

BOSTJAN GOLOB
UNIVERSITY OF LJUBLJANA /
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University
of Ljubljana



"Jozef Stefan"
Institute

ALSO WITH



INTRODUCTION

FACILITIES

SPECTROSCOPY

MIXING

CPV

(RARE) DECAYS

2ND OPEN BELLE II PHYSICS WEEK
KEK
28TH OCT - 1ST NOV 2019

DISCLAIMER

CHOICE OF SUBJECTS, AND ESPECIALLY EXAMPLES, HAD TO BE MADE;

SPEAKER IS TO BE BLAMED FOR NOT SHOWING YOUR FAVORITE MEASUREMENT

FREQUENTLY USED REFERENCES:

PDG: M. TANABASHI ET AL. (PARTICLE DATA GROUP), PHYS. REV. D 98, 030001 (2018).

HFLAV: HEAVY FLAVOR AVERAGING GROUP, [HTTPS://HFLAV.WEB.CERN.CH/](https://hflav.web.cern.ch/)

PBF : THE PHYSICS OF THE B FACTORIES, A. BEVAN, B. GOLOB, T. MANNEL, S. PRELL, B. YABSLEY EDS., EUR. PHYS. J. C 74 (2014) .

BIIPB: E. KOU, P. URQUIJO ETN AL. (BELLE II COLL.), ARXIV:1808.10567

MULTI-BODY SELF CONJUGATED STATES

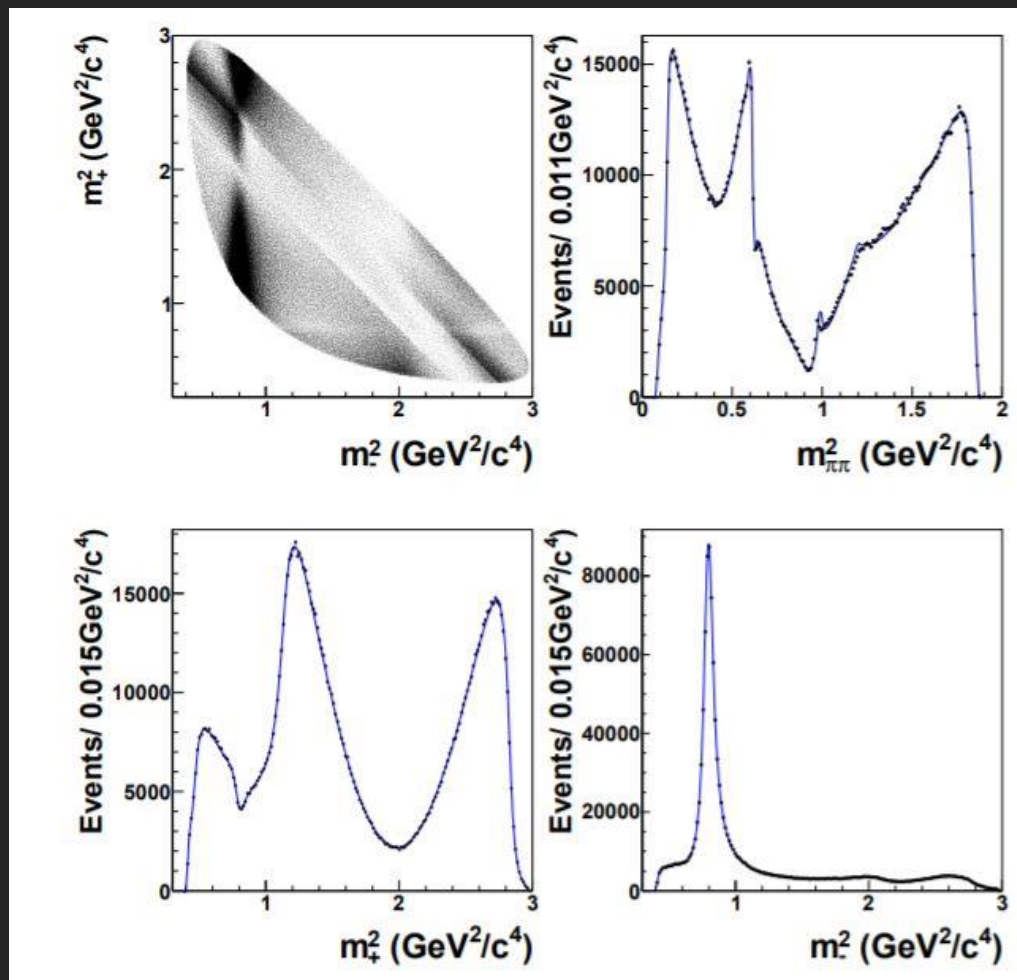
$$D^0 \rightarrow K_S \pi^+ \pi^-$$

NO CPV RESULT:

$$x = (0.56 \pm 0.19 \pm_{0.09}^{0.03} \pm_{0.09}^{0.06})\%$$

$$y = (0.30 \pm 0.15 \pm_{0.05}^{0.04} \pm_{0.06}^{0.03})\%$$

↑
UNCERTAINTY DUE TO
DALITZ MODEL



T. PENG ET AL., (BELLE COLL.), PRD 89, 091103 (2014)

MULTI-BODY SELF CONJUGATED STATES

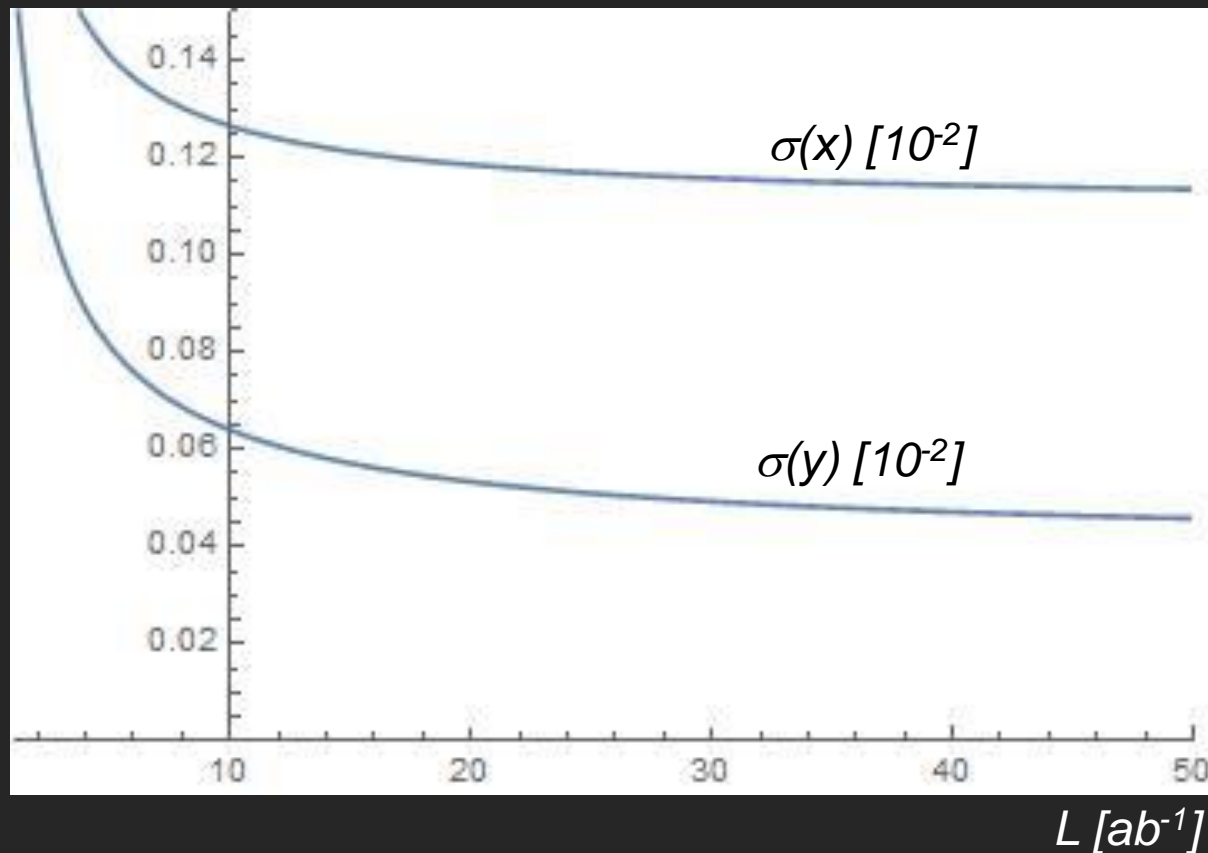
$$D^0 \rightarrow K_S \pi^+ \pi^-$$

BELLE II:
SYST. UNCERTAINTY
DOMINATES @ FEW AB^{-1}

IN TURN, SYST. UNCERTAINTY
DOMINATED BY THE MODEL
UNCERTAINTY

CAN THIS BE EVADED?

BY MEASURING STRONG
PHASE VARIATION ACROSS
DALITZ PLANE USING
COHERENT $D^0 D^0$ PAIRS (BES III)



MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

A. BONDAR, A. POLUEKTOV AND V. VOROBIEV, PRD 82, 034033 (2010)
A. GIRI, Y. GROSSMAN, A. SOFFER, AND J. ZUPAN, PR D 68, 054018 (2003)

MODEL INDEPENDENT METHOD

DALITZ- AND t DEPENDENT AMPLITUDE UP TO $O(x^2, y^2)$

NOTATION: $\frac{q}{p} = r_{CP} e^{i\alpha_{CP}}$

$$\mathcal{P}_{D^0}(m_{12}^2, m_{13}^2, t) = \Gamma e^{-\Gamma t} \left[a_{12,13}^2 + r_{CP} a_{12,13} a_{13,12} \Gamma t \left\{ y_D \cos(\delta_{12,13} - \delta_{13,12} - \alpha_{CP}) + x_D \sin(\delta_{12,13} - \delta_{13,12} - \alpha_{CP}) \right\} \right]$$

C. THOMAS,
G. WILKINSON,
JHEP 2012:185

INTEGRATING OVER DALITZ- AND t BIN

$$\int_i \int_{t_a}^{t_b} \mathcal{P}_{D^0}(m_{12}^2, m_{13}^2, t) dt dm_{12}^2 dm_{13}^2 =$$

2N symmetric bins

$$n \left\{ (e^{-\Gamma t_a} - e^{-\Gamma t_b}) T_i + [\Gamma (e^{-\Gamma t_a} t_a - e^{-\Gamma t_b} t_b) + (e^{-\Gamma t_a} - e^{-\Gamma t_b})] \right. \\ \left. \times \left\{ r_{CP} \sqrt{T_i T_{-i}} (y_D [c_i \cos(\alpha_{CP}) + s_i \sin(\alpha_{CP})] + x_D [s_i \cos(\alpha_{CP}) - c_i \sin(\alpha_{CP})]) \right\} \right\}$$

$$T_i \equiv \int_i a_{12,13}^2 dm_{12}^2 dm_{13}^2,$$

$$C_{-i} = C_i$$

$$S_{-i} = -S_i$$

$$c_i \equiv \frac{1}{\sqrt{T_i T_{-i}}} \int_i a_{12,13} a_{13,12} \cos(\delta_{12,13} - \delta_{13,12}) dm_{12}^2 dm_{13}^2,$$

$$s_i \equiv \frac{1}{\sqrt{T_i T_{-i}}} \int_i a_{12,13} a_{13,12} \sin(\delta_{12,13} - \delta_{13,12}) dm_{12}^2 dm_{13}^2.$$

IN LIMIT OF NO MIXING AND NO CPV
OF EVENTS FROM D^0 IN i TH BIN

→ FREE PARAM. OF FIT

COSINE AND SINE OF AVERAGE
STRONG PHASE DIFFERENCE D^0/\bar{D}^0

IN BIN i WEIGHTED BY RATE

→ QUANTUM CORR. $D^0\bar{D}^0$ PAIRS

MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

J. LIBBY ET AL. (CLEO-C COLL.), PRD 82,112006 (2010)

MODEL INDEPENDENT METHOD

BINNING OF DALITZ PLANE BASED ON

A. POLUEKTOV ET AL. (BELLE COLL.), PR D 81, 112002 (2010)

$(\Delta\delta \sim \text{CONST. ACROSS BIN})$

RESULTS USING $L=0.8 \text{ FB}^{-1}$

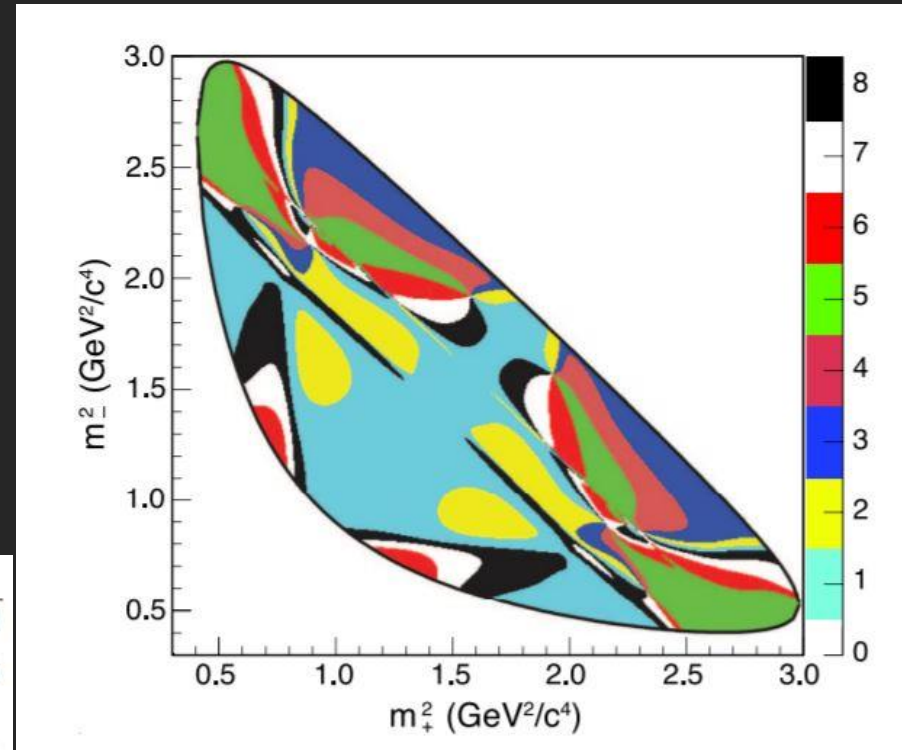
| i | c_i | s_i |
|-----------------------------------------------|------------------------------|------------------------------|
| $\mathcal{N} = 4$ equal $\Delta\delta_D$ bins | | |
| 1 | $0.858 \pm 0.059 \pm 0.034$ | $0.309 \pm 0.248 \pm 0.180$ |
| 2 | $0.176 \pm 0.223 \pm 0.091$ | $0.992 \pm 0.473 \pm 0.403$ |
| 3 | $-0.819 \pm 0.095 \pm 0.045$ | $0.307 \pm 0.267 \pm 0.201$ |
| 4 | $0.376 \pm 0.329 \pm 0.157$ | $-0.133 \pm 0.659 \pm 0.323$ |

J. LIBBY ET AL. (CLEO-C COLL.), PRD 82,112006 (2010)

METHOD P. 42 DALITZ t -DEPENDENCE P. 44

UNCERTAINTIES ON c_i, s_i PROPAGATE TO MEASURED VARIABLES (AS SYSTEMATIC UNCERTAINTY);

STILL STATISTICS DOMINATED \rightarrow BESIII HAS 3 FB^{-1} OF DATA, PLANNING TO RECORD 10 FB^{-1} MORE



MULTI-BODY SELF CONJUGATED STATES

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

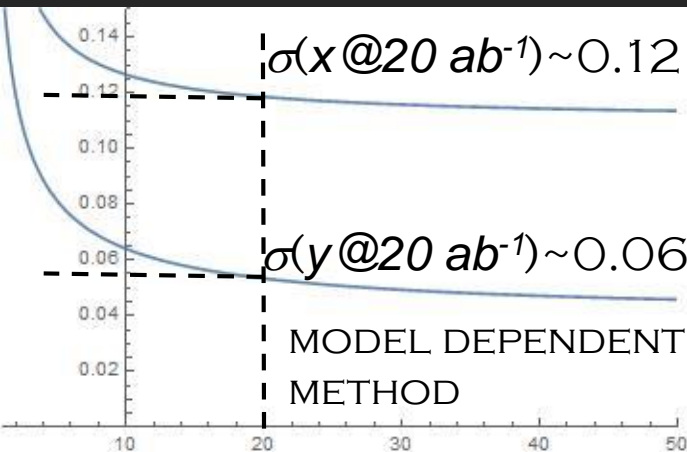
MODEL INDEPENDENT METHOD

T. PENG ET AL., (BELLE COLL.), PRD 89, 091103 (2014) : $1.33 \cdot 10^6 D^*$ TAGGED $D^0 \rightarrow K_S \pi^+ \pi^- / AB^{-1}$

C. THOMAS, G. WILKINSON, JHEP 2012:185 : $100 \cdot 10^6 D^*$ TAGGED $D^0 \rightarrow K_S \pi^+ \pi^-$:
 $\sigma(x) = [\pm 0.017 \pm 0.076(c_i, s_j)] 10^{-2}$ CLEO-C (0.8 FB^{-1})
 $\sigma(y) = [\pm 0.019 \pm 0.087(c_i, s_j)] 10^{-2}$

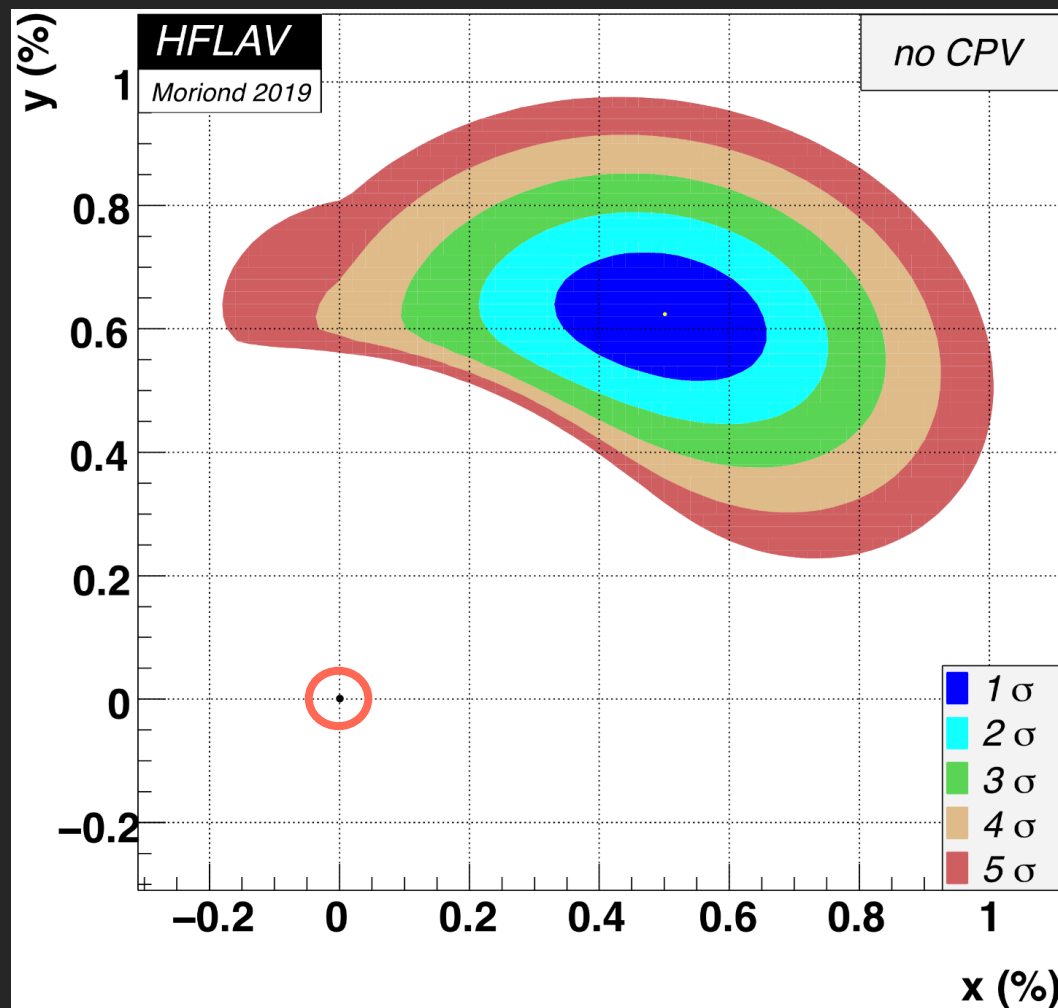
LHCb NEED ADDITIONAL
 $\sim 1 FB^{-1}$ (IN ADDITION TO
 EXISTING 9 FB^{-1}) TO REACH
 THIS STAT. ACCURACY

$27 \cdot 10^6 D^*$ TAGGED $D^0 \rightarrow K_S \pi^+ \pi^-$: (BELLE II @ 20 AB^{-1})
 $\sigma(x) = [\pm 0.032 \pm 0.039(c_i, s_j)] 10^{-2}$ BESIII WITH 3 FB^{-1}
 $\sigma(y) = [\pm 0.036 \pm 0.045(c_i, s_j)] 10^{-2}$ (ONLY SIMPLE SCALING WITH L)



WHERE DO WE STAND?

HFLAV



○ NO MIXING POINT

$$x = (0.50 \pm_{0.14}^{0.13})\%$$

$$y = (0.62 \pm 0.07)\%$$

REPEAT FROM P. 29, W/O ANY
DISCLAIMER:

D^0 MESONS, LIKE OTHER M^0 ,
DO MIX, WITH THE LOWEST
PROBABILITY OF ALL

$$P(D^0 \rightarrow \bar{D}^0) \sim 3 \cdot 10^{-5}$$

D^0 MIXING IS DATA DRIVEN FIELD
(N.B. x, y NEEDED FOR CPV PREDICTIONS)

... IS SMALL

CKM IN WOLFENSTEIN
PARAM. (TO $O(\lambda^3)$)

ELEMENTS RELATED TO
CHARM ARE REAL

⇒ NO COMPLEX PHASE, NO CPV (IN SM)

$$\begin{pmatrix}
 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\
 -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\
 A\lambda^3[1 - (1 - \lambda^2/2)(\rho + i\eta)] & -A\lambda^2 & 1
 \end{pmatrix}
 + O(\lambda^4)$$

... IS SMALL

CKM IN WOLFENSTEIN
PARAM. (TO $O(\lambda^3)$)

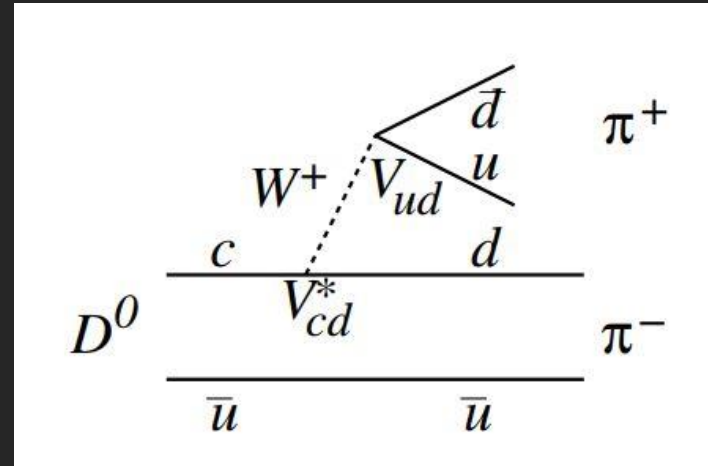
$$\begin{pmatrix} 1 - \lambda^2/2 - \lambda^4/8 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + A^2\lambda^5[1 - 2(\rho + i\eta)]/2 & 1 - \lambda^2/2 - \lambda^4(1 + 4A^2)/8 & A\lambda^2 \\ A\lambda^3[1 - (1 - \lambda^2/2)(\rho + i\eta)] & -A\lambda^2 + A\lambda^4[1 - 2(\rho + i\eta)]/2 & 1 - A^2\lambda^4/2 \end{pmatrix} + O(\lambda^4)$$

ELEMENTS RELATED TO
CHARM ARE REAL

⇒ NO COMPLEX PHASE, NO CPV (IN SM)

CKM IN WOLFENSTEIN
PARAM. (TO $O(\lambda^5)$)

$$\arg \frac{\langle \pi^+ \pi^- | D^0 \rangle}{\langle \pi^+ \pi^- | \bar{D}^0 \rangle} = 2 \arg(V_{cd}^* V_{ud}) \approx 2A^2\lambda^4\eta = 1.2 \times 10^{-3}$$



CPV IN CHARM SECTOR IS SMALL, ASYMMETRIES $\sim O(10^{-3})$ IN SM.
POTENTIALLY GOOD PLACE TO LOOK FOR NP EFFECTS.

SOME REMINDERS

$$f = \bar{f} = f_{CP}$$

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |A_f|^2 \left[1 - y \text{Re}(\lambda_f) \bar{\Gamma}t + x \text{Im}(\lambda_f) \bar{\Gamma}t \right]$$

1) $|\bar{A}_f| \neq |A_f|$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} |\bar{A}_f|^2 \left[1 - y \frac{1}{|\lambda_f|^2} \text{Re}(\lambda_f) \bar{\Gamma}t - x \frac{1}{|\lambda_f|^2} \text{Im}(\lambda_f) \bar{\Gamma}t \right]$$

CPV IN DECAY (CPVDEC)

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

2) $|\lambda_f| \neq 1$, AND

TAKING INTO ACCOUNT 1),

$$\left| \frac{q}{p} \right| \neq 1$$

CPV IN MIXING (CPVMIX)

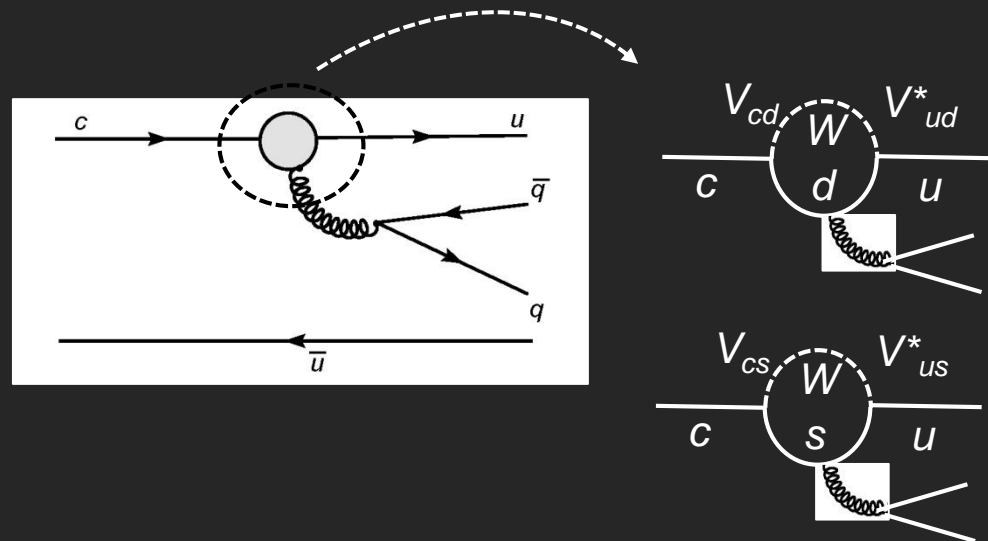
3) $\text{Im}(\lambda_f) \neq 0$ CPV IN INTERFERENCE BETWEEN DECAYS W/ AND W/O MIXING (CPVINT)

SOME REMINDERS

FOR CPV AT LEAST TWO PROCESSES WITH DISTINCT WEAK AND STRONG PHASE NECESSARY (EXAMPLE OF CPV IN DECAY)

$$\begin{aligned}
 A_f &= a_1 + a_2 = |a_1| e^{i(\delta_1 + \varphi_1)} + |a_2| e^{i(\delta_2 + \varphi_2)} \\
 A_{CP} &= \frac{\Gamma(M \rightarrow f) - \Gamma(\bar{M} \rightarrow \bar{f})}{\Gamma(M \rightarrow f) + \Gamma(\bar{M} \rightarrow \bar{f})} = \frac{|A_f / \bar{A}_{\bar{f}}|^2 - 1}{|A_f / \bar{A}_{\bar{f}}|^2 + 1} = \\
 &= \dots = \frac{2 |a_1 a_2| \sin(\delta_2 - \delta_1) \sin(\varphi_2 - \varphi_1)}{|a_1|^2 + |a_2|^2 + 2 |a_1 a_2| \cos(\delta_2 - \delta_1) \cos(\varphi_2 - \varphi_1)}
 \end{aligned}$$

IN D MESON DECAYS THIS IS ONLY POSSIBLE IN SCS DECAYS WITH CONTRIBUTION OF PENGUIN DECAYS (BESIDE TREE CONTRIB.)



$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

WITH CPV PARAMETRIZATION

MORE INVOLVED

(N.B. $A_M, A_{dir}^f \ll 1$)

A_M : CPVMIX

A_{dir}^f : CPVDEC

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f} = \left| \frac{q}{p} \right| \left| \frac{\bar{A}_f}{A_f} \right| e^{i\varphi} \quad \eta_f = \begin{cases} +1 & f = CP+ \\ -1 & f = CP- \end{cases}$$

$$A_m = \left| \frac{q}{p} \right|^2 - 1 \quad A_{dir}^f = \frac{|\bar{A}_f|^2}{|A_f|^2} - 1$$

EXPRESSION FOR y_{CP} GETS
MODIFIED BY KEEPING TERMS q/p

IN „MASTER“ FORMULAE

ON P. 23:

$$y_{CP} = \eta_f \left[y \cos \phi - \frac{A_{dir}^f + A_m}{2} x \sin \phi \right]$$

IN LIMIT OF NO CPV $|q/p|=1, \phi=0 \Rightarrow y_{CP}=y$;

MOREOVER,

$$\frac{dN(D^0 \rightarrow f_{CP}^+)}{dt} \neq \frac{dN(\bar{D}^0 \rightarrow f_{CP}^+)}{dt}$$

$$D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$$

NEGLECTING CPV

$$\frac{1}{\tau_{eff}^{fCP}} = \frac{1}{\bar{\tau}_{eff}^{fCP}} = \frac{1 + y_{CP}}{\tau}$$

ASSUMING CPV

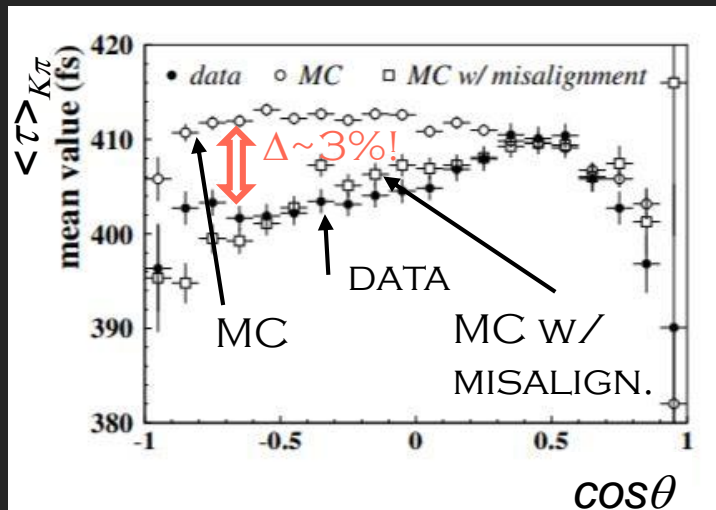
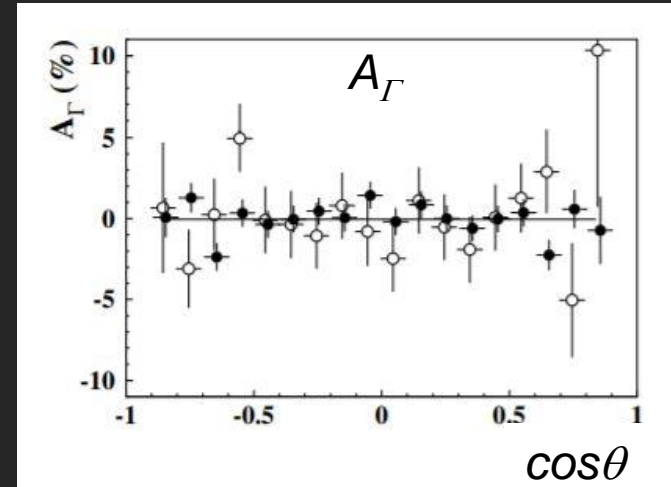
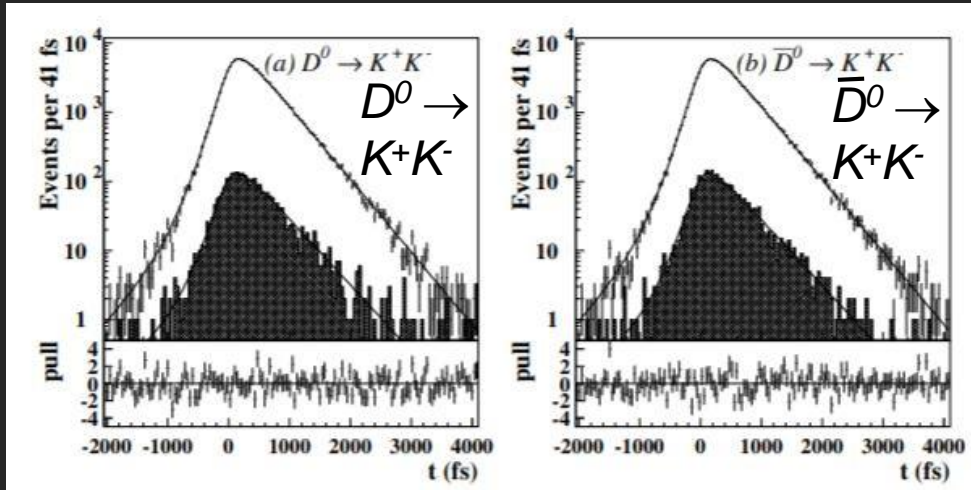
$$A_{\Gamma} = \frac{\bar{\tau}_{fCP}^{eff} - \tau_{fCP}^{eff}}{\bar{\tau}_{fCP}^{eff} + \tau_{fCP}^{eff}} \approx \left(\frac{A_{dir}^{fCP} + A_m}{2} \right) y \cos \phi - x \sin \phi$$

DERIVATIONIN LIMIT OF NO CPV $|q/p|=1, \phi=0 \Rightarrow A_{\Gamma}=0$

$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

ASYMMETRY A_Γ MEASURED TOGETHER WITH y_{CP} (JUST DIVIDING THE SAMPLE INTO D^0 / \bar{D}^0 TAGGED)

M. STARIC ET AL. (BELLE COLL.), PLB 753, 412 (2016)



$$A_\Gamma = (-0.03 \pm 0.20 \pm 0.07)\%$$

SUBTLE / IMPORTANT EFFECTS OF SVD MISALIGNMENT;
IN τ MEASUREMENTS O(%) EFFECTS MAY BE INCLUDED IN SYST. UNCERTAINTY;
IN DETERMINATION OF $\%_0$ EFFECTS NOT

$$D^0 \rightarrow K^+K^-, \pi^+\pi^-$$

B FACTORIES:

$$A_\Gamma = \frac{\bar{\tau}_{fCP}^{eff} - \tau_{fCP}^{eff}}{\bar{\tau}_{fCP}^{eff} + \tau_{fCP}^{eff}}$$

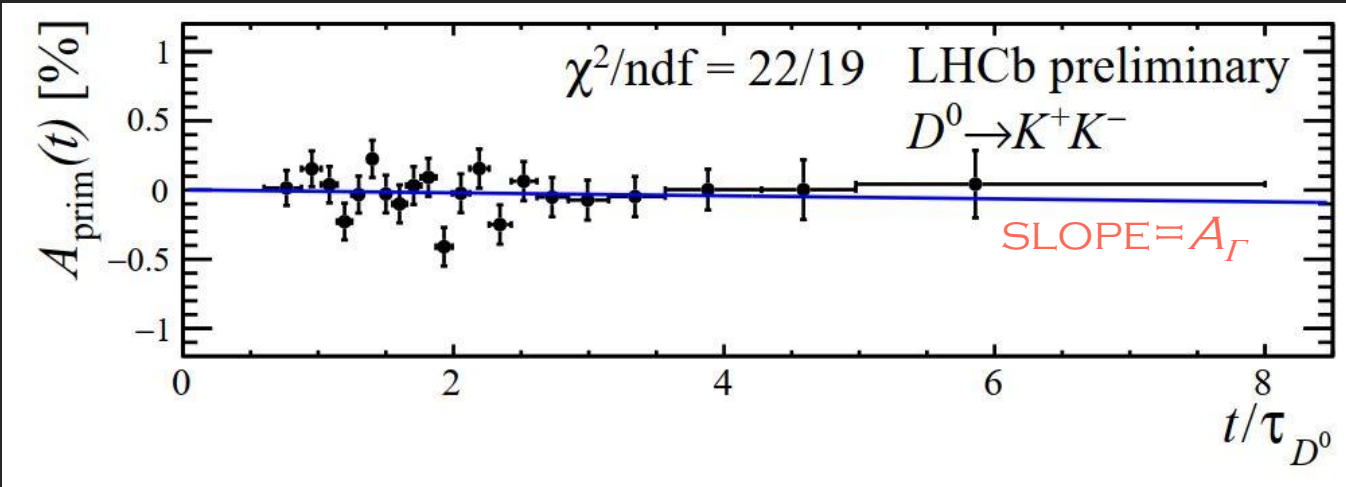
LHCb:

$$\frac{\left(\frac{dN(D^0 \rightarrow f)}{dt}\right) - \left(\frac{dN(\bar{D}^0 \rightarrow f)}{dt}\right)}{\left(\frac{dN(D^0 \rightarrow f)}{dt}\right) + \left(\frac{dN(\bar{D}^0 \rightarrow f)}{dt}\right)} \approx A_{dir}^f - \tilde{A}_\Gamma \bar{\Gamma} t$$

$$A_\Gamma = (1.3 \pm 3.5 \pm 0.07) \cdot 10^{-4}$$

R. AAJ ET AL. (LHCb COLL.), LHCb-PAPER-2019-032

USING PROMPT $D^{*'}S$;
SIMILAR RESULT WITH
 $b \rightarrow c\mu X$



CURRENT COMBINED
EXP. SENSITIVITY
 $O(10^{-4})$;

TH. PREDICTIONS FOR
 $A_\Gamma \sim O(10^{-5})$

A. CERRI ET AL., ARXIV:1812.07638

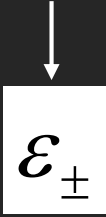
$$D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$$

LHCb:

$$\left(\frac{1}{\epsilon_+} \frac{dN^{meas}(D^0 \rightarrow f)}{dt} \right) - \left(\frac{1}{\epsilon_-} \frac{dN^{meas}(\bar{D}^0 \rightarrow f)}{dt} \right)$$

$$\left(\frac{1}{\epsilon_+} \frac{dN^{meas}(D^0 \rightarrow f)}{dt} \right) + \left(\frac{1}{\epsilon_-} \frac{dN^{meas}(\bar{D}^0 \rightarrow f)}{dt} \right)$$

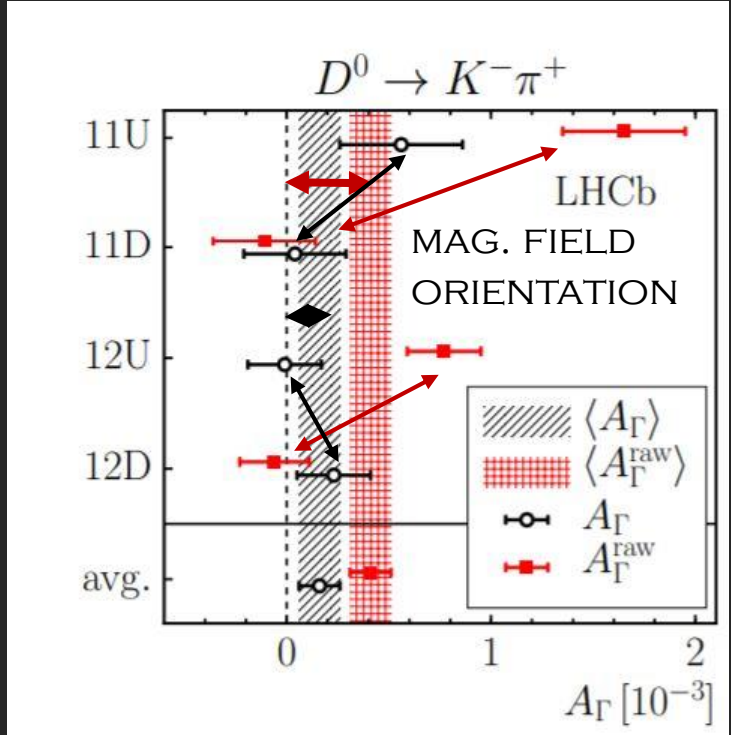
$$D^{*\pm} \rightarrow D^0 (\bar{D}^0) \pi_s^\pm$$



$$D^{*\pm} \rightarrow D^0 (\bar{D}^0) \pi_s^\pm$$

$$|\rightarrow K^- \pi^+ (K^+ \pi^-)$$

NO PHYSICS (CPV) ASYM. EXPECTED
(CF DECAY) → CORRECT ϵ_{\pm} IN BINS
OF KINEMATIC VARIABLES SO THAT
 $N(D^{*+}) = N(D^{*-})$ IN EACH BIN



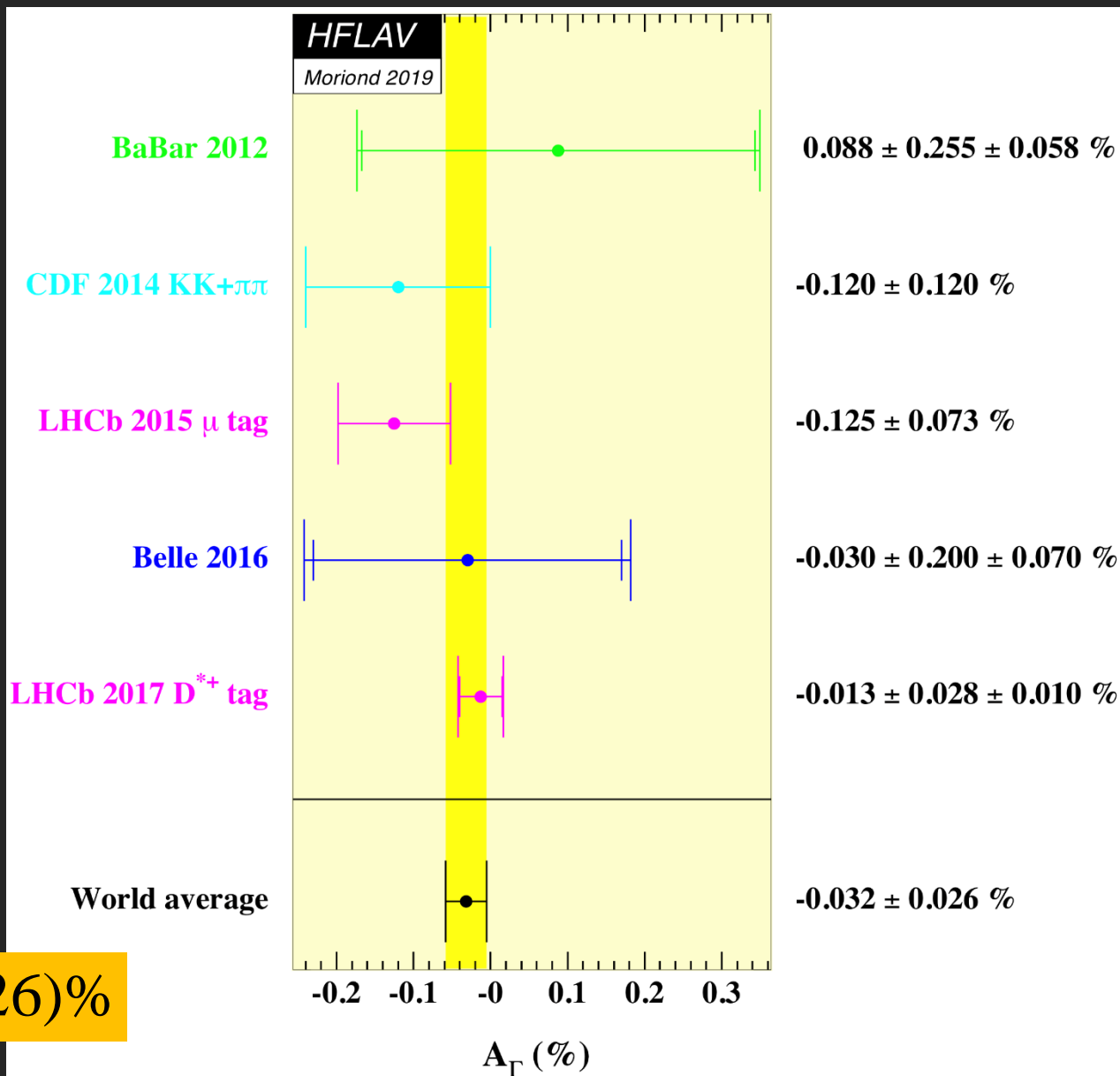
R. AAJ ET AL. (LHCb COLL.), PRL 118, 261803 (2017)



ASYMMETRY A_Γ

LHCb USING $b \rightarrow c$

LHCb USING PROMPT
 $D^{*'}S$



$A_\Gamma = (-0.032 \pm 0.026)\%$

T-INDEPENDENT METHODS

t-INTEGRATED ASYMMETRY A_{CP}

$$A_{CP}^f \equiv \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})}$$

FOR GENERAL f : $A_{CP}^f \sim A_{dir}^f + C_1 y \cos \phi + C_2 x \sin \phi$
WHY? P. 48

$f=f_{CP}$

$$A_{CP}^f \approx A_d^f - y \frac{A_d^f + A_m}{2} \cos \phi + x \sin \phi$$

MEASUREMENT INCLUDES
DETECTOR INDUCED
ASYMMETRIES
(EXAMPLE OF D^+)

$$A_{rec} = \frac{N(D^+ \rightarrow Xh^+) - N(D^- \rightarrow Xh^-)}{N(D^+ \rightarrow Xh^+) + N(D^- \rightarrow Xh^-)}$$

$|A_i| \ll 1$

$$A_{rec} = A_{CP} + A_{FB} + A_{\epsilon}^{h^+}$$

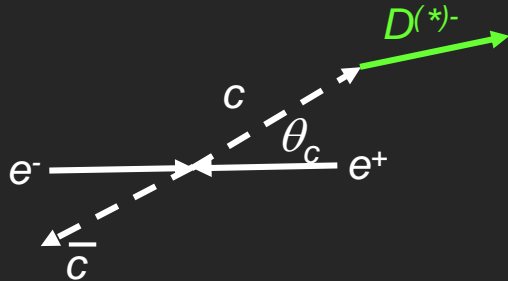
PHYSICS ASYMM.

DIFFERENCE IN h^\pm
INTERACTIONS ON
MATERIAL

FORWARD-BACKWARD
ASYMM. IN $e^+e^- \rightarrow c\bar{c}$;
VANISHES IF INTEGRATED
OVER FULL POLAR ANGLE

T-INDEPENDENT METHODS

FORWARD BACKWARD
ASYMMETRY A_{fb}



$$\frac{N_c(\cos \theta_c) - N_{\bar{c}}(\cos \theta_c)}{N_c(\cos \theta_c) + N_{\bar{c}}(\cos \theta_c)} = \frac{8A_{FB}^0 \cos \theta_c}{3(1 + \cos^2 \theta_c)}$$

$$A_{CP} = [A_{\text{rec}}^{\text{corr}}(\cos \theta^*) + A_{\text{rec}}^{\text{corr}}(-\cos \theta^*)]/2$$

$$A_{FB} = [A_{\text{rec}}^{\text{corr}}(\cos \theta^*) - A_{\text{rec}}^{\text{corr}}(-\cos \theta^*)]/2$$

$$A_{\text{rec}} = A_{CP} + A_{FB} + A_{\epsilon}^{\pi_s}$$

ϵ ASYMMETRIES

EXAMPLE OF $D^{*+} \rightarrow D^0 (\rightarrow K^+K^-, \pi^+\pi^-) \pi_s^+$
 $D^{*-} \rightarrow \bar{D}^0 (\rightarrow K^+K^-, \pi^+\pi^-) \pi_s^-$

NEED SAMPLE W/O PHYSICS ASYMM. TO CORRECT* OR TWO SAMPLES TO SUBTRACT
 $\rightarrow CF$ DECAYS

$D^{*+} \rightarrow D^0 (\rightarrow K^-\pi^+) \pi_s^+$
 $D^0 \rightarrow K^-\pi^+$

$$A_{\text{rec}}^{\text{tag}} = A_{CP}^{K\pi} + A_{FB} + A_{\epsilon}^{K\pi} + A_{\epsilon}^{\pi_s}$$

$$A_{\text{rec}}^{\text{untag}} = A_{CP}^{K\pi} + A_{FB} + A_{\epsilon}^{K\pi}.$$

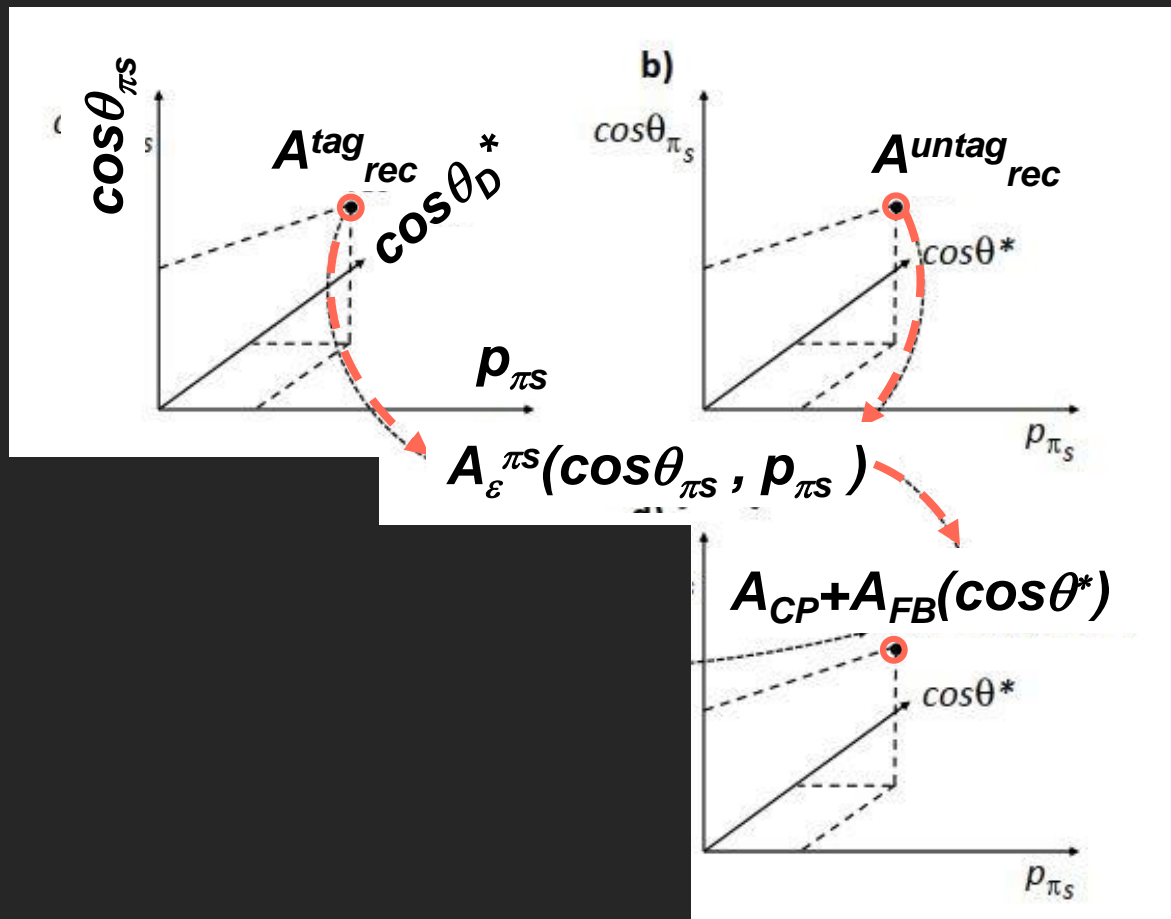
* MC TYPICALLY NOT RELIABLE AT $\leq O(\%)$

T-INDEPENDENT METHODS

ASYMMETRY $A_{\epsilon}^{\pi_S}$ DEPENDS ON
 π_S KINEMATICS \rightarrow
BINNED IN p_{π_S} , $\cos\theta_{\pi_S}$
... AND IN $\cos\theta_D^*$ WHY?

BECAUSE θ_{π_S} CORRELATED
WITH θ_D^*

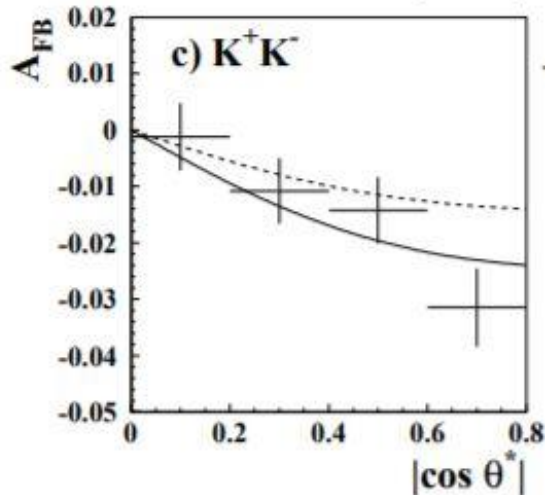
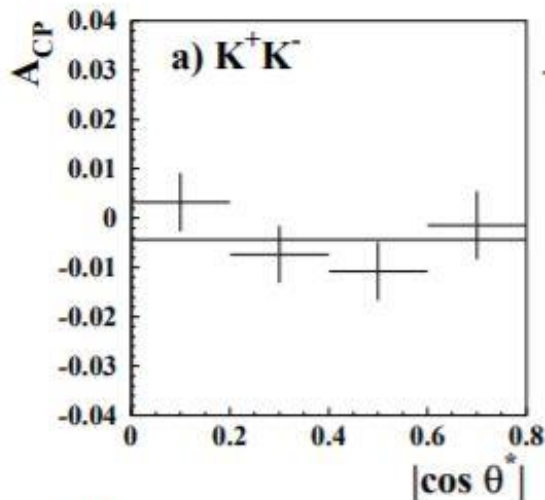
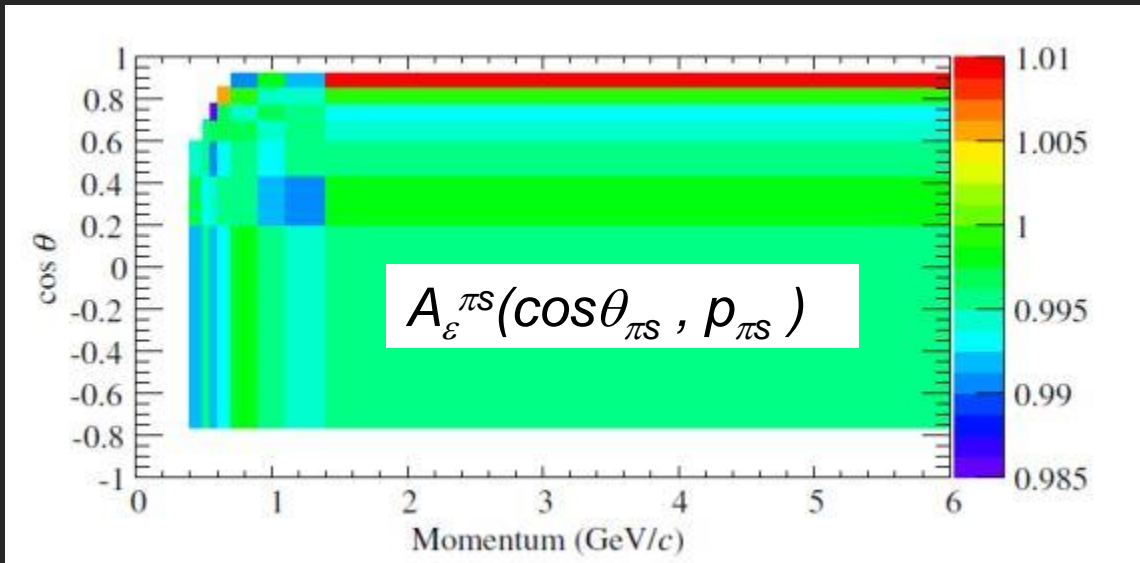
INTEGRATION OVER θ_D^* IN A
GIVEN BIN OF θ_{π_S} DOES NOT
COVER FULL θ_D^* INTERVAL \Rightarrow
DOES NOT ASSURE VANISHING
OF A_{FB}



T-INDEPENDENT METHODS

ASYMMETRIES

B. AUBERT ET AL. (BABAR COLLAB.), PRL 100, 061803 (2008)



SLIGHT DEVIATION OF DATA
FROM A_{FB} PREDICTION P. 50

$$A_{CP}^{KK} = (-0.43 \pm 0.30 \pm 0.11) \cdot 10^{-2}$$

M. STARIC ET AL. (BELLE COLLAB.), PLB 670, 190 (2008)

T-INDEPENDENT METHODS

OTHER INGENUINE METHODS TO DETERMINE UNWANTED ASYMMETRIES, E.G. LHCb:

$$\Delta A_{CP} = A_{CP}^{\bar{f}} - A_{CP}^f$$

M. SCHUBIGER, BEAUTY 2019

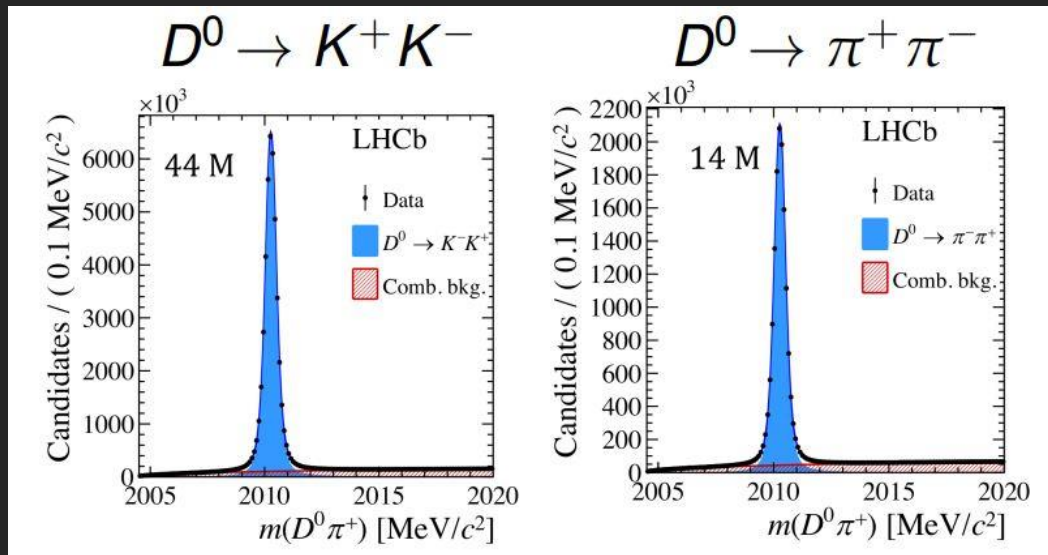
$$f = K^+ K^-, \bar{f} = \pi^+ \pi^-$$

$$A_{rec} = A_{CP} + A_{prod} + A_{\epsilon}^{\pi_s}$$

$$A_{rec}^{KK} = A_{CP}^{KK} + A_{prod} + A_{\epsilon}^{\pi_s}$$

$$A_{rec}^{\pi\pi} = A_{CP}^{\pi\pi} + A_{prod} + A_{\epsilon}^{\pi_s}$$

$$\Delta A_{rec} = A_{rec}^{KK} - A_{rec}^{\pi\pi} = A_{CP}^{KK} - A_{CP}^{\pi\pi}$$



R. AAJ ET AL. (LHCb COLLAB.), PRL 122, 211803 (2019)

T-INDEPENDENT METHODS

$$A_{rec} = A_{CP} + A_{prod} + A_{\epsilon}^{\pi_s}$$

OTHER INGENUINE METHODS TO DETERMINE UNWANTED ASYMMETRIES, E.G. LHCb:

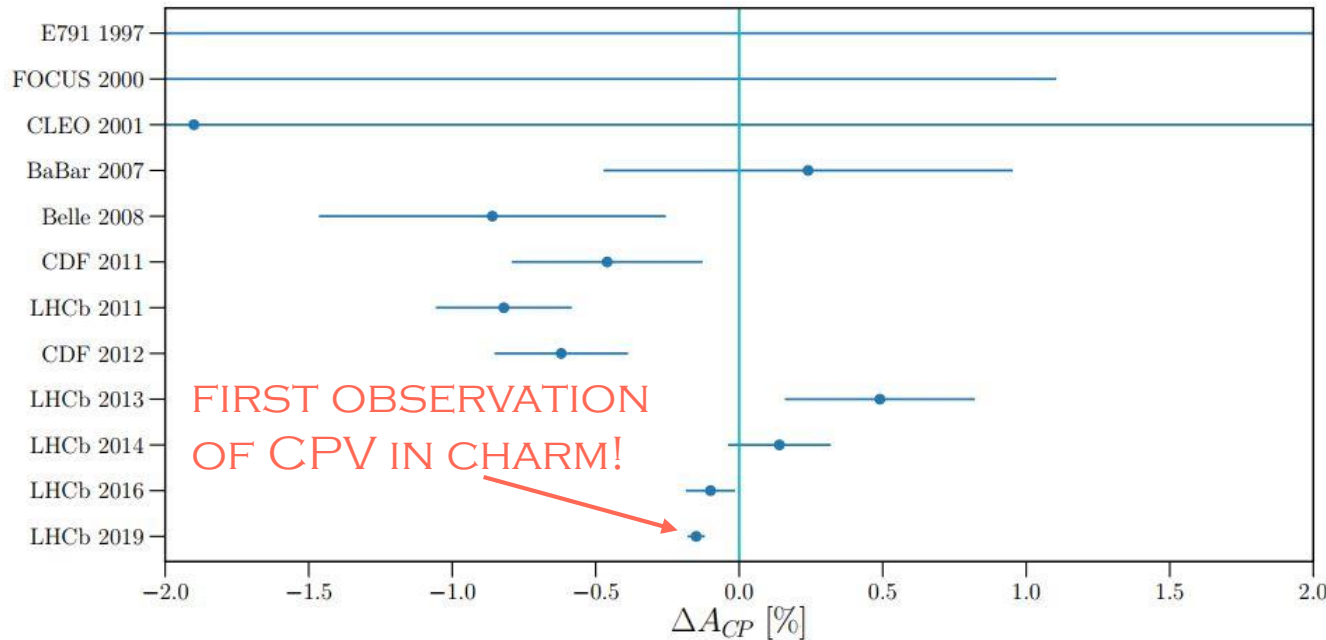
$$A_{rec}^{KK} = A_{CP}^{KK} + A_{prod} + A_{\epsilon}^{\pi_s}$$

$$A_{rec}^{\pi\pi} = A_{CP}^{\pi\pi} + A_{prod} + A_{\epsilon}^{\pi_s}$$

$$\Delta A_{rec} = A_{rec}^{KK} - A_{rec}^{\pi\pi} = A_{CP}^{KK} - A_{CP}^{\pi\pi}$$

$$\Delta A_{CP} = A_{CP}^f - A_{CP}^{\bar{f}}$$

M. SCHUBIGER, BEAUTY 2019



R. AAJ ET AL. (LHCb COLLAB.), PRL 122, 211803 (2019)

FIRST OBSERVATION OF CPV IN CHARM

$$\Delta A_{CP} = (-15.4 \pm 2.9) \cdot 10^{-4}$$

T-INDEPENDENT METHODS

OTHER INGENUINE METHODS TO DETERMINE UNWANTED ASYMMETRIES, E.G. BABAR IN $D^+ \rightarrow K_S \pi^+$:

P. DEL AMO SANCHEZ, ET AL. (BABAR COLLAB.), PRD 83, 071103 (2011)

$Y(4S) \rightarrow B\bar{B}$: STRONG INT. (NO CPV), ISOTROPIC DISTR. OF TRACKS IN B SYSTEM

THE SAME DOES NOT HOLD FOR $e^+e^- \rightarrow qq$!

USE INCLUSIVE SAMPLE OF TRACKS FROM $B\bar{B}$; DETERMINE ASYMMETRY OF π^\pm IN KINEMATIC BINS;

USE INCLUSIVE SAMPLE OF TRACKS FROM CONTINUUM; DETERMINE ASYMMETRY OF π^\pm IN KINEMATIC BINS;

DIFFERENCE IS $A_{\text{det}}(\pi^\pm \text{kinematics})$

→ APPLY CORRECTION TO MEASURED ASYMM.

$$A_{\text{rec}} = A_{CP} + \underbrace{A_{FB} + A_{\varepsilon}^{\pi^\pm} + A_{\varepsilon}^{\pi_s}}_{A_{\text{det}}}$$

NEED TO BE CAREFUL NOT TO BIAS INCLUSIVENESS BY SELECTION

COMPARISON TO PREDICTIONS

$$\Delta A_{CP} = (-15.4 \pm 2.9) \cdot 10^{-4}$$

R. AAJ ET AL. (LHCb COLLAB.), PRL 122, 211803 (2019)

DIFFICULT TO CALCULATE (ASK ALEXEY/ALEX/...)

WITHIN $SU(3)_{FLAVOR}$: $A_{CP}^{KK} \sim -A_{CP}^{\pi+\pi}$

BUT THEN AGAIN, DATA SHOW $SU(3)_{FLAVOR}$ VIOLATED AT O(30%) IN AMPLITUDES

U. NIERSTE, BEAUTY 2019

CP asymmetries of hadronic charm decays ...

... are proportional to $\text{Im} \frac{\lambda_b}{\lambda_{sd}} = -6 \cdot 10^{-4}$ in the Standard Model

... and probe **new physics** in flavour transitions of **up-type** quarks,

... are very difficult to predict in the **Standard Model**.

$$\text{Im} \left(\frac{2V_{cb}^* V_{ub}}{V_{cs}^* V_{us} - V_{cd}^* V_{ud}} \right) \sim -6 \cdot 10^{-4}$$

COMPARISON TO PREDICTIONS

SORRY, NEED TO DO (REPEAT!) A KIND JOKE:

U. NIERSTE, BEAUTY 2019

The theory community has delivered a **perfect service** to the experimental colleagues:

Every measurement hinting at some non-zero CP asymmetry was **successfully postdicted** offering interpretations both

- within the **Standard Model**
and
- as evidence for **new physics!**

And we are not stubborn at all: After new measurements we eagerly change our opinions!

COMPARISON TO PREDICTIONS

SO.....

$$A_{CP}^f \propto \text{Im} \left(\frac{2V_{cb}^* V_{ub}}{V_{cs}^* V_{us} - V_{cd}^* V_{ud}} \right) \sim -6 \cdot 10^{-4}$$

... BUT THE PREFACTOR??

USING QCD SUM RULES

A. KHODJAMIRIAN, A.A. PETROV, PLB 774, 235 (2017)

$$A_{CP}^{KK} \sim -A_{CP}^{\pi\pi}$$

$$\Delta A_{CP} \sim 2.0 \cdot 10^{-4} \pm 0.3 \cdot 10^{-4}$$

ACTUAL **PREDICTION**

$$\Delta A_{CP} = (-15.4 \pm 2.9) \cdot 10^{-4}$$

R. AAJ ET AL. (LHCb COLLAB.), PRL 122, 211803 (2019)

SIGN??

NEED FURTHER EXPERIMENTAL
INFORMATION / CLARIFICATION

$$|a_{CP}^{\text{dir}}(D^0 \rightarrow K_S K_S)| \leq 1.1\%$$

U. NIERSTE, ST. SCHACHT, PRD 92, 054036 (2015)

$$|a_{CP}^{\text{dir}}(D^0 \rightarrow \bar{K}^{*0} K_S)| \leq 0.003$$

U. NIERSTE, ST. SCHACHT, PRL 119, 251801 (2017)

SEPARATE A_{CP}^{KK} , $A_{CP}^{\pi+\pi^-}$

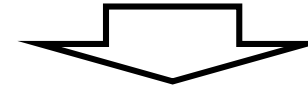
A_{CP} SUM RULES P. 52

$$D^0 \rightarrow K^+ \pi^-$$

t -DEPENDENT
RATES FITTED
SEPARATELY FOR D^0
AND \bar{D}^0

MANY PARAMETERS...

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \left[r^2 - ry' \bar{\Gamma}t + \frac{x'^2 + y'^2}{4} (\bar{\Gamma}t)^2 \right]$$



$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \left[r_+^2 - r_+ y_+ \bar{\Gamma}t + \frac{x_+'^2 + y_+'^2}{4} (\bar{\Gamma}t)^2 \right]$$

$$\frac{dN(\bar{D}^0 \rightarrow \bar{f})}{dt} \propto e^{-\bar{\Gamma}t} \left[r_-^2 - r_- y_- \bar{\Gamma}t + \frac{x_-'^2 + y_-'^2}{4} (\bar{\Gamma}t)^2 \right]$$

SIMILARLY IN
 $D^0 \rightarrow K_S \pi^+ \pi^-$
WHERE $|q/p|$ AND ϕ
ENTER DIRECTLY AS
FIT PARAMETERS

$$x'^{\pm} = \left[\frac{1 \pm A_M}{1 \mp A_M} \right]^{1/4} (x' \cos \phi \pm y' \sin \phi)$$

$$y'^{\pm} = \left[\frac{1 \pm A_M}{1 \mp A_M} \right]^{1/4} (y' \cos \phi \mp x' \sin \phi)$$

$$A_{dir}^f = \frac{r_+ - r_-}{r_+ + r_-}$$

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f} = \left| \frac{q}{p} \right| \left| \frac{\bar{A}_f}{A_f} \right| e^{i\phi}$$

AVERAGES

69 MEAS. OF
INDIVIDUAL
PARAMETERS
ENTER THE FIT;

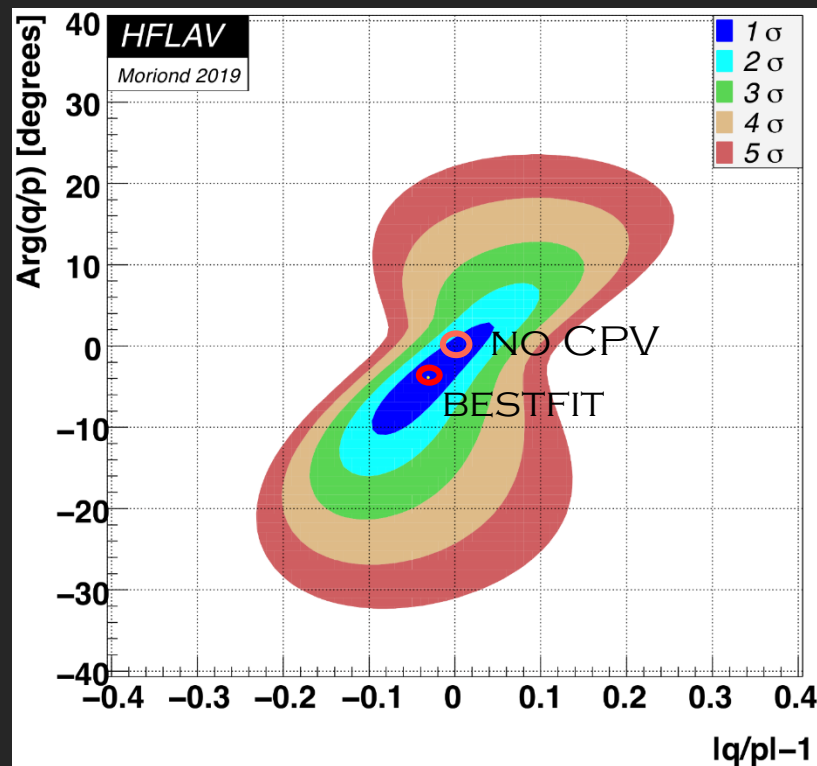
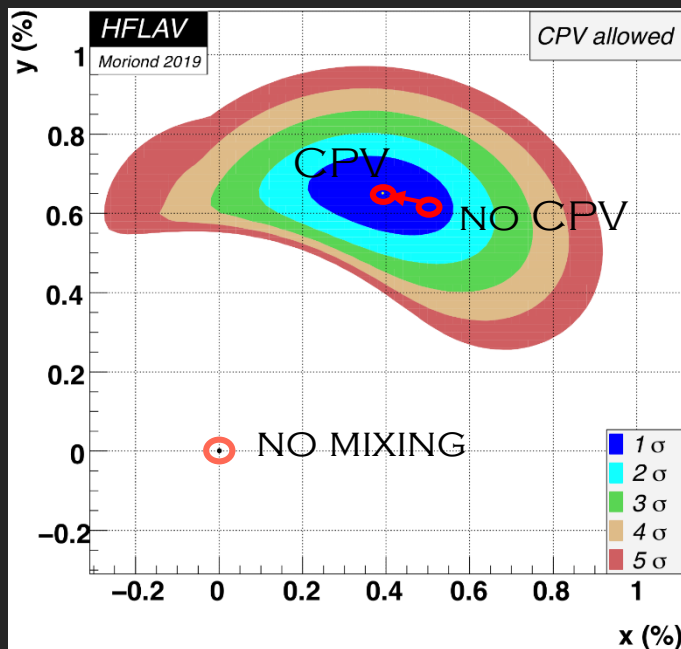
10 FREE PARAM.

$A_{dir}^{KK}, A_{dir}^{\pi\pi}$
ENTER FIT AS
INDIVIDUAL FREE
PARAMETERS;

$\chi^2/ndf \sim 1.5$

MIXING

NO CPVMIX, CPVINT



DETAILS
P. 54

NO CPVDEC

$$A_{dir}^{KK} = -0.09 \pm 0.16 \quad A_{dir}^{\pi\pi} = 0.06 \pm 0.16$$

$$\delta_{K\pi} = 26^\circ \pm \begin{matrix} 23^\circ \\ 24^\circ \end{matrix}$$

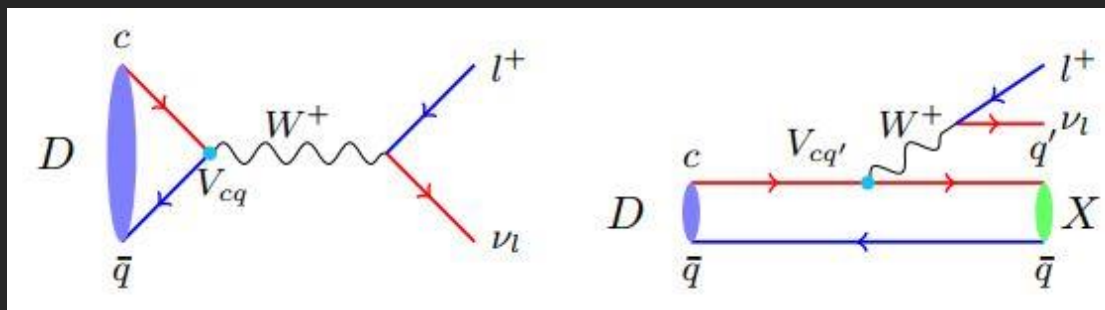
$$x = (0.39 \pm \begin{matrix} 0.11 \\ 0.12 \end{matrix})\%$$

$$y = (0.65 \pm \begin{matrix} 0.06 \\ 0.07 \end{matrix})\%$$

$$\left| \frac{q}{p} \right| = 0.97 \pm 0.05$$

$$\phi = -3.9^\circ \pm \begin{matrix} 4.5^\circ \\ 4.6^\circ \end{matrix}$$

(SEMI)LEPTONIC DECAYS



L. ZHANG, BEAUTY 2019

BES III

DOUBLE TAG
METHOD

$e^+ e^- \rightarrow \psi(3770) \rightarrow D^- D^+$ $e^+ e^- \rightarrow \psi(4160) \rightarrow D_s^- D_s^+$

TAG SIDE:

SIGNAL SIDE:

@ $E_{cm} = 3.773\text{GeV} \Rightarrow \mathcal{B}_{sig} = \frac{N_{sig}}{\sum_{\alpha} N_{tag}^{\alpha} \epsilon_{tag,sig}^{\alpha} / \epsilon_{tag}^{\alpha}}$

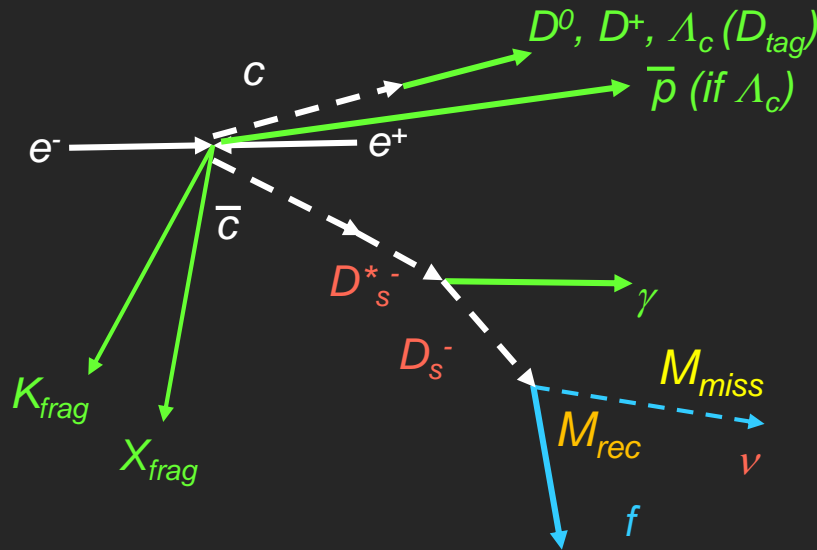
@ $E_{cm} = 4.178\text{GeV} \Rightarrow \mathcal{B}_{sig} = \frac{N_{sig}}{\mathcal{B}(D_s^* \rightarrow \gamma D_s) \sum_{\alpha} N_{tag}^{\alpha} \epsilon_{tag,sig}^{\alpha} / \epsilon_{tag}^{\alpha}}$

A. ZUPANC ET AL. (BELLE COLL.), JHEP 09, 139 (2013)

(SEMI)LEPTONIC DECAYS

B-FACTORY METHOD

$$N_{sig}(M_{miss}) / [\epsilon(f) N_{sig}(M_{rec})] = Br(D_s \rightarrow f)$$



(SEMI)LEPTONIC DECAYS

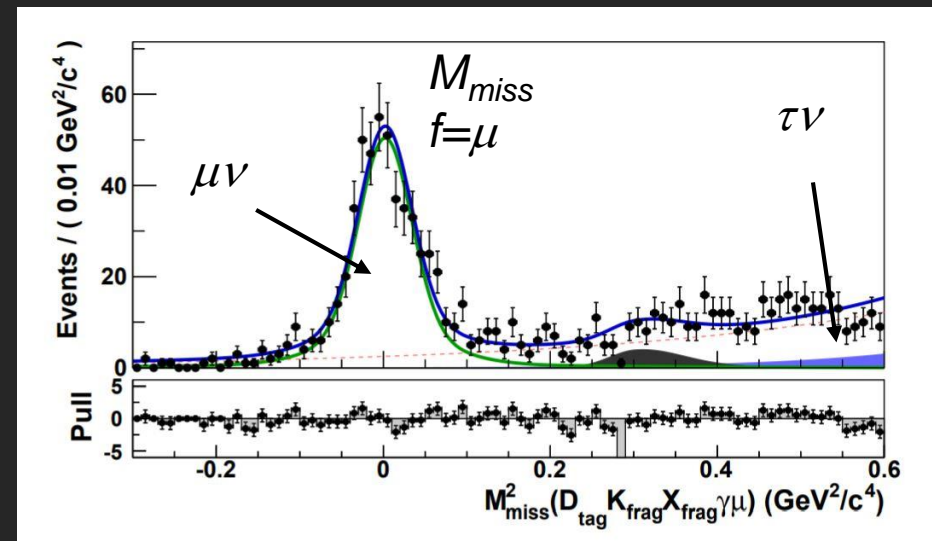
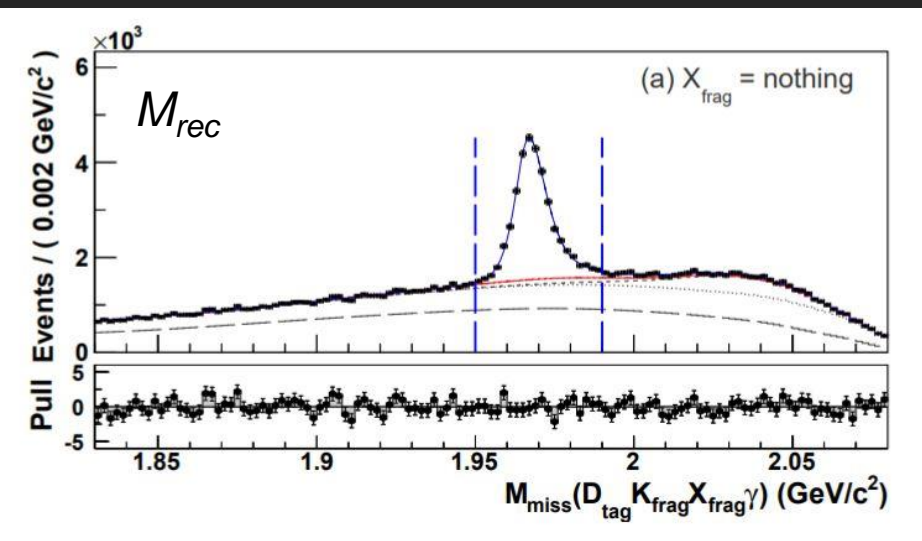
B-FACTORY METHOD

$$\mathcal{B}(D_s^+ \rightarrow \ell^+ \nu_\ell) = \frac{\tau_{D_s} m_{D_s}}{8\pi} f_{D_s}^2 G_F^2 |V_{cs}|^2 m_\ell^2 \left(1 - \frac{m_\ell^2}{m_{D_s}^2}\right)^2$$

$$N_{sig}(M_{miss}) / [\varepsilon(f) N_{sig}(M_{rec})] = Br(D_s \rightarrow f)$$

LEPTONIC DECAYS:

A. ZUPANC ET AL. (BELLE COLL.), JHEP 09, 139 (2013)

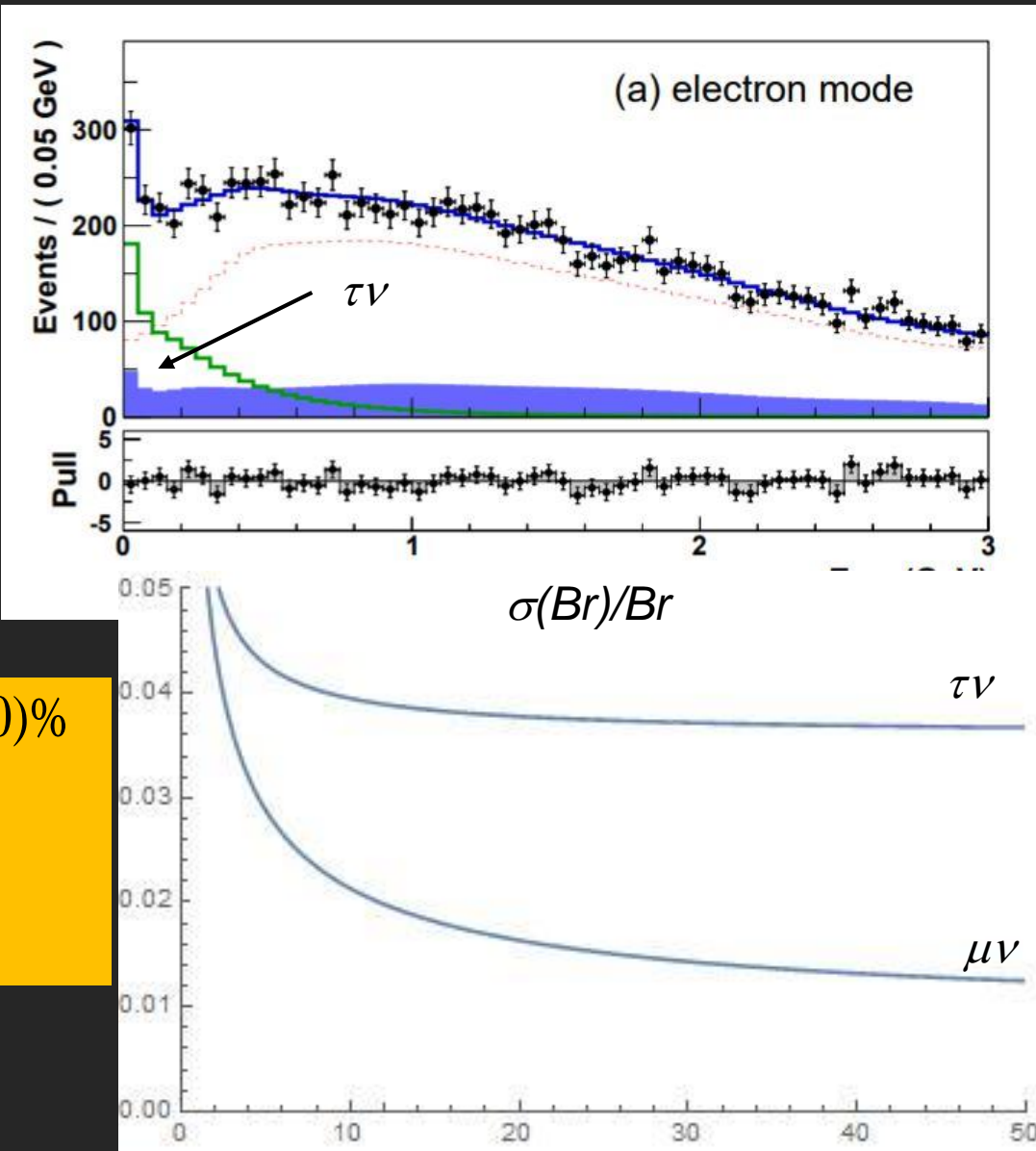


MORE P. 57

(SEMI)LEPTONIC DECAYS

B-FACTORY
METHOD

FOR $\tau\nu$ BESIDE M_{MISS} ALSO
 E_{ECL} EXPLOITED

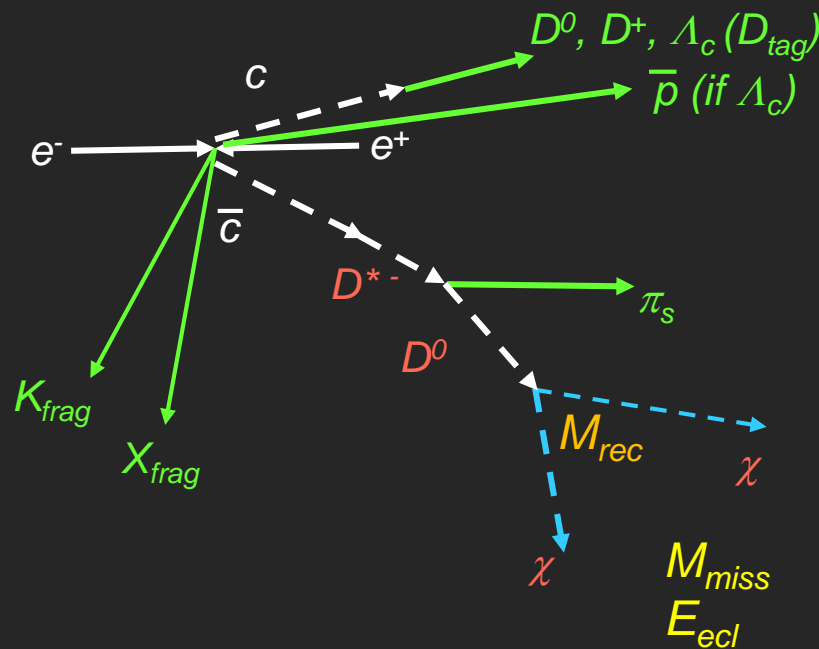


$Br(D_s \rightarrow \mu\nu) = (0.531 \pm 0.028 \pm 0.020)\%$
 $Br(D_s \rightarrow \tau\nu) = (5.70 \pm 0.21 \pm_{0.30}^{0.31})\%$
 $f_{D_s} = (255.5 \pm 4.2 \pm 5.1) \text{ MeV}$

(SEMI)LEPTONIC DECAYS

B-FACTORY

METHOD CAN BE USED FOR D^0/D_S
DECAYS TO INVISIBLE FINAL STATE



SENSITIVITY P. 59

BESIII LEPTONIC DECAYS

$$D_s \rightarrow \mu \nu$$

$$Br(D_s \rightarrow \mu \nu) = (0.549 \pm 0.016 \pm 0.015)\%$$

$$R_{\tau/\mu} = \frac{Br^{PDG}(D_s \rightarrow \tau \nu)}{Br(D_s \rightarrow \mu \nu)} = 9.98 \pm 0.52$$

$$R_{\tau/\mu}^{SM} = 9.76 \pm 0.03$$

SEVERAL IMPORTANT SOURCES OF SYS.
UNCERTAINTIES:

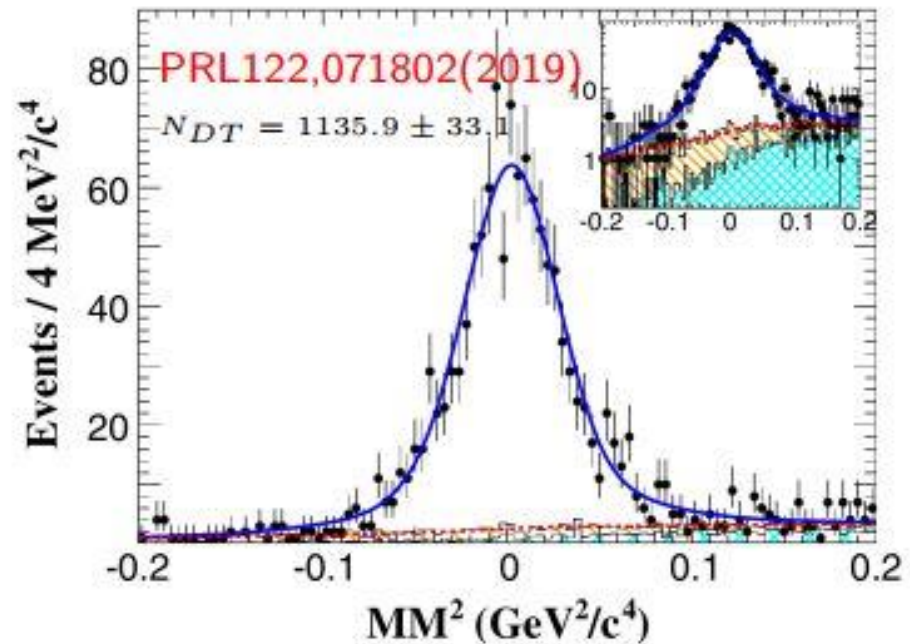
ε_γ ON SIGNAL SIDE $\sim 1\%$

AMOUNT OF BKG. WITH UNMATCHED γ ON SIGNAL SIDE $\sim 1\%$

CONTRIB. OF D_s RADIATIVE DECAYS ($D_s \rightarrow \mu \nu \gamma$) $\sim 1\%$

IF TOTAL UNCERTAINTY SCALABLE: $\sigma(BR)/BR \sim 0.024\%$ WITH 10 FB^{-1}
SAME AS TOTAL UNCERTAINTY AT BELLE II @ 7 AB^{-1}

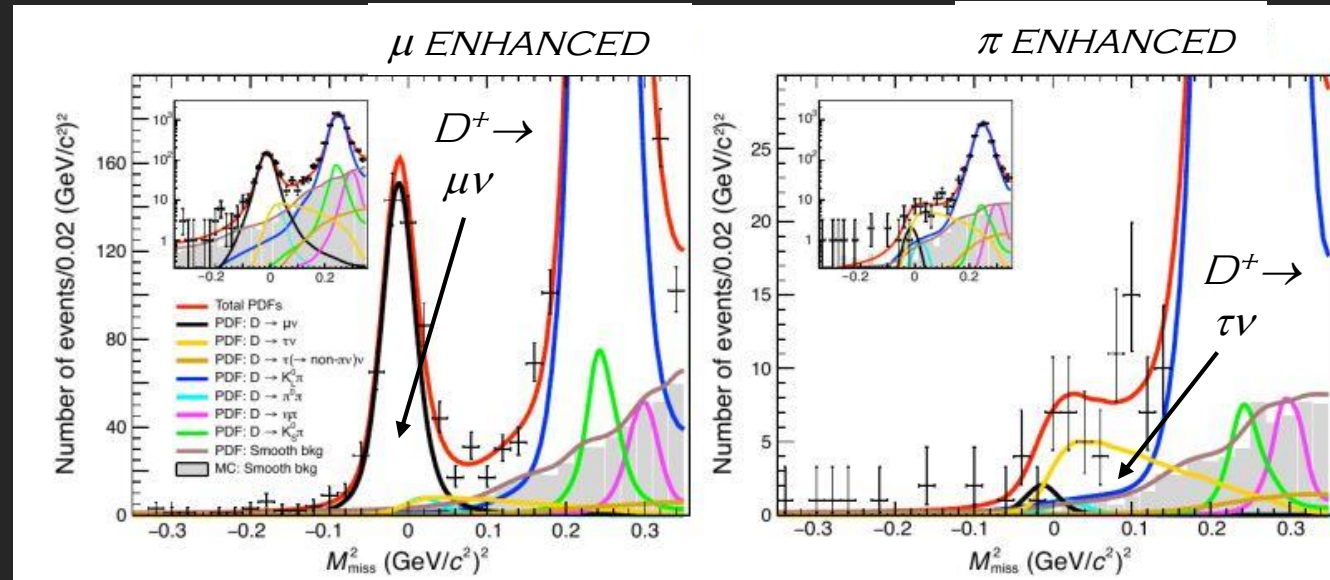
M. ABLIKIM ET AL. (BESIII COLL.), PRL 122, 071802 (2019)



BESIII LEPTONIC DECAYS

$$D^+ \rightarrow \tau(\rightarrow \pi\nu)\nu$$

LARGEST SOURCES OF
SYS. UNCERTAINTY:
 $BR(D^+ \rightarrow \mu\nu) \sim 7\%$
BKG. SHAPE $\sim 4\%$



FIRST OBSERVATION

$$Br(D^+ \rightarrow \tau\nu) = (0.120 \pm 0.024 \pm 0.012)\%$$

$$R_{\tau/\mu} = \frac{Br^{PDG}(D^+ \rightarrow \tau\nu)}{Br(D^+ \rightarrow \mu\nu)} = 3.21 \pm 0.64 \pm 0.43$$

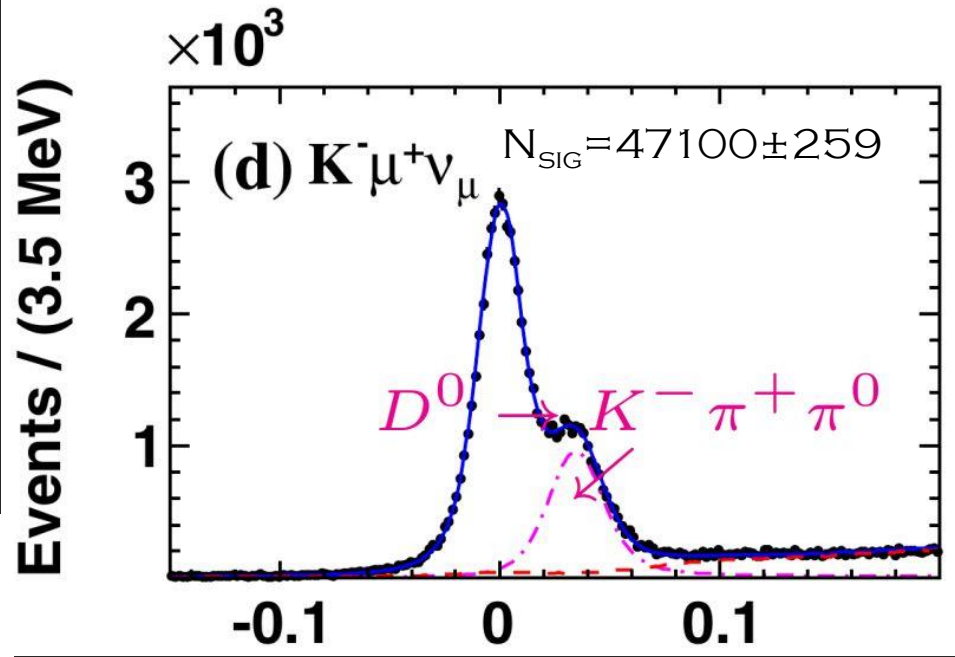
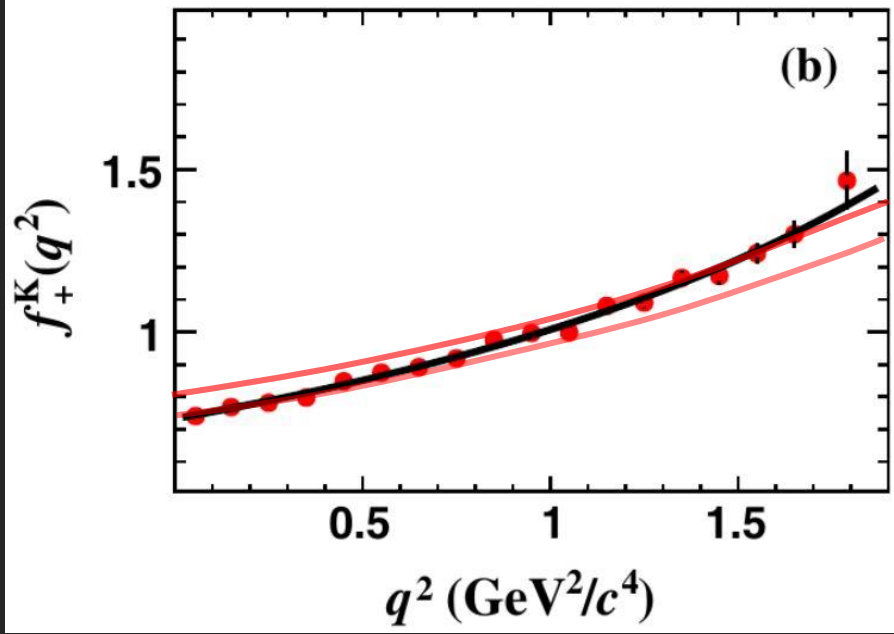
$$R_{\tau/\mu}^{SM} = 2.67$$

BESIII SEMILEPTONIC DECAYS

$$D^0 \rightarrow K^- \mu^+ \nu$$

$$\frac{d\Gamma(D^0 \rightarrow P^- \ell^+ \nu_\ell)}{dq^2} = |V_{cQ}|^2 \frac{G_F^2}{24\pi^3} \frac{(q^2 - m_\ell^2)^2 \sqrt{E_P^2 - m_P^2}}{q^4 m_{D^0}^2} \left(1 + \frac{m_\ell^2}{2q^2}\right) m_{D^0} (E_P^2 - m_P^2) |f_+(q^2)|^2$$

FORM FACTOR $f_+(q^2)$



$$U_{\text{miss}} \equiv E_{\text{miss}} - |\vec{p}_{\text{miss}}|$$

$$E_{\text{miss}} \equiv E_{\text{beam}} - E_{K^-} - E_{\mu^+}$$

BELLE II @ 50 AB⁻¹ USING METHOD FOR
 $D_s \rightarrow \mu \nu$ PROBABLY LOWER STATISTICS
THAN BES III WITH 10 FB⁻¹ P. 60
COMPARISON TO LQCD

$$D^0 \rightarrow V\gamma$$

RADIATIVE DECAYS $D^0 \rightarrow V\gamma$

$$V = \rho^0, \phi, K^{*0}$$

T. NANUT ET AL. (BELLE COLL.), PRL 118, 051801 (2017)

IMPROVED MEAS. OF BR'S, INCL.

1ST OBSERVATION OF

$$D^0 \rightarrow \rho^0\gamma$$

NP COULD ENHANCE

$$A_{CP}(D^0 \rightarrow V\gamma) \sim O(0.1)$$

G. ISIDORI, J.F. KAMENIK, PRL 109, 171801 (2012)

J. LYON, R. ZWICKY, ARXIV:1210.6546

S. DE BOER, G. HILLER, JHEP08 (2017) 091

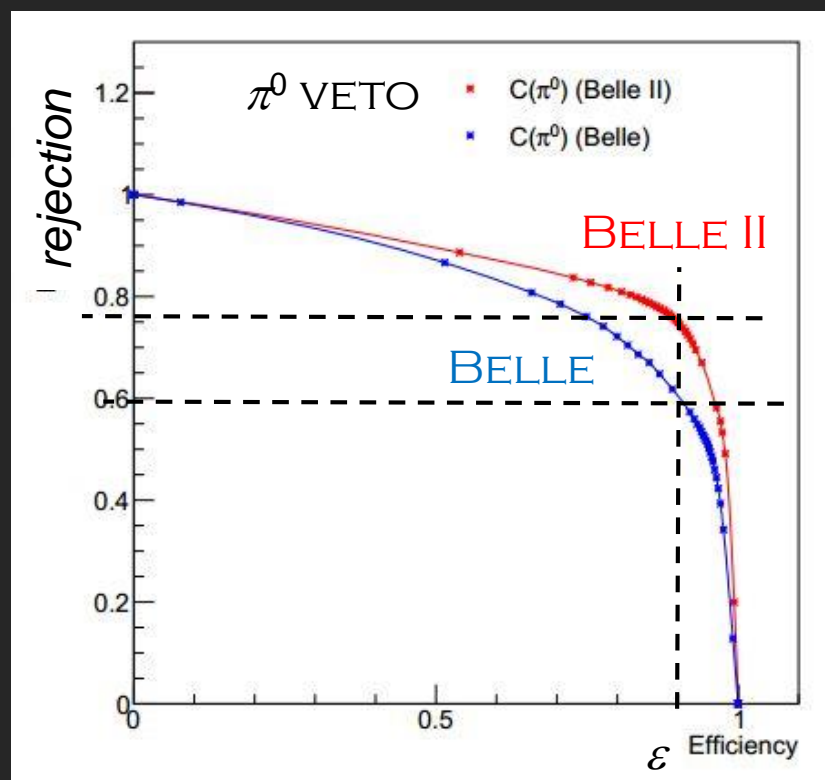
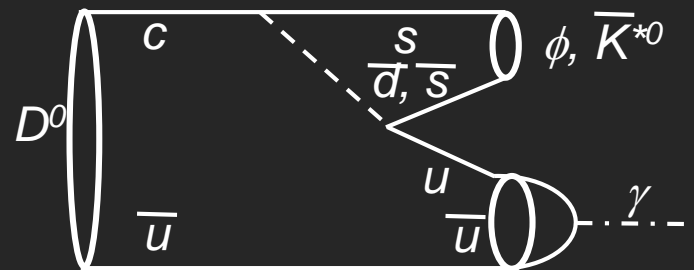
FIRST MEAS'S OF A_{CP}

$$\text{MAIN BKG. } D^0 \rightarrow h^+h^-\pi^0 (\rightarrow \gamma\gamma)$$

IMPORTANT $\pi^0 (\rightarrow \gamma\gamma)$ VETO TO REDUCE

BACKGROUNDS

NN VETO



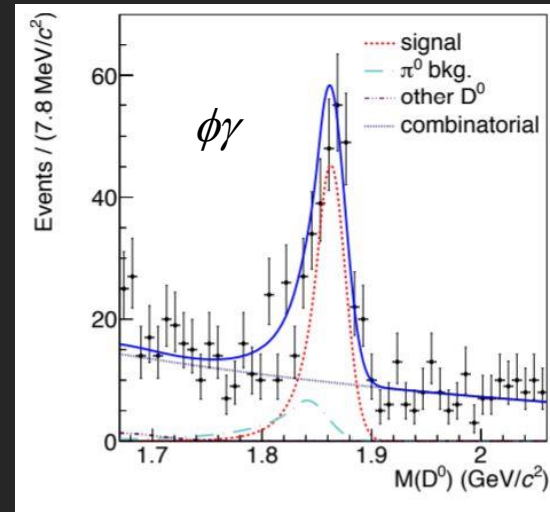
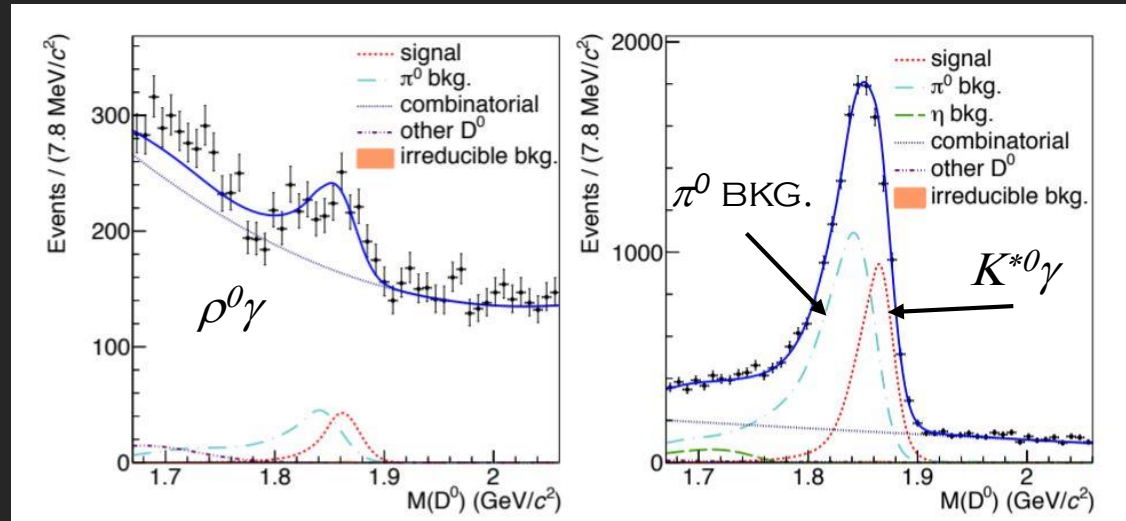
BR AND CPV

T. NANUT ET AL. (BELLE COLL.), PRL 118, 051801 (2017)

RADIATIVE DECAYS $D^0 \rightarrow V\gamma$
 $V = \rho^0, \phi, K^{*0}$

HELICITY ANGLE AND $M(D^0)$
TO ISOLATE SIGNAL

BR (AND A_{CP}) DETERMINED
W.R.T. NORMALIZATION MODES
 $\pi^+\pi^-, K^+K^-, K^-\pi^+$



$$\mathcal{B}(D^0 \rightarrow \rho^0\gamma) = (1.77 \pm 0.30 \pm 0.07) \times 10^{-5},$$

$$\mathcal{B}(D^0 \rightarrow \phi\gamma) = (2.76 \pm 0.19 \pm 0.10) \times 10^{-5},$$

$$\mathcal{B}(D^0 \rightarrow \bar{K}^{*0}\gamma) = (4.66 \pm 0.21 \pm 0.21) \times 10^{-4}.$$

CALCULATIONS $(0.1 - 1) \cdot 10^{-5}$ $\rho^0\gamma$
 $(0.1-2) \cdot 10^{-5}$ $\phi\gamma$
 $10 \times \phi\gamma$ $K^{*0}\gamma$

S. DE BOER, G. HILLER, JHEP08 (2017) 091

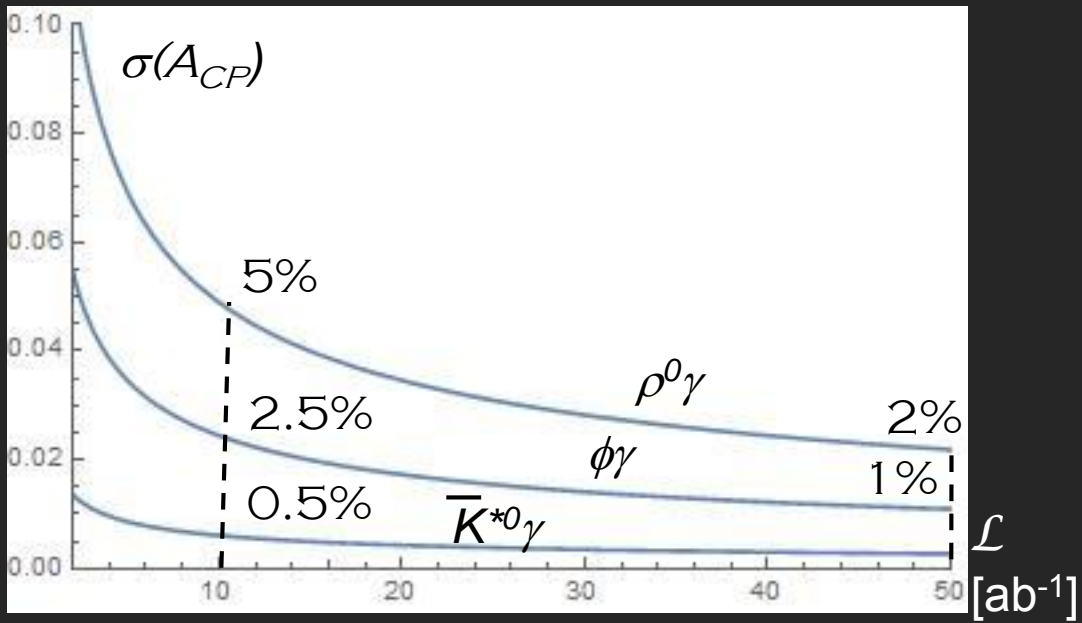
BR AND CPV

RADIATIVE DECAYS $D^0 \rightarrow V\gamma$
 $V = \rho^0, \phi, K^{*0}$

ASYMMETRIES OTHER THAN A_{CP}
CANCELED BY NORMALIZATION
MODES

$$\mathcal{A}_{CP}^{\text{sig}} = A_{\text{raw}}^{\text{sig}} - A_{\text{raw}}^{\text{norm}} + \mathcal{A}_{CP}^{\text{norm}}$$

$$\begin{aligned} \mathcal{A}_{CP}(D^0 \rightarrow \rho^0 \gamma) &= +0.056 \pm 0.152 \pm 0.006, \\ \mathcal{A}_{CP}(D^0 \rightarrow \phi \gamma) &= -0.094 \pm 0.066 \pm 0.001, \\ \mathcal{A}_{CP}(D^0 \rightarrow \bar{K}^{*0} \gamma) &= -0.003 \pm 0.020 \pm 0.000, \end{aligned}$$



u, d

1968 ISOSPIN VIOLATED
(ENLARGED TO $SU(3)_{\text{FLAVOR}}$)

PREDICTED BY M. GELL-MANN,
G. ZWEIG

s

1964 CP VIOLATED

NOT PREDICTED

b

2001 LARGE CP VIOLATION

PREDICTED BY M. KOBAYASHI,
T. MASKAWA

c

????

NOT PREDICTED

REMEMBER THE WORDS BY KARIM: „CHARM IS THE NEW BEAUTY!“

METHOD OF STRONG PHASE DIFFERENCE D^0 / \bar{D}^0 DETERM. USING COHERENT PRODUCTION OF D MESON PAIRS J. LIBBY ET AL. (CLEO-C COLL.), PRD 82,112006 (2010)

$\psi(3770) (CP = +1) \rightarrow D_1 D_2;$

if $D_1 \rightarrow CP+ \Rightarrow D_2$ is $CP-$; (CP-TAGGED)

$$CP = CP(D_1)CP(D_2)(-1)^{\ell=1}$$

if $D_1 \rightarrow D^0 \rightarrow f_{flav} \Rightarrow D_2$ is \bar{D}^0 (FLAVOR-TAGGED)

EVTS IN BIN i FOR FLAVOR TAGGED (D^0) DECAY:

$$K_i = A_D \int_i |f_D(m_+^2, m_-^2)|^2 dm_+^2 dm_-^2 = A_D F_i \quad (\text{SAME FOR } \bar{D}^0 \text{ WITH } m_+ \leftrightarrow m_-)$$

J. LIBBY ET AL. (CLEO-C COLL.), PRD 82,112006 (2010)

DALITZ DIST. FOR CP TAGGED (CP_+ , CP_-) DECAYS

$$f_{CP_{\pm}}(m_+^2, m_-^2) = \frac{1}{\sqrt{2}} [f_D(m_+^2, m_-^2) \pm f_D(m_-^2, m_+^2)]$$

EVTS IN BIN i

FOR CP TAGGED (CP_+ , CP_-) DECAY:

$$M_i^{\pm} = h_{CP_{\pm}} (K_i \pm 2c_i \sqrt{K_i K_{-i} + K_{-i}})$$

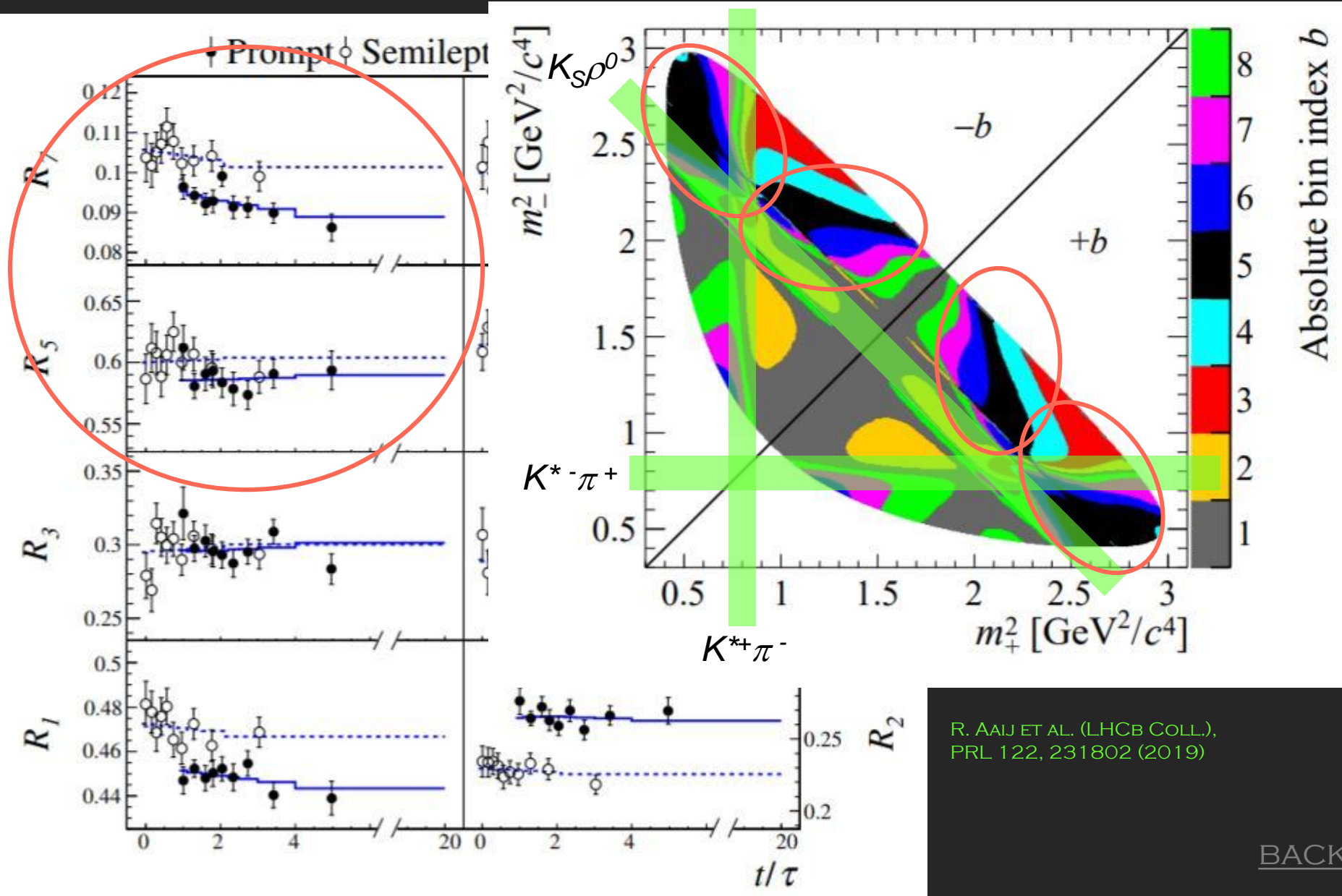
FLAVOR-TAGGED:

$$K_i = A_D \int_i |f_D(m_+^2, m_-^2)|^2 dm_+^2 dm_-^2 = A_D F_i$$

$$c_i \equiv \frac{1}{\sqrt{F_i F_{-i}}} \int_i |f_D(m_+^2, m_-^2)| |f_D(m_-^2, m_+^2)| \cos[\Delta\delta_D(m_+^2, m_-^2)] dm_+^2 dm_-^2$$

$$s_i \equiv \frac{1}{\sqrt{F_i F_{-i}}} \int_i |f_D(m_+^2, m_-^2)| |f_D(m_-^2, m_+^2)| \sin[\Delta\delta_D(m_+^2, m_-^2)] dm_+^2 dm_-^2$$

[BACK](#)



R. AAJ ET AL. (LHCb COLL.),
PRL 122, 231802 (2019)

[BACK](#)

CPV PARAMETRIZATION

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f} = \left| \frac{q}{p} \right| \left| \frac{\bar{A}_f}{A_f} \right| e^{i\varphi}$$

$$A_m = \left| \frac{q}{p} \right|^2 - 1 \quad A_{dir}^f = \frac{|\bar{A}_f|^2}{|A_f|^2} - 1$$

QUANTITY MEASURED BY B FACTORIES

$$\frac{dN(D^0 \rightarrow f)}{dt} \approx |A_f|^2 e^{-(1+y_D)\bar{\Gamma}t} \quad y_D \approx \eta_f \left(1 + \frac{A_{dir}^f + A_m}{2} \right) (y \cos \varphi - x \sin \varphi)$$

$$\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \approx |\bar{A}_f|^2 e^{-(1+y_{\bar{D}})\bar{\Gamma}t} \quad y_{\bar{D}} \approx \eta_f \left(1 - \frac{A_{dir}^f + A_m}{2} \right) (y \cos \varphi + x \sin \varphi)$$

$$y_{CP} = \frac{y_D + y_{\bar{D}}}{2} \approx \eta_f \left[y \cos \varphi - \left(\frac{A_{dir}^f + A_m}{2} \right) x \sin \varphi \right]$$

$$A_{\Gamma} = \frac{\tau_{\bar{D}} - \tau_D}{\tau_{\bar{D}} + \tau_D} \approx \frac{y_D - y_{\bar{D}}}{2} \approx \eta_f \left[\left(\frac{A_{dir}^f + A_m}{2} \right) y \cos \varphi - x \sin \varphi \right]$$

BACK

CPV PARAMETRIZATION

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f} = \left| \frac{q}{p} \right| \left| \frac{\bar{A}_f}{A_f} \right| e^{i\phi}$$

$$A_m = \left| \frac{q}{p} \right|^2 - 1 \quad A_{dir}^f = \frac{|\bar{A}_f|^2}{|A_f|^2} - 1$$

QUANTITY MEASURED BY LHCb



$$\frac{\left(\frac{dN(D^0 \rightarrow f)}{dt} \right) - \left(\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \right)}{\left(\frac{dN(D^0 \rightarrow f)}{dt} \right) + \left(\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \right)} \approx A_{dir}^f - \tilde{A}_\Gamma \bar{\Gamma} t$$

$$\tilde{A}_\Gamma = \left(\frac{A_m - A_{dir}^f}{2} \right) y \cos \phi - x \sin \phi = A_\Gamma - A_{dir}^f y \cos \phi$$

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CPV PARAMETRIZATION

$$\left(\frac{dN(D^0 \rightarrow f)}{dt} \right) - \left(\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \right) = \left(A_{dir}^f - \tilde{A}_\Gamma \bar{\Gamma} t \right) \left[\left(\frac{dN(D^0 \rightarrow f)}{dt} \right) + \left(\frac{dN(\bar{D}^0 \rightarrow f)}{dt} \right) \right]$$

$$\int_0^\infty \frac{dN(D^0 \rightarrow f)}{dt} dt = \int_0^\infty |A_f|^2 e^{-\bar{\Gamma}t} (1 + y_D \bar{\Gamma}t) dt = |A_f|^2 \bar{\tau} (1 + y_D)$$

$$\int_0^\infty \frac{dN(\bar{D}^0 \rightarrow f)}{dt} dt = \int_0^\infty |\bar{A}_f|^2 e^{-\bar{\Gamma}t} (1 + y_{\bar{D}} \bar{\Gamma}t) dt = |\bar{A}_f|^2 \bar{\tau} (1 + y_{\bar{D}})$$

$$\int_0^\infty t \frac{dN(D^0 \rightarrow f)}{dt} dt = \int_0^\infty |A_f|^2 e^{-\bar{\Gamma}t} (t + y_D \bar{\Gamma}t^2) dt = |A_f|^2 \bar{\tau}^2 (1 + 2y_D)$$

$$\int_0^\infty t \frac{dN(\bar{D}^0 \rightarrow f)}{dt} dt = \int_0^\infty |\bar{A}_f|^2 e^{-\bar{\Gamma}t} (t + y_{\bar{D}} \bar{\Gamma}t^2) dt = |\bar{A}_f|^2 \bar{\tau}^2 (1 + 2y_{\bar{D}})$$

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t-INTEGRATED CPV

$$A_{CP}^f \equiv \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})}$$

FOR GENERAL *f*: $A_{CP}^f \sim A_{dir}^f + C_1 y \cos \phi + C_2 x \sin \phi$

$f=f_{CP}$

$$A_{CP}^f \approx A_d^f - y \frac{A_d^f + A_m}{2} \cos \phi + x \sin \phi$$

WHY IN CHARM SISTEM T-INTEGRATED ASYMMETRY (A_{CP}) BESIDE DIRECT RECEIVES CONTRIB. FROM INDIRECT CPV, WHILE IN B SISTEM @ B-FACTORIES ONLY DIRECT CPV CONTRIBUTES?

NO *y* TERM BECAUSE $y \propto \Delta\Gamma$ NEGLIGIBLE IN B_d SYSTEM;

x TERM: IMPORTANT DIFFERENCE IN PRODUCTION OF $B\bar{B}$ AND $C\bar{C}$ PAIRS: FORMER QUANTUM ENTANGLED \Rightarrow NOT *t*- BUT Δt -DEPENDENCE OF RATES:

$$\begin{aligned} \frac{d\Gamma(P^0 \rightarrow f_{CP})}{d(\Delta t)} &= \frac{1}{2} |A_f|^2 (1 + |\lambda|^2) \mathcal{N} e^{-\Gamma|\Delta t|} \left[1 + \frac{1 - |\lambda|^2}{1 + |\lambda|^2} \cos(\Delta m \Delta t) - 2 \frac{\text{Im}(\lambda)}{1 + |\lambda|^2} \sin(\Delta m \Delta t) \right] \\ \frac{d\Gamma(\bar{P}^0 \rightarrow f_{CP})}{d(\Delta t)} &= \frac{1}{2} |A_f|^2 (1 + |\lambda|^2) \left| \frac{p}{q} \right|^2 \mathcal{N} e^{-\Gamma|\Delta t|} \left[1 - \frac{1 - |\lambda|^2}{1 + |\lambda|^2} \cos(\Delta m \Delta t) + \right. \\ &\quad \left. + 2 \frac{\text{Im}(\lambda)}{1 + |\lambda|^2} \sin(\Delta m \Delta t) \right] . \end{aligned} \tag{3.46}$$

t-INTEGRATED CPV

CHARM HADRONS PRODUCED IN FRAGMENTATION, NOT ENTANGLED,
t-DEPENDENT RATE;
 INTEGRATION OVER Δt FOR *B* PAIRS
 $[-\infty, \infty]$:

PART $\propto \text{Im}(\lambda)$ VANISHES!

FOR CHARM MESONS INTEGRATION
 OVER $t [0, \infty]$:

PART $\propto \text{Im}(\lambda)$ IS PROPORTIONAL TO
 Δm ($\sim x$), DOES NOT VANISH;
 \Rightarrow TERM WITH $x \sin\phi$ IN A_{CP} !

$$\int_{-\infty}^{\infty} e^{-\Gamma|\Delta t|} \cos(\Delta m \Delta t) d(\Delta t) = \frac{2\Gamma}{\Gamma^2 + \Delta m^2}$$

$$\int_{-\infty}^{\infty} e^{-\Gamma|\Delta t|} \sin(\Delta m \Delta t) d(\Delta t) = 0$$

$$\int_0^{\infty} e^{-\Gamma|\Delta t|} \cos(\Delta m \Delta t) d(\Delta t) = \frac{\Gamma}{\Gamma^2 + \Delta m^2}$$

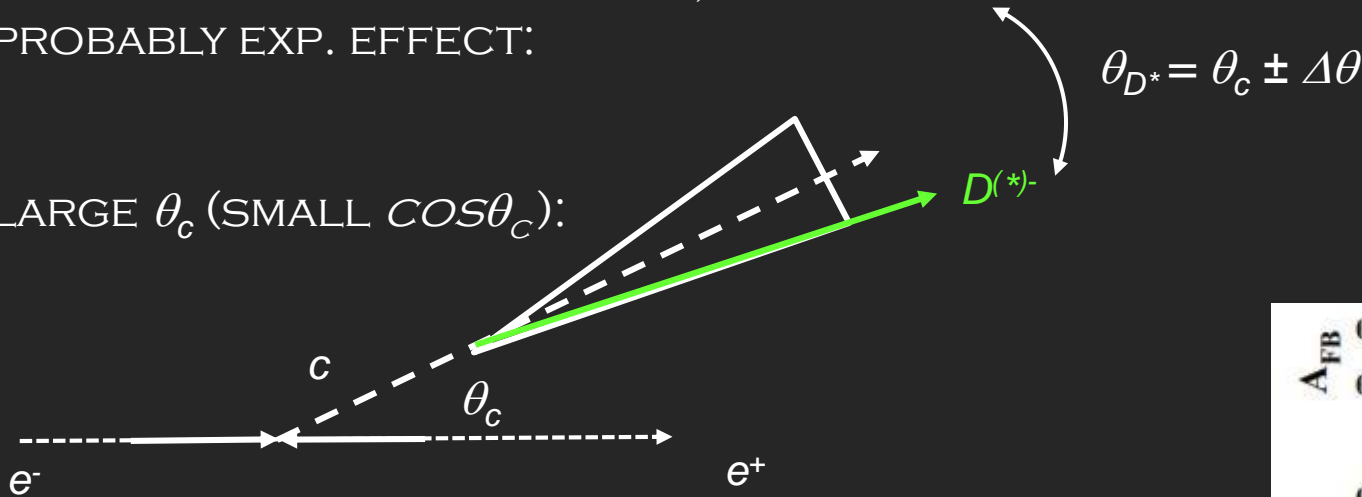
$$\int_0^{\infty} e^{-\Gamma|\Delta t|} \sin(\Delta m \Delta t) d(\Delta t) = \frac{\Delta m}{\Gamma^2 + \Delta m^2}$$

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t-INTEGRATED CPV

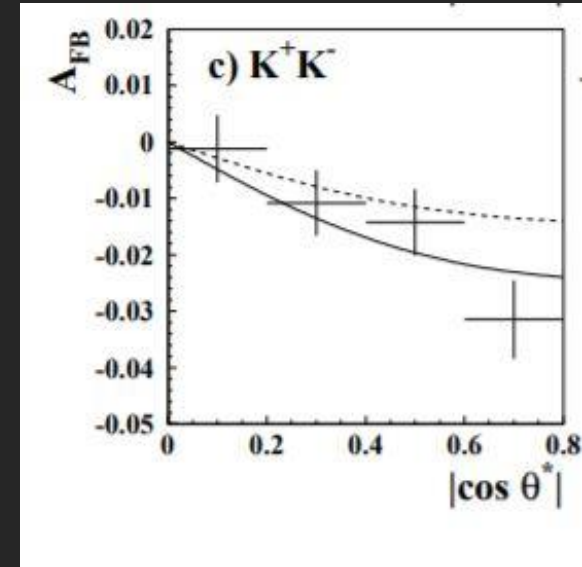
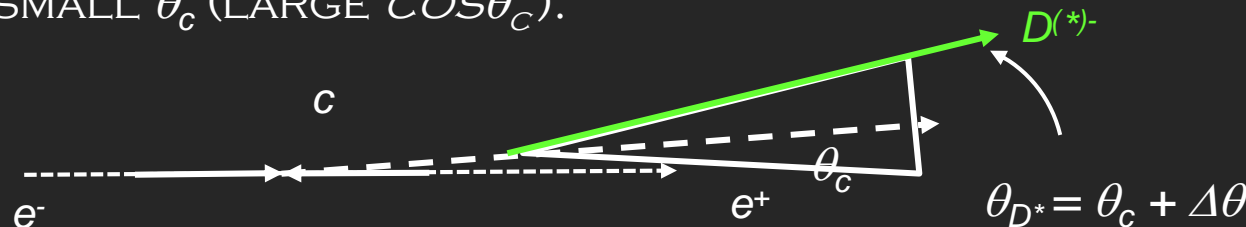
SLIGHT DEVIATION OF DATA FROM AFB PREDICTION
OBSERVED IN SEVERAL MEAS' S;
PROBABLY EXP. EFFECT:

LARGE θ_c (SMALL $\cos\theta_c$):



AT SMALL θ_c ANY
DEVIATION OF θ_{D^*}
FROM θ_c CAN ONLY
BE IN DIREVTION
OF LARGER
POLAR ANGLE

SMALL θ_c (LARGE $\cos\theta_c$):



INTERESTING ASYMMETRIES

SUM RULES FOR A_{CP} [S. MÜLLER ET AL., PRL 115, 251802 \(2015\)](#)
RELATING

$$1) D^0 \rightarrow K^+K^-, \pi^+\pi^-, \pi^0\pi^0$$

$$2) D^+ \rightarrow K^0K^+, D_s^+ \rightarrow K^0\pi^+, K^+\pi^0$$

(W/O INCLUDING $SU(3)_F$ BREAKING OF PENGUIN
CONTR., UP TO $0.3 A_{CP}$)

OTHER INTERESTING PREDICTIONS

$$A_{CP}(D^0 \rightarrow K_s K_s) \leq \sim 0.01 \quad \text{U. NIERSTE, S. SCHACHT, PRD 92, 054036 (2015)}$$

$$A_{CP}(D^+ \rightarrow \pi^+\pi^0) = 0 \quad \text{F. BUCCELLA ET AL., PLB 302, 319 (1993)}$$

(UP TO $10^{-2} A_{CP}$)

CPV IN CHARM

$$A_{CP}(D^+ \rightarrow \pi^+ \pi^0) = 0$$

$$D^{*+} \rightarrow D^+ \pi^0, D^+ \rightarrow \pi^+ \pi^0$$

$$\sigma(A_{CP}(D^+ \rightarrow \pi^+ \pi^0)) \sim 0.2\% - 0.4\% @ 50 \text{ AB}^{-1}$$

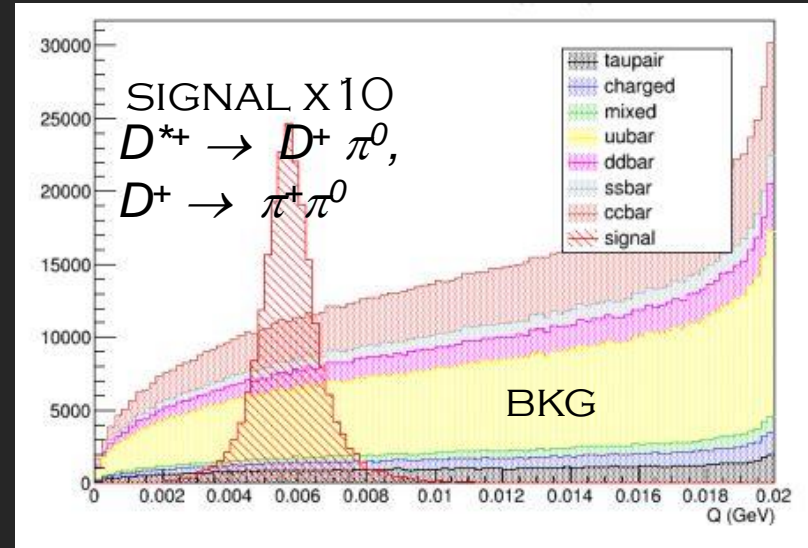
$$(A_{CP}^{SM}(D^+ \rightarrow \pi^+ \pi^0) = 0)$$

$$\sigma(A_{CP}(D^+ \rightarrow K_S K_S)) \sim 0.25\% @ 50 \text{ AB}^{-1}$$

$$(A_{CP}^{SM}(D^+ \rightarrow K_S K_S) \sim 1\%)$$

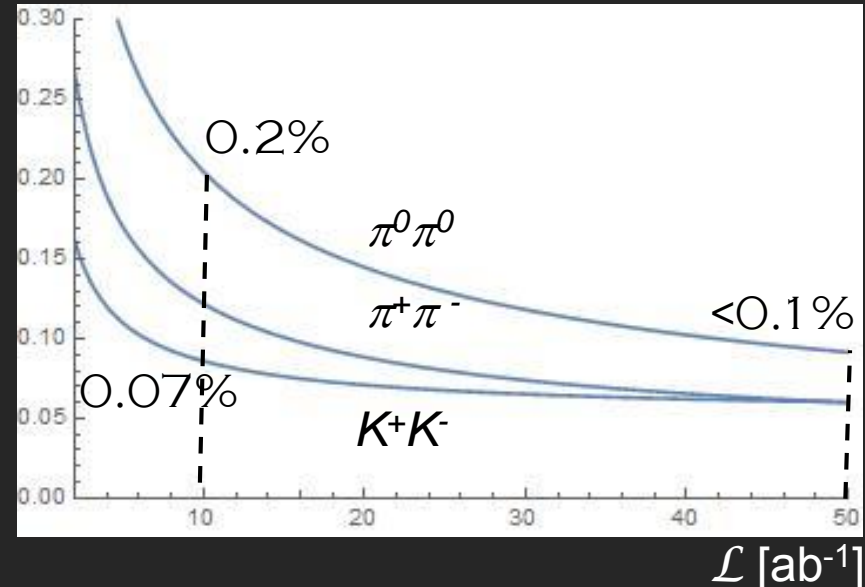
A_{CP} IN SUM RULES

[BACK](#)



E. KOU, P. URQUIJO EDS., THE BELLE II PHYSICS BOOK TO BE PUBLISHED IN PROG. THEOR. EXP. PHYS.

$\sigma(A_{CP})[\%]$



AVERAGES
RESULTS

[BACK](#)

| Parameter | No <i>CPV</i> | No direct <i>CPV</i> in DCS decays | <i>CPV</i> -allowed | <i>CPV</i> -allowed 95% CL Interval |
|------------------------|------------------------|---------------------------------------|---------------------------|----------------------------------------|
| x (%) | $0.50^{+0.13}_{-0.14}$ | $0.43^{+0.10}_{-0.11}$ | $0.39^{+0.11}_{-0.12}$ | [0.16, 0.61] |
| y (%) | 0.62 ± 0.07 | 0.63 ± 0.06 | $0.651^{+0.063}_{-0.069}$ | [0.51, 0.77] |
| $\delta_{K\pi}$ (°) | $8.9^{+8.2}_{-8.9}$ | $9.3^{+8.3}_{-9.2}$ | $12.1^{+8.6}_{-10.2}$ | [-10.4, 28.2] |
| R_D (%) | 0.344 ± 0.002 | 0.344 ± 0.002 | 0.344 ± 0.002 | [0.339, 0.348] |
| A_D (%) | — | — | $-0.55^{+0.49}_{-0.51}$ | [-1.5, 0.4] |
| $ q/p $ | — | 0.998 ± 0.008 | $0.969^{+0.050}_{-0.045}$ | [0.89, 1.07] |
| ϕ (°) | — | 0.08 ± 0.31 | $-3.9^{+4.5}_{-4.6}$ | [-13.2, 5.1] |
| $\delta_{K\pi\pi}$ (°) | $18.5^{+22.7}_{-23.4}$ | $22.1^{+22.6}_{-23.4}$ | $25.8^{+23.0}_{-23.8}$ | [-21.3, 70.3] |
| A_π (%) | — | 0.05 ± 0.16 | 0.06 ± 0.16 | [-0.25, 0.38] |
| A_K (%) | — | -0.11 ± 0.16 | -0.09 ± 0.16 | [-0.40, 0.22] |
| x_{12} (%) | — | $0.43^{+0.10}_{-0.11}$ | — | [0.22, 0.63] |
| y_{12} (%) | — | 0.63 ± 0.06 | — | [0.50, 0.75] |
| ϕ_{12} (°) | — | $-0.25^{+0.96}_{-0.99}$ | — | [-2.5, 1.8] |

AVERAGES

 χ^2

| Observable | χ^2 | $\sum \chi^2$ |
|--------------------------------------------|----------|---------------|
| $y_{CP}(K^+K^-, \pi^+\pi^-)$ World Average | 0.35 | 0.35 |
| A_Γ World Average | 2.07 | 2.41 |
| $x_{K^0\pi^+\pi^-}$ Belle | 0.71 | 3.12 |
| $y_{K^0\pi^+\pi^-}$ Belle | 4.42 | 7.54 |
| $ q/p _{K^0\pi^+\pi^-}$ Belle | 0.48 | 8.02 |
| $\phi_{K^0\pi^+\pi^-}$ Belle | 0.53 | 8.55 |
| $x_{CP}(K^0\pi^+\pi^-)$ LHCb | 0.55 | 9.10 |
| $y_{CP}(K^0\pi^+\pi^-)$ LHCb | 0.06 | 9.16 |
| $\Delta x(K^0\pi^+\pi^-)$ LHCb | 0.00 | 9.16 |
| $\Delta y(K^0\pi^+\pi^-)$ LHCb | 0.09 | 9.26 |
| $x_{K^0h^+h^-}$ Babar | 0.73 | 9.98 |
| $y_{K^0h^+h^-}$ Babar | 0.08 | 10.06 |
| $x_{\pi^0\pi^+\pi^-}$ Babar | 0.68 | 10.74 |
| $y_{\pi^0\pi^+\pi^-}$ Babar | 0.19 | 10.93 |
| $(x^2 + y^2)_{K+\ell-\nu}$ | 0.14 | 11.07 |

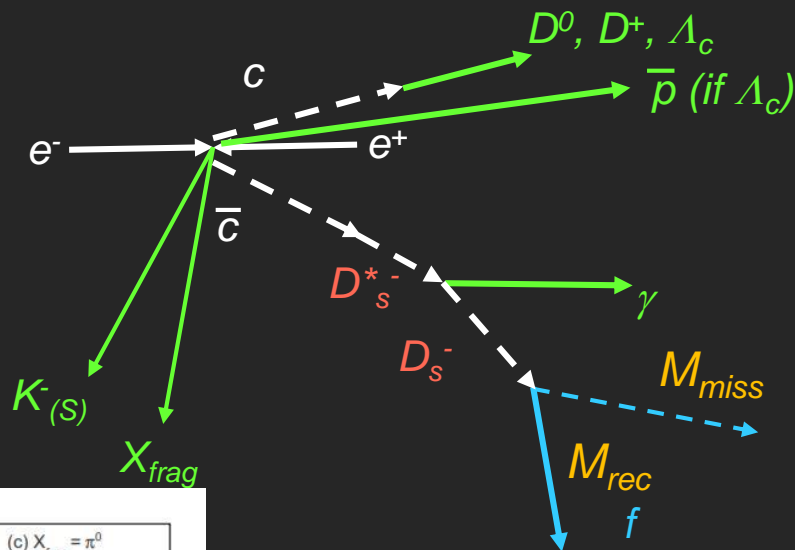
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| | | |
|---------------------------------------------------------------------|-------|-------|
| $x_{K^+\pi^-\pi^0}$ Babar | 7.10 | 18.17 |
| $y_{K^+\pi^-\pi^0}$ Babar | 3.91 | 22.08 |
| CLEOc | | |
| $(x/y/R_D/\cos\delta/\sin\delta)$ | 10.53 | 32.60 |
| $R_D^+/x'^{2+}/y'^+$ Babar | 8.69 | 41.30 |
| $R_D^-/x'^{2-}/y'^-$ Babar | 4.02 | 45.32 |
| $R_D^+/x'^{2+}/y'^+$ Belle | 1.88 | 47.20 |
| $R_D^-/x'^{2-}/y'^-$ Belle | 2.36 | 49.56 |
| $R_D/x'^2/y'$ CDF | 1.20 | 50.76 |
| $R_D^+/x'^{2+}/y'^+$ LHCb | 1.29 | 52.05 |
| $R_D^-/x'^{2-}/y'^-$ LHCb | 0.67 | 52.72 |
| $A_{KK}/A_{\pi\pi}$ Babar | 0.35 | 53.08 |
| $A_{KK}/A_{\pi\pi}$ CDF | 4.07 | 57.14 |
| $A_{KK} - A_{\pi\pi}$ LHCb ($D^*, B^0 \rightarrow D^0 \mu X$ tags) | 0.05 | 57.19 |
| $(x^2 + y^2)_{K^+\pi^-\pi^+\pi^-}$ LHCb | 3.47 | 60.67 |

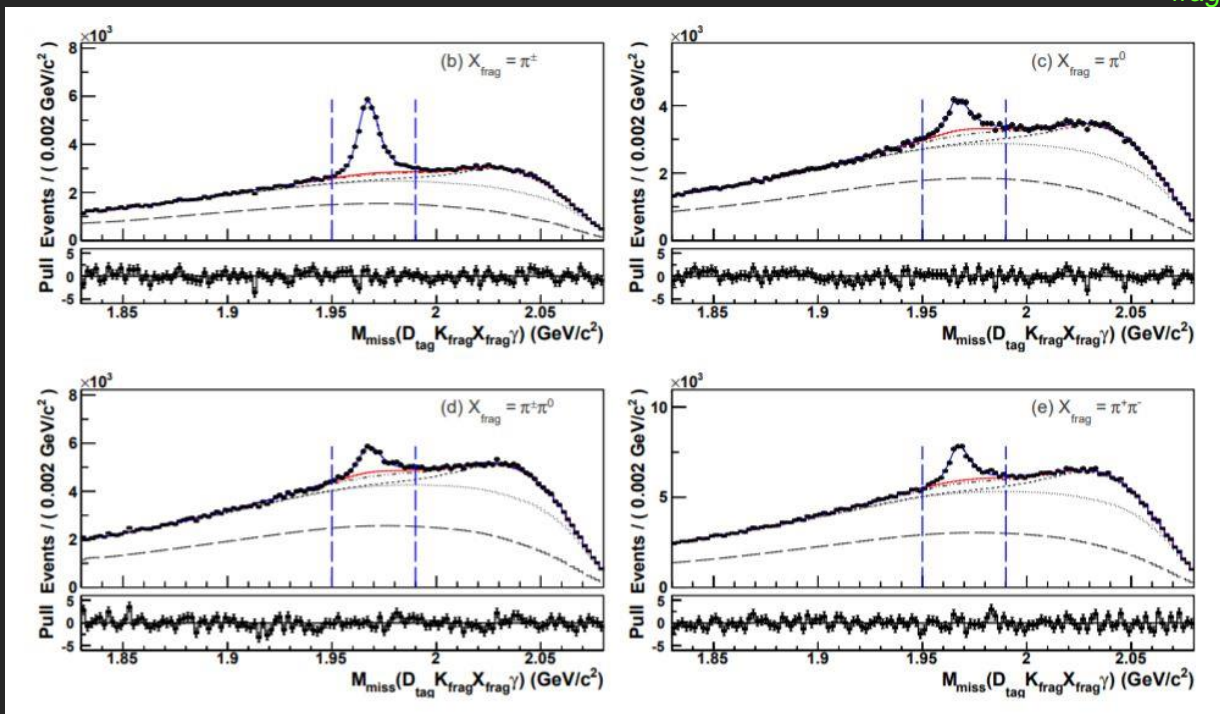
A. ZUPANC ET AL. (BELLE COLL.), JHEP 09, 139 (2013)

DECAYS B-FACTORY METHOD

$$N_{sig}(f) / [\varepsilon(f) N_{sig}(M_{rec})] = Br(D_s \rightarrow f)$$



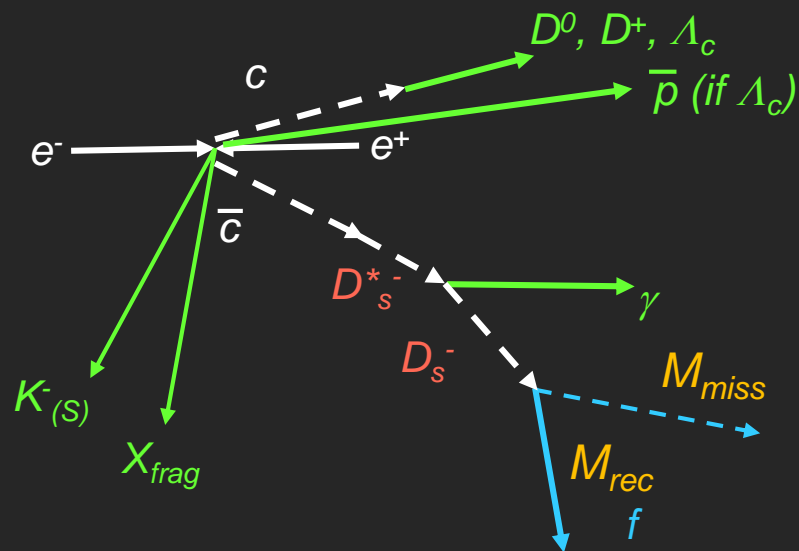
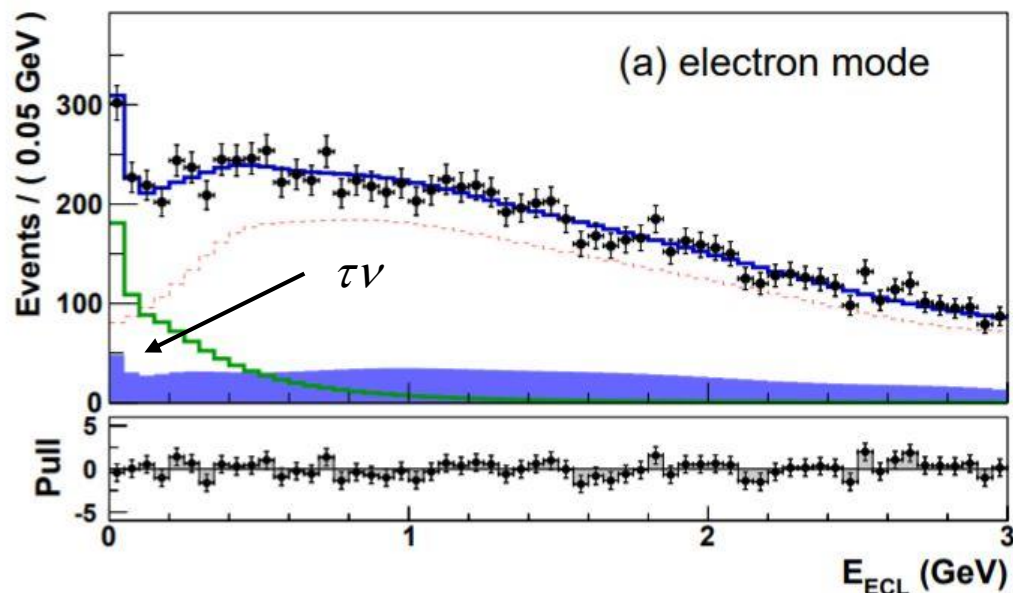
$$N_{D_s}^{inc} \approx (94.3 \pm 1.3) \cdot 10^3$$



A. ZUPANC ET AL. (BELLE COLL.), JHEP 09, 139 (2013)

DECAYS B-FACTORY METHOD

FOR $\tau\nu$ BESIDE M_{MISS} ALSO E_{ECL} EXPLOITED



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DECAYS

B-FACTORY METHOD

SEARCH FOR INVISIBLE D DECAYS

$$N_{Ds}^{inc} \approx (94.3 \pm 1.3) \cdot 10^3$$

$$\sim 10^5 N_{DS}^{INC} (1 \pm 0.015) / \text{AB}^{-1}$$

$$@ 20 \text{ AB}^{-1} 2 \cdot 10^6 (1 \pm 0.003)$$

$$\sim \sigma(N_{SIG}^{ECL}) @ 1 \text{ AB}^{-1} \sim 100$$

SENSITIVITY TO DECAYS TO INVISIBLE STATES

(IF BKG LIKE IN $\tau\nu$ CASE ?)

$$\sim 20 \cdot 100 / 2 \cdot 10^6 \sim 10^{-3}$$

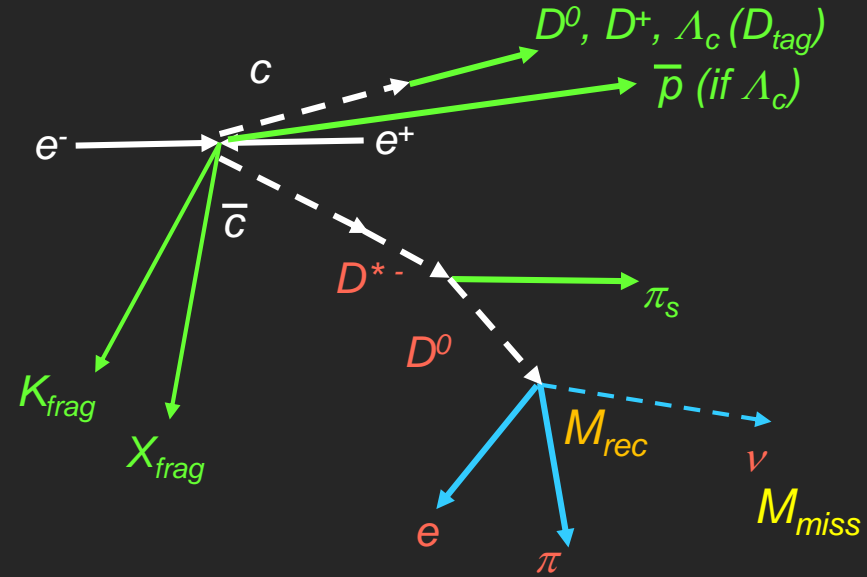
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SEMILEPTONIC DECAYS

$$D^0 \rightarrow K^- \mu^+ \nu$$

BELLE: $N_{SIG}(D_S \rightarrow \mu^+ \nu) @ 1 \text{ AB}^{-1} = 492 \pm 26$

A. ZUPANC ET AL. (BELLE COLL.), JHEP 09, 139 (2013)



$$N_{sig}(D^0 \rightarrow K\mu\nu) \sim N_{sig}(D_s \rightarrow \mu\nu) \frac{\sigma(D^{*+})}{\sigma(D_s^*)} \frac{Br(D^* \rightarrow D^0\pi)}{Br(D_s^* \rightarrow D_s\gamma)} \frac{Br(D^0 \rightarrow K\mu\nu)}{Br(D_s \rightarrow \mu\nu)} \frac{\epsilon_K \epsilon_\pi}{\epsilon_\gamma} \sim$$

$$\sim N_{sig}(D_s \rightarrow \mu\nu) \underbrace{\frac{\sigma(D^{*+})}{0.5\sigma(D_s)}}_{\sim 5} \underbrace{\frac{Br(D^* \rightarrow D^0\pi)}{Br(D_s^* \rightarrow D_s\gamma)}}_{\sim 0.7} \underbrace{\frac{Br(D^0 \rightarrow K\mu\nu)}{Br(D_s \rightarrow \mu\nu)}}_{\sim 6} \underbrace{\frac{\epsilon_K \epsilon_\pi}{\epsilon_\gamma}}_{\sim 1} \sim 20 N_{sig}(D_s \rightarrow \mu\nu)$$

$$\sigma(D^*)/\sigma(D)$$

R. SEUSTER ET AL. (BELLE COLL.), PHYS.REV. D73, 032002 (2006)

BELLE II: $N_{SIG}(D^0 \rightarrow K^- \mu^+ \nu) @ 20 \text{ AB}^{-1} \sim 2 \cdot 10^4$

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