

BOSTJAN GOLOB
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JOZEF STEFAN INSTITUTE



University
of Ljubljana



"Jozef Stefan"
Institute

ALSO WITH



INTRODUCTION

FACILITIES

SPECTROSCOPY

MIXING

CPV

(RARE) DECAYS

2ND OPEN BELLE II PHYSICS WEEK
KEK
28TH OCT - 1ST NOV 2019

DISCLAIMER

OVERVIEW OF EXPERIMENTAL METHODS (NOT EXHAUSTIVE) WITH SELECTED EXAMPLES

CHOICE OF SUBJECTS, AND ESPECIALLY EXAMPLES, HAD TO BE MADE;

SPEAKER IS TO BE BLAMED FOR NOT SHOWING YOUR FAVORITE MEASUREMENT

FREQUENTLY USED REFERENCES:

PDG: M. TANABASHI ET AL. (PARTICLE DATA GROUP), PHYS. REV. D 98, 030001 (2018).

HFLAV: HEAVY FLAVOR AVERAGING GROUP, [HTTPS://HFLAV.WEB.CERN.CH/](https://hflav.web.cern.ch/)

PBF: THE PHYSICS OF THE B FACTORIES, A. BEVAN, B. GOLOB, T. MANNEL, S. PRELL, B. YABSLEY EDS., EUR. PHYS. J. C 74 (2014) .

BIIPB: E. KOU, P. URQUIJO ETN AL. (BELLE II COLL.), ARXIV:1808.10567

SETTING THE SCENE



K. TRABELSI
????

ON DEPUTY SPOKESPERSON'S REQUEST:



J. CRONIN, V. FITCH,
1980

1964: CPV IN KAON SYSTEM

$$K_L \rightarrow 45 (2\pi) / 23 \cdot 10^3 (3\pi)$$

1999 - 2010: BEAUTY IS THE NEW STRANGE

LARGE CPV IN B^0 SYSTEM (2001)

WITH $\sim 7 \cdot 10^2 B^0 \rightarrow J/\psi K_S$

2015 - : CHARM IS THE NEW BEAUTY

CPV IN D^0 DECAYS (2019)

WITH $1.4 \cdot 10^7 D^0 \rightarrow \pi\pi$



M. KOBAYASHI,
T. MASKAWA,



2008

* SOME EXPLANATION OF THIS DIFFERENT DATA SIZES
P. 58

PRECISE CHARM MEASUREMENTS REQUIRE LARGE DATA SAMPLES
AND GOOD CONTROL OF SYSTEMATIC UNCERTAINTIES

WHY (NOT) CHARM PHYSICS?

CHARM QUARK:

- UPLIKE

PROCESSES WITH CHARM HADRONS ARE PROBING POTENTIAL NEW PHYSICS IN UPLIKE SECTOR

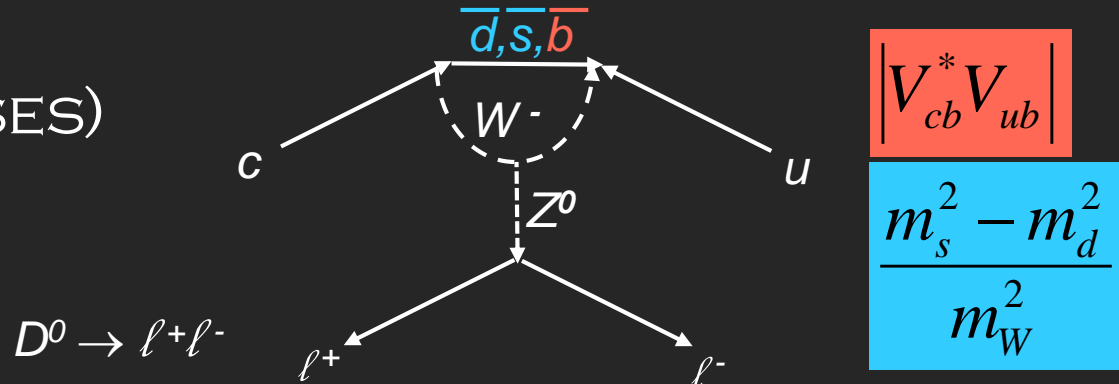
- SEMI-HEAVY

PROCESSES WITH CHARM HADRONS ARE SUBJECT TO RELATIVELY LARGE HADRONIC UNCERTAINTIES ($\sim 1/m_c$)

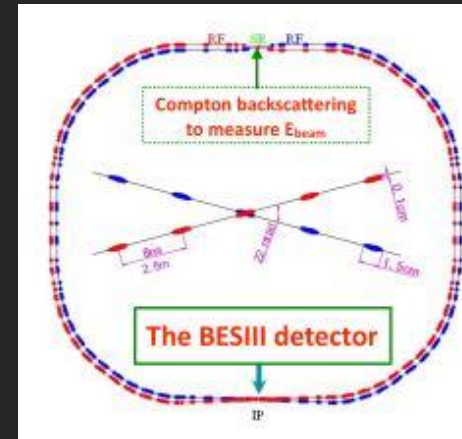
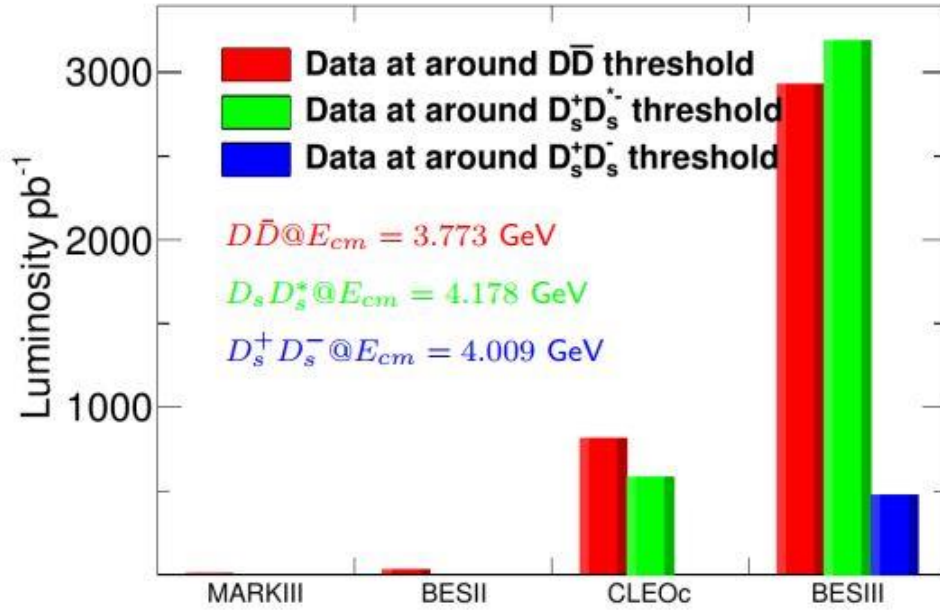
- SUPPRESSED

FCNC (LOOP PROCESSES)
HEAVILY SUPPRESSED

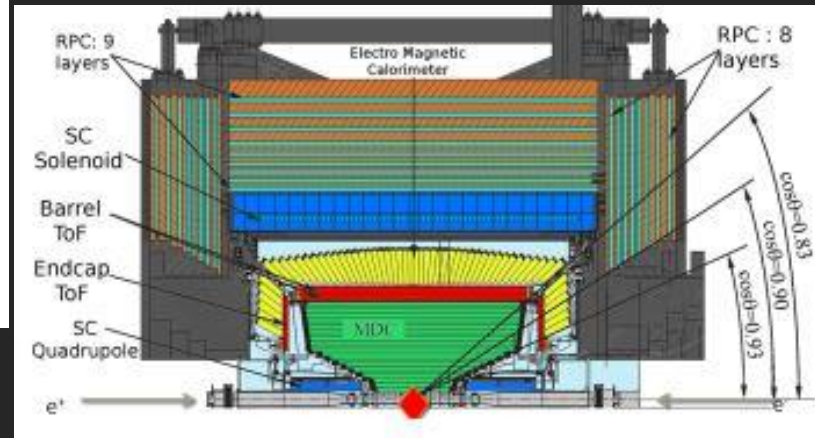
MORE ON GIM P. 29



BES III @ BEPC2



MORE ON P. 59



$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$
 $\sigma \sim \text{few nb, few} \cdot 10^7 D\bar{D}$



- BACKGROUND FREE SAMPLES
- TAGGING (SINGLE MESON RECONSTRUCTION, BOTH MESONS RECONSTRUCTION)
- $\epsilon \sim O(10\%)$

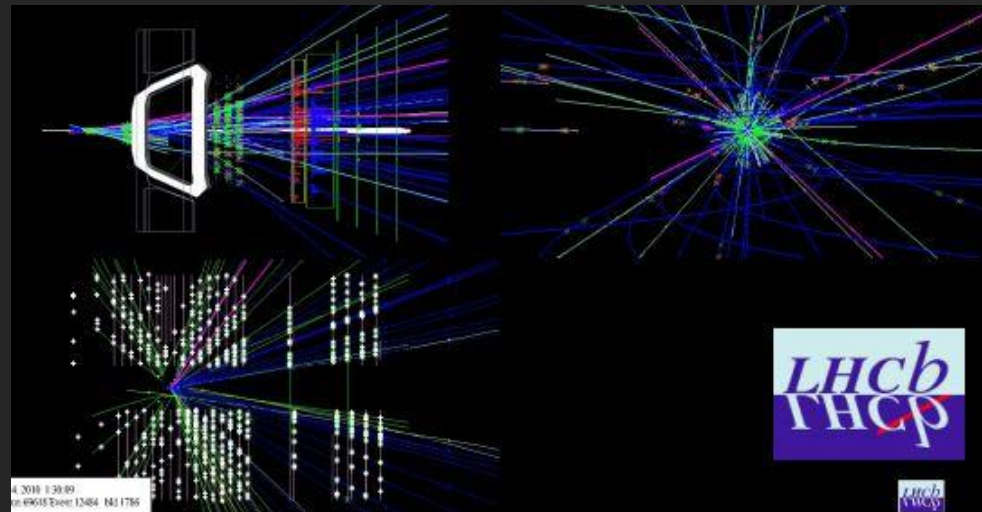
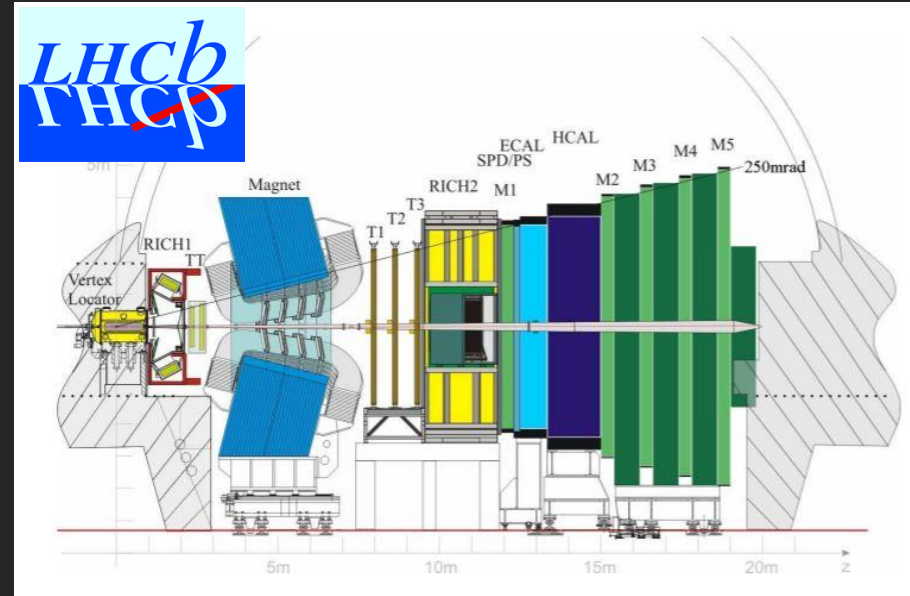
LHCB @ LHC

$$\begin{aligned} \sigma(pp \rightarrow D^0 X) &= 2072 \pm 2 \pm 124 \mu\text{b}, \\ \sigma(pp \rightarrow D^+ X) &= 834 \pm 2 \pm 78 \mu\text{b}, \\ \sigma(pp \rightarrow D_s^+ X) &= 353 \pm 9 \pm 76 \mu\text{b}, \\ \sigma(pp \rightarrow D^{*+} X) &= 784 \pm 4 \pm 87 \mu\text{b}, \end{aligned}$$

R. AAJ ET AL., (LHCb COLL.), JHEP 03 (2016) 159

$$\begin{aligned} \int L dt &= 9 \text{ FB}^{-1} \\ &\sim 10^{10} D^{*+} \end{aligned}$$

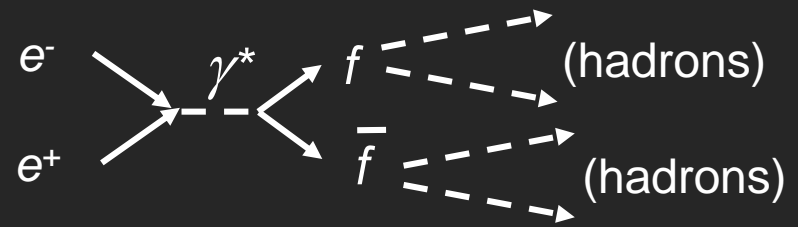
- COMPLICATED TRIGGERS, VTXING
- $\epsilon \sim O(0.1\%)$





BELLE (II) @ (SUPER)KEKB

- $\sigma(e^+e^- \rightarrow c\bar{c}) @ \sqrt{s} \sim 10.6 \text{ GEV} \sim 1.3 \text{ NB}$
 (N.B. $\sigma(e^+e^- \rightarrow Y(4S) \rightarrow B\bar{B}) = 1.1 \text{ NB}$)



X_C	$\sigma(X_C Y) [PB]$
$D^0 \rightarrow K^- \pi^+$	$1449 \pm 2 \pm 64 \pm 38$
$D^+ \rightarrow K^- \pi^+ \pi^+$	$654 \pm 1 \pm 36 \pm 46$
$D_s^+ \rightarrow \phi \pi^+$	$231 \pm 2 \pm 92 \pm 77$
$\Lambda_c^+ \rightarrow p^+ K^- \pi^+$	$189 \pm 1 \pm 66 \pm 66$
$D^{*0} \rightarrow D^0 \pi^0$	$510 \pm 3 \pm 84 \pm 39$
$D^{*+} \rightarrow D^0 \pi^+$	$598 \pm 2 \pm 77 \pm 20$
$D^{*+} \rightarrow D^+ \pi^0$	$590 \pm 5 \pm 78 \pm 53$

$\Sigma \sim 2.5 \text{ NB} \sim 2 \cdot 1.3 \text{ NB}^*$
 * WHY SUMMING ONLY THESE? P. 60

$$\int L dt = 1 \text{ AB}^{-1}$$

$$\sim 1.5 \cdot 10^9 D^0$$

R. SEUSTER ET AL. (BELLE COLL.), PHYS.REV. D73, 032002 (2006)

- FULL RECONSTRUCTION (TAGGING) POSSIBLE
 - $\epsilon \sim O(1\%)$

BELLE (II) @ (SUPER)KEKB



PRODUCTION IN $B \rightarrow h_c X$

h_c $\langle N(h_c) \rangle / B \text{ DECAY}$

$D^0 \rightarrow K^- \pi^+$	$0.644 \pm 0.003 \pm 0.024 \pm 0.021$
$D^+ \rightarrow K^- \pi^+ \pi^+$	$0.248 \pm 0.004 \pm 0.033 \pm 0.020$
$D_s^+ \rightarrow \phi \pi^+$	$0.122 \pm 0.015 \pm 0.033 \pm 0.030$
$\Lambda_c^+ \rightarrow p^+ K^- \pi^+$	$0.042 \pm 0.011 \pm 0.033 \pm 0.018$
$D^{*0} \rightarrow D^0 \pi^0$	$0.217 \pm 0.014 \pm 0.020 \pm 0.018$
$D^{*+} \rightarrow D^0 \pi^+$	$0.218 \pm 0.007 \pm 0.020 \pm 0.015$
$\rightarrow D^+ \pi^0$	$0.202 \pm 0.014 \pm 0.022 \pm 0.018$



$\sim 1.05 h_c / B \text{ DECAY}$

$\sim 8 \cdot 10^8 B \rightarrow D^0 X$
IN BELLE DATASET

R. SEUSTER ET AL.. (BELLE COLL.), PHYS.REV. D73, 032002 (2006)

LHCb @ LHC



ALSO CASCADE PRODUCTION R. AAJ ET AL.. (LHCb COLL.), JHEP 12 (2017) 026

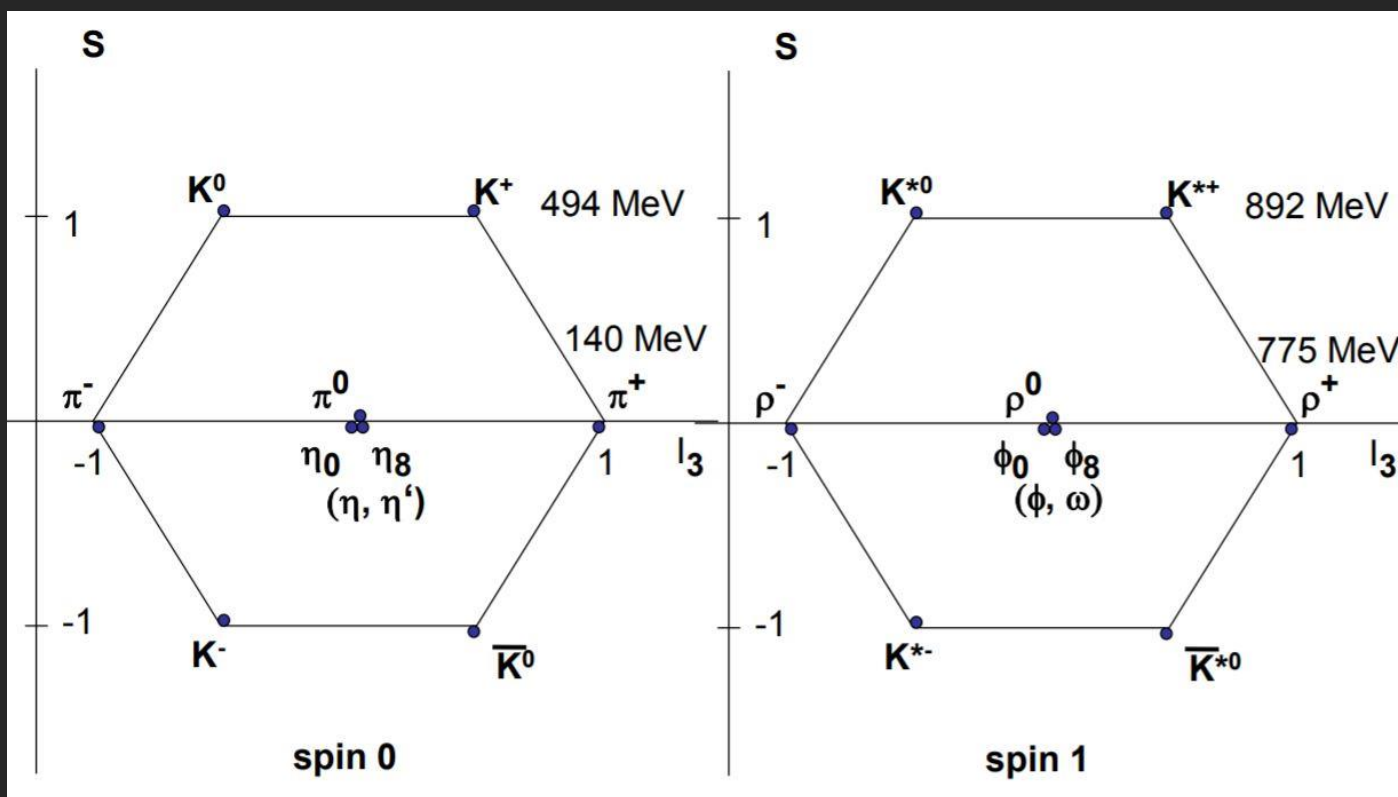
$$\sigma(pp \rightarrow B^\pm X, \sqrt{s} = 7 \text{ TeV}) = 43.0 \pm 0.2 \pm 2.5 \pm 1.7 \mu\text{b}$$

$$\sigma(pp \rightarrow B^\pm X, \sqrt{s} = 13 \text{ TeV}) = 86.6 \pm 0.5 \pm 5.4 \pm 3.4 \mu\text{b}$$

$\rightarrow \sim 8 \cdot 10^{11} B \rightarrow h_c X$

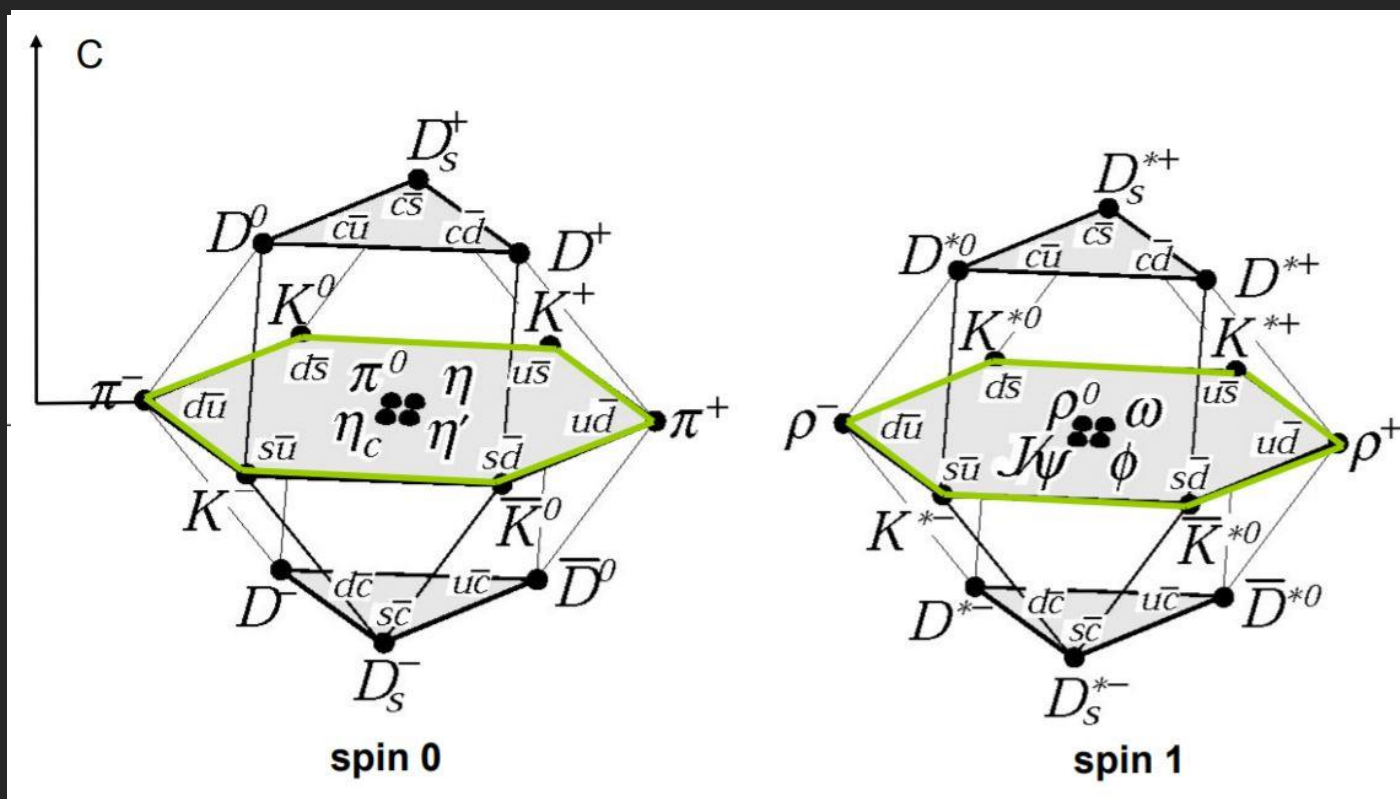
CONVENTIONAL MESONS

QUARK MODEL FOR u, d, s



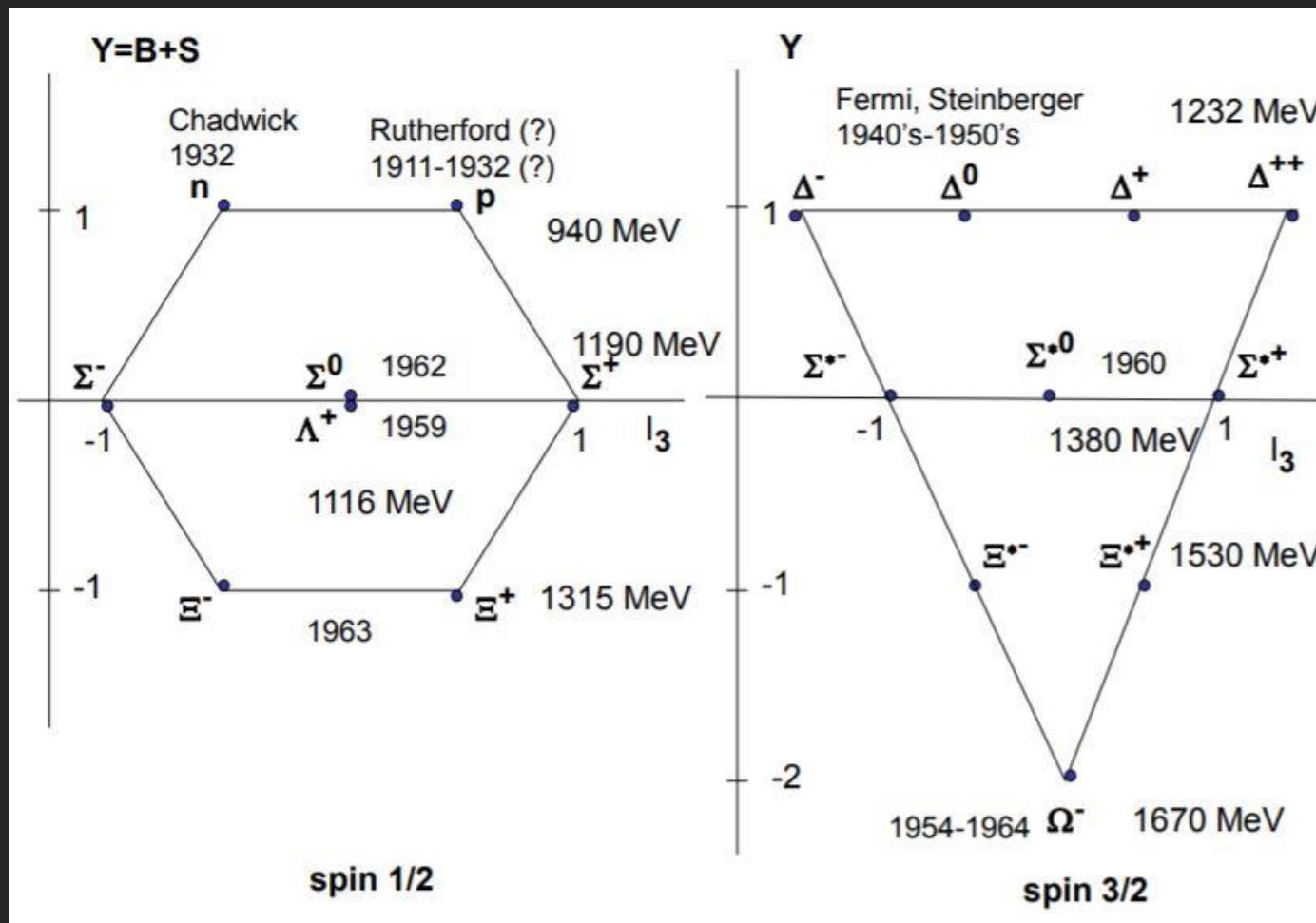
CONVENTIONAL MESONS

QUARK MODEL FOR u, d, s + c



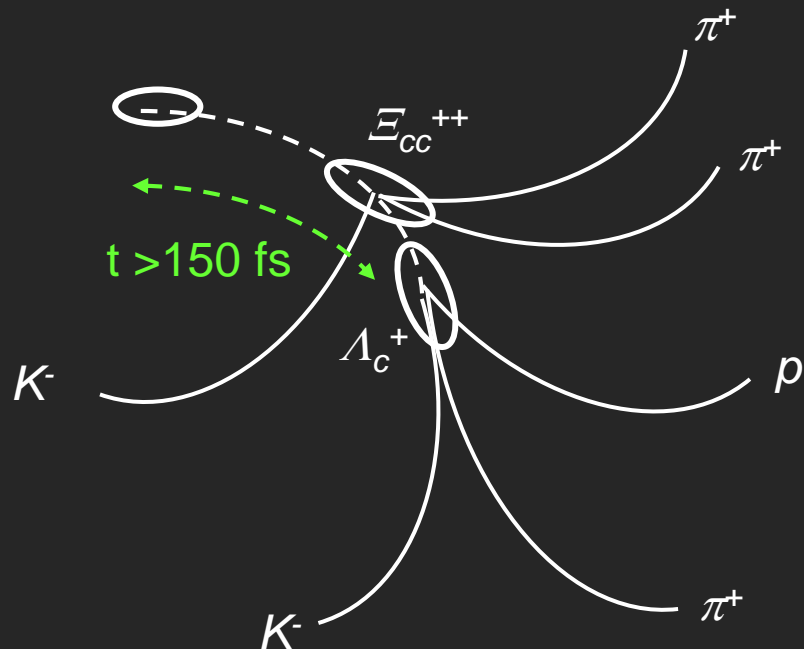
CONVENTIONAL BARYONS

QUARK MODEL FOR u, d, s



Ξ_{cc} @ LHCb

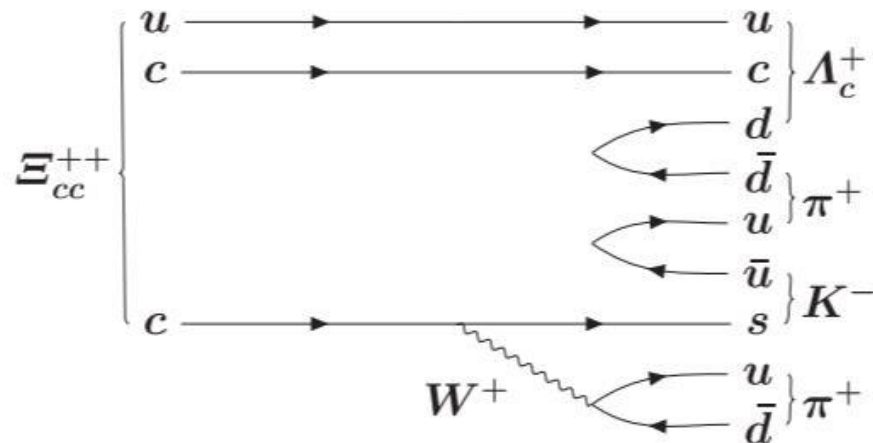
PRECISE VTXING FOR BKG REJECTION



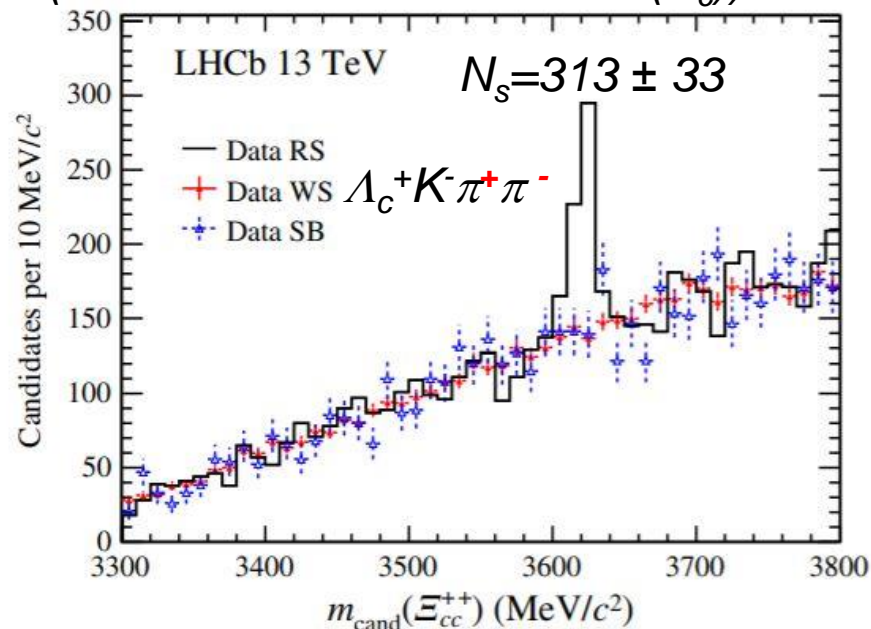
ALSO $\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+$

R. AAJ ET AL., (LHCb COLL.), PRL 121,162002 (2018)

$$\frac{\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+)}{\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+)} \approx 0.5$$



$$M = (3621.4 \pm 0.72 \pm 0.27 \pm 0.14(\Lambda_c)) \text{ MeV}$$



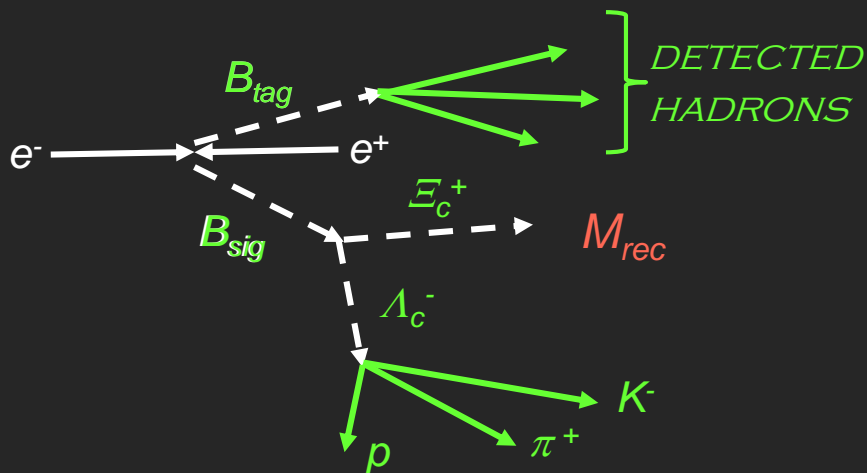
R. AAJ ET AL., (LHCb COLL.), PRL 119,112001 (2017)

ABSOLUTE* BR MEASUREMENTS

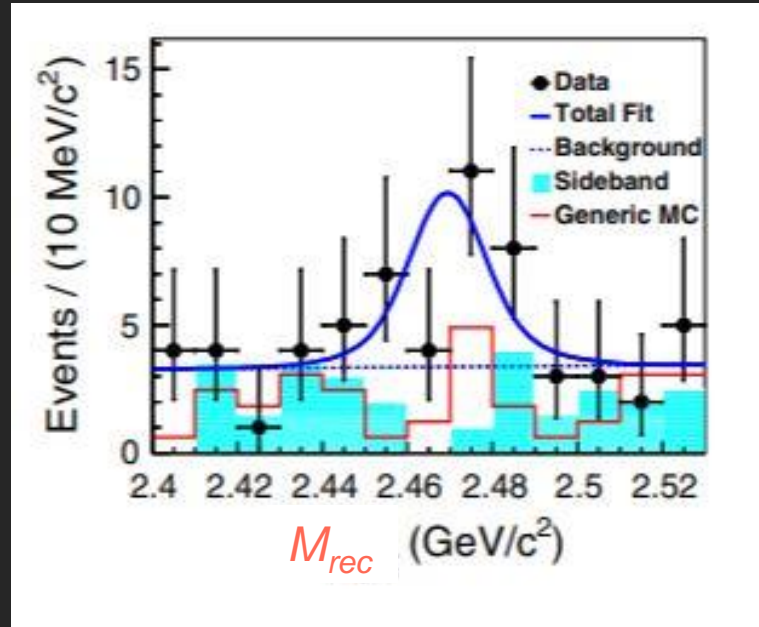
BR($\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+$) POSSIBLE
BECAUSE BR($\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$) KNOWN

1) BR($B \rightarrow \Xi_c^+ \Lambda_c^-$)

HADRONIC TAGGING (FEI @ BELLE II)



Y. B. LI ET AL.. (BELLE COLL.), PRD 100, 031101(R) (2019)



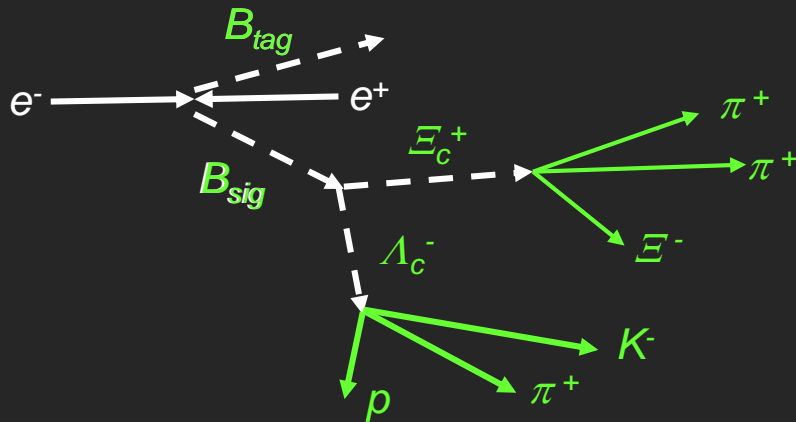
* AS OPPOSED TO RELATIVE W.R.T. SOME OTHER DECAY

ABSOLUTE* BR MEASUREMENTS

BR($\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+$) POSSIBLE
BECAUSE BR($\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$) KNOWN

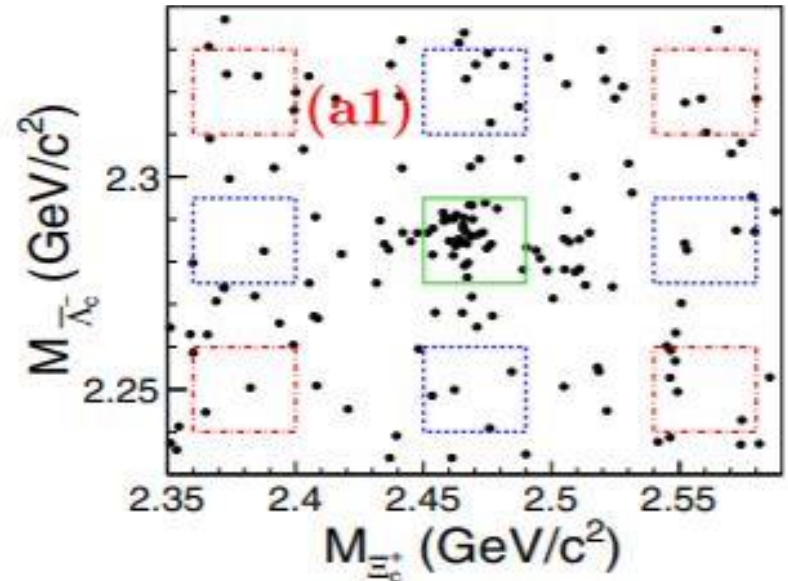
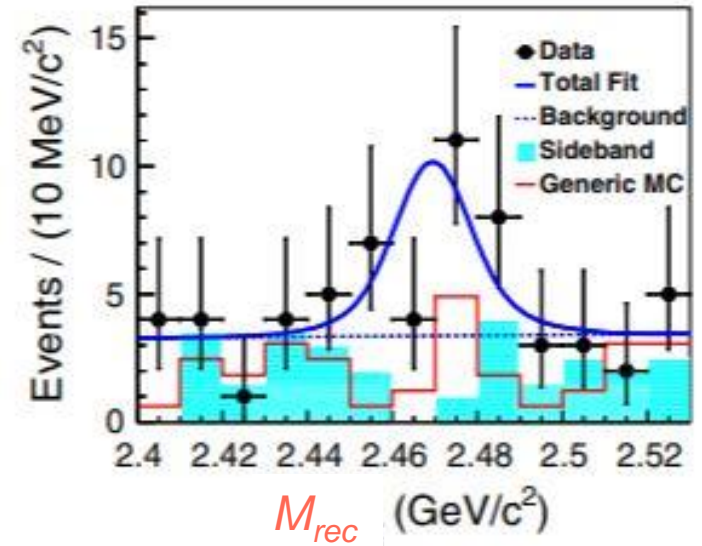
- 1) BR($B \rightarrow \Xi_c^+ \Lambda_c^-$)
- 2) BR($B \rightarrow \Xi_c^+ \Lambda_c^-$) · BR($\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$)

HADRONIC TAGGING (FEI @ BELLE II)



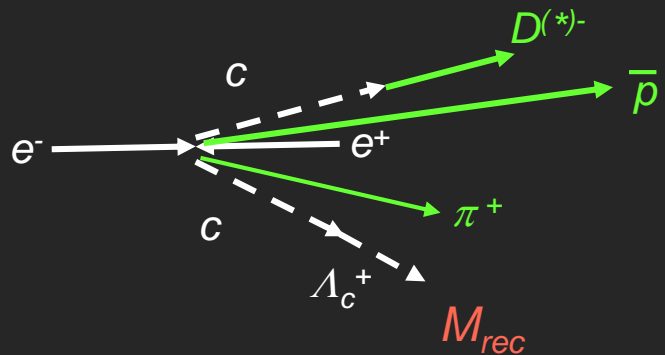
* AS OPPOSED TO RELATIVE W.R.T. SOME OTHER DECAY

Y. B. LI ET AL.. (BELLE COLL.), PRD 100, 031101(R) (2019)

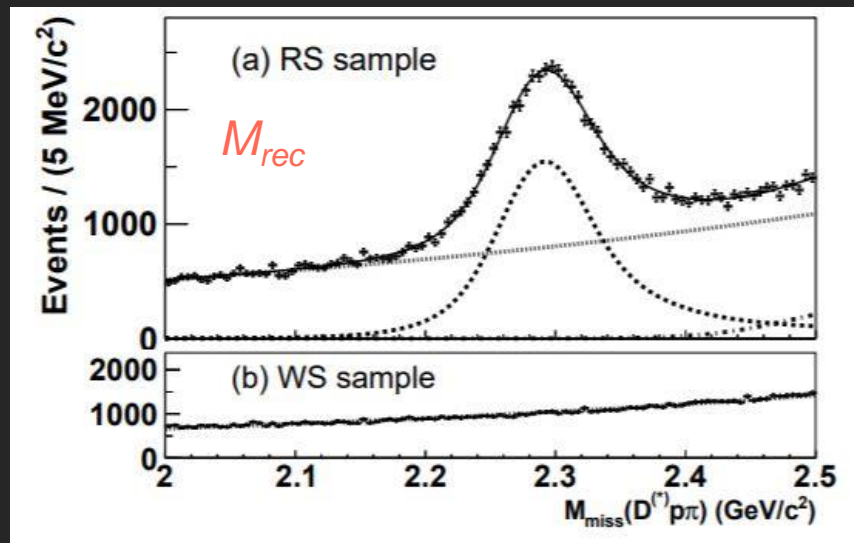


ABSOLUTE BR MEASUREMENTS

$$\text{BR}(\Lambda_c^+ \rightarrow p K^- \pi^+)$$



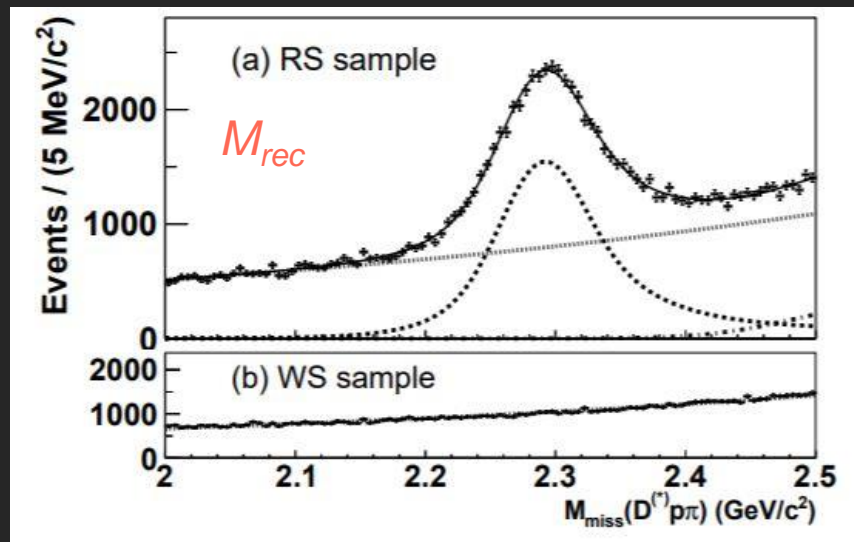
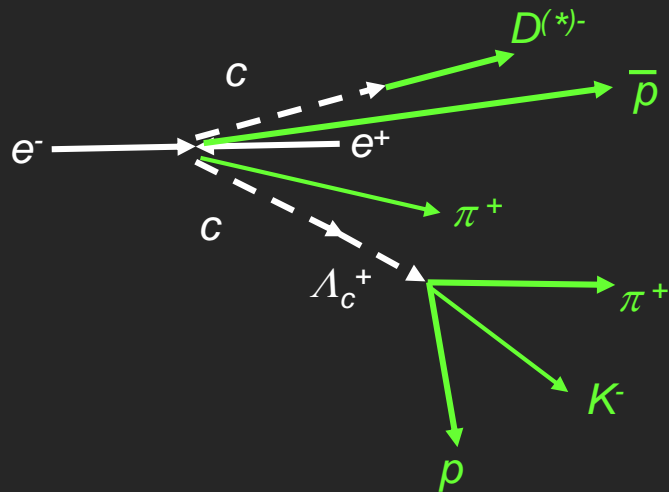
A. ZUPANC ET AL., (BELLE COLL.), PRL 113, 042002 (2014)



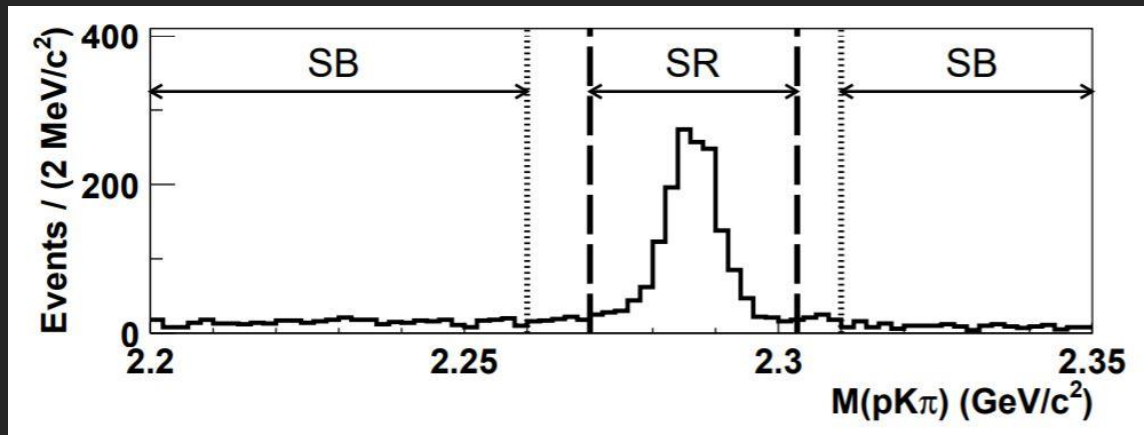
ABSOLUTE BR MEASUREMENTS

A. ZUPANC ET AL.. (BELLE COLL.), PRL 113, 042002 (2014)

$$\text{BR}(\Lambda_c^+ \rightarrow p K^- \pi^+)$$



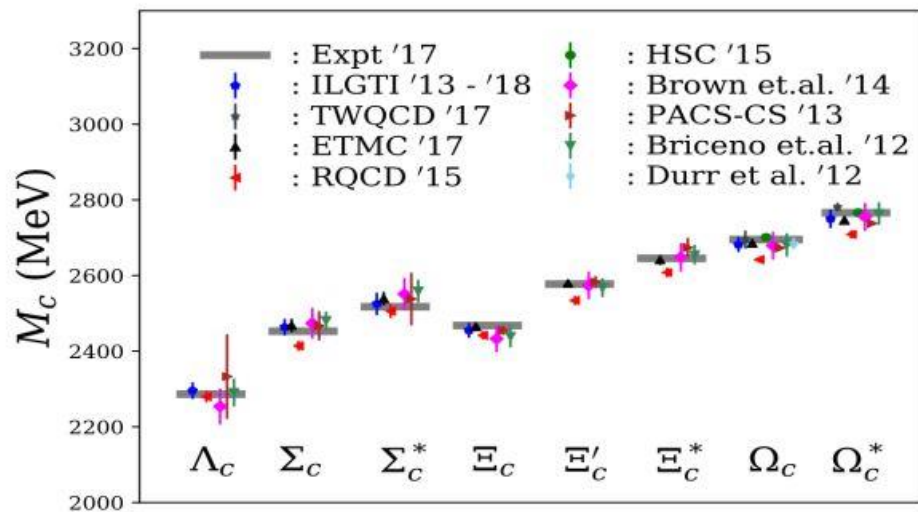
BEFORE: $\pm 26\%$
(FOR MANY YEARS)
AFTER: $\pm 5\%$



COMPARISON TO LQCD

CHARMED BARYONS

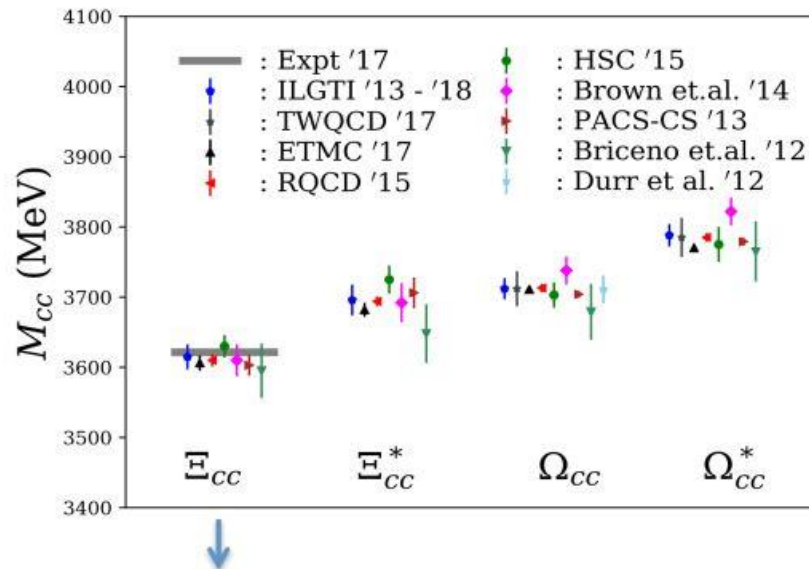
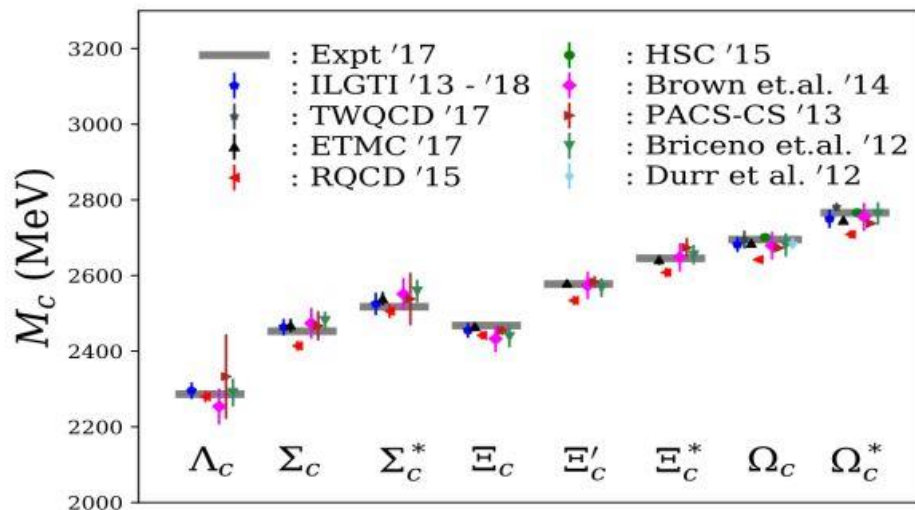
S. PRELOVSEK, BEAUTY 2019



COMPARISON TO LQCD

CHARMED BARYONS

S. PRELOVSEK, BEAUTY 2019



R. AAJ ET AL., (LHCb COLL.), PRL 119, 112001 (2017)

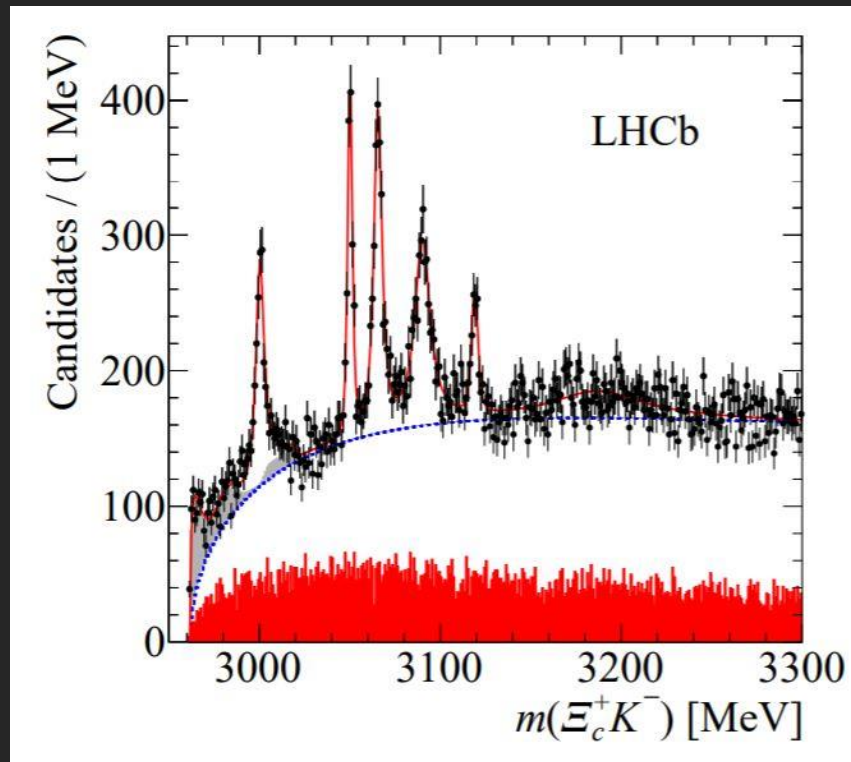
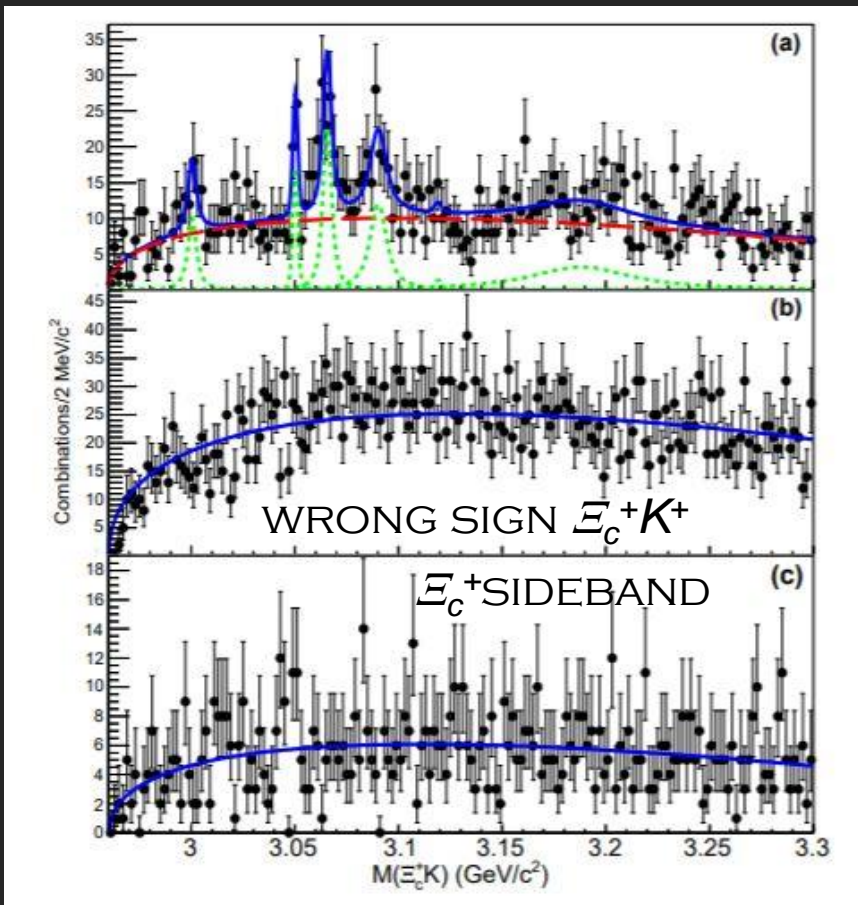
TEST OF LQCD METHODS

EXCITED STATES

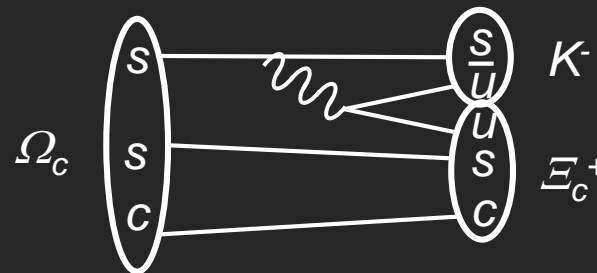
EXCITED Ω_c

$$\Omega_c^* \rightarrow \Xi_c^+(p K^- \pi^+) K^-$$

(N.B. $M(\Omega_c) = 2.695 \text{ GEV}$)



R. AAJ ET AL.. (LHCb COLL.), PRL 118, 182001 (2017)

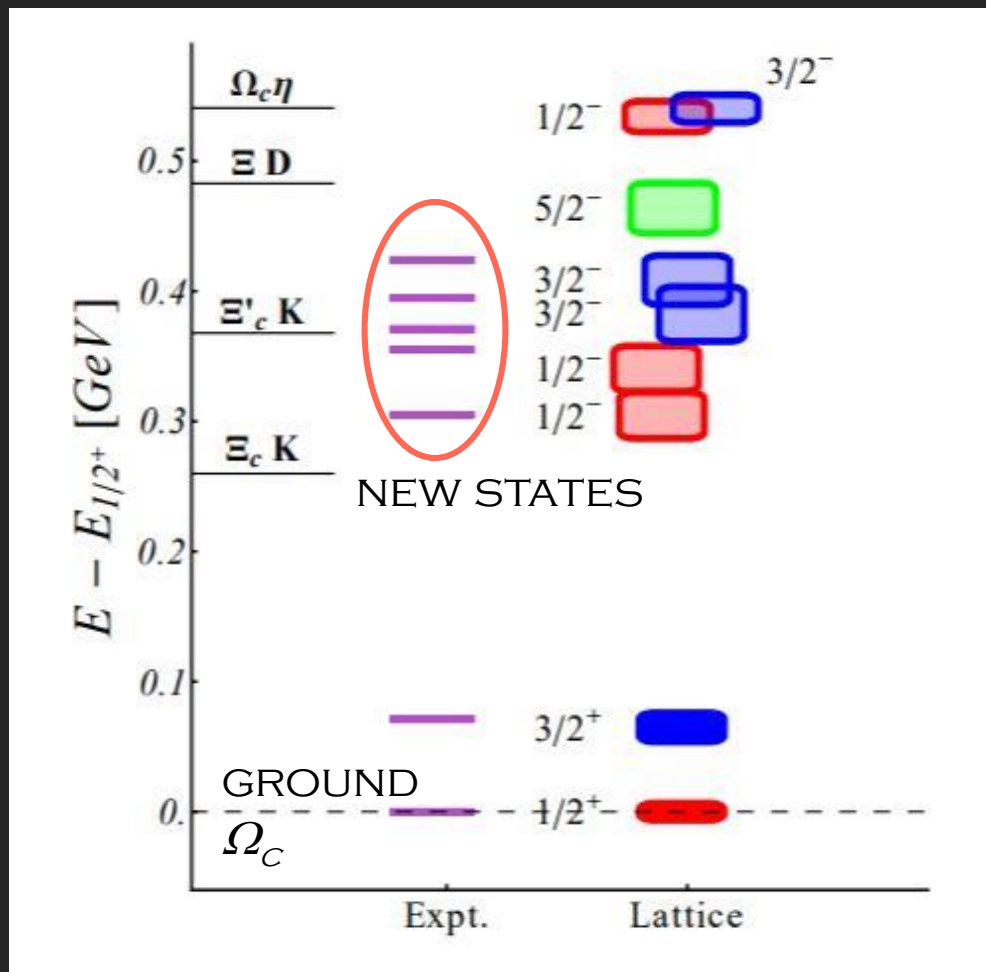


J. YELTON ET AL.. (BELLE COLL.), PRD 97, 051102 (2018)

COMPARISON TO LQCD

EXCITED Ω_C

QUANTUM NUMBERS NOT MEASURED



M. PADMANATH, N. MATHUR, PRL 119, 042001 (2017)

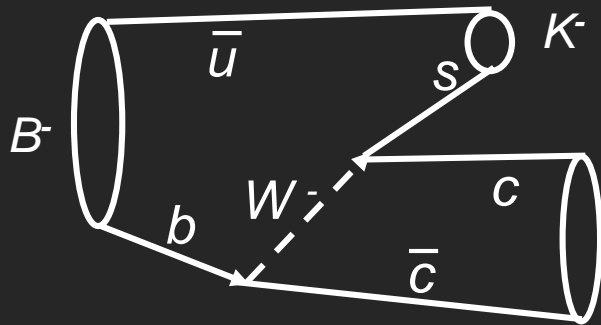
UNCONVENTIONAL HADRONS

QCD: NO APRIORI LIMITATIONS ON HADRONS BEING COMPOSED ONLY AS $|q_1 \bar{q}_2\rangle$ OR $|q_1 q_2 q_3\rangle$

HADRONS WITH OTHER COMPOSITION: EXOTIC EXPLANATION ABOUT EXOTICS P. 62
FIRST EXAMPLE: $X(3872)$

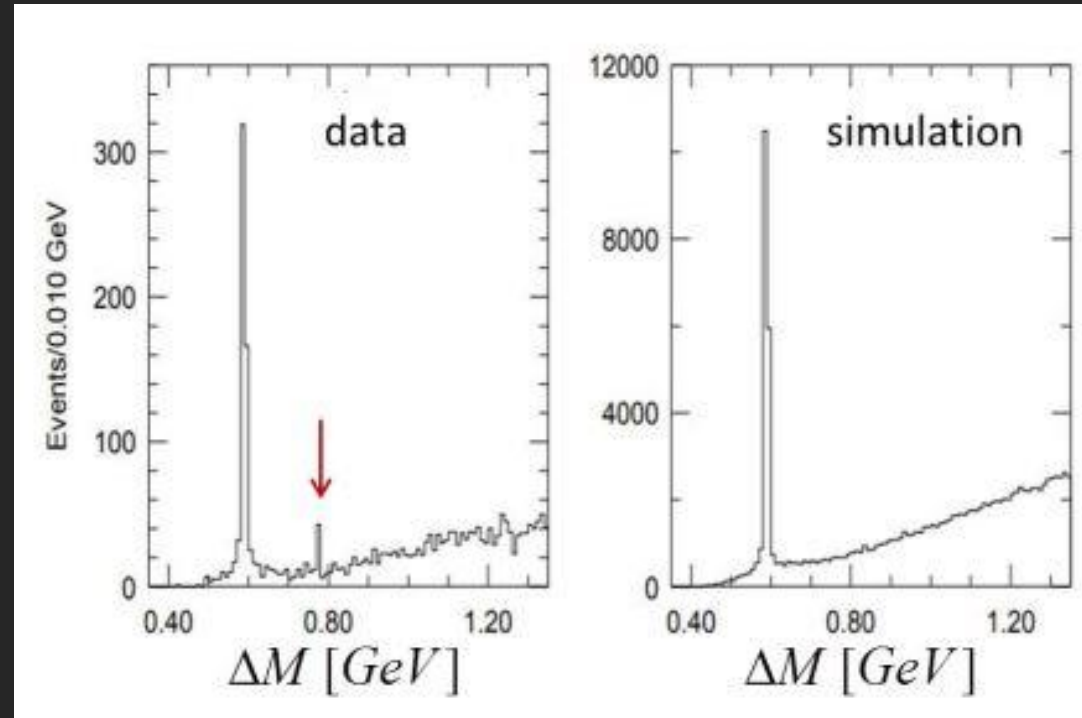
$$B^+ \rightarrow K^+ J/\psi (\ell^+ \ell^-) \pi^+ \pi^-$$

$$\Delta M = M(\pi^+ \pi^- \ell^+ \ell^-) - M(\ell^+ \ell^-)$$



$$B^+ \rightarrow K^+ X(\rightarrow J/\psi (\ell^+ \ell^-) \pi^+ \pi^-)$$

MOST PROBABLY MIXTURE OF
 $c\bar{c}$ & $c\bar{q}c\bar{q}$ WHY? P. 63
 $X(3872)$ ON LATTICE P. 64



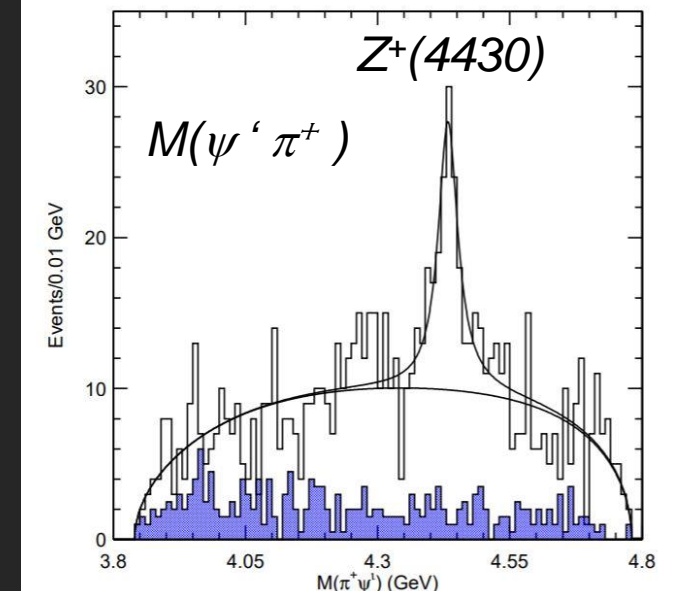
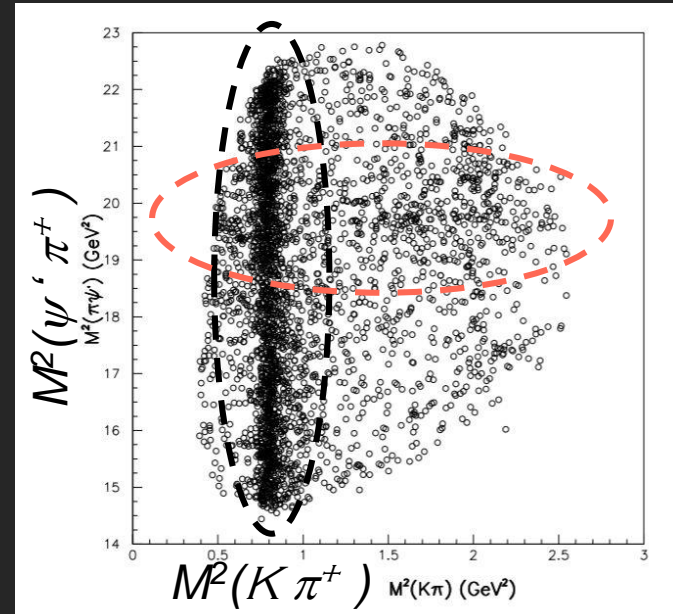
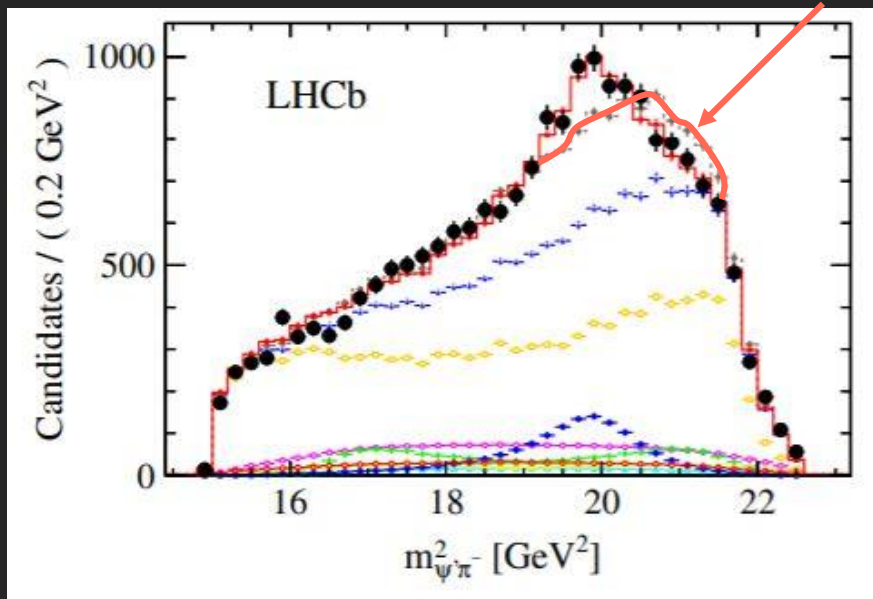
S.-K. CHOI ET AL. (BELLE COLL.), PRL 91, 262001 (2003)
(MOST CITED BELLE PAPER!)

UNCONVENTIONAL HADRONS

IF $c\bar{q}c\bar{q}$, WHY NOT $c\bar{u}c\bar{d}$?

$B \rightarrow K \psi(2S) \pi^+$ MORE EXOTIC STATES, INCLUDING PQ'S P.66

R. AAJ ET AL. (LHCb COLL.), PRL 112, 222002 (2014) FIT W/O $Z^+(4430)$



FOR NEW STATES: ANGULAR ANALYSIS TO DETERMINE SPIN & PARITY!

E.G.: $X(3915)$ IN $B \rightarrow K @ J/\psi$

IS IT $\chi_c(2P)$ (2^{++}) OR SOMETHING ELSE

UNCONVENTIONAL HADRONS

S.-K. CHOI ET AL. (BELLE COLL.), PRL 100,142001 (2008)

$$B \rightarrow K \psi(2S) \pi^\pm$$

$$Br(B^0 \rightarrow K^\mp Z^\pm) Br(Z^\pm \rightarrow \pi^\pm \psi') = (4.1 \pm 1.0 \pm 1.4) \cdot 10^{-5}$$

$$\Gamma = (45^{+18+30}_{-13-13}) \text{ MeV}$$

*SYST. UNCERTAINTY DOMINATED BY BKG.;
MAJORITY OF BKG. COMBINATORIAL FROM B*

121 ± 30 $Z^+(4430)$ SIGNAL EVTS FROM 605 FB^{-1}

200 ± 40 $Z^+(4430)$ SIGNAL EVTS / AB^{-1}

AT CERTAIN POINT NEED TO REDUCE BKG. (FOR LOWER SYST. UNCERTAINTY) \rightarrow
LOWERING ε (LARGER STAT. UNCERTAINTY) FEI!

SOME TRIVIAL STATISTICS P. 65

ASSUMING P WITH FEI IMPROVED BY 6X & $\varepsilon_{\text{FEI}} \sim 1\%$:

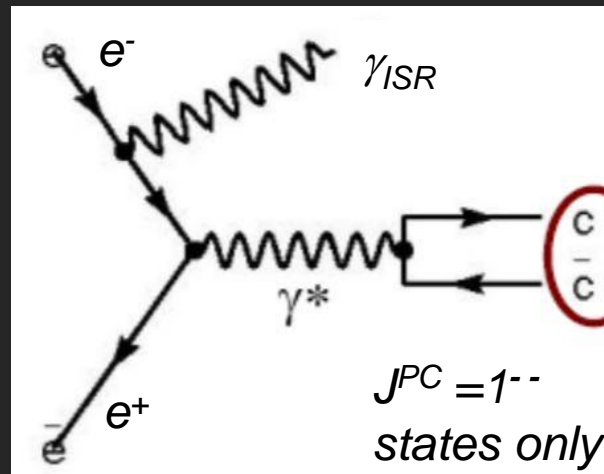
NEED $L \sim 15 \text{ AB}^{-1}$ TO REACH SAME STAT. UNCERTAINTY AS AT 605 FB^{-1}

(AND PRESUMABLY MUCH LOWER SYST. UNCERTAINTY)

ISR PRODUCTION

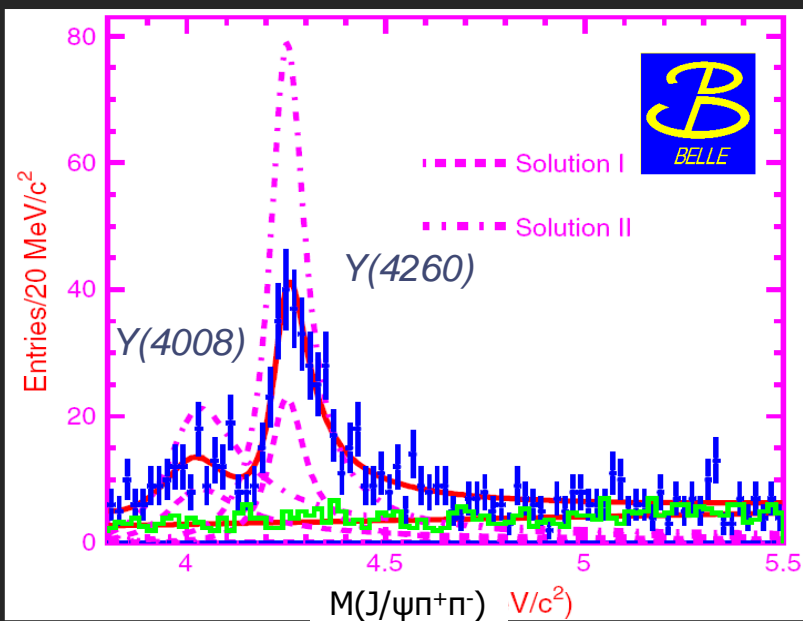
$$e^+e^- \rightarrow J/\psi \pi^+ \pi^- \gamma_{ISR} \text{ AND } \psi(2S) \pi^+ \pi^- \gamma_{ISR}$$

γ_{ISR} MAY BE RECONSTRUCTED
(TAGGED ANALYSIS)
OR NOT (UNTAGGED, PROCESS
IDENTIFIED THROUGH MISSING MASS)

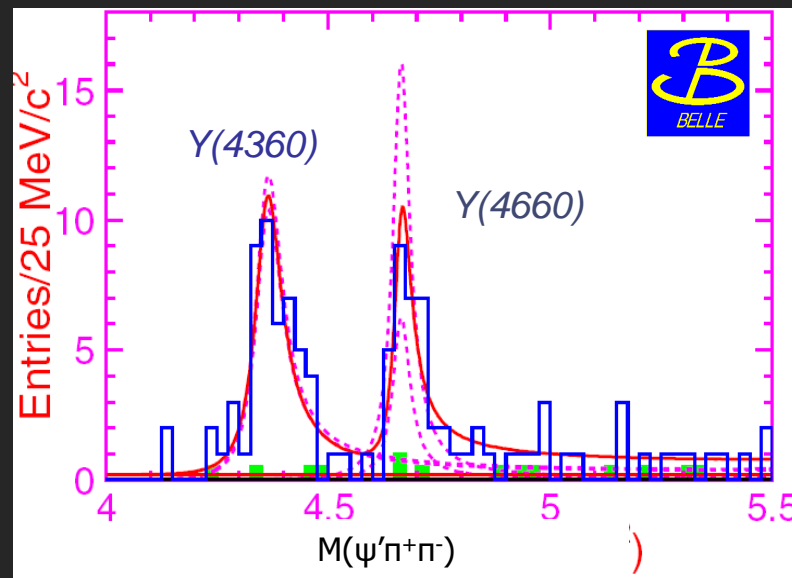


ISR PRODUCTION P. 67

C.Z. YUAN ET AL. (BELLE COLL.), PRL 99, 182004 (2007)



X.L. WANG ET AL. (BELLE COLL.), PRL 99, 142002 (2007)



EXOTIC ZOO

RECONSTRUCTED IN $B \rightarrow X K$ $e^+e^- \rightarrow \gamma_{ISR} X$

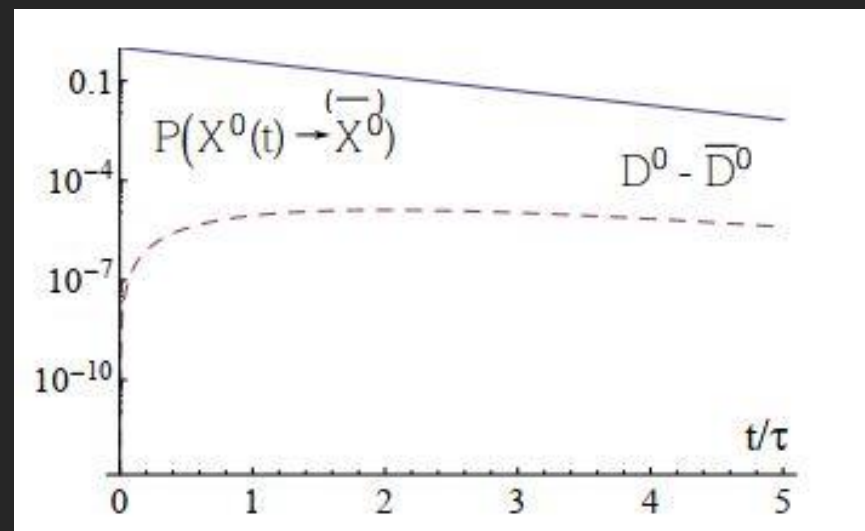
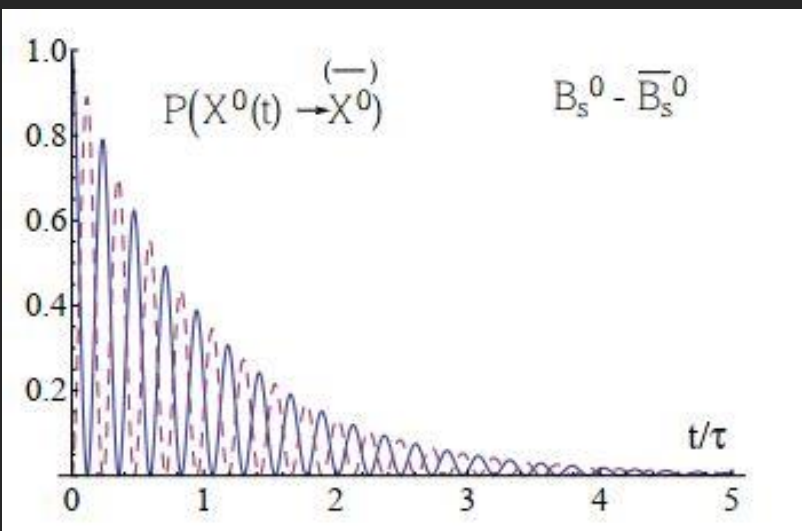
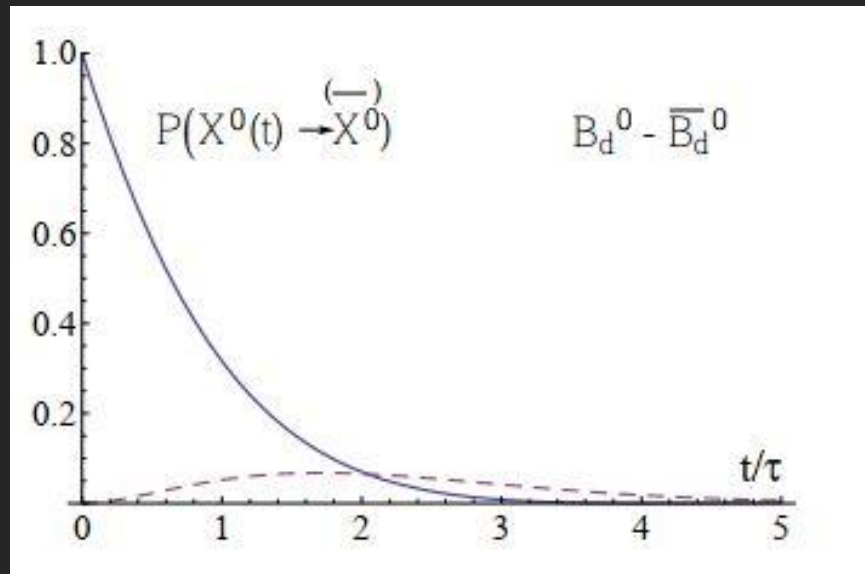
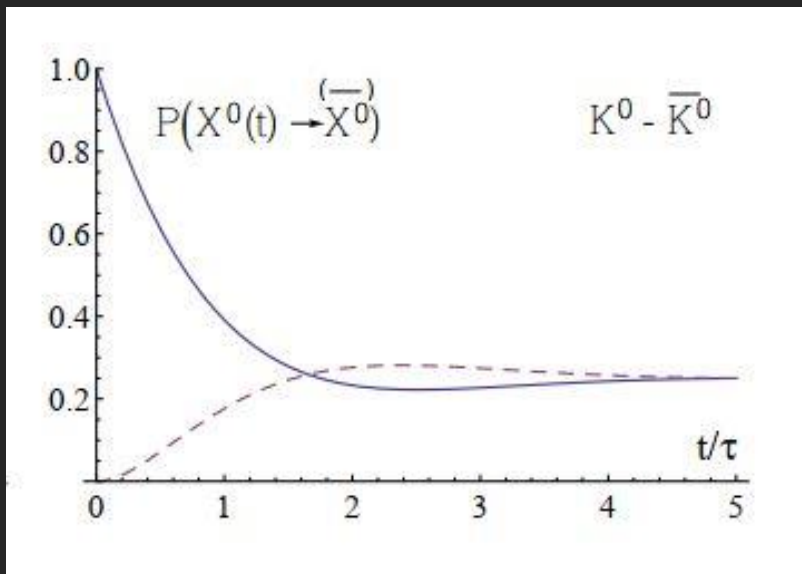
PBF

State	J^{PC}
X(3872)	1^{++}
Y(3940)	J^{P+}
Z(3930)	2^{++}
Y(4140)	J^{P+}
X(4160)	0^{P+}
Y(4260)	1^{--}
X(4350)	J^{P+}
Y(4350)	1^{--}
Y(4660)	1^{--}

State	J^{PC}
Y(4260)	1^{--}
Y(4350)	1^{--}
Y(4660)	1^{--}

SPECTROSCOPY OF CHARMED HADRONS REPRESENTS A TESTBED FOR (L)QCD;
SEVERAL UNCONVENTIONAL STATES REPRESENT A CHALLENGE FOR THEORETICAL
DESCRIPTION

OSCILLATIONS $M^0 \leftrightarrow \bar{M}^0$



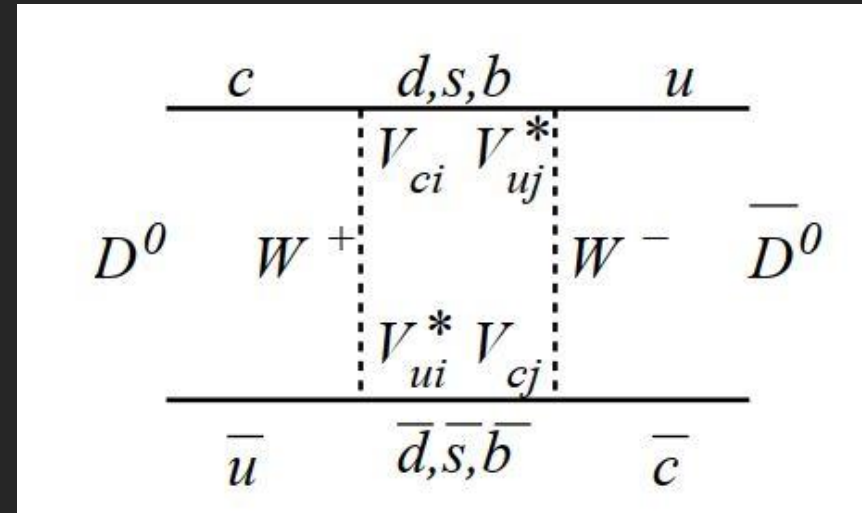
PBF

OSCILLATIONS $M^0 \leftrightarrow \bar{M}^0$

Meson	Discovery year and place	Mixing parameter
K^0	1950 Caltech	
Mixing	1956 Columbia	$x \approx 1, y \approx 1$
B_d^0	1983 CERN	
Mixing	1987 DESY	$x \approx 0.8, y \sim 0$
B_s^0	1992 LEP	
Mixing	2006 Fermilab	$x \approx 26, y \sim 0.05$
D^0	1976 SLAC	
Mixing	2007 KEK, SLAC	$x \sim 0.01, y \sim 0.01$

PBF

WHY SO SMALL?



$$\langle \bar{D}^0 | H^{\Delta C=2} | D^0 \rangle =$$

$$= \sum_{i,j=d,s,b} V_{ui}^* V_{ci} V_{cj} V_{uj}^* \mathcal{F}(m_W^2, m_i^2, m_j^2)$$

$$\mathcal{F}(m_W^2, m_i^2, m_j^2) \propto f_0 m_W^2 + f_1 m_i^2 + f_2 m_j^2 + f_3 m_i m_j + \mathcal{O}(m_W^{-2})$$

$$\langle \bar{D}^0 | H^{\Delta C=2} | D^0 \rangle = \frac{G_F^2 m_c^2}{4\pi^2} V_{cs}^* V_{cd}^* V_{ud} V_{us} \frac{(m_s^2 - m_d^2)^2}{m_c^4} \times \langle \bar{D}^0 | \bar{u} \gamma_\mu (1 - \gamma^5) c \bar{u} \gamma^\mu (1 - \gamma^5) c | D^0 \rangle .$$

DOUBLY CABIBBO SUPP.
VANISHES IN EXACT
 $SU(3)_{\text{FLAVOR}}$

D^0 MIXING PARAMETERS ARE DRIVEN BY DIFFICULT TO CALCULATE LONG-DISTANCE EFFECTS. NO LQCD CALCULATIONS EXIST (YET).

PHENOMENOLOGY

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$$

TIME EVOLUTION

FLAVOR STATES \neq H_{EFF} EIGENSTATES:
(DEFINED FLAVOR) (DEFINED $m_{1,2}$ AND $\Gamma_{1,2}$)

$$x \equiv \frac{m_1 - m_2}{\bar{\Gamma}}; y \equiv \frac{\Gamma_1 - \Gamma_2}{2\bar{\Gamma}};$$

$$|D^0(t)\rangle = \left[|D^0\rangle \cosh\left(\frac{ix + y}{2} \bar{\Gamma} t\right) - \frac{q}{p} |\bar{D}^0\rangle \sinh\left(\frac{ix + y}{2} \bar{\Gamma} t\right) \right] e^{-i\bar{m}t - \frac{\bar{\Gamma}}{2}t}$$

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

SM: $|x|, |y| \leq \mathcal{O}(10^{-2})$ $|x|, |y| \ll 1 \Rightarrow$

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \langle f | D^0 \rangle \left| 1 - \frac{q}{p} \frac{\langle f | \bar{D}^0 \rangle}{\langle f | D^0 \rangle} \frac{ix + y}{2} \bar{\Gamma} t \right|^2$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \langle f | \bar{D}^0 \rangle \left| 1 - \frac{p}{q} \frac{\langle f | D^0 \rangle}{\langle f | \bar{D}^0 \rangle} \frac{ix + y}{2} \bar{\Gamma} t \right|^2$$

„MASTER“ FORMULAE
FOR t -DEPENDENT RATES
(UP TO $\mathcal{O}(x,y)$)

MORE DETAILS P. 68

PHENOMENOLOGY

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$$

TIME EVOLUTION

FLAVOR STATES (DEFINED FLAVOR) \neq H_{EFF} EIGENSTATES: (DEFINED $m_{1,2}$ AND $\Gamma_{1,2}$)

$$x \equiv \frac{m_1 - m_2}{\bar{\Gamma}}; y \equiv \frac{\Gamma_1 - \Gamma_2}{2\bar{\Gamma}};$$

$$|D^0(t)\rangle = \left[|D^0\rangle \cosh\left(\frac{ix + y}{2} \bar{\Gamma} t\right) - \frac{q}{p} |\bar{D}^0\rangle \sinh\left(\frac{ix + y}{2} \bar{\Gamma} t\right) \right] e^{-i\bar{m}t - \frac{\bar{\Gamma}}{2}t}$$

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

SM: $|x|, |y| \leq \mathcal{O}(10^{-2})$ $|x|, |y| \ll 1 \Rightarrow$

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \langle f | D^0 \rangle \left| 1 - \frac{q}{p} \frac{\langle f | \bar{D}^0 \rangle}{\langle f | D^0 \rangle} \frac{ix + y}{2} \bar{\Gamma} t \right|^2$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \langle f | \bar{D}^0 \rangle \left| 1 - \frac{p}{q} \frac{\langle f | D^0 \rangle}{\langle f | \bar{D}^0 \rangle} \frac{ix + y}{2} \bar{\Gamma} t \right|^2$$

„MASTER“ FORMULAE FOR t -DEPENDENT RATES (UP TO $\mathcal{O}(x,y)$)

MORE DETAILS P. 68

DECAY TIME DISTRIBUTION OF EXPERIMENTALLY ACCESSIBLE STATES D^0, \bar{D}^0
SENSITIVE TO MIXING PARAMETERS x AND y , DEPENDING ON FINAL STATE

GENERAL FEATURES OF MEAS'S

TAGGING

(BELLE, LHCb)

$$D^{*+} \rightarrow D^0 \pi_s^+$$

CHARGE OF $\pi_s \Rightarrow$ FLAVOR OF D^0 ;

$$\Delta M = M(D^0 \pi_s) - M(D^0)$$

(or $q = \Delta M - m_\pi$) \Rightarrow

BACKGROUND REDUCTION

$$\varepsilon_{D^*} \sim 80\%, \omega_{D^*} \sim 0.2\%$$

REST OF EVENT (BELLE)

$$\varepsilon_{D^*} \sim 27\%, \omega_{D^*} \sim 13\%$$

3X MORE PRODUCED D^0 'S

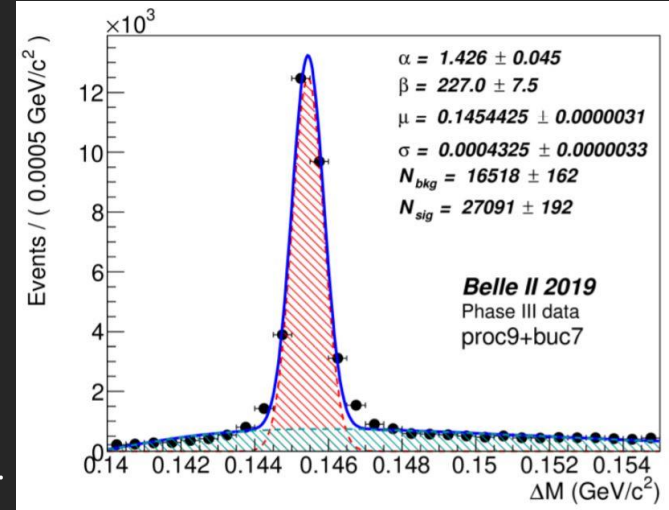
$\sigma(A_{CP})$ REDUCED BY $\sim 15\%$

USING ALSO ROE

B SEMIL. DECAYS (LHCb)

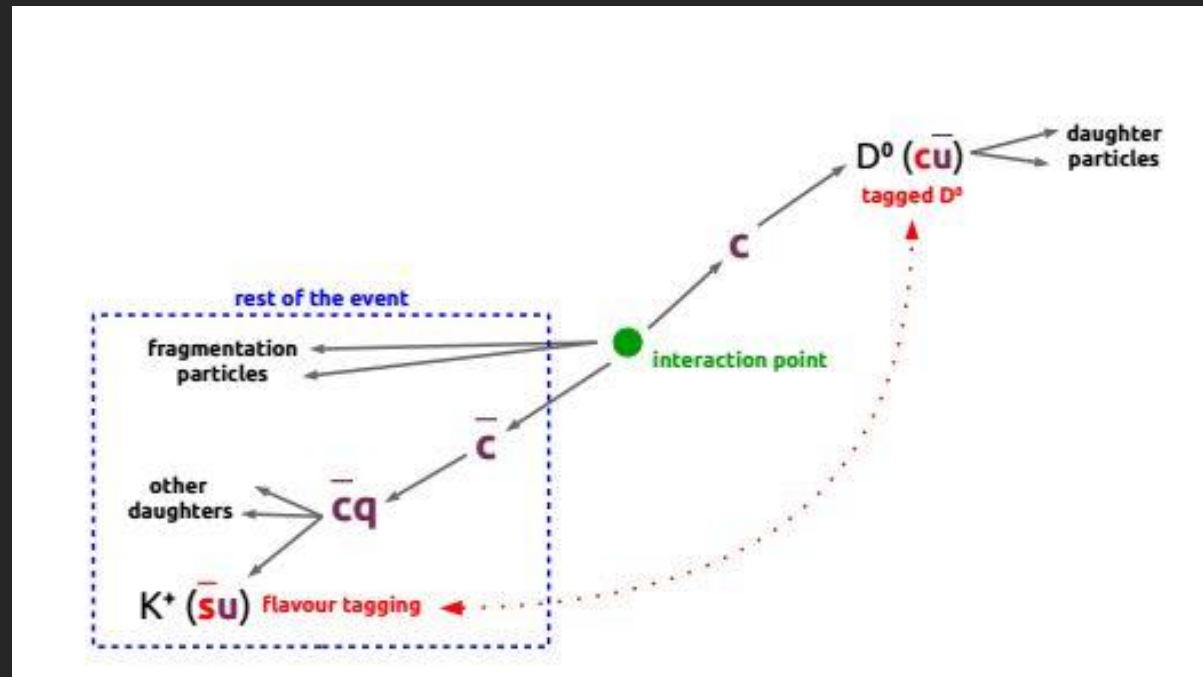
$$b \rightarrow c \mu \bar{\nu}$$

KINEMATIC
RECONSTR.
P. 71

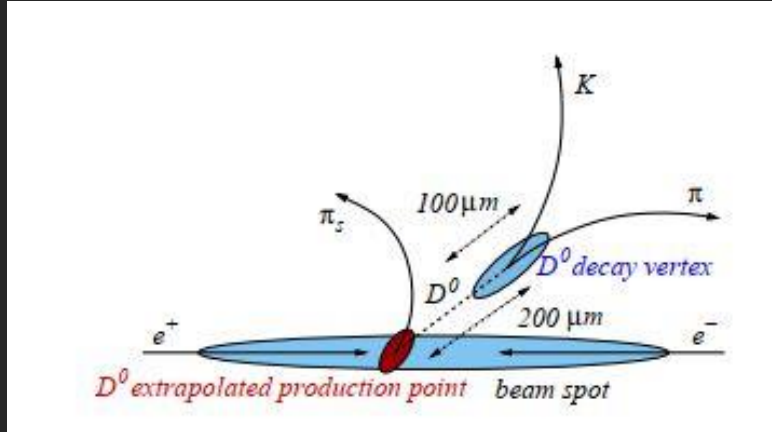


S. SANDILYA ET AL. (BELLE II COLL.), B2GM OCT 2019

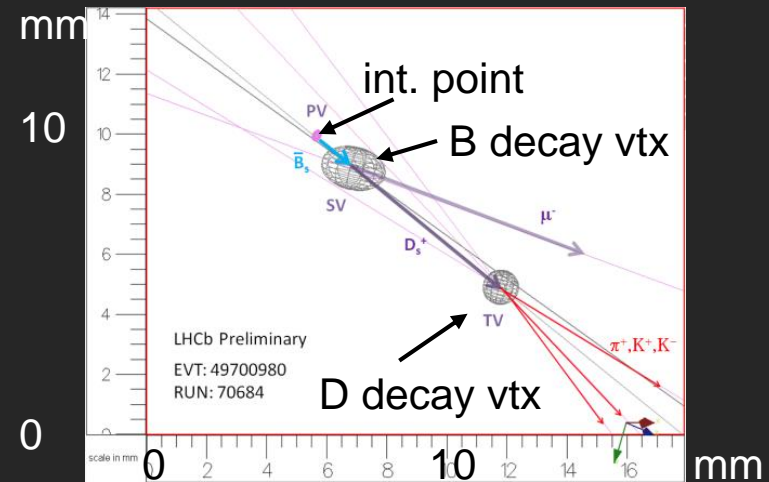
BIIPB



GENERAL FEATURES OF MEAS'S



DECAY TIME
RESOL. P. 72



DECAY TIME (BELLE): D^0 DECAY PRODUCTS VERTEX; D^0 MOMENTUM

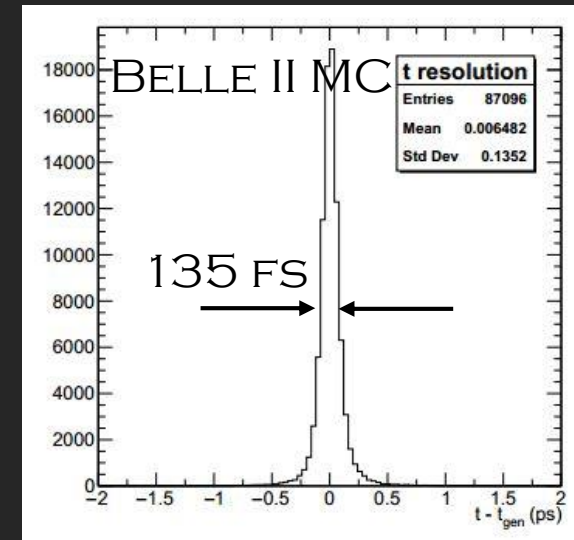
& INT. REGION;

BELLE $\sigma(t_{D^0}) \sim 270$ FS

BELLE II: $\sigma(t_{D^0}) \sim 100$ FS

(LHCb): PRIMARY VTX, B DECAY VTX, D DECAY VTX;

$\sim 2X$ BETTER $\sigma(t_{D^0})$



BIIPB

GENERAL FEATURES OF MEAS'S

BELLE

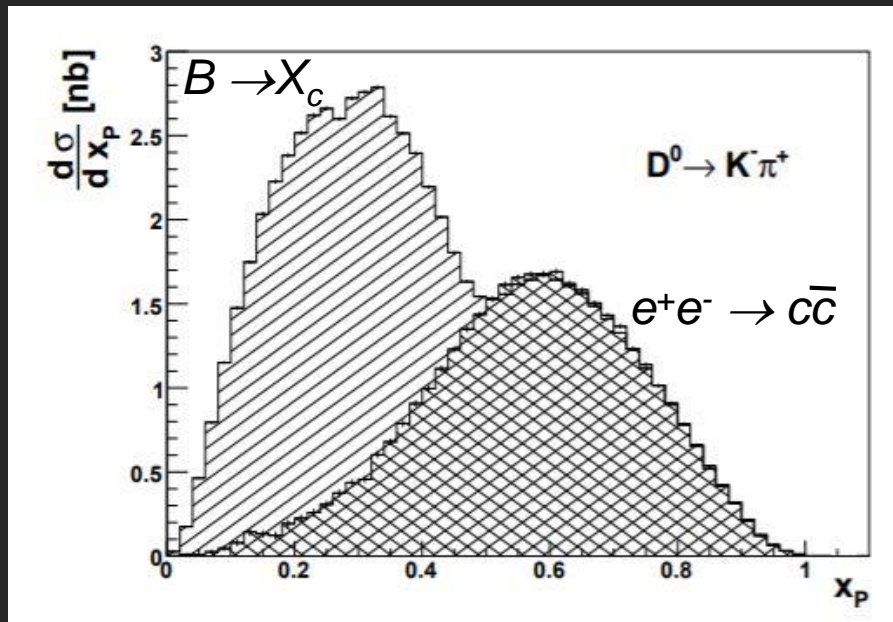
$p^*(D^*) > 2.5 \text{ GeV}/c$

ELIMINATES D^0 FROM $b \rightarrow c$

LHCb

CAN SEPARATE PROMPT AND
CASCADE PRODUCTION USING
VTXING

R. SEUSTER ET AL.. (BELLE COLL.), PHYS.REV. D73, 032002 (2006)



$$x_p = \frac{p^*}{\sqrt{s/4 - m_h^2}}$$

$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

CPV WILL BE ADDRESSED LATER;
IN CHARM SYSTEM (AND SM) CPV IS SMALL
 \Rightarrow DISCUSS MIXING W/O CPV (I.E. $q=p=1/\sqrt{2}$)

IF NO CPV:

$$CP |D_1\rangle = |D_1\rangle$$

$|D_1\rangle$ IS CP EVEN STATE

(PHASE CONVENTION AS IN PDG P. 69);

ONLY $|D_1\rangle$ COMPONENT OF D^0/\bar{D}^0 DECAYS TO
 $K^+K^- / \pi^+\pi^-$;

MEASURING LIFETIME IN THESE DECAYS $\Rightarrow \tau = 1/\Gamma_1$;

MEASURING LIFETIME IN FLAVOR SPECIFIC FINAL STATE $\Rightarrow \tau = 1/\bar{\Gamma}$;

$$\frac{dN(D^0(\bar{D}^0) \rightarrow f_{CP}^+)}{dt} \propto e^{-\bar{\Gamma}t} [1 - y\bar{\Gamma}t] \approx e^{-\bar{\Gamma}t} e^{-y\bar{\Gamma}t} = e^{-(1+y)\bar{\Gamma}t}$$

$$|D^0\rangle = \frac{1}{\sqrt{2}} [|D_1\rangle + |D_2\rangle]$$

$$|\bar{D}^0\rangle = \frac{1}{\sqrt{2}} [|D_1\rangle - |D_2\rangle]$$

$$CP |K^+K^-, \pi^+\pi^- \rangle = + |K^+K^-, \pi^+\pi^- \rangle$$

$$\langle f_{CP^+} | D^0 \rangle = \langle f_{CP^+} | D_1 \rangle = \langle f_{CP^+} | \bar{D}^0 \rangle$$

$$\langle f_{CP^-} | D^0 \rangle = \langle f_{CP^-} | D_2 \rangle = - \langle f_{CP^-} | \bar{D}^0 \rangle$$

$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

BY MEASURING EFFECTIVE LIFETIMES IN

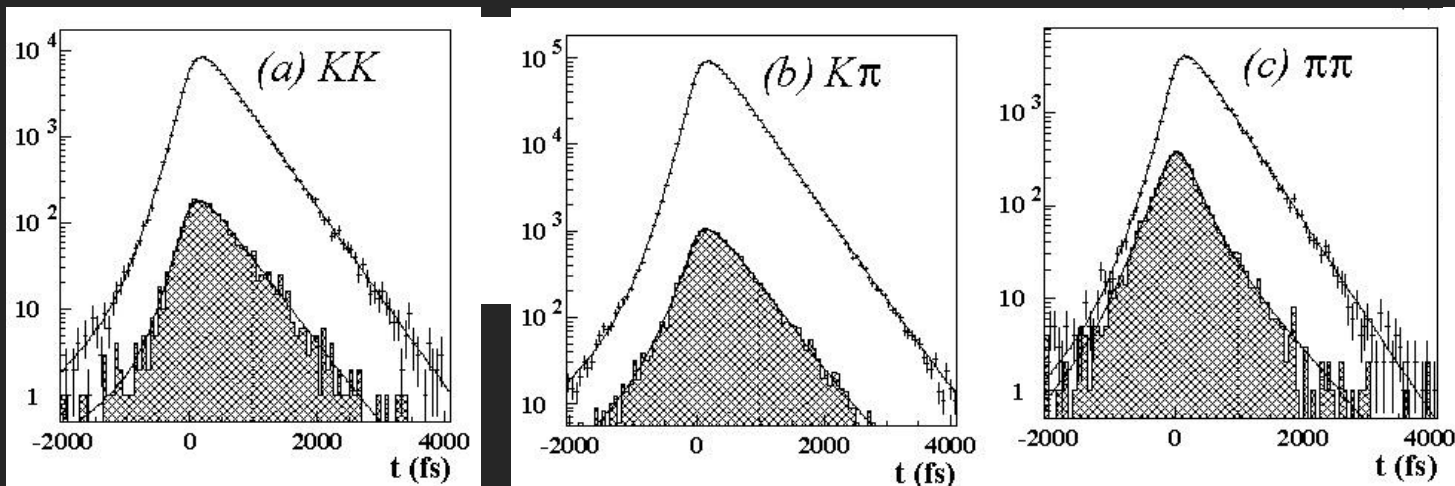
$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

$$\text{AND IN } D^0 \rightarrow K^-\pi^+$$

ONE CAN DETERMINE y

$$y_{CP} = \frac{\tau(K^-\pi^+)}{\tau(K^+K^-)} - 1$$

M. STARIC ET AL., (BELLE COLL.), PRL 98, 211803 (2007)



$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

BY MEASURING EFFECTIVE LIFETIMES IN

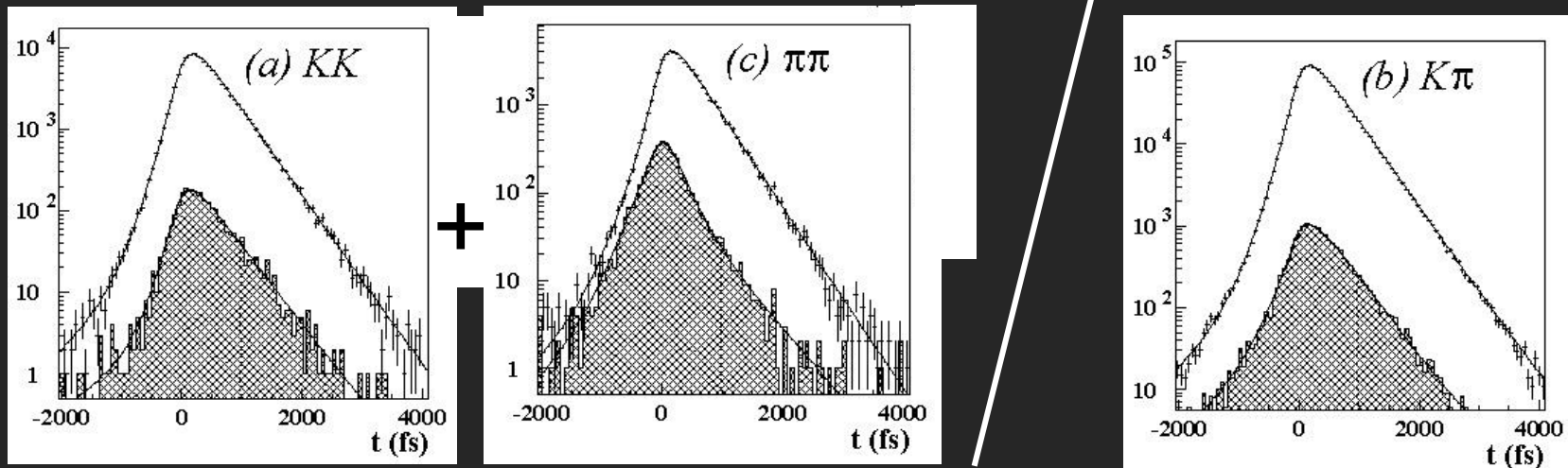
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M. STARIC ET AL., (BELLE COLL.), PRL 98, 211803 (2007)



$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

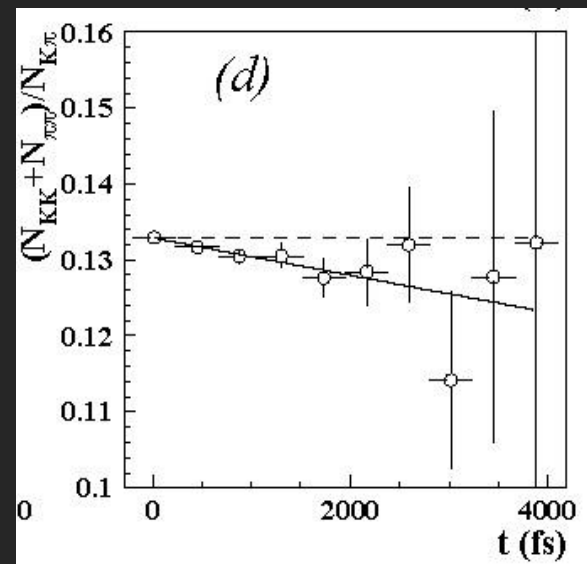
BY MEASURING EFFECTIVE LIFETIMES IN

$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

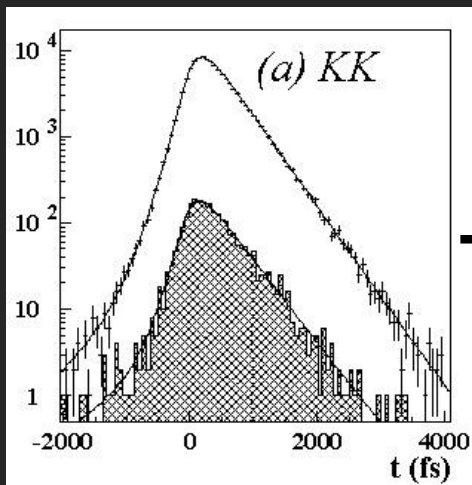
$$\text{AND IN } D^0 \rightarrow K^-\pi^+$$

ONE CAN DETERMINE y

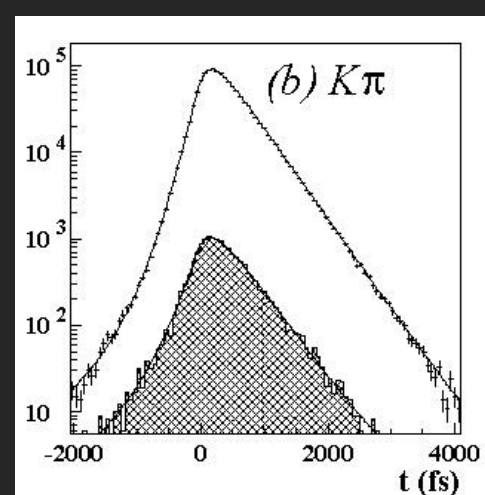
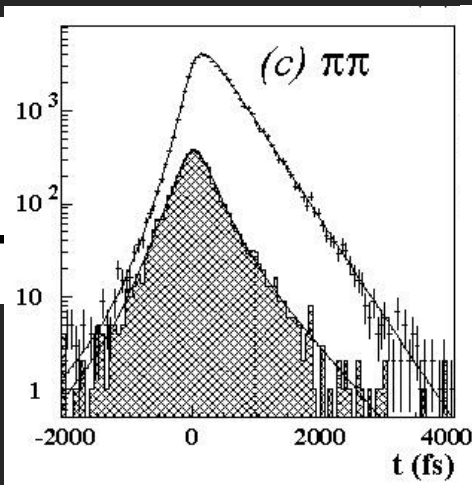
$$y_{CP} = \frac{\tau(K^-\pi^+)}{\tau(K^-K^+)} - 1$$



M. STARIC ET AL., (BELLE COLL.), PRL 98, 211803 (2007)



+



$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

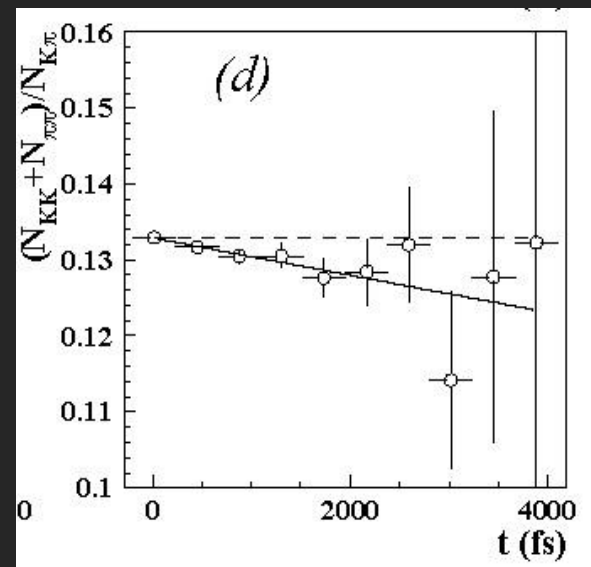
BY MEASURING EFFECTIVE LIFETIMES IN

$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

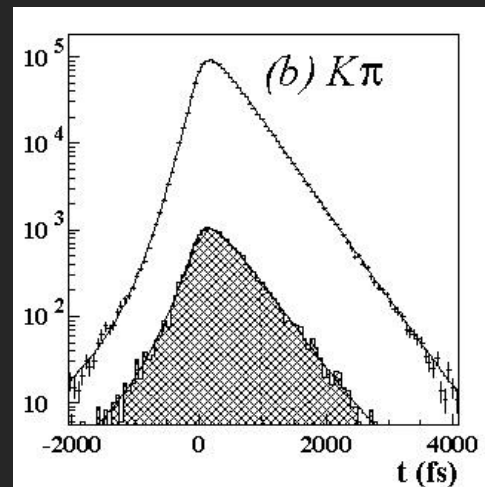
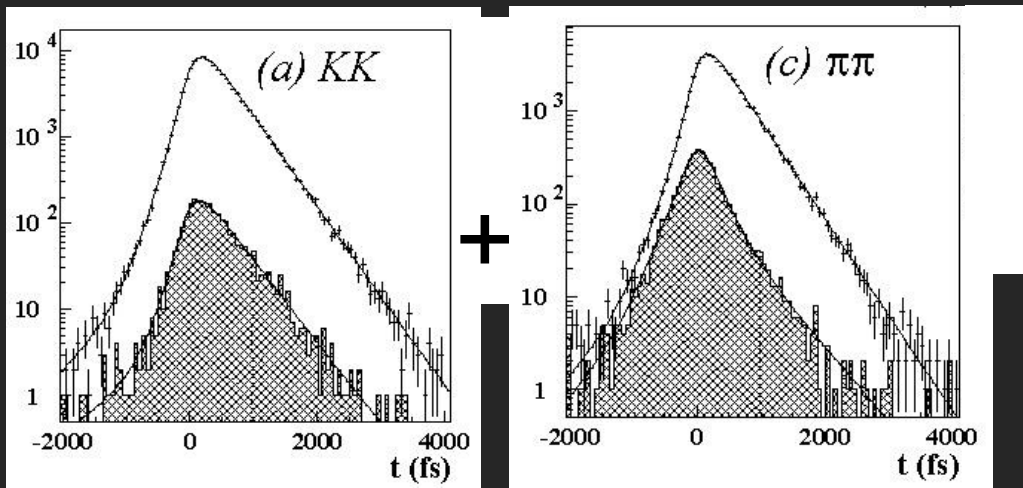
$$\text{AND IN } D^0 \rightarrow K^-\pi^+$$

ONE CAN DETERMINE y

$$y_{CP} = \frac{\tau(K^-\pi^+)}{\tau(K^+K^-)} - 1$$



M. STARIC ET AL., (BELLE COLL.), PRL 98, 211803 (2007)



$\chi^2/\text{ndf} = 1.084$
($\text{ndf} = 289$)

FIRST EVIDENCE OF D^0 MIXING

(BACK-TO-BACK WITH BABAR'S $D^0 \rightarrow K^+\pi^-$)

$$y_{CP} = (1.31 \pm 0.32 \pm 0.25)\%$$

$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

BY MEASURING EFFECTIVE LIFETIMES IN

$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

$$\text{AND IN } D^0 \rightarrow K^-\pi^+$$

ONE CAN DETERMINE y

CELEBRATING D^0 MIXING DISCOVERY
AT MORIOND EW 2007



Moriond's new cocktail: the DDbar mix



CP-ODD STATES
LOWER STAT. PRECISION

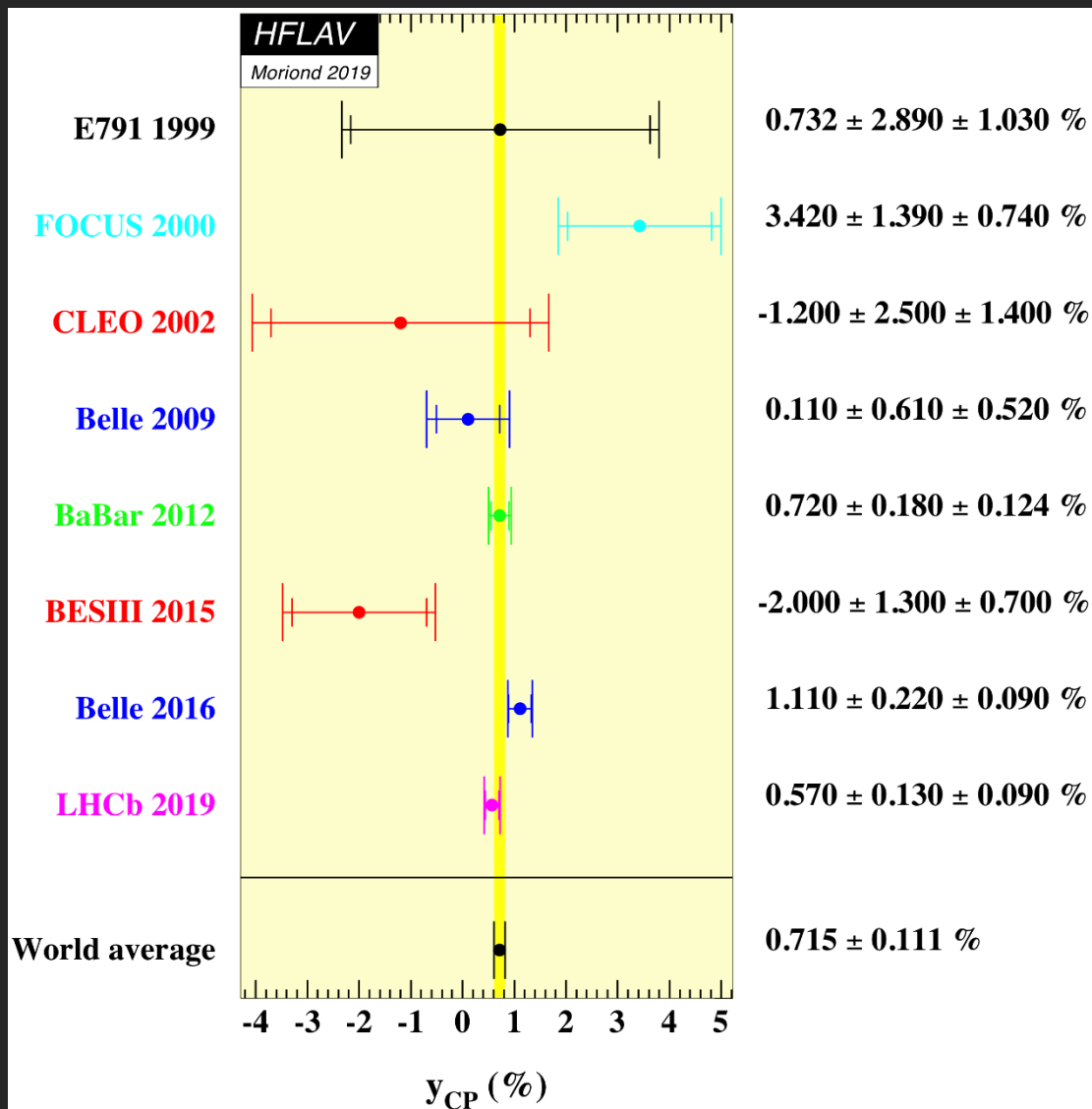
AVERAGING

$$y_{CP} = (0.715 \pm 0.111)\%$$

D^0 MESONS, LIKE OTHER M^0 ,
DO MIX, WITH THE LOWEST
PROBABILITY OF ALL*

* ACTUALLY, t -INTEGRATED
MIXING PROBABILITY P. 69

$$p(D^0 \rightarrow \bar{D}^0) = \frac{x^2 + y^2}{2(1 + x^2)}$$



HFLAV



DCS DECAYS

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f} = \left| \frac{q}{p} \right| \frac{1}{r} e^{i(\delta_f + \varphi)} \quad f = K^+ \pi^-$$

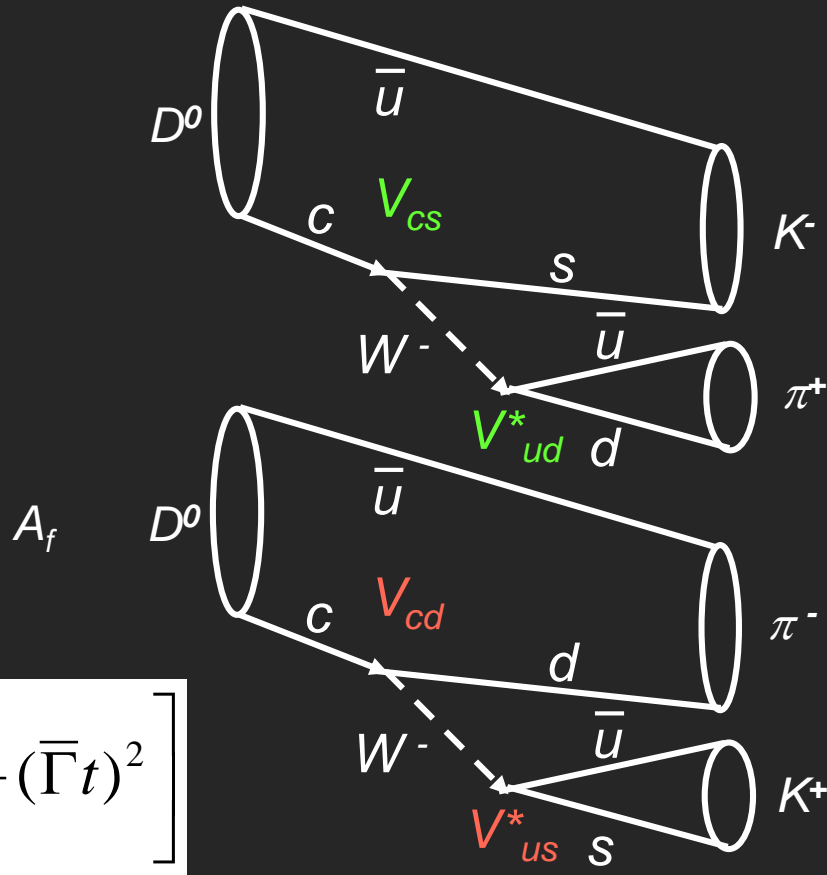
$\delta_{K\pi}$: (UNKNOWN) PHASE DIFFERENCE BETWEEN A_f AND \bar{A}_f
 $|A_f / \bar{A}_f| = r \ll 1$

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \left[r^2 - ry' \bar{\Gamma}t + \frac{x'^2 + y'^2}{4} (\bar{\Gamma}t)^2 \right]$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \left[1 - ry \cos(\delta_{K\pi}) \bar{\Gamma}t + \dots \right]$$

$$y' = y \cos(\delta_{K\pi}) - x \sin(\delta_{K\pi})$$

$$x' = x \cos(\delta_{K\pi}) + y \sin(\delta_{K\pi})$$

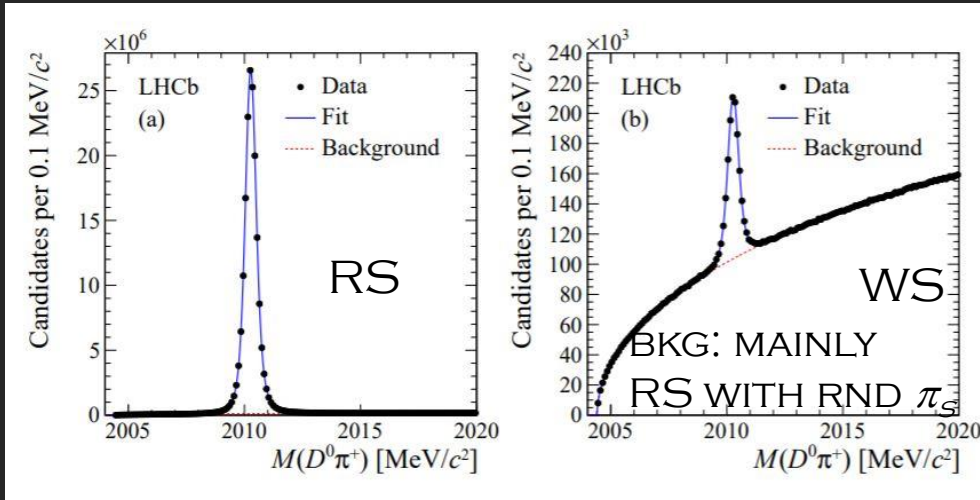


$$\mathcal{O}\left(\frac{ry}{r^2} = \frac{y}{r} \sim 1\right)$$

$$\mathcal{O}\left(\frac{ry}{1} = ry \ll 1\right)$$



$$\frac{dN(D^0 \rightarrow f)}{dt} / \frac{dN(\bar{D}^0 \rightarrow f)}{dt} = \left[1 - \frac{y'}{r} \bar{\Gamma} t + \frac{x'^2 + y'^2}{4r^2} (\bar{\Gamma} t)^2 \right]$$

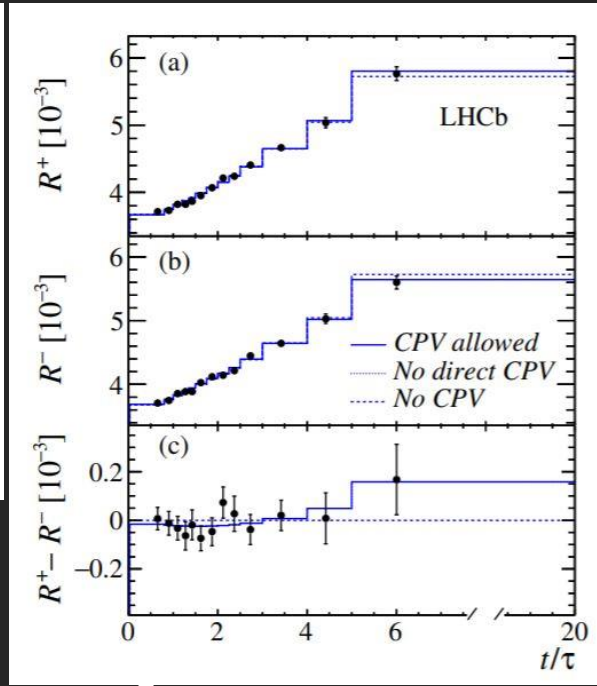


R. AAJ ET AL., (LHCb COLL.), PRD 97, 031101 (2018)

$y' = (0.528 \pm 0.052)\%$
 $x'^2 = (3.9 \pm 2.7) \cdot 10^{-5}$

STAT. +
SYST.

FIT IN BINS OF t/τ



RESULT USING PRIMARY D^{*} 'S (REQUIRING D^{*} VTX CONSISTENT WITH PRIMARY)
MAIN SYTS. UNCERTAINTY ($\sim 1/2$ OF STAT.) FROM REMAINING SECONDARY D^{*} 'S
@ B-FACTORIES: NOT RATIO BUT INDIVIDUAL t -DEPENDENT RATES FITTED

$$D^0 \rightarrow K^+ \pi^-$$

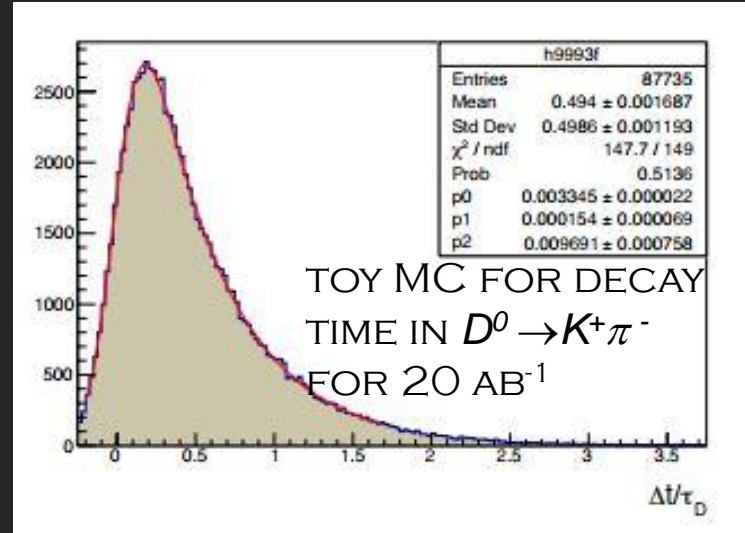
D. ASNER ET AL., (CLEO-C COLL.), PRD 86, 112001 (2012)

$\delta_{K\pi}$ CAN BE DETERMINED USING QUANTUM CORRELATED $D^0\bar{D}^0$ PAIRS AT BES III;

HOWEVER, CURRENTLY ONLY CLEO-C MEAS. EXISTS, AND $\delta_{K\pi}$ IS MORE PRECISELY DETERMINED BY COMBINATION OF y' , y AND x MEAS'S.

BELLE II EXPECTATIONS:

$$\cos \delta_{K\pi} = 0.81^{+0.22}_{-0.18} \quad ^{+0.07}_{-0.05}$$



BIIPB

	5 ab^{-1}	20 ab^{-1}	50 ab^{-1}	Current best
$\sigma(x'^2) [10^{-5}]$	10	5	3	2.7
$\sigma(y') [\%]$	0.15	0.07	0.05	0.05

BIIPB

HFLAV

INCLUDING 20% AND 12% ADDITIONAL UNCERTAINTY DUE TO BKG. & SYSTEMATICS, RESPECTIVELY (?)

MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

DIFFERENT TYPES OF INTERM.
STATES;

$$\text{CF: } D^0 \rightarrow K^{*0} \pi^0$$

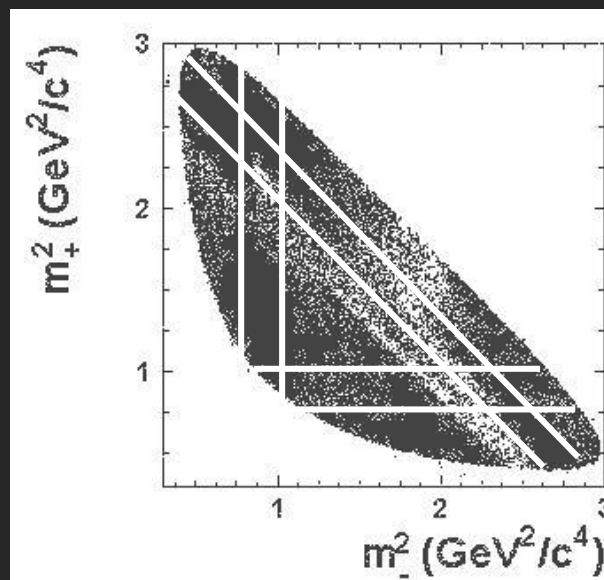
$$\text{DCS: } D^0 \rightarrow K^{*+} \pi^-$$

$$\text{CP: } D^0 \rightarrow \rho^0 K_S$$

IF $f = \bar{f} \Rightarrow$ POPULATE SAME DALITZ
PLOT;

RELATIVE PHASES DETERMINED
(UNLIKE $D^0 \rightarrow K^+ \pi^-$);

$$D^0 \rightarrow K_S \pi^+ \pi^-$$



MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

DIFFERENT TYPES OF INTERM.
STATES;

CF: $D^0 \rightarrow K^{*0} \pi^0$

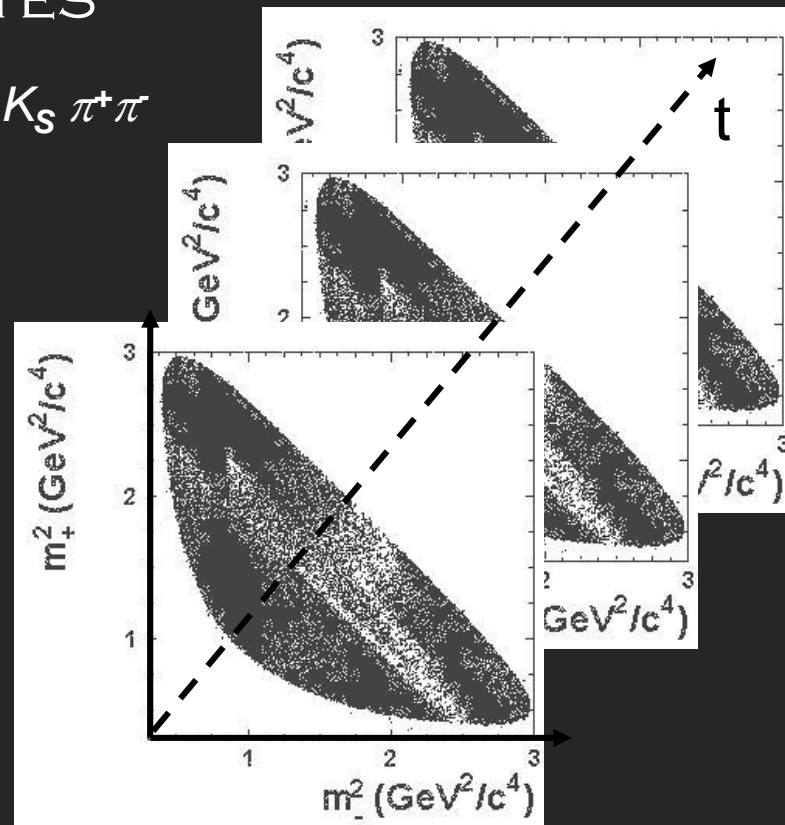
DCS: $D^0 \rightarrow K^{*+} \pi^-$

CP: $D^0 \rightarrow \rho^0 K_S$

IF $f = \bar{f} \Rightarrow$ POPULATE SAME DALITZ
PLOT;

RELATIVE PHASES DETERMINED
(UNLIKE $D^0 \rightarrow K^+ \pi^-$);

SPECIFIC REGIONS OF DALITZ PLANE \rightarrow
SPECIFIC ADMIXTURE OF INTERM. STATES \rightarrow
SPECIFIC t DEPENDENCE $f(x, y)$;



MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

t-DEPENDENT DECAY AMPL. DEPENDS ON DALITZ VARIABLES;
CONTAINS D^0 AND \bar{D}^0 PART (DUE TO MIXING) THAT PROPAGATE DIFFERENTLY IN TIME,
 $\lambda_{1,2} = f(x, y)$;

$$m_{\pm}^2 = m^2(K_S \pi^{\pm});$$

INSTANTANEOUS AMPLITUDE:

SUM OF INTERMEDIATE STATES WITH (UNKNOWN) RELATIVE STRONG PHASES

$$\begin{aligned} \mathcal{M}(m_-^2, m_+^2, t) &\equiv \langle K_S \pi^+ \pi^- | D^0(t) \rangle = \\ &= \frac{1}{2} \mathcal{A}(m_-^2, m_+^2) \left[e^{-i\lambda_1 t} + e^{-i\lambda_2 t} \right] + \\ &+ \frac{1}{2} \bar{\mathcal{A}}(m_-^2, m_+^2) \left[e^{-i\lambda_1 t} - e^{-i\lambda_2 t} \right] \end{aligned}$$

BY STUDYING THE DECAY TIME EVOLUTION OF DALITZ PLANE \rightarrow ACCESS DIRECTLY x, y

$$\begin{aligned} \mathcal{A}(m_-^2, m_+^2) &= \\ &= \sum a_r e^{i\Phi_r} B(m_-^2, m_+^2) + a_{NR} e^{i\Phi_{NR}} \end{aligned}$$

$$\begin{aligned} \bar{\mathcal{A}}(m_-^2, m_+^2) &= \\ &= \sum a_r e^{i\Phi_r} B(m_+^2, m_-^2) + a_{NR} e^{i\Phi_{NR}} \end{aligned}$$

MULTI-BODY SELF CONJUGATED STATES

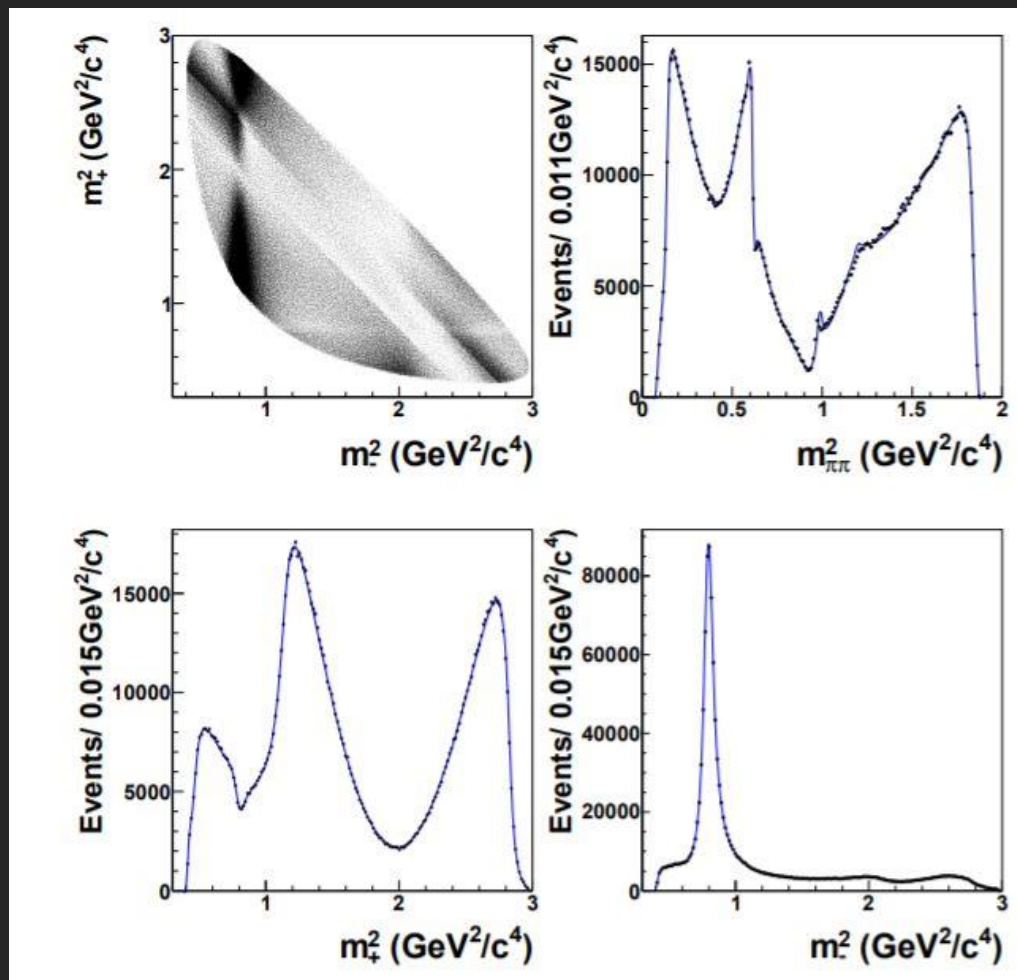


NO CPV RESULT:

$$x = (0.56 \pm 0.19 \pm_{0.09}^{0.03} \pm_{0.09}^{0.06})\%$$

$$y = (0.30 \pm 0.15 \pm_{0.05}^{0.04} \pm_{0.06}^{0.03})\%$$

↑
UNCERTAINTY DUE TO
DALITZ MODEL



T. PENG ET AL., (BELLE COLL.), PRD 89, 091103 (2014)

MULTI-BODY SELF CONJUGATED STATES

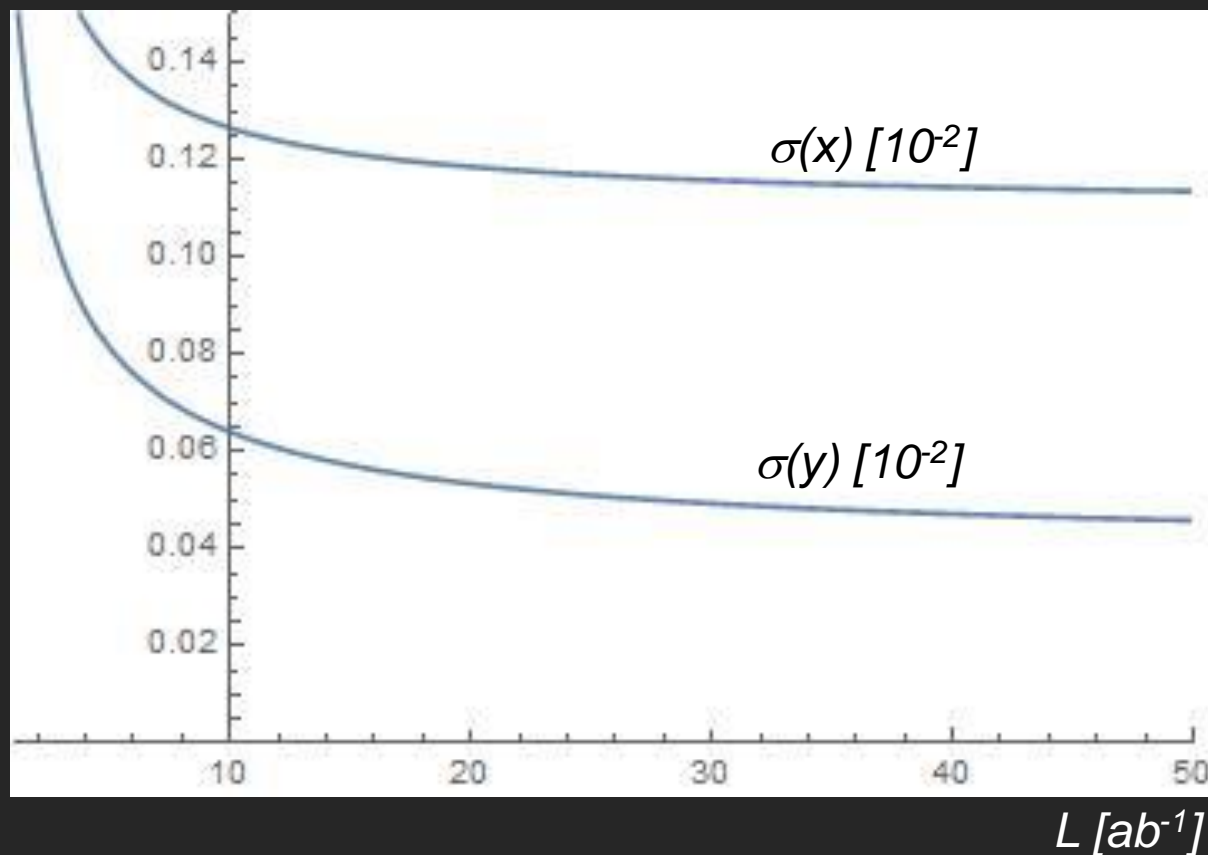
$$D^0 \rightarrow K_S \pi^+ \pi^-$$

BELLE II:
SYST. UNCERTAINTY
DOMINATES @ FEW AB^{-1}

IN TURN, SYST. UNCERTAINTY
DOMINATED BY THE MODEL
UNCERTAINTY

CAN THIS BE EVADED?

BY MEASURING STRONG
PHASE VARIATION ACROSS
DALITZ PLANE USING
COHERENT $D^0 D^0$ PAIRS (BES III)



MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

A. BONDAR, A. POLUEKTOV AND V. VOROBIEV, PRD 82, 034033 (2010)
A. GIRI, Y. GROSSMAN, A. SOFFER, AND J. ZUPAN, PR D 68, 054018 (2003)

MODEL INDEPENDENT METHOD

DALITZ- AND t DEPENDENT AMPLITUDE UP TO $O(x^2, y^2)$ NOTATION: $\frac{q}{p} = r_{CP} e^{i\alpha_{CP}}$

$$\mathcal{P}_{D^0}(m_{12}^2, m_{13}^2, t) = \Gamma e^{-\Gamma t} \left[a_{12,13}^2 + r_{CP} a_{12,13} a_{13,12} \Gamma t \left\{ y_D \cos(\delta_{12,13} - \delta_{13,12} - \alpha_{CP}) + x_D \sin(\delta_{12,13} - \delta_{13,12} - \alpha_{CP}) \right\} \right]$$

C. THOMAS,
G. WILKINSON,
JHEP 2012:185

INTEGRATING OVER DALITZ- AND t BIN

$$\int_i \int_{t_a}^{t_b} \mathcal{P}_{D^0}(m_{12}^2, m_{13}^2, t) dt dm_{12}^2 dm_{13}^2 =$$

$$n \left\{ (e^{-\Gamma t_a} - e^{-\Gamma t_b}) T_i + [\Gamma (e^{-\Gamma t_a} t_a - e^{-\Gamma t_b} t_b) + (e^{-\Gamma t_a} - e^{-\Gamma t_b})] \right.$$

2N symmetric bins

$$\left. \times \left\{ r_{CP} \sqrt{T_i T_{-i}} (y_D [c_i \cos(\alpha_{CP}) + s_i \sin(\alpha_{CP})] + x_D [s_i \cos(\alpha_{CP}) - c_i \sin(\alpha_{CP})]) \right\} \right\}$$

$$T_i \equiv \int_i a_{12,13}^2 dm_{12}^2 dm_{13}^2,$$

$$C_{-i} = C_i$$

$$S_{-i} = -S_i$$

$$c_i \equiv \frac{1}{\sqrt{T_i T_{-i}}} \int_i a_{12,13} a_{13,12} \cos(\delta_{12,13} - \delta_{13,12}) dm_{12}^2 dm_{13}^2,$$

$$s_i \equiv \frac{1}{\sqrt{T_i T_{-i}}} \int_i a_{12,13} a_{13,12} \sin(\delta_{12,13} - \delta_{13,12}) dm_{12}^2 dm_{13}^2.$$

IN LIMIT OF NO MIXING AND NO CPV
OF EVENTS FROM D^0 IN i TH BIN

→ FREE PARAM. OF FIT

COSINE AND SINE OF AVERAGE
STRONG PHASE DIFFERENCE D^0/\bar{D}^0

IN BIN i WEIGHTED BY RATE→ QUANTUM CORR. $D^0\bar{D}^0$ PAIRS

MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

J. LIBBY ET AL. (CLEO-C COLL.), PRD 82,112006 (2010)

MODEL INDEPENDENT METHOD

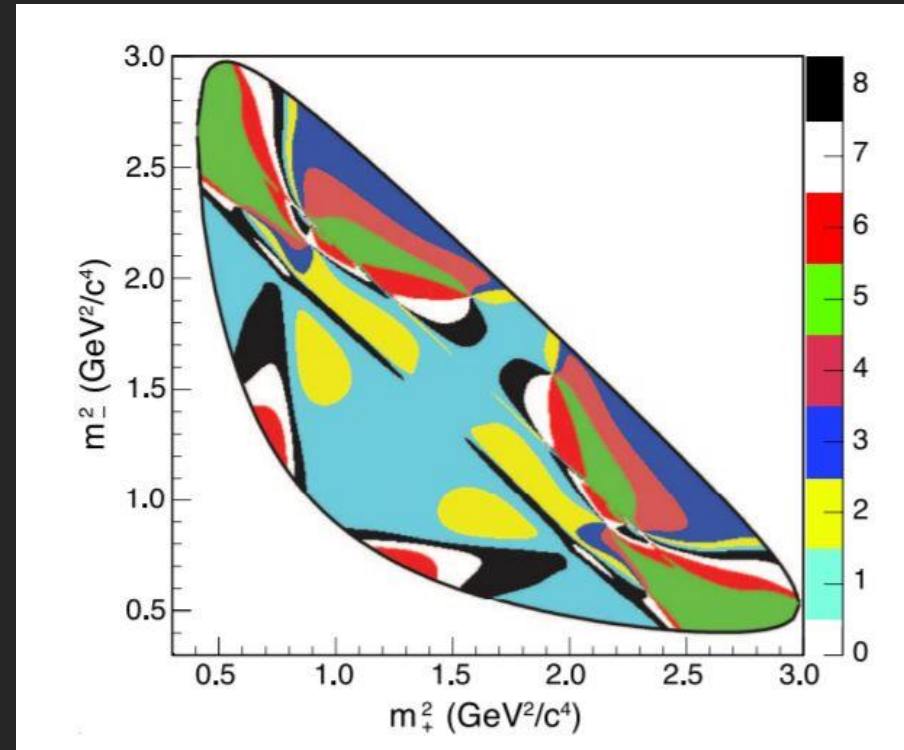
BINNING OF DALITZ PLANE BASED ON

A. POLUEKTOV ET AL. (BELLE COLL.), PR D 81, 112002 (2010)

$(\Delta\delta \sim \text{CONST. ACROSS BIN})$

RESULTS USING $L=0.8 \text{ FB}^{-1}$

i	c_i	s_i
	Equal $\Delta\delta_D$ Belle	
i	c_i	s_i
1	$0.710 \pm 0.034 \pm 0.038$	$-0.013 \pm 0.097 \pm 0.031$
2	$0.481 \pm 0.080 \pm 0.070$	$-0.147 \pm 0.177 \pm 0.107$
3	$0.008 \pm 0.080 \pm 0.087$	$0.938 \pm 0.120 \pm 0.047$
4	$-0.757 \pm 0.099 \pm 0.065$	$0.386 \pm 0.208 \pm 0.067$
5	$-0.884 \pm 0.056 \pm 0.054$	$-0.162 \pm 0.130 \pm 0.041$
6	$-0.462 \pm 0.100 \pm 0.082$	$-0.616 \pm 0.188 \pm 0.052$
7	$0.106 \pm 0.105 \pm 0.100$	$-1.063 \pm 0.174 \pm 0.066$
8	$0.365 \pm 0.071 \pm 0.078$	$-0.179 \pm 0.166 \pm 0.048$



t -DEPENDENCE OF DALITZ

J. LIBBY ET AL. (CLEO-C COLL.), PRD 82,112006 (2010)

METHOD P. 76

UNCERTAINTIES ON c_i, s_i PROPAGATE TO MEASURED VARIABLES (AS SYST. UNCERTAINTY);
STILL STAT. DOMINATED \rightarrow BESIII HAS 3 FB^{-1} OF DATA, PLANNING TO RECORD 10 FB^{-1} MORE

MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

MODEL INDEPENDENT METHOD

T. PENG ET AL., (BELLE COLL.), PRD 89, 091103 (2014) : $1.33 \cdot 10^6 D^*$ TAGGED $D^0 \rightarrow K_S \pi^+ \pi^- / \text{AB}^{-1}$

C. THOMAS, G. WILKINSON, JHEP 2012:185 : $100 \cdot 10^6 D^*$ TAGGED $D^0 \rightarrow K_S \pi^+ \pi^-$:

LHCb SAME STAT.
UNCERTAINTY WITH
~ADDITIONAL 1 FB^{-1}

$$\sigma(x) = [\pm 0.017 \pm 0.076(c_i, s_j)] 10^{-2} \quad \text{CLEO-C (0.8 FB}^{-1}\text{)}$$

$$\sigma(y) = [\pm 0.019 \pm 0.087(c_i, s_j)] 10^{-2}$$

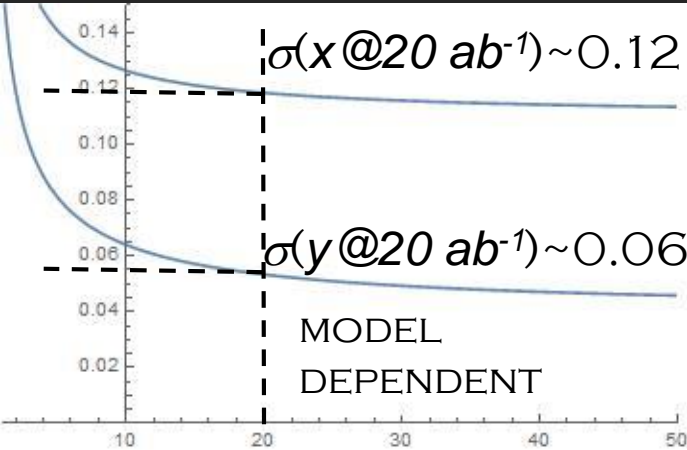
(IN ADDITION TO EXISTING
 9 FB^{-1})

$27 \cdot 10^6 D^*$ TAGGED $D^0 \rightarrow K_S \pi^+ \pi^-$: (BELLE II @ 20 AB^{-1})

$$\sigma(x) = [\pm 0.032 \pm 0.039(c_i, s_j)] 10^{-2} \quad \text{BESIII (3 FB}^{-1}\text{)}$$

$$\sigma(y) = [\pm 0.036 \pm 0.045(c_i, s_j)] 10^{-2} \quad \text{(JUST NAIVE SCALING WITH L)}$$

I. BEDIAGA ET AL. (LHCb COLL.), LHCb-PUB-2018-009



WHERE DO WE STAND?

HFLAV

INPUTS TO FIT

y_{CP}	$(0.715 \pm 0.111)\%$	<u>World average (COMBOS combination)</u> of $D^0 \rightarrow K^+ K^- / \pi^+ \pi^- / K^+ K^- K^0$																									
x (no CPV) y (no CPV)	$0.56 \pm 0.19^{+0.067}_{-0.127}$ $0.30 \pm 0.15^{+0.050}_{-0.078}$	<p><u>LHCb</u> $D^0 \rightarrow K^0_S \pi^+ \pi^-$ results using 1 fb^{-1} ($\sqrt{s} = 7 \text{ TeV}$) Correlation coefficient = +0.37, no CPV.</p> <p><u>BaBar</u> $D^0 \rightarrow K^0_S \pi^+ \pi^-$ and $D^0 \rightarrow K^0_S K^+ K^-$ combined; Correlation coefficient = +0.0615, no CPV.</p> <p><u>BaBar</u> $D^0 \rightarrow \pi^0 \pi^+ \pi^-$ Correlation coefficient = -0.006, no CPV.</p>																									
x (no CPV) y (no CPV)	$(-0.86 \pm 0.53 \pm 0.17)\%$ $(0.03 \pm 0.46 \pm 0.13)\%$																										
x	$(0.16 \pm 0.23 \pm 0.12 \pm 0.08)\%$																										
y	$(0.57 \pm 0.20 \pm 0.13 \pm 0.07)\%$																										
x y	$(1.5 \pm 1.2 \pm 0.6)\%$ $(0.2 \pm 0.9 \pm 0.5)\%$																										
$(x^2 + y^2)/2$	$(0.0130 \pm 0.0269)\%$	<u>World average (COMBOS combination)</u> of $D^0 \rightarrow K^+ l^- \nu$ results																									
x'' y''	$(2.61^{+0.57}_{-0.68} \pm 0.39)\%$ $(-0.06^{+0.55}_{-0.64} \pm 0.34)\%$	<p><u>BaBar</u> $K^+ \pi^- \pi^0$ result; correlation coefficient = -0.75. Note: $x'' = x \cos \delta_{K\pi\pi} + y \sin \delta_{K\pi\pi}$, $y'' = y \cos \delta_{K\pi\pi} - x \sin \delta_{K\pi\pi}$.</p>																									
R_D x^2 y cos δ sin δ	$(0.533 \pm 0.107 \pm 0.045)\%$ $(0.06 \pm 0.23 \pm 0.11)\%$ $(4.2 \pm 2.0 \pm 1.0)\%$ $0.81^{+0.22}_{-0.18} \pm 0.07^{+0.07}_{-0.05}$ $-0.01 \pm 0.41 \pm 0.04$	<p><u>CLEO-c</u> $\Psi(3770)$ results; correlation coefficients:</p> <table style="margin-left: 20px;"> <tr> <td>1</td> <td>0</td> <td>0</td> <td>-0.42</td> <td>0.01</td> </tr> <tr> <td></td> <td>1</td> <td>-0.73</td> <td>0.39</td> <td>0.02</td> </tr> <tr> <td></td> <td></td> <td>1</td> <td>-0.53</td> <td>-0.03</td> </tr> <tr> <td></td> <td></td> <td></td> <td>1</td> <td>0.04</td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td>1</td> </tr> </table>	1	0	0	-0.42	0.01		1	-0.73	0.39	0.02			1	-0.53	-0.03				1	0.04					1
1	0	0	-0.42	0.01																							
	1	-0.73	0.39	0.02																							
		1	-0.53	-0.03																							
			1	0.04																							
				1																							

WHERE DO WE STAND?

HFLAV

INPUTS TO FIT

R_D	$(0.351 \pm 0.035)\%$	CDF $K^+ \pi^-$ results for 9.6 fb^{-1} . Correlation coefficients: 1 0.90 -0.97 0.90 1 -0.98 -0.97 -0.98 1
x'^2	$(0.008 \pm 0.018)\%$	
y'	$(0.43 \pm 0.43)\%$	
R_D^+	$(0.3454 \pm 0.0045)\%$	LHCb $K^+ \pi^-$ results for 5.0 fb^{-1} ($\sqrt{s} = 7, 8 \text{ TeV}$) Correlation coefficients: 1 0.843 -0.935 0.843 1 -0.963 -0.935 -0.963 1
x'^{2+}	$(0.0061 \pm 0.0037)\%$	
y'^+	$(0.501 \pm 0.074)\%$	
R_D^-	$(0.3454 \pm 0.0045)\%$	LHCb $K^+ \pi^-$ results for 5.0 fb^{-1} ($\sqrt{s} = 7, 8 \text{ TeV}$) Correlation coefficients: 1 0.846 -0.935 0.846 1 -0.964 -0.935 -0.964 1
x'^{2-}	$(0.0016 \pm 0.0039)\%$	
y'^-	$(0.554 \pm 0.074)\%$	

WHERE DO WE STAND?

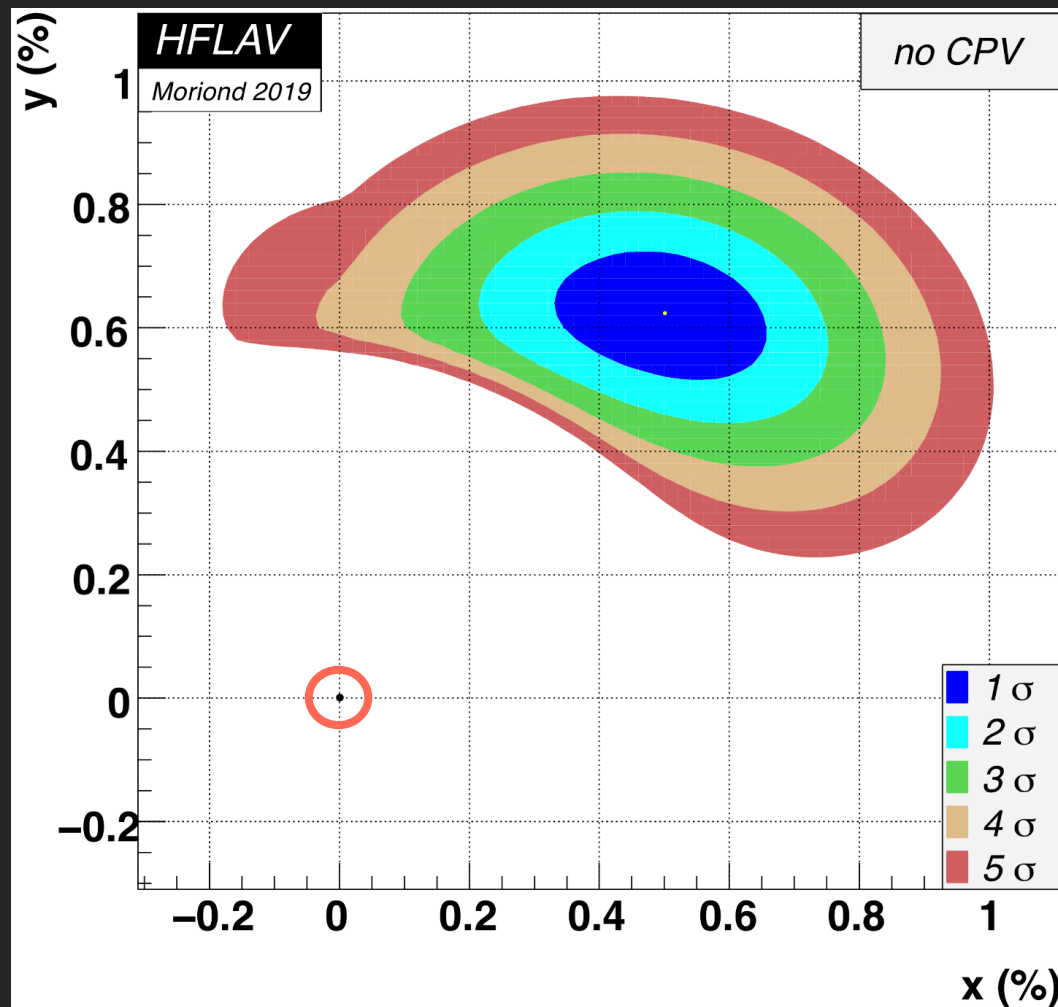
HFLAV

INPUTS TO FIT

R_D x'^{2+} y'^{+}	$(0.303 \pm 0.0189)\%$ $(-0.024 \pm 0.052)\%$ $(0.98 \pm 0.78)\%$	<u>BaBar</u> $K^+ \pi^-$ results; correlation coefficients: $\begin{matrix} 1 & +0.77 & -0.87 \\ +0.77 & 1 & -0.94 \\ -0.87 & -0.94 & 1 \end{matrix}$
A_D x'^{2-} y'^{-}	$(-2.1 \pm 5.4)\%$ $(-0.020 \pm 0.050)\%$ $(0.96 \pm 0.75)\%$	<u>BaBar</u> $K^+ \pi^-$ results; correlation coefficients same as above.
R_D x'^2 y'	$(0.353 \pm 0.013)\%$ $(0.009 \pm 0.022)\%$ $(0.46 \pm 0.34)\%$	<u>Belle</u> $K^+ \pi^-$ no-CPV results using 976 fb^{-1} . Correlation coefficients: $\begin{matrix} 1 & +0.737 & -0.865 \\ +0.737 & 1 & -0.948 \\ -0.865 & -0.948 & 1 \end{matrix}$
$(x^2 + y^2)/4$	$(0.0048 \pm 0.0018)\%$	<u>LHCb</u> 3.0 fb^{-1} pp collisions at $\sqrt{s} = 7, 8 \text{ TeV}$ $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$

WHERE DO WE STAND?

HFLAV



○ NO MIXING POINT

$$x = (0.50 \pm_{0.14}^{0.13})\%$$

$$y = (0.62 \pm 0.07)\%$$

REPEAT FROM P. 29, W/O ANY
DISCLAIMER:

D^0 MESONS, LIKE OTHER M^0 ,
DO MIX, WITH THE LOWEST
PROBABILITY OF ALL

$$P(D^0 \rightarrow \bar{D}^0) \sim 3 \cdot 10^{-5}$$

D^0 MIXING IS DATA DRIVEN FIELD
(N.B. x, y NEEDED FOR CPV PREDICTIONS)

UNCERTAINTIES

$$A = \frac{N - \bar{N}}{N + \bar{N}} \Rightarrow \frac{\sigma_A}{A} = \frac{1}{\sqrt{2}} \frac{1}{A} \frac{\sigma_N}{N}$$

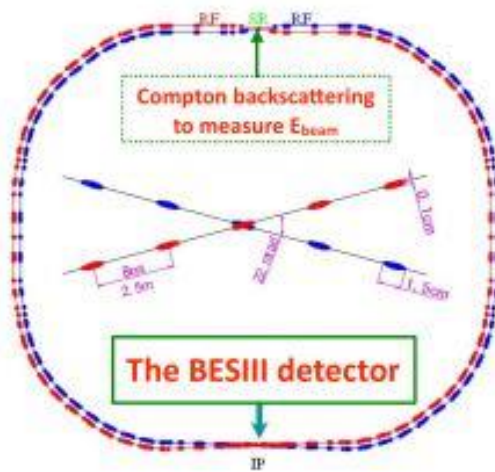
ASYMMETRY (B^0, D^0)

$$r = \frac{N'}{N} \Rightarrow \frac{\sigma_r}{r} = \sqrt{2} \frac{\sigma_N}{N}$$

RATIO (K_L)BACK

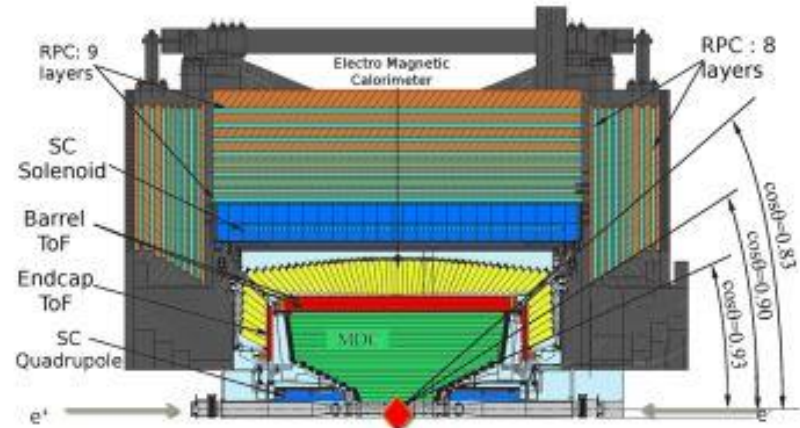
BESIII Experiment

Beijing Electron Positron Collider II (BEPCII)



- ▶ Double ring e^+e^- collider
- ▶ E_{cm} : 2 ~ 4.6 GeV, operated since 2008
- ▶ Designed Luminosity : $10^{33} \text{cm}^{-2} \text{s}^{-1}$ was achieved in April 2016!
- ▶ Beam crossing angle: 22 mrad

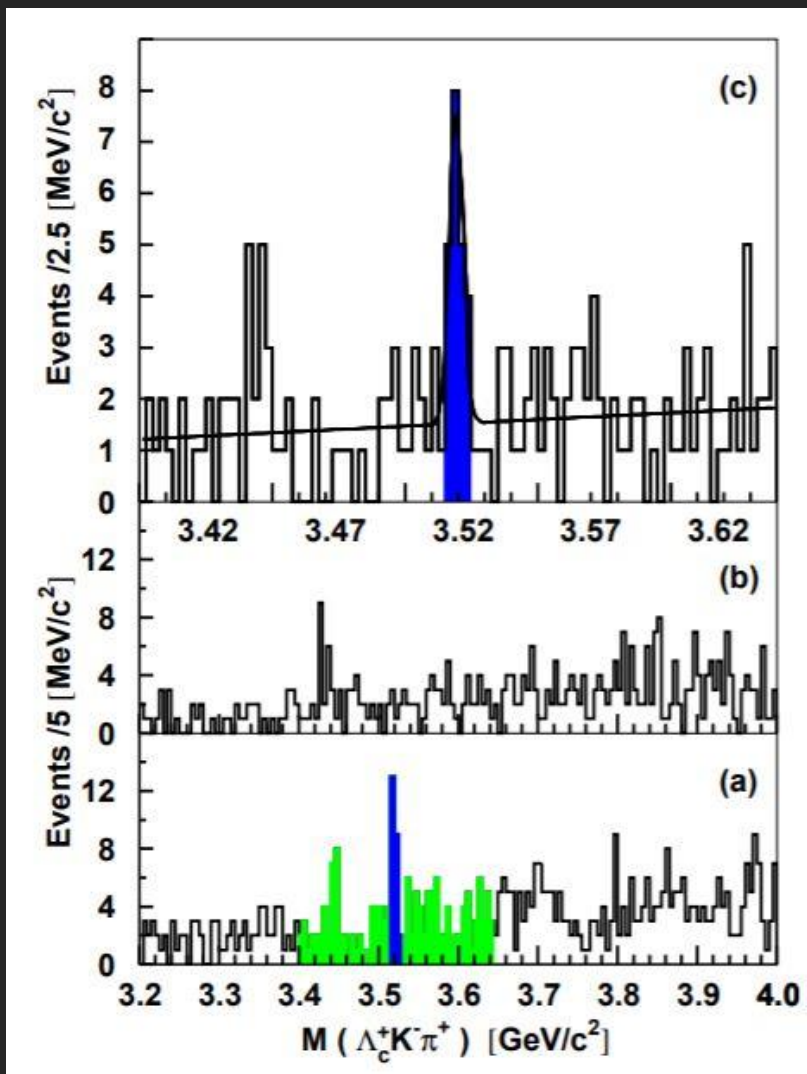
(Beijing Spectrometer III) BESIII



- ▶ Acceptance: 93% of 4π
- ▶ MDC: $\sigma_p/p = 0.5\%$ at 1 GeV
- ▶ EMC: $\sigma_E/E = 2.5\%$ at 1 GeV
- ▶ ToF: $\sigma = 80\text{ps}$ (110 ps) in barrel (endcap)
- ▶ 9 layer RPC Muon System
- ▶ Superconducting Solenoid: 1 T

~ 1.3 NB IS σ FOR TWO c QUARKS \rightarrow AT LEAST TWO CHARMED HADRONS

$\sigma(e^+e^- \rightarrow X_c \gamma)$ GIVEN IN THE TABLE ARE NOT INDEPENDENT
(E.G. $\sigma(e^+e^- \rightarrow D \gamma)$ INCLUDES $\sigma(e^+e^- \rightarrow D^* \gamma)$ WITH $D^* \rightarrow D \dots$);
HENCE WE INCLUDE ONLY $\sigma(e^+e^- \rightarrow D \gamma)$ IN THE SUM



M. MATTSON ET AL. (SELEX COLL.), PRL 89, 112001 (2002)

SELEX: Σ^- BEAM ON TARGET;
PRODUCTION OF CHARM HADRONS;
FERMILAB

HYPOTETICAL

$$\Xi_{CC}^+ \rightarrow \Lambda_c^+ K^- \pi^+$$

NEVER CONFIRMED BY BABAR,
BELLE OR LHCb

EXOTIC MESONS

STATES OTHER THAN $q_1\bar{q}_2$, $q_1q_2q_3$ NOT FORBIDDEN IN SM;
EXOTIC J^{PC} (e.g. 0^{+-} , 1^{-+} , 2^{+-} , ... FORBIDDEN FOR $q\bar{q}$);
EXOTIC DECAY MODES (NOT POSSIBLE FROM $q\bar{q}$);
STRANGE PROPERTIES (WIDTHS, ...);

PENTAQUARKS:

$$q_1q_2q_3q_4q_5;$$

HYBRIDS:

$$c\bar{c} + g's;$$

TETRAQUARKS:

$$\text{DIQUARK-ANTIDIQUARK, } [c\bar{q}][\bar{c}q]$$

MOLECULES:

$$M(c\bar{q})M(\bar{c}q), \text{ LOOSELY BOUND MESONS}$$

[BACK](#)

SINCE $m(X(3872)) \sim m(D)+m(D^*)$
→ DD^* MOLECULE?

SUCH A MOLECULE IS IDEAL MIXTURE OF ISOSPIN COMPONENTS:

$$|I, I_3\rangle = |0, 0\rangle + |1, I_3\rangle;$$

$X(3872)$ DECAYS TO $J/\psi \rho$ ($\pi\pi$) ($I=1$) AND $J/\psi \omega$ ($\pi\pi\pi$) ($I=0$);

DUE TO LIMITED PHASE SPACE FOR $J/\psi \omega$ IT WOULD DECAY PREFERENTIALLY
(STRONGLY) TO $J/\psi \rho$;

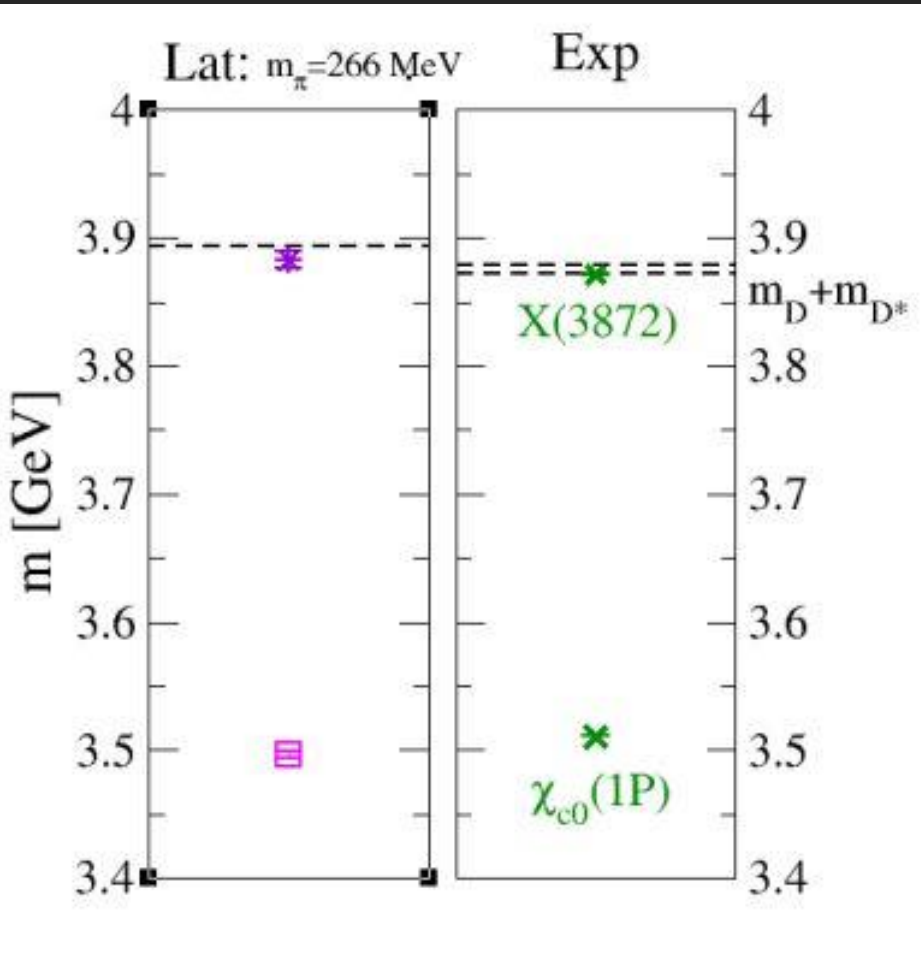
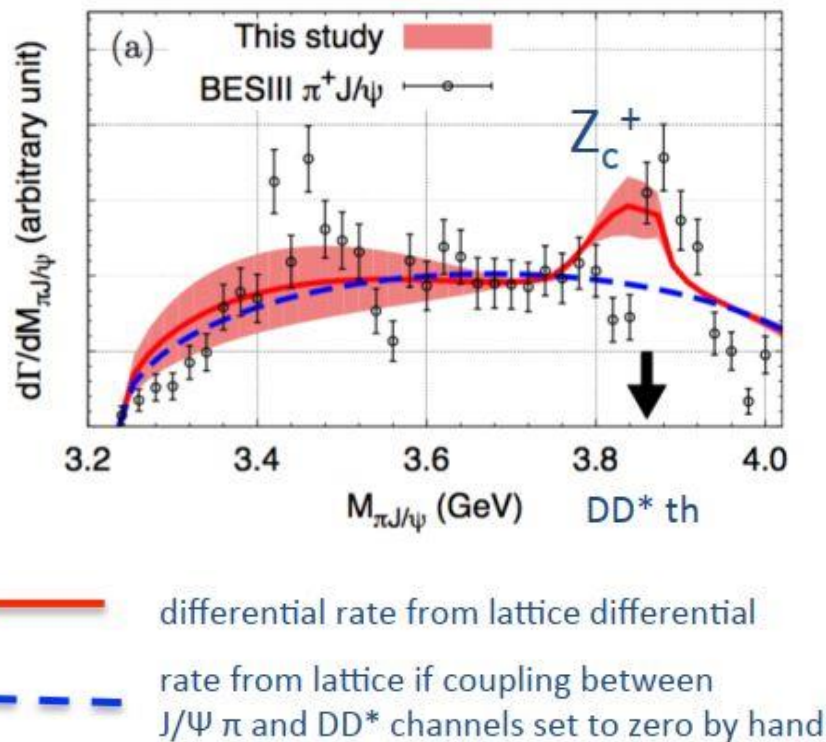
EXPERIMENT: $Br(J/\psi \rho) \sim Br(J/\psi \omega)$; ISOSPIN VIOLATION?

⇒ NEW MODELS WITH ADDITION OF $c\bar{c}$ ($I=0$)

[BACK](#)

X(3872) ON LATTICE
ATTEMPT FOR $Z_c^+(3900)$

S. PRELOVSEK, L. LESKOVEC, PRL 111, 192001 (2013)



Y. IKEDA ET AL. (HALQCD COLL.), PRL 117, 242001 (2016)

[BACK](#)

APPROXIMATE DEPENDENCE OF RELATIVE ACCURACY OF YIELD ON LUMINOSITY AND PURITY

$$\frac{\sigma_{N_s}}{N_s} = \frac{\sqrt{N_s + N_b}}{N_s}; \quad P = \frac{N_s}{N_s + N_b}, \quad \frac{\sigma_{N_s}}{N_s} = \sqrt{\frac{L_0}{N_{s0}}} \frac{1}{\sqrt{LP}} \left(= \sqrt{\frac{L_0}{L}} \left(\frac{\sigma_{N_s}}{N_s} \right)_0 \right)$$

$$\left(P = 1 \Rightarrow \frac{\sigma_{N_s}}{N_s} = \sqrt{\frac{1}{N_s}} \right)$$

INTRODUCING FEI WITH EFF. $\varepsilon \sim 1\%$, IMPROVING PURITY TO $P' \sim 0.5$

$$\frac{\sigma_{N_s}}{N_s} = \sqrt{\frac{L_0}{N_{s0}}} \frac{1}{\sqrt{\varepsilon LP'}}$$

REQUIRING SAME STAT. UNCERTAINTY

$$\frac{\sigma_{N_s}}{N_s} = \left(\frac{\sigma_{N_s}}{N_s} \right)_0$$

$$\Rightarrow L \sim 15 \text{ AB}^{-1}$$

[BACK](#)

$$P_c^+ \rightarrow J/\psi p$$

$$uudc\bar{c}$$

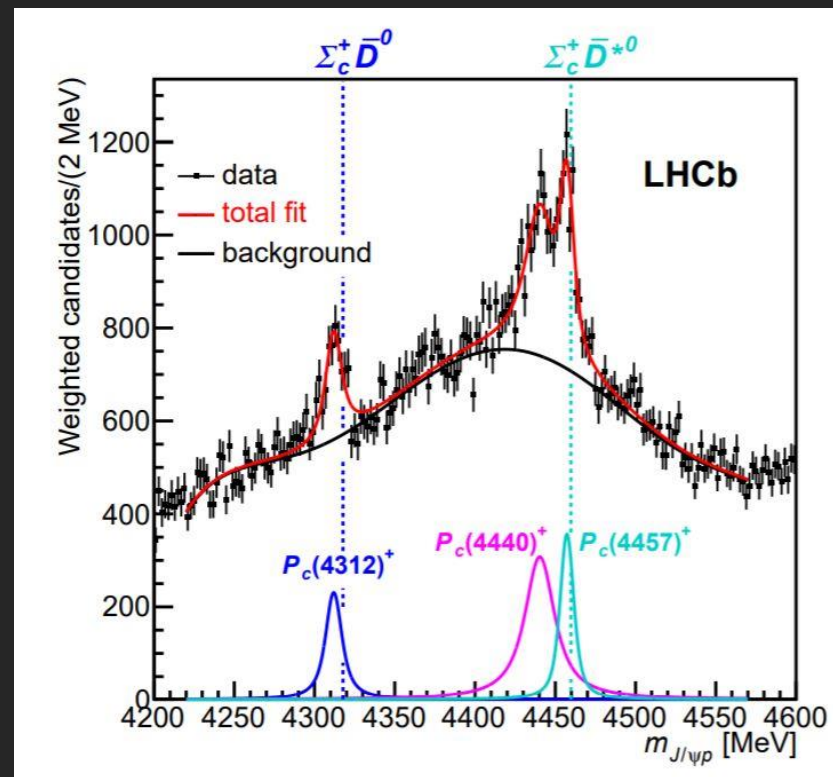
R. AAJ ET AL. (LHCb COLL.), PRL 115, 072001 (2015)

LQCD: P_c DOES NOT APPEAR IN
 $J/\psi p \rightarrow P_c^+ \rightarrow J/\psi p$
SCATTERING, DECOUPLED FROM OTHER
CHANNELS

U. SKERBIS, S. PFRELOVSEK, PRD 99, 094505 (2019)

BACK

UPDATE



R. AAJ ET AL. (LHCb COLL.), PRL 122, 222001 (2019)

ISR PRODUCTION

DIFF. CROSS SECTION
FOR ISR PRODUCTION

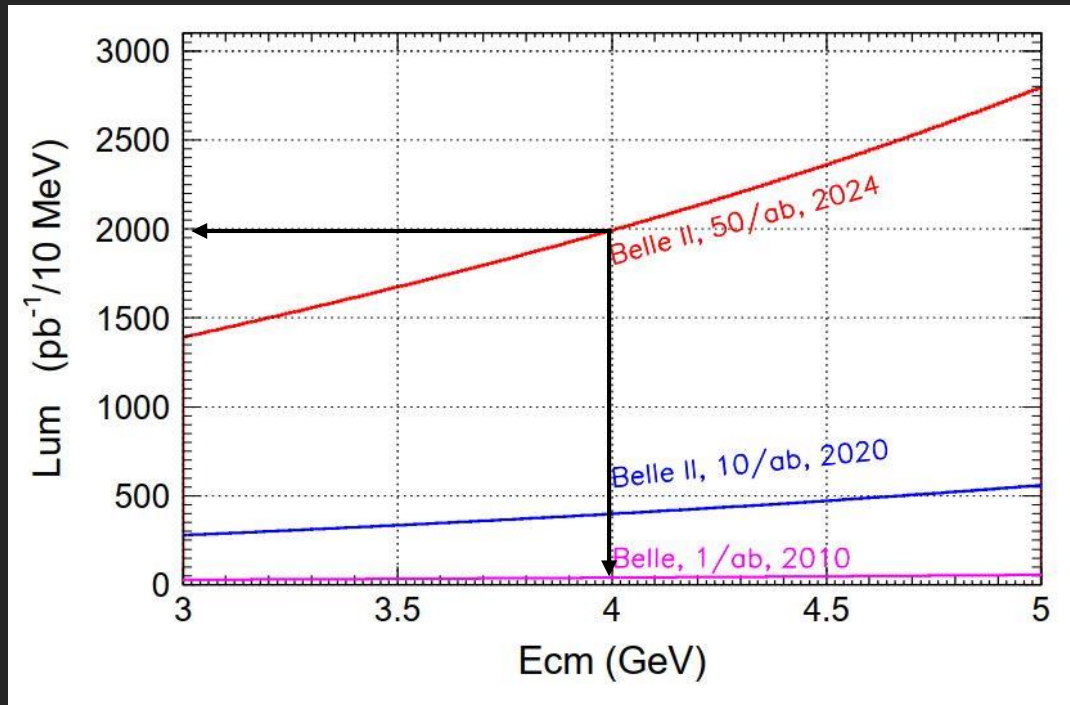
CROSS SECTION FOR
 $e^+e^- \rightarrow f$ PRODUCTION

$$x = 2E_{\gamma_{ISR}} / \sqrt{s}$$

$$\frac{\sigma_f(s, x)}{dx} = W(s, x)\sigma_f(s(1-x))$$

EFFECTIVE LUMINOSITY

PROBAB. FOR γ_{ISR} EMISSION
(KNOWN TO BETTER THAN 1%)



AT $L=50 \text{ AB}^{-1}$
WE WILL HAVE 2 FB^{-1}
LUMINOSITY TO
PRODUCE ISR EVENT
WITH
 $\sqrt{s'} \in [4 \text{ GEV} - 5 \text{ MEV},$
 $4 \text{ GEV} + 5 \text{ MEV}]$

B2PB

[BACK](#)

$$|\psi(t=0)\rangle = a(0)|P^0\rangle + b(0)|\bar{P}^0\rangle$$

$$|\psi(t)\rangle = a(t)|P^0\rangle + b(t)|\bar{P}^0\rangle + \dots$$

$$i\frac{\partial}{\partial t} \begin{bmatrix} |P^0(t)\rangle \\ |\bar{P}^0(t)\rangle \end{bmatrix} = \left(\mathbf{M} - \frac{i}{2}\mathbf{\Gamma} \right) \begin{bmatrix} |P^0(t)\rangle \\ |\bar{P}^0(t)\rangle \end{bmatrix}$$

$$|P_{1,2}\rangle = p|P^0\rangle \pm q|\bar{P}^0\rangle$$

$$\begin{bmatrix} M - i\frac{\Gamma}{2} & M_{12} - i\frac{\Gamma_{12}}{2} \\ M_{12}^* - i\frac{\Gamma_{12}^*}{2} & M - i\frac{\Gamma}{2} \end{bmatrix} \begin{bmatrix} p \\ \pm q \end{bmatrix} = \lambda_{1,2} \begin{bmatrix} p \\ \pm q \end{bmatrix}$$

$$\lambda_{1,2} = M - i\frac{\Gamma}{2} \pm \frac{q}{p} \left[M_{12} - i\frac{\Gamma_{12}}{2} \right] \equiv m_{1,2} - i\frac{\Gamma_{1,2}}{2}, \quad \left(\frac{q}{p} \right)^2 = \frac{M_{12}^* - i\frac{\Gamma_{12}^*}{2}}{M_{12} - i\frac{\Gamma_{12}}{2}}$$

$$|P_{1,2}(t)\rangle = e^{-i\lambda_{1,2}t} |P_{1,2}(t=0)\rangle$$

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$$

$$\hat{C}\hat{P}|D^0\rangle = +|\bar{D}^0\rangle$$

NO CPV: $\hat{C}\hat{P}|D_{1,2}\rangle = |\bar{D}^0\rangle \pm |D^0\rangle = \pm |D_{1,2}\rangle$

TIME EVOLUTION:

$$|D^0(t)\rangle = \left[|D^0\rangle \cosh\left(\frac{ix+y}{2}\bar{\Gamma}t\right) - \frac{q}{p}|\bar{D}^0\rangle \sinh\left(\frac{ix+y}{2}\bar{\Gamma}t\right) \right] e^{-i\bar{m}t - \frac{\bar{\Gamma}}{2}t}$$

$$|\bar{D}^0(t)\rangle = \left[|\bar{D}^0\rangle \cosh\left(\frac{ix+y}{2}\bar{\Gamma}t\right) - \frac{p}{q}|D^0\rangle \sinh\left(\frac{ix+y}{2}\bar{\Gamma}t\right) \right] e^{-i\bar{m}t - \frac{\bar{\Gamma}}{2}t}$$

$$\left| \langle \bar{D}^0 | D^0(t) \rangle \right|^2 = \left| \frac{q}{p} \right|^2 \left| \sinh\left(\frac{ix+y}{2}\bar{\Gamma}t\right) \right|^2 e^{-\bar{\Gamma}t} \quad \left| \langle D^0 | D^0(t) \rangle \right|^2 = \left| \cosh\left(\frac{ix+y}{2}\bar{\Gamma}t\right) \right|^2 e^{-\bar{\Gamma}t}$$

$$r = \int_0^\infty \left| \langle \bar{D}^0 | D^0(t) \rangle \right|^2 dt \Big/ \int_0^\infty \left| \langle \bar{D}^0 | D^0(t) \rangle \right|^2 dt + \int_0^\infty \left| \langle D^0 | D^0(t) \rangle \right|^2 dt = \frac{x^2 + y^2}{2(1+x^2)}$$

[BACK](#)

TIME EVOLUTION:

$$|x|, |y| \ll 1 \Rightarrow \frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \left| \langle f | D^0 \rangle - \frac{q}{p} \frac{ix+y}{2} \langle f | \bar{D}^0 \rangle \bar{\Gamma}t \right|^2$$

$$|x|, |y| \ll 1 \Rightarrow \frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \left| \langle f | \bar{D}^0 \rangle - \frac{p}{q} \frac{ix+y}{2} \langle f | D^0 \rangle \bar{\Gamma}t \right|^2$$

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |A_f|^2 \left| 1 - \lambda_f \frac{ix+y}{2} \bar{\Gamma}t \right|^2$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |\bar{A}_f|^2 \left| 1 - \lambda_f^{-1} \frac{ix+y}{2} \bar{\Gamma}t \right|^2$$

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |A_f|^2 \left[1 - y \operatorname{Re}(\lambda_f) \bar{\Gamma}t + x \operatorname{Im}(\lambda_f) \bar{\Gamma}t \right]$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |\bar{A}_f|^2 \left[1 - y \frac{1}{|\lambda_f|^2} \operatorname{Re}(\lambda_f) \bar{\Gamma}t - x \frac{1}{|\lambda_f|^2} \operatorname{Im}(\lambda_f) \bar{\Gamma}t \right]$$

$$\operatorname{Re}\left(\frac{1}{\lambda_f}\right) = \frac{1}{|\lambda_f|^2} \cos \phi_\lambda$$

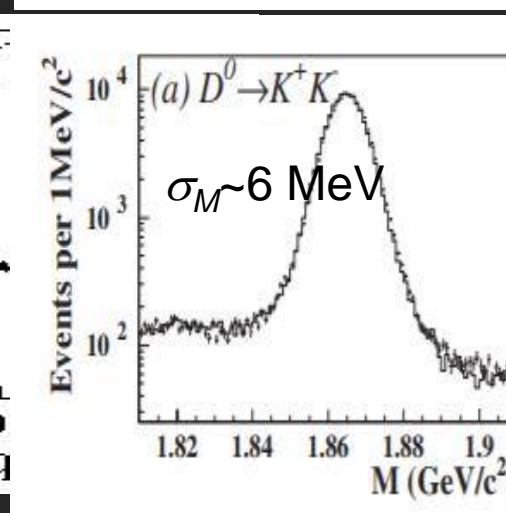
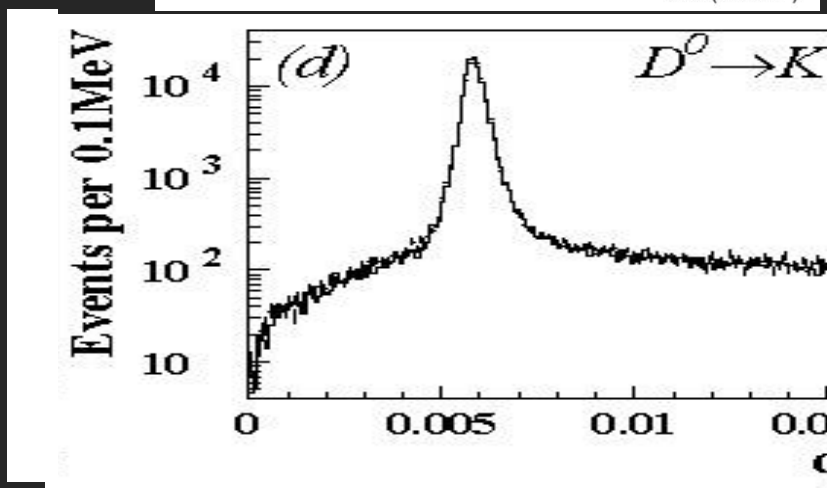
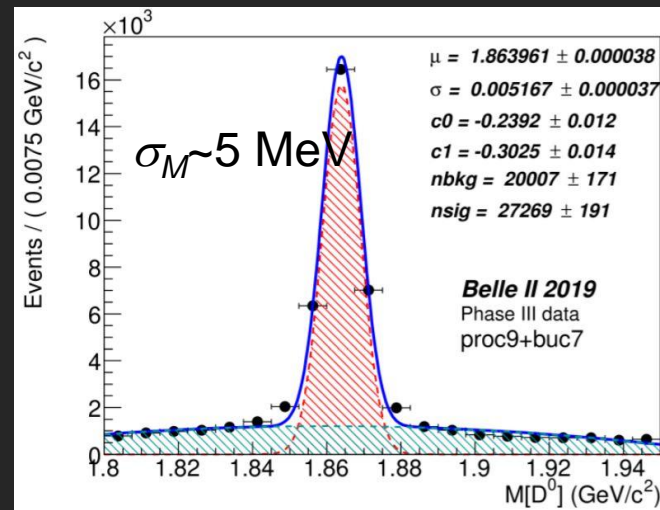
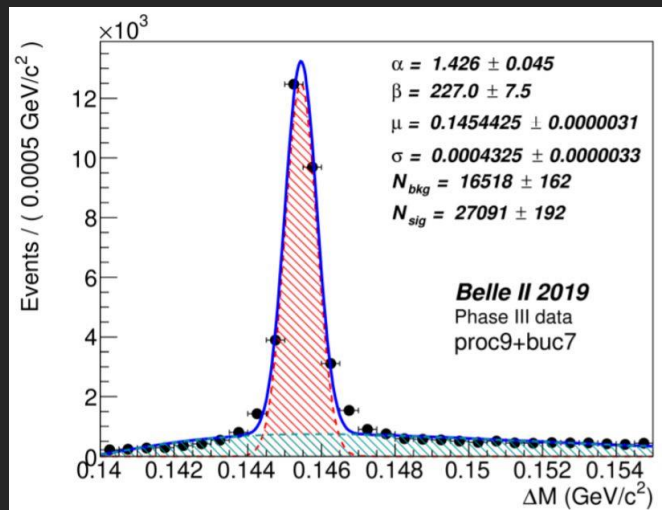
$$\operatorname{Im}\left(\frac{1}{\lambda_f}\right) = -\frac{1}{|\lambda_f|^2} \sin \phi_\lambda$$

$$\phi_\lambda = \arg(\lambda_f)$$

[BACK](#)

TAGGING WITH D^{*+} 'S

S. SANDILYA ET AL. (BELLE II COLL.), B2GM OCT 2019



M. STARIC ET AL. (BELLE COLL.), PRL 98, 211803 (2007)

[BACK](#)

DECAY TIME

BELLE II

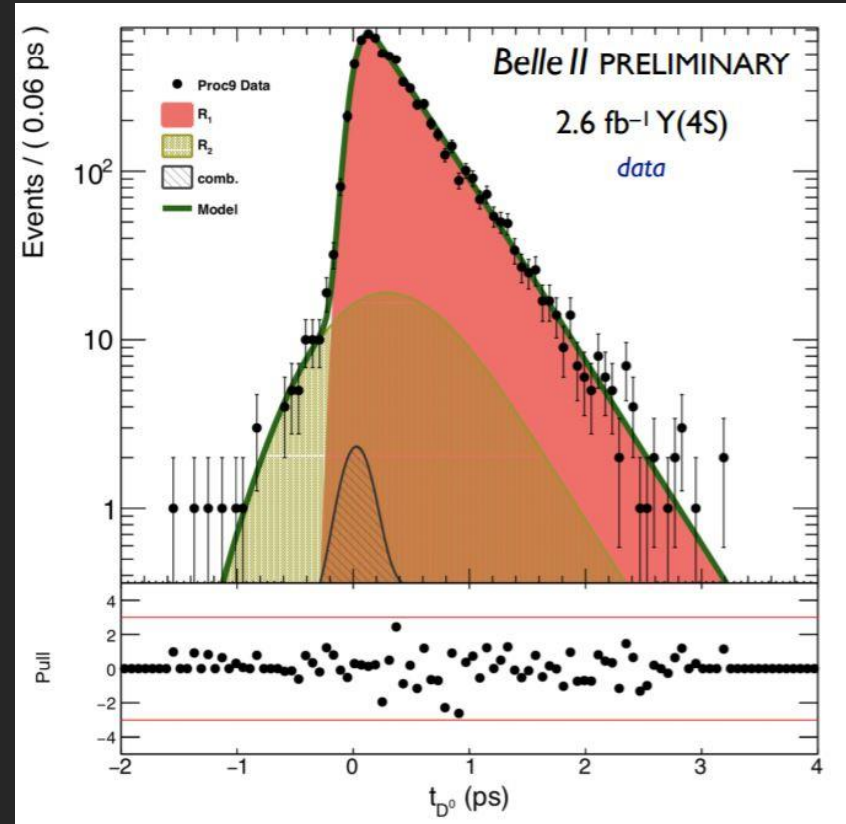
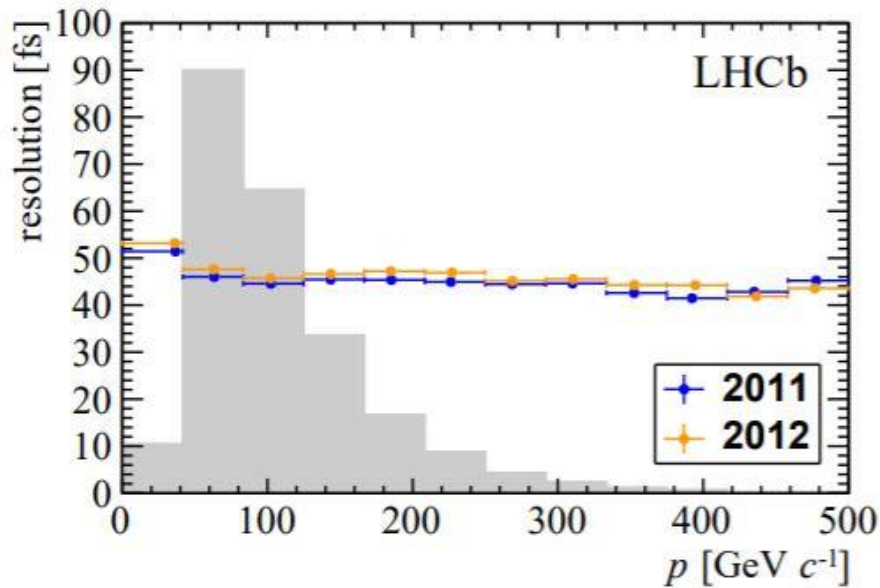
$$D^* \rightarrow D^0(K\pi)\pi$$

$$\langle \sigma_t \rangle \sim 100 \text{ FS}$$

LHCb

$$B_s \rightarrow J/\psi \phi$$

$$\langle \sigma_t \rangle \sim 40 \text{ FS}$$



$$\lambda_f = \frac{q}{p} \eta_f$$

$$|A_f| = |\bar{A}_f| = |A|$$

$$\phi_f = \arg(\lambda_f) = \arg\left(\frac{q}{p}\right) \equiv \phi$$

$\eta_f = +1$ CP EVEN STATES

$\eta_f = -1$ CP ODD STATES

$$\langle f_{CP} | D^0 \rangle = \frac{1}{\sqrt{2}} [\langle f_{CP} | D_1 \rangle + \langle f_{CP} | D_2 \rangle]$$

$$\langle f_{CP} | \bar{D}^0 \rangle = \frac{1}{\sqrt{2}} [\langle f_{CP} | D_1 \rangle - \langle f_{CP} | D_2 \rangle]$$

$$\langle f_{CP}^+ | D^0 \rangle = \frac{1}{\sqrt{2}} \langle f_{CP}^+ | D_1 \rangle = \langle f_{CP}^+ | \bar{D}^0 \rangle$$

$$\langle f_{CP}^- | D^0 \rangle = \frac{1}{\sqrt{2}} \langle f_{CP}^- | D_2 \rangle = -\langle f_{CP}^- | \bar{D}^0 \rangle$$

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |A|^2 \left[1 - \eta_f y \left| \frac{q}{p} \right| \cos \phi \bar{\Gamma} t + \eta_f x \left| \frac{q}{p} \right| \sin \phi \bar{\Gamma} t \right]$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |A|^2 \left[1 - \eta_f y \left| \frac{p}{q} \right| \cos \phi \bar{\Gamma} t - \eta_f x \left| \frac{p}{q} \right| \sin \phi \bar{\Gamma} t \right]$$

[BACK](#)

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |A|^2 \left[1 - \eta_f y \left| \frac{q}{p} \right| \cos \phi \bar{\Gamma} t + \eta_f x \left| \frac{q}{p} \right| \sin \phi \bar{\Gamma} t \right]$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |A|^2 \left[1 - \eta_f y \left| \frac{p}{q} \right| \cos \phi \bar{\Gamma} t - \eta_f x \left| \frac{p}{q} \right| \sin \phi \bar{\Gamma} t \right]$$

$$\frac{dN(D^0 \rightarrow f)}{dt} + \frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |A|^2 [1 - y_{CP} \bar{\Gamma} t]$$

$$y_{CP} \equiv y$$

$$q=p_{-}$$

$$A_f = \bar{A}_f$$

y_{CP} TAKING INTO ACCOUNT
CPV IS GIVEN IN 2ND PART OF
LECTURES

$K^+K^-, \pi^+\pi^-$: CP EVEN STATES

$K_S\phi, K_S\omega$: CP ODD STATES

[BACK](#)

$$f=K^+\pi^- \quad \lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f} = \left| \frac{q}{p} \right| \frac{1}{r} e^{i(\delta_f + \phi)}$$

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |\bar{A}_{K^+\pi^-}|^2 \left[r^2 - ry \left| \frac{q}{p} \right| \cos(\delta_{K\pi} + \phi) \bar{\Gamma}t + rx \left| \frac{q}{p} \right| \sin(\delta_{K\pi} + \phi) \bar{\Gamma}t \right]$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |\bar{A}_{K^+\pi^-}|^2 \left[1 - ry \left| \frac{p}{q} \right| \cos(\delta_{K\pi} + \phi) \bar{\Gamma}t + rx \left| \frac{p}{q} \right| \sin(\delta_{K\pi} + \phi) \bar{\Gamma}t \right]$$

NEGLECTING CPV (AND GOING TO 2ND ORDER IN x, y):

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |\bar{A}_{K^+\pi^-}|^2 \left[r^2 - ry' \bar{\Gamma}t + \frac{x'^2 + y'^2}{4} (\bar{\Gamma}t)^2 \right]$$

$$y' = y \cos(\delta_{K\pi}) - x \sin(\delta_{K\pi})$$

$$x' = x \cos(\delta_{K\pi}) + y \sin(\delta_{K\pi})$$

[BACK](#)

METHOD OF STRONG PHASE DIFFERENCE D^0 / \bar{D}^0 DETERM. USING COHERENT PRODUCTION OF D MESON PAIRS J. LIBBY ET AL. (CLEO-C COLL.), PRD 82,112006 (2010)

$\psi(3770)$ ($CP = +1$) $\rightarrow D_1 D_2$;

if $D_1 \rightarrow CP+$ $\Rightarrow D_2$ is $CP-$; (CP-TAGGED)

$$CP = CP(D_1)CP(D_2)(-1)^{\ell=1}$$

if $D_1 \rightarrow D^0 \rightarrow f_{flav} \Rightarrow D_2$ is \bar{D}^0 (FLAVOR-TAGGED)

EVTS IN BIN i FOR FLAVOR TAGGED (D^0) DECAY:

$$K_i = A_D \int_i |f_D(m_+^2, m_-^2)|^2 dm_+^2 dm_-^2 = A_D F_i \quad (\text{SAME FOR } \bar{D}^0 \text{ WITH } m_+ \leftrightarrow m_-)$$

J. LIBBY ET AL. (CLEO-C COLL.), PRD 82,112006 (2010)

DALITZ DIST. FOR CP TAGGED (CP_+ , CP_-) DECAYS

$$f_{CP_{\pm}}(m_+^2, m_-^2) = \frac{1}{\sqrt{2}} [f_D(m_+^2, m_-^2) \pm f_D(m_-^2, m_+^2)]$$

EVTS IN BIN i

FOR CP TAGGED (CP_+ , CP_-) DECAY:

$$M_i^{\pm} = h_{CP_{\pm}} (K_i \pm 2c_i \sqrt{K_i K_{-i} + K_{-i}})$$

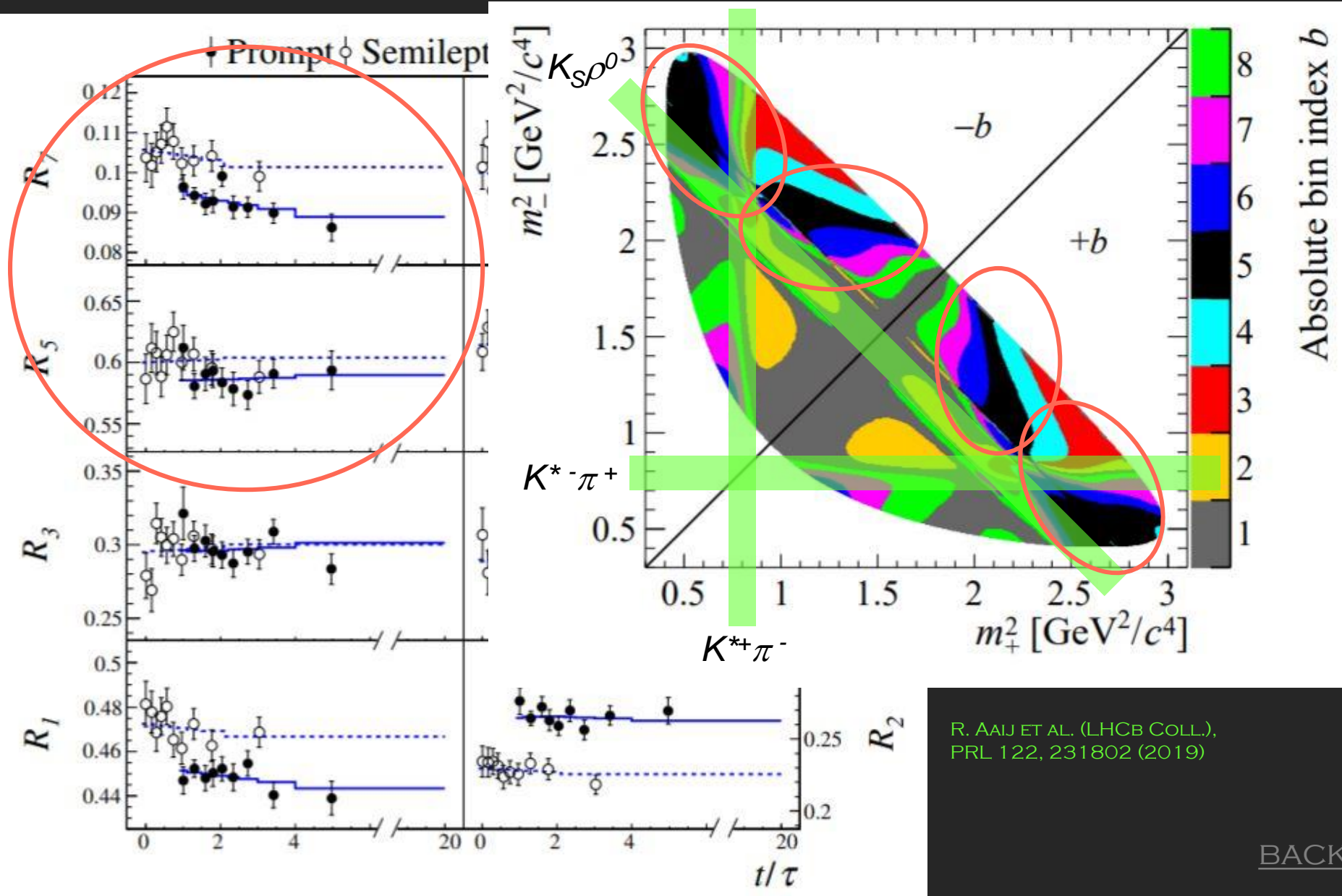
FLAVOR-TAGGED:

$$K_i = A_D \int_i |f_D(m_+^2, m_-^2)|^2 dm_+^2 dm_-^2 = A_D F_i$$

$$c_i \equiv \frac{1}{\sqrt{F_i F_{-i}}} \int_i |f_D(m_+^2, m_-^2)| |f_D(m_-^2, m_+^2)| \cos[\Delta\delta_D(m_+^2, m_-^2)] dm_+^2 dm_-^2$$

$$s_i \equiv \frac{1}{\sqrt{F_i F_{-i}}} \int_i |f_D(m_+^2, m_-^2)| |f_D(m_-^2, m_+^2)| \sin[\Delta\delta_D(m_+^2, m_-^2)] dm_+^2 dm_-^2$$

[BACK](#)



R. AAJ ET AL. (LHCb COLL.),
PRL 122, 231802 (2019)

[BACK](#)