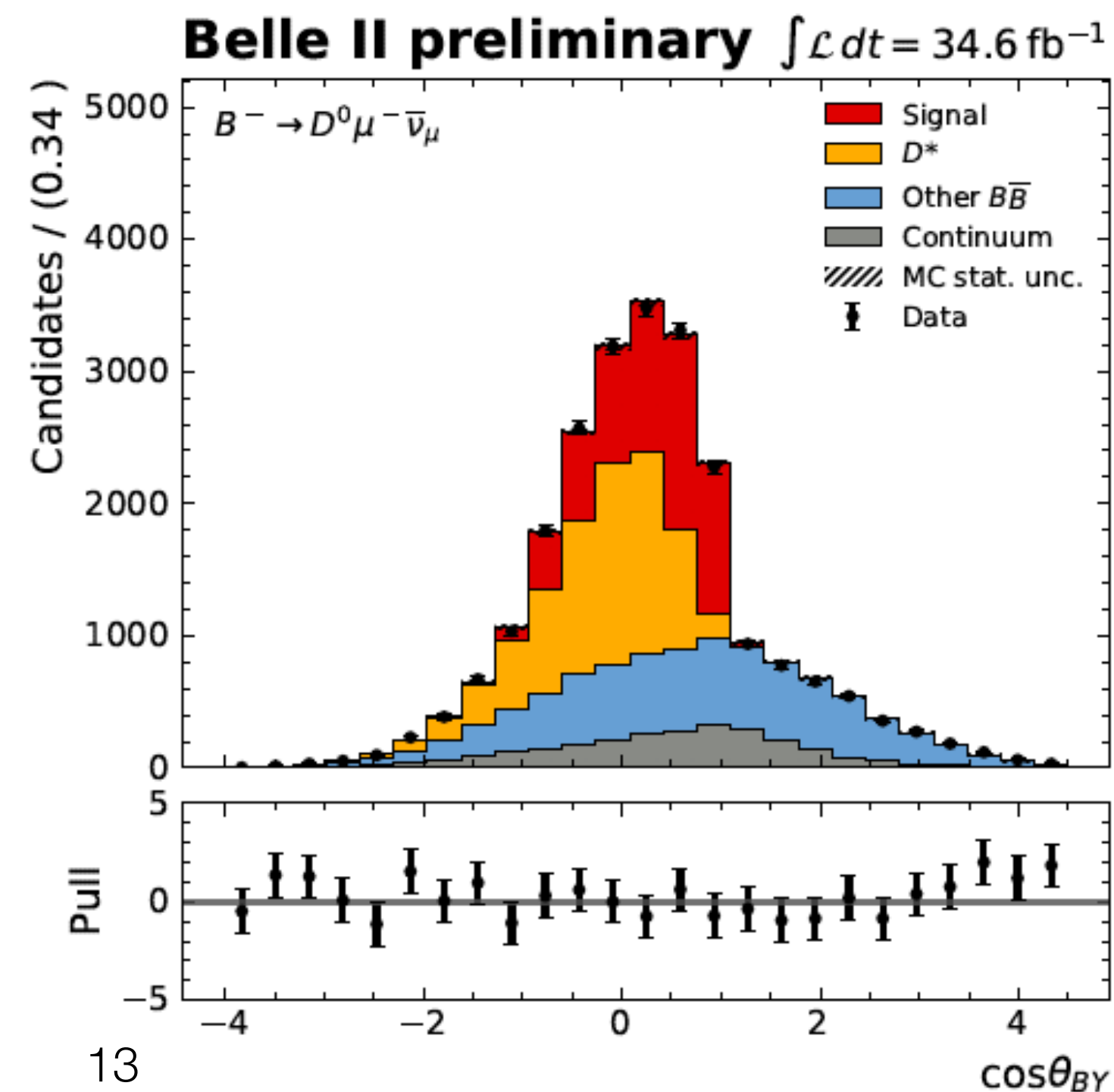
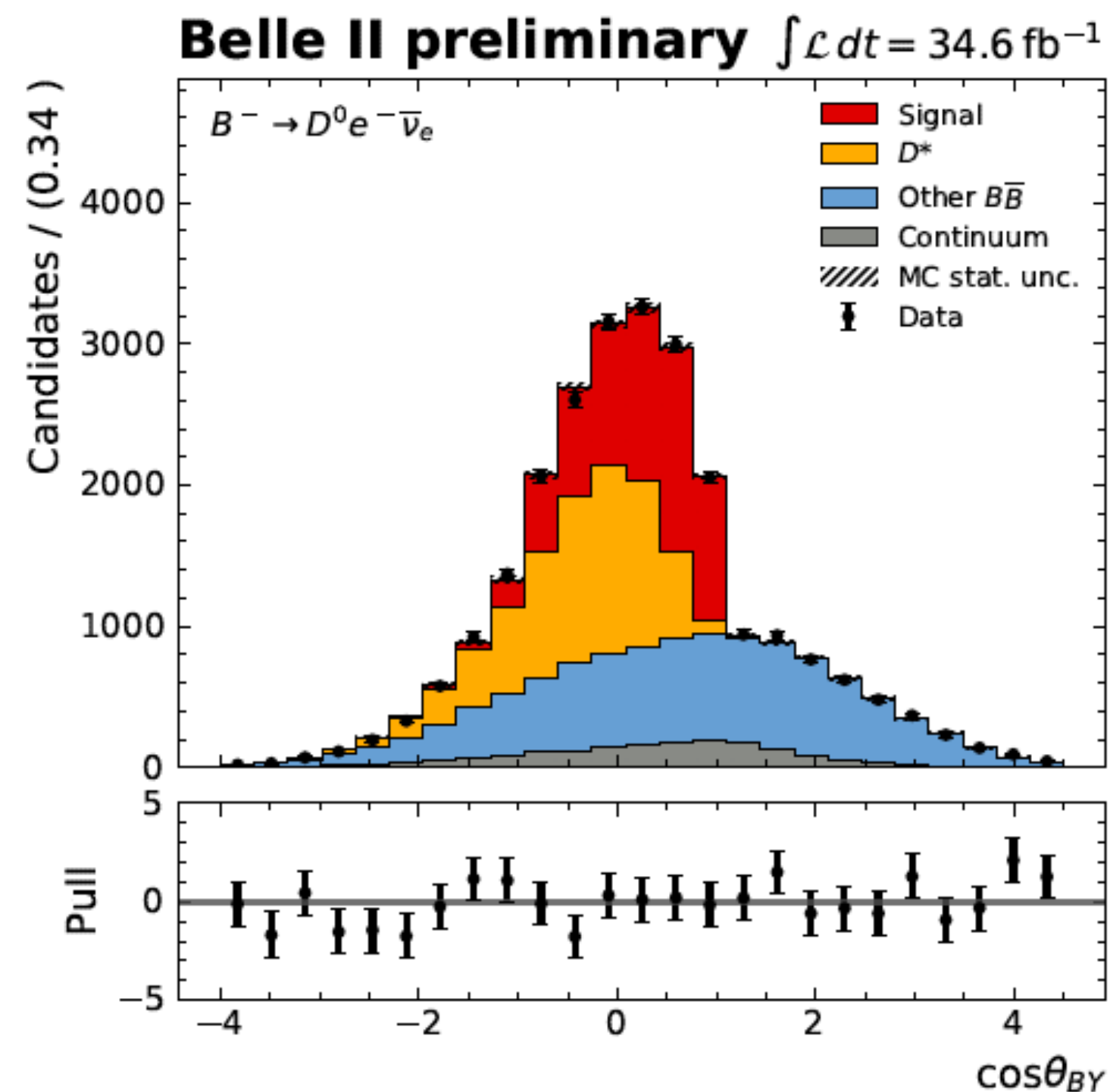
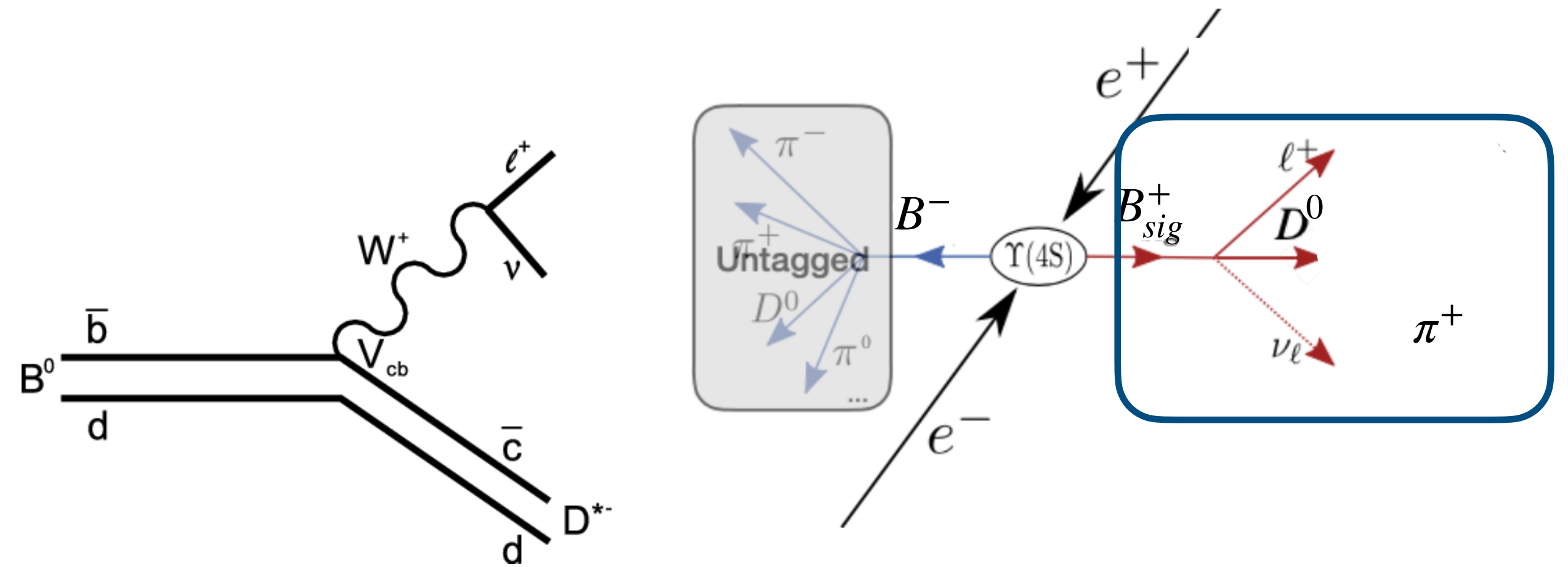
Identify lepton using PID algorithms.

Suppress $e^+e^- \rightarrow q\bar{q}$ events using $p_{D^*} < 2.4 \text{ GeV}/c$ and $R_2 < 0.3$

Apply D^* veto by combining D candidates with:

π_s^+ and exclude $\Delta m \in [0.144, 0.148] \text{ GeV}/c^2$

γ, π_s^0 and exclude $\Delta m \in [0.141, 0.146] \text{ GeV}/c^2$



First measurement at Belle II !

Inclusive $B \rightarrow X_c \ell \nu$

- Heavy Quark Expansion (HQE) in powers of $1/m_b$
- Determine parameters of HQE using moments of the differential rate.

$$\langle E^n \rangle_{\text{cut}} = \frac{\int_{E_\ell > E_{\text{cut}}} dE_\ell E_\ell^n \frac{d\Gamma}{dE_\ell}}{\int_{E_\ell > E_{\text{cut}}} dE_\ell \frac{d\Gamma}{dE_\ell}} \quad \langle (M_X^2)^n \rangle_{\text{cut}} = \frac{\int_{E_\ell > E_{\text{cut}}} dM_X^2 (M_X^2)^n \frac{d\Gamma}{dM_X^2}}{\int_{E_\ell > E_{\text{cut}}} dM_X^2 \frac{d\Gamma}{dM_X^2}} \quad R^*(E_{\text{cut}}) = \frac{\int_{E_\ell > E_{\text{cut}}} dE_\ell \frac{d\Gamma}{dE_\ell}}{\int_0 dE_\ell \frac{d\Gamma}{dE_\ell}}$$

$$\mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, m_b, (m_c)$$

- Using the branching fraction, determine $|V_{cb}|$

$$\text{Br}(\bar{B} \rightarrow X_c \ell \bar{\nu}) \propto \frac{|V_{cb}|^2}{\tau_B} \left[\Gamma_0 + \Gamma_{\mu_\pi} \frac{\mu_\pi^2}{m_b^2} + \Gamma_{\mu_G} \frac{\mu_G^2}{m_b^2} + \Gamma_{\rho_D} \frac{\rho_D^3}{m_b^3} \right]$$

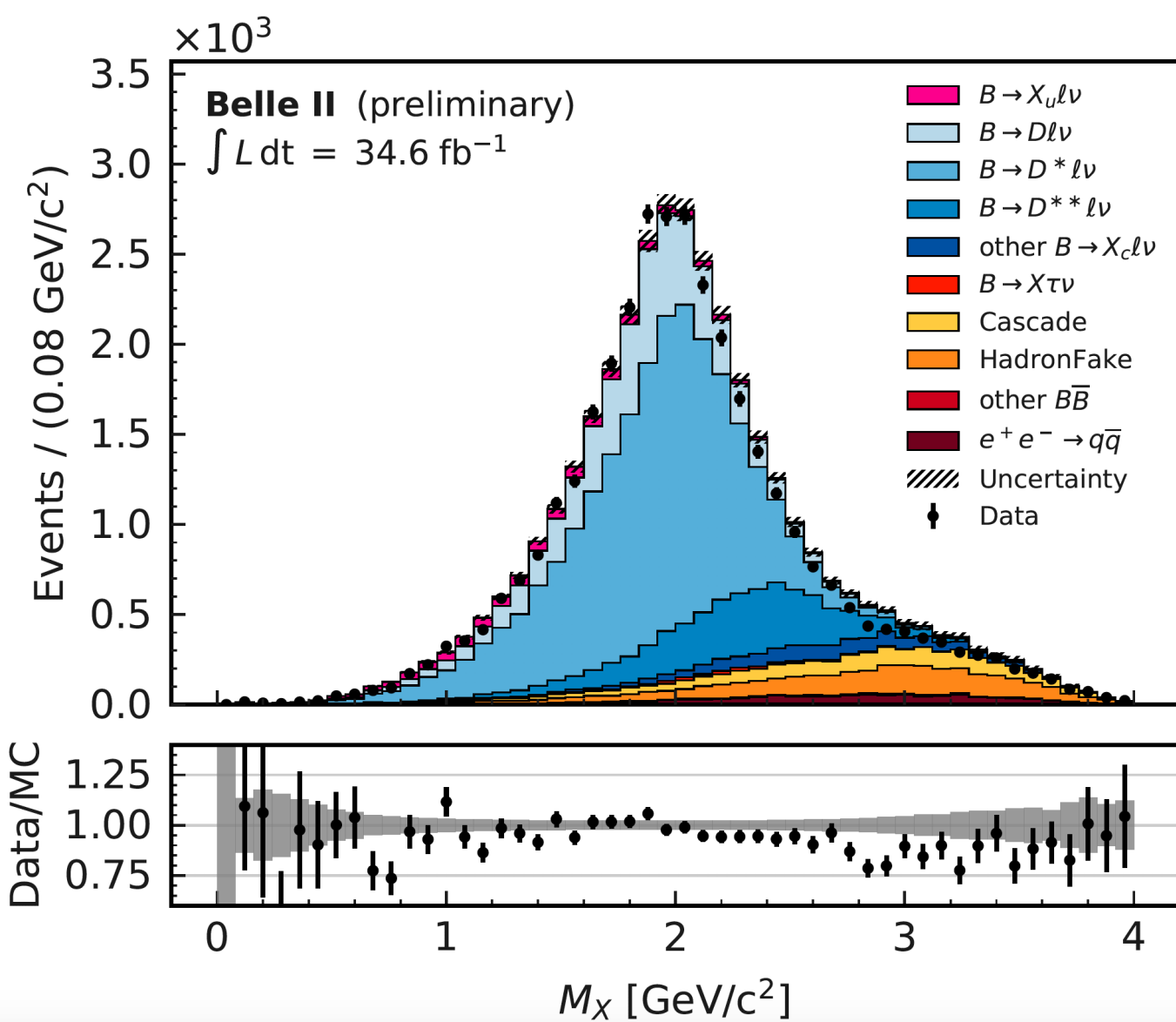
	Kinetic scheme	1S scheme
$O(1)$	m_b, m_c	m_b
$O(1/m_b^2)$	μ_π^2, μ_G^2	λ_1, λ_2
$O(1/m_b^3)$	ρ_D^3, ρ_{LS}^3	ρ_1, τ_{1-3}

JHEP 1109 055 (2011)

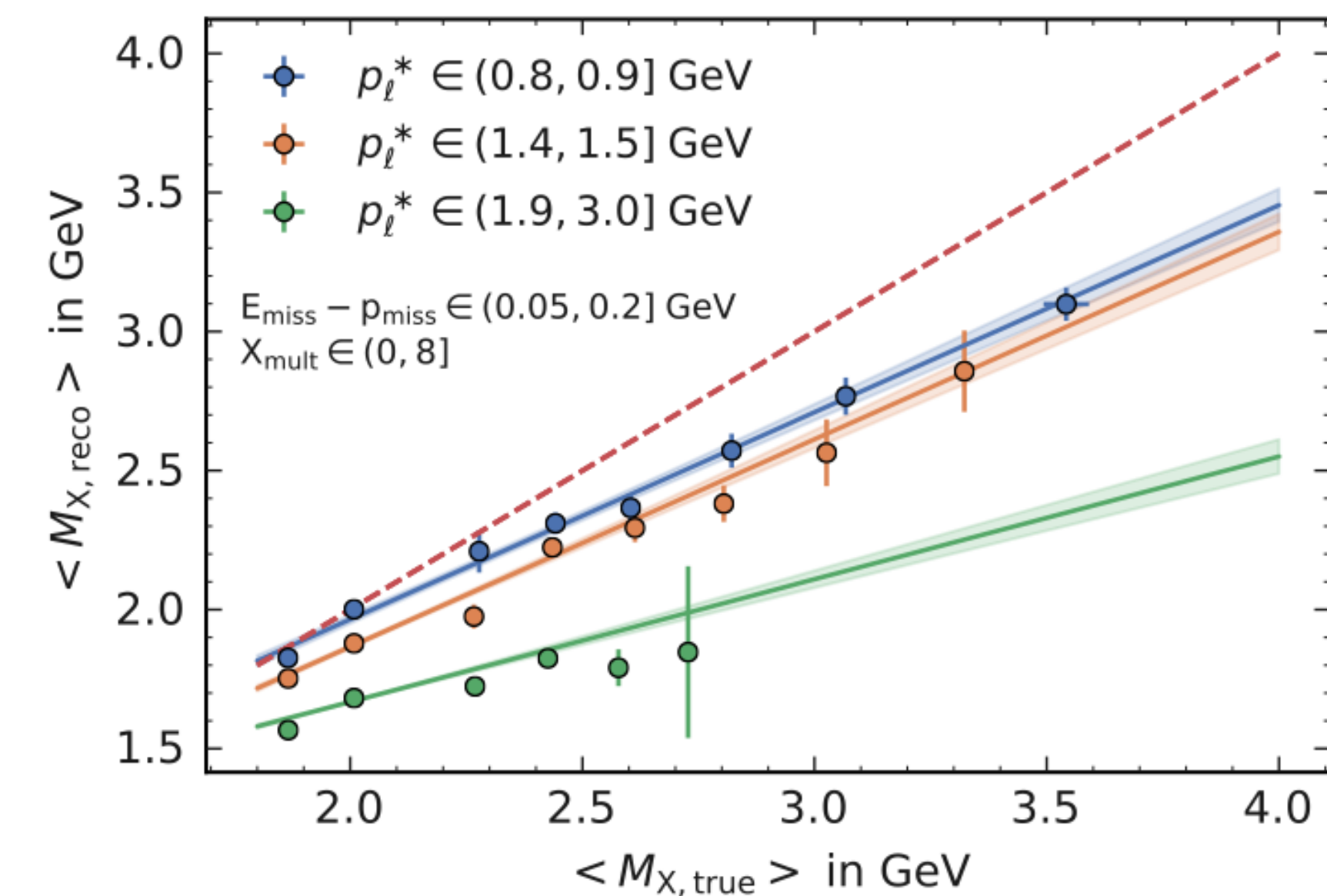
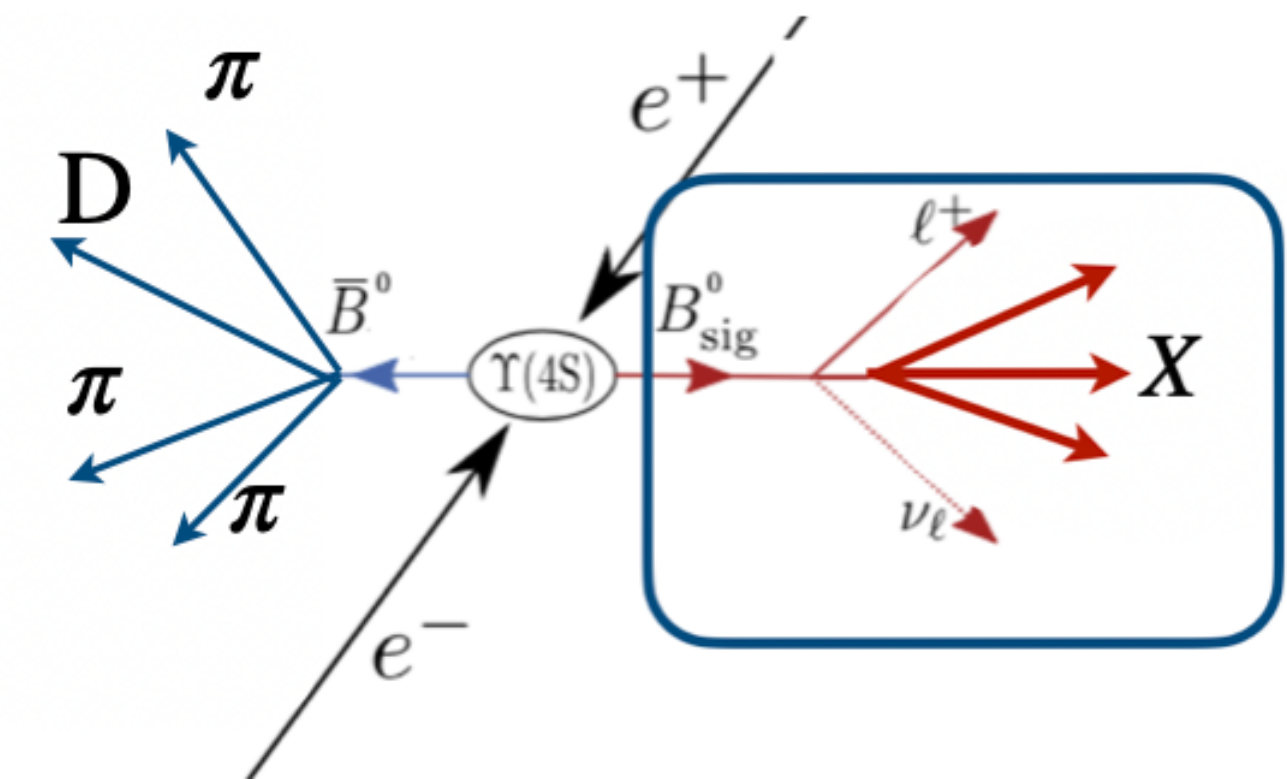
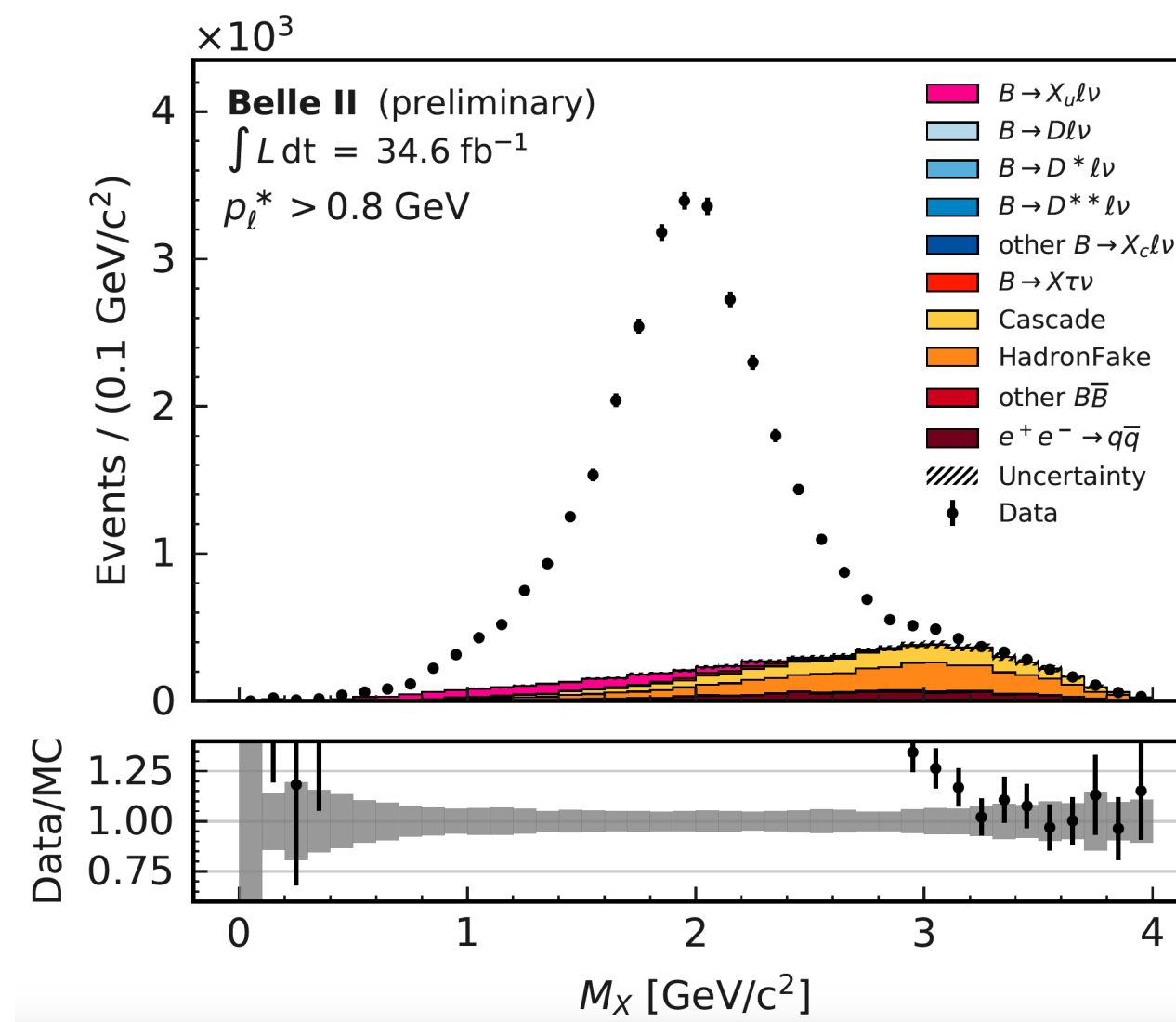
Phys. Rev. D **70**, 094017 (2004)

Hadronic Mass Moments of $B \rightarrow X_c \ell \nu_\ell$

- Use hadronic FEI tagging and identify one lepton with $p^*_\ell > 0.8 \text{ GeV}/c$.



Subtract background by
 assigning a signal
 probability to each event



Extract hadronic mass moments as a weighted average using the following:

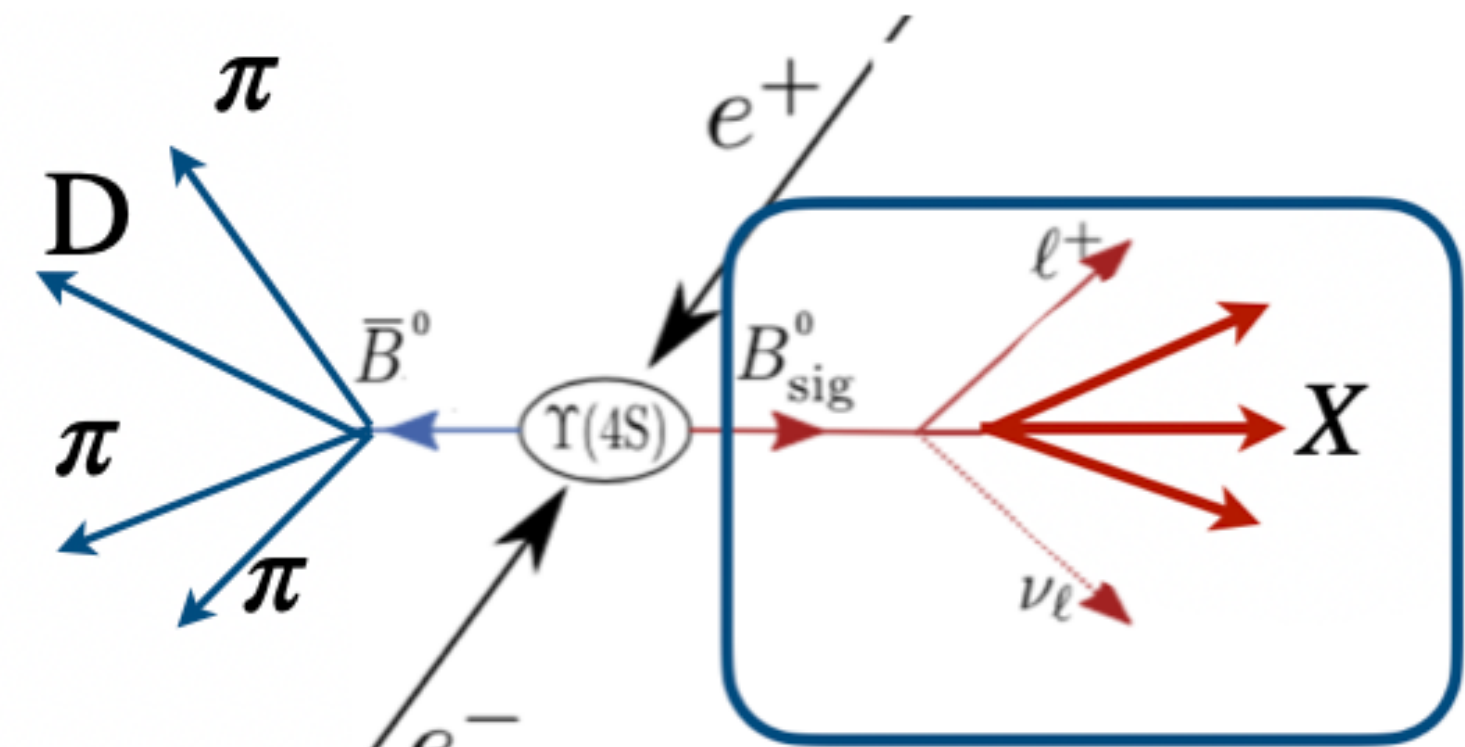
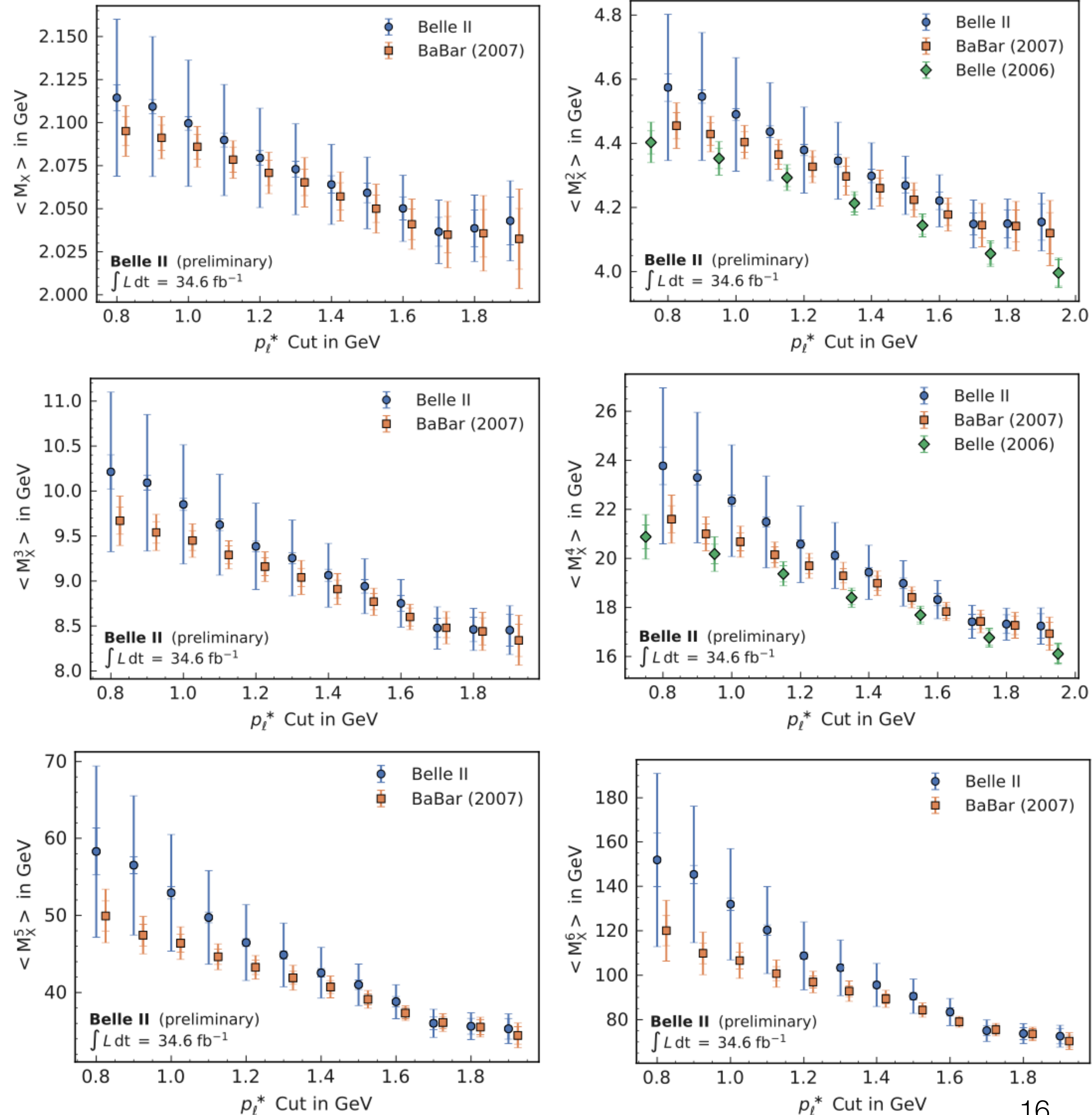
$$\langle M_X^n \rangle = \frac{\sum_i w_i(M_X) M_{X, \text{calib}, i}^n}{\sum_i w_i(M_X)} \times C_{\text{calib}} \times C_{\text{true}}$$

Reconstruction bias

Calibration Bias

Determine calibration functions, in bins of p_ℓ , to correct for experimental effects on M_X^n .

Hadronic Mass Moments of $B \rightarrow X_c \ell \nu$



Phys. Rev. D 75, 032005, 2007
BABAR-CONF-07/003 arXiv:0707.2670

Alternative Inclusive $|V_{cb}|$

- Achieve more precision by including higher order:

$$\Gamma \propto |V_{cb}|^2 m_b^5 \left[\Gamma_0 + \Gamma_0^{(1)} \frac{\alpha_s}{\pi} + \Gamma_0^{(2)} \left(\frac{\alpha_s}{\pi} \right)^2 + \frac{\mu_\pi^2}{m_b^2} \left(\Gamma^{(\pi,0)} + \frac{\alpha_s}{\pi} \Gamma^{(\pi,1)} \right) \right. \\ \left. + \frac{\mu_G^2}{m_b^2} \left(\Gamma^{(G,0)} + \frac{\alpha_s}{\pi} \Gamma^{(G,1)} \right) + \frac{\rho_D^3}{m_b^3} \Gamma^{(D,0)} + \mathcal{O} \left(\frac{1}{m_b^4} \right) \dots \right]$$

**NOVEL
APPROACH!!!**

Fael, Mannel, Vos , JHEP 02 (2019) 177

- Number of parameters: 4 up to $1/m_b^3$, 13 up to $1/m_b^4$ and 31 up to $1/m_b^5$
- Use reparametrization invariance to link different orders of $1/m_b$ and reduce the number of total parameters
- Requires RPI observables such as q^2

8 parameters instead of 13 !

$$\begin{aligned} - 2M_B r_G^4 &\equiv \frac{1}{2} \langle B | \bar{b}_\nu [iD_\mu, iD_\nu] [iD^\mu, iD^\nu] b_\nu | B \rangle \propto \langle \vec{E}^2 - \vec{B}^2 \rangle \\ - 2M_B r_E^4 &\equiv \frac{1}{2} \langle B | \bar{b}_\nu [ivD, iD_\mu] [ivD, iD^\mu] b_\nu | B \rangle \propto \langle \vec{E}^2 \rangle \\ - 2M_B s_B^4 &\equiv \frac{1}{2} \langle B | \bar{b}_\nu [iD_\mu, iD_\alpha] [iD^\mu, iD_\beta] (-i\sigma^{\alpha\beta}) b_\nu | B \rangle \propto \langle \vec{\sigma} \cdot \vec{B} \times \vec{B} \rangle \end{aligned}$$

$$\langle (q^2)^n \rangle_{\text{cut}} = \int_{q^2 > q_{\text{cut}}^2} dq^2 (q^2)^n \frac{d\Gamma}{dq^2} \bigg/ \int_{q^2 > q_{\text{cut}}^2} dq^2 \frac{d\Gamma}{dq^2}$$

$$R^*(q_{\text{cut}}^2) = \int_{q^2 > q_{\text{cut}}^2} dq^2 \frac{d\Gamma}{dq^2} \bigg/ \int_0 dq^2 \frac{d\Gamma}{dq^2}$$

- HQE expressed in higher order terms

$$\text{Br}(\bar{B} \rightarrow X_c \ell \bar{\nu}) \propto \frac{|V_{cb}|^2}{\tau_B} \left[\Gamma_{\mu_3} \mu_3 + \Gamma_{\mu_G} \frac{\mu_G^2}{m_b^2} + \Gamma_{\tilde{\rho}_D} \frac{\tilde{\rho}_D^3}{m_b^3} \right. \\ \left. + \Gamma_{r_E} \frac{r_E^4}{m_b^4} + \Gamma_{r_G} \frac{r_G^4}{m_b^4} + \Gamma_{s_B} \frac{s_B^4}{m_b^4} + \Gamma_{s_E} \frac{s_E^4}{m_b^4} + \Gamma_{s_{qB}} \frac{s_{qB}^4}{m_b^4} \right]$$

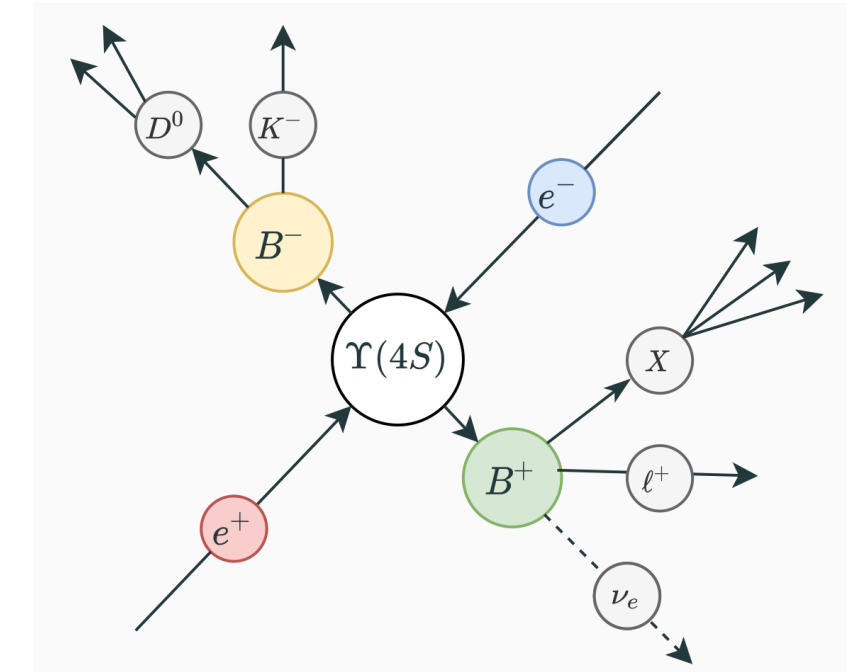
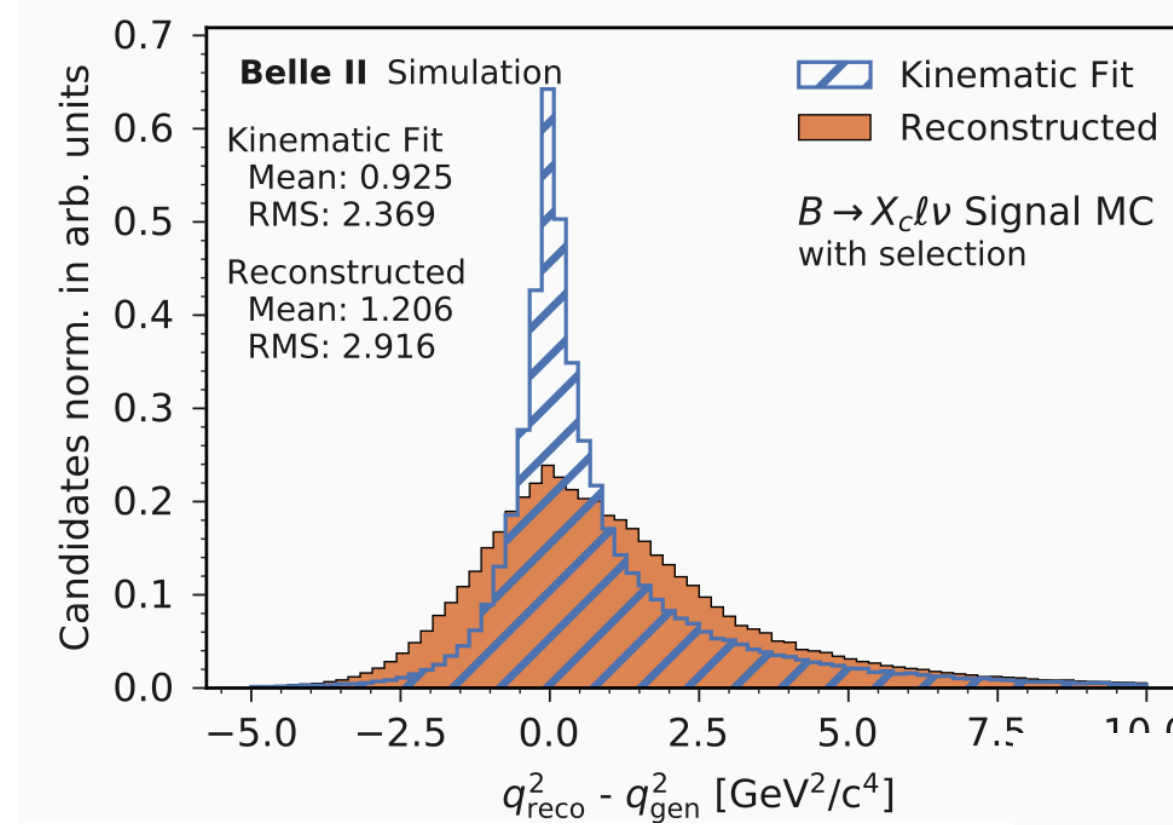
$$\mu_3, \mu_G, \tilde{\rho}_D, r_E, r_G, s_E, s_B, s_{qB}, m_b, m_c$$

Determine moments and use it to determine $|V_{cb}|$

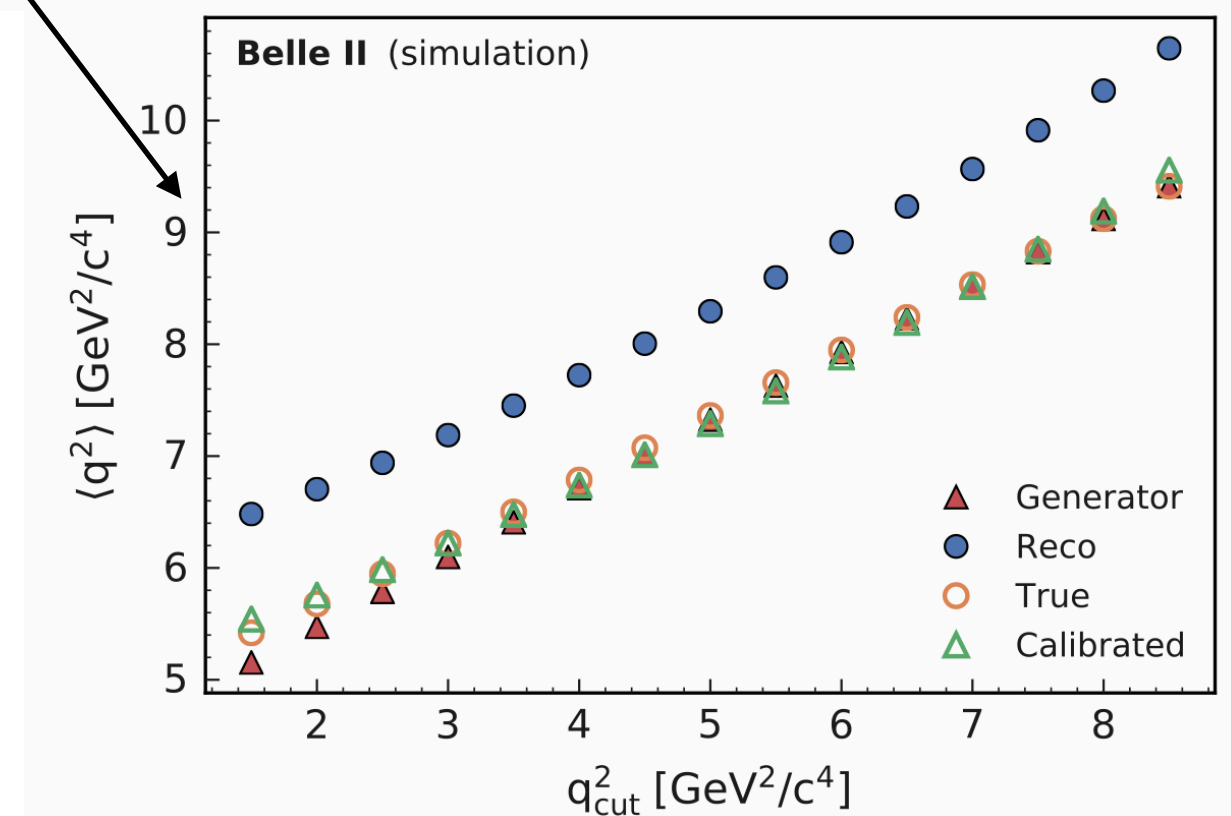
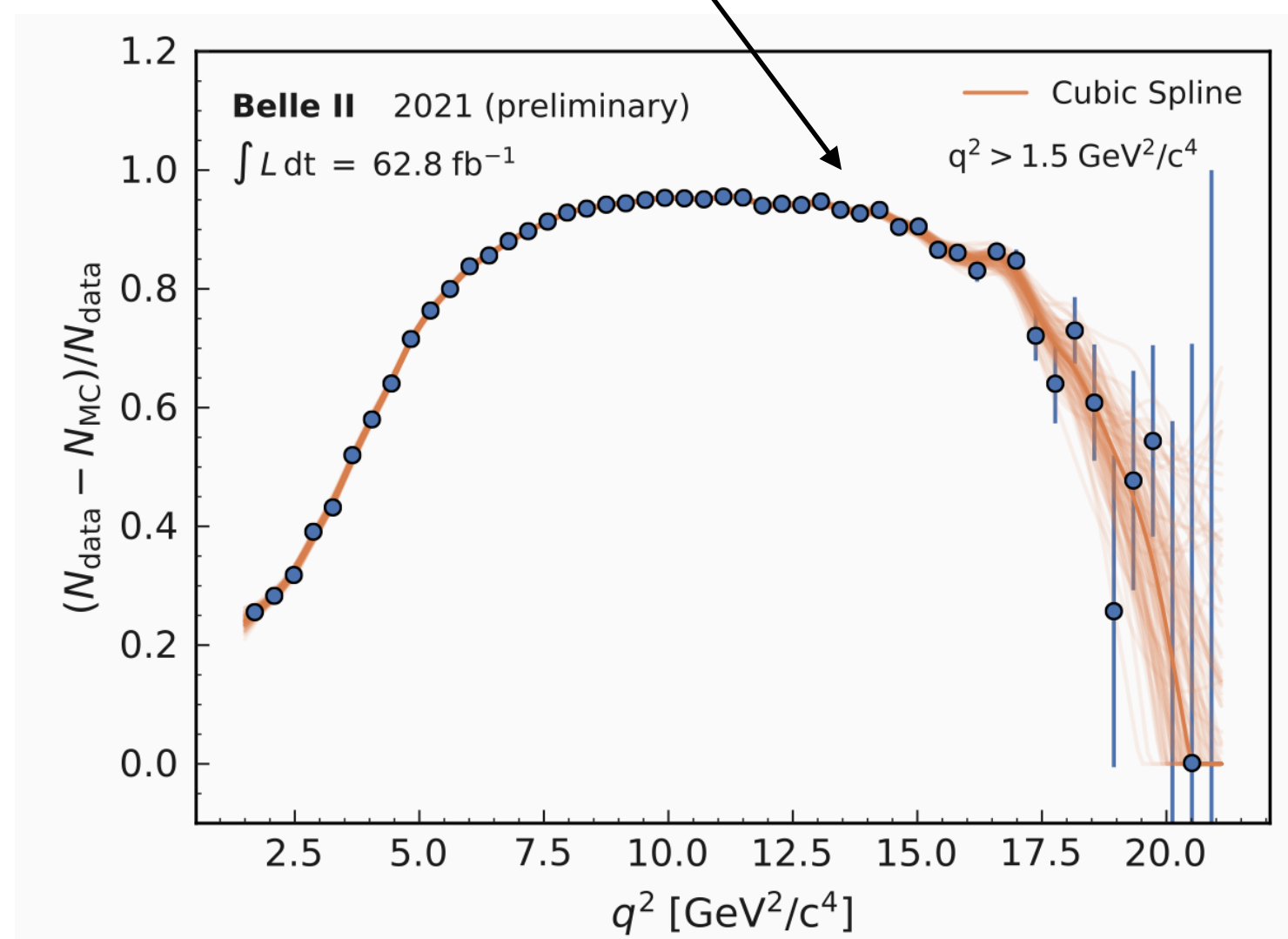
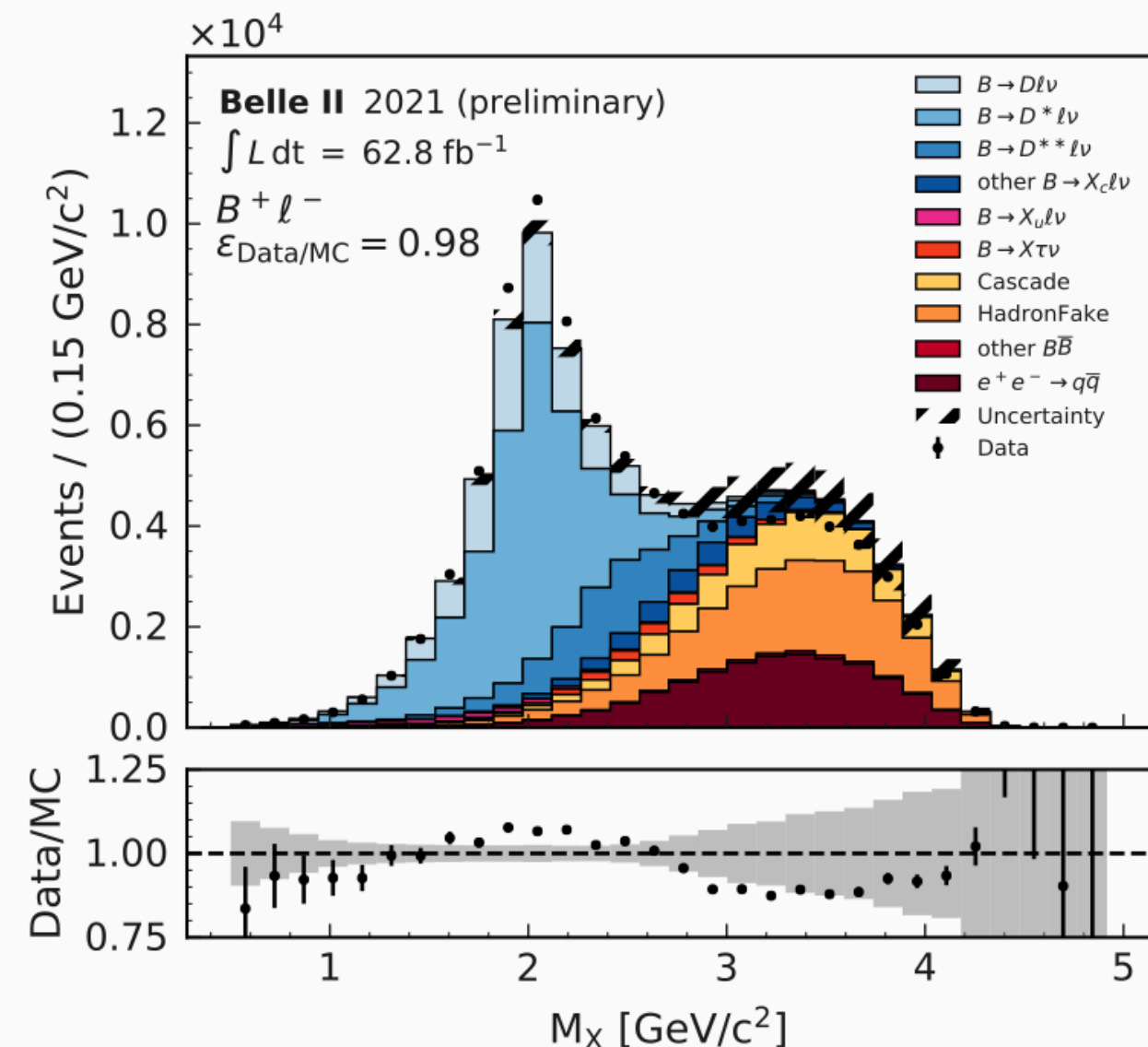
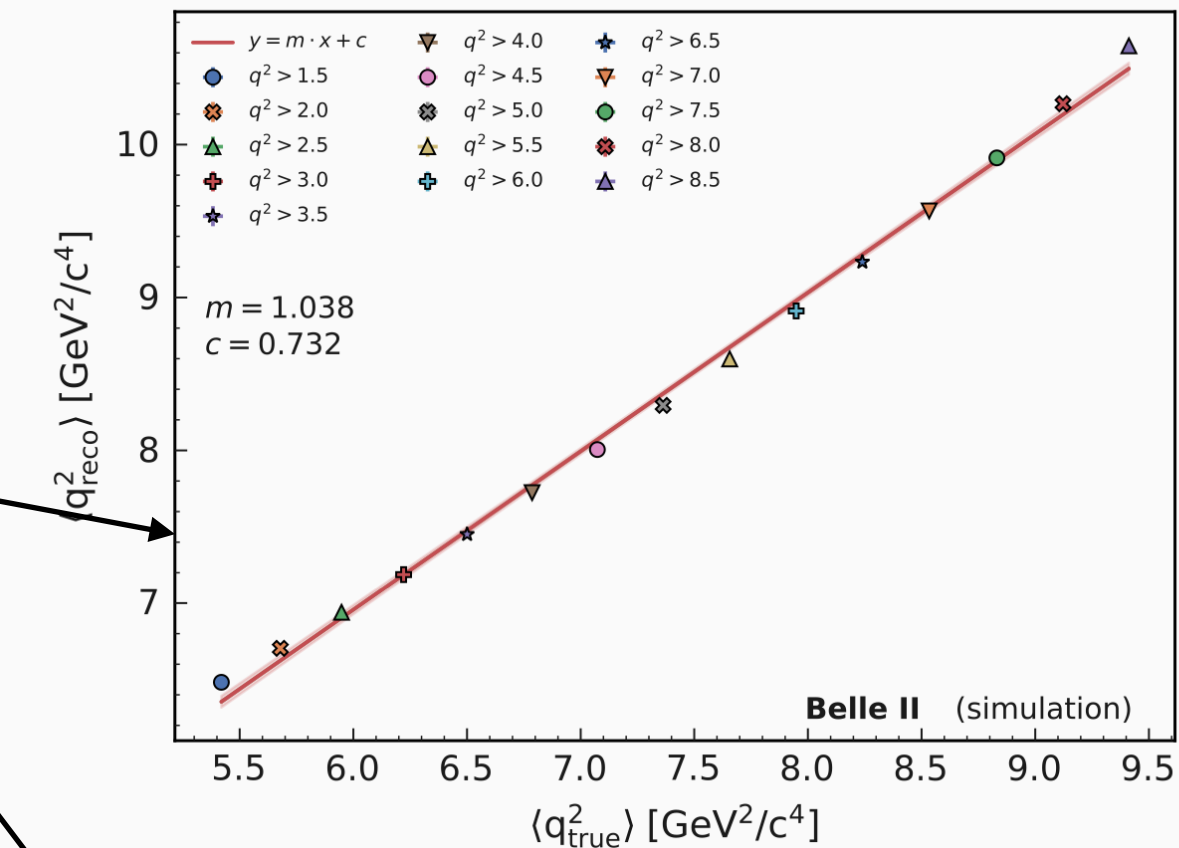
q^2 moments from $B \rightarrow X_c \ell \nu$

- Similar to m_X moments, use hadronic tagging and reconstruct X from rest-of-event (ROE).
- Apply kinematic fit with B mass constraint to improve the q^2 resolution.
- Fit to independent variable M_X in order to fix background normalization and determine signal probability

Paper draft in preparation.



$$\langle q^{2^n} \rangle = \frac{\sum_i w_i(q^2) q_{\text{calib},i}^{2^n}}{\sum_i w_i(q^2)} \times \mathcal{C}_{\text{calib}} \times \mathcal{C}_{\text{true}}$$



Untagged analysis in progress and targeting summer 2021.

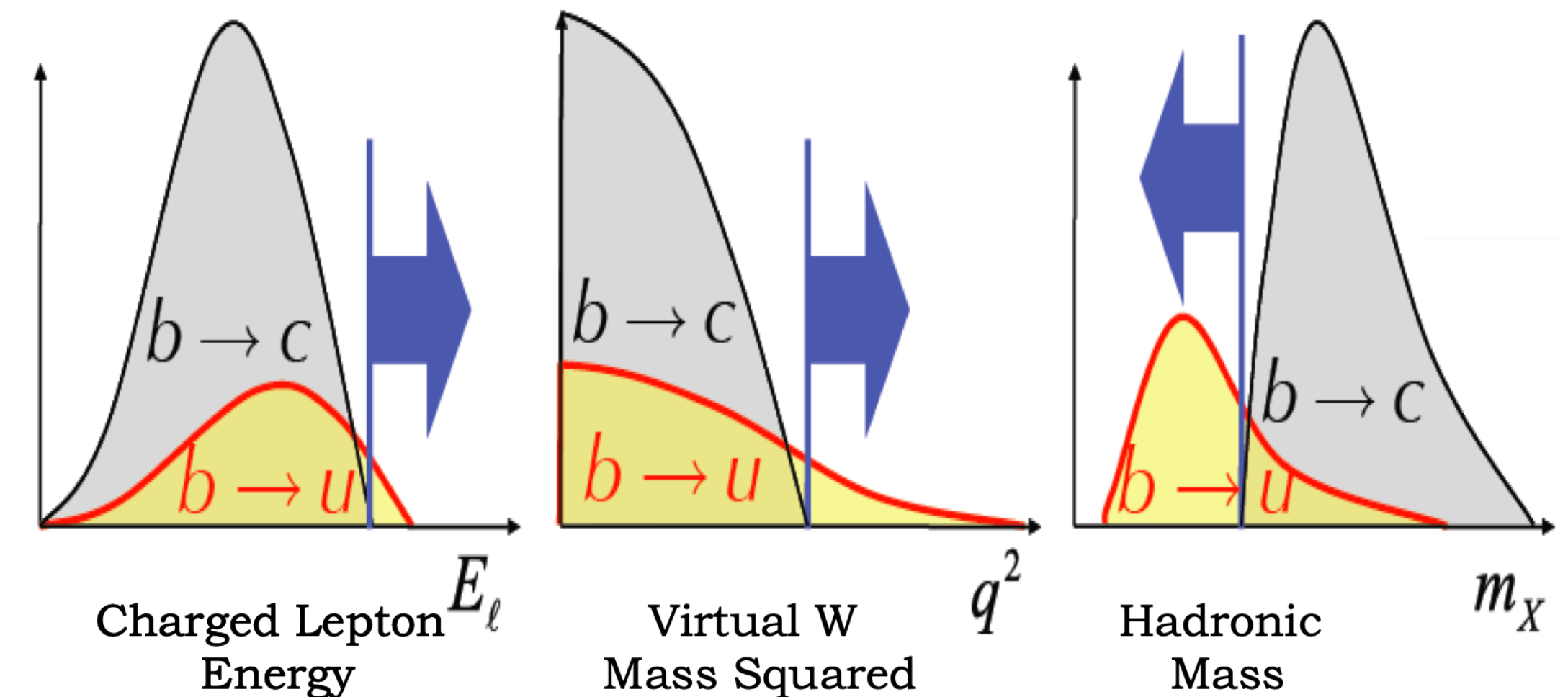
$b \rightarrow u \ell \nu$

- Experimentally challenging due to dominant $b \rightarrow c \ell \nu$ background.
- Only certain kinematic regions allow for clean separation: lepton momentum endpoint spectrum or low m_X .
- $B \rightarrow X_u \ell \nu$ is used for inclusive $|V_{ub}|$ measurement.
 - Precision of ($\sim 7\%$)
 - Operator Product Expansion (OPE) = Heavy Quark Expansion.
 - HQE breaks down and a non-perturbative shape function is

$$d\Gamma = d\Gamma_0 + d\Gamma_2 \left(\frac{\Lambda_{\text{QCD}}}{m_b} \right)^2 + d\Gamma_3 \left(\frac{\Lambda_{\text{QCD}}}{m_b} \right)^3 + d\Gamma_4 \left(\frac{\Lambda_{\text{QCD}}}{m_b} \right)^4$$

- $B \rightarrow \pi \ell \nu$ is used for exclusive $|V_{ub}|$ measurement.
 - Most precise determination of $|V_{ub}|$ ($\sim 4\%$)
 - Requires form factor determination: non-perturbative from lattice QCD (high q^2) or LCSR ($q^2 \sim 0$).

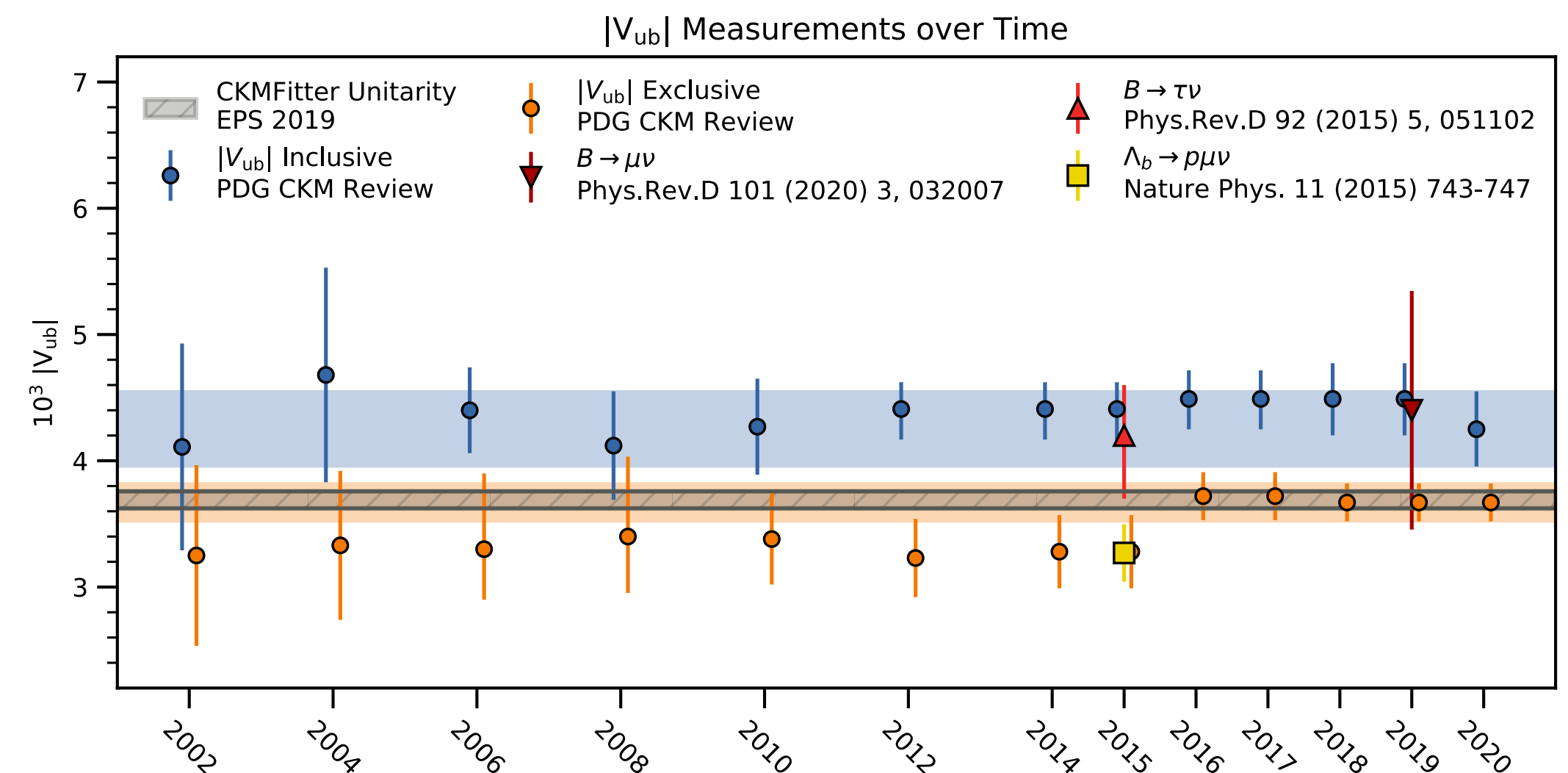
$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 |V_{ub}|^2}{24\pi^3} |p_\pi|^3 |f_+(q^2)|^2$$



Current $\sim 3\sigma$ tension between inclusive and exclusive determinations

$$|V_{ub}| = (4.25 \pm 0.12^{+0.15}_{-0.14} \pm 0.23) \times 10^{-3} \quad \text{PDG inclusive}$$

$$|V_{ub}| = (3.70 \pm 0.10 \pm 0.12) \times 10^{-3} \quad \text{PDG exclusive}$$



Hybrid Modeling for $B \rightarrow X_u \ell \nu$

- Non-resonant component overestimated in generic Belle II MC
- Use hybrid modeling instead, where the non-resonant component is weighted down such that the total number of events matches the inclusive rate:

$$H_i = R_i + w_i l_i,$$

H_i : total number of hybrid events per bin

R_i : number of resonant events per bin

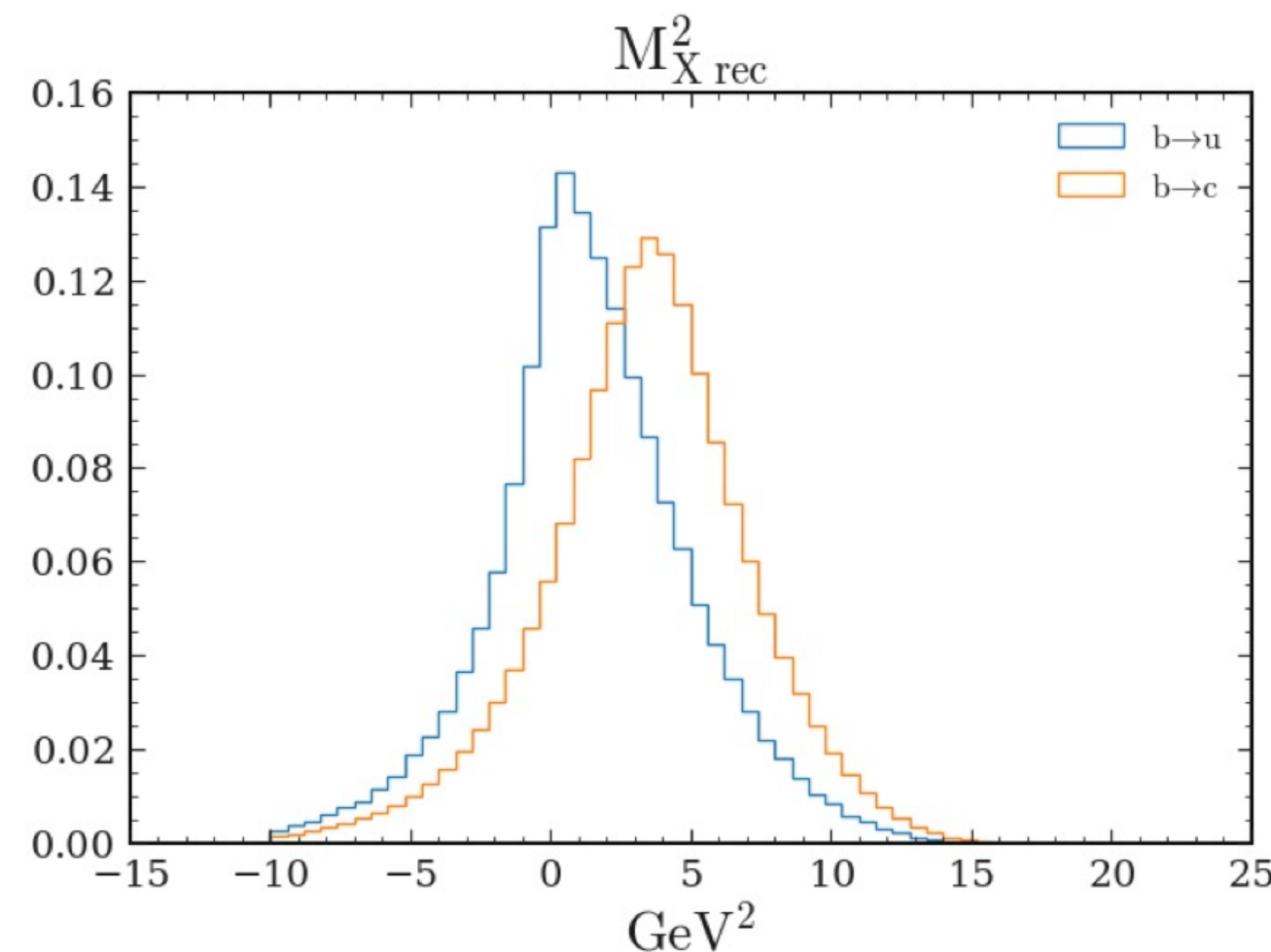
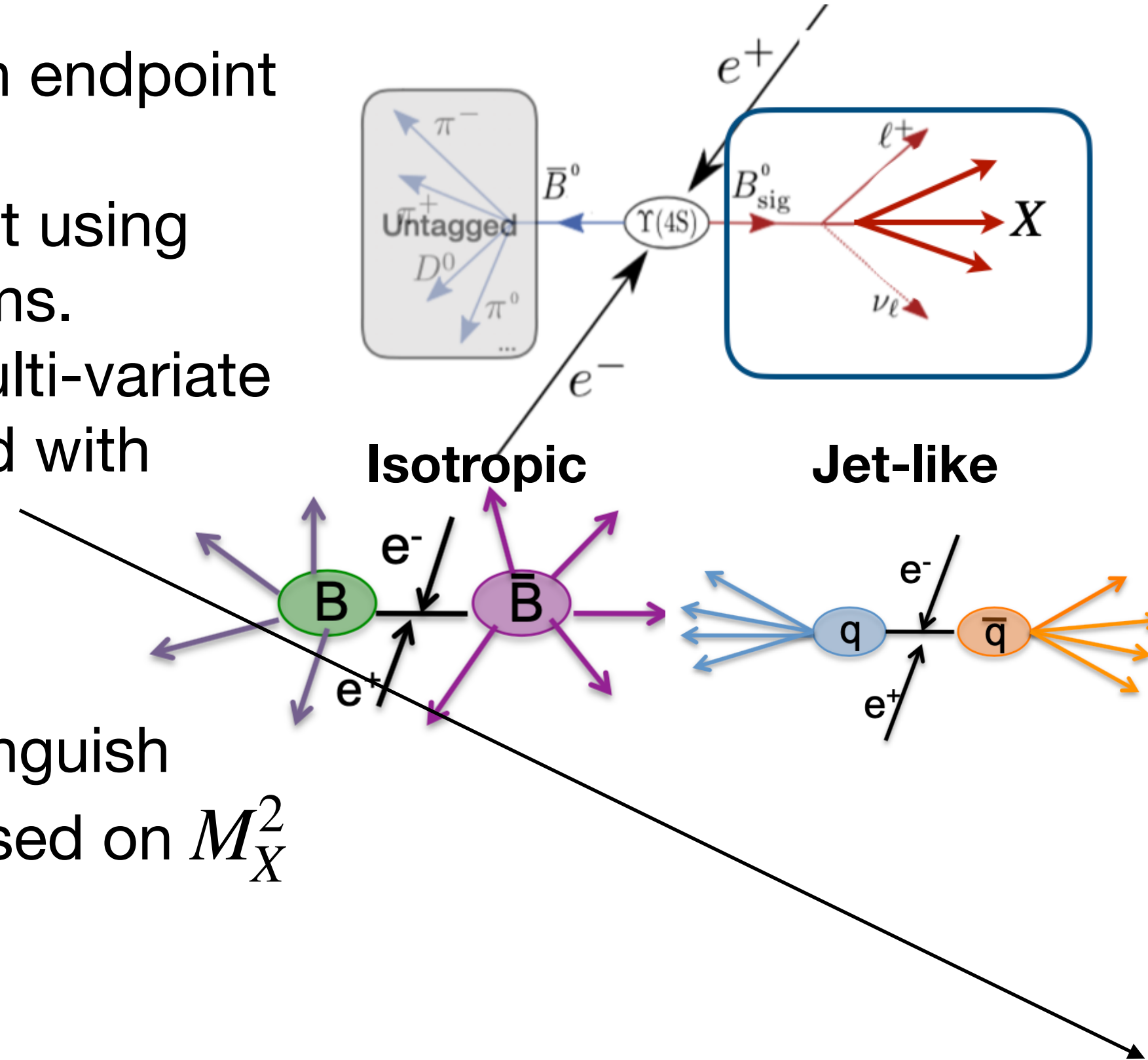
w_i : hybrid weight per bin

l_i : number of non-resonant events per bin

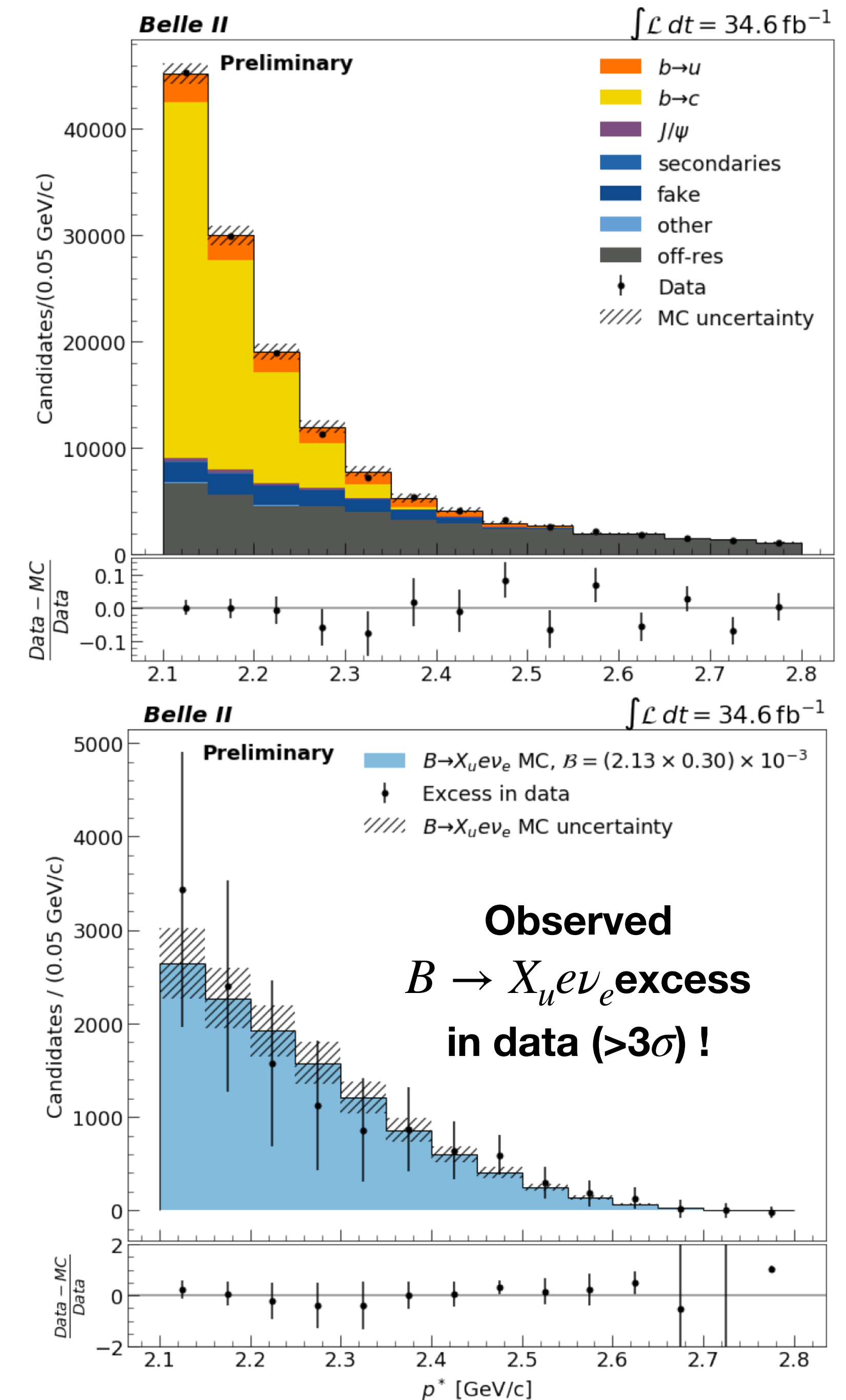
- Re-weighting done via eFFORT, in 3D bins of E_B, m_X, q^2
 - E_B : lepton energy in Bsig frame
 - M_X : mass of hadronic system X
 - q^2 : 4-momentum transfer to leptonic system

Inclusive $B \rightarrow X_u e \bar{\nu}_e$

- Measurement of $|V_{ub}|$ in the lepton endpoint momentum spectrum.
 - Identify one lepton in the event using Particle Identification algorithms.
 - Suppress continuum using multi-variate Boosted Decision Tree trained with event shape variables.
- In progress: train MVA to distinguish $b \rightarrow u$ from $b \rightarrow c$ events based on M_X^2 or rest-of-event variables.

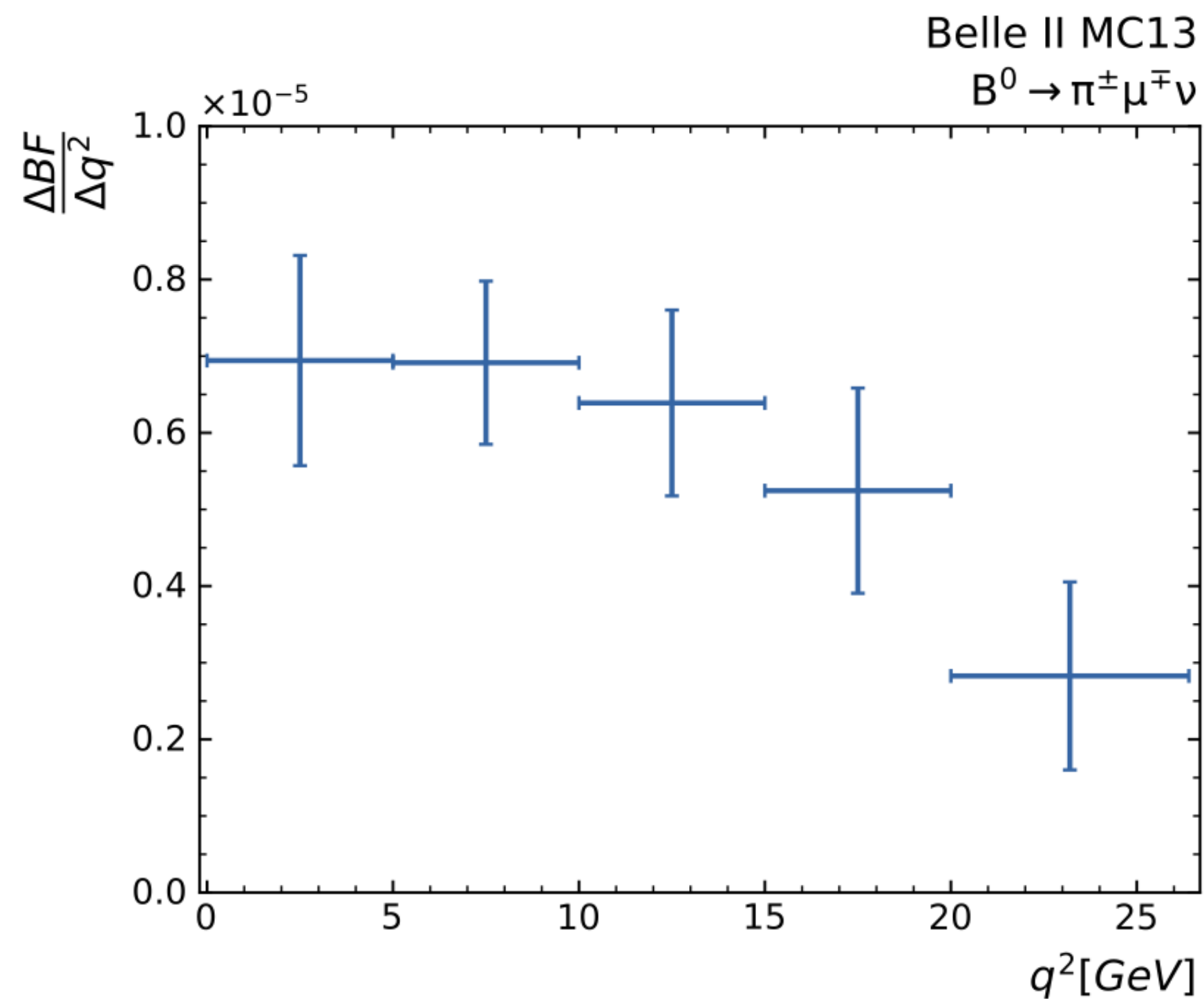
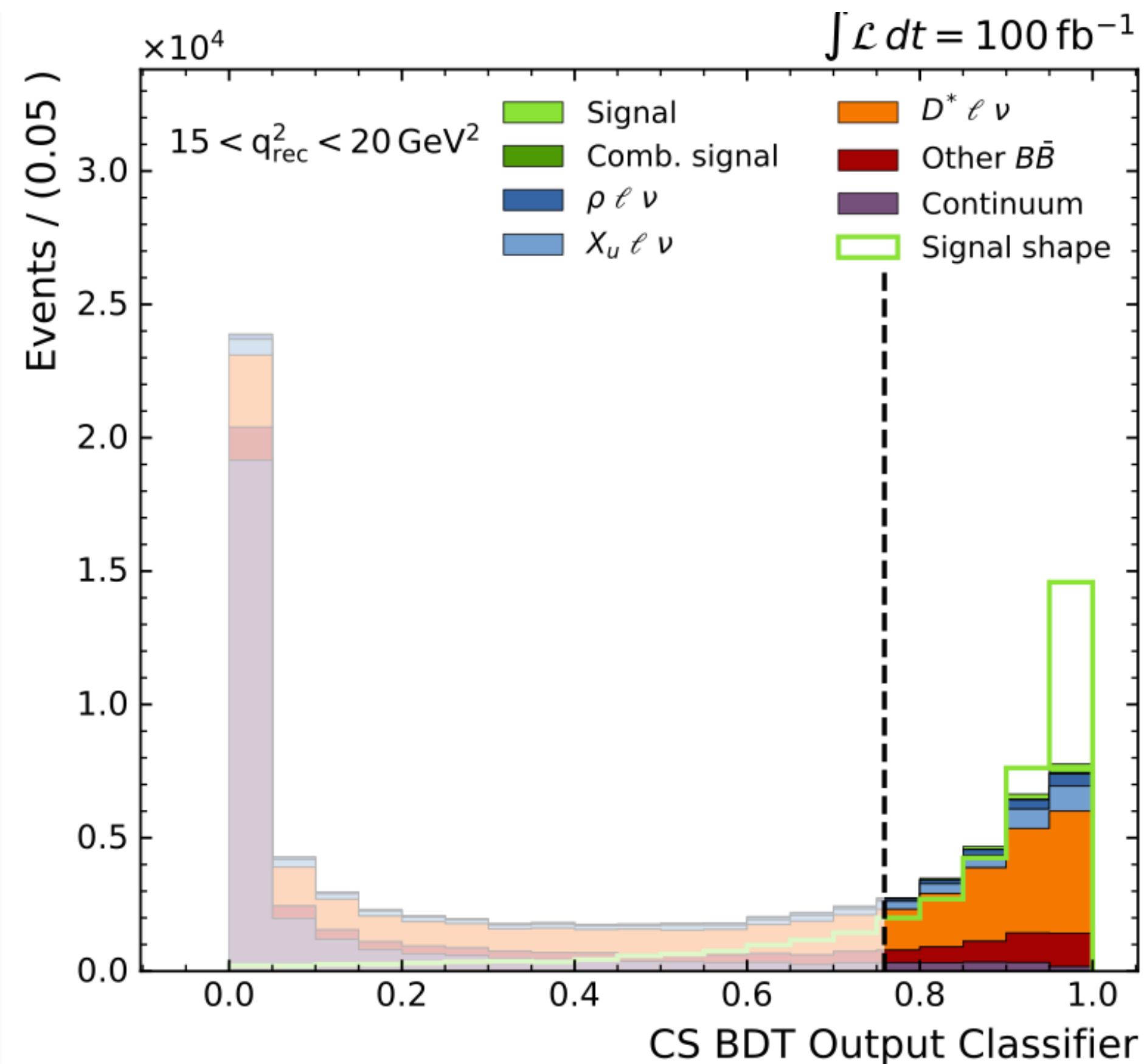


Implement rest-of-event selection on remaining tracks and clusters to isolate neutrino 4-vector.



Untagged $B \rightarrow \pi \ell \nu$

- Measured in 5 bins of $q^2 = (p_B - p_\pi)^2$ to extract $|V_{ub}|$.
- Identify pion and lepton using PID algorithm with vertex fit to parent B .
- Suppress continuum using multivariate Boosted Decision Trees trained in each q^2 bin.
- Constrain background from simultaneous fit to p_l in sideband region.
- Signal extraction from a 3D fit to $\Delta E, M_{bc}, q^2$



In progress !

$$BF^i = \frac{N_{\text{yield}}^i}{2 \times \epsilon_{\text{rec}}^i \times f \times N_{BB}}$$

$$f = \text{BF}(\Upsilon(4S) \rightarrow B^0 \bar{B}^0)$$

Signal Region: $|\cos\theta_{BY}| < 1.1$
Sideband: $1.2 < |\cos\theta_{BY}| < 2.4$

Tagged Exclusive $B^0 \rightarrow \pi^- \ell \nu_\ell$

- FEI hadronic tagging to measure $\mathcal{B}(B^0 \rightarrow \pi^- \ell \nu)$.
- Identify oppositely charged lepton, $p_e > 0.3$ and $p_\mu > 0.6$ GeV/c, and pion using PID algorithms.
- Suppress continuum using FoxWolfram moment R2.
- Apply $E_{\text{miss}} > 0.3$ and $E_{\text{residual}} < 1.0$ GeV.

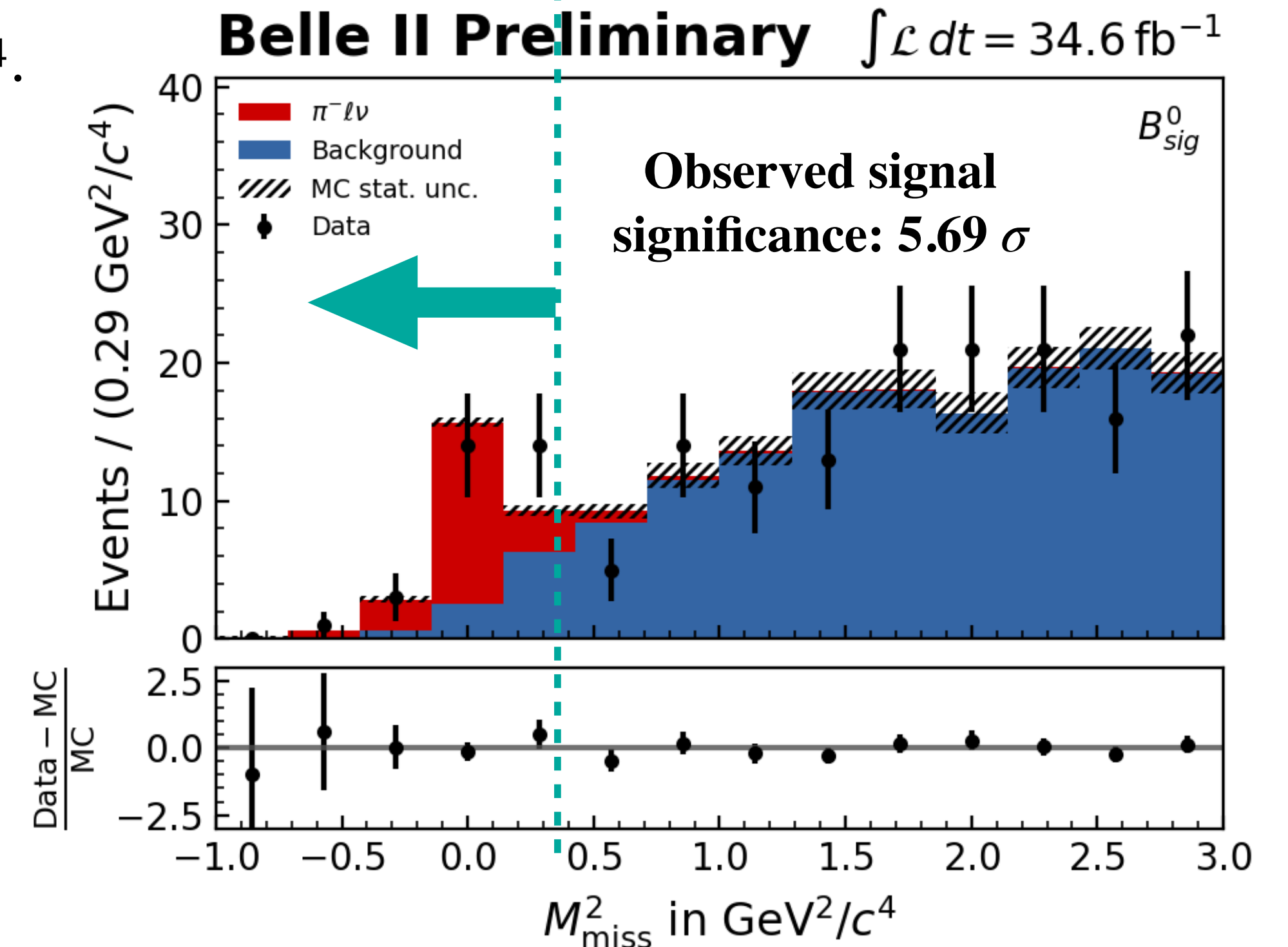
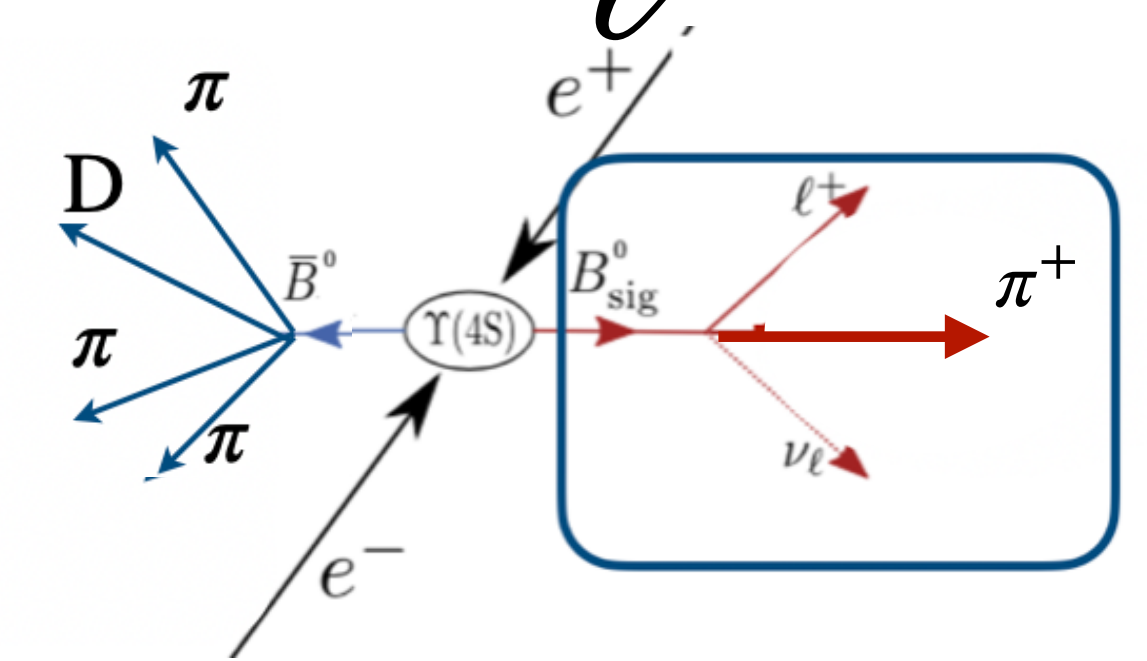
$$p_{\text{miss}} \equiv (E_{\text{miss}}, \vec{p}_{\text{miss}}) = p_{B_{\text{sig}}} - p_Y$$

- Analysis performed blinded in the signal region $M_{\text{miss}}^2 \leq 1 \text{ GeV}^2/c^4$.

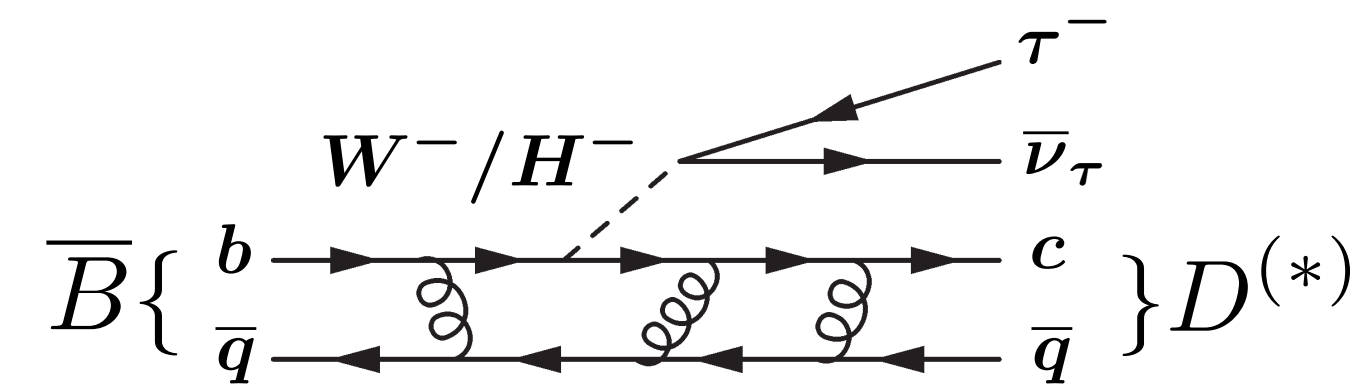
$$\mathcal{B}(B^0 \rightarrow \pi^- \ell \nu) = (1.58 \pm 0.43_{\text{stat}} \pm 0.07_{\text{sys}}) \times 10^{-4}$$

In agreement with world average.

Extract signal yields in bins of q^2 and determine $|V_{\text{ub}}|$.
 Similar effort in channels: $B \rightarrow X \ell \nu$, $X = \pi^0, \rho^+ \rho^0$



R(D) and R(D*)



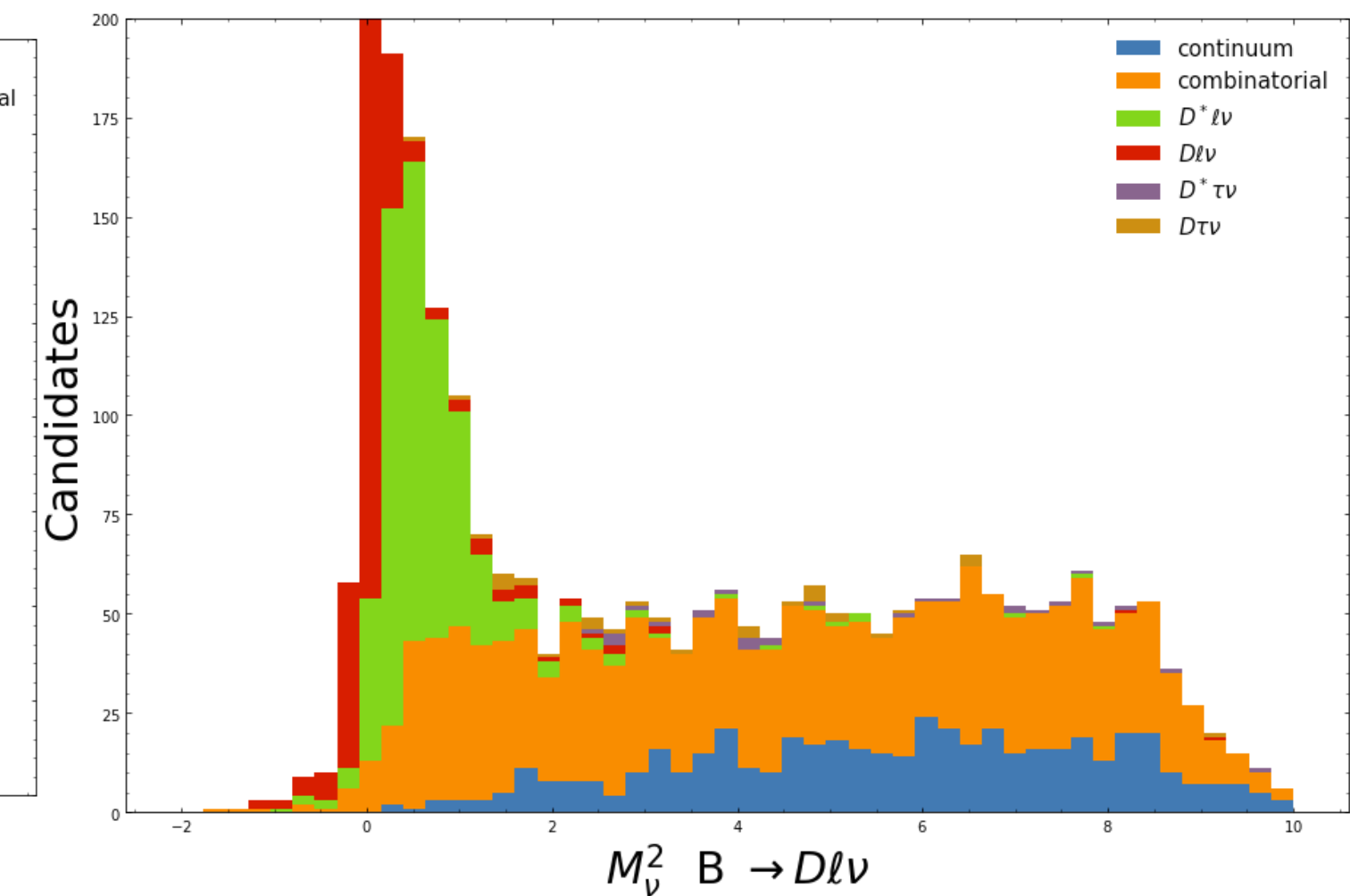
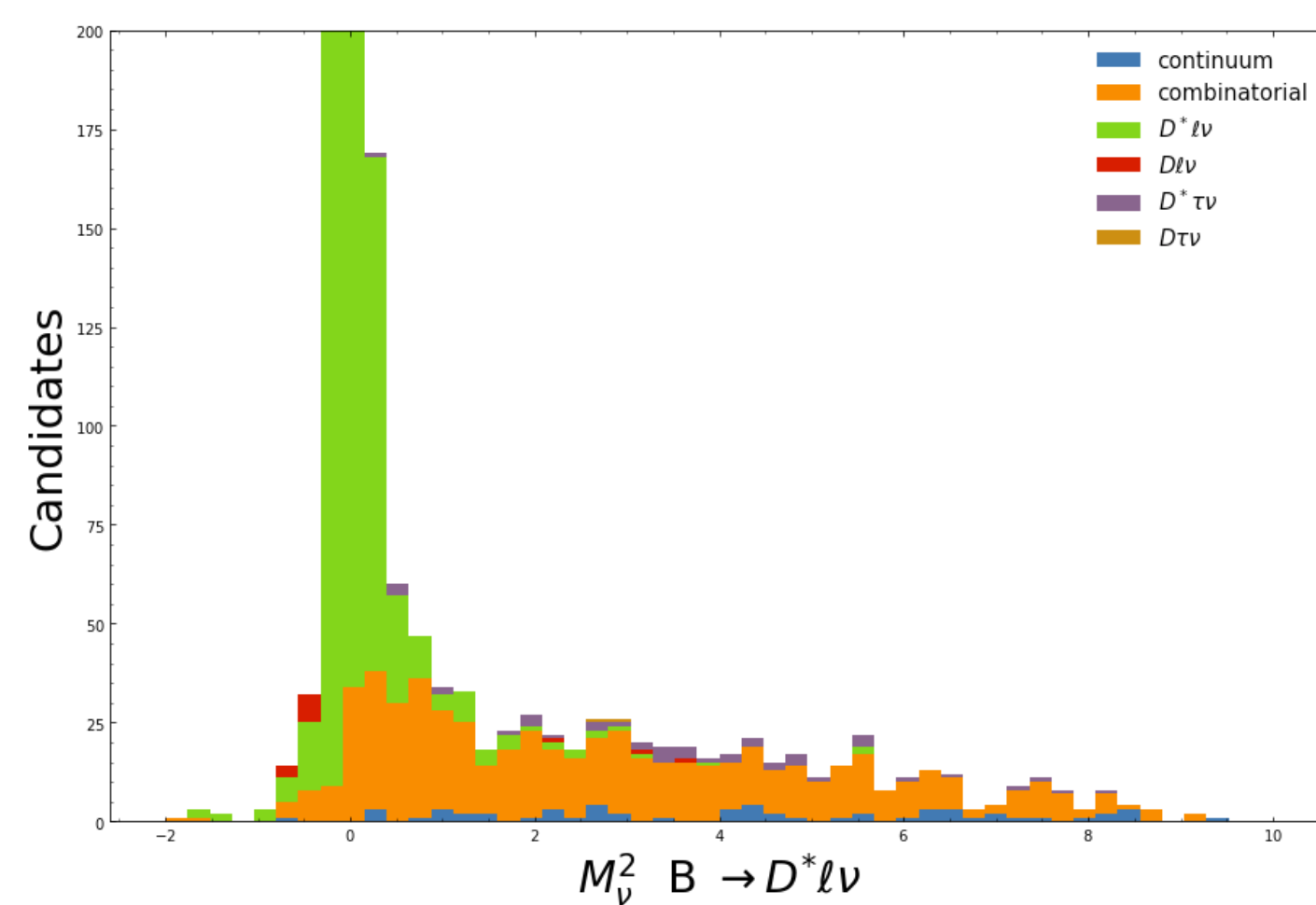
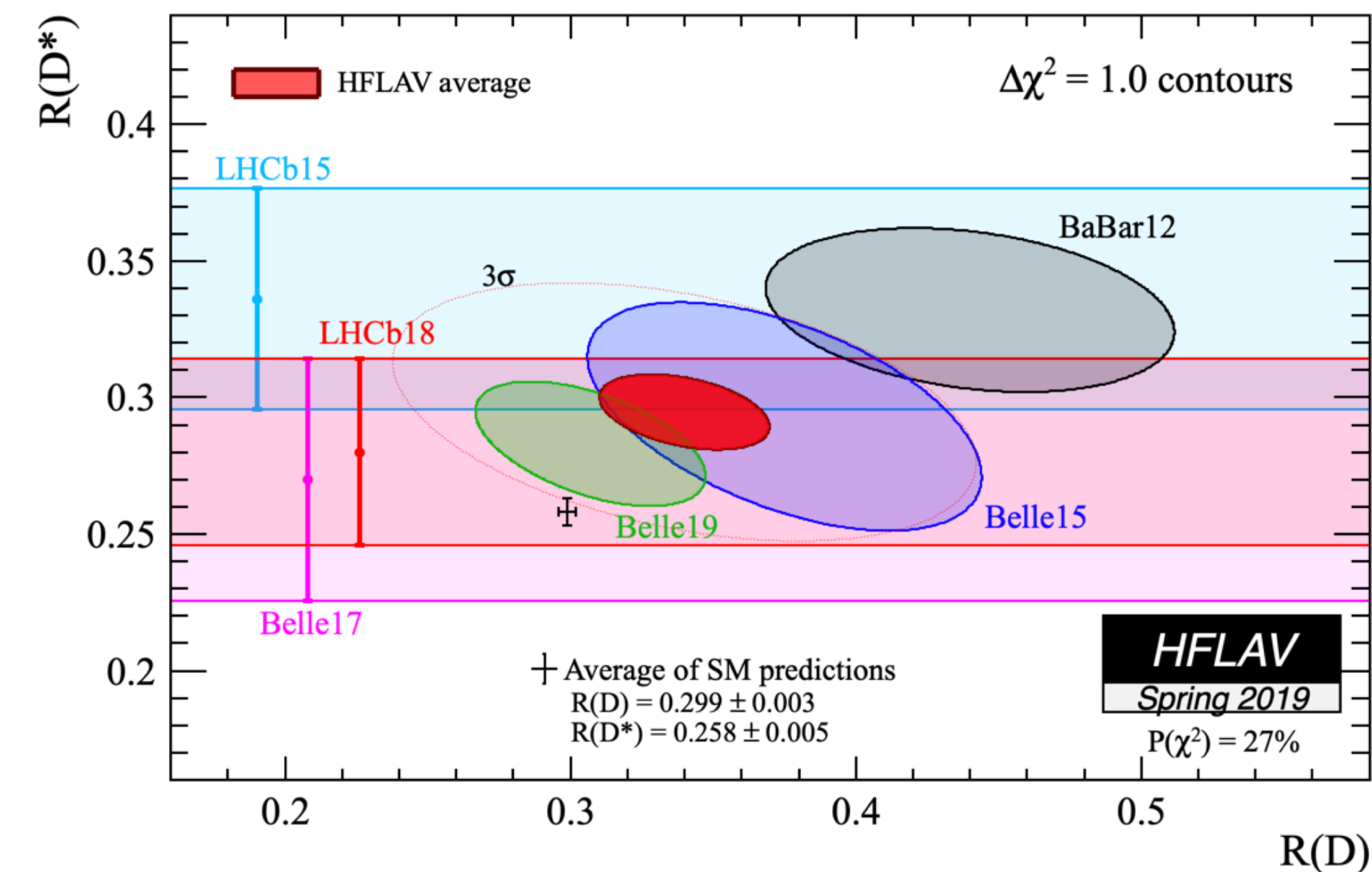
Persistent deviation from Standard Model prediction, measured by Belle, BaBar and LHCb.

$$R(D) = \frac{\mathcal{B}(\bar{B} \rightarrow D^+ \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^+ \ell^- \bar{\nu}_\ell)} \quad R(D^*) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{*+} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{*+} \ell^- \bar{\nu}_\ell)}$$

Signal Mode
Normalization Mode

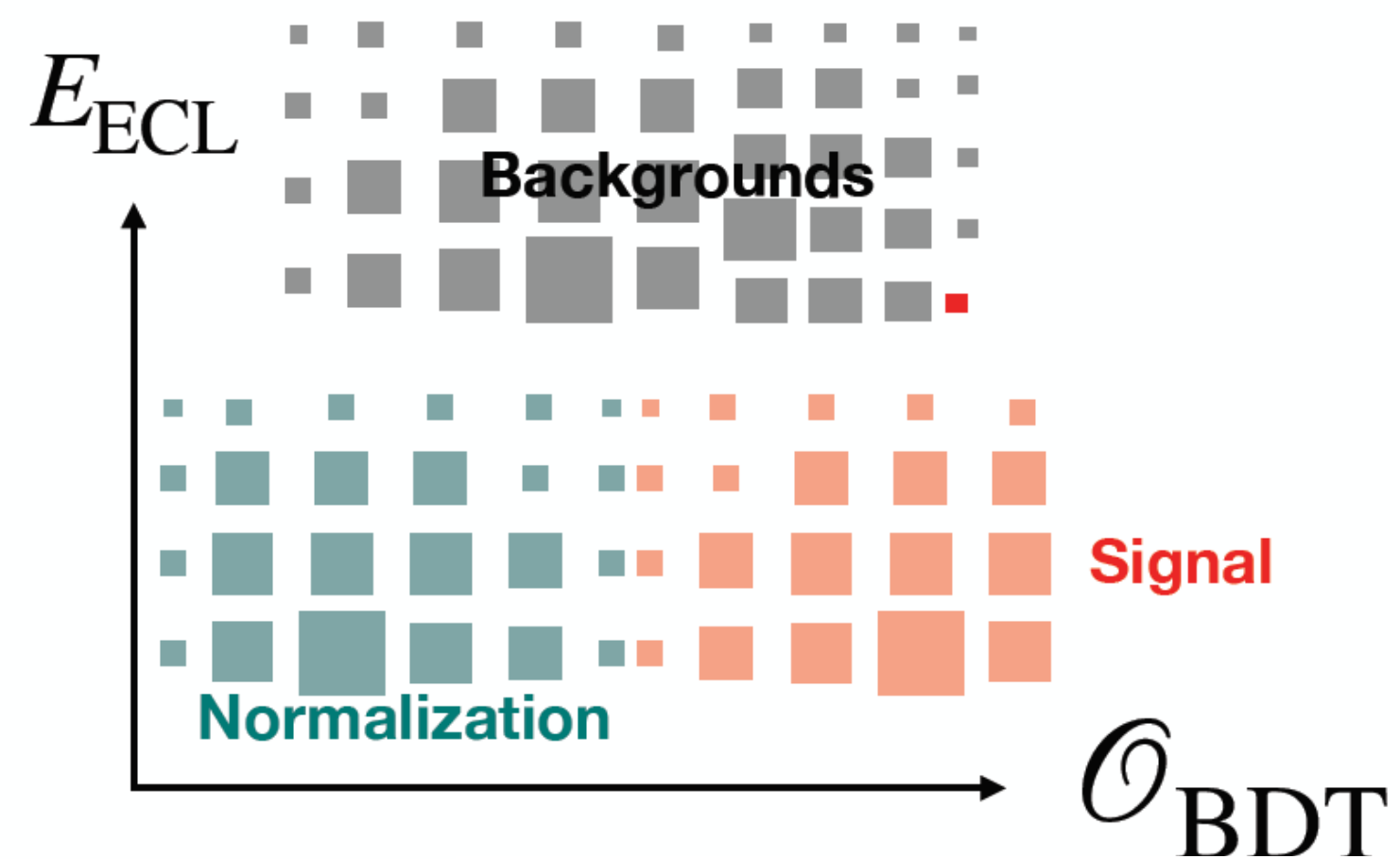
- Current ongoing analyses with FEI hadronic tagging:
 - Leptonic tau decays
 - Hadronic tau decays
 - Inclusive $B \rightarrow X\tau\nu$
- Analyses well established. Current effort to minimize background and optimize signal extraction.
- Initial plan: confirm anomaly with $\sim 0.5 \text{ ab}^{-1}$ of Belle II data.

$$B^0 \rightarrow D^{(*)+} \ell \nu$$



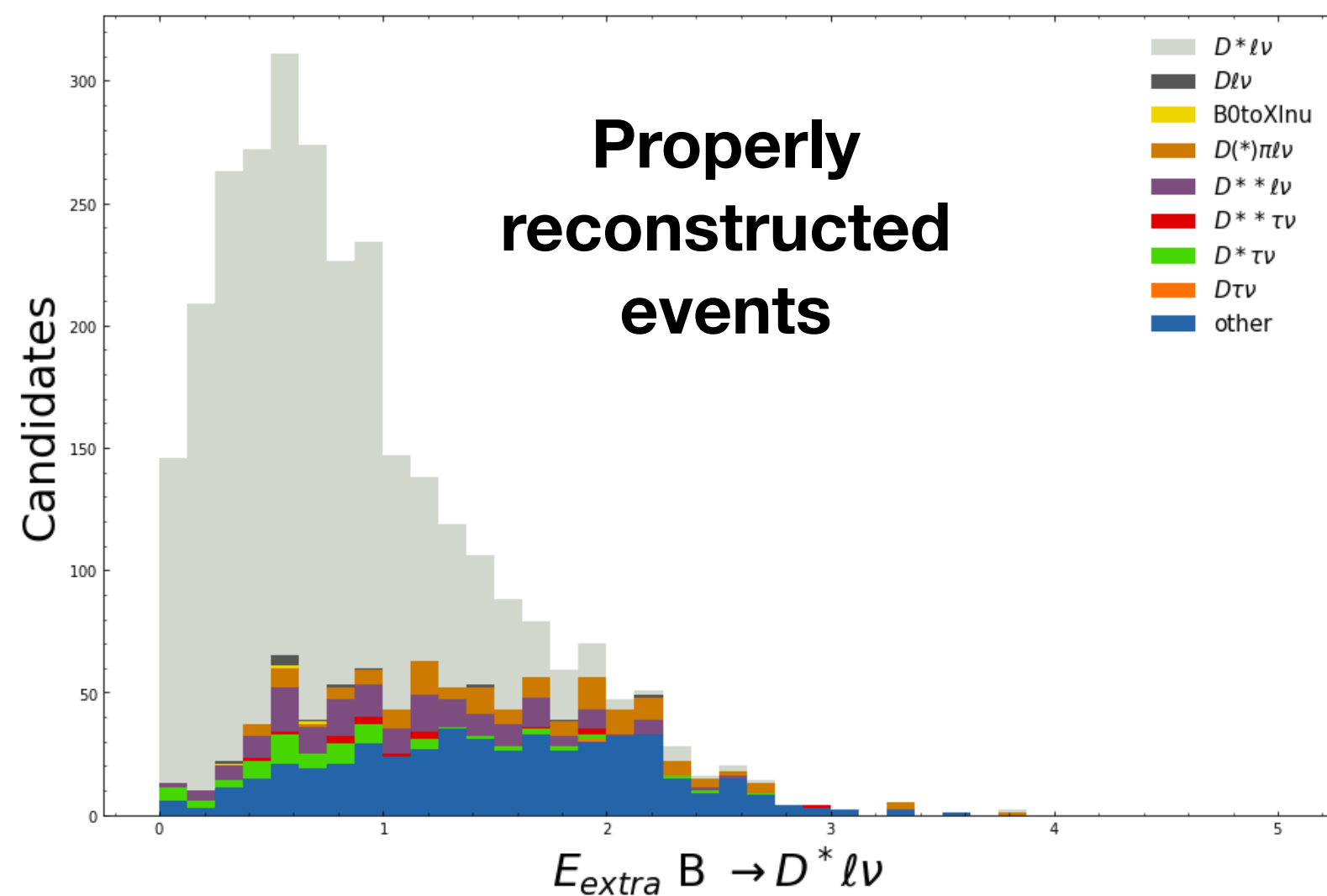
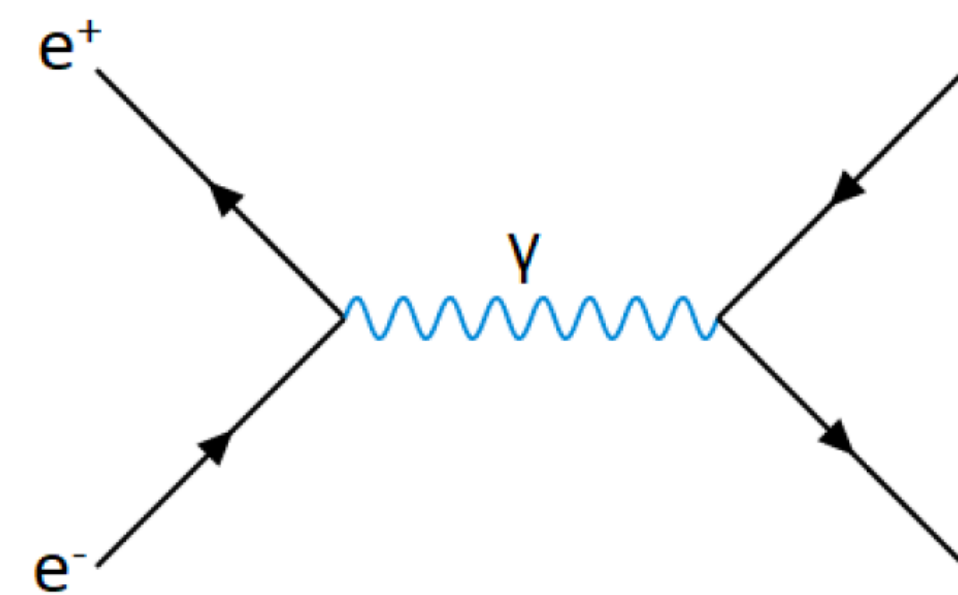
R(D) and R(D*)

- Separation between signal, normalization and background modes can be established with E_{ECL} , sum energy of all neutral deposits in the event not related to the B_{sig} or B_{tag} reconstruction.
- At Belle II, beam backgrounds contribute to E_{ECL} and dilute separation between signal and background.

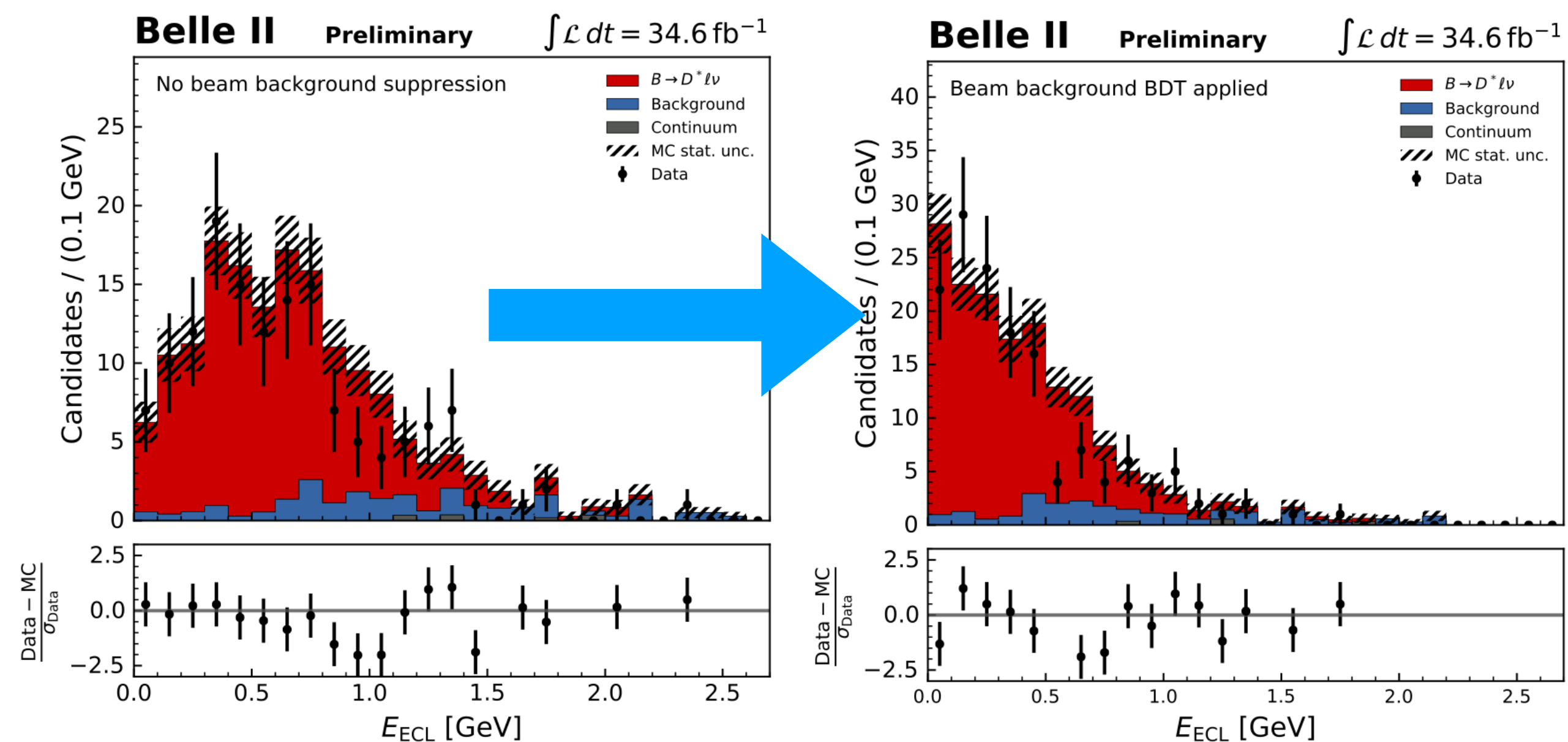


Use $e^+e^- \rightarrow \mu^+\mu^-$ data events and examine the cluster shape and energy distribution of energy deposits related to beam backgrounds.

Train MVA to suppress beam background contributions in E_{ECL} .



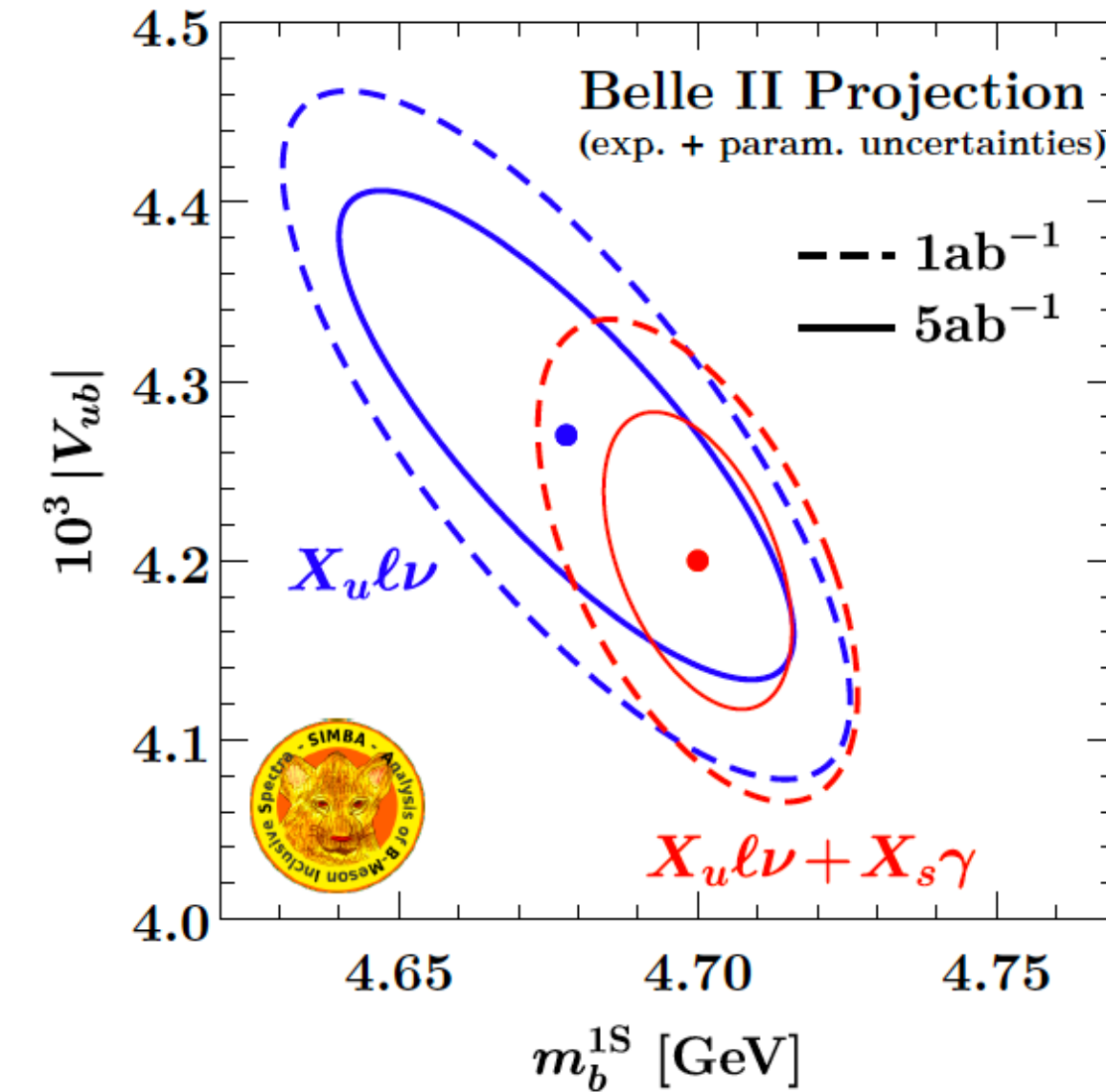
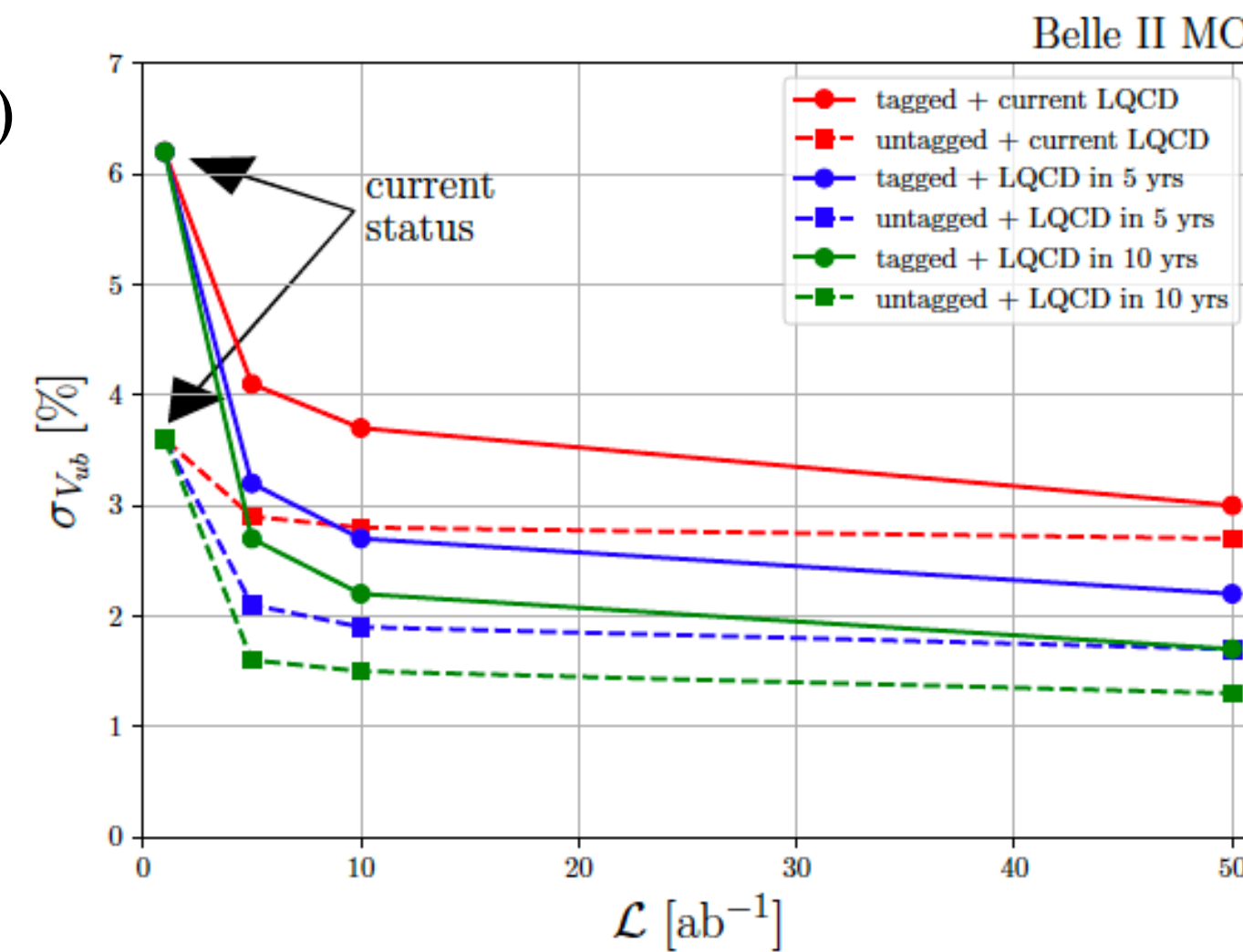
Work in progress for further optimization and suppression of hadronic split-offs as well.





$B \rightarrow X\ell\nu$ Prospects at Belle II

- With 1 ab^{-1} size dataset, the limitation will mainly be systematic.
 - Improved tracking, PID and vertexing tools.
- Improved tagging techniques Full Event Interpretation(see backup) is expected to increase efficiency by $\sim 2\%$
- Improved measurements for $N_{B\bar{B}}$ and f^{+0}
- Achieve higher precision in the measurements of the moments for inclusive $|V_{cb}|$.
 - Valuable input for theory!
- Provide complementary kinetic information by measuring other single differential spectra, such as the hadronic energy or q^2 .
 - Work already in progress.
- Improved measurements of $B \rightarrow D^{**}\ell\nu$ with 1 ab^{-1}
- For inclusive $|V_{ub}|$, maximize shape function information by measuring a large number of differential spectra
- Global fit to the full spectrum, combining $B \rightarrow X_u\ell\nu$ and $B \rightarrow X_s\gamma$ with constraints on HQE parameters from $B \rightarrow X_c\ell\nu$ simultaneously.



	Statistical	Systematic (reducible, irreducible)	Total Exp	Theory	Total
$ V_{ub} $ exclusive (had. tagged)					
711 fb^{-1}	3.0	(2.3, 1.0)	3.8	7.0	8.0
5 ab^{-1}	1.1	(0.9, 1.0)	1.8	1.7	3.2
50 ab^{-1}	0.4	(0.3, 1.0)	1.2	0.9	1.7
$ V_{ub} $ exclusive (untagged)					
605 fb^{-1}	1.4	(2.1, 0.8)	2.7	7.0	7.5
5 ab^{-1}	1.0	(0.8, 0.8)	1.2	1.7	2.1
50 ab^{-1}	0.3	(0.3, 0.8)	0.9	0.9	1.3

Conclusion

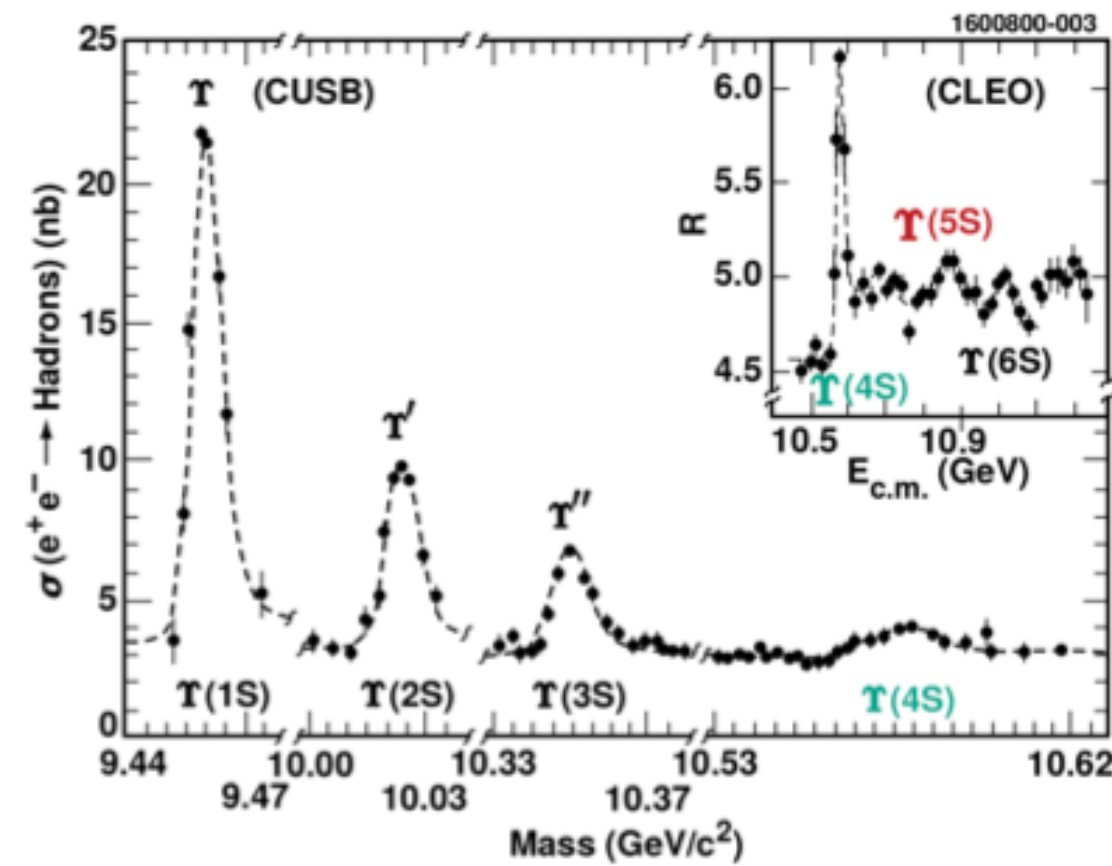
- $B \rightarrow D^{(*)}\ell\nu$ and exclusive $|V_{cb}|$:
 - Work in progress at Belle II for improved precision in $B \rightarrow D\ell\nu$ and $B \rightarrow D^*\ell\nu$ results.
 - Expected first $|V_{cb}|$ measurement by EPS 2021 for untagged $B \rightarrow D^*\ell\nu$.
- $B \rightarrow X_c\ell\nu$ and inclusive $|V_{cb}|$:
 - Novel q^2 moments to be measured at Belle II using tagged and untagged approaches.
 - First results expected by EPS2021.
- $B \rightarrow \pi, \rho, \eta\ell\nu$ and exclusive $|V_{ub}|$
 - Upcoming results on untagged $B \rightarrow \pi\ell\nu$ for Fall 2021.
 - Work in progress at Belle II for improved precision in $B \rightarrow \pi\ell\nu$ and $B \rightarrow \rho\ell\nu$, results by EPS 2021.
- $B \rightarrow X_u\ell\nu$ and inclusive $|V_{ub}|$:
 - Work in progress at Belle II for first results using lepton endpoint spectrum analysis.



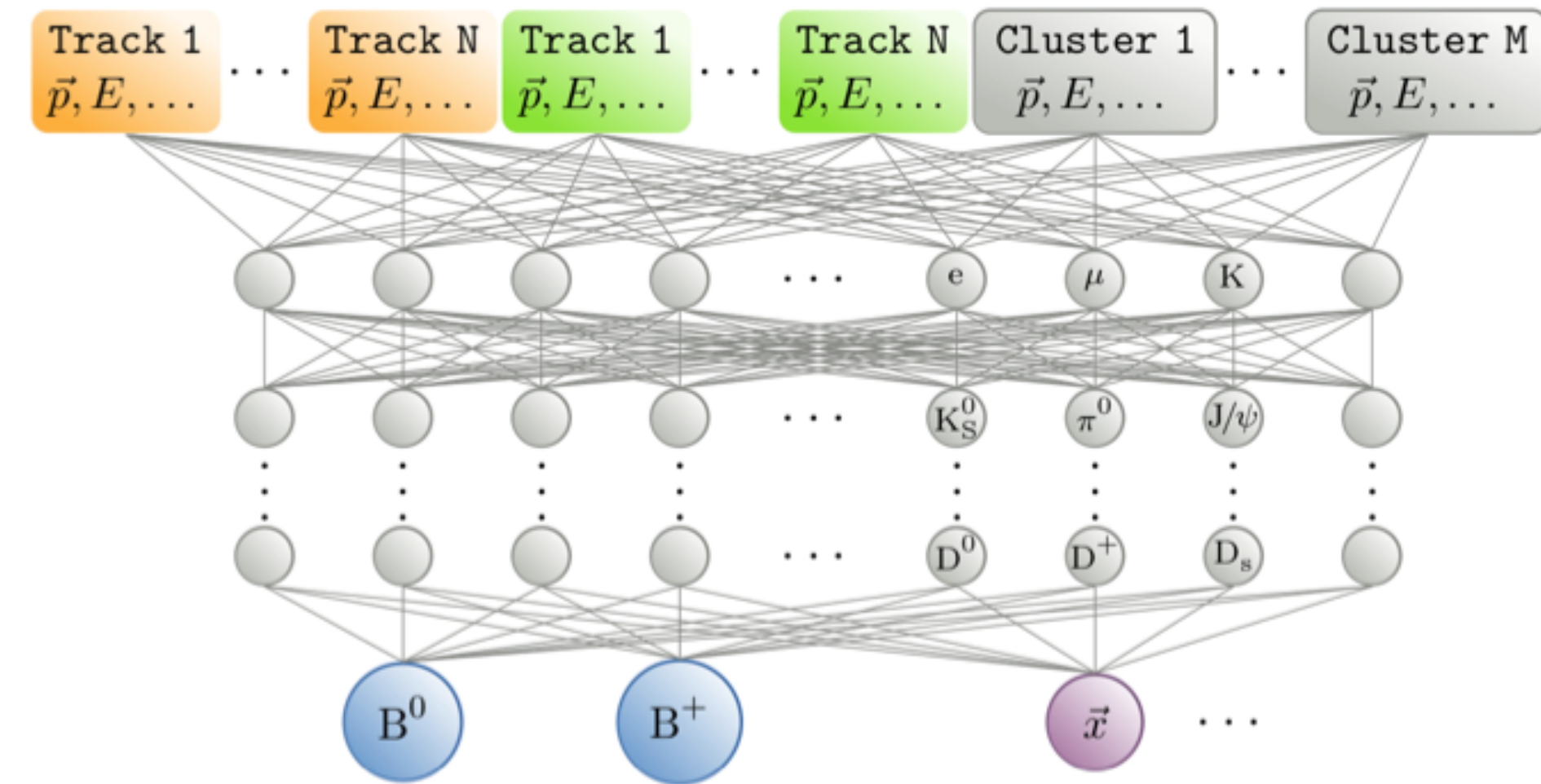
Back up

FEl prospects

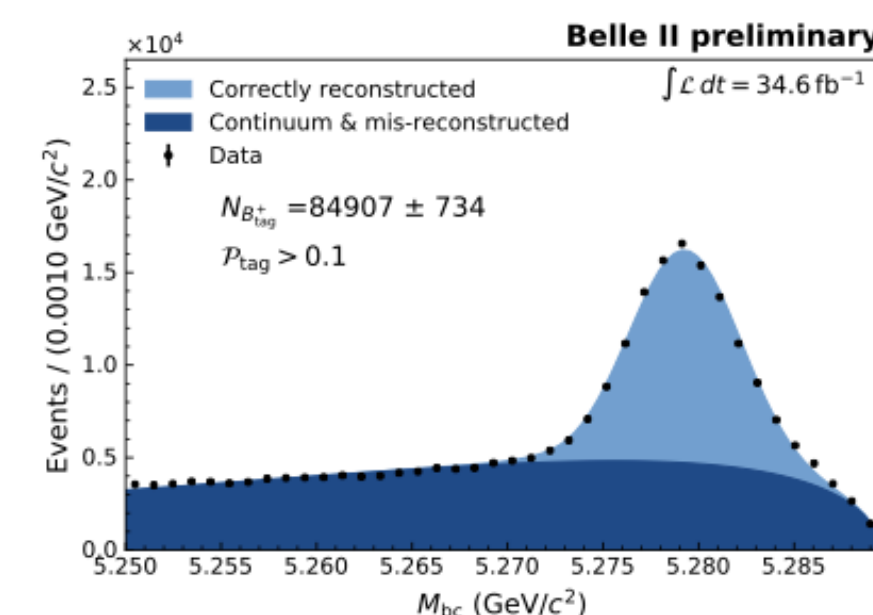
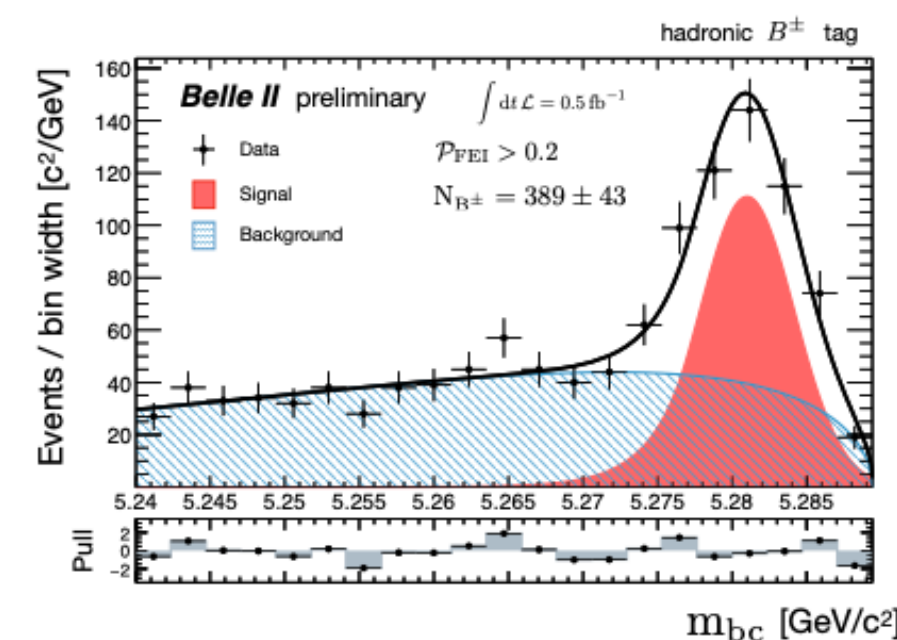
- Algorithm has been successfully applied to the $\Upsilon(5S)$ resonance.



- Exploring deep extensions of the FEl.



- We can look forward to exciting physics results from the growing number of B tags at Belle II!

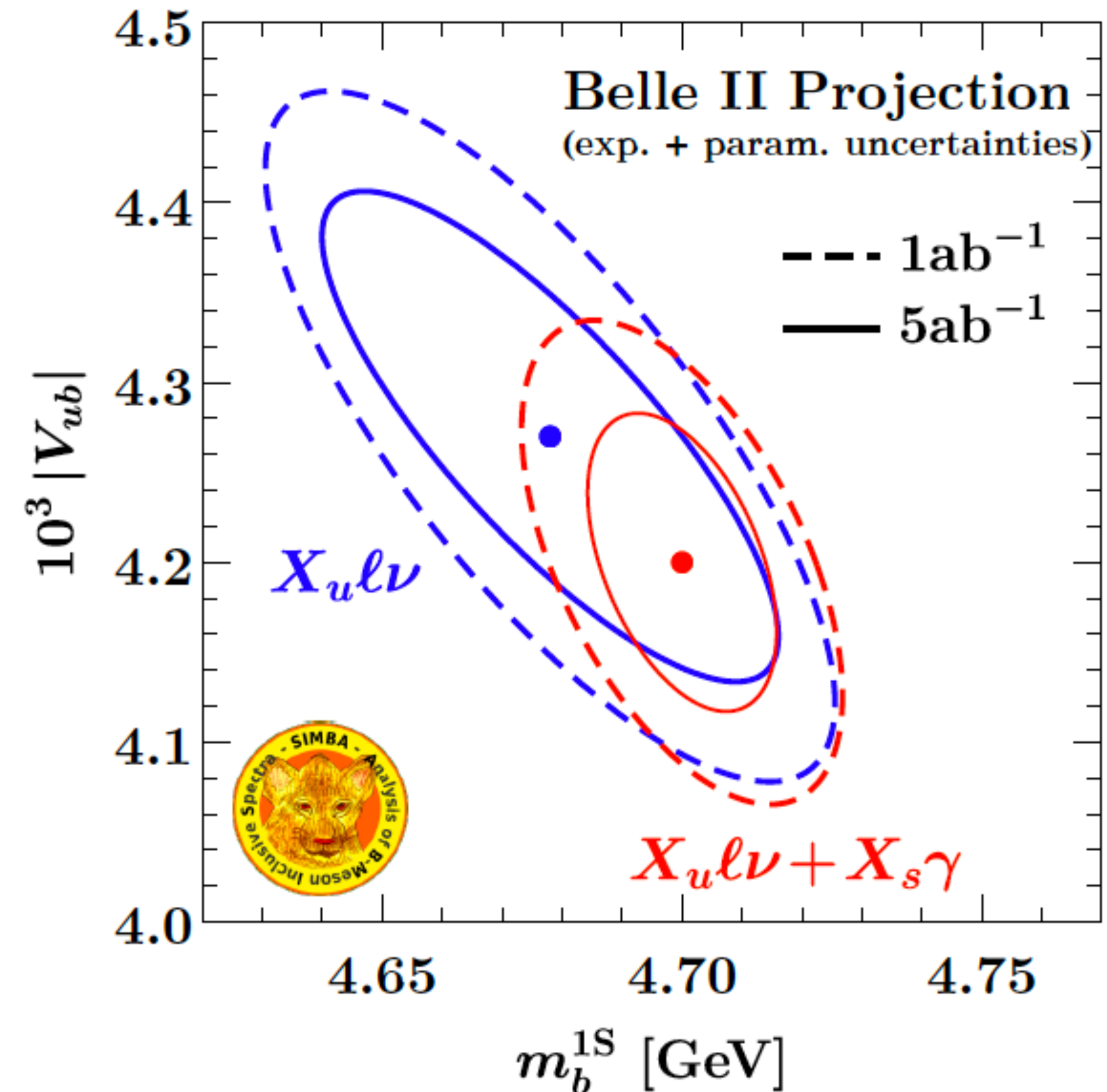


Inclusive $B \rightarrow X_u \ell \nu$ at Belle II

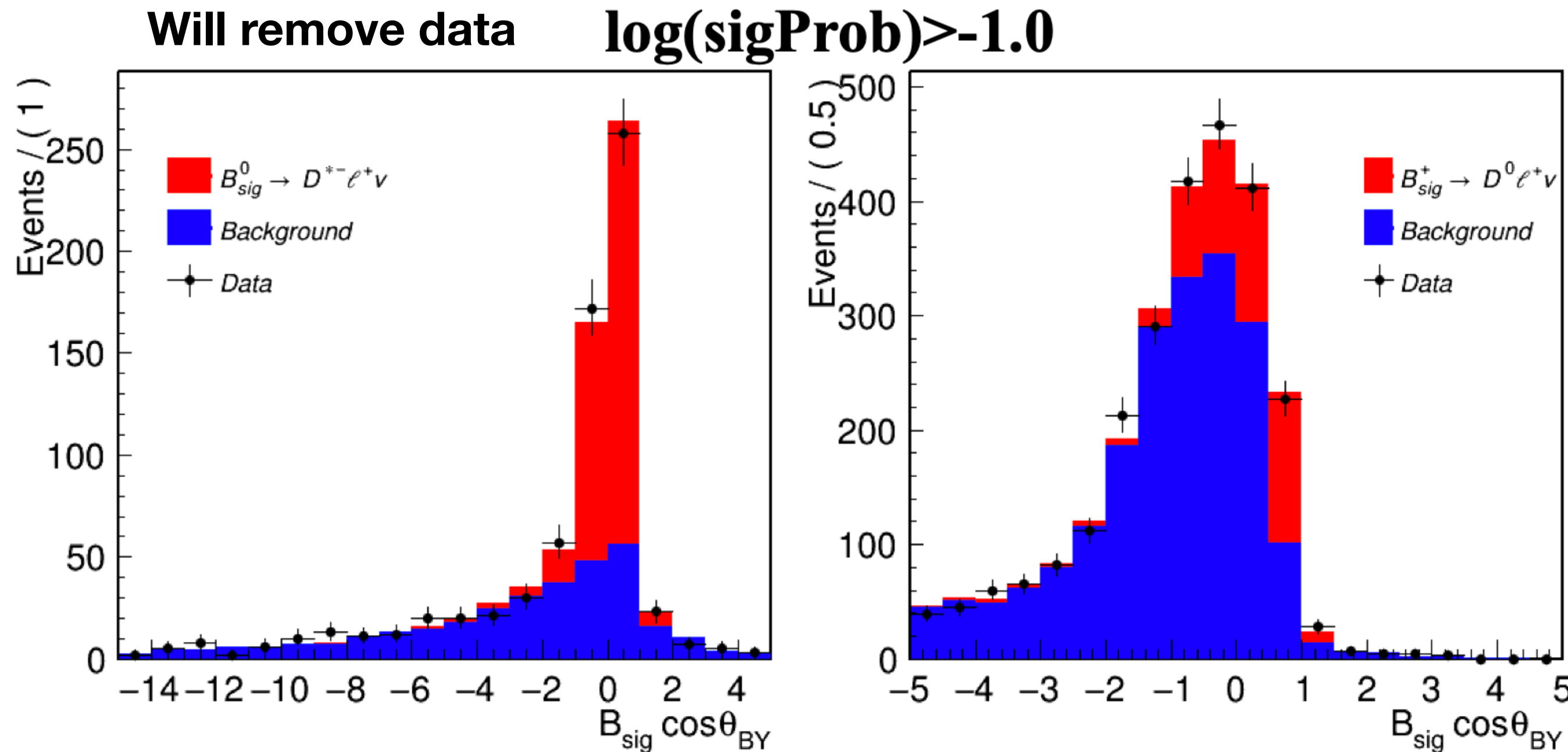
- Maximize shape function information by measuring a large number of differential spectra
- Global fit to the full spectrum, combining $B \rightarrow X_u \ell \nu$ and $B \rightarrow X_s \gamma$ with constraints on HQE parameters from $B \rightarrow X_c \ell \nu$ simultaneously
- This has been demonstrated by SIMBA, **A**nalysis of **B**-Meson, **I**nclusive **S**pectra, group.

	Statistical	Systematic (reducible, irreducible)	Total Exp	Theory	Total
$ \bar{V}_{ub} $ inclusive					
605 fb ⁻¹ (old B tag)	4.5	(3.7, 1.6)	6.0	2.5–4.5	6.5–7.5
5 ab ⁻¹	1.1	(1.3, 1.6)	2.3	2.5–4.5	3.4–5.1
50 ab ⁻¹	0.4	(0.4, 1.6)	1.7	2.5–4.5	3.0–4.8

- Systematic uncertainties related to tracking and PID will be improved by Belle II upgrades:
 - New and improved PID in the barrel region (time of propagation counter)
 - Smaller drift chamber cell size .
 - Improved detector performance



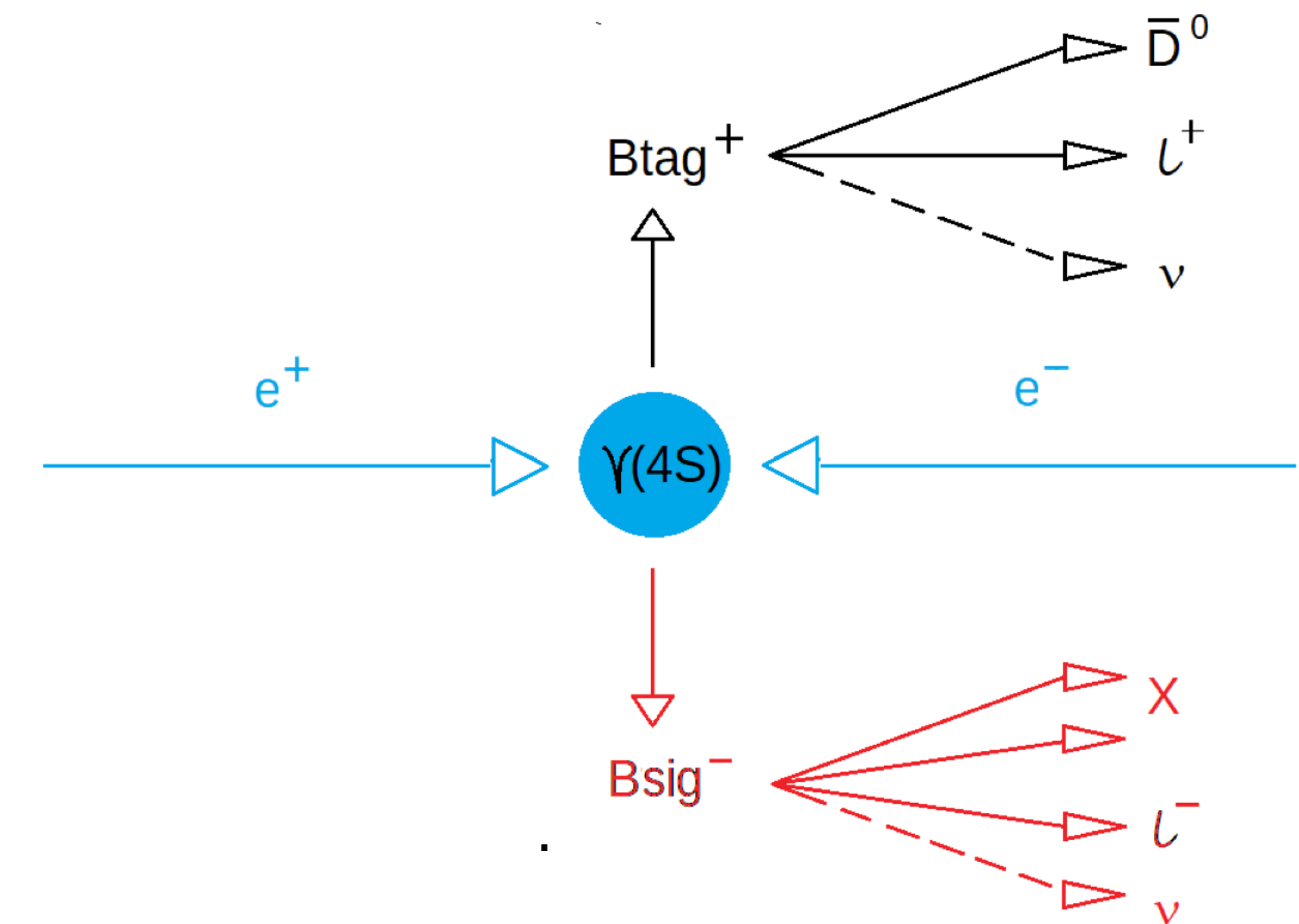
Semi-leptonic FEI calibration



~5% purity

	B^+	B^0
FEI efficiency (%)	2.04	1.80
Full Reconstruction (%) Belle	0.34	0.31

Determined using simulated MC.



- Progress in the semi-leptonic FEI calibration .
- Currently two approaches:
 - $B \rightarrow X \ell \nu$: similar approach to hadronic calibration
 - $B \rightarrow D^{(*)} \ell \nu$: start with cleaner tag modes
- Effort to converge both approaches and unify procedure for summer 2021 analyses.
- Upcoming measurement of $B \rightarrow \pi \ell \nu$ with semi-leptonic tagging.

Hadronic FEI Systematics

Sources of uncertainty in %								
Channel	Fit Model	$\mathcal{B}(B^{0/+} \rightarrow X\ell\nu)$	Lepton ID	Fit Stat.	Tracking	MC Stat.	$D^*\ell\nu$ FF	$D\ell\nu$ FF
B^+e^-	2.67	2.09	0.76	0.93	0.91	0.39	0.41	0.06
$B^+\mu^-$	2.93	2.1	2.13	0.86	0.91	0.37	0.38	0.06
B^0e^-	3.72	2.1	0.73	1.22	0.91	0.62	0.43	0.07
$B^0\mu^-$	3.17	2.09	2.13	1.19	0.91	0.6	0.41	0.06

Diamond Frame definition

- q^2 reconstructed using Diamond Frame method
- Takes a **weighted** average over four different possible configurations of the B direction

$$q^2 = (p_B - p_\pi)^2$$

