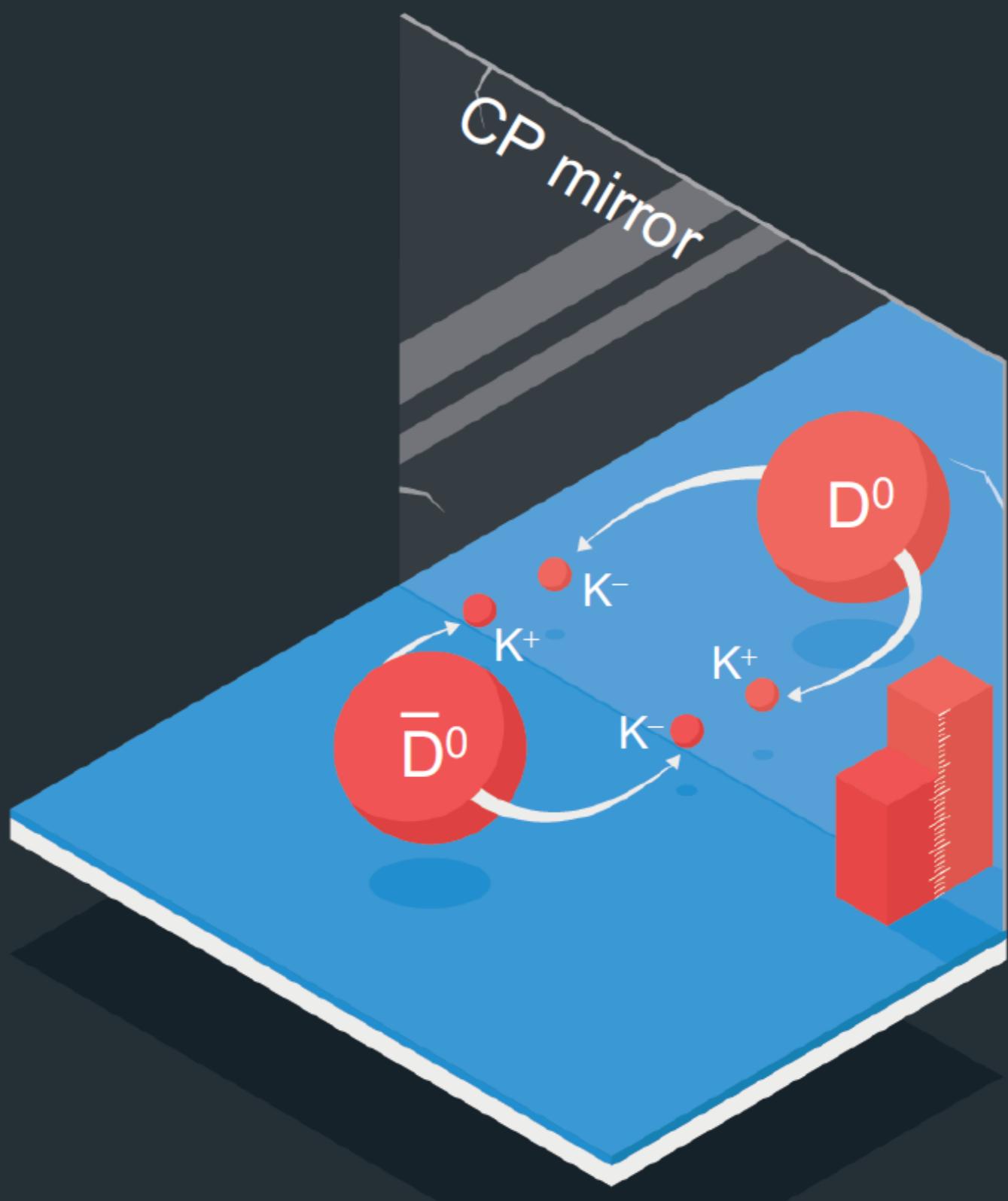


# 2nd Belle II Physics week

October 28–November 1, 2019  
KEK, Tsukuba, Japan



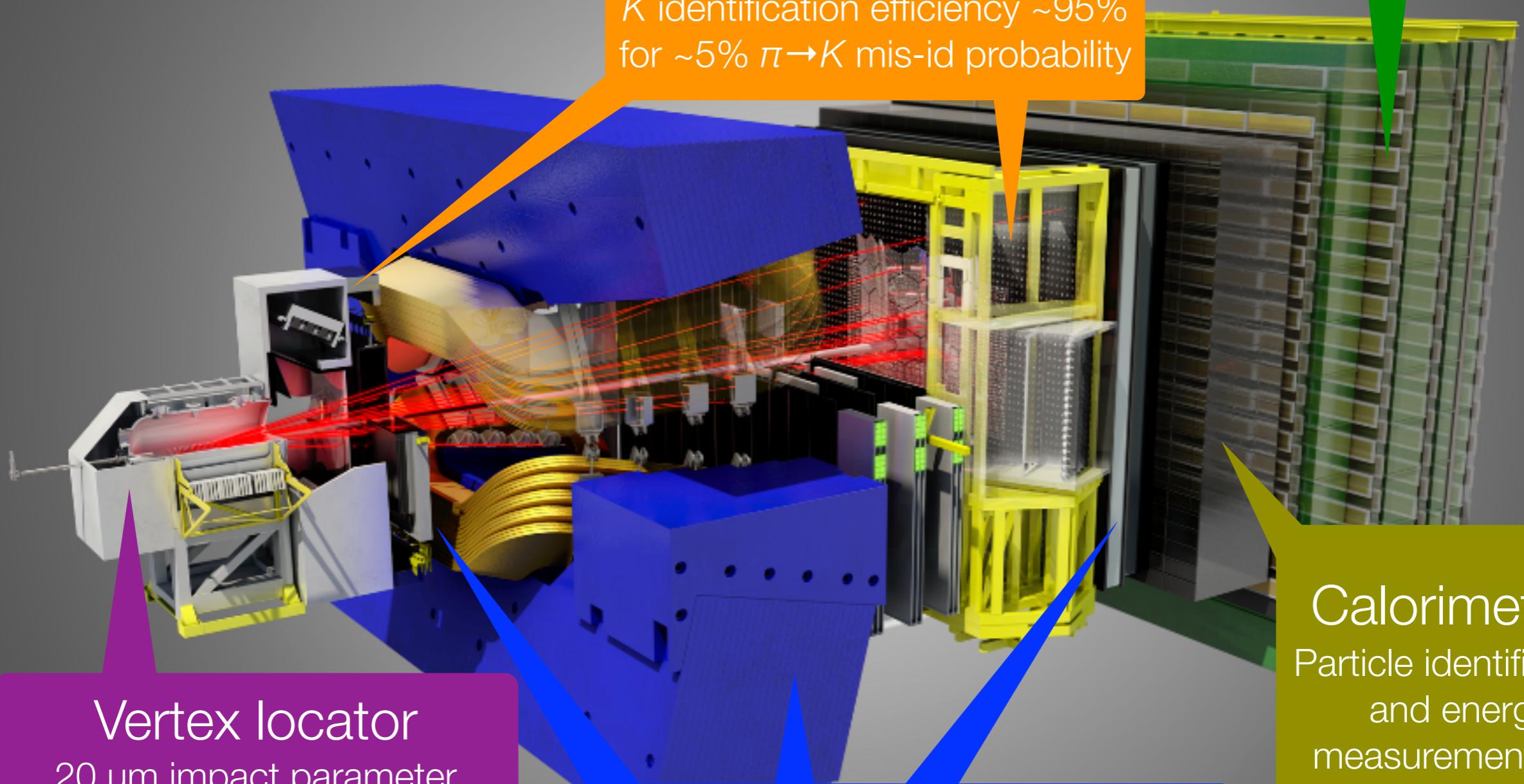
## Charm physics at LHCb

(from the perspective of a former LHCb member that recently joined Belle II)

*Angelo Di Canto*

**BROOKHAVEN**  
NATIONAL LABORATORY

# The beauty of the LHC



**Vertex locator**  
20  $\mu\text{m}$  impact parameter resolution, corresponding to ~45 fs decay-time resolution for  $b/c$  hadrons

**Dipole + tracking stations**  
 $\Delta p/p = 0.4\text{-}0.6\%$  at 5-100  $\text{GeV}/c$

**RICHes**

$K$  identification efficiency ~95% for ~5%  $\pi \rightarrow K$  mis-id probability

**Muon stations**  
 $\mu$  identification efficiency ~97% for 1-3%  $\pi \rightarrow \mu$  mis-id probability

**Calorimeters**  
Particle identification and energy measurements for electrons/photons  
 $1\%+10\%/\sqrt{E[\text{GeV}]}$

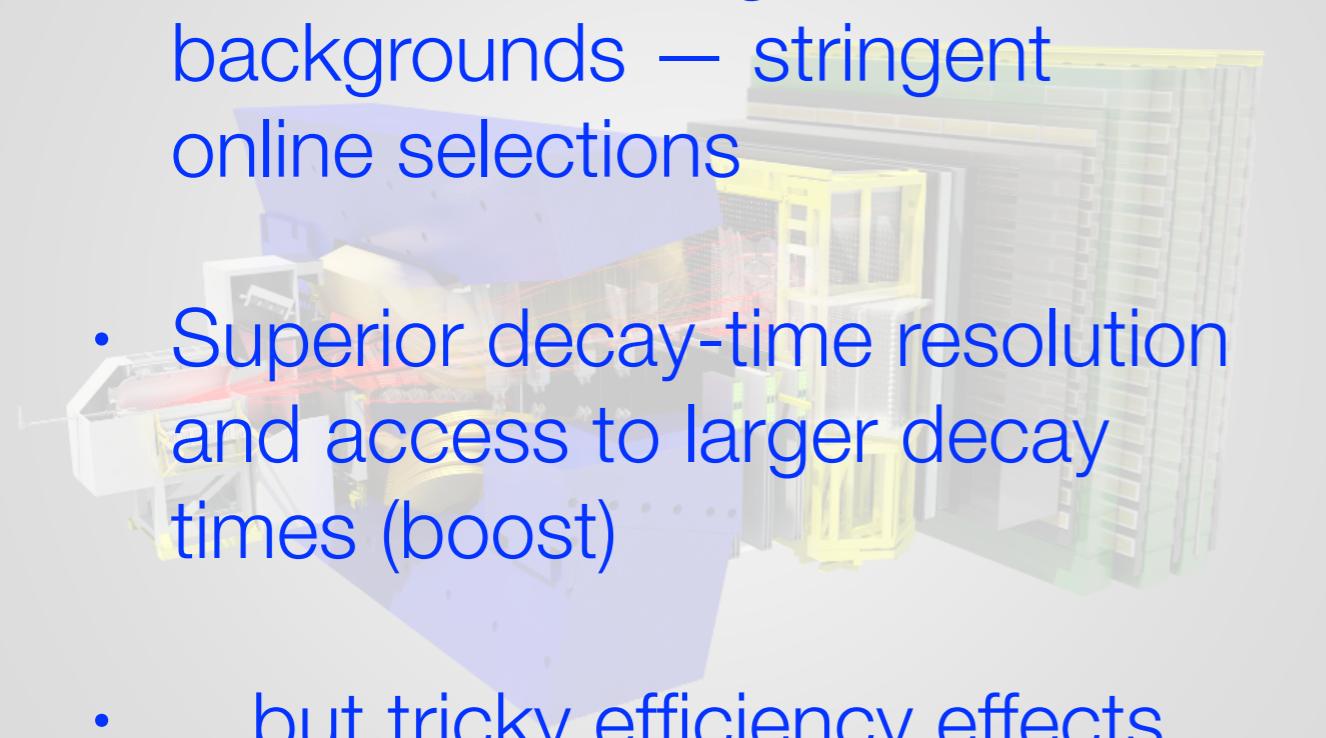
charm

# Finally two concurrent ~~beauty~~ factories

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## LHCb

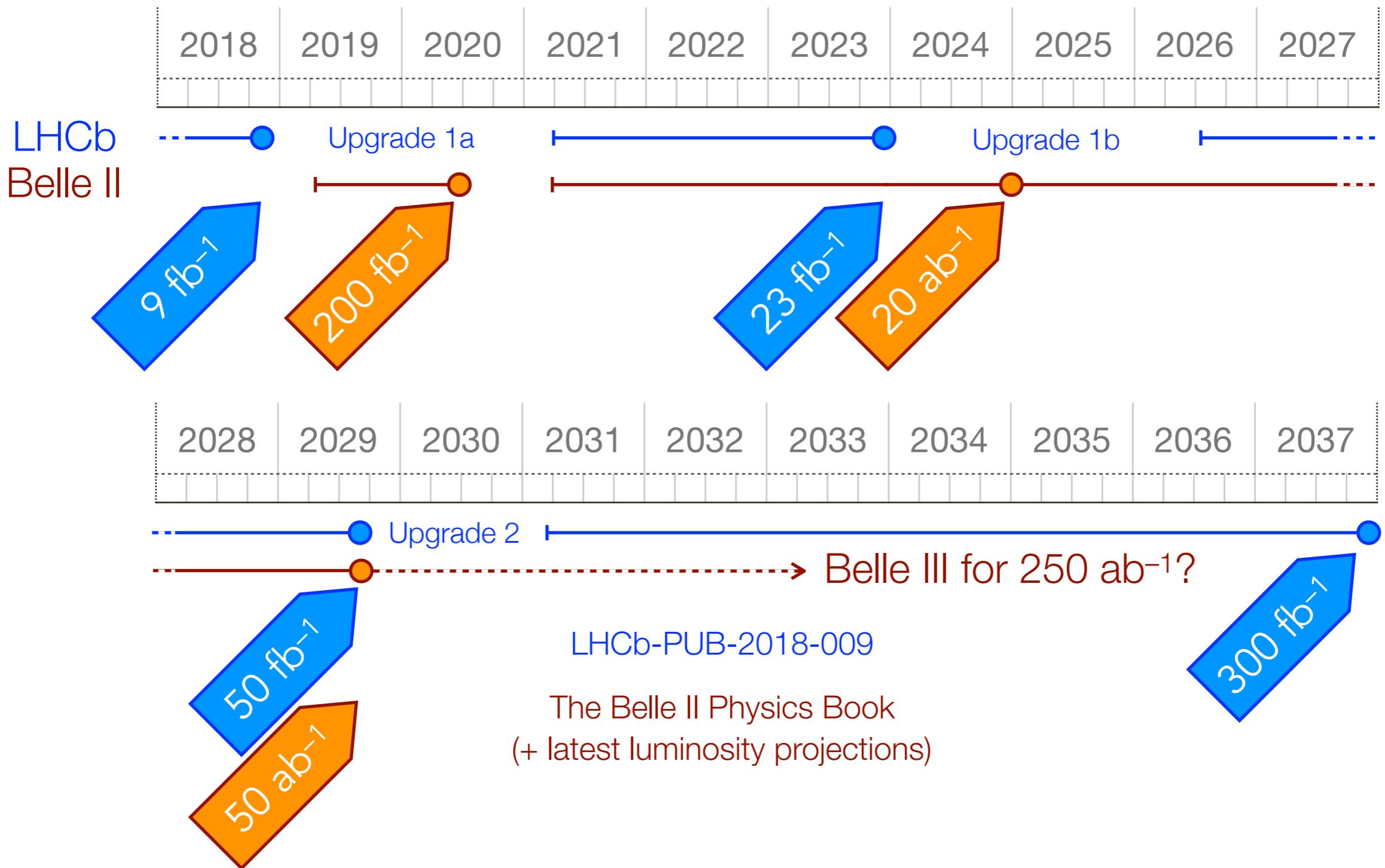
- Huge advantage in production rate, but also large backgrounds — stringent online selections
- Superior decay-time resolution and access to larger decay times (boost)
- ...but tricky efficiency effects (e.g. decay-time acceptance)



## Belle II

- Cleaner environment allows for more generous selections — milder efficiency effects
- Better reconstruction of final states with neutrals/invisible particles
- Much easier separation between promptly produced charm and secondary (from- $B$ ) decays

# Prospects of data collection



# The rule of thumb

$$1/fb^{-1} \sim 1/ab^{-1}$$

# The rule of thumb

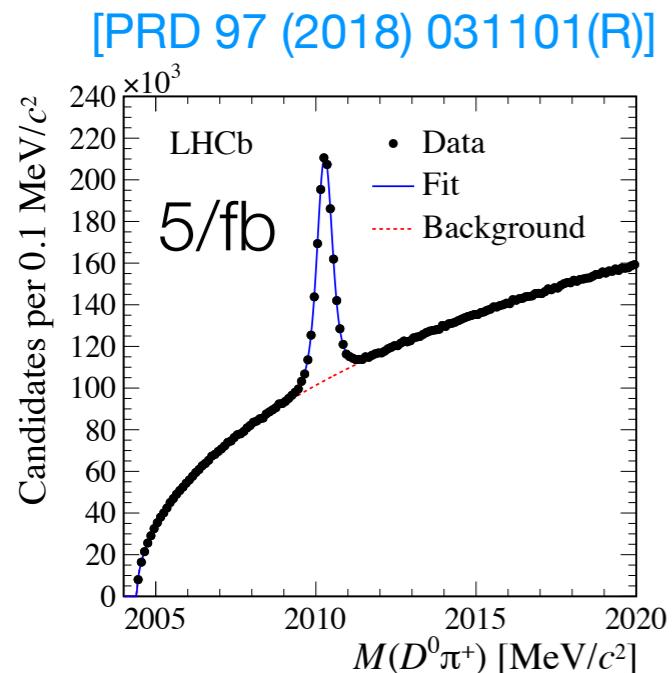
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$1 \text{ fb}^{-1}$   
@ LHCb

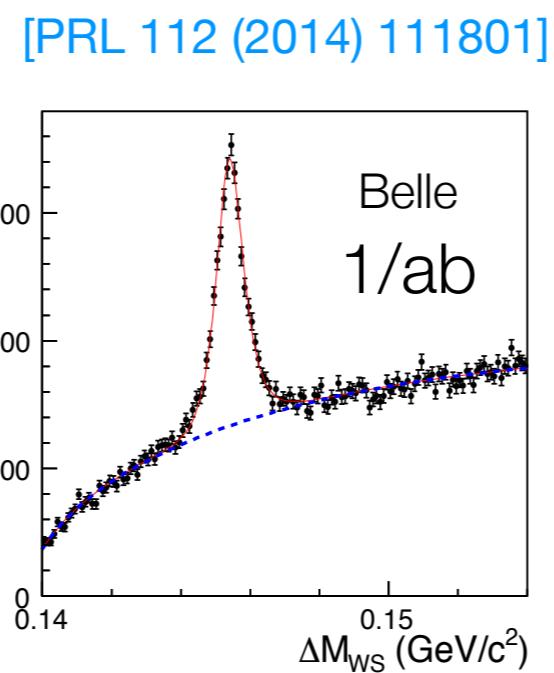
$1 \text{ ab}^{-1}$   
@ Belle II

does not hold for charm

# The rule of thumb



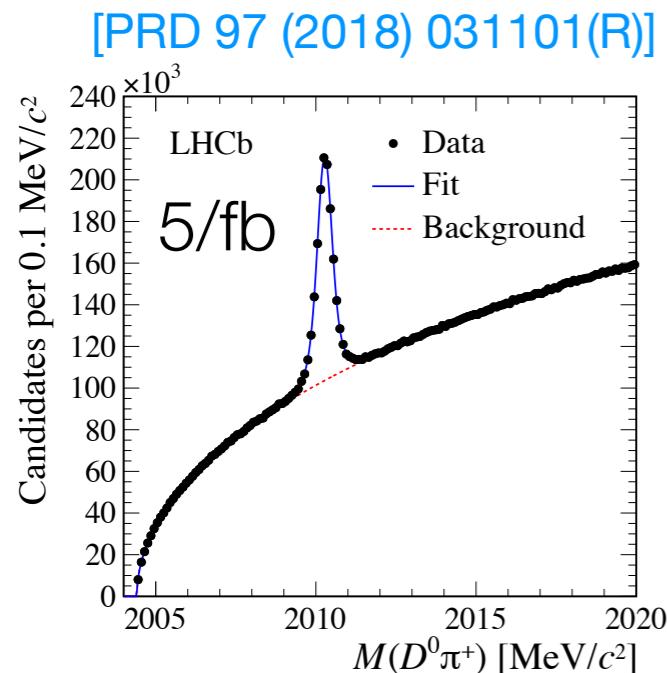
$N/\mathcal{L} \sim 150\text{k}$



$N/\mathcal{L} \sim 10\text{k}$

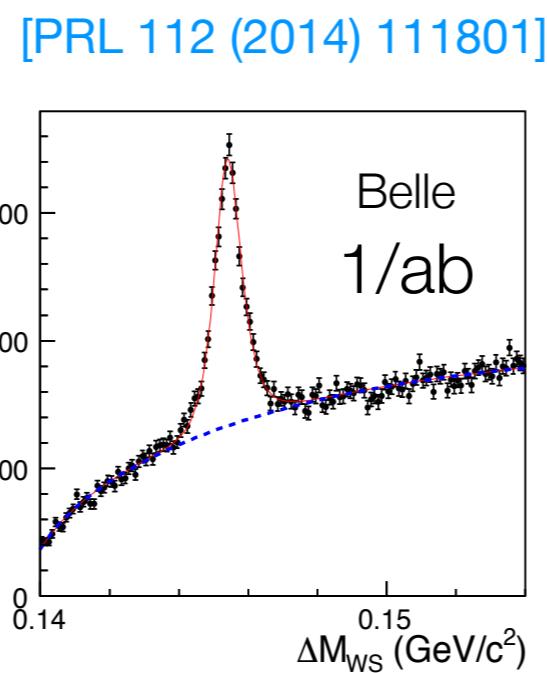
$$D^{*+} \rightarrow D^0 (\rightarrow K^+\pi^-)\pi^+$$

# The rule of thumb

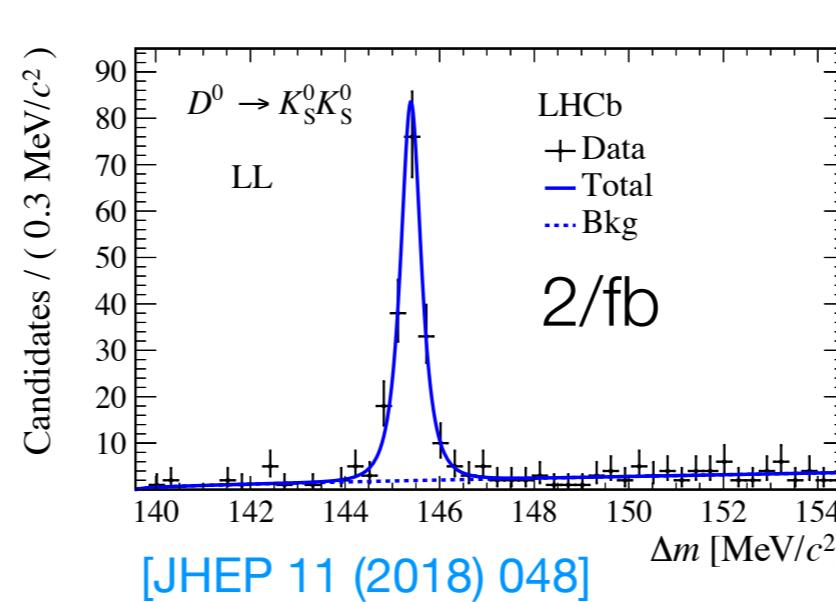


$N/\mathcal{L} \sim 150k$

$D^{*+} \rightarrow D^0(\rightarrow K_S K_S)\pi^+$

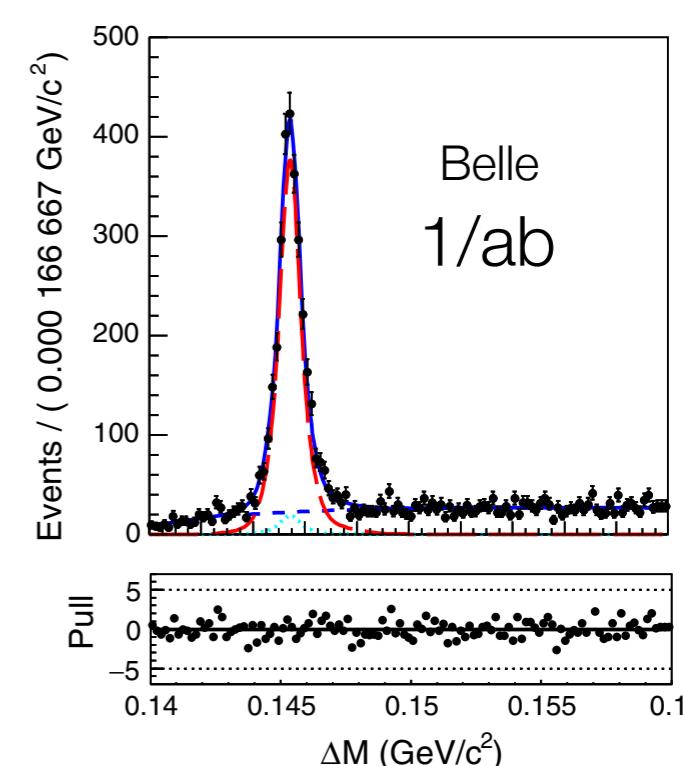


$N/\mathcal{L} \sim 10k$

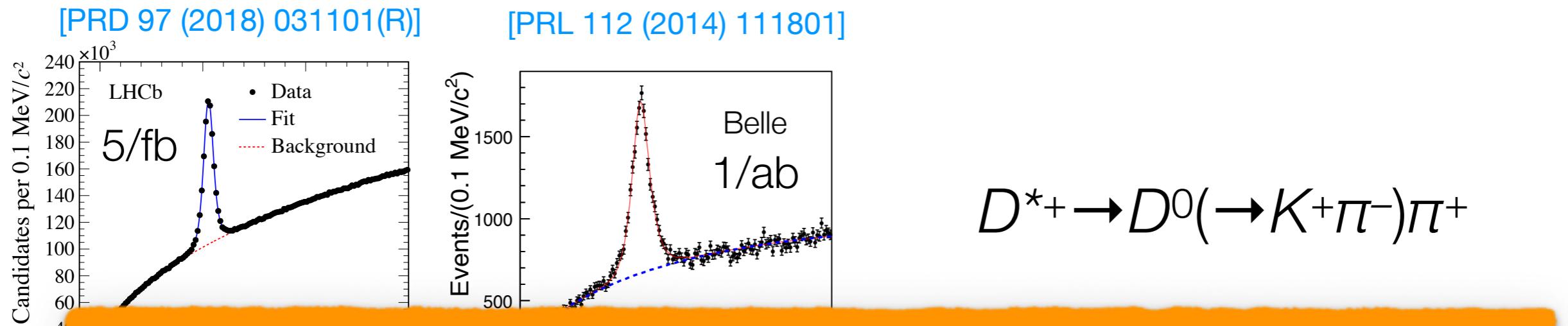


$N/\mathcal{L} \sim 0.5k$

$D^{*+} \rightarrow D^0(\rightarrow K^+\pi^-)\pi^+$

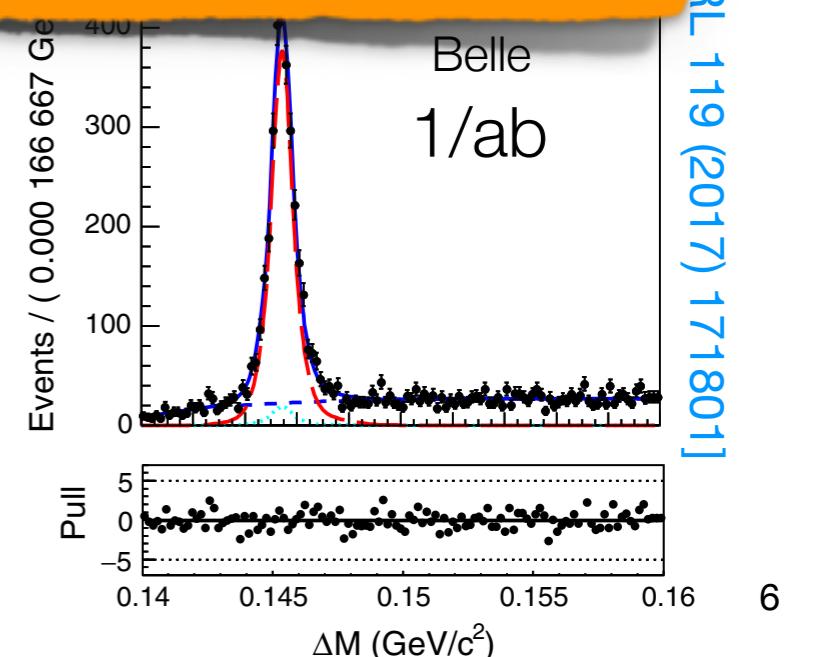
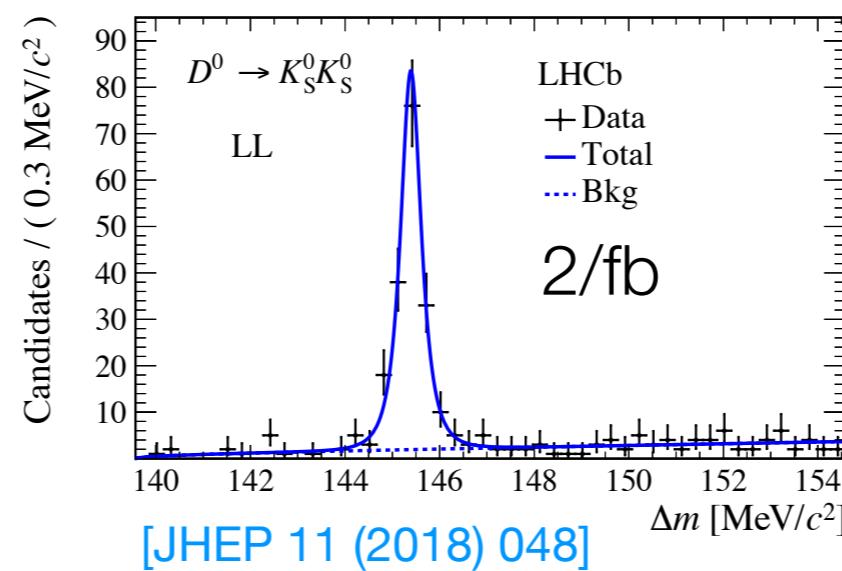


# The rule of thumb



COMPLEMENTARITY

$D^{*+} \rightarrow D^0(\rightarrow K_S K_S)\pi^+$



# Charm Physics program at LHCb

## Mixing & *CPV*

- Time-dependent
- $D^0 \rightarrow h^- h^+$
- $D^0 \rightarrow K_S h^- h^+$
- Time-integrated
- $\Delta A_{\text{CP}}$
- $D^+ \rightarrow K_S h^+, \eta' h^+$
- Local *CPV* in multibody decays
- *CPV* in baryons
- ...

## Production & spectroscopy

- Cross sections
- Masses, lifetimes
- Amplitude analyses
- $D_{(S)J}$  states
- Charmed baryons
- Production asymmetries
- ...

## Rare decays

- LFV, LNV
  - $D^0 \rightarrow e^- \mu^+$
  - $D_{(S)} \rightarrow h^- \mu^+ \mu^+$
- FCNC
  - $D^0 \rightarrow \mu^- \mu^+$
  - $D^0 \rightarrow h^- h^+ \mu^- \mu^+$
  - $D_{(S)} \rightarrow h^+ \mu^- \mu^+$
  - ...

# Charm Physics program at LHCb

## Mixing & CPV

- Time-dependent
- $D^0 \rightarrow h-h^+$
- $D^0 \rightarrow K_S h-h^+$
- Time-integrated
- $\Delta A_{CP}$
- $D^+ \rightarrow K_S h^+, \eta' h^+$
- Local CPV in multibody decays
- CPV in baryons
- ...

## Production & spectroscopy

- Cross sections
- Masses, lifetimes
- Amplitude analyses
- $D_{(S)J}$  states
- Charmed baryons
- Production asymmetries
- ...

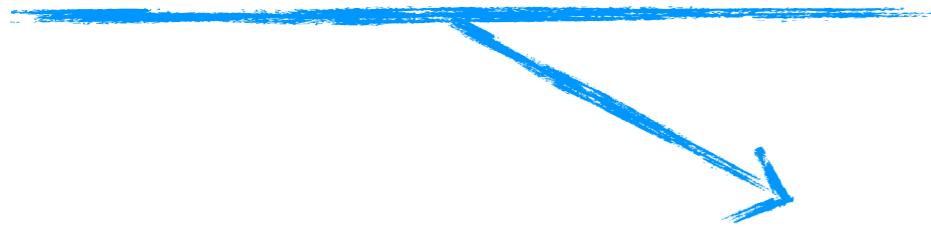
*See Boštjan's talk  
on Monday*

## Rare decays

- LFV, LNV
- $D^0 \rightarrow e^- \mu^+$
- $D_{(S)} \rightarrow \mu^+ \mu^+$
- FCNC
- $D^0 \rightarrow \mu^- \mu^+$
- $D^0 \rightarrow h-h^+ \mu^-\mu^+$
- $D_{(S)} \rightarrow h^+ \mu^-\mu^+$
- ...

*Supplementary slides  
(if time allows)*

Direct  $CP$  violation


$$|\bar{d} \rightarrow f|^2 \neq |\bar{\bar{d}} \rightarrow \bar{f}|^2$$

# What do we measure?

---

$$A_{CP}(D^0 \rightarrow h^+ h^-) = \frac{\Gamma(D^0 \rightarrow h^+ h^-) - \Gamma(\bar{D}^0 \rightarrow h^+ h^-)}{\Gamma(D^0 \rightarrow h^+ h^-) + \Gamma(\bar{D}^0 \rightarrow h^+ h^-)}$$

# What do we really measure?

---

$$A(D^0 \rightarrow h^+h^-) = \frac{N(D^0 \rightarrow h^+h^-) - N(\bar{D}^0 \rightarrow h^+h^-)}{N(D^0 \rightarrow h^+h^-) + N(\bar{D}^0 \rightarrow h^+h^-)}$$

# What do we really measure?

$$A(D^0 \rightarrow h^+ h^-) = \frac{N(D^0 \rightarrow h^+ h^-) - N(\bar{D}^0 \rightarrow h^+ h^-)}{N(D^0 \rightarrow h^+ h^-) + N(\bar{D}^0 \rightarrow h^+ h^-)}$$

$$\approx A_{CP}(h^+ h^-) + A_D + A_P$$

The  $CP$  asymmetry we want to measure

Detection asymmetry of tagging particle ( $\pi^+$  or  $\mu^-$ ) –  $D^0$  final state does not contribute being charge symmetric

Production asymmetry of parent hadron ( $D^{*+}$  or  $\bar{B}$ )

# What do we really measure?

$$A(D^0 \rightarrow h^+ h^-) = \frac{N(D^0 \rightarrow h^+ h^-) - N(\bar{D}^0 \rightarrow h^+ h^-)}{N(D^0 \rightarrow h^+ h^-) + N(\bar{D}^0 \rightarrow h^+ h^-)}$$

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Production asymmetry of parent hadron ( $D^{*+}$  or  $\bar{B}$ )

$$\Delta A_{CP} = A_{CP}(K^+ K^-) - A_{CP}(\pi^+ \pi^-) = A(K^+ K^-) - A(\pi^+ \pi^-)$$

# What do we really measure?

$$A(D^0 \rightarrow h^+h^-) = \frac{N(D^0 \rightarrow h^+h^-) - N(\bar{D}^0 \rightarrow h^+h^-)}{N(D^0 \rightarrow h^+h^-) + N(\bar{D}^0 \rightarrow h^+h^-)}$$

$$\approx A_{CP}(h^+h^-) + A_D + A_P$$

The  $CP$  asymmetry we want to measure

Detection asymmetry of tagging particle ( $\pi^+$  or  $\mu^-$ ) –  $D^0$  final state does not contribute being charge symmetric

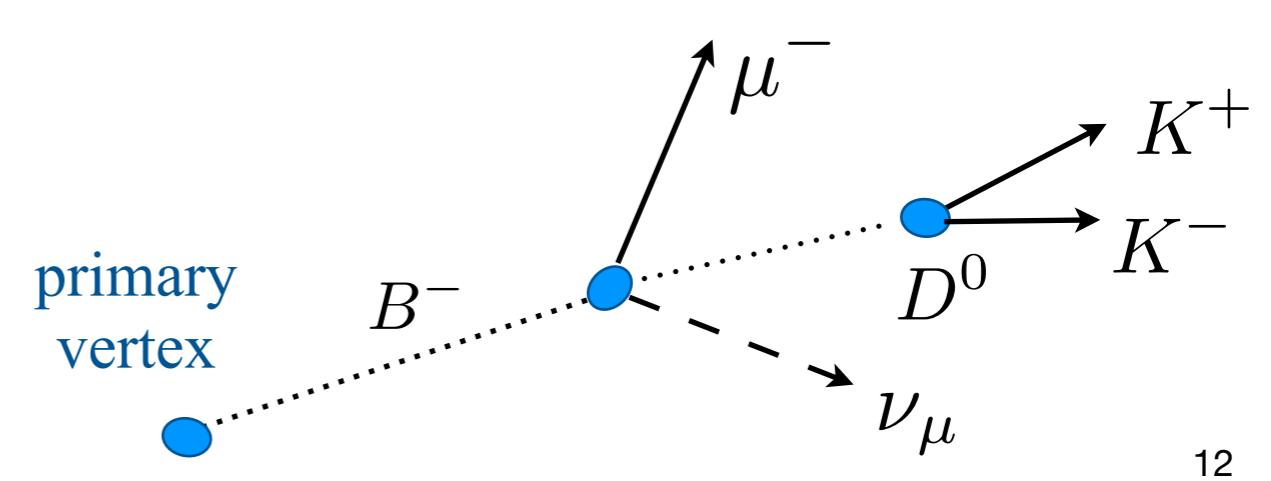
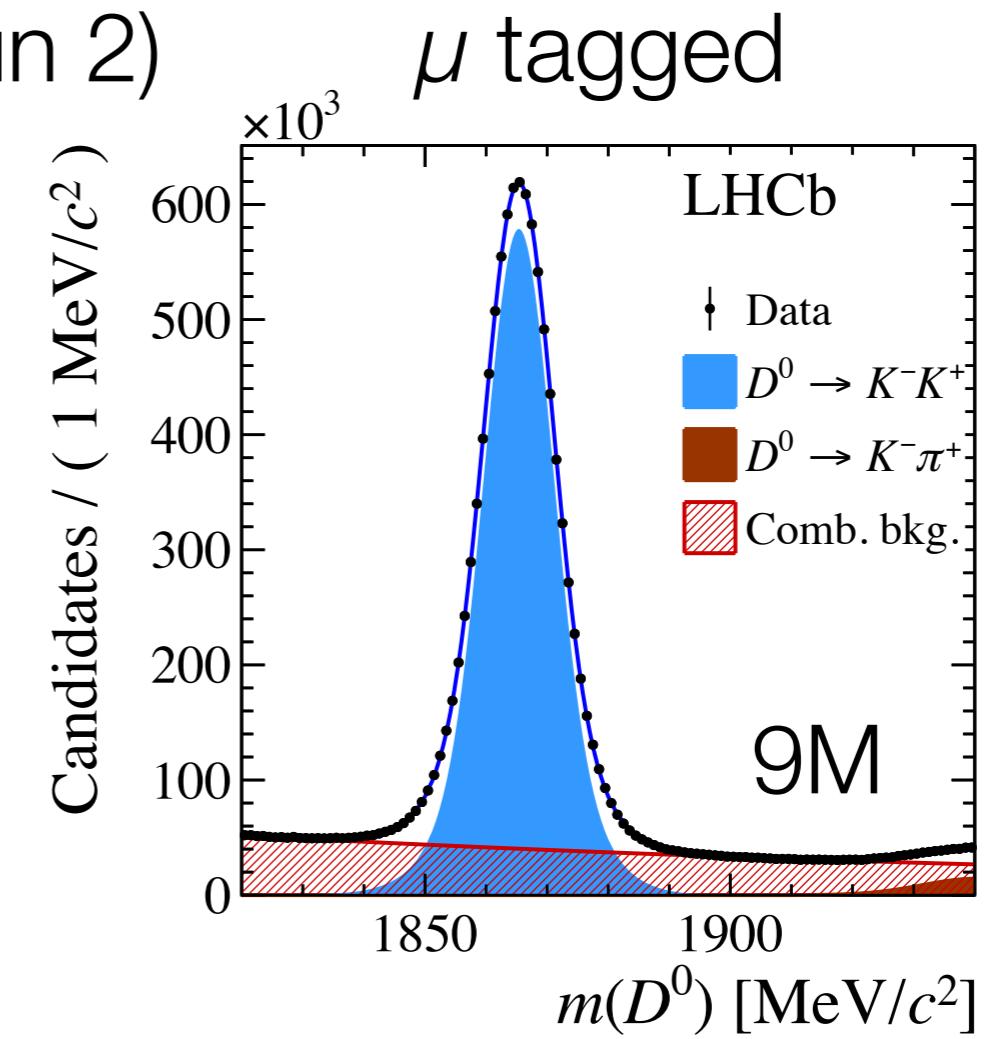
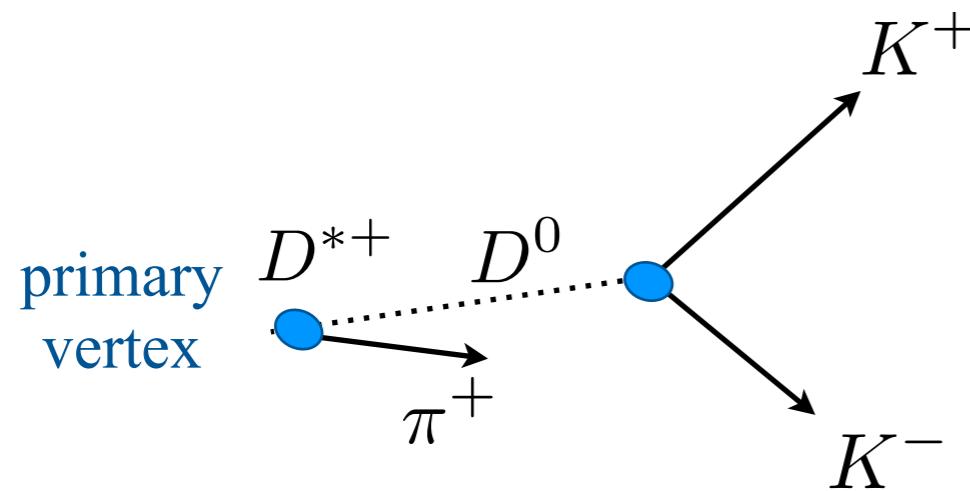
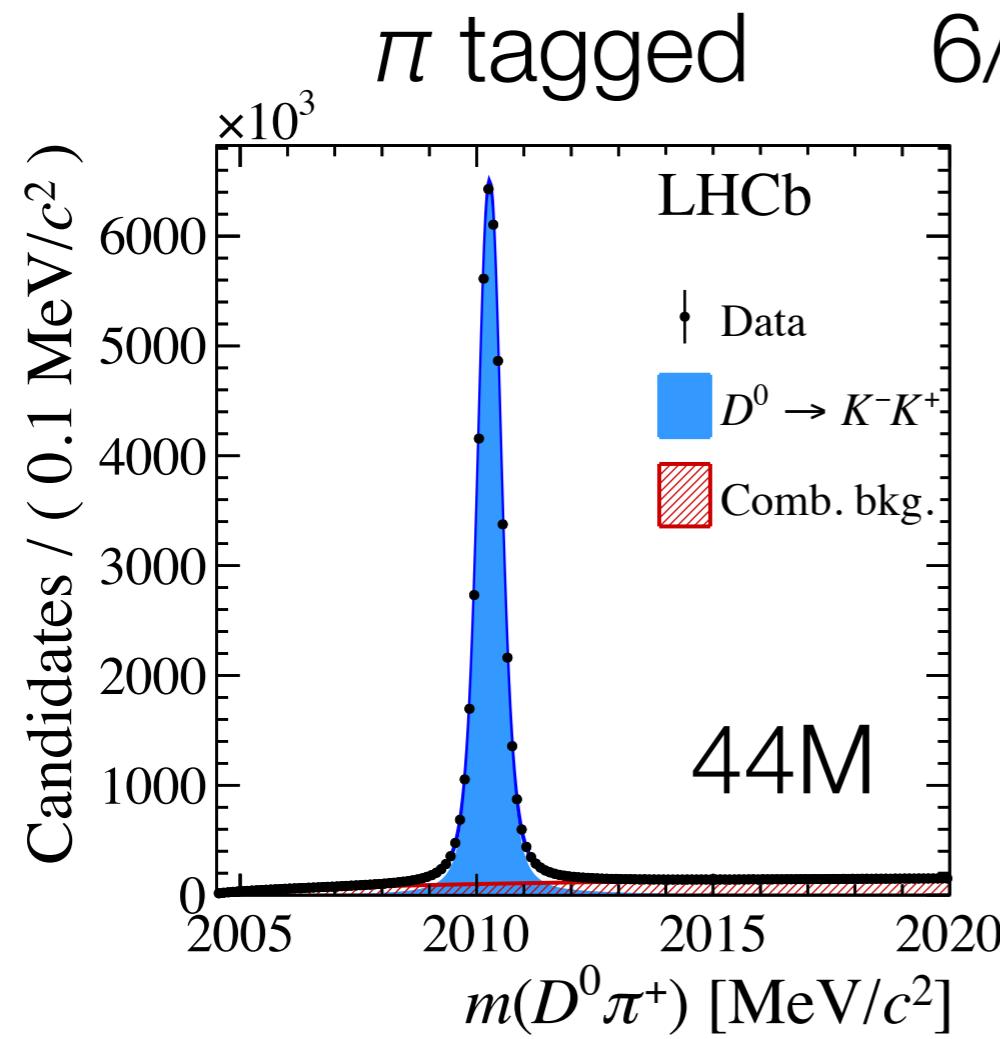
Production asymmetry of parent hadron ( $D^{*+}$  or  $\bar{B}$ )

$$\Delta A_{CP} = A_{CP}(K^+K^-) - A_{CP}(\pi^+\pi^-) = A(K^+K^-) - A(\pi^+\pi^-)$$

- In the limit of SU(3)/U-spin symmetry,  $A_{CP}(K^+K^-)$  and  $A_{CP}(\pi^+\pi^-)$  have same magnitude and opposite signs  $\implies$  in addition to be robust against experimental biases,  $\Delta A_{CP}$  provides 2 $\times$  enhanced sensitivity to  $CP$  violation

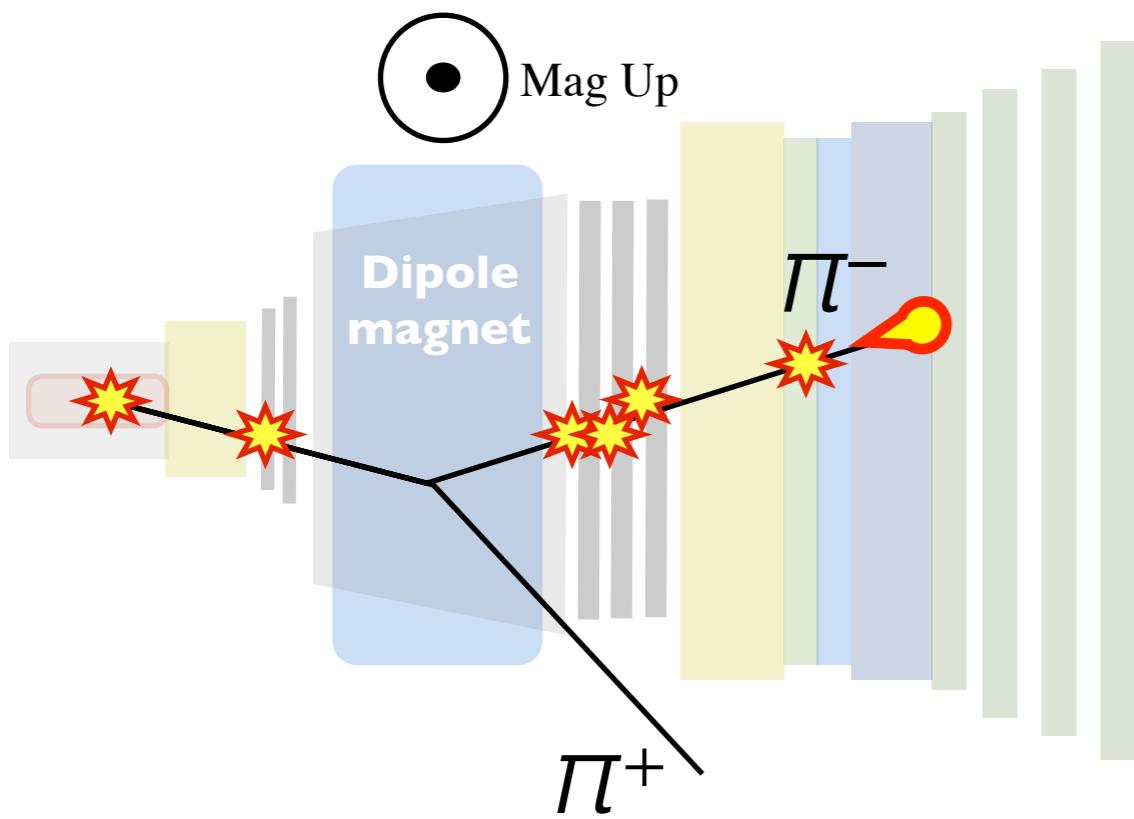
# $D^0 \rightarrow h^+h^-$ decays at LHCb

[PRL 122 (2019) 211803]

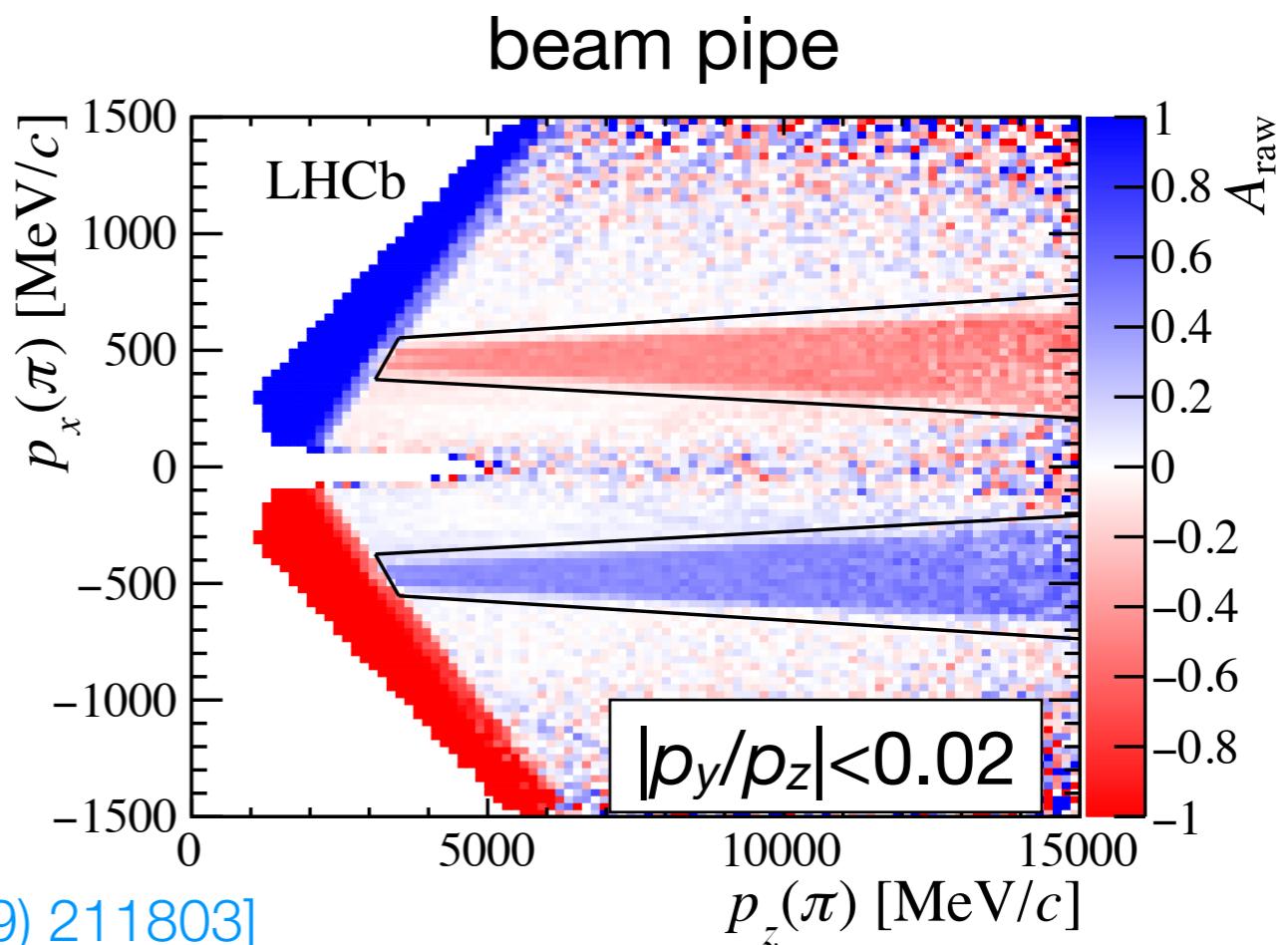
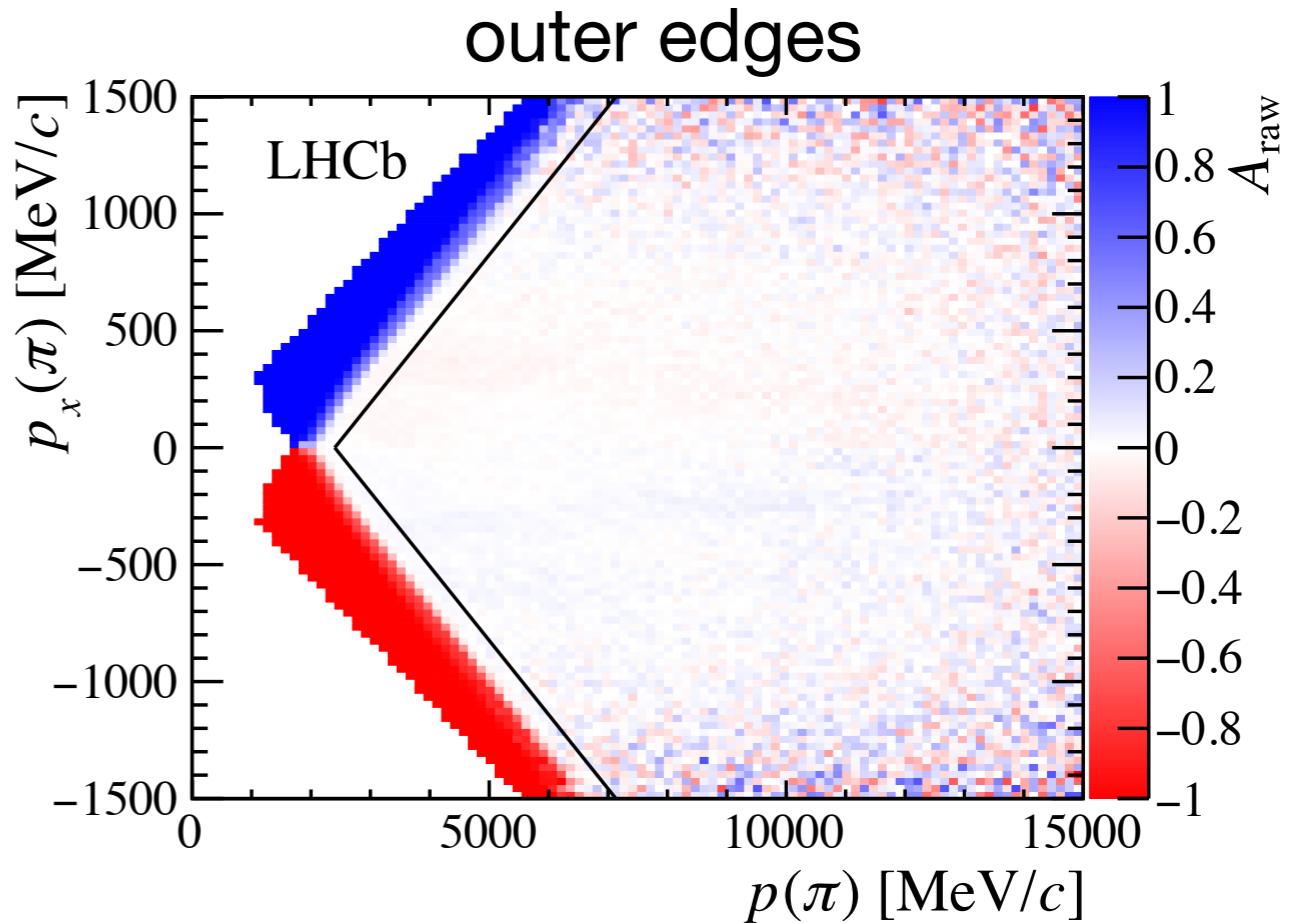


# Fiducial requirements

- For specific regions of phase space, the soft pion of a given charge is kicked out of the detector acceptance by the magnetic field

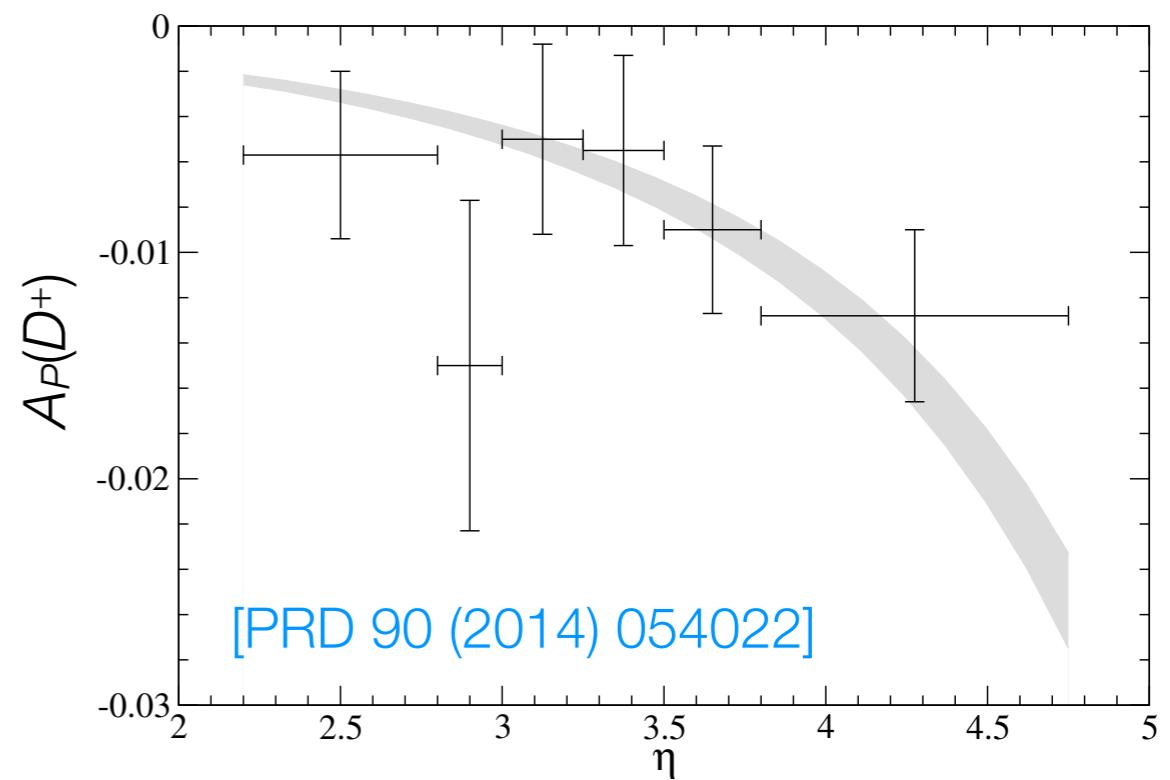
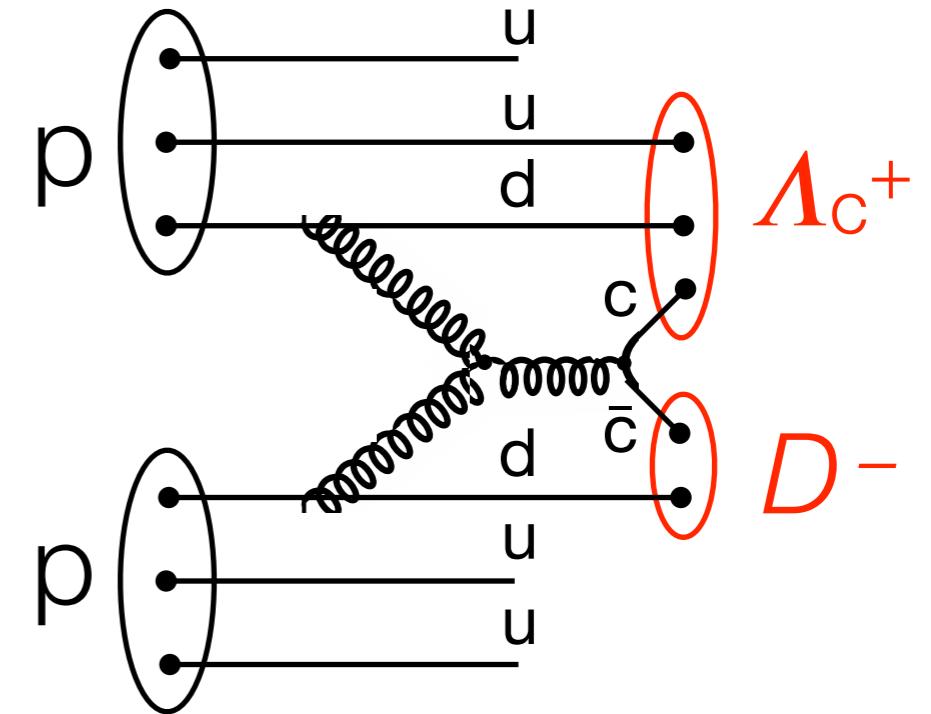


- $O(1)$  detection asymmetries break the linear decomposition of the raw asymmetry



# Production asymmetry

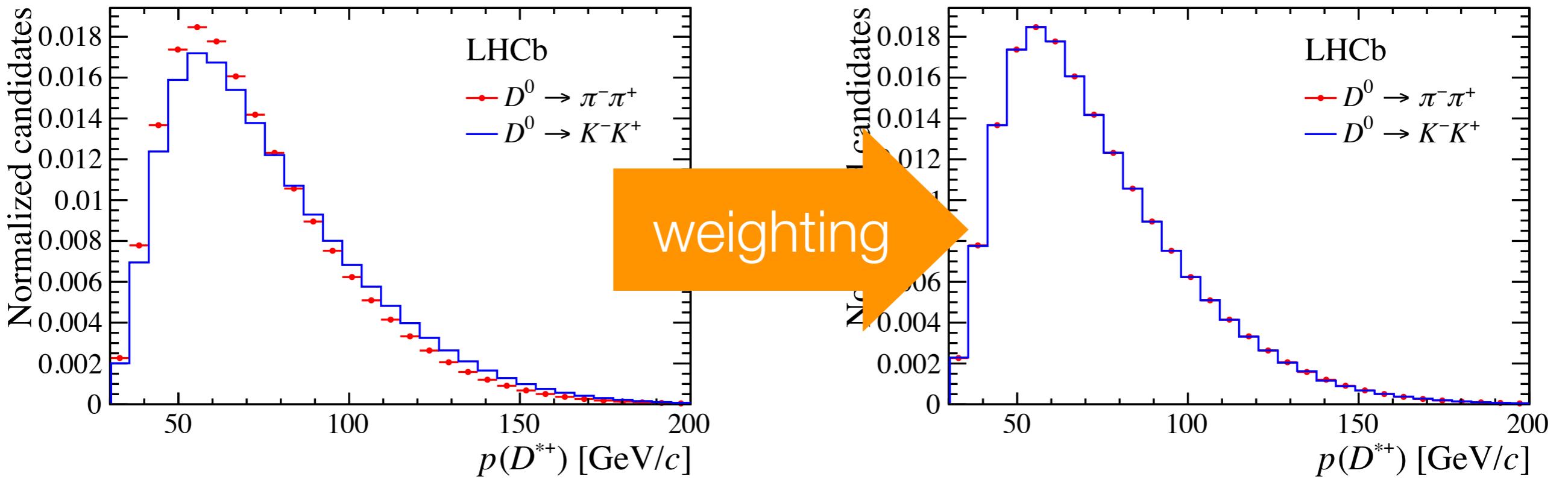
- In  $pp$  collision charm quarks are produced mostly through gluon fusion (which is charge symmetric)
- However, the  $c$  and the  $\bar{c}$  quarks may “recombine” with some of the proton valence quarks (beam-drag effect) creating an asymmetric production of charm mesons or baryons
- The effect is enhanced in the forward region, where the charm pair is collinear with the protons’ direction



# Kinematic weighting

[PRL 122 (2019) 211803]

- Detection and production asymmetries are expected to depend on kinematics
- Their cancellation may not be accurate if the kinematic distributions of the reconstructed  $D^0 \rightarrow K^+K^-$  and  $D^0 \rightarrow \pi^+\pi^-$  candidates differ
- Observed differences are removed through a weighting procedure — the resulting net effect on  $\Delta A_{CP}$  is anyhow marginal (below  $10^{-4}$ )



# Results

[PRL 122 (2019) 211803]

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$\Delta A_{CP}$ [10 <sup>-4</sup> ]	
$-18.2 \pm 3.2 \text{ (stat)} \pm 0.9 \text{ (syst)}$	$\pi$ tagged (Run 2)
$-9 \pm 8 \text{ (stat)} \pm 5 \text{ (syst)}$	$\mu$ tagged (Run 2)

# Results

[PRL 122 (2019) 211803]

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$\Delta A_{CP}$ [10 <sup>-4</sup> ]	
$-18.2 \pm 3.2 \text{ (stat)} \pm 0.9 \text{ (syst)}$	$\pi$ tagged (Run 2)
$-9 \pm 8 \text{ (stat)} \pm 5 \text{ (syst)}$	$\mu$ tagged (Run 2)
$-10 \pm 8 \text{ (stat)} \pm 3 \text{ (syst)}$	$\pi$ tagged (Run 1) [PRL 116 (2016) 191601]
$-14 \pm 16 \text{ (stat)} \pm 8 \text{ (syst)}$	$\mu$ tagged (Run 1) [JHEP 07 (2014) 041]

# Results

[PRL 122 (2019) 211803]

$\Delta A_{CP}$ [10 <sup>-4</sup> ]	
-18.2 ± 3.2 (stat) ± 0.9 (syst)	$\pi$ tagged (Run 2)
-9 ± 8 (stat) ± 5 (syst)	$\mu$ tagged (Run 2)
-10 ± 8 (stat) ± 3 (syst)	$\pi$ tagged (Run 1) [PRL 116 (2016) 191601]
-14 ± 16 (stat) ± 8 (syst)	$\mu$ tagged (Run 1) [JHEP 07 (2014) 041]
<b>-15.4 ± 2.9 (stat+syst)</b>	combined

5.3 $\sigma$  deviation from zero  
first observation of  $CP$  violation in charm

# Now what?

- Measured value is in the ballpark of the standard model value
- Difficult to say if new physics is at play. Need better control of the QCD effects
- Experimentally look for  $CP$  violation in radiative decays, test isospin sum rules and SU(3) related modes
- Huge program of measurements, where Belle II role with neutrals will be crucial

from Alexey's talk yesterday

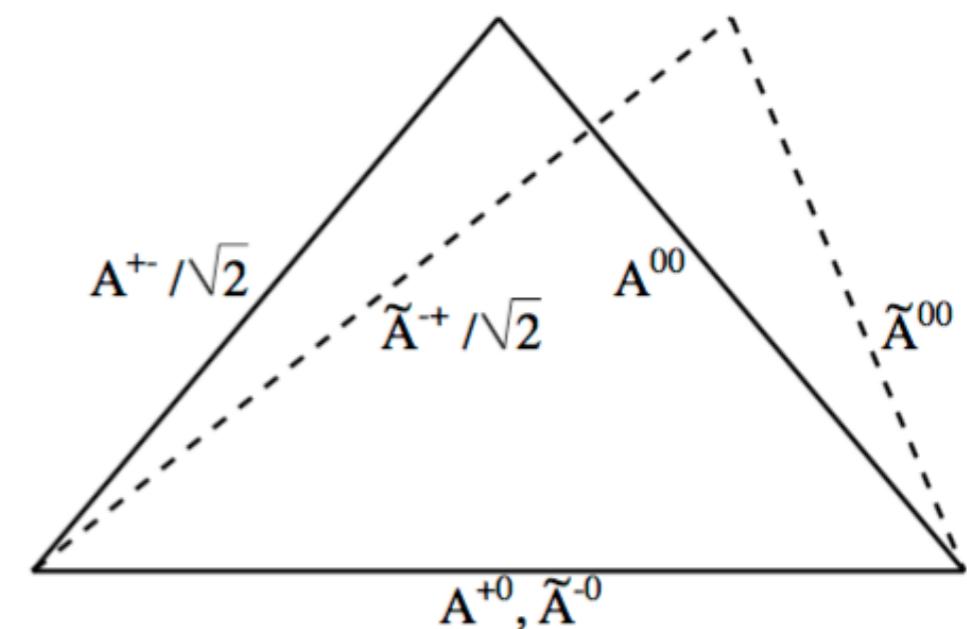
- several final states possible, for  $D \rightarrow \pi^i \pi^k$

$$\frac{1}{\sqrt{2}} A^{+-} = A^{+0} - A^{00},$$

$$\frac{1}{\sqrt{2}} \bar{A}^{-+} = \bar{A}^{-0} - \bar{A}^{00},$$

Gronau, London  
Bevan, Meadows

- others include  $D \rightarrow \pi\pi, \rho\pi, \rho\rho$

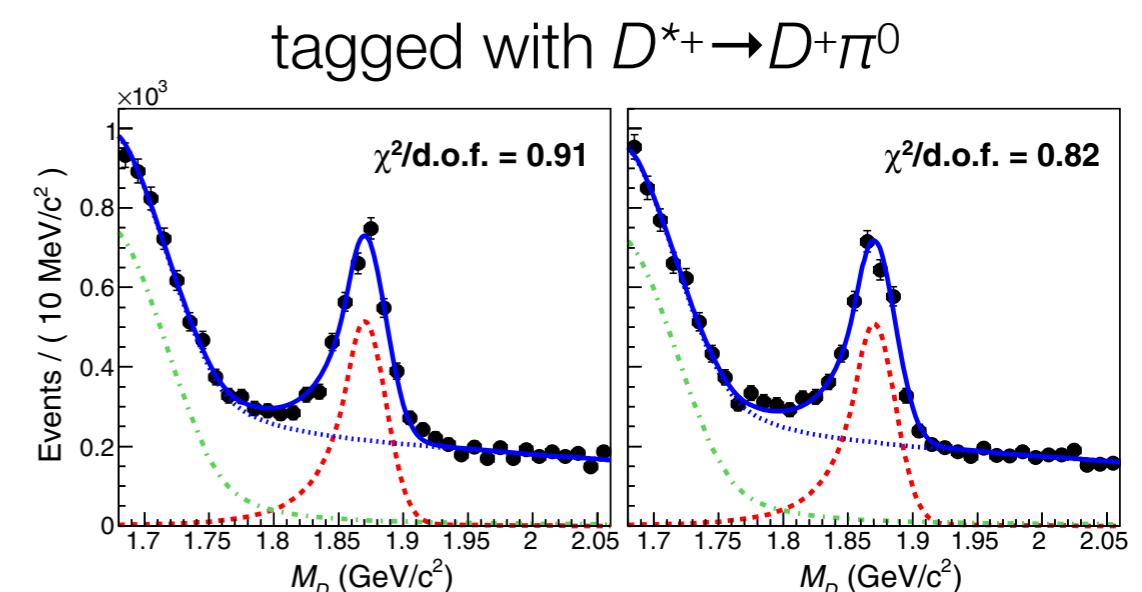
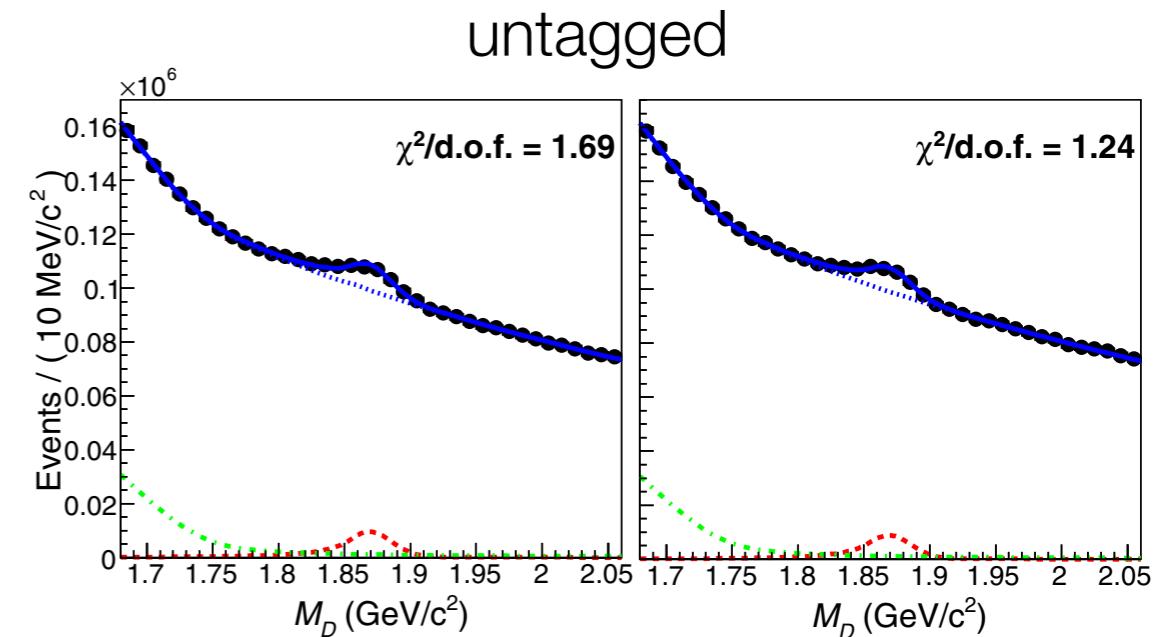


# $CP$ violation in $D^+ \rightarrow \pi^+ \pi^0$ decays

- In the standard model  $\Delta A_{CP}$  comes from  $\Delta U=0$  transitions
- $CP$  violation in  $\Delta U=1$ , e.g. in  $D^+ \rightarrow \pi^+ \pi^0$ , would unambiguously be new physics
- Current best measurement from Belle (1/ab)

$$A_{CP} = (2.3 \pm 1.2 \pm 0.2)\%$$

- $D^{*+}$  tagging crucial in suppressing the background
- Similar performances expected for Belle II. Sensitivity with 50/ab  $\sim 0.17\%$ , maybe possible at LHCb but difficult



[PRD 97 (2018) 011101(R)]

# Prospects for direct $CP$ violation

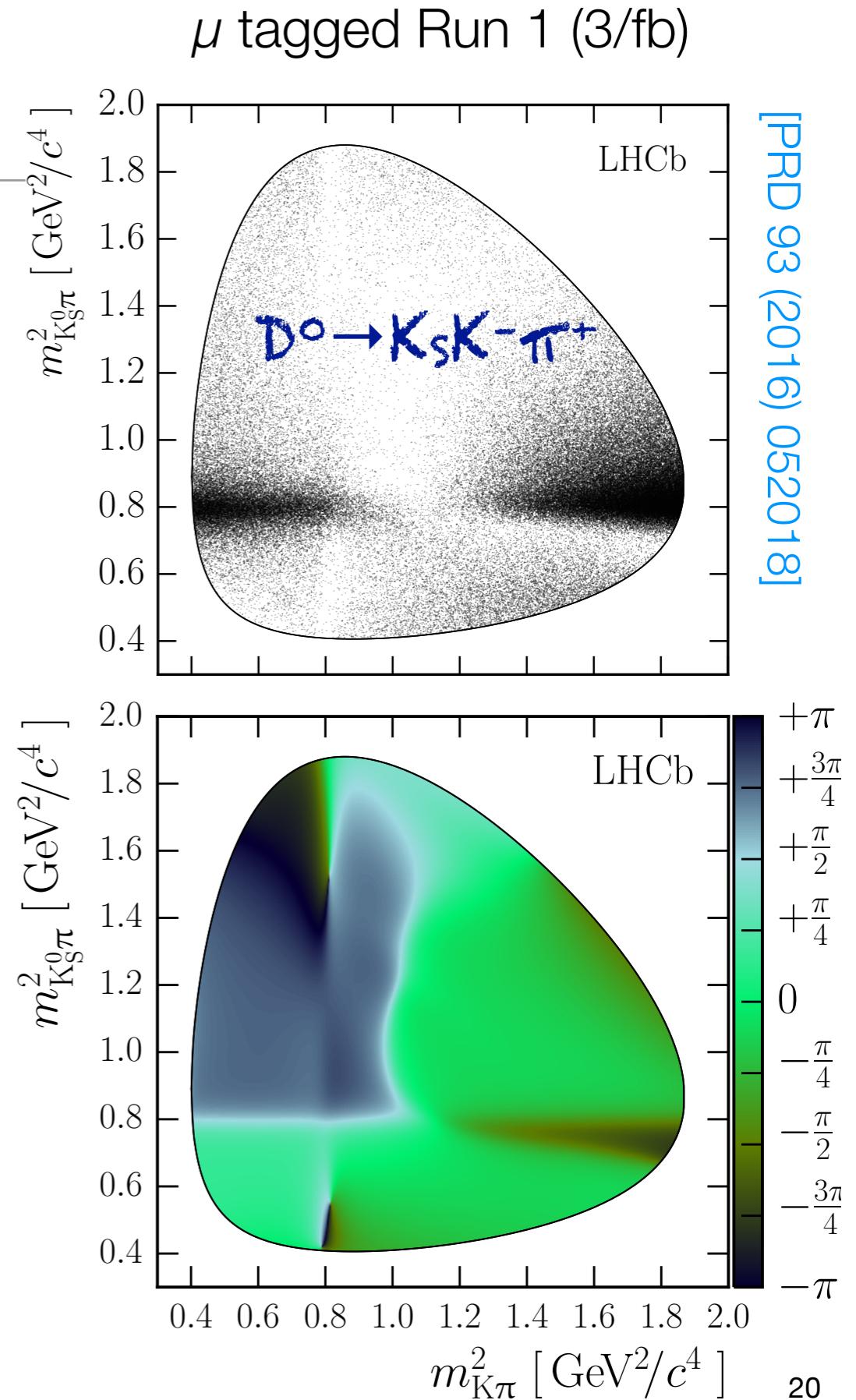
Decay mode	Current best sensitivity (stat + syst) [ $10^{-3}$ ]	LHCb 300/fb (stat only) [ $10^{-3}$ ]	Belle II 50/ab (stat+syst) [ $10^{-3}$ ]
$\Delta A_{CP}$	0.29	LHCb (9/fb)	0.03
$D^0 \rightarrow K^+ K^-$	1.8	LHCb (3/fb)	0.07
$D^0 \rightarrow \pi^+ \pi^-$	1.8	LHCb (3/fb)	0.07
$D^0 \rightarrow \pi^0 \pi^0$	6.5	Belle (1/ab)	(?)
$D^0 \rightarrow K^+ \pi^-$	9.1	LHCb (5/fb)	0.5
$D^0 \rightarrow K_S K_S$	15	Belle (1/ab)	2.8
$D_s \rightarrow K_S \pi^+$	18	LHCb (6.8/fb)	0.32
$D^+ \rightarrow K_S K^+$	0.76	LHCb (6.8/fb)	0.12
$D^0 \rightarrow \phi \gamma$	66	Belle (1/ab)	(?)
$D^0 \rightarrow \rho^0 \gamma$	150	Belle (1/ab)	(?)
$D^+ \rightarrow \phi \pi^+$	0.49	LHCb (4.8/fb)	0.06
$D^+ \rightarrow \pi^0 \pi^+$	13	Belle (1/ab)	(?)

# CPV in multi-body decays

- Enriched dynamics of multi-body decays allows to look for  $CP$  violation in subregions of the phase space
  - Additional sensitivity with respect to global asymmetries (which could average to zero for small values of  $\delta$ )

$$A_{CP} \sim \sin \phi \sin \delta$$

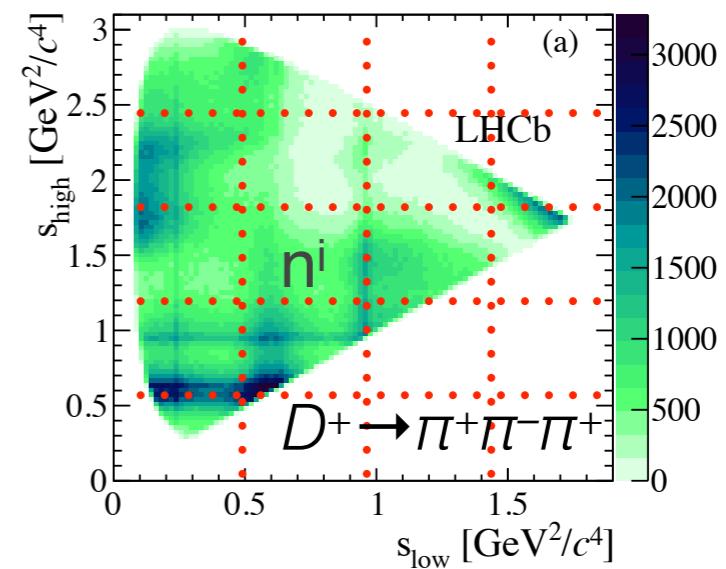
- Mostly insensitive to production and detection asymmetries
- Both model-dependent and model-independent measurements are possible
- 4-body final states give also access to  $CP$  violation in  $P$ -odd amplitudes ( $\sim \cos \delta$ )



# Search for “local” $CP$ violation across Dalitz plot

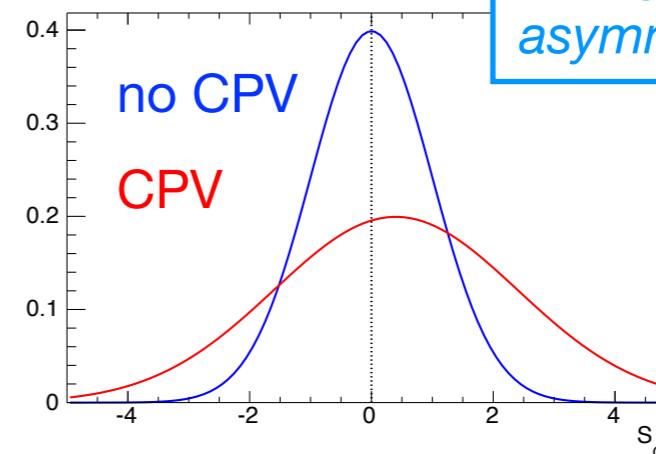
- Compute local  $CP$  asymmetry in different bins of the Dalitz plot
- In absence of  $CP$  violation, the distribution of local asymmetry is Gaussian with zero mean and unit variance
- Get  $p$ -value from  $\chi^2 = \sum_i (S_{CP}^i)^2$
- Test several binning schemes (same number of events/same strong phase) to enhance sensitivity

Binned (a.k.a. Miranda) method



$$S_{CP}^i = \frac{n^i(D^+) - \alpha n^i(D^-)}{\sqrt{n^i(D^+) + \alpha n^i(D^-)}}$$

to account  
for global  
asymmetries  $\alpha = \frac{N(D^+)}{N(D^-)}$



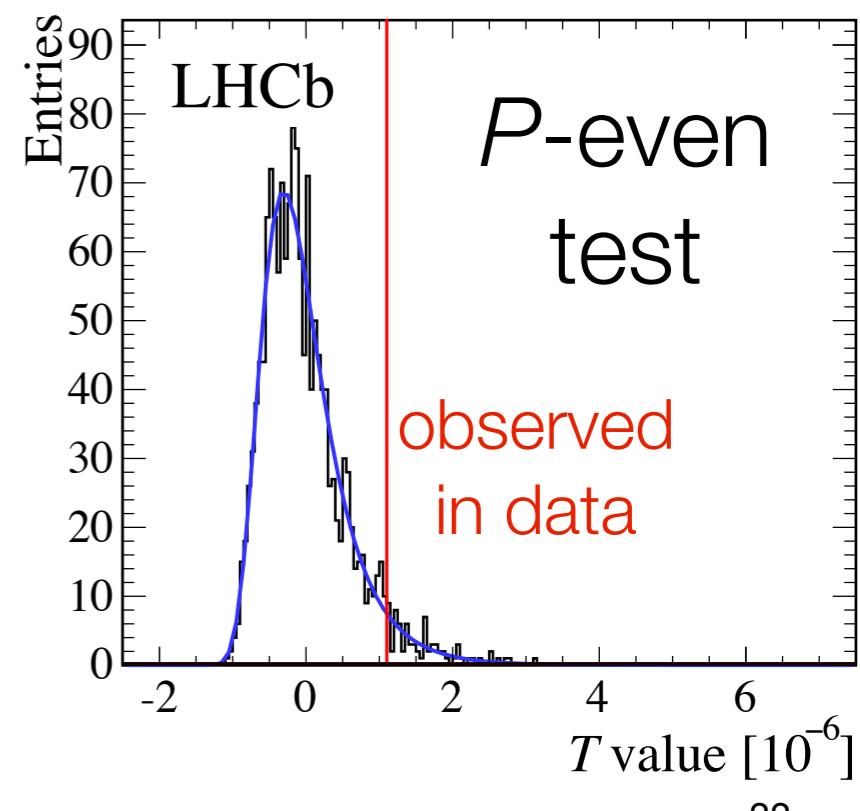
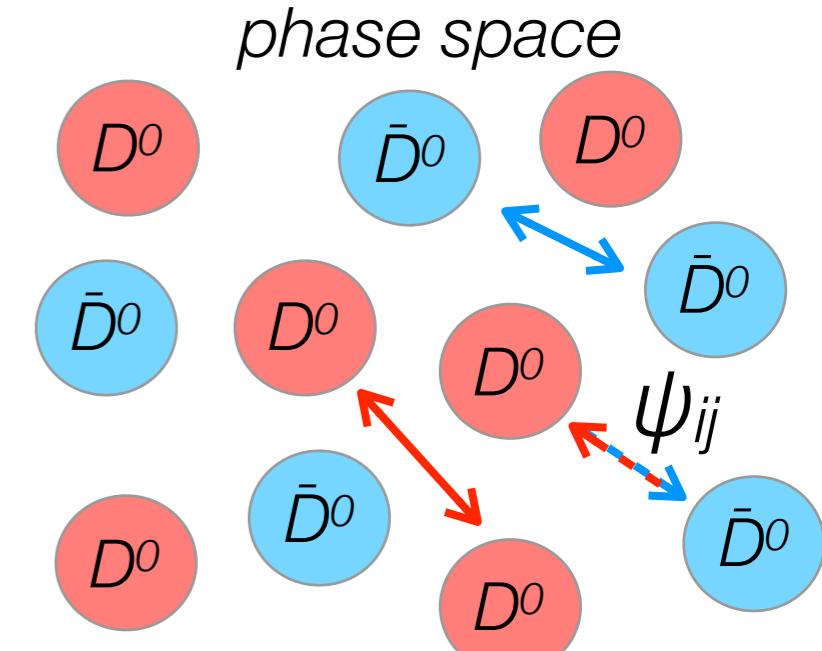
# Local CPV in $D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ decays

[PLB 769 (2017) 345]

- Statistical comparison of two distributions based on distance in phase space between pairs of particles

$$T = \left[ \sum_{i,j>i}^n \frac{\psi_{ij}}{n(n-1)} \right] + \left[ \sum_{i,j>i}^{\bar{n}} \frac{\psi_{ij}}{\bar{n}(\bar{n}-1)} \right] - \left[ \sum_{i,j}^{n,\bar{n}} \frac{\psi_{ij}}{n\bar{n}} \right],$$

- Compare with  $T$  distribution of no  $CP$ -violation case (randomize  $D$  flavor)
- Consistent with  $CP$  symmetry (in  $P$ -even amplitudes)



# Local CPV in $D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ decays

[PLB 769 (2017) 345]

- Statistical comparison of two distributions based on distance in phase space between pairs of particles

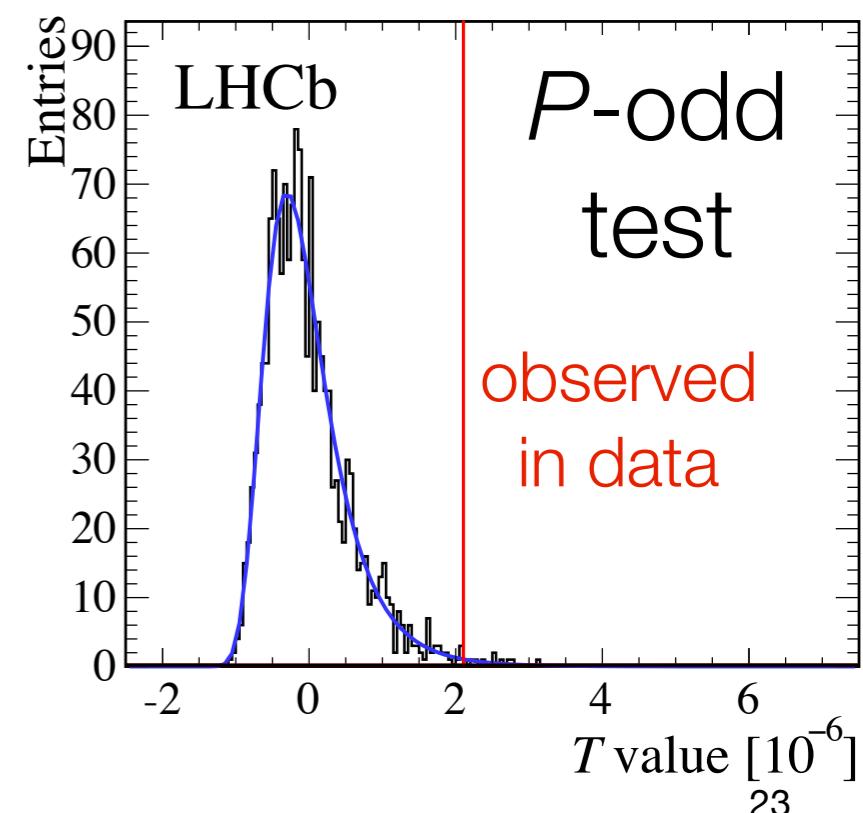
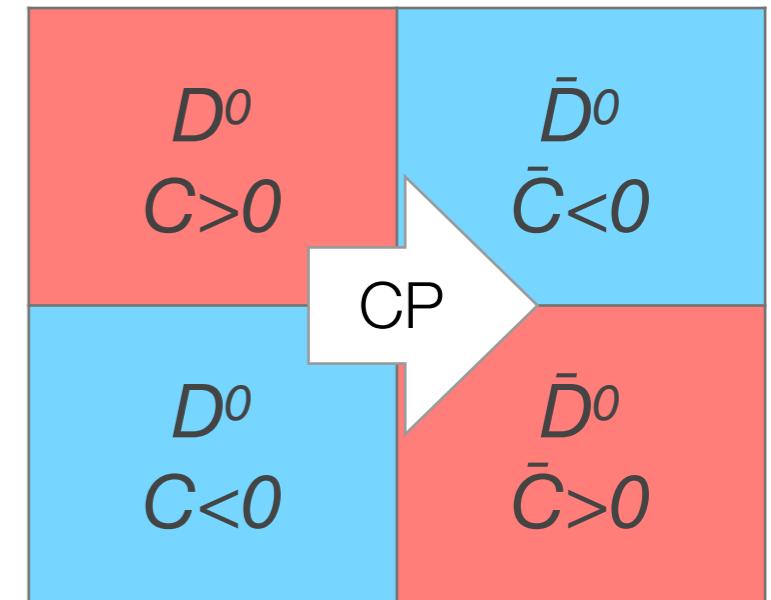
$$T = \sum_{i,j>i}^n \frac{\psi_{ij}}{n(n-1)} + \sum_{i,j>i}^{\bar{n}} \frac{\psi_{ij}}{\bar{n}(\bar{n}-1)} - \sum_{i,j}^{n,\bar{n}} \frac{\psi_{ij}}{n\bar{n}},$$

- Compare with  $T$  distribution of no  $CP$ -violation case (randomize  $D$  flavor)
- Use triple product to access  $P$ -odd  $CP$  violation

$$C = \vec{p}_{\pi^+} \cdot (\vec{p}_{\pi^+} \times \vec{p}_{\pi^-})$$

$$\bar{C} = \vec{p}_{\pi^-} \cdot (\vec{p}_{\pi^-} \times \vec{p}_{\pi^+})$$

- Results is marginally consistent with  $CP$  symmetry ( $2.7\sigma$ )



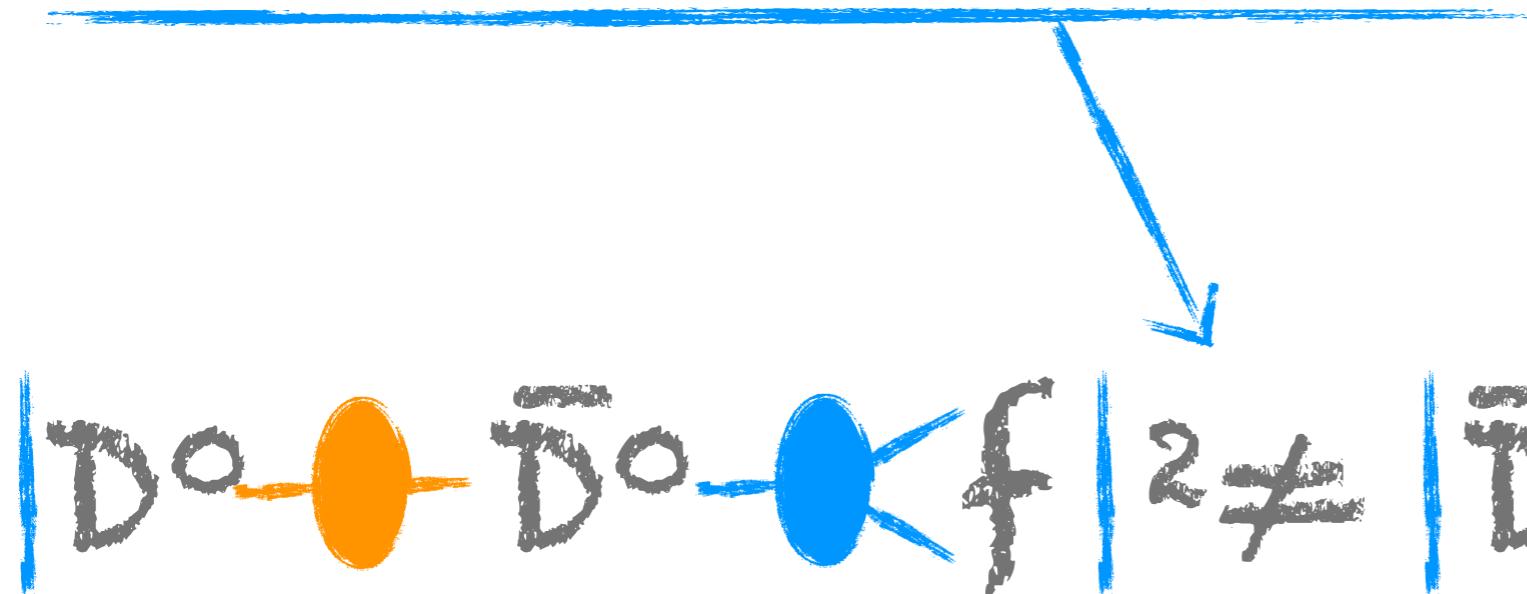
$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$$

$$x = (m_1 - m_2)/\Gamma$$

$$y = (\Gamma_1 - \Gamma_2)/2\Gamma$$

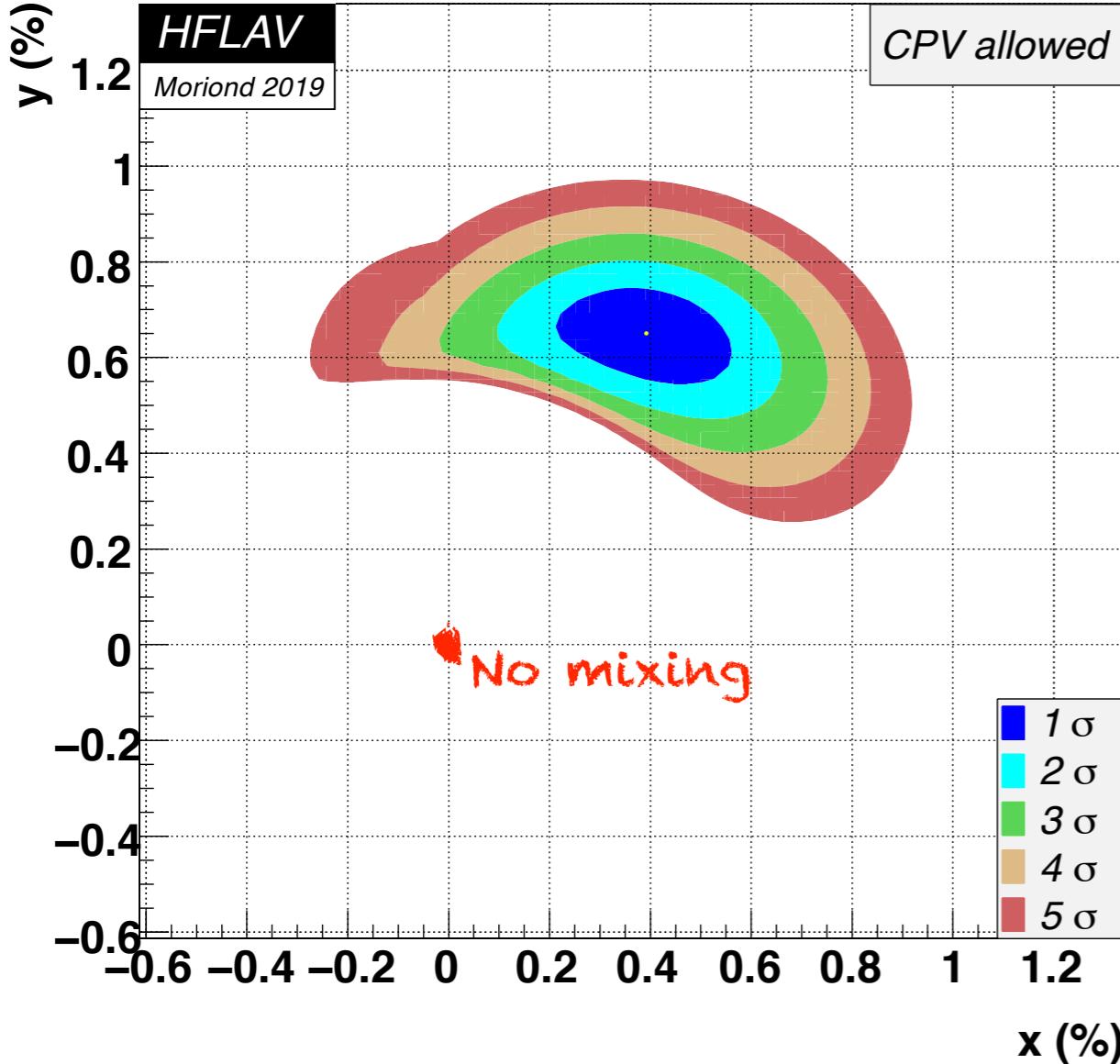
Mixing-induced  $CP$  violation

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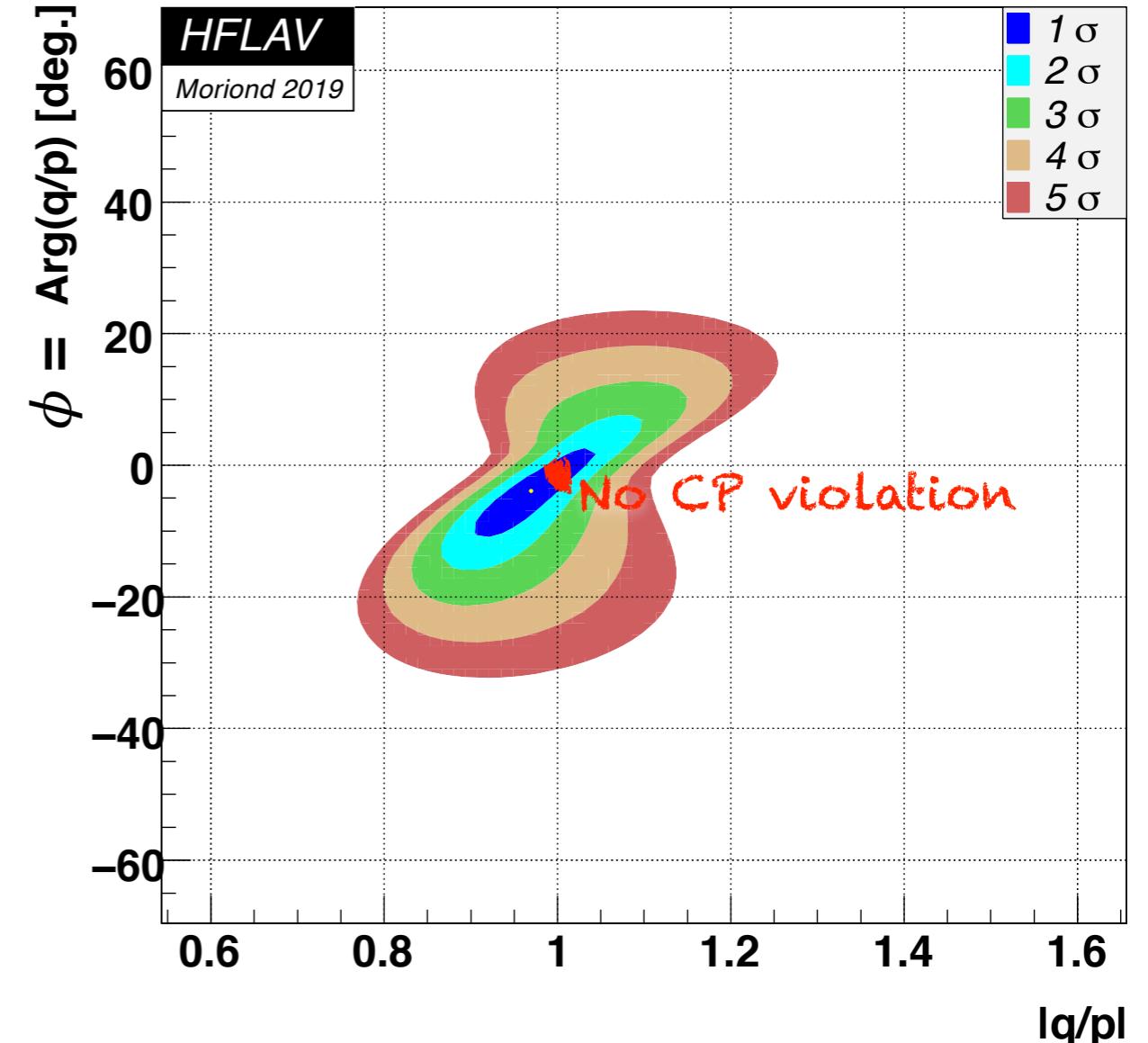
$$|D^0 -> D^0 -> f|^2 \neq |\bar{D}^0 -> D^0 -> f|^2$$

# Experimental status



$$x = (3.9 \pm 1.1) \times 10^{-3}$$

$$y = (6.51 \pm 0.63) \times 10^{-3}$$



$$|q/p| = 0.969^{+0.050}_{-0.045}$$

$$\phi = (-3.9 \pm 4.5)^\circ$$

# Mixing with $D^0 \rightarrow K^+ \pi^-$

$$R(t) = \frac{\Gamma(D^0 \rightarrow K^+ \pi^- | t)}{\Gamma(D^0 \rightarrow K^- \pi^+ | t)} \approx R_D + \sqrt{R_D} y' \left( \frac{t}{\tau} \right) + \frac{x'^2 + y'^2}{4} \left( \frac{t}{\tau} \right)^2$$

- The latest analysis from LHCb (5/fb) measures

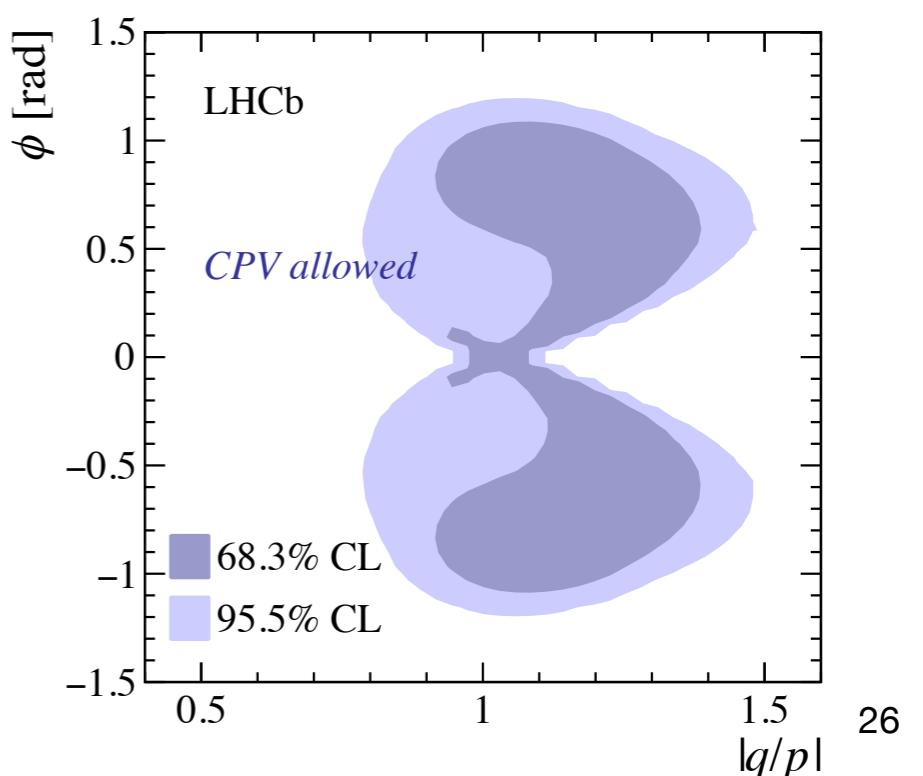
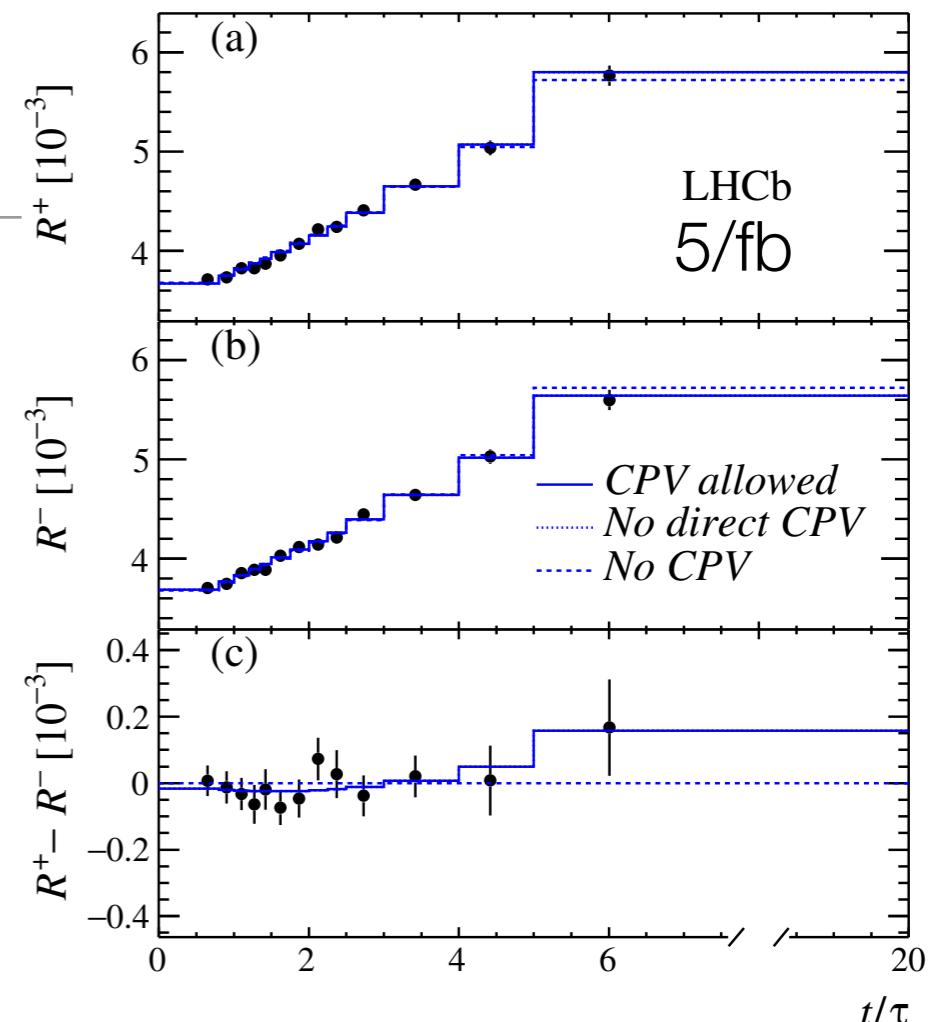
$$x'^2 = (3.9 \pm 2.7) \times 10^{-5}$$

$$y' = (5.28 \pm 0.52) \times 10^{-3}$$

and provides stringent bounds on direct CPV in DCS decays and CPV in mixing

$$1.00 < |q/p| < 1.35 @ 68\% \text{ CL}$$

- Belle II sensitivity with 50/fb not sufficient to compete with LHCb 9/fb

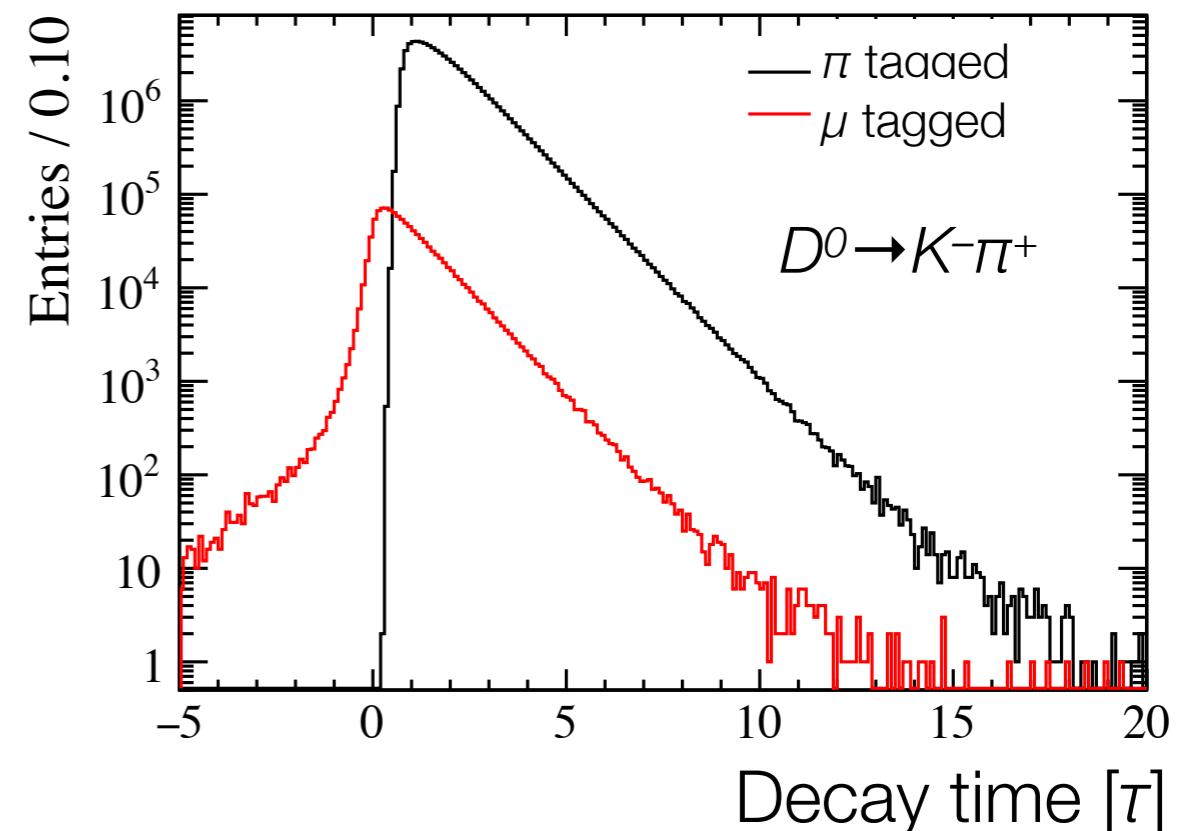
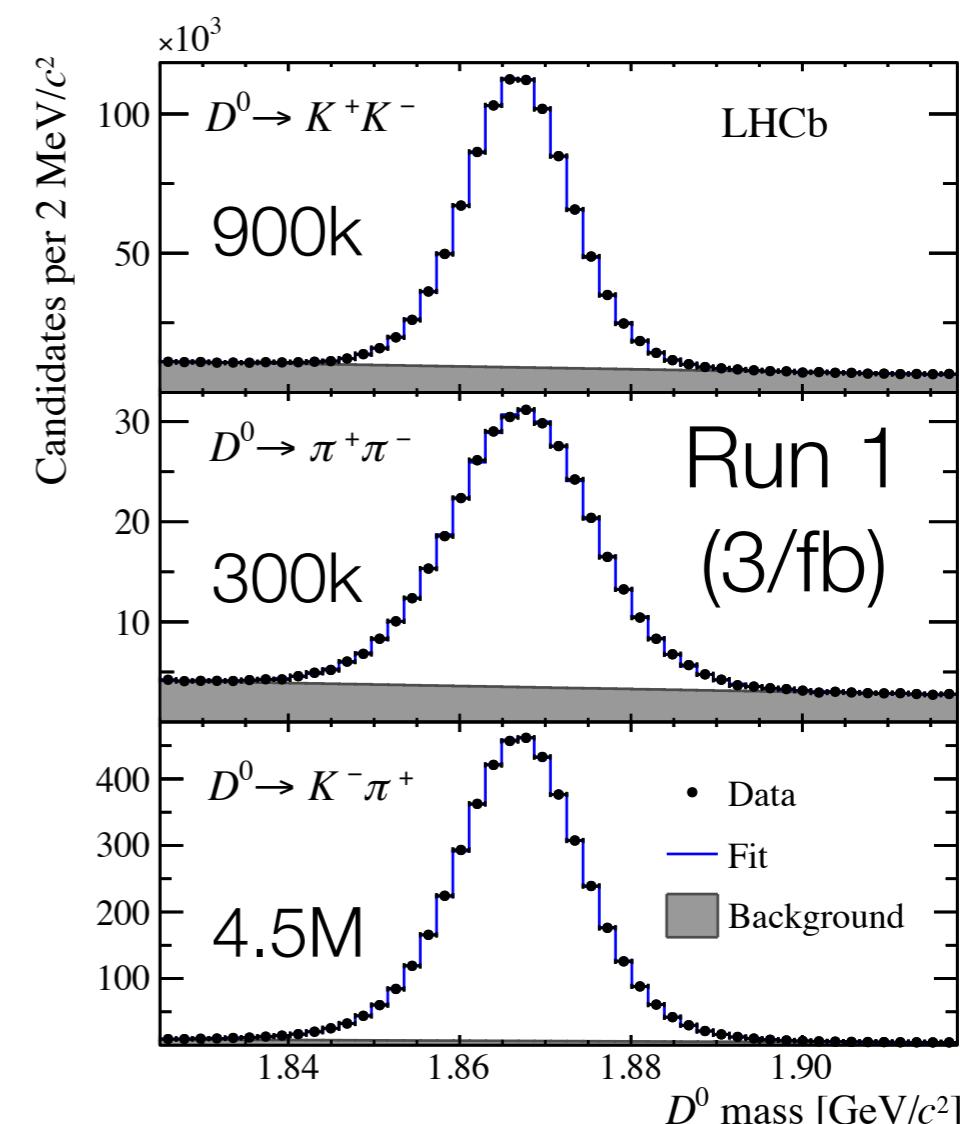


# Measurement of $y_{CP}$

- Effective lifetime of decays to  $CP$ -even final state (relative to  $CP$ -mixed)

$$y_{CP} \equiv \frac{\tau(K^-\pi^+)}{\tau(h^+h^-)} - 1$$

- Equal to  $y$  in case of  $CP$  symmetry
- Use  $\mu$ -tagged decays to reduce biases on  $D^0$  decay time
- Result with Run 1 data is as precise as the world average
- If LHCb does not manage to analyze the  $\pi$ -tagged sample, could be a measurement where Belle II can compete

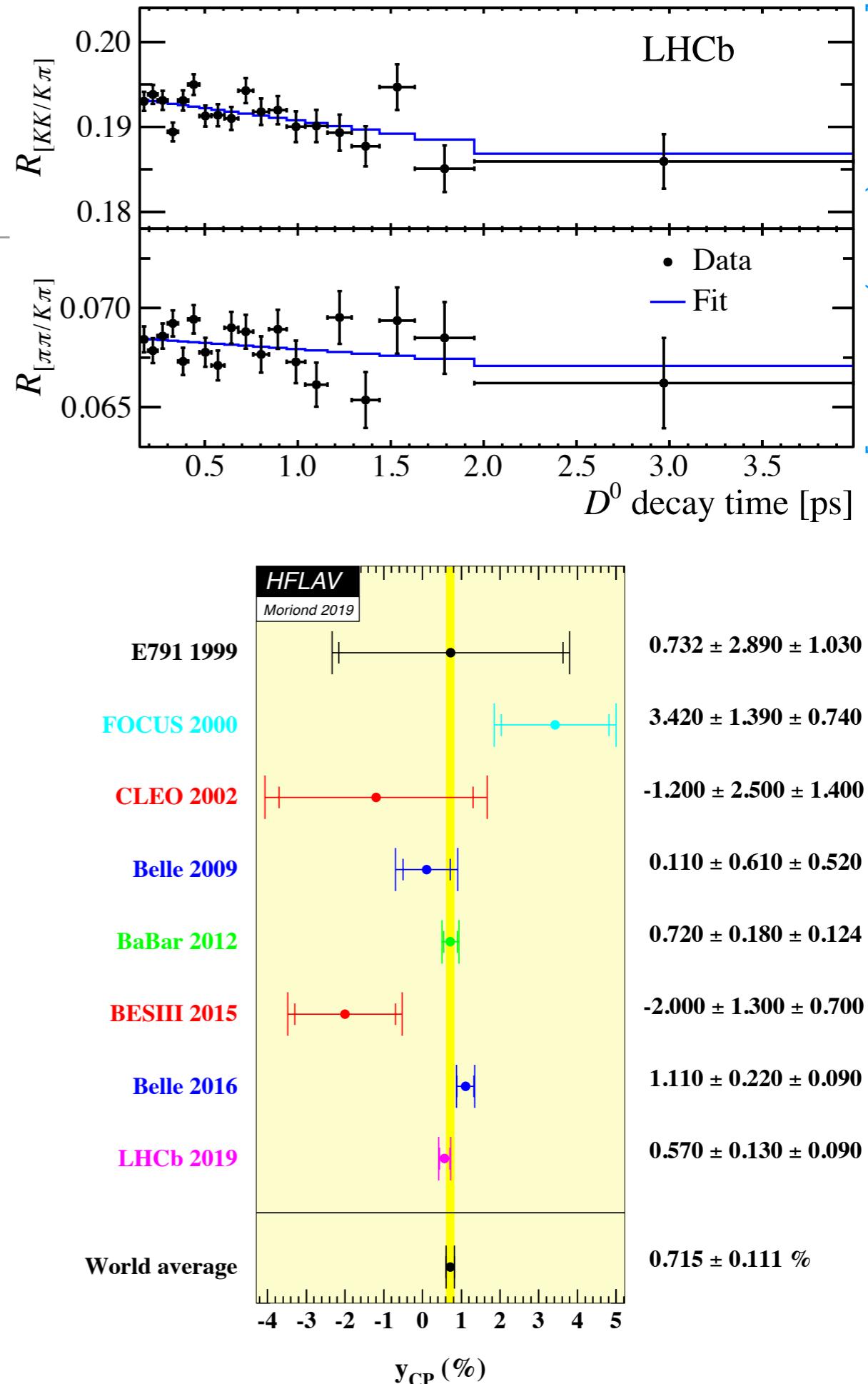


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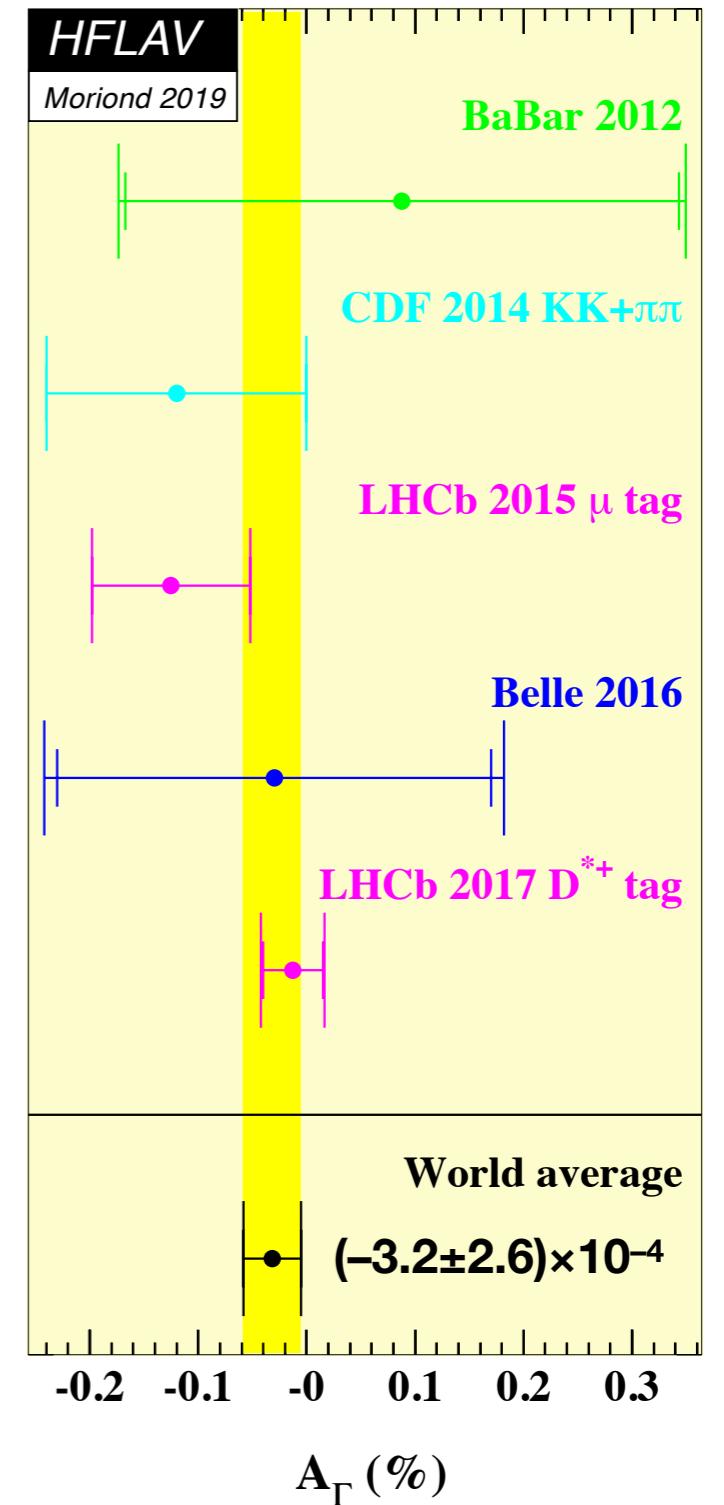


# Time-dependent $CP$ asymmetry in $D^0 \rightarrow h^+h^-$

- Small  $D^0$ - $\bar{D}^0$  mixing rate implies that time-dependent  $CP$  asymmetries can be approximated as

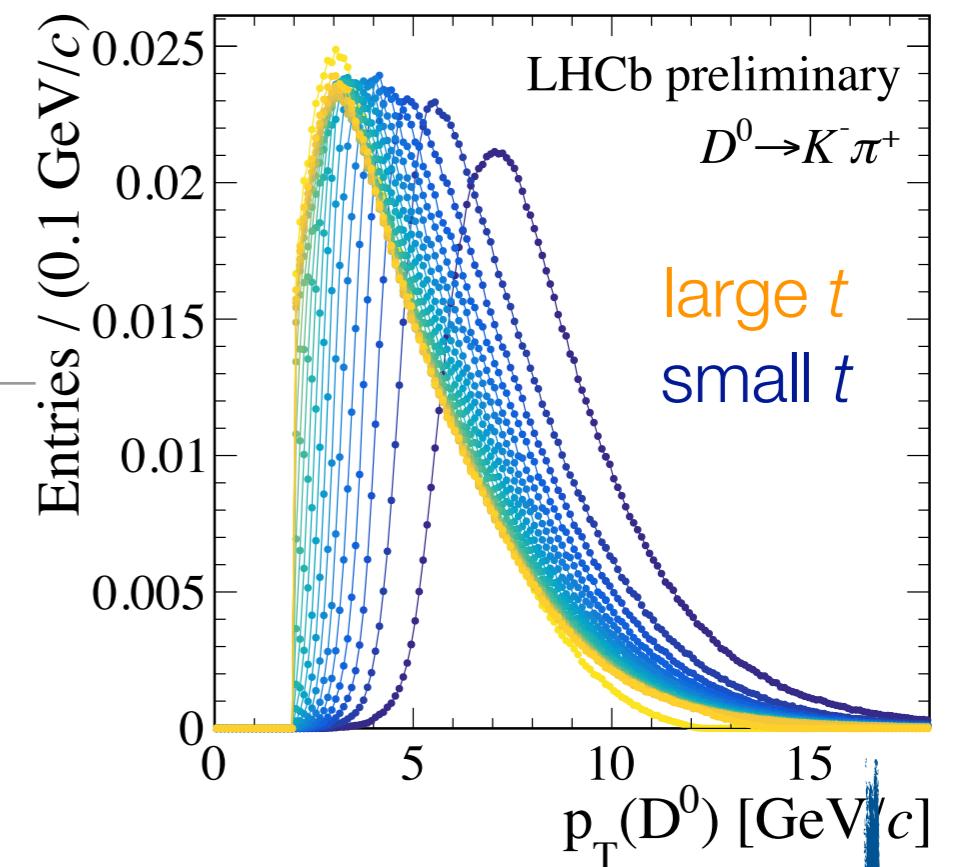
$$A_{CP}(h^+h^-) \approx a_{CP}^{\text{dir}}(h^+h^-) - \frac{t}{\tau} A_\Gamma$$

- Mixing-induced  $CP$  violation results in a nonzero value of the linear term
- Standard model expectation is at least one order of magnitude below the current experimental sensitivity

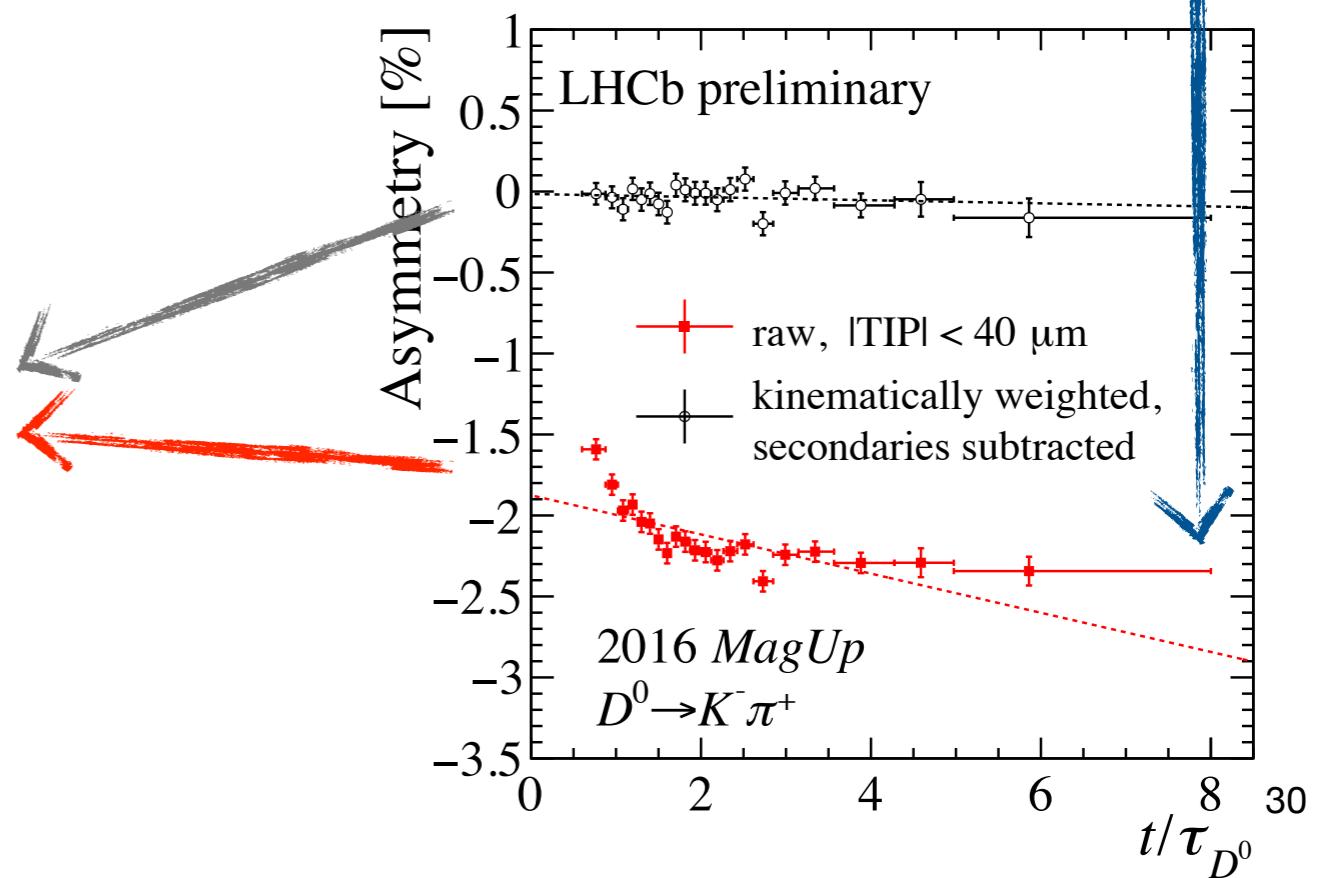
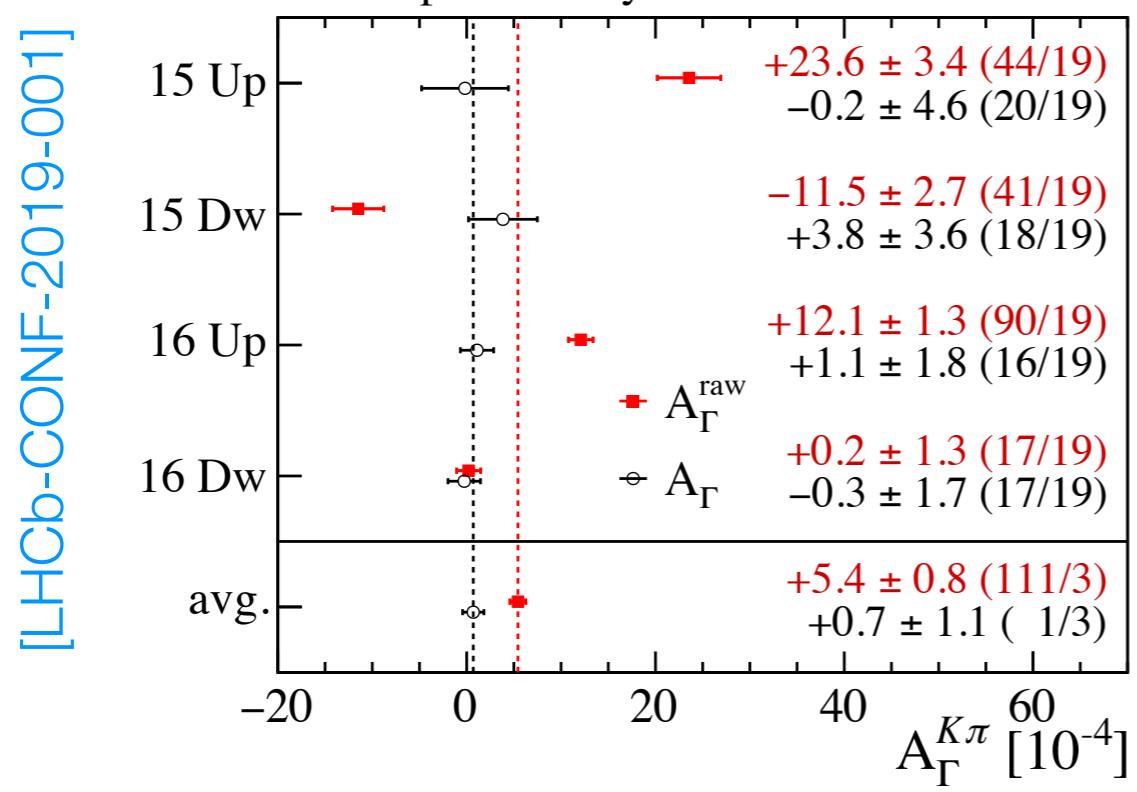


# Detection asymmetries

- Time-dependent detection asymmetries studied with large-yield samples of  $D^0 \rightarrow K^- \pi^+$  decays
- Removed by equalizing the 3D momentum distributions of  $D^0$  and  $\bar{D}^0$  candidates (separately for data-taking period and magnet polarity)



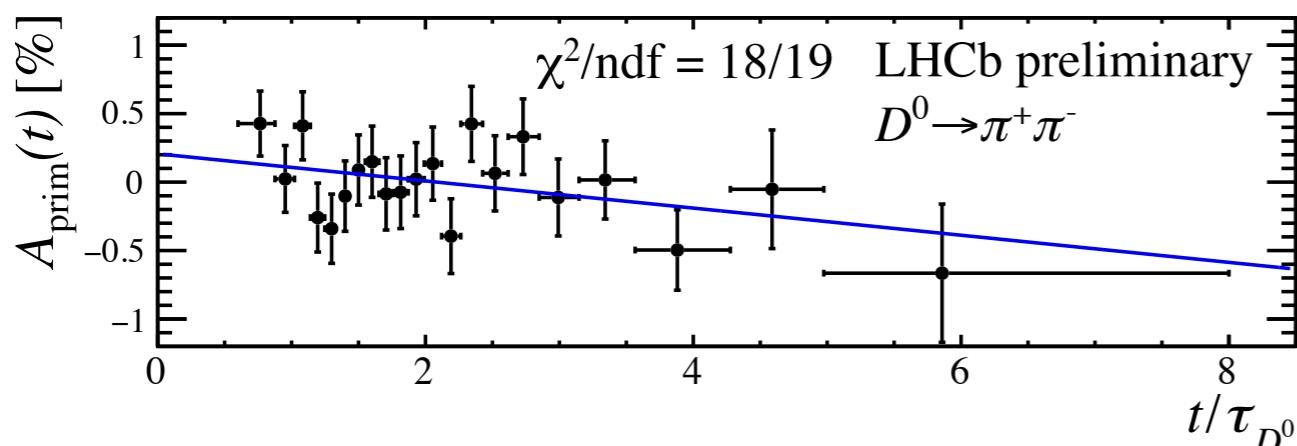
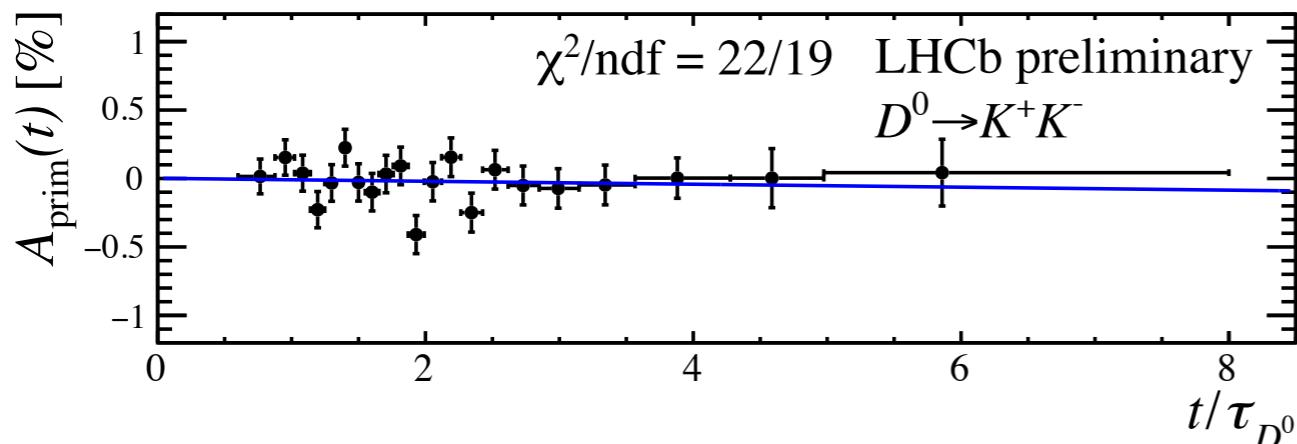
$p$ -dependent asymmetries and  $(p, t)$  correlations induce  $t$ -dependent asymmetries



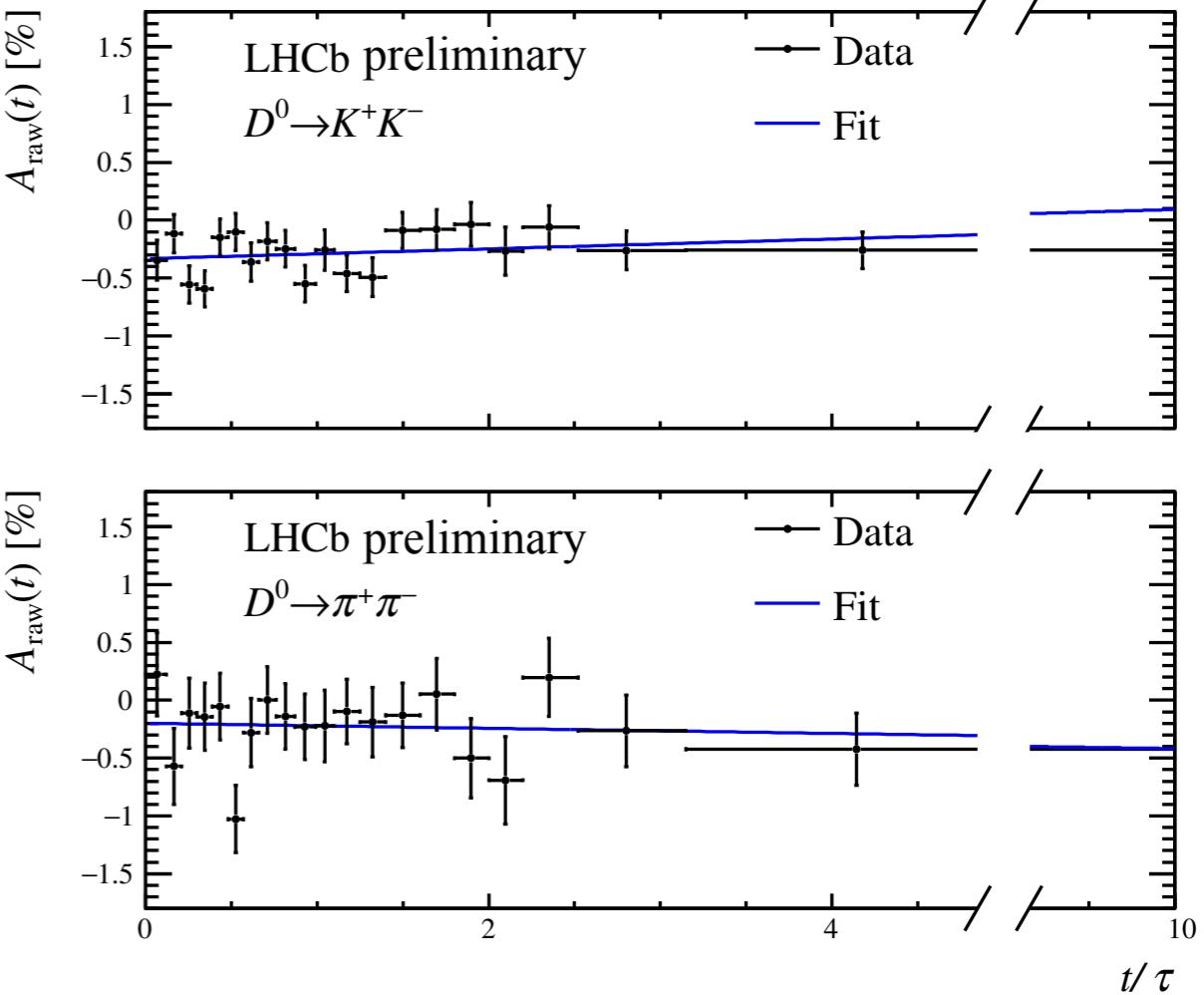
# Time-dependent $CP$ asymmetry in $D^0 \rightarrow h^+h^-$

[LHCb-CONF-2019-001]

$\pi$  tagged 1.9/fb (Run 2)



**NEW**  $\mu$  tagged 5.4/fb (Run 2)

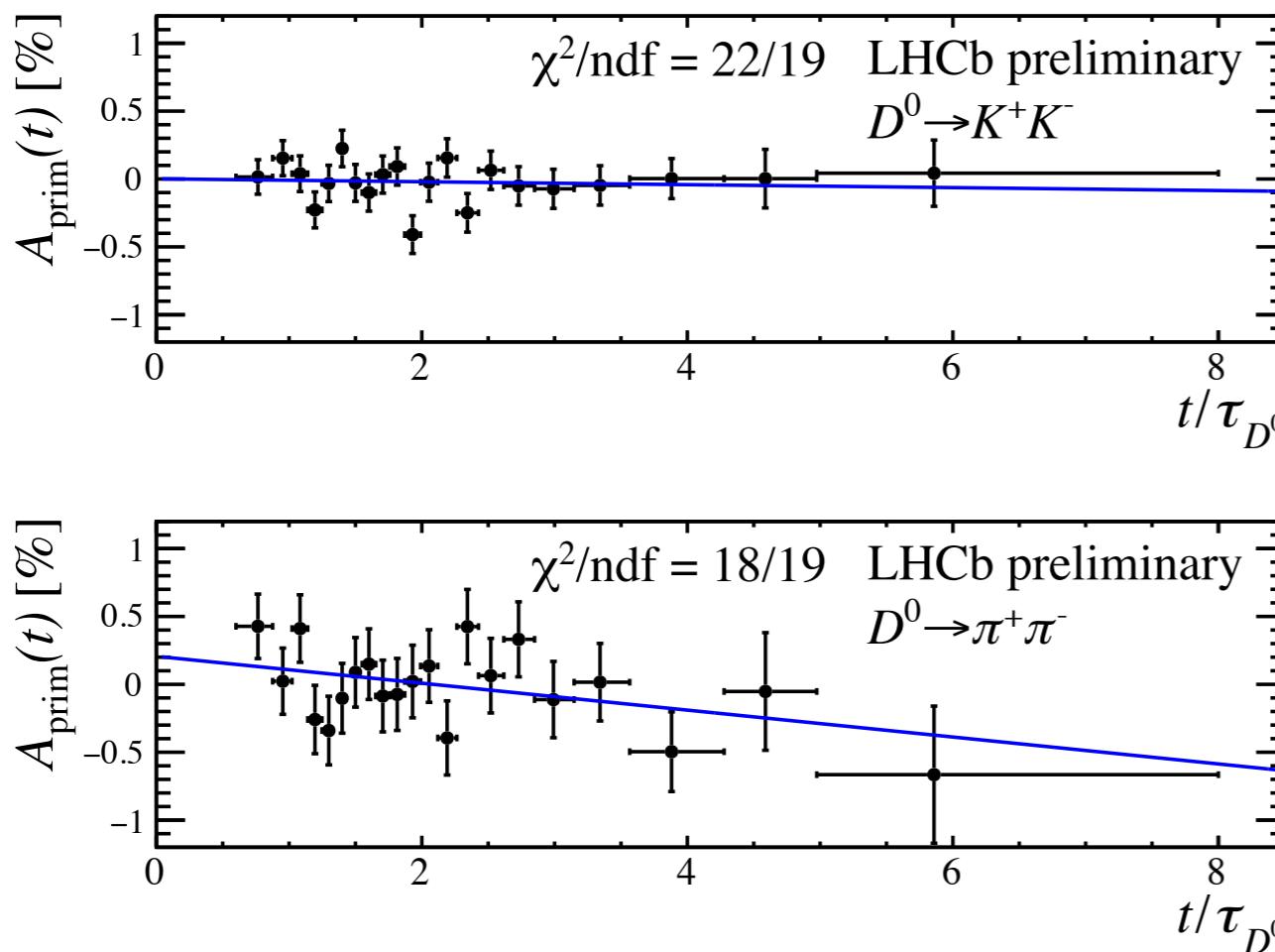


[LHCb-PAPER-2019-032 (in preparation)]

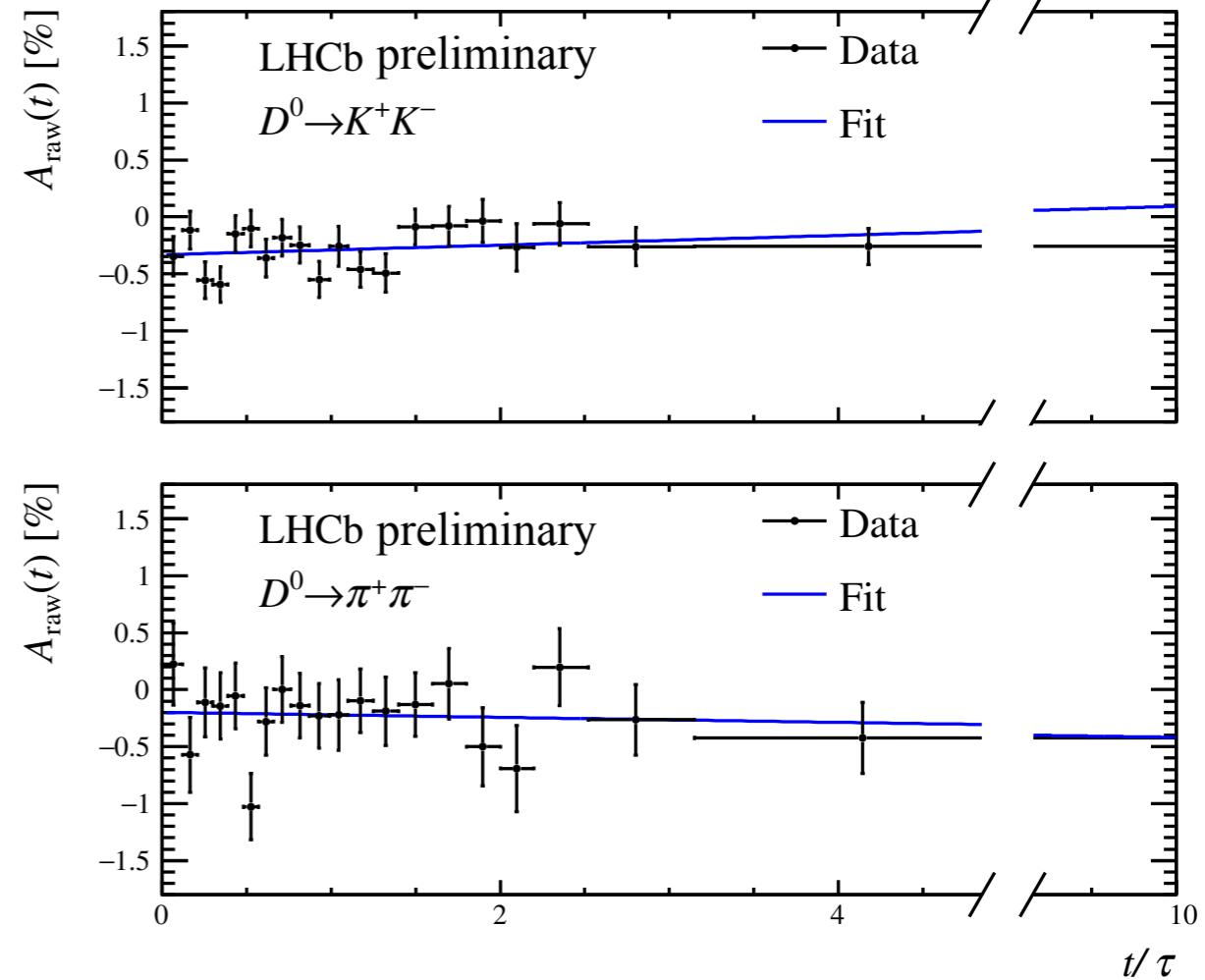
# Time-dependent $CP$ asymmetry in $D^0 \rightarrow h^+h^-$

[LHCb-CONF-2019-001]

$\pi$  tagged 1.9/fb (Run 2)



**NEW**  $\mu$  tagged 5.4/fb (Run 2)



- Averaging the four samples and combining with Run 1

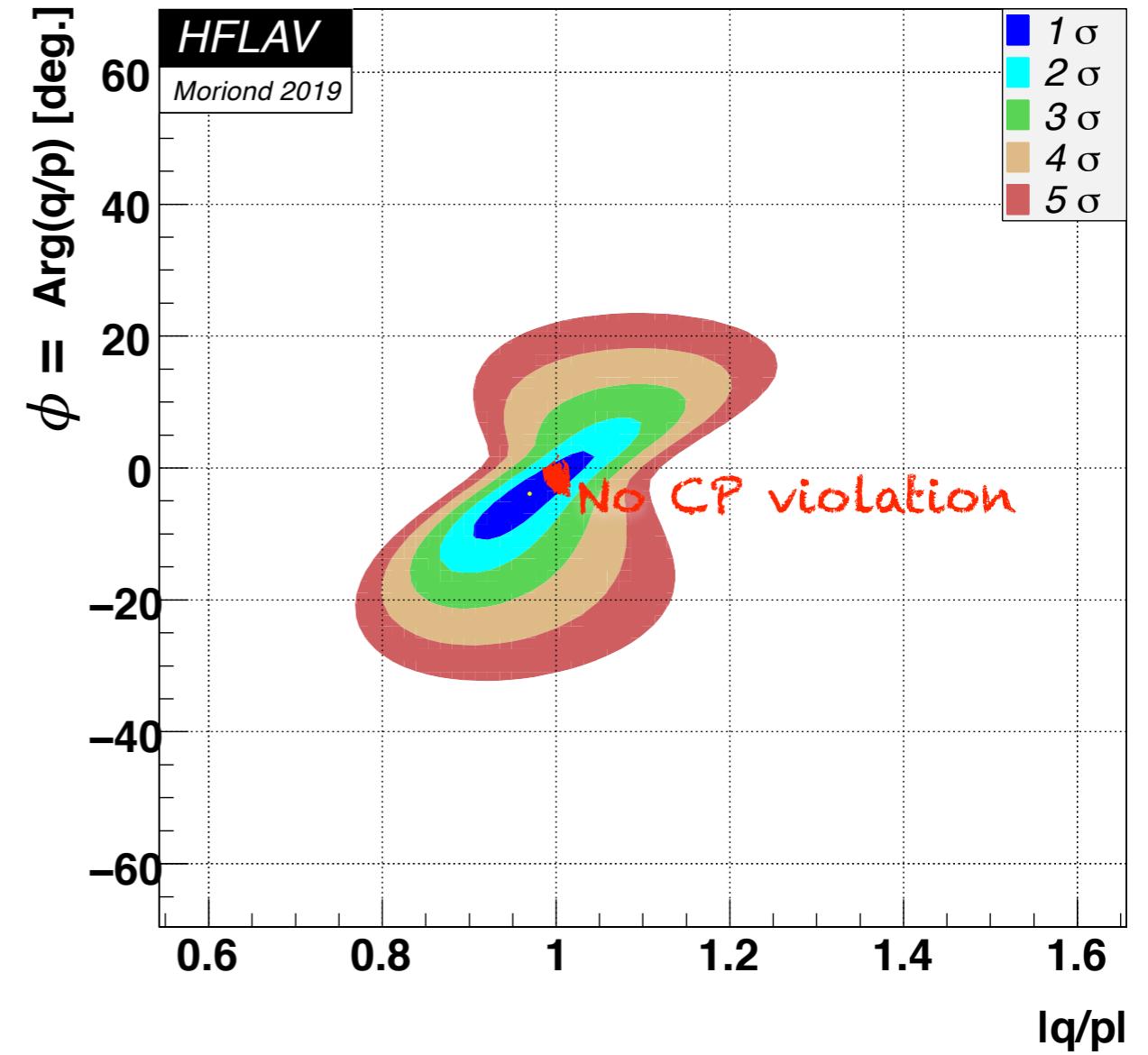
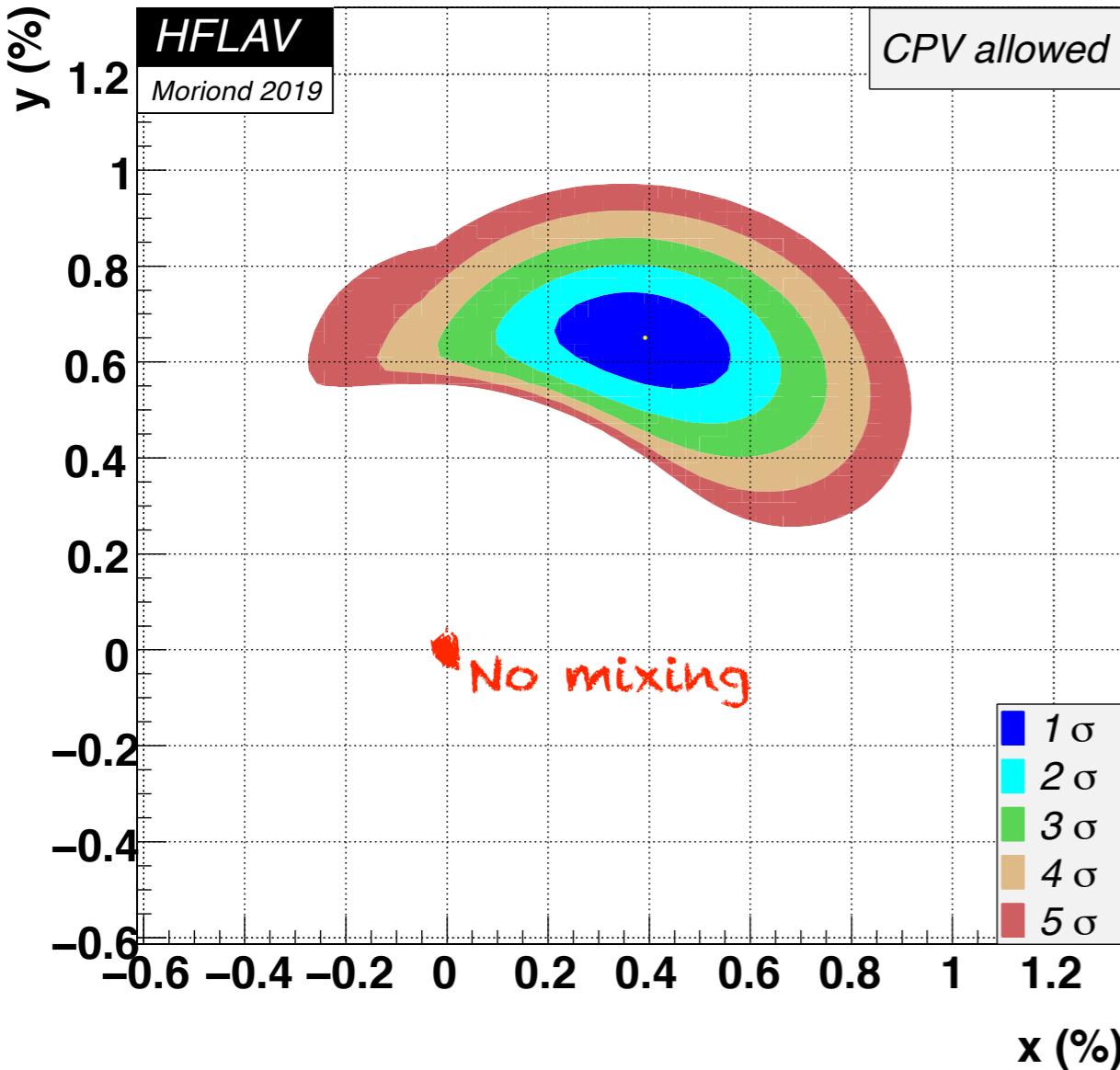
[PRL 118 (2017) 261803, JHEP 04 (2015) 043]

**PRELIMINARY**

$$A_\Gamma = [-1.1 \pm 1.7 \text{ (stat)} \pm 0.5 \text{ (stat)}] \times 10^{-4}$$

[LHCb-PAPER-2019-032 (in preparation)]

# Experimental status



$$x = (3.9 \pm 1.1) \times 10^{-3}$$

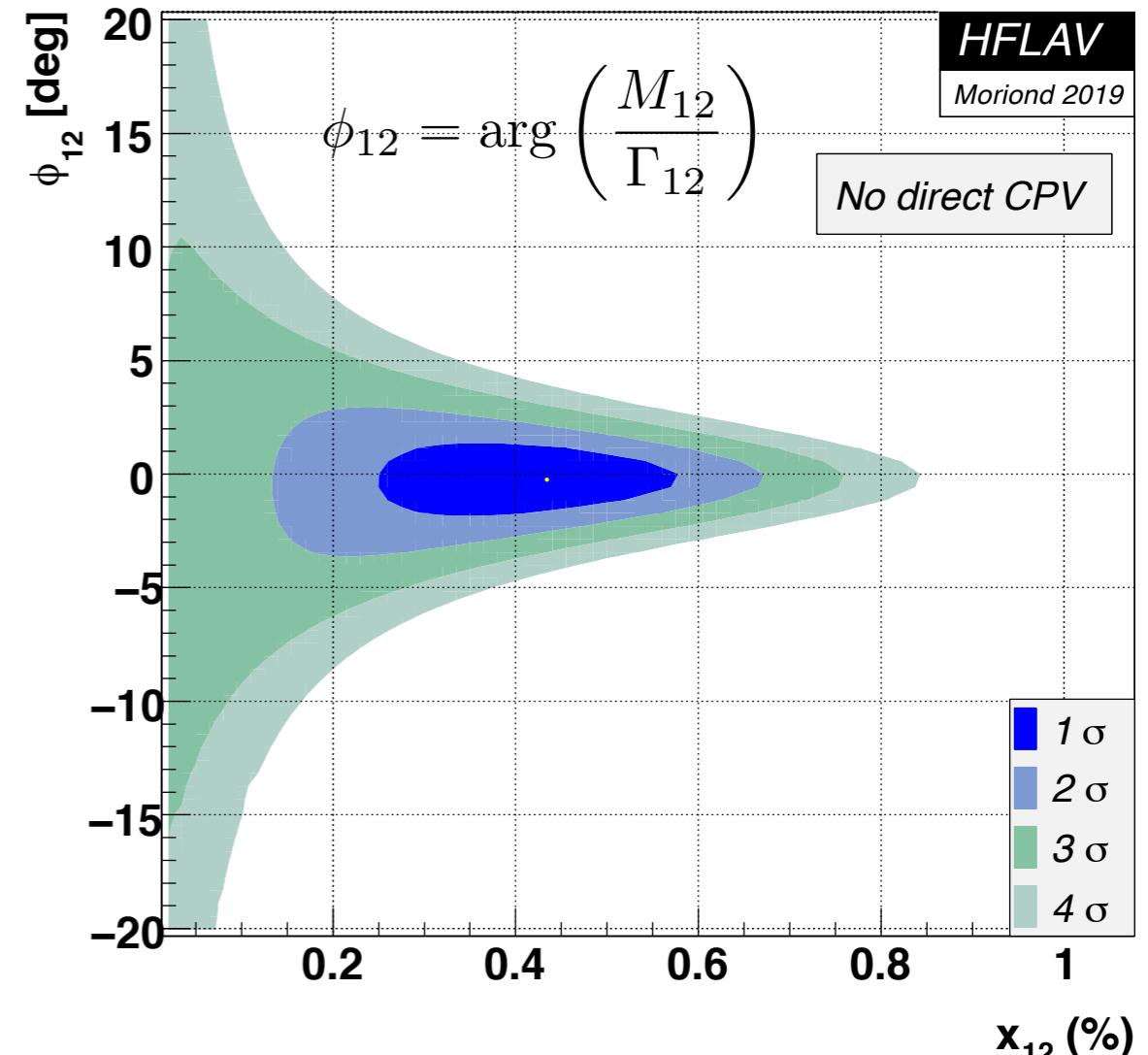
$$y = (6.51 \pm 0.63) \times 10^{-3}$$

$$|q/p| = 0.969 \pm 0.050$$

$$\phi = (-3.9 \pm 4.5)^\circ$$

# $x$ is the key

- Experimental sensitivity to the CP-violation in mixing limited by the knowledge of  $x_{12} \approx x$ 
  - $A_\Gamma \approx -x_{12} \sin\phi_{12}$  (superweak approx.)
  - Available mixing measurements are mostly based on decays to two-body final states ( $y_{CP} \approx y, y' \approx y$ )
  - Need more measurements with multi-body final states



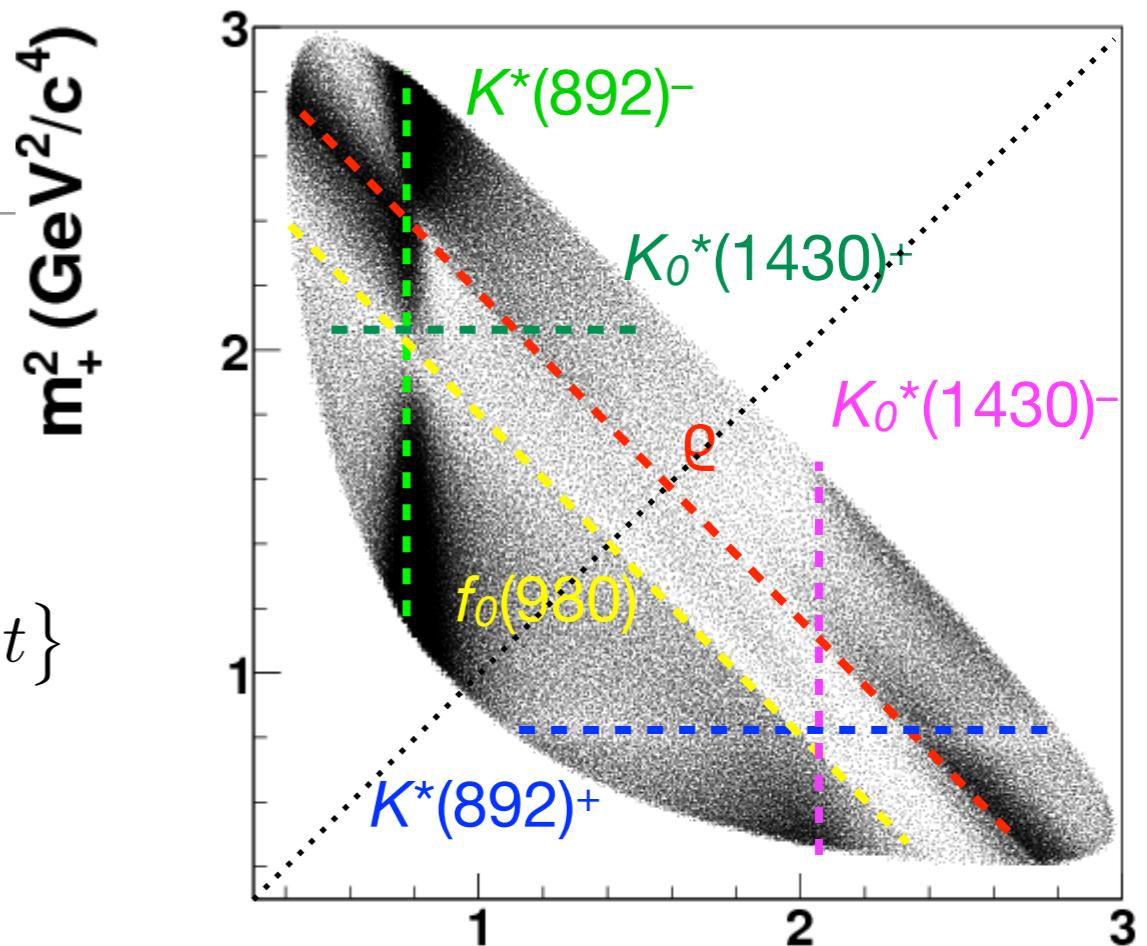
$$\phi_{12} = (-0.25^{+0.99}_{-0.96})^\circ$$

# Mixing with $D^0 \rightarrow K_S \pi^+ \pi^-$

- Multiple interfering amplitudes enhance the sensitivity to mixing

$$\mathcal{P}_{D^0} \propto e^{-\Gamma t} \{ |\mathcal{A}_{D^0}|^2 - \text{Re}[\mathcal{A}_{D^0}^* \mathcal{A}_{\bar{D}^0}(y + ix)] \Gamma t \}$$

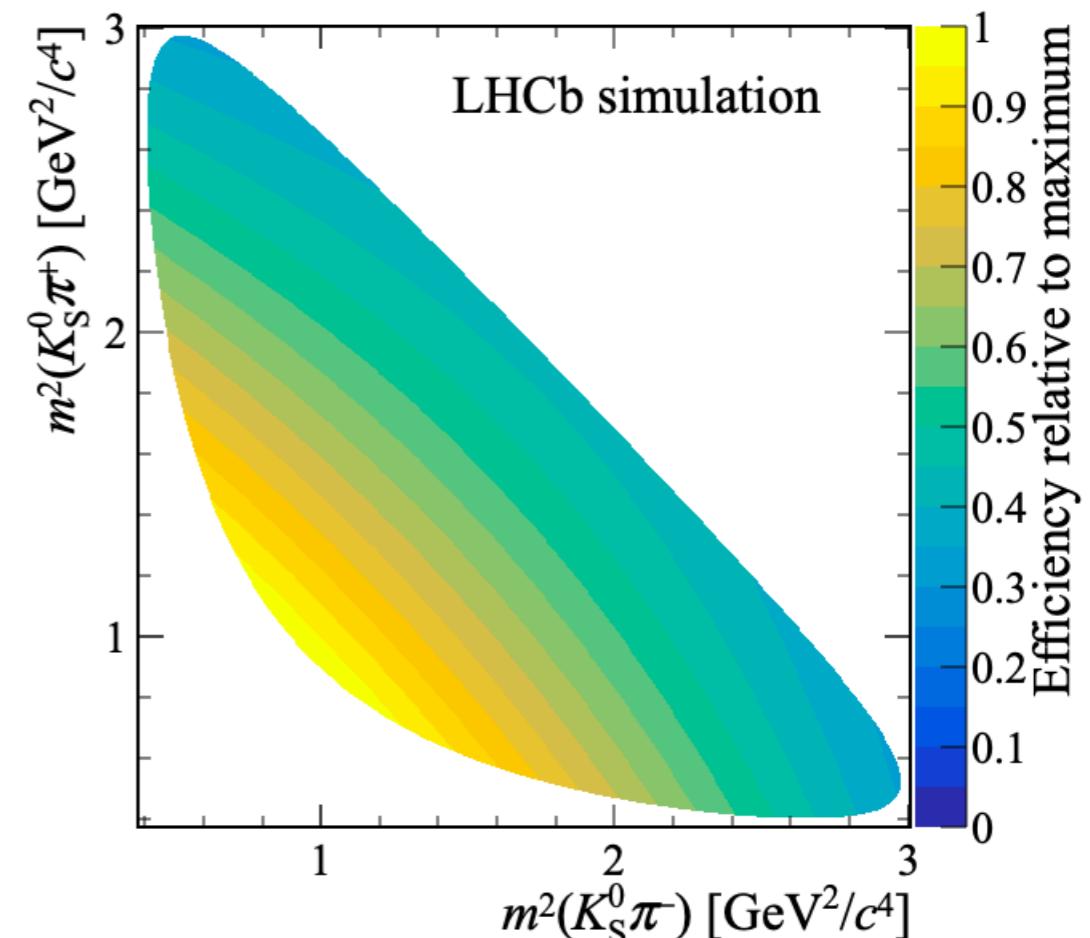
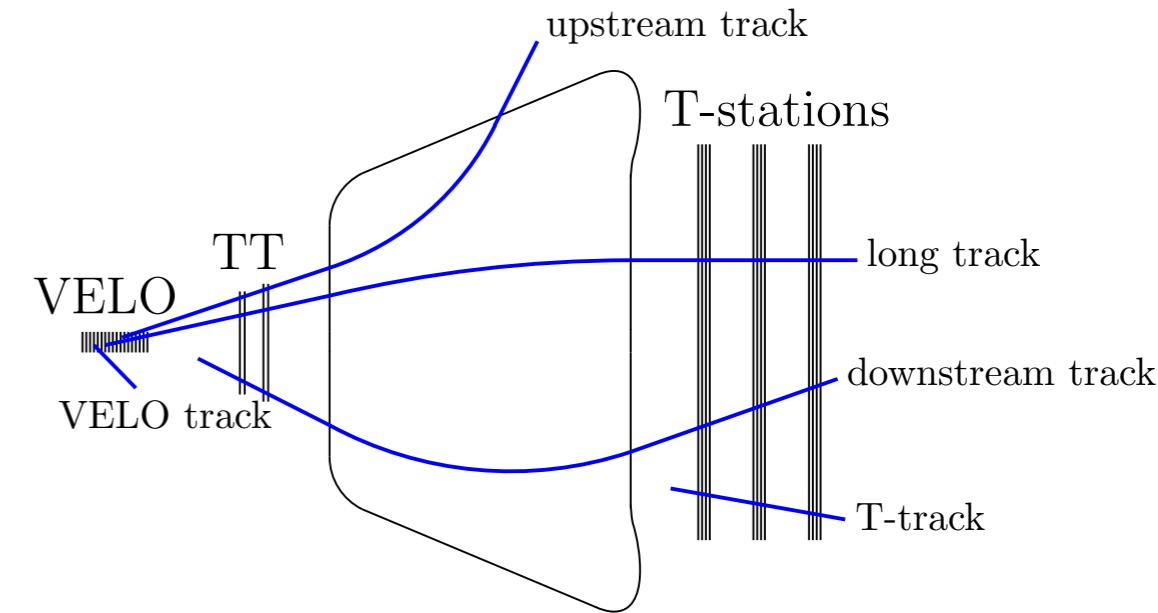
- Requires a time-dependent Dalitz-plot analysis
- Pioneered by CLEO in 2005, then followed by  $B$  factories with larger yields
- Belle 1/ab result has been for long the best determination of  $x$  available



Belle		$m^2 (\text{GeV}^2/\text{c}^4)$
Fit type	Parameter	Fit result
No CPV	$x(\%)$	$0.56 \pm 0.19^{+0.03+0.06}_{-0.09-0.09}$
	$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.06}$
CPV	$x(\%)$	$0.56 \pm 0.19^{+0.04+0.06}_{-0.08-0.08}$
	$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.07}$
	$ q/p $	$0.90^{+0.16+0.05+0.06}_{-0.15-0.04-0.05}$
	$\arg(q/p)(^\circ)$	$-6 \pm 11 \pm 3^{+3}_{-4}$

# $D^0 \rightarrow K_S \pi^+ \pi^-$ at LHCb

- $K_S \rightarrow \pi^+ \pi^-$  are difficult to reconstruct in LHCb
  - In the early stages of the trigger only  $K_S$  decaying inside the VELO ( $t < 0.5 \tau_{K_S}$ ) can be reconstructed
  - Trigger relies mostly on the two pions from the  $D^0$  decay  $\Rightarrow$  non-uniform efficiency over the Dalitz plot (which is also correlated with the  $D^0$  decay time)
  - Could be overcome using  $\mu$ -tagged  $D^0$  decays  $\Rightarrow$  reduced efficiency and larger background levels
  - A time-dependent amplitude analysis is very challenging at LHCb



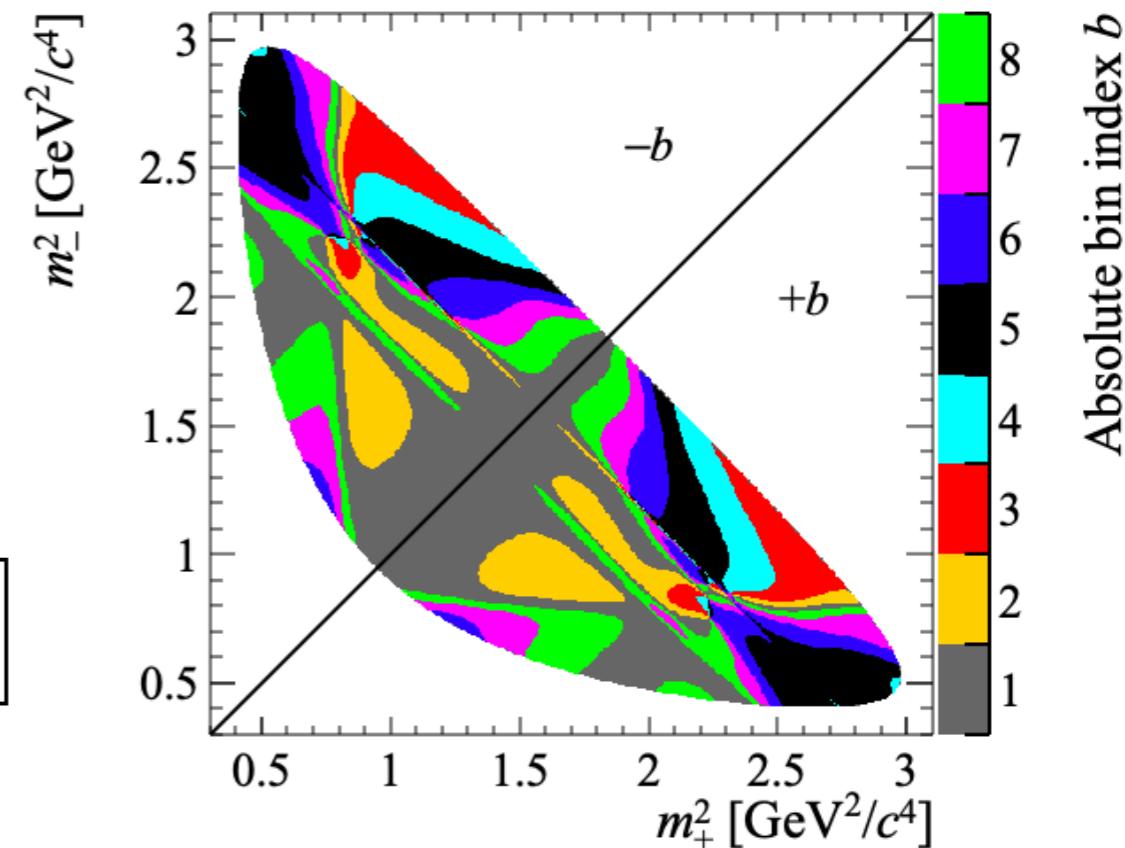
[PRL 122 (2019) 231802]

# $D^0 \rightarrow K_S \pi^+ \pi^-$ with a model-independent approach

- Avoid amplitude analysis by integrating over Dalitz-plot bins with constant strong-phase variation

$$\mathcal{P}_{D^0} \propto e^{-\Gamma t} \left[ F_b - \sqrt{F_b F_{-b}} (c_b y - s_b x) \Gamma t \right]$$

- Constrain hadronic parameters ( $c_b, s_b$ ) using measurements with quantum-correlated  $D^0 \bar{D}^0$  pairs, *i.e.* at CLEO and BESIII



$$F_b = \int_b |\mathcal{A}_{D^0}|^2 dm_+^2 dm_-^2$$

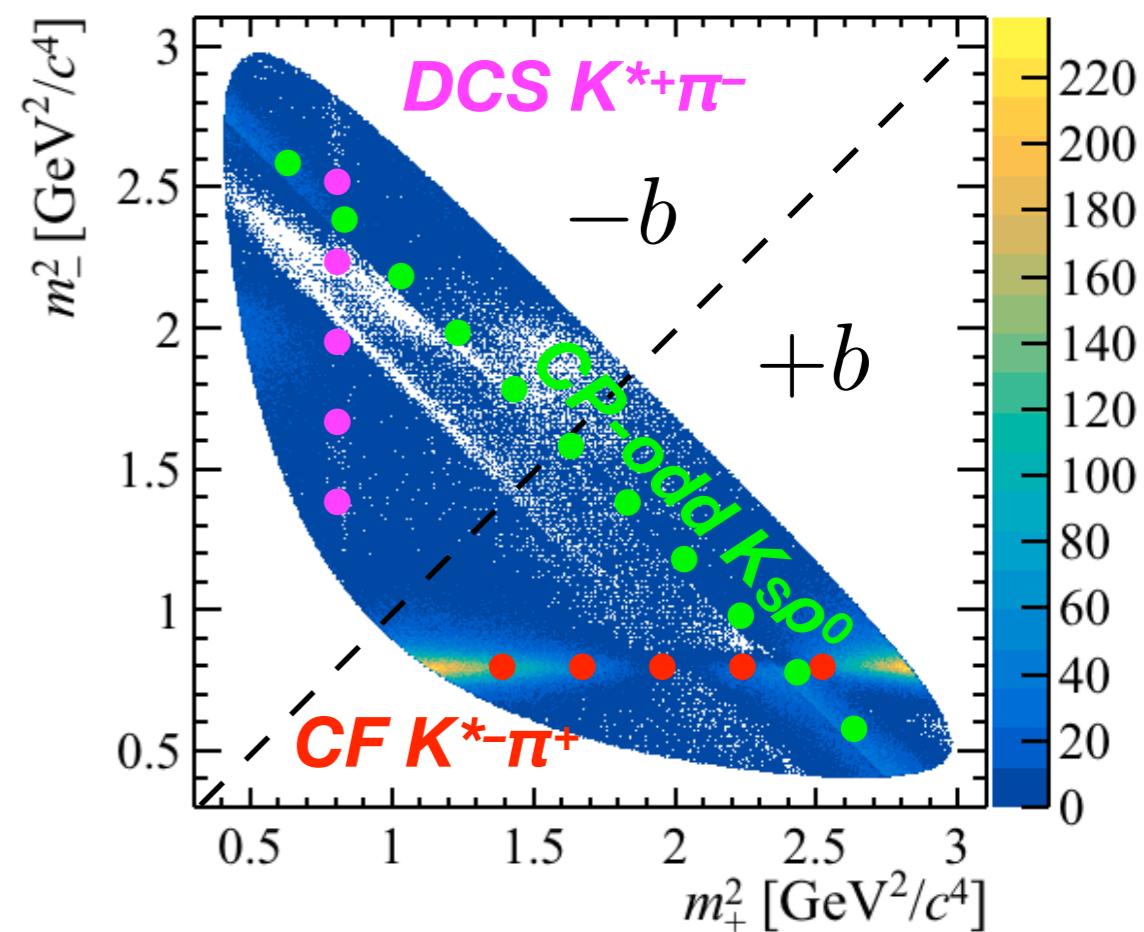
$$c_b - is_b \propto \int_b \mathcal{A}_{D^0}^* \mathcal{A}_{\bar{D}^0} dm_+^2 dm_-^2$$

# Bin-flip method

- Inspired by the WS  $D^0 \rightarrow K\pi$  analysis: ratio of events in bin  $-b$  to events in bin  $b$  to suppress effects due to non-uniform efficiency variations and enhance sensitivity to  $x$

$$R_b \approx r_b - \sqrt{r_b} [(1 - r_b)c_b y - (1 + r_b)s_b x] \Gamma t$$

- Mixing parameters from simultaneous fit to all bins. Split in  $D^0$  and  $\bar{D}^0$  to access also indirect  $CP$  violation
- Model-independent and completely data driven
- Comes with the price of degraded sensitivity to mixing effects from  $CP$ -even/odd amplitudes (*i.e.* to  $y$ )



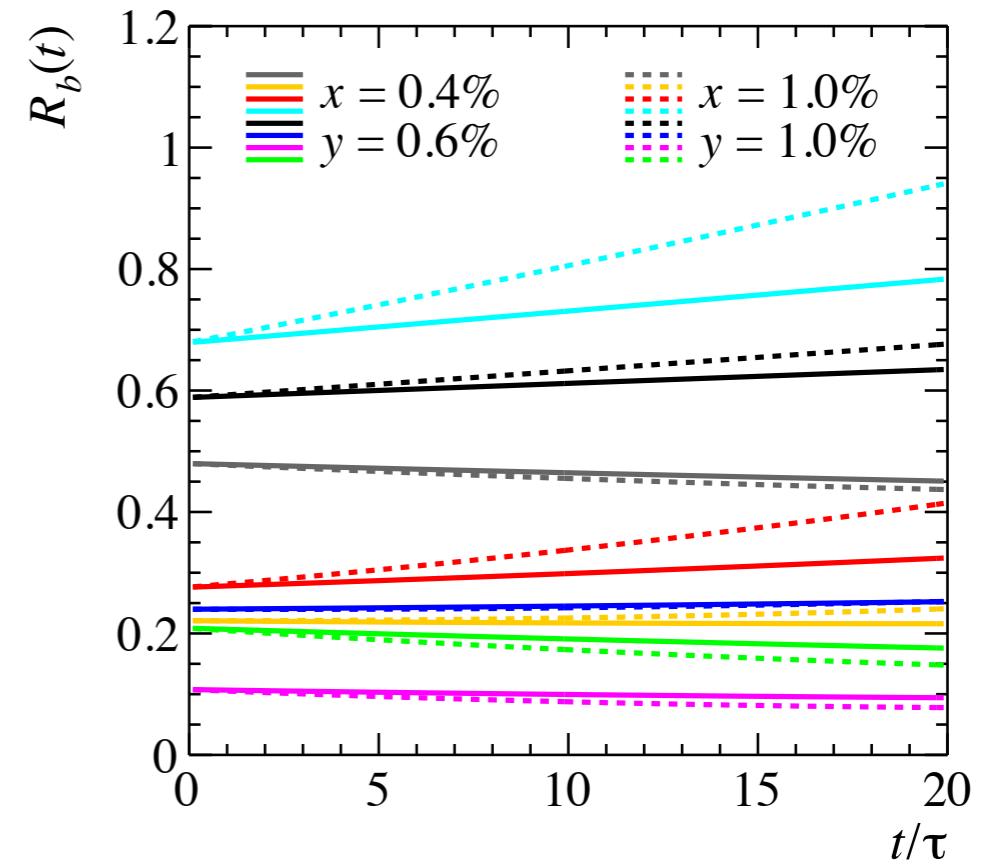
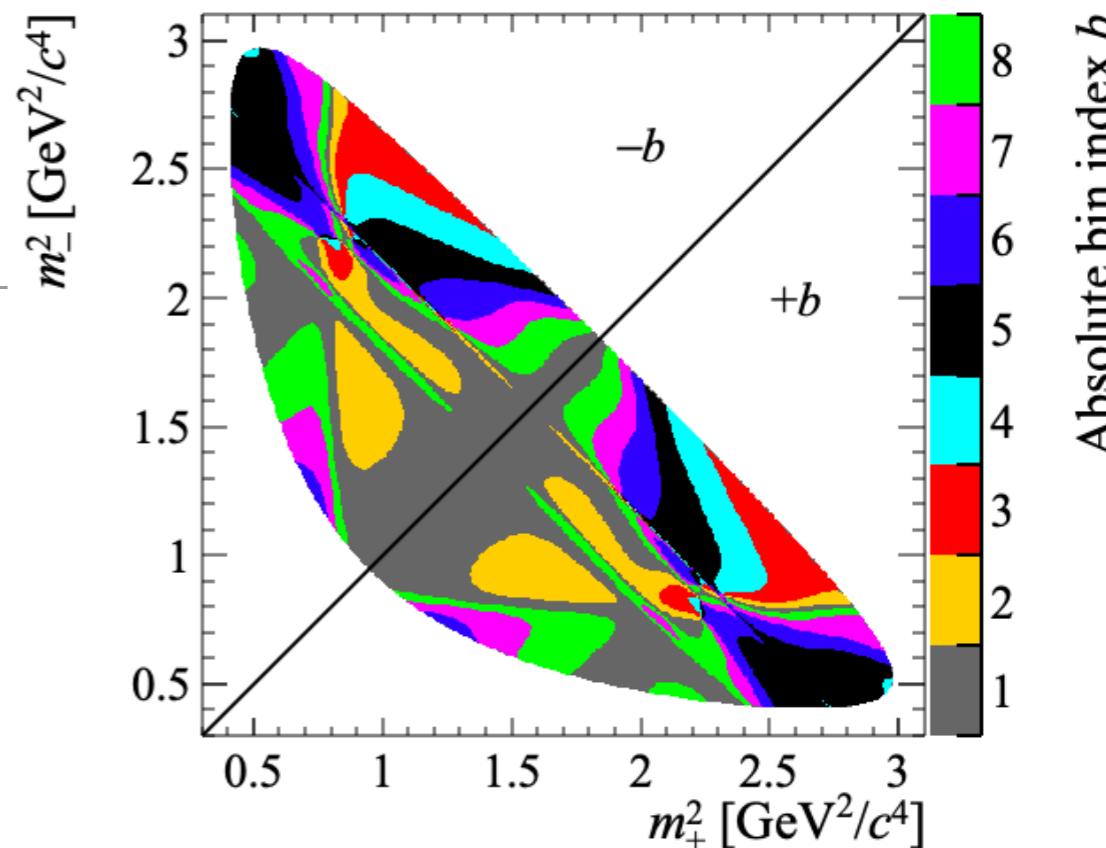
$$r_b = \frac{F_{-b}}{F_b}$$

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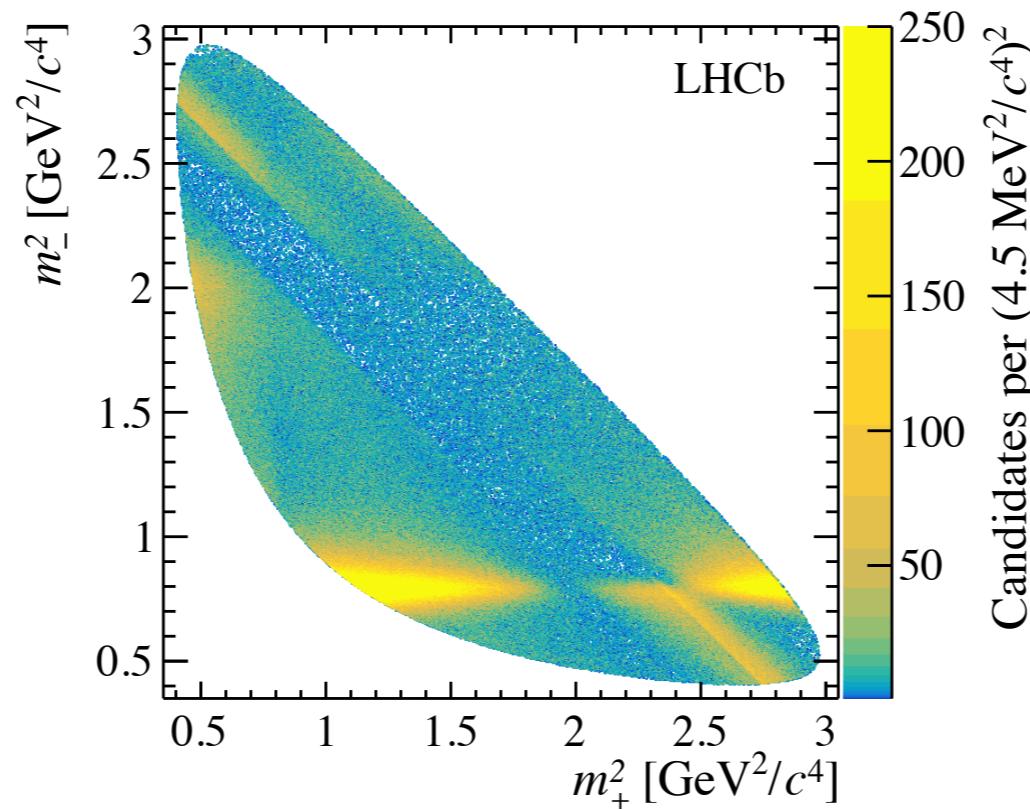
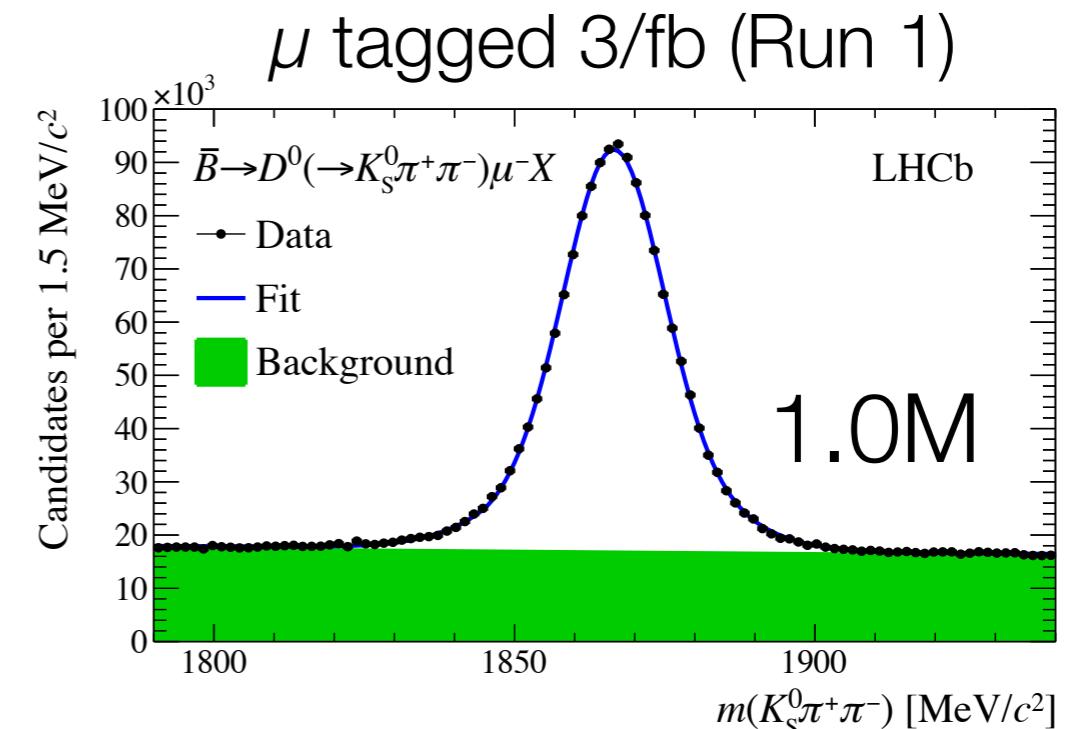
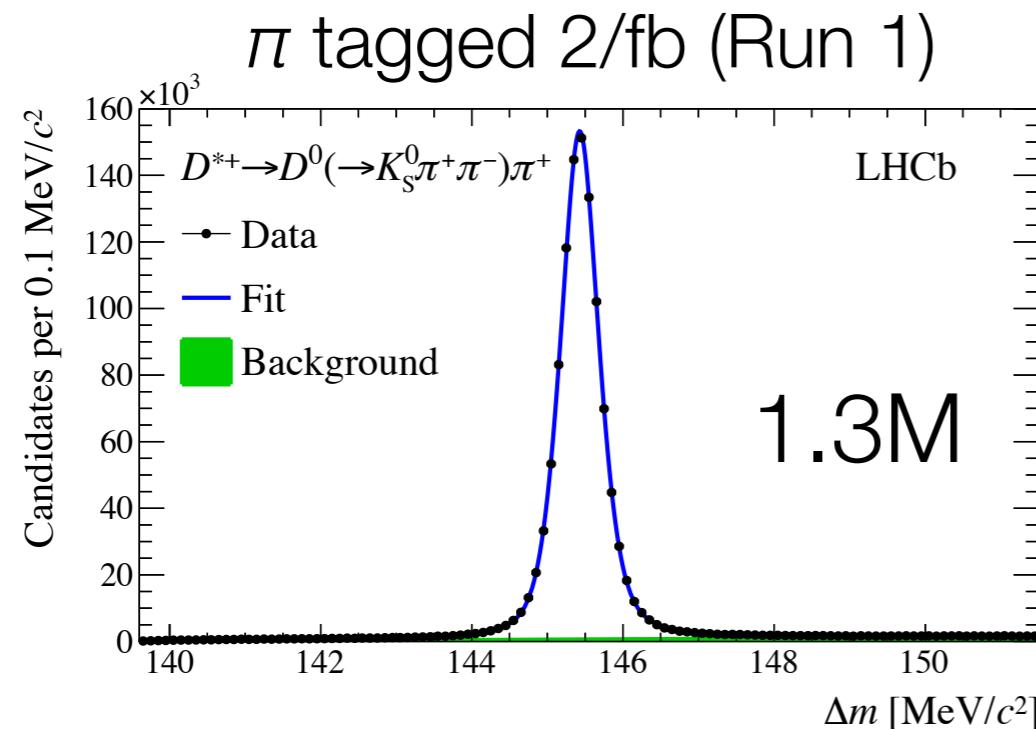
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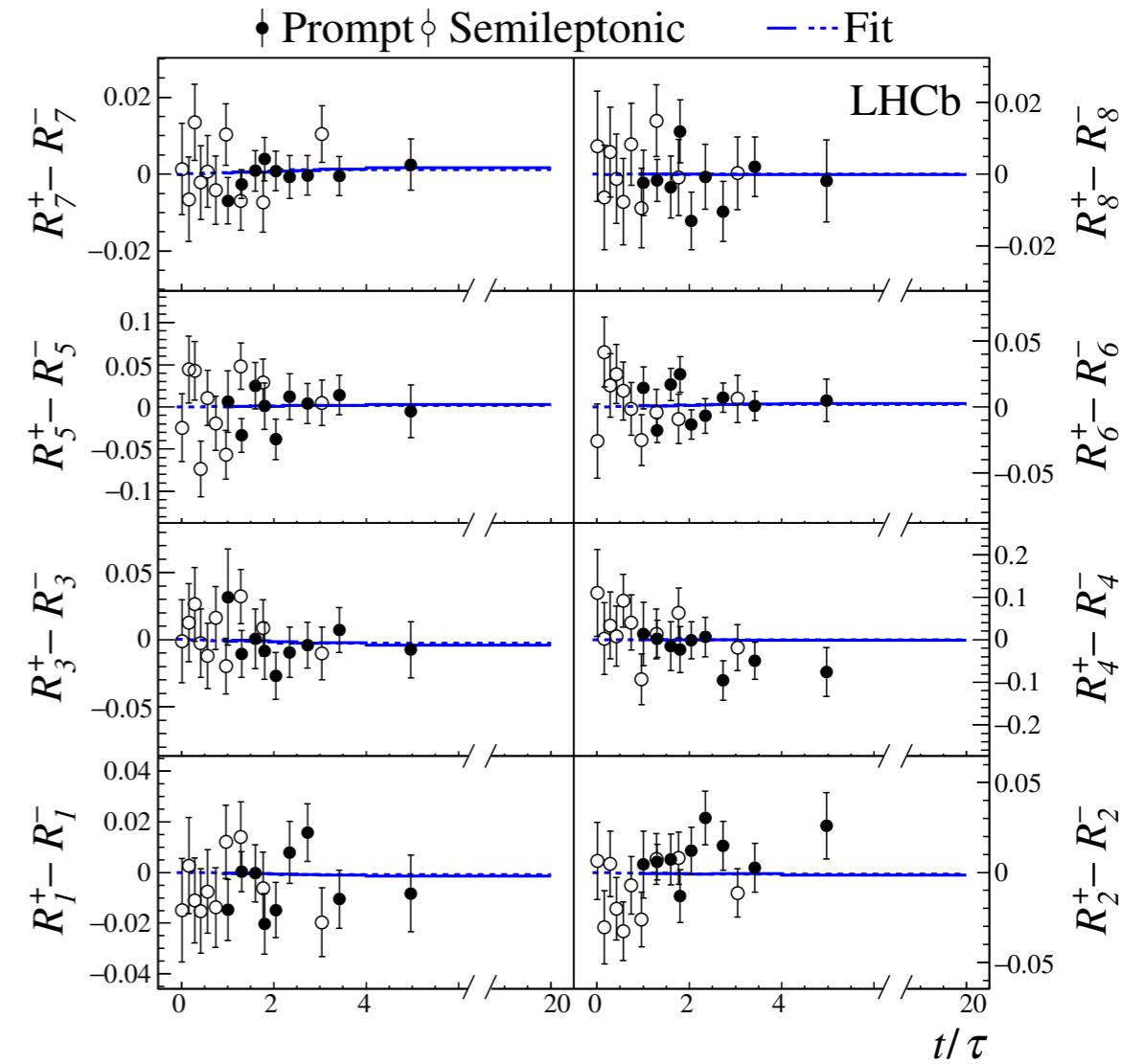
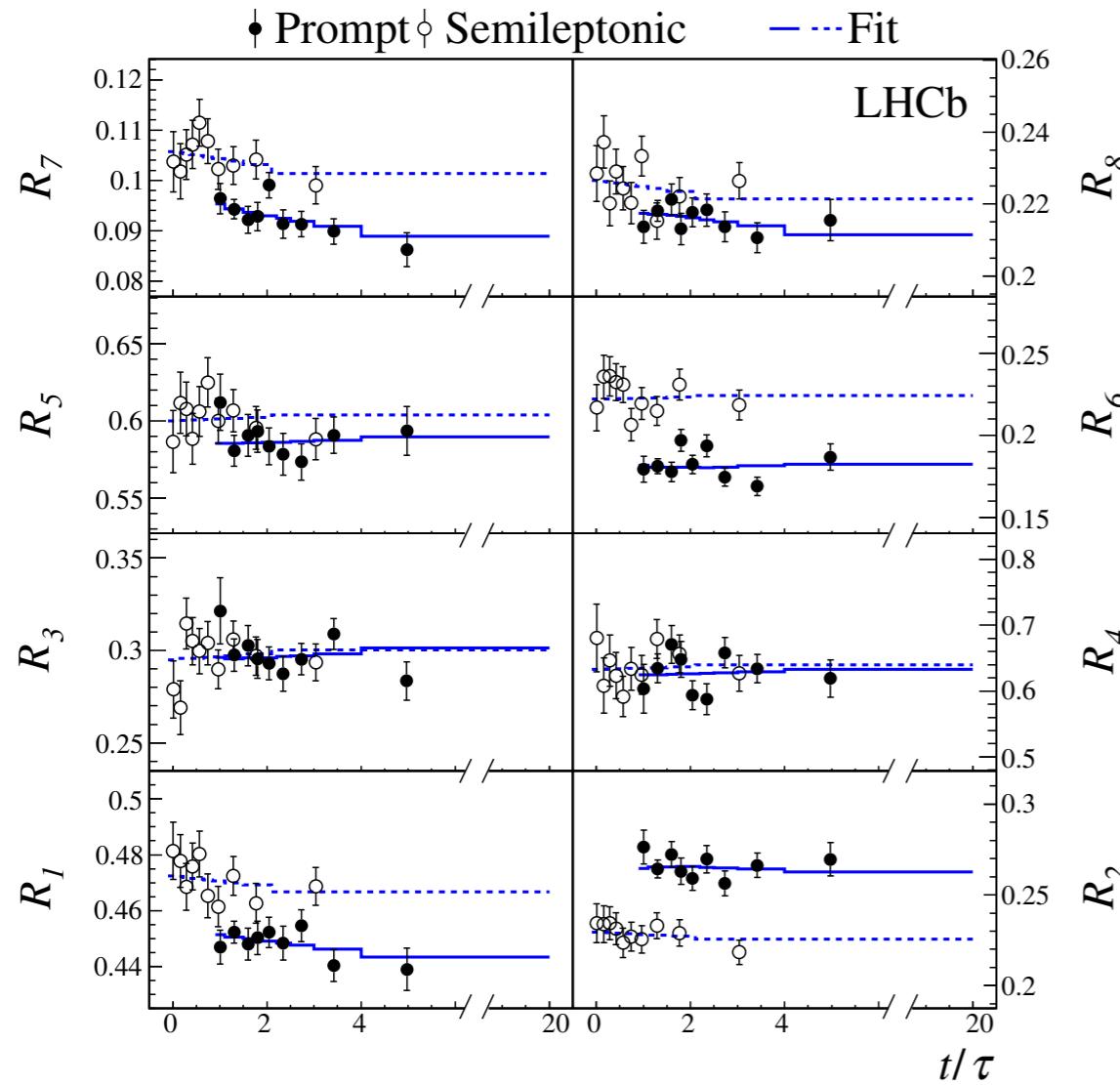
# Bin-flip $D^0 \rightarrow K_S \pi^+ \pi^-$ at LHCb

[PRL 122 (2019) 231802]



# Bin-flip $D^0 \rightarrow K_S \pi^+ \pi^-$ at LHCb

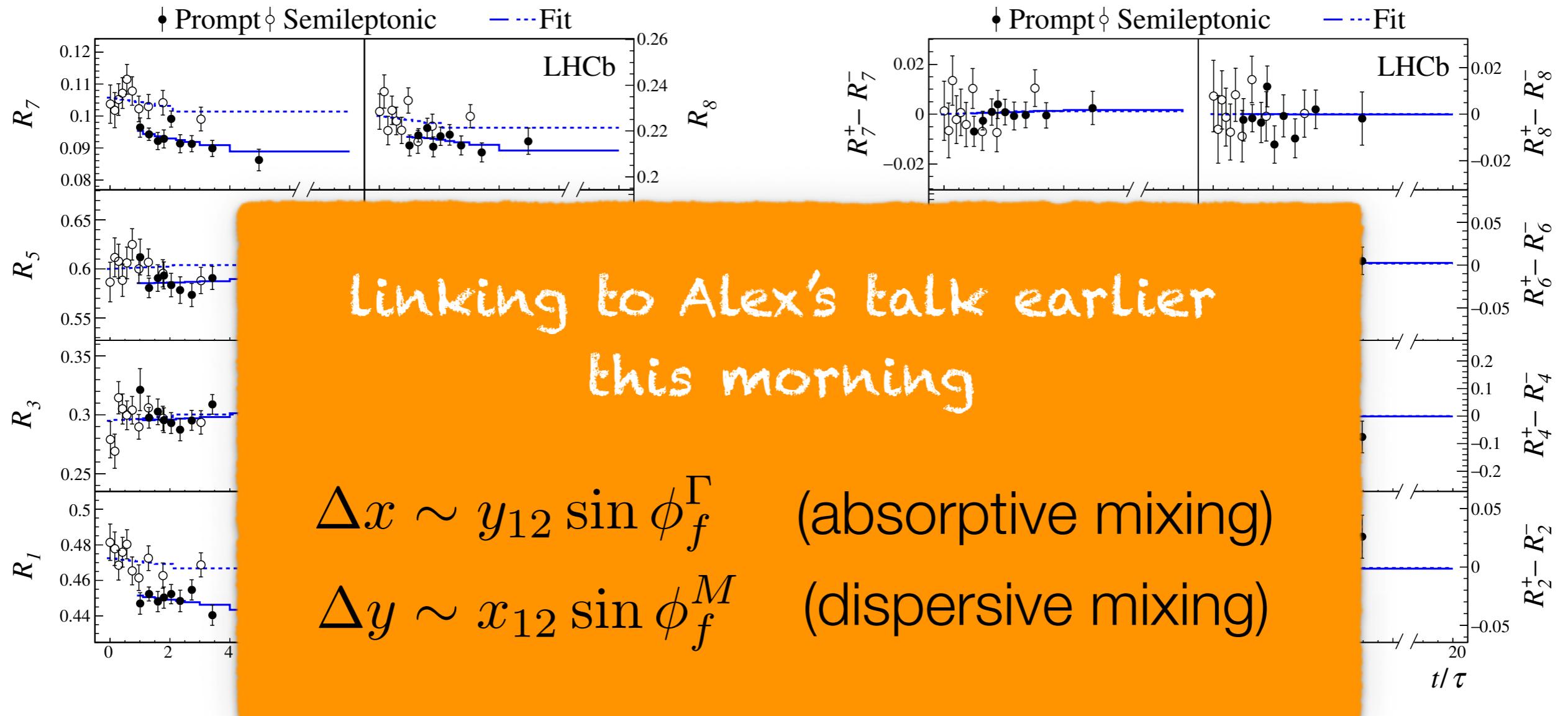
[PRL 122 (2019) 231802]



Parameter	Value [ $10^{-3}$ ]	Stat. correlations		Syst. correlations	
		$y_{CP}$	$\Delta x$	$\Delta y$	$y_{CP}$
$x_{CP}$	$2.7 \pm 1.6 \pm 0.4$	-0.17	0.04	-0.02	0.15
$y_{CP}$	$7.4 \pm 3.6 \pm 1.1$		-0.03	0.01	-0.05
$\Delta x$	$-0.53 \pm 0.70 \pm 0.22$			-0.13	0.14
$\Delta y$	$0.6 \pm 1.6 \pm 0.3$				

# Bin-flip $D^0 \rightarrow K_S \pi^+ \pi^-$ at LHCb

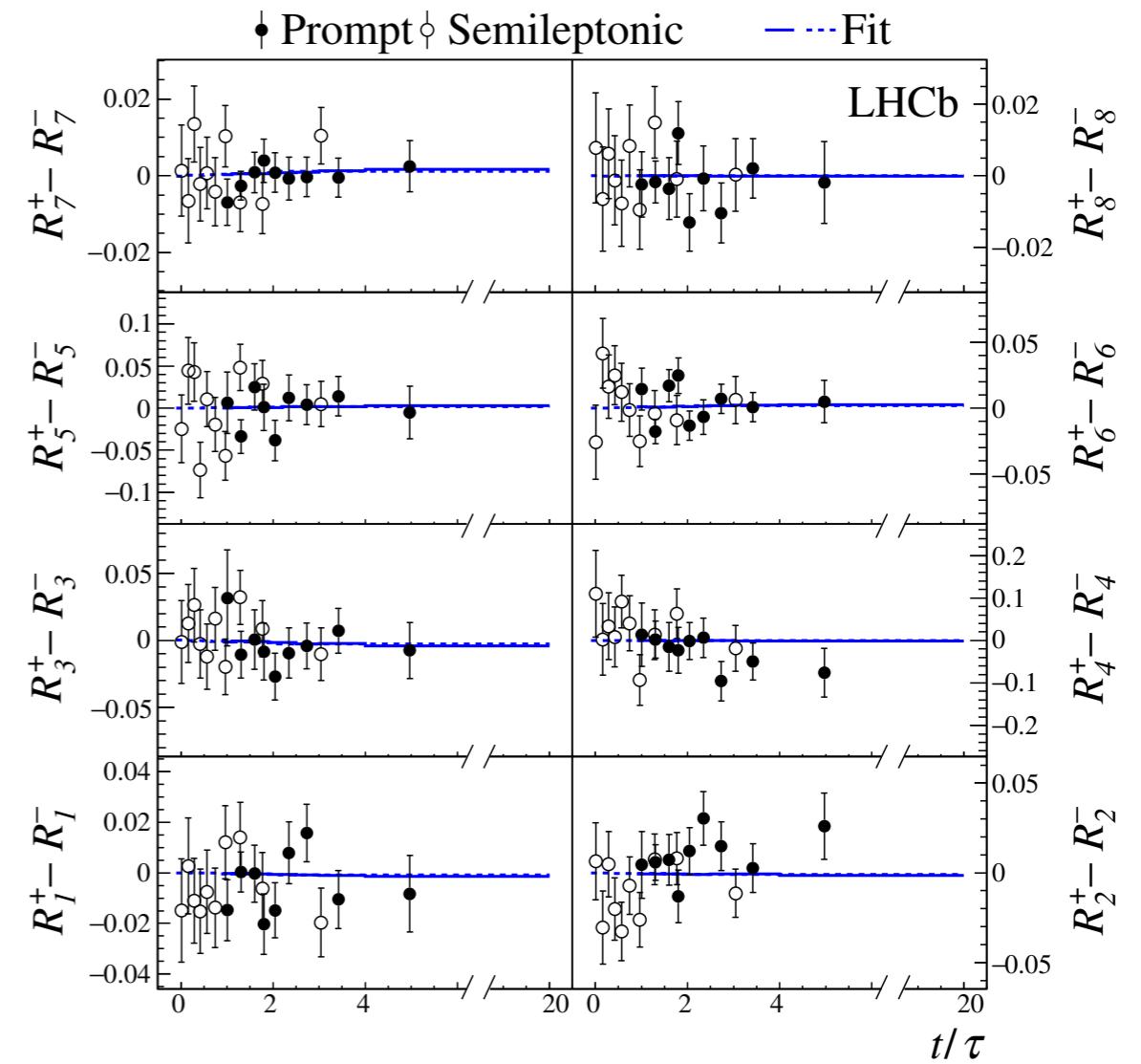
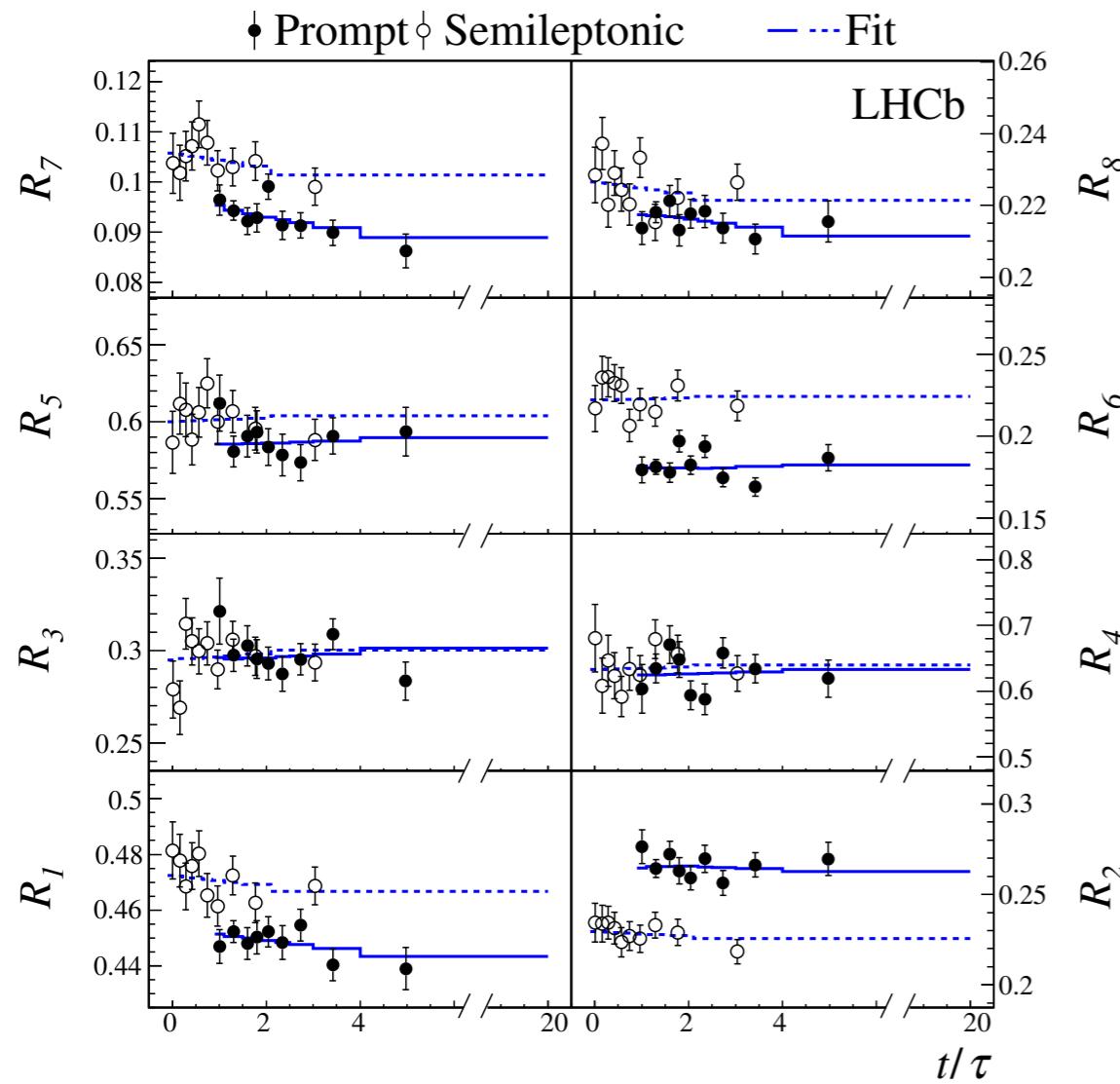
[PRL 122 (2019) 231802]



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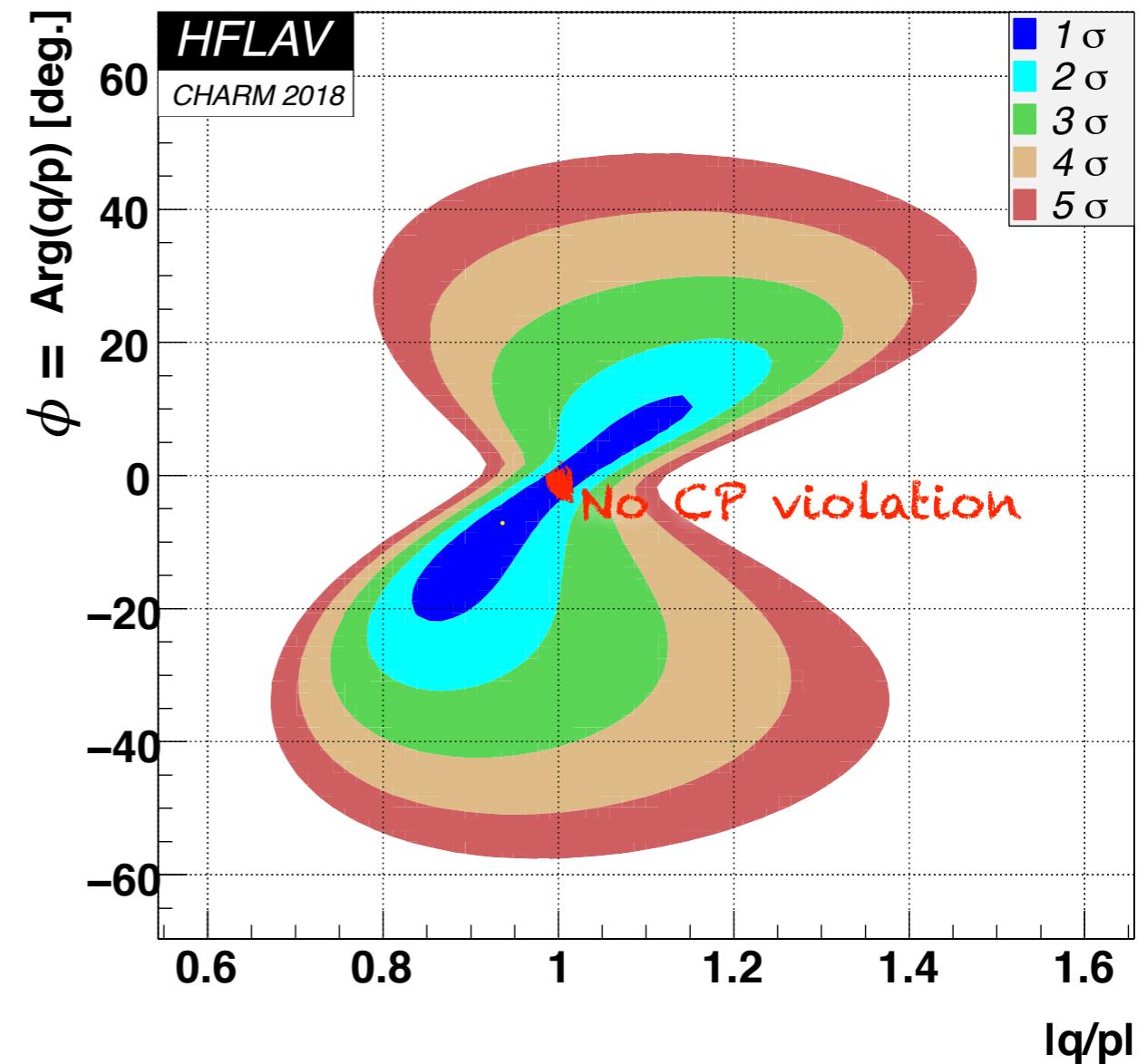
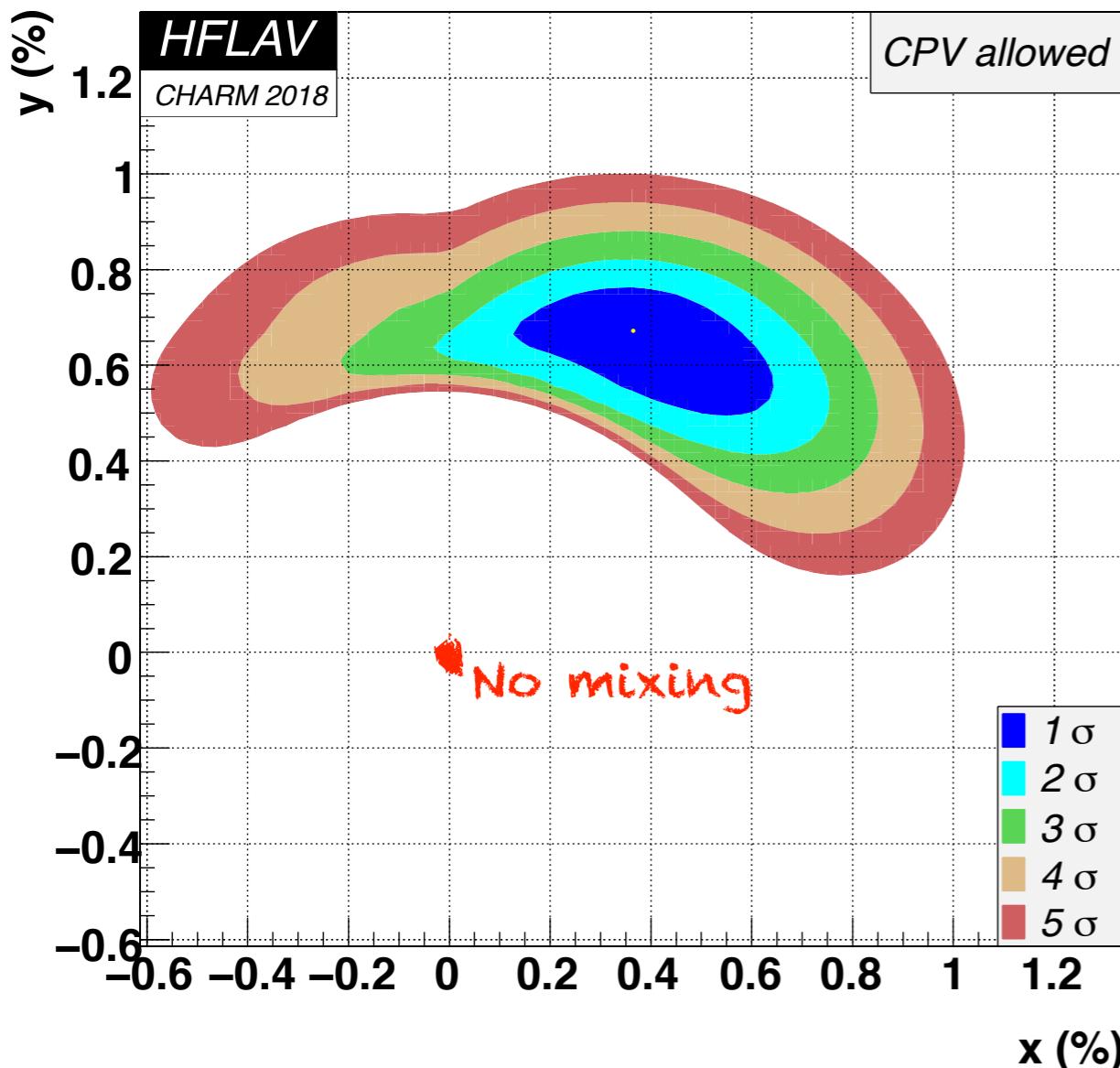
# Bin-flip $D^0 \rightarrow K_S \pi^+ \pi^-$ at LHCb

[PRL 122 (2019) 231802]

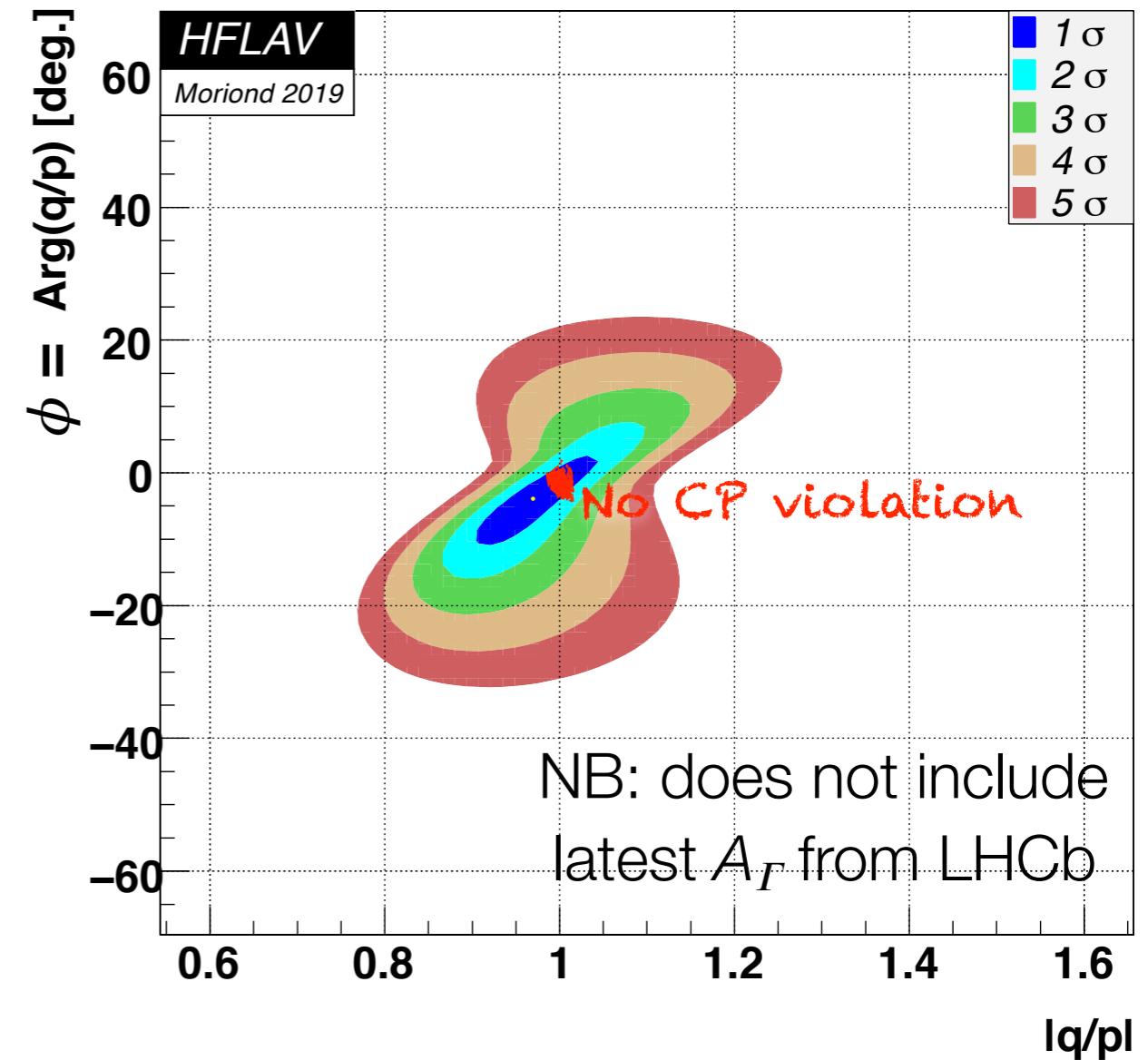
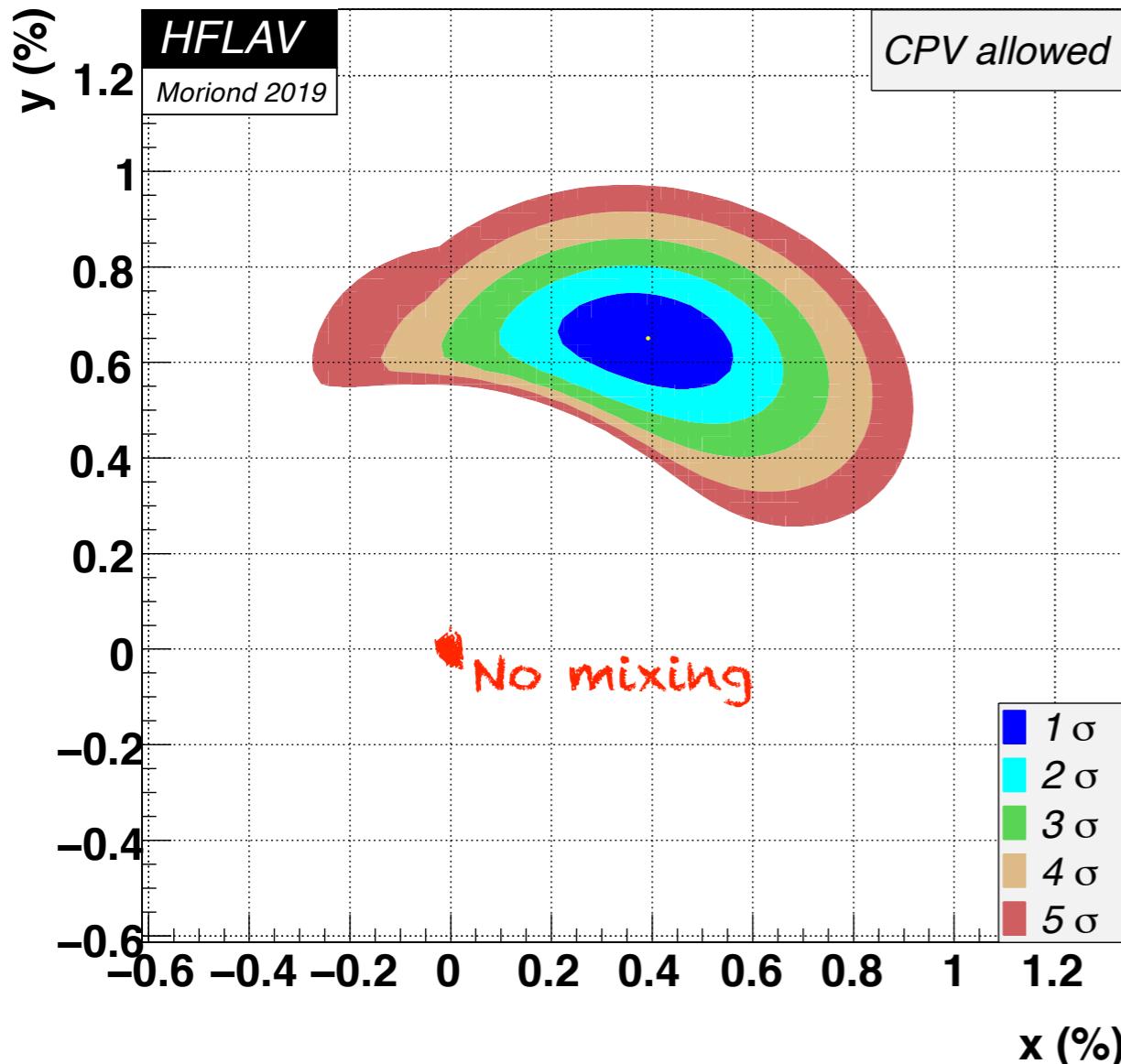


Parameter	Value	95.5% CL interval
$x [10^{-2}]$	$0.27^{+0.17}_{-0.15}$	[-0.05, 0.60]
$y [10^{-2}]$	$0.74 \pm 0.37$	[ 0.00, 1.50]
$ q/p $	$1.05^{+0.22}_{-0.17}$	[ 0.55, 2.15]
$\phi$	$-0.09^{+0.11}_{-0.16}$	[-0.73, 0.29]

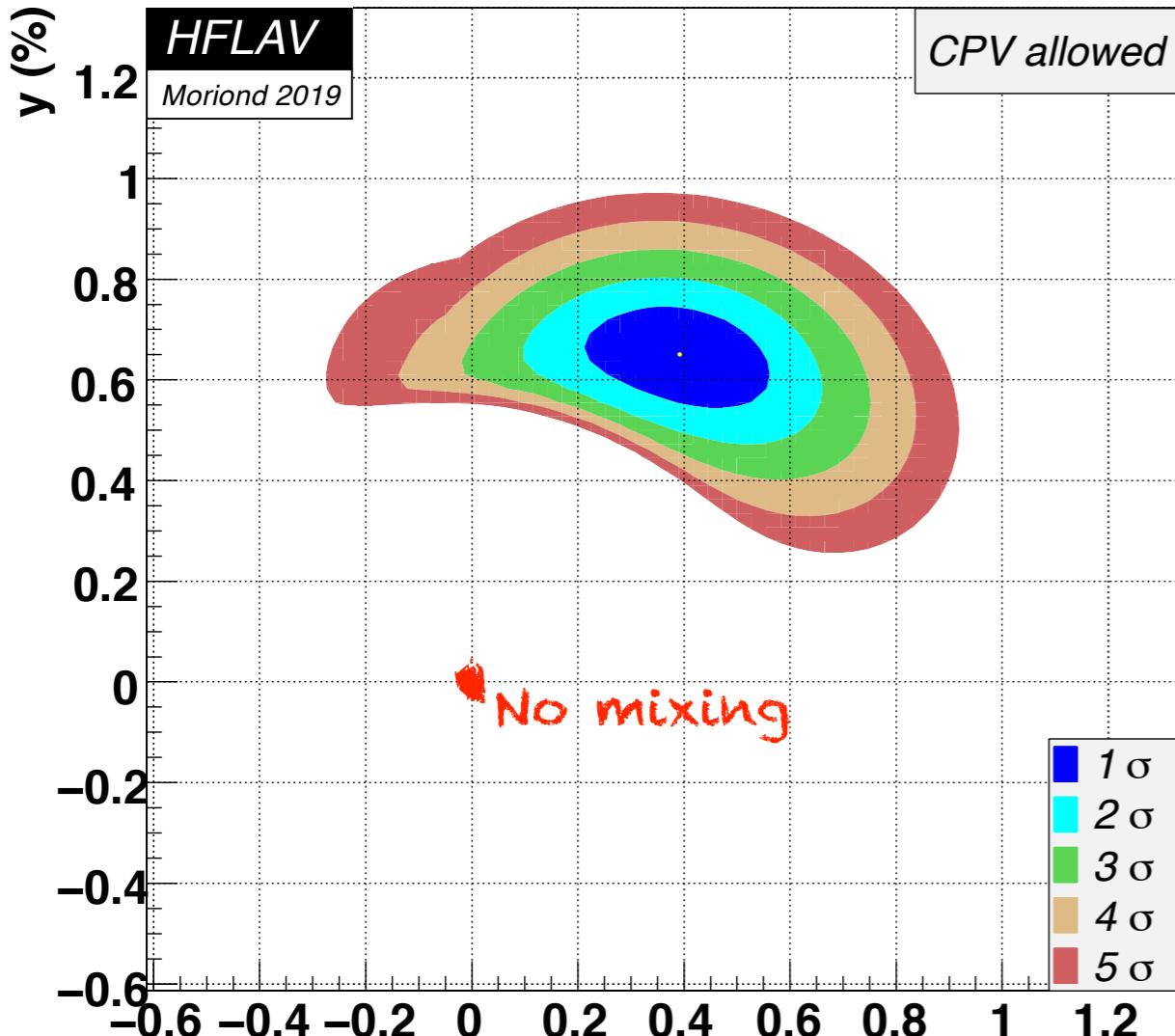
# Impact on world average



# Impact on world average

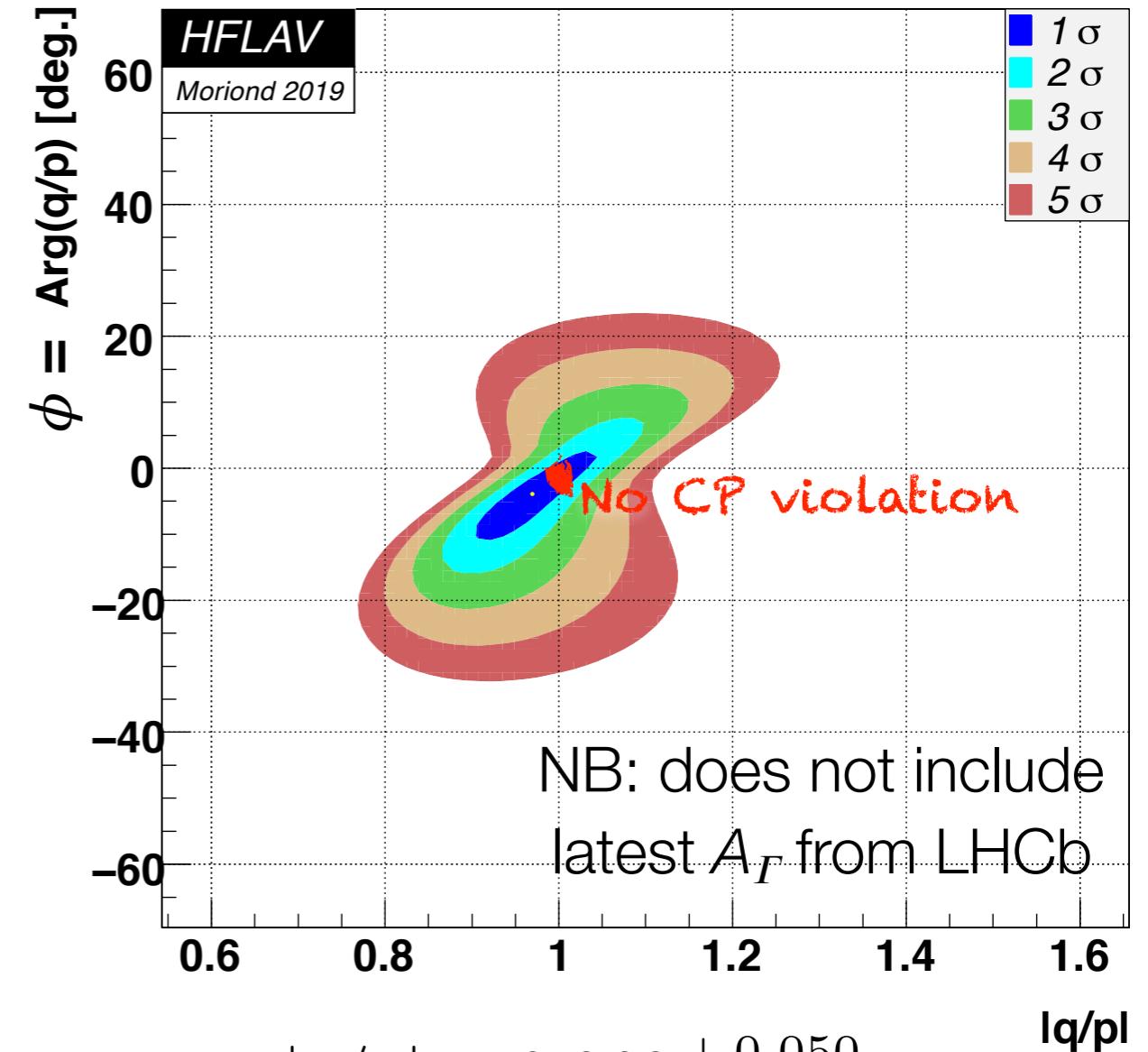


# Impact on world average



$$x = (3.9 \begin{array}{l} +1.1 \\ -1.2 \end{array}) \times 10^{-3}$$

$$y = (6.51 \begin{array}{l} +0.63 \\ -0.69 \end{array}) \times 10^{-3}$$



$$|q/p| = 0.969 \begin{array}{l} +0.050 \\ -0.045 \end{array}$$

$$\phi = (-3.9 \begin{array}{l} +4.5 \\ -4.6 \end{array})^\circ$$

first evidence for nonzero (positive) value of  $x$

# Prospects for $D^0 \rightarrow K_S \pi^+ \pi^-$

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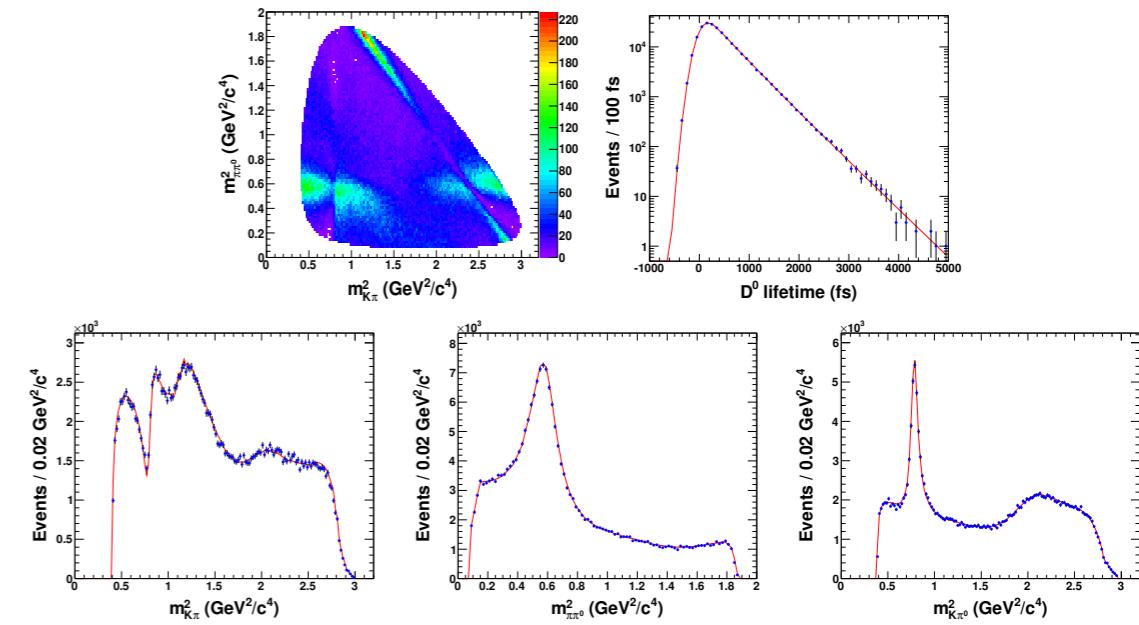
- In Run 1+2 LHCb has collected  $\sim 36M$   $\pi$ -tagged  $D^0 \rightarrow K_S \pi^+ \pi^-$  decays and  $\sim 10M$   $\mu$ -tagged decays
  - Expected sensitivity (my own extrapolation, not official)

Uncertainty ( $\times 10^{-3}$ )	$x_{CP}$	$y_{CP}$	$\Delta x$	$\Delta y$
CLEO inputs	0.3	1.0	0.07	0.13
Data statistics	0.4	0.8	0.16	0.34
Total	0.5	1.3	0.18	0.39

- Belle II will collect  $\sim 50M$  ( $\pi$ -tagged) decays with 50/ab. Difficult to compete if LHCb keeps same efficiency in the Upgrade
- Can Belle II do  $D^0 \rightarrow K_L \pi^+ \pi^-$ ? (it is being considered for  $\gamma/\phi 3$ )

# More multibodies

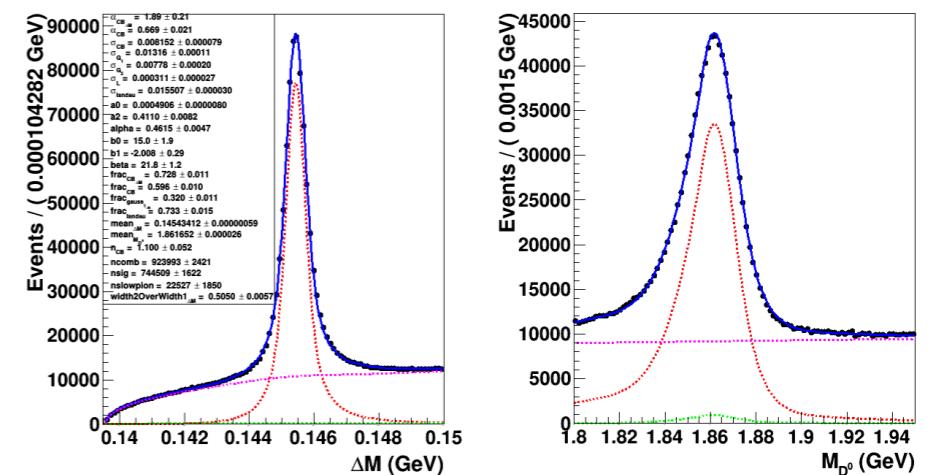
- Lots of other promising final states not yet explored/fully exploited experimentally: e.g.  
 $D^0 \rightarrow K^+ \pi^- \pi^0$ ,  $D^0 \rightarrow K_S \pi^+ \pi^- \pi^0$ ,  
 $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$ , ...



$\sim 225k D^0 \rightarrow K^+ \pi^- \pi^0$   
expected at Belle II (50/ab)  
 $\sigma(x' \approx x) \sim 0.5 \times 10^{-3}$

- Model-independent analyses would have to rely on BESIII measurements of the strong-phase parameters

[PRD 95 (2017) 091101]



$\sim 750M D^0 \rightarrow K_S \pi^+ \pi^- \pi^0$   
at Belle (1/ab)

# Summary

---

- Observed (direct)  $CP$  violation in charm decays
  - Measured asymmetry seems consistent with standard model, although predictions suffer from large uncertainties due to strong-interaction effects
  - Additional searches for  $CP$  violation in different decay modes can help to clarify the picture, together with improved theory calculations
- Yet no signs for mixing-induced  $CP$  violation. Precision still  $\sim 10\times$  larger than naive standard model expectation, so plenty of room for new physics
- Huge experimental progress expected in the next decade(s) at LHCb and Belle II (with valuable inputs from BESIII) if we fully exploit the excellent complementarity between the two experiments

“Charm is the new beauty!”

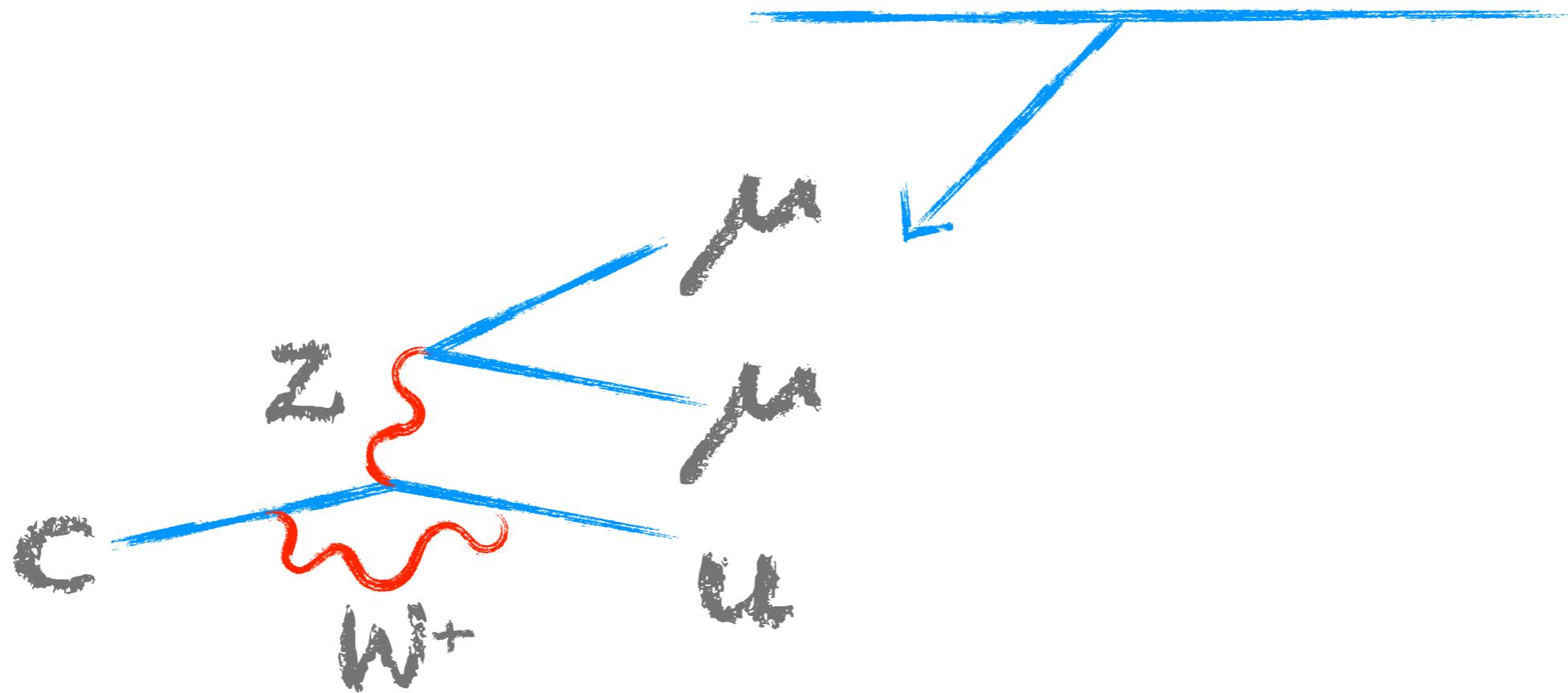




Charm is more valuable than beauty.  
You can resist beauty, but you can't  
resist charm.

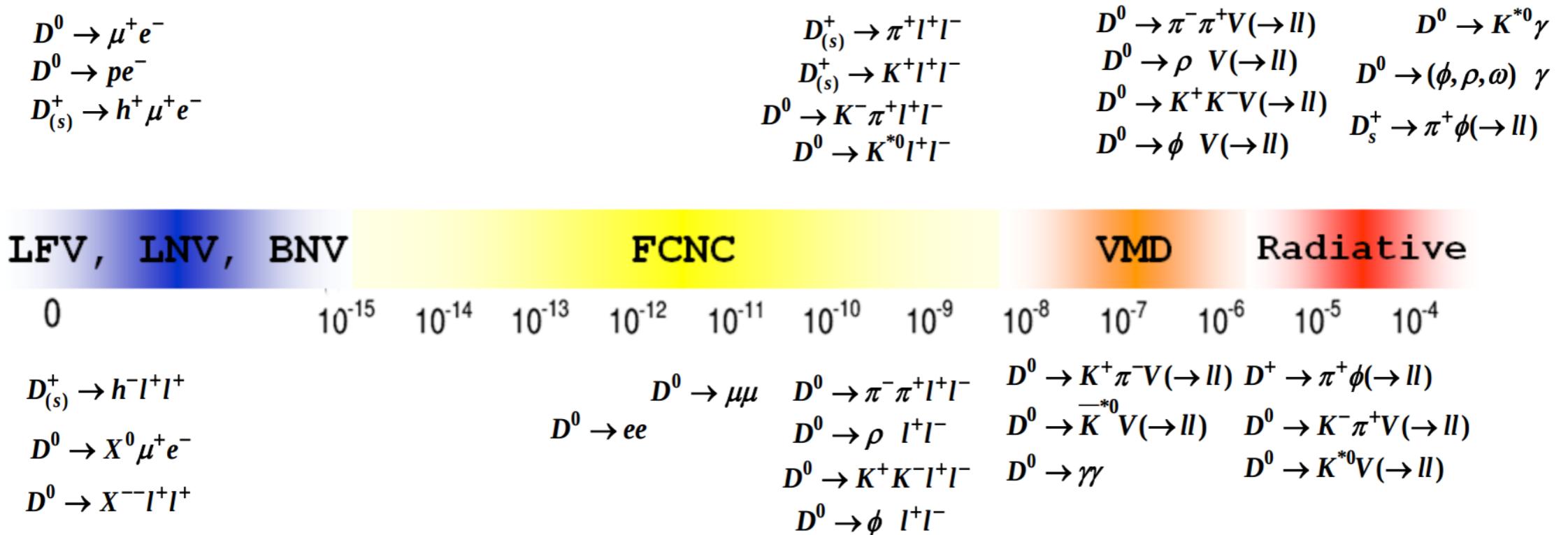
— *Audrey Tautou* —

## Supplementary slides on rare charm decays



# Rare charm decays at LHCb

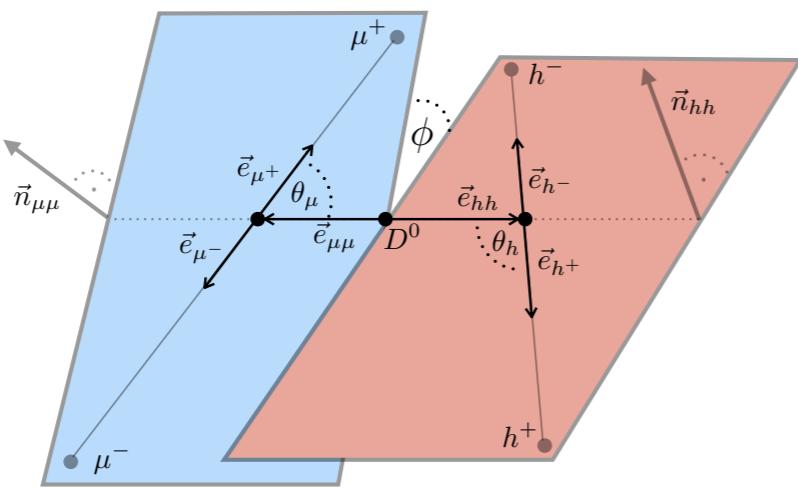
- A rainbow of different physics, ranging from forbidden to (not-so-rare) radiative decays



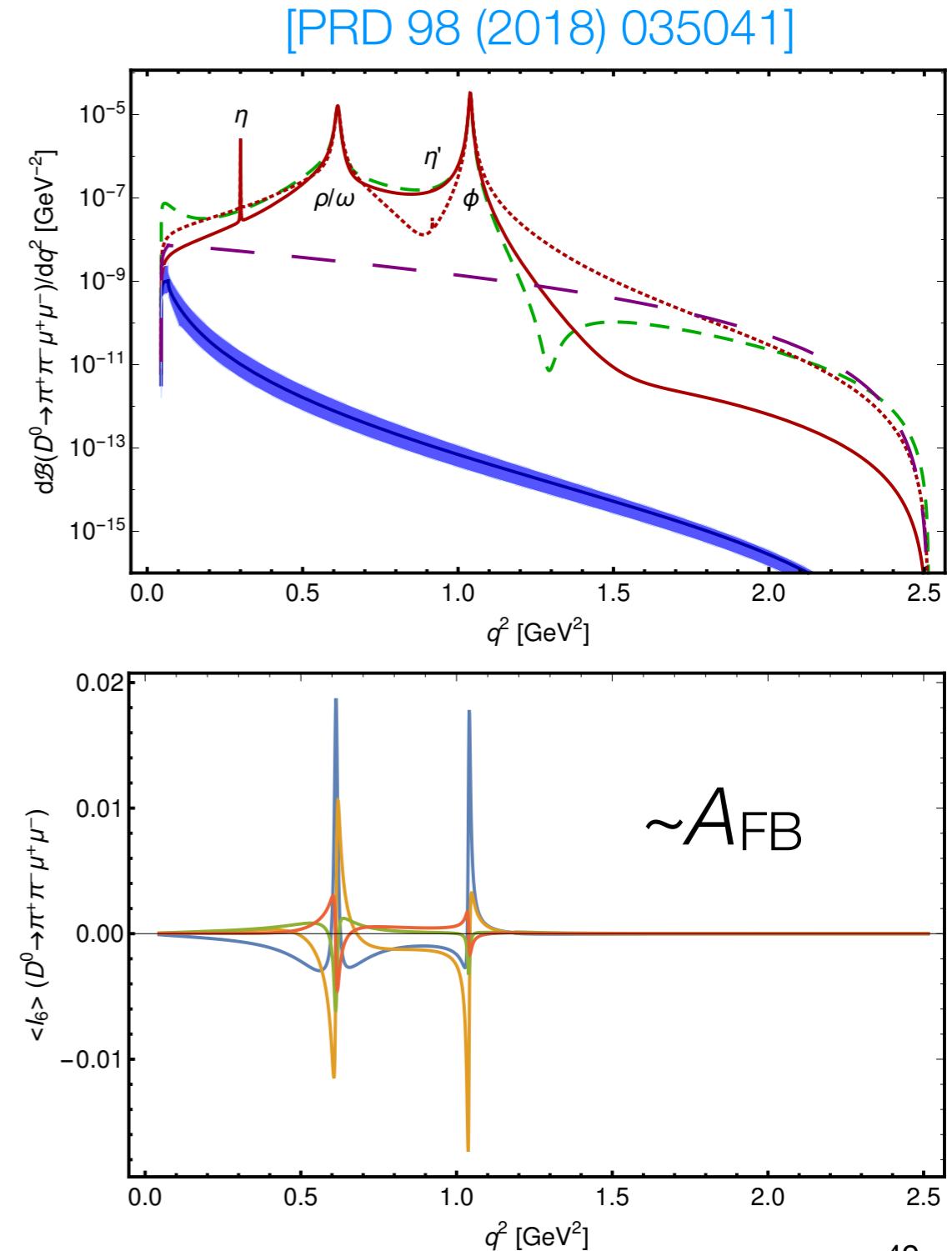
- So far LHCb focused mostly on final states with 2 muons:
  - Best limit on  $D^0 \rightarrow \mu^+ \mu^-$  [PLB 725 (2013) 15],  $D_{(s)} \rightarrow \pi^+ \mu^+ \mu^-$ ,  $\pi^- \mu^+ \mu^+$  [PLB 724 (2013) 203],  $D^0 \rightarrow h^+ h^- \mu^+ \mu^-$  [PLB 728 (2014) 234],  $D^0 \rightarrow e^+ \mu^-$  [PLB 754 (2016) 167],  $\Lambda_c \rightarrow p \mu^+ \mu^-$  [PRD 97 (2018) 091101]
  - First observation of  $D^0 \rightarrow K^-\pi^+ V(\rightarrow \mu^+ \mu^-)$  [PLB 757 (2016) 558],  $K^+ K^- V(\rightarrow \mu^+ \mu^-)$ ,  $\pi^+ \pi^- V(\rightarrow \mu^+ \mu^-)$  [PRL 119 (2017) 181805, PRL 121 (2018) 091801],  $\Lambda_c \rightarrow p V(\rightarrow \mu^+ \mu^-)$  [PRD 97 (2018) 091101]

# The richness of $D^0 \rightarrow h^+h^-\mu^+\mu^-$ decays

- Overwhelming contribution from long-distance amplitudes proceeding through intermediate vector resonances in the dimuon spectrum
- Such penalty is overly compensated by the rich and diverse dynamics of multibody decays

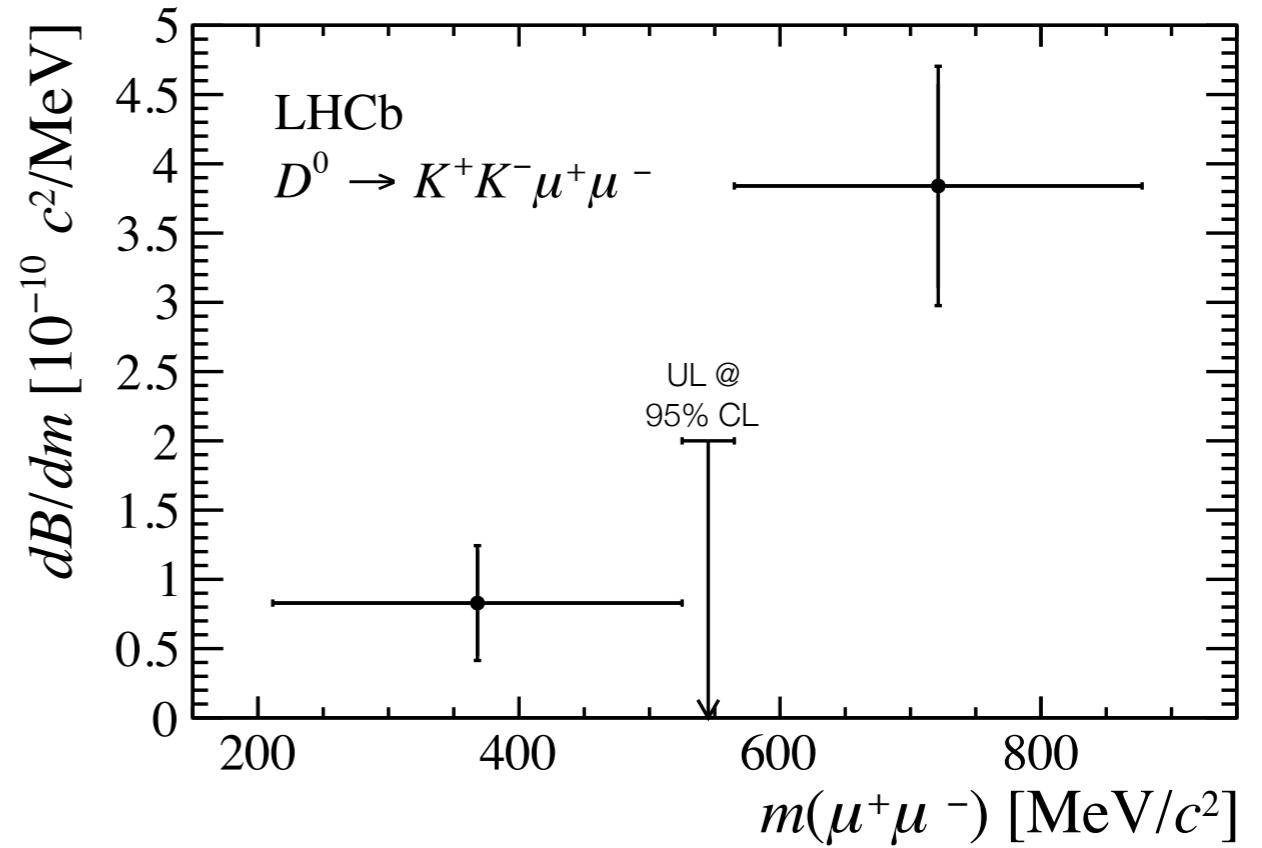
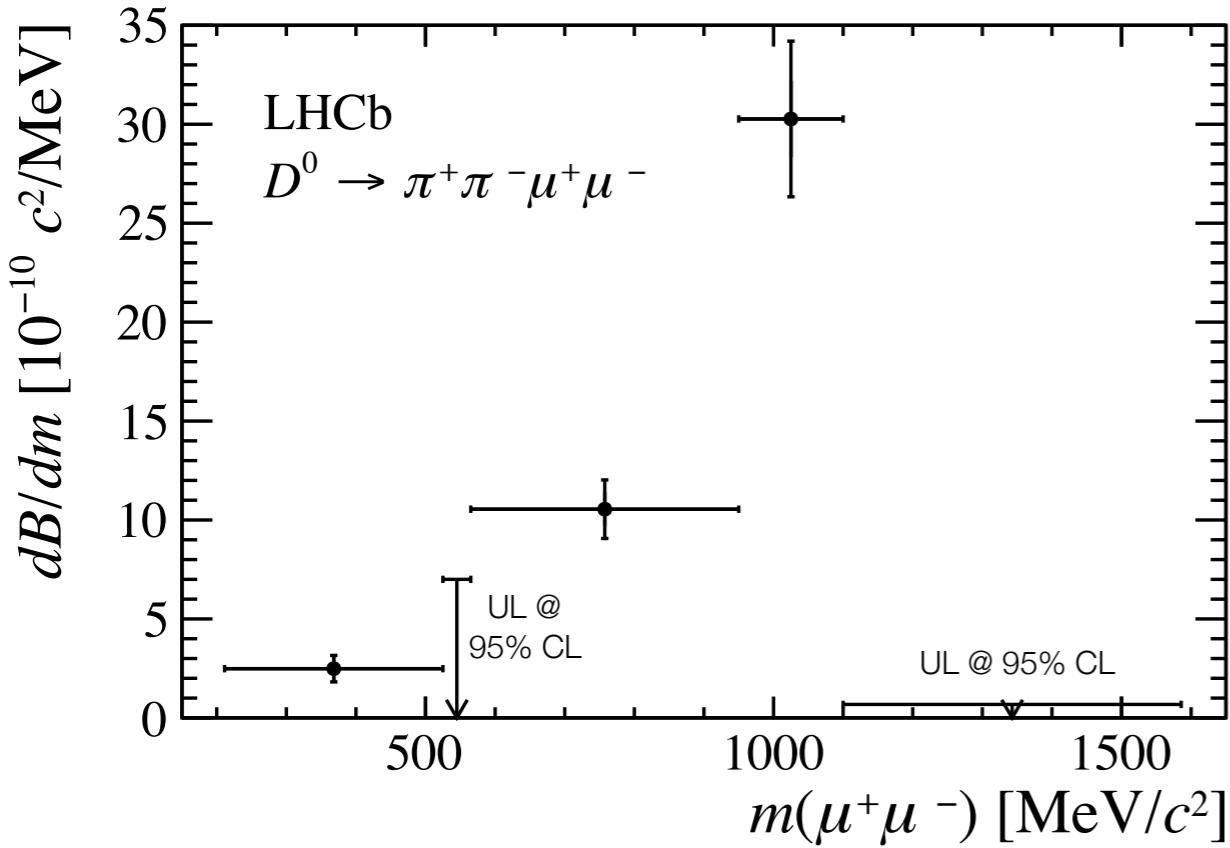


- Access to angular and  $CP$  asymmetries can greatly increase sensitivity to short-distance physics
- $O(1\%)$  asymmetries may be generated by NP [JHEP 04 (2013) 135, PRD 87 (2013) 054026, PRD 98 (2018) 035041]



# $D^0 \rightarrow h^+h^- \mu^+\mu^-$ : branching fraction

Run 1 (2/fb)  
 [PRL 119 (2017) 181805]



- Rarest charm-hadron decays ever observed:

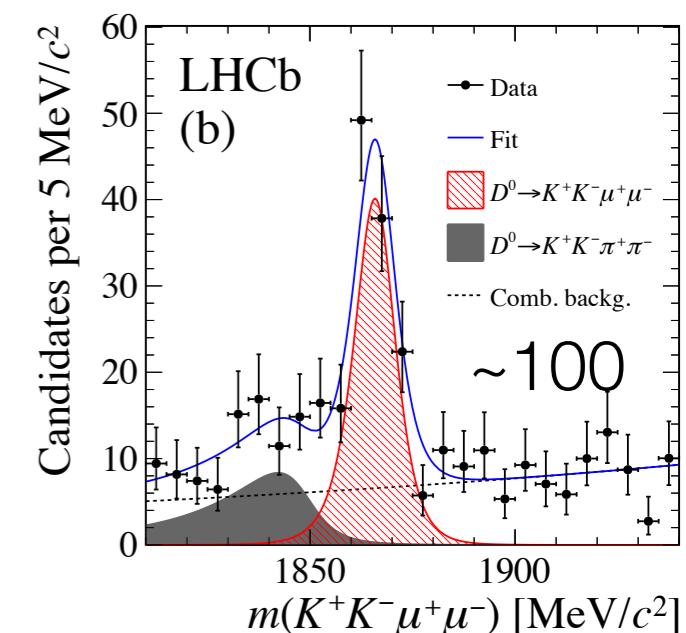
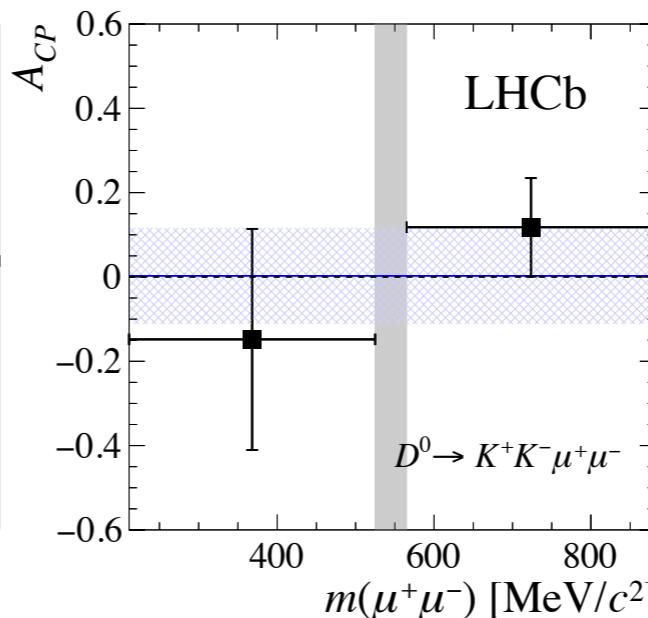
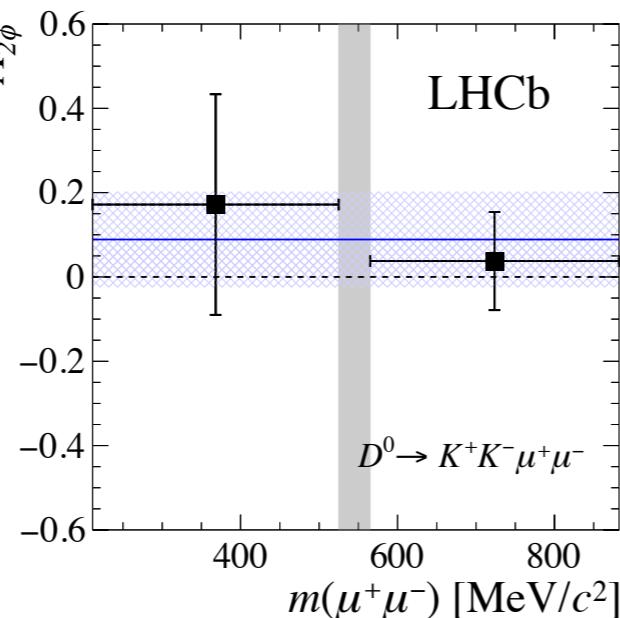
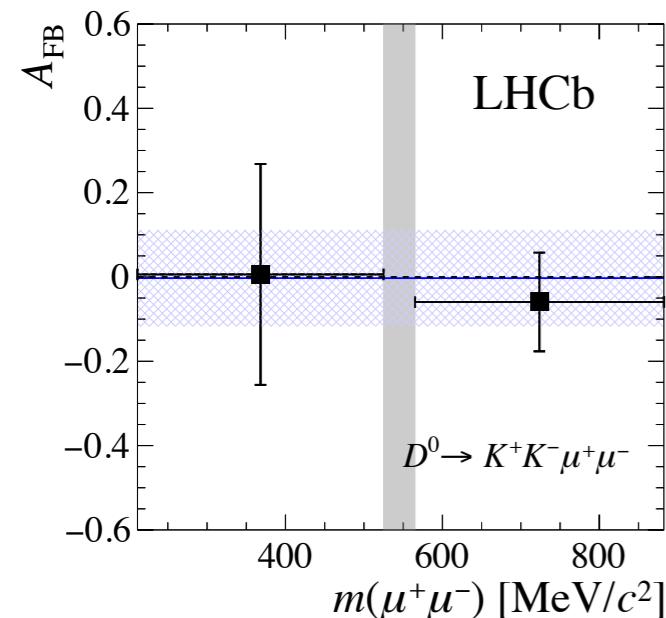
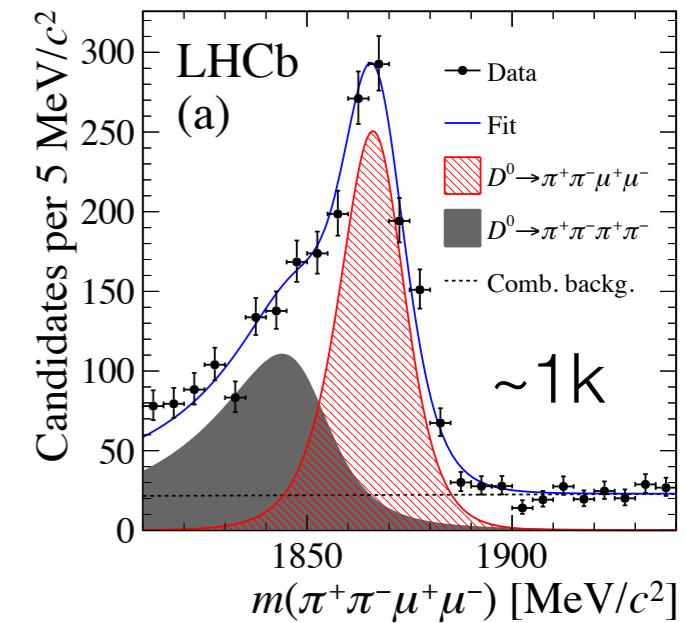
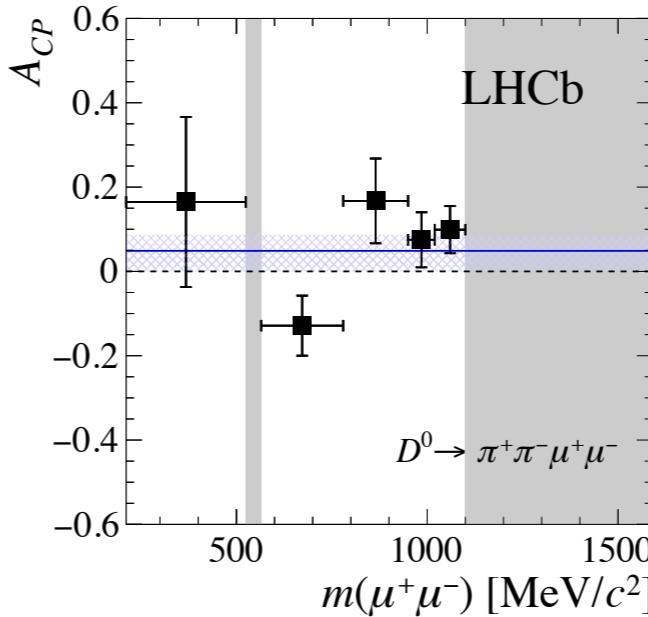
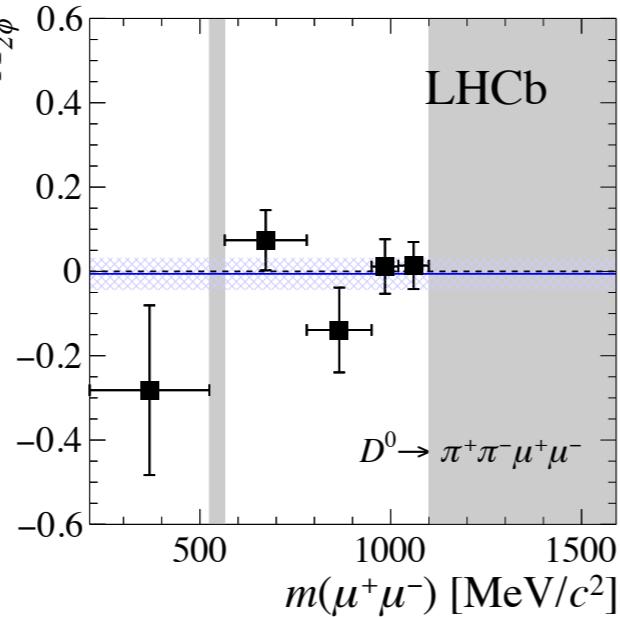
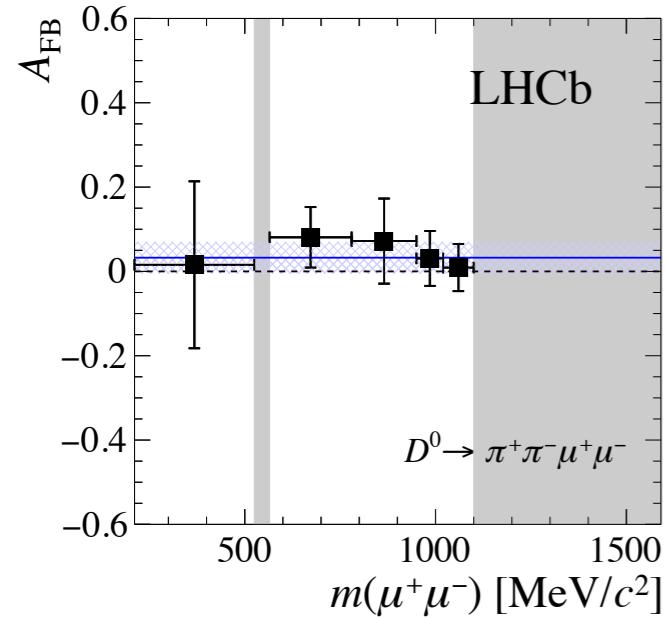
$$\mathcal{B}(D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-) = (9.64 \pm 0.48 \pm 0.51 \pm 0.97) \times 10^{-7}$$

$$\mathcal{B}(D^0 \rightarrow K^+ K^- \mu^+ \mu^-) = (1.54 \pm 0.27 \pm 0.09 \pm 0.16) \times 10^{-7}$$

where the uncertainties are statistical, systematic and due to the BF of the normalization decay

# $D^0 \rightarrow h^+h^- \mu^+\mu^-$ : angular and $CP$ asymmetries

Run 1+2 (5/fb)



# Which final states for Belle II?

- Electron modes to test LFU: e.g.

$$D_{(S)} \rightarrow h^+ e^+ e^-, D^0 \rightarrow h^- h^+ e^+ e^-$$

$$D^0 \rightarrow \pi^0 e^+ e^-, \dots$$

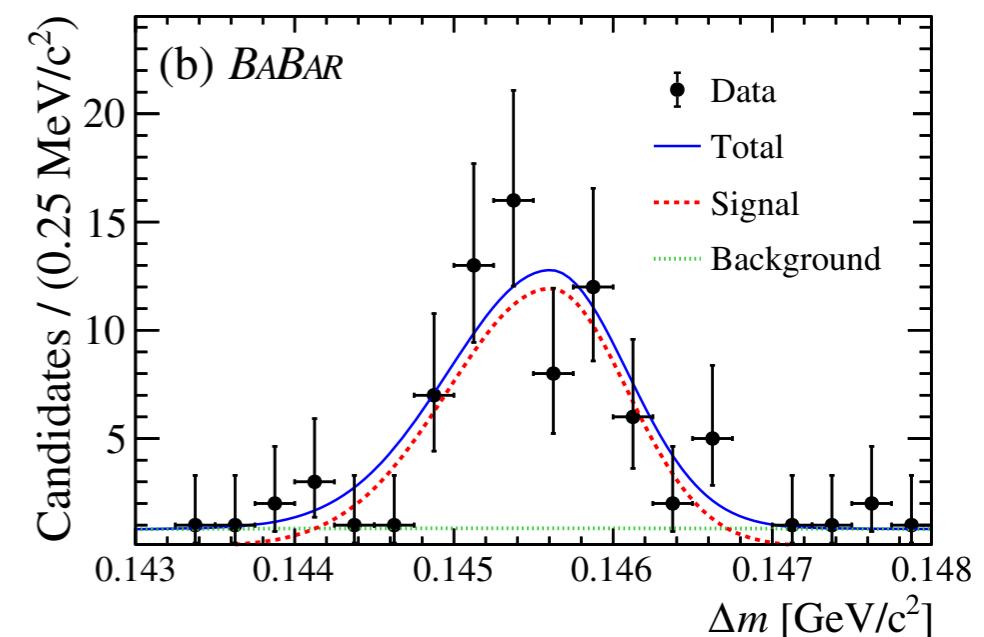
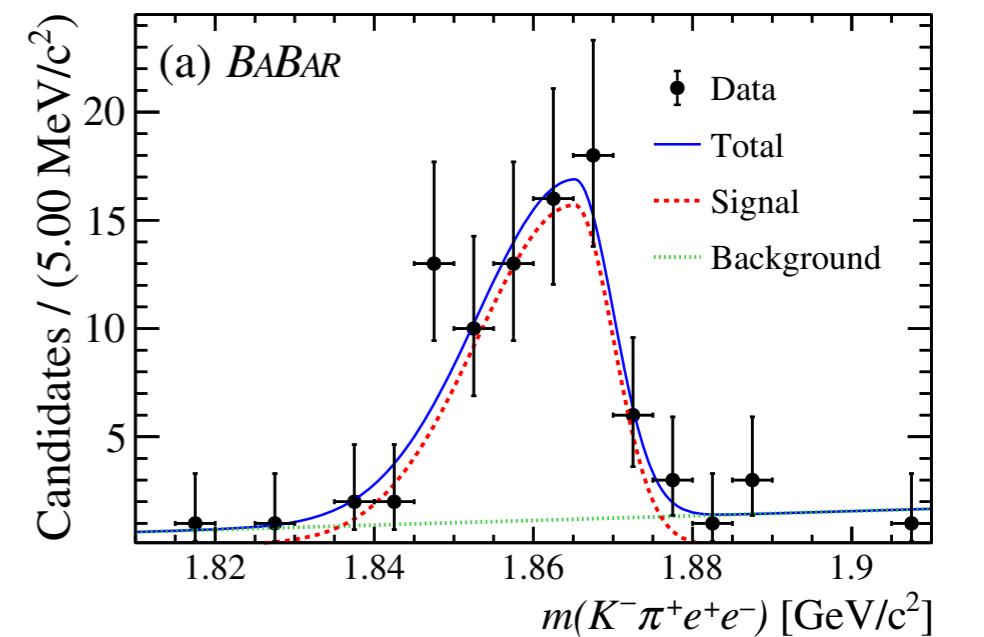
- First observation of  $D^0 \rightarrow K^- \pi^+ e^+ e^-$  at BaBar with  $0.5/\text{ab}$

$$\begin{aligned} \mathcal{B}(D^0 \rightarrow K^- \pi^+ [e^+ e^-]_{\rho^0/\omega}) \\ = (4.0 \pm 0.5) \times 10^{-6} \end{aligned}$$

- Radiative and neutrals: e.g.

$$D^0 \rightarrow V^0 \gamma, D^0 \rightarrow \gamma \gamma, D_{(S)} \rightarrow K \pi \pi \gamma, \dots$$

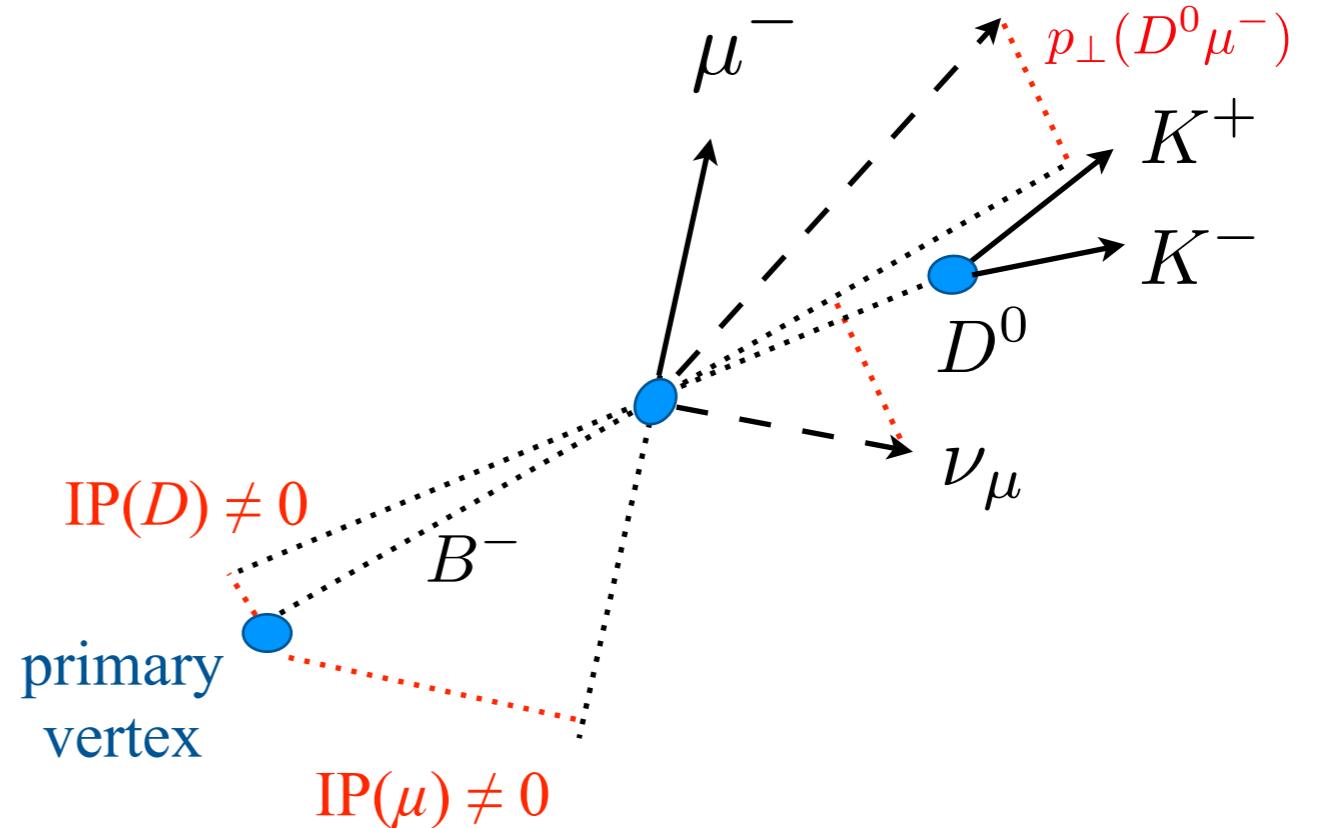
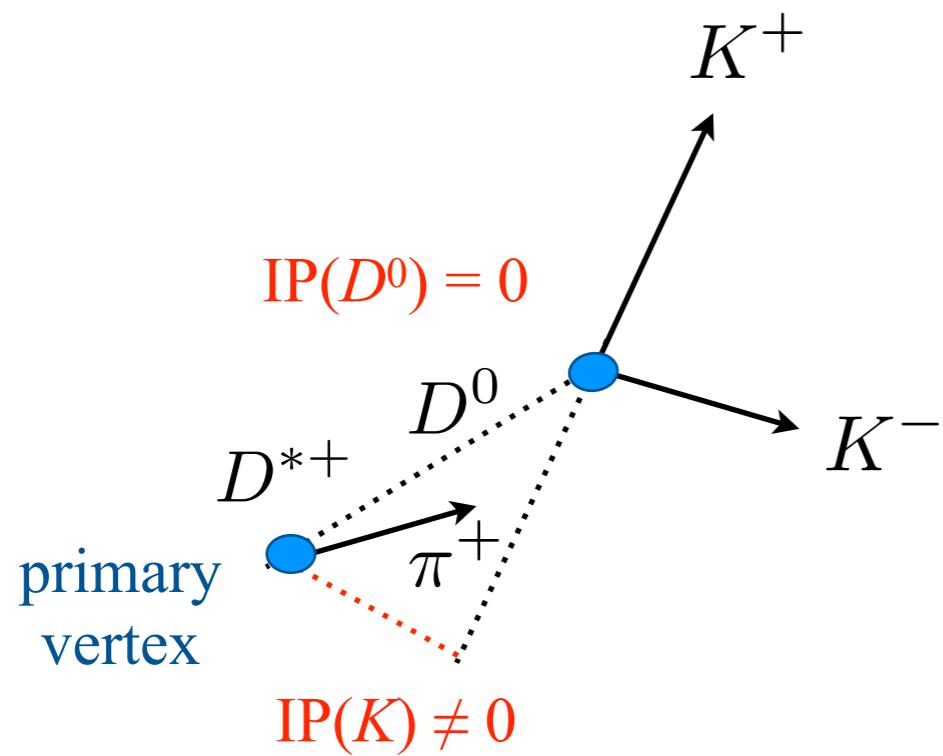
[PRL 122 (2019) 081802]



# Backup slides

# $D^0 \rightarrow h^+ h^-$ decays at LHCb

$$m_{\text{corr}} = \sqrt{m^2(D^0\mu^-) + p_\perp(D^0\mu^-)^2} + p_\perp(D^0\mu^-)$$



- Prompt charm ( $\pi$  tagged): well identified kaons/pions forming a displaced secondary vertex, paired with low-momentum pion to form a  $D^{*+}$  vertex that coincides with the primary vertex
- From semileptonic  $B$  decays ( $\mu$  tagged): well identified and displaced muon paired with  $D^0$  candidate, requirement on corrected mass to (partly) compensate for undetected neutrino

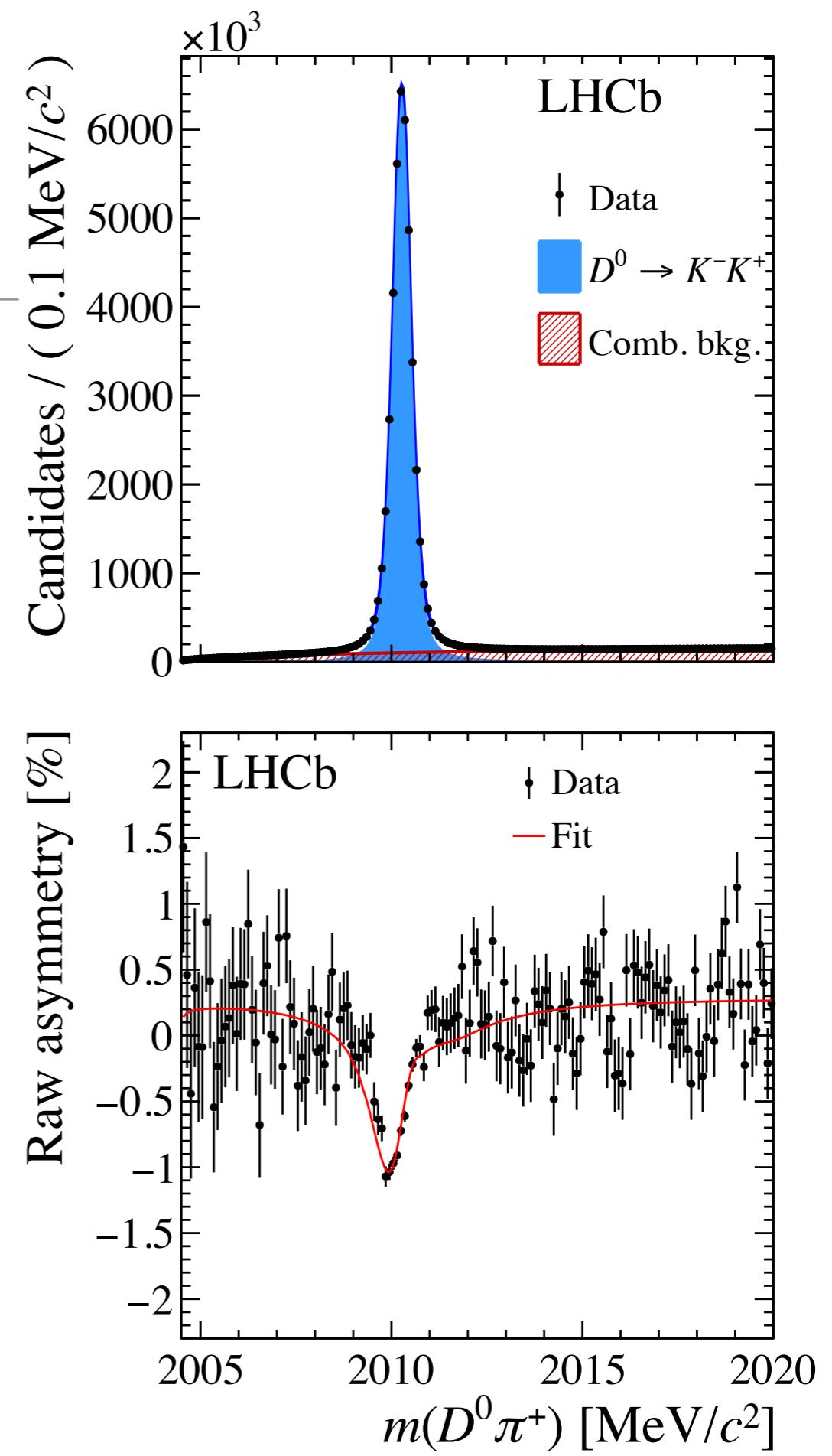
# Systematic uncertainties

[PRL 122 (2019) 211803]

Source	$\pi$ -tagged	$\mu$ -tagged
Fit model	0.6	2
Mistag	—	4
Weighting	0.2	1
Secondary decays	0.3	—
$B$ fractions	—	1
$B$ reco. efficiency	—	2
Peaking background	0.5	—
Total	0.9	5

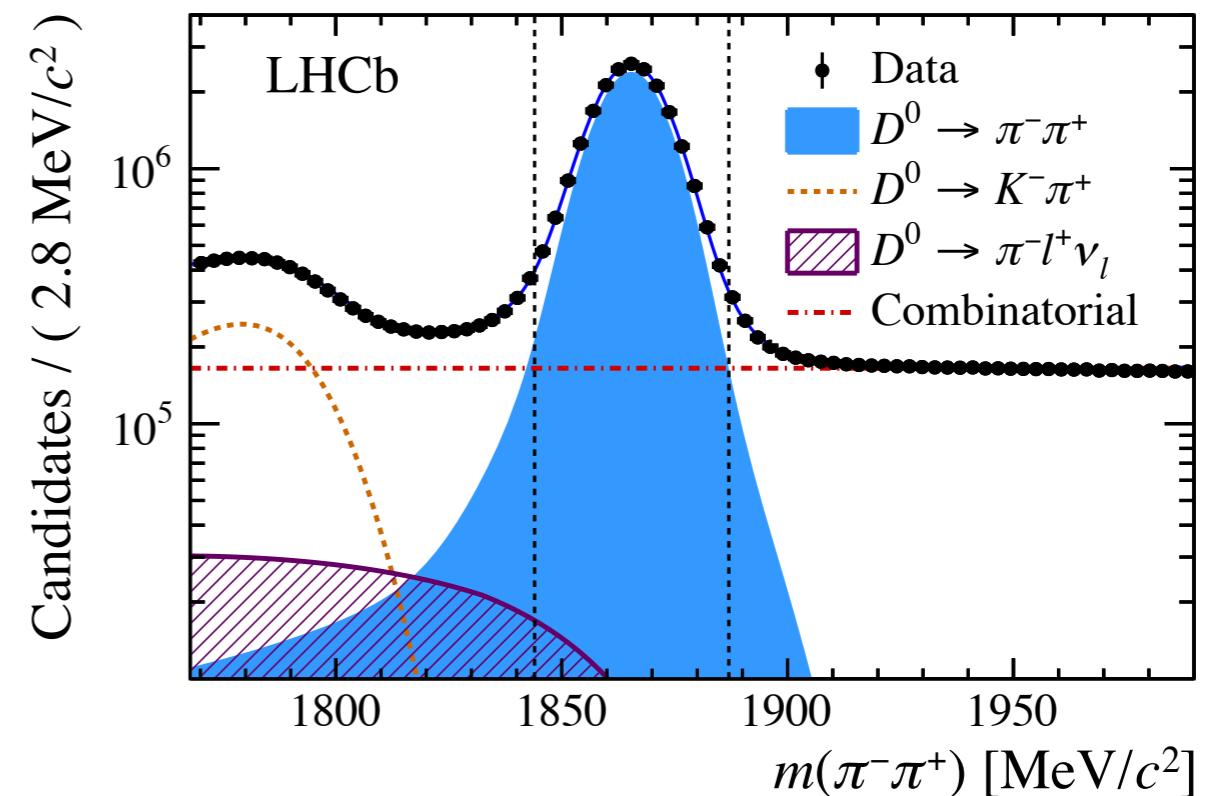
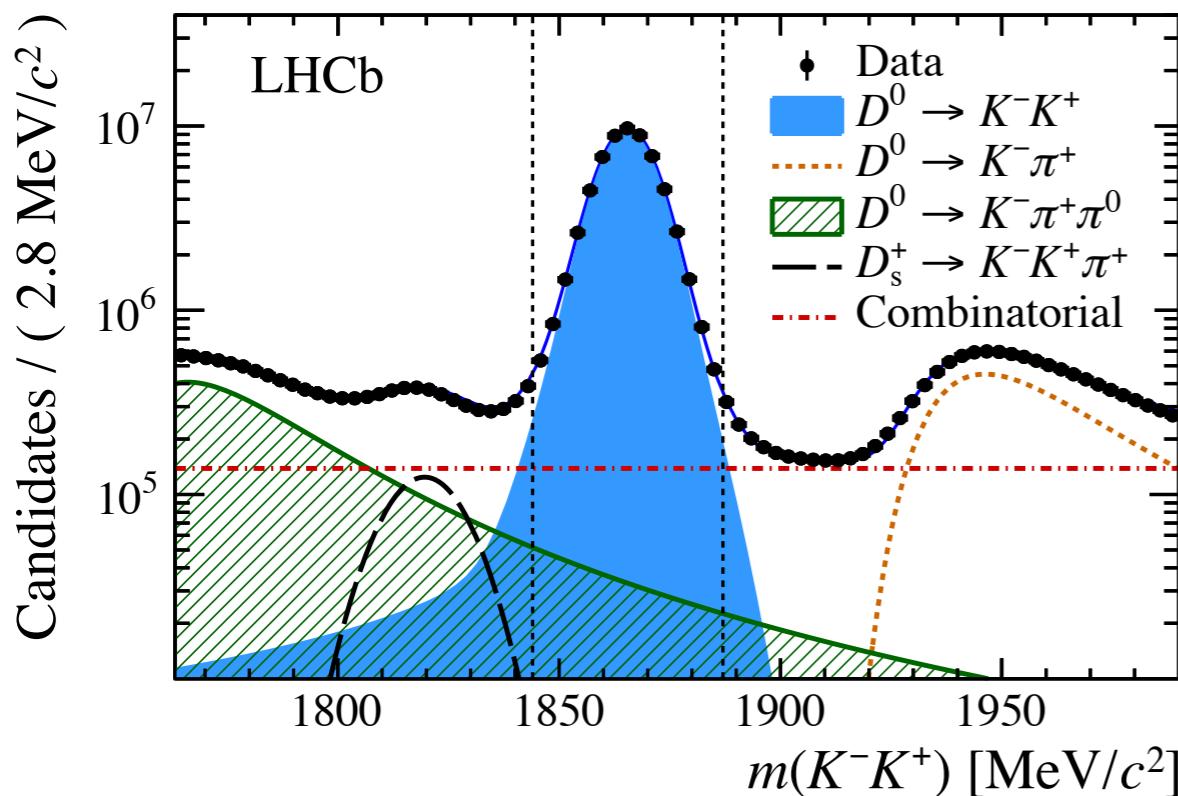
# Fit model

- Mass model with  $O(10M)$  candidates is never perfect
- Impact on asymmetries is generally marginal
- However, mass shapes may also be charge asymmetric (momentum scale/resolution is slightly asymmetric)
- Tested a variety of alternative models, bias on signal asymmetry estimated using pseudoexperiments



# Peaking background

[PRL 122 (2019) 211803]

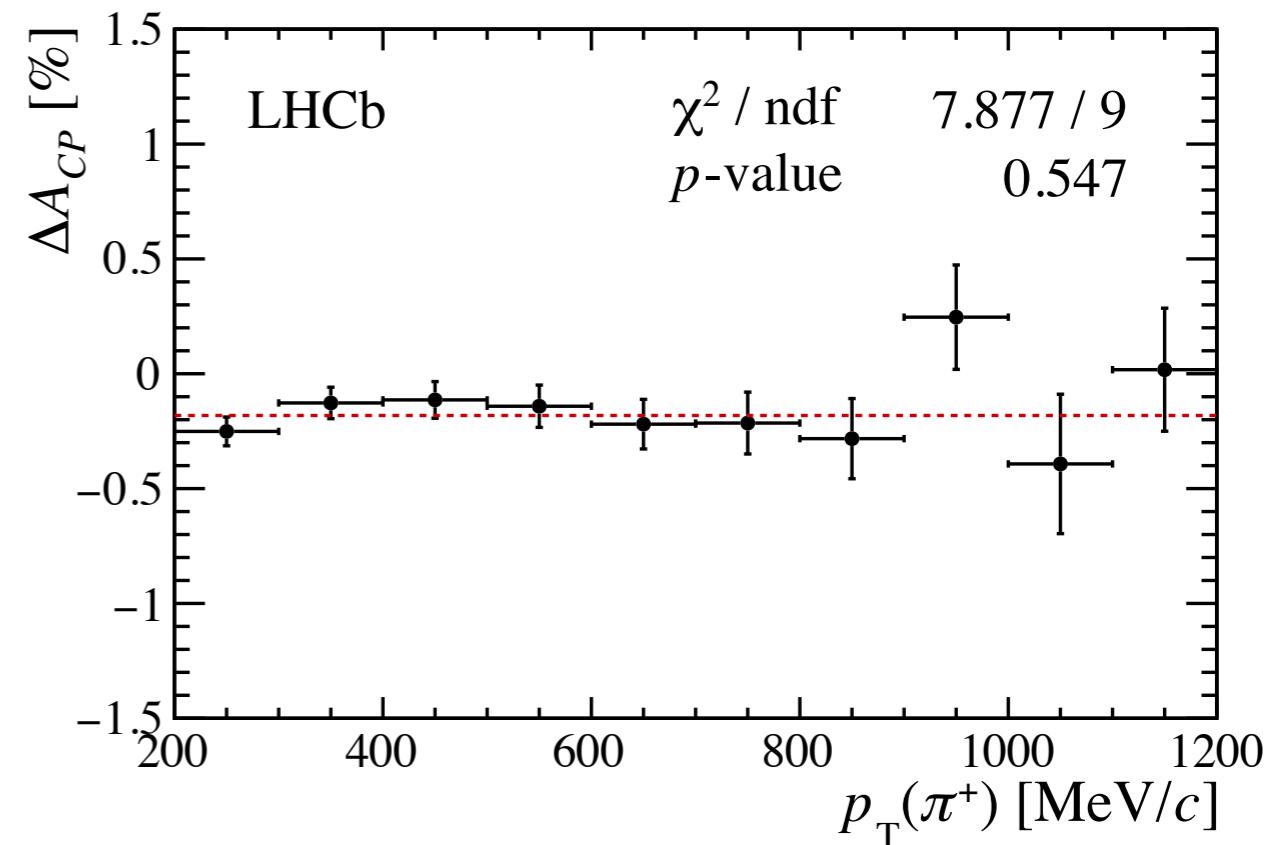
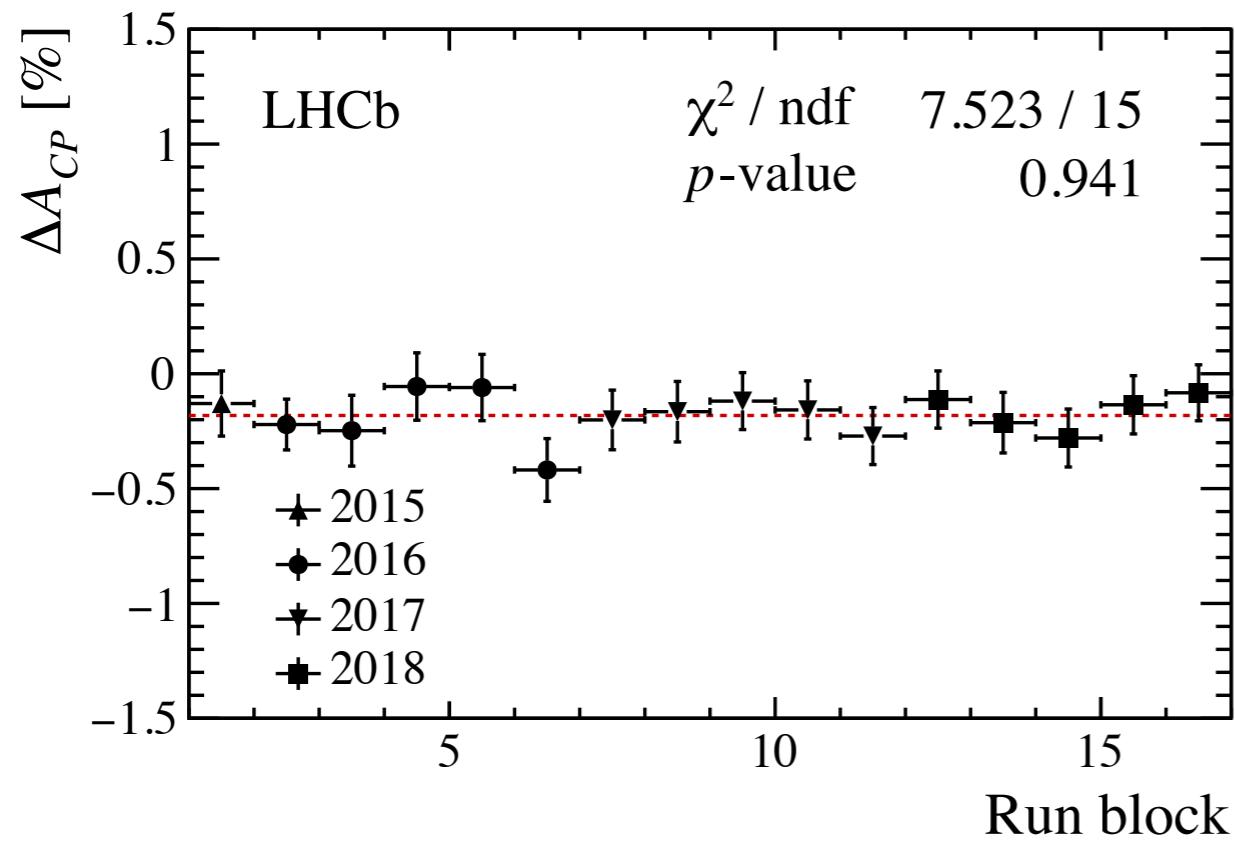


- Backgrounds due to  $D^{*+} \rightarrow D^0 \pi^+$  decays, where the  $D^0$  is mis- or partially reconstructed would peak in  $m(D^0 \pi^+)$
- Bias on signal asymmetry estimated by measuring backgrounds asymmetry and contamination in the  $D^0$ -mass signal region

# Consistency checks

[PRL 122 (2019) 211803]

- Measured value of  $\Delta A_{CP}$  studied as a function of several variables (e.g., magnet polarity, data-taking period, kinematics)



- No evidence found for unexpected dependences

# Interpretation of $\Delta A_{CP}$

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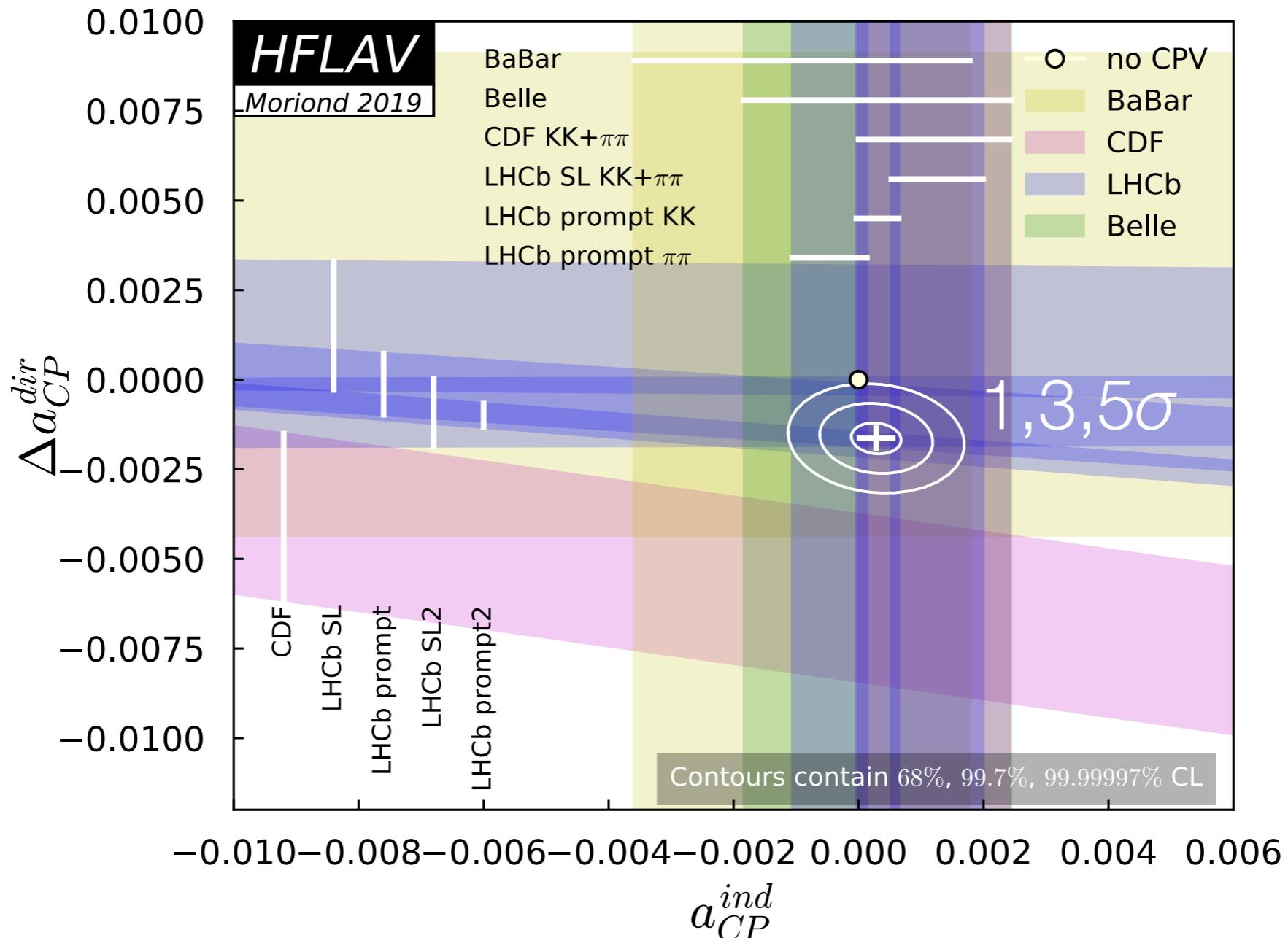
- The time-integrated asymmetry receives contribution from  $CP$  violation in the decay amplitudes (direct) and in  $D^0-\bar{D}^0$  mixing (indirect)

$$A_{CP}(h^+ h^-) \approx a_{CP}^{\text{dir}}(h^+ h^-) + \frac{\langle t \rangle}{\tau} a_{CP}^{\text{ind}}$$

- Indirect contribution is to a good approximation independent of the decay mode
- Since  $\Delta \langle t \rangle \sim 0.1 \tau$ ,  $\Delta A_{CP}$  is mostly a measurement of direct  $CP$  violation

$$\Delta A_{CP} \approx \Delta a_{CP}^{\text{dir}} + \frac{\Delta \langle t \rangle}{\tau} a_{CP}^{\text{ind}}$$

# Experimental status of $CP$ violation in $D^0 \rightarrow h^+h^-$

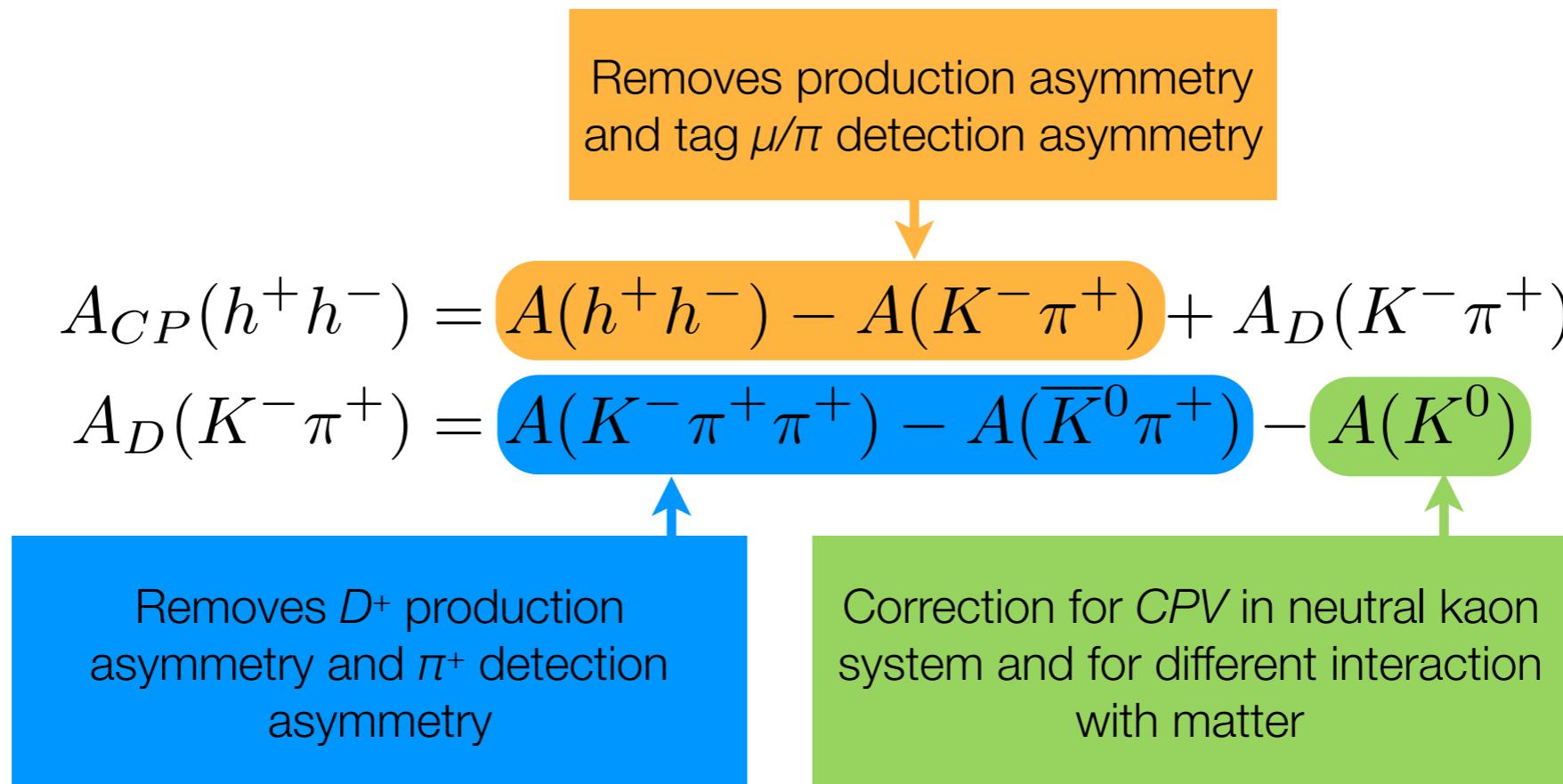


$$\Delta a_{CP}^{\text{dir}} = (-16.4 \pm 2.8) \times 10^{-4}$$

$$a_{CP}^{\text{ind}} = (-2.8 \pm 2.6) \times 10^{-4}$$

# Individual asymmetries at LHCb

- Use large samples of Cabibbo-favored  $D^0 \rightarrow K^-\pi^+$ ,  $D^+ \rightarrow K^-\pi^+\pi^+$  and  $D^+ \rightarrow \bar{K}^0\pi^+$  decays (where no CPV is expected) to cancel detector and production asymmetries



$$A_{CP}(D^0 \rightarrow K^+K^-) = (1.4 \pm 1.5 \pm 1.0) \times 10^{-3}$$

$$A_{CP}(D^0 \rightarrow \pi^+\pi^-) = (2.4 \pm 1.5 \pm 1.1) \times 10^{-3}$$

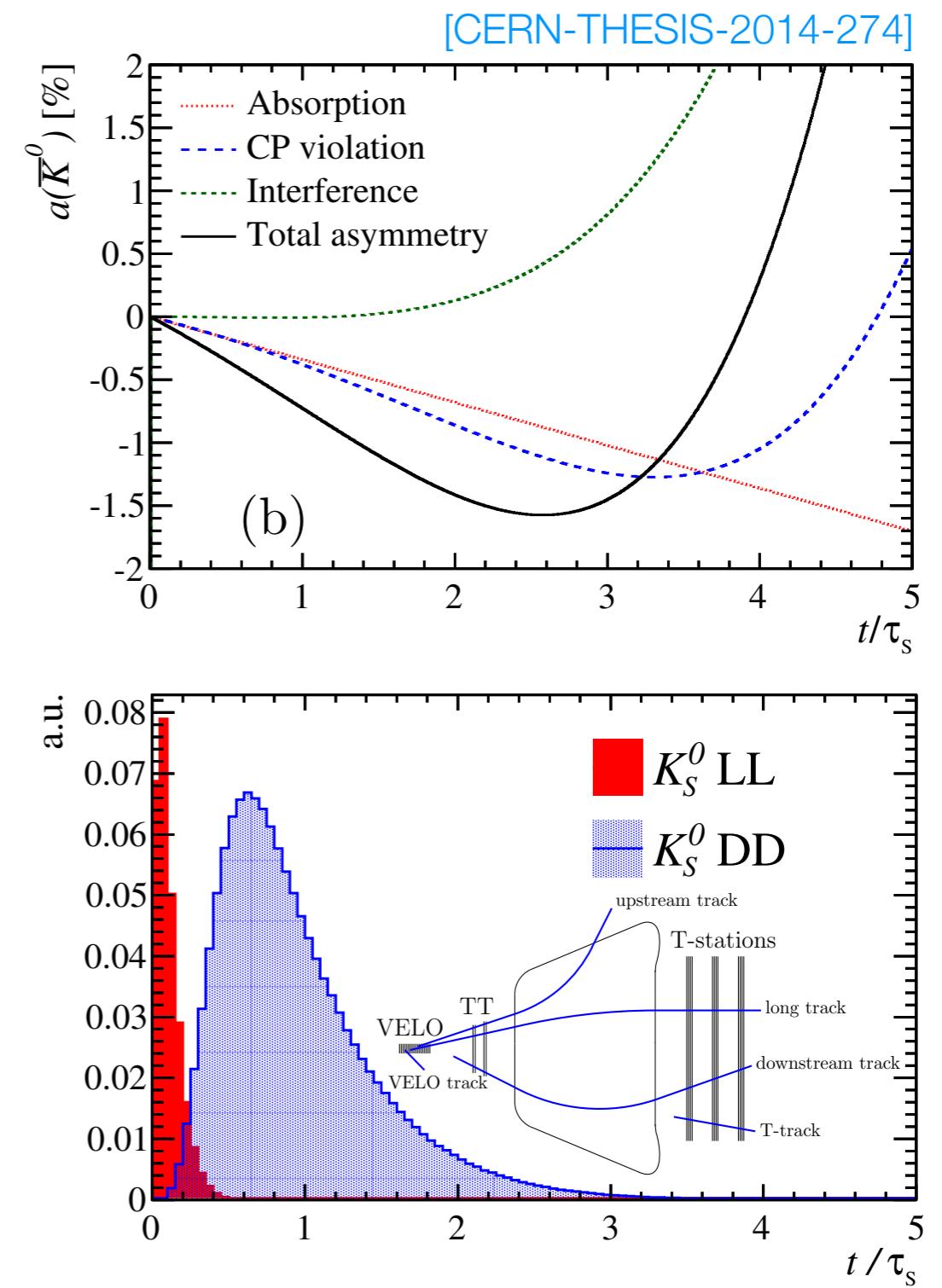
# Neutral kaons asymmetry

- Neutral kaons violates  $CP$  and their mixing can be affected by material interactions (*i.e.* regeneration of  $K_S$  in  $K_L$  beams)
- Both effects lead to tiny detection asymmetries when using  $K_S$  that decay in the VELO (LL)

$$A(K_S \text{ LL}) = (-0.73 \pm 0.05) \times 10^{-3}$$

$$A(K_S \text{ DD}) = (-6.2 \pm 0.3) \times 10^{-3}$$

- Uncertainty limited by the knowledge of the detector material — if not under control, may impact the ultimate precision
- $CP$  asymmetries with one  $K_S$  mesons in the final state are currently limited to LL candidates (~1/3 of reconstructed decays)



# Phase-space binning

$$c_b \equiv \frac{1}{\sqrt{F_b F_{-b}}} \int_b dm_+^2 dm_-^2 |A_f(m_+^2, m_-^2)| |A_f(m_-^2, m_+^2)| \cos[\Delta\delta(m_+^2, m_-^2)], \quad (26)$$

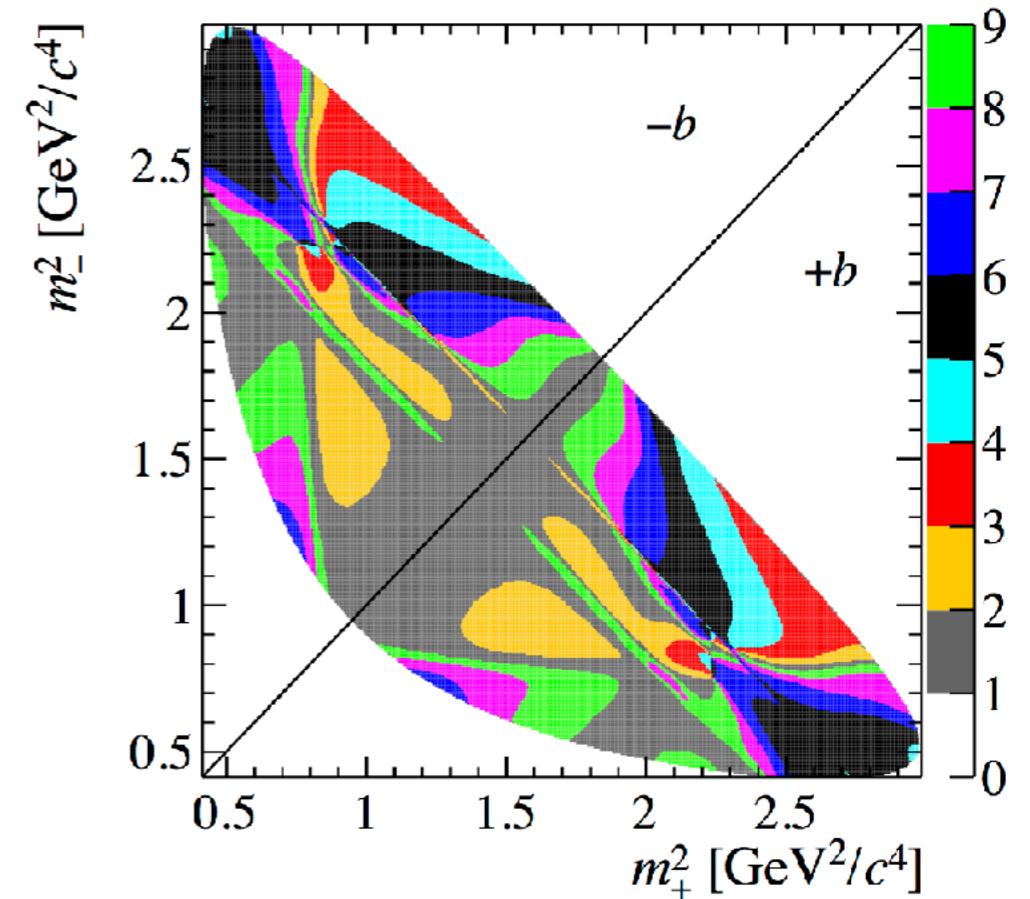
$$s_b \equiv \frac{1}{\sqrt{F_b F_{-b}}} \int_b dm_+^2 dm_-^2 |A_f(m_+^2, m_-^2)| |A_f(m_-^2, m_+^2)| \sin[\Delta\delta(m_+^2, m_-^2)], \quad (27)$$

where  $\Delta\delta(m_+^2, m_-^2) = \delta(m_+^2, m_-^2) - \delta(m_-^2, m_+^2)$  and  $\delta(m_+^2, m_-^2)$  is the phase of  $A_f(m_+^2, m_-^2)$ .

$$2\pi(b - 3/2)/n < \Delta\delta(m_+^2, m_-^2) < 2\pi(b - 1/2)/n, \quad b = 1, \dots, n.$$

$b$	$c_b$	$s_b$
1	$0.655 \pm 0.036 \pm 0.042$	$-0.025 \pm 0.098 \pm 0.043$
2	$0.511 \pm 0.068 \pm 0.063$	$0.141 \pm 0.183 \pm 0.066$
3	$0.024 \pm 0.140 \pm 0.080$	$1.111 \pm 0.131 \pm 0.044$
4	$-0.569 \pm 0.118 \pm 0.098$	$0.328 \pm 0.202 \pm 0.072$
5	$-0.903 \pm 0.045 \pm 0.042$	$-0.181 \pm 0.131 \pm 0.026$
6	$-0.616 \pm 0.103 \pm 0.072$	$-0.520 \pm 0.196 \pm 0.059$
7	$0.100 \pm 0.106 \pm 0.124$	$-1.129 \pm 0.120 \pm 0.096$
8	$0.422 \pm 0.069 \pm 0.075$	$-0.350 \pm 0.151 \pm 0.045$

[PRD 82 (2010) 112006]



# Sensitivity study

[PRD 99 (2019) 012007]

- Generated 1M signal-only  $D^0 \rightarrow K_S \pi^+ \pi^-$  decays using the BaBar amplitude model and compared sensitivity to  $x$  and  $y$  with different analysis methods (all other nuisance parameters fixed)

Analysis method	$\sigma(x)$	$\sigma(y)$
Model-dependent	0.11%	0.10%
Original model-independent	0.20%	0.18%
Bin-flip model-independent	0.15%	0.29%

- Bin-flip method gives better sensitivity to  $x$  than the original model-independent method
- Similar ratios of sensitivities hold for the  $CP$ -violation parameters when fitting  $D^0$  and  $\bar{D}^0$  decays separately

$$\begin{aligned}x &\longrightarrow x^\pm = x_{CP} \pm \Delta x \\y &\longrightarrow y^\pm = y_{CP} \pm \Delta y\end{aligned}$$

# A new parametrization

[PRD 99 (2019) 012007]

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$$z_{CP} \pm \Delta z = -(q/p)^{\pm 1}(y + ix)$$

$$x_{CP} = -\Im(z_{CP}) = \frac{1}{2} \left[ x \cos \phi \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) + y \sin \phi \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \right]$$

$$\Delta x = -\Im(\Delta z) = \frac{1}{2} \left[ x \cos \phi \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) + y \sin \phi \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \right]$$

$$y_{CP} = -\Re(z_{CP}) = \frac{1}{2} \left[ y \cos \phi \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) - x \sin \phi \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \right]$$

$$\Delta y = -\Re(\Delta z) = \frac{1}{2} \left[ y \cos \phi \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) - x \sin \phi \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \right]$$