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LMU München

Belle II Germany Meeting, 20 Sep 2022









#### Introduction



- Prediction of decay channels from final state particles
  - -> Tell the branching ratios of different decay modes in a dataset
- Full reconstructions of decay trees





#### Introduction

# **Goals:**

- Prediction of decay channels from final state particles
  - -> Tell the branching ratios of different decay modes in a dataset
- Full reconstructions of decay trees

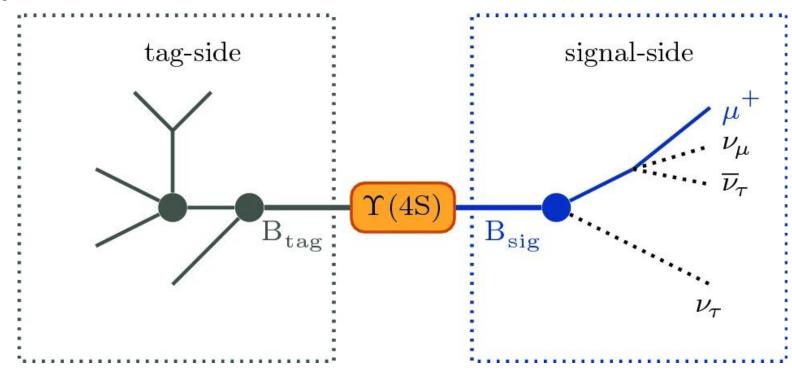
# **Related work:**

Full Event Interpretation



Motivation

# **Full Event Interpretation**



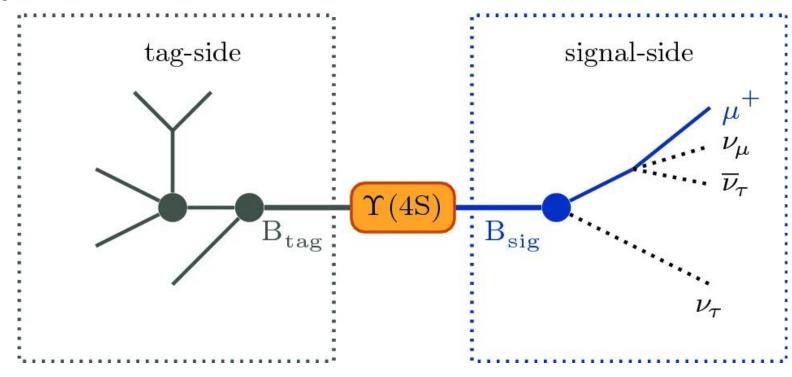
- Explicitly reconstruct tag side
- Recover the kinematic and flavour information of signal side





#### Motivation

# **Full Event Interpretation**



- Explicitly reconstruct tag side
- Recover the kinematic and flavour information of signal side
- Kernel: Decision Tree to predict reconstructions
  - -> Performance strongly restricted by training





#### Motivation



# **Full Event Interpretation**

Low tag-side efficiency (the fraction of correctly tagged Y(4S) events)

	<b>B</b> <sup>±</sup> (%)	B <sup>0</sup> (%)
Hadronic	0.76	0.46
Semileptonic	1.80	2.04

Low covered branching fractions

	Inclusive		Exclusive	
	$m{B}^{\pm}~(\%)$	<b>B</b> <sup>0</sup> (%)	$m{B}^{\pm}$ (%)	<b>B</b> <sup>0</sup> (%)
Hadronic	9.0	9.8	1.7	1.1
Semileptonic	17.4	15.3	5.2	4.0



#### Introduction



## Goals:

- Prediction of decay channels from final state particles
  - -> Tell the branching ratios of different decay modes in a dataset
- Full reconstructions of decay trees

#### Related work:

Full Event Interpretation

#### **Limitation of FEI:**

- Low tagging efficiency or tag-side efficiency
- Low covered branching fractions



#### Motivation



- Create a space to continuously represent all possible decays
  - -> not restriced by the channels used in the training



#### Motivation



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- Encode decay relations in the space



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- Tolerant to missing particles
  - -> ensure higher efficiency



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  - -> enable the reconstruction of both B mesons at the same time



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- Encode decay relations in the space
- Tolerant to missing particles
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  - -> enable the reconstruction of both B mesons at the same time
- Build dynamics in the space to introduce reconstruction processes



Hyperbolic Space

Possible solution: Hyperbolic Space

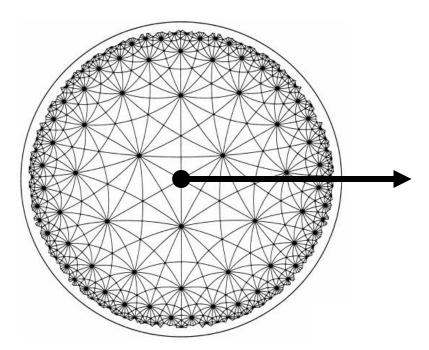




#### Hyperbolic Space



# Possible solution: Hyperbolic Space (2D example – Poincare disc)



Curves = Straight lines in Poincare disc

$$\mathbb{D}^n = \{ x \in \mathbb{R}^n : c ||x||^2 < 1, c \ge 0 \}$$

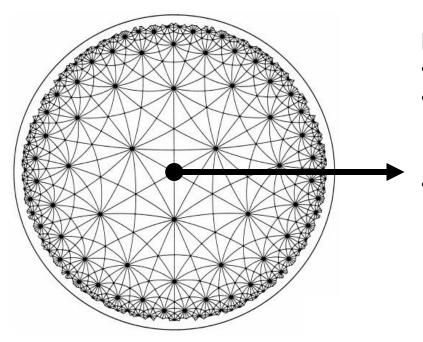
$$g^{\mathbb{D}} = \lambda_c^2 g^E$$

$$\lambda_c = \frac{2}{1 - c ||x||^2}$$



#### Hyperbolic Space

# Possible solution: Hyperbolic Space (2D example – Poincare disc)



#### Properties:

- Rotational symmetry
- Size of an object with distance d to the center is proportional to  $1-d^2$ 
  - -> Points will never reach the boundary
  - -> Effective space near the boundary is infinite
- Volume of the space scales exponentially with radius

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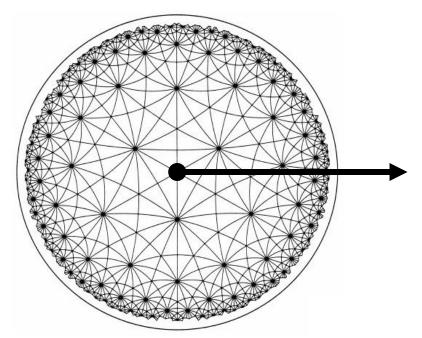
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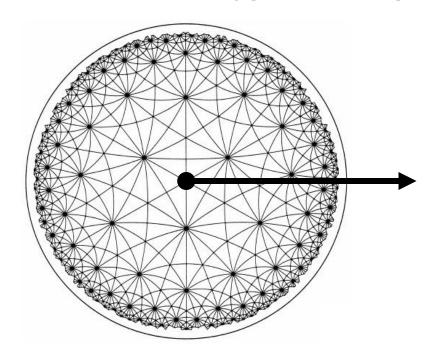
#### Comparison:

- In Euclidean spaces: Volume grows **polynomially** with radius
- For trees: Number of nodes grows exponentially with level



Hyperbolic Space

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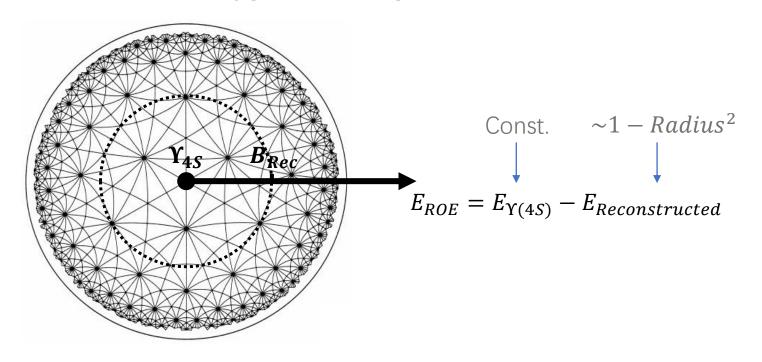






### Hyperbolic Space

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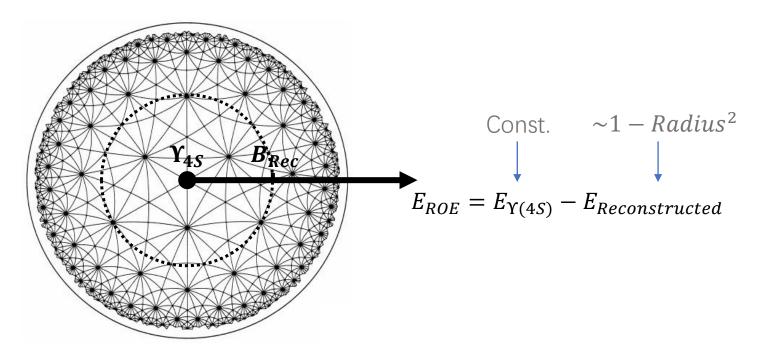




#### Hyperbolic Space



# Possible solution: Hyperbolic Space (2D example – Poincare disc)



- Center: Singularity containing all full reconstructions of  $\Upsilon(4S)$  -> Empty rest of event (ROE)
- Bulk points: Partially reconstructed decays
- Points near boundary: Starting points of reconstructions
  - -> The less reconstructed, the smaller branching ratio (taking less place in embedded space)
  - -> Enable all possible decays

#### Preparation



# **Proof of concept: Toy Monte Carlo**

#### **Dataset:**

Four channels:

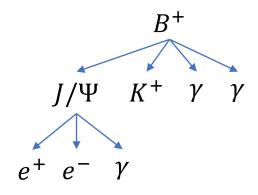
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$$B^+ \rightarrow (J/\Psi \rightarrow e^+e^-)K^+$$

• 
$$B^- \to (D^0 \to K^- \pi^+) \pi^-$$

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$$B^+ \rightarrow \overline{D^0} \pi^+ \pi^0$$

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Each event (Y4S Decay) produces several samples according to the depth of particles to its root B meson, e.g.



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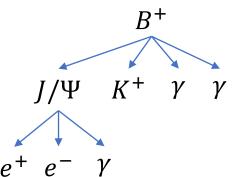
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- Depth 2 (Sample 2)
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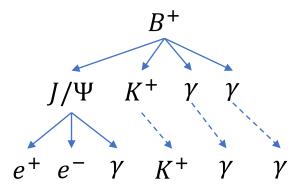
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Depth 1 (Sample 1)

 $J/\Psi$   $K^+$   $\gamma$   $\gamma$ 

 $B^+$ 

- Depth 2 (Sample 2)
- Depth 3 (Sample 3)

Each particle carries 12 features (**Bold** for reconstruction part)

**PDG**, mass, charge, energy, production time, x, y, z, **px**, **py**, **pz**, nDaughters



# Preparation



Stage	Neural Networks	Task	Technics	Status
Particle Level Embedding				
Sample Level Embedding				
Reconstruction				



# Preparation



Stage	Neural Networks	Task	Technics	Status
Particle Level Embedding	Automatic Feature Interaction (AutoInt) + Transformer Encoder			
Sample Level Embedding	Transformer Encoder + Hyperbolic Embedding (HypTr)			
Reconstruction	Hyperbolic Transformer Decoder + Generative Adversarial Set Transformer (GAST)			



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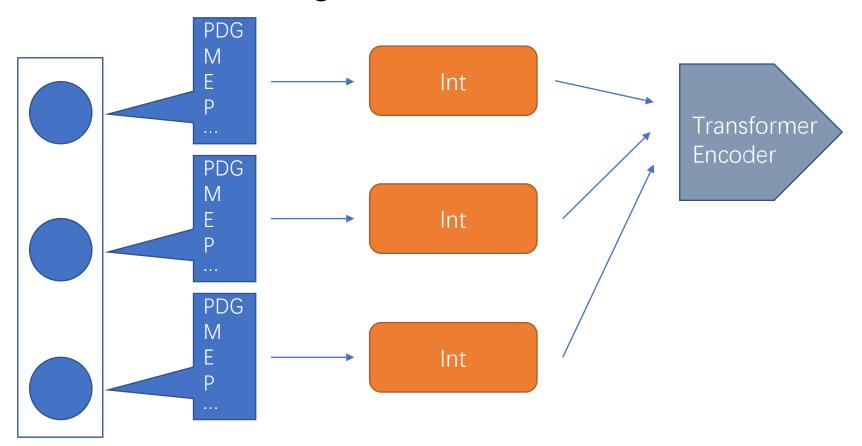


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Particle Level Embedding	Automatic Feature Interaction (AutoInt) + Transformer Encoder	Prediction of combinations of daughter particles	Supervised pre-training	Finished on toy MC
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Reconstruction	Hyperbolic Transformer Decoder + Generative Adversarial Set Transformer (GAST)	Generation of samples with mother particles	Unsupervised training + Knowledge transfer	On going



Practice

# Particle Level Embedding:

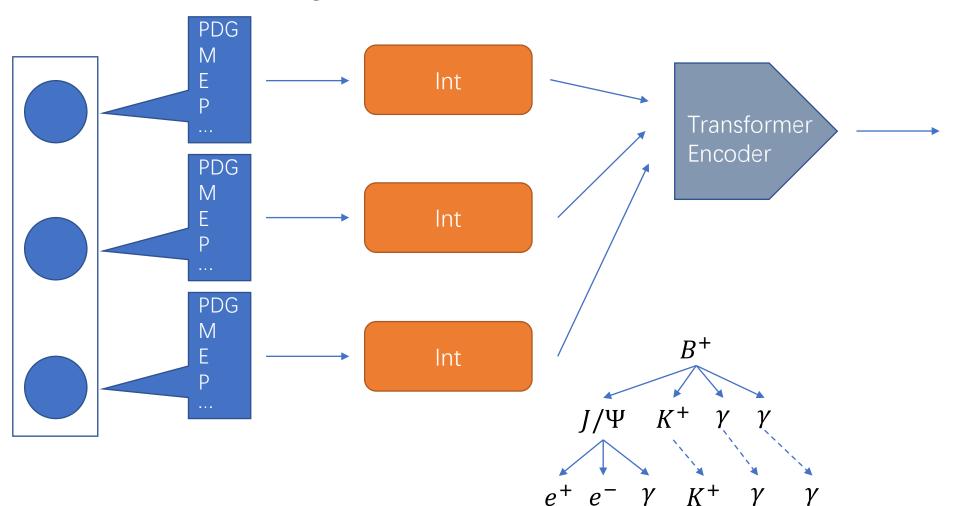




Practice

Sub-Task

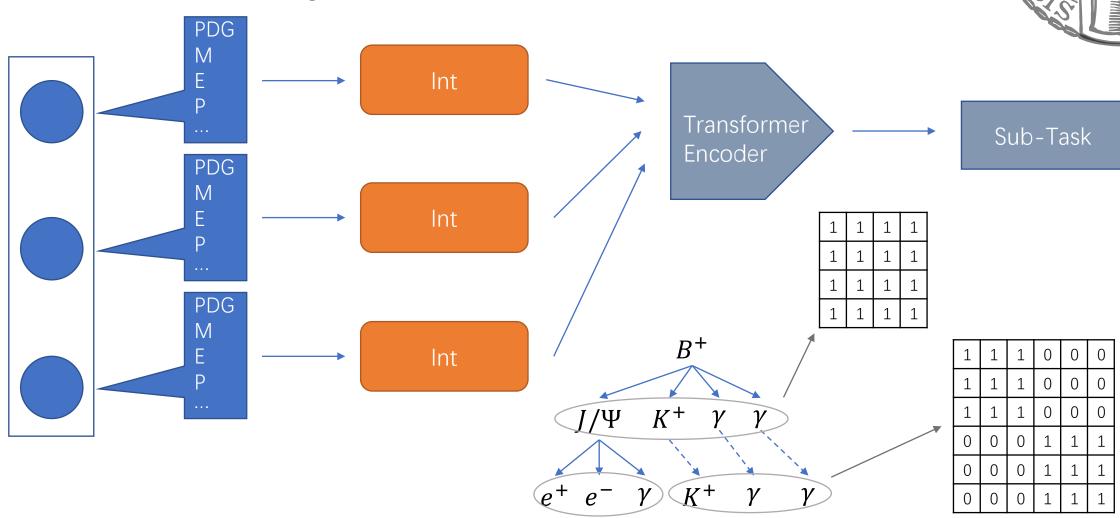
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Practice

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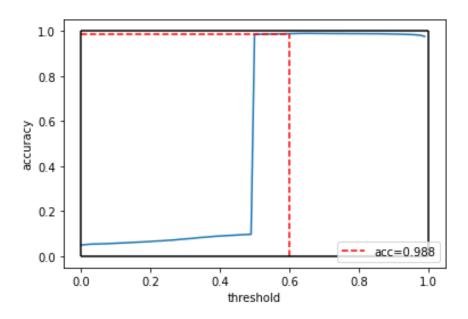


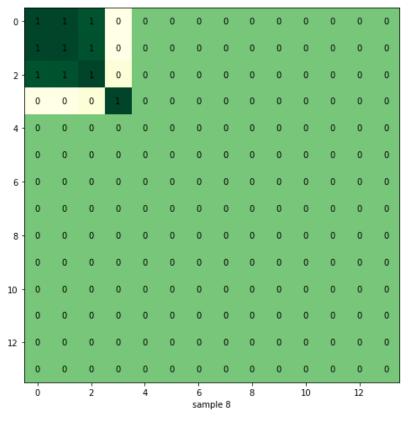


Practice

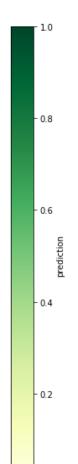
# Particle Level Embedding:

Performance on toy MC



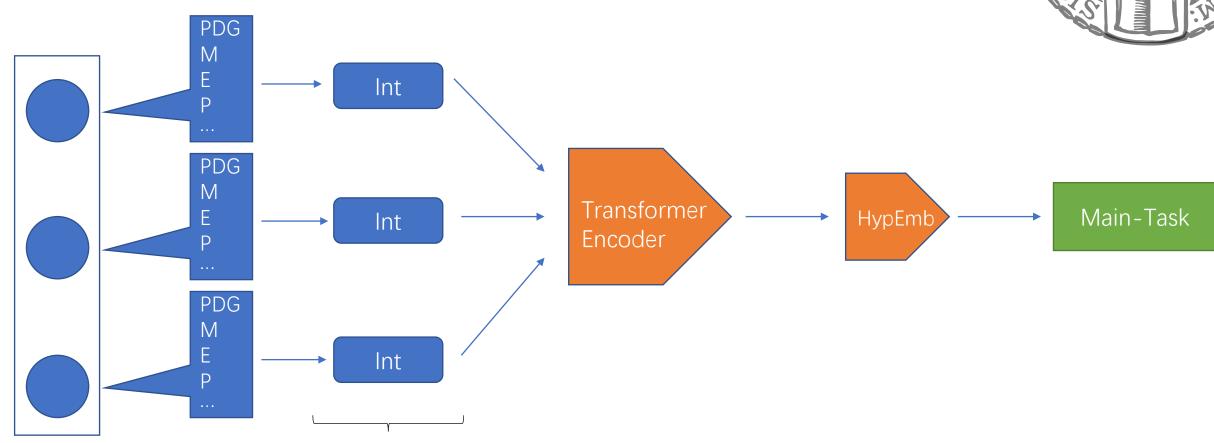






Practice

# Sample Level Embedding:



Pre-learned particle level embedding: Frozen at the beginning of trainings

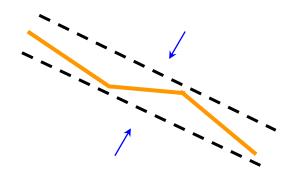


#### Practice



# **Sample Level Embedding –** Losses:

• Intra loss: align the samples from the same decay event, separate otherwise



Intra loss

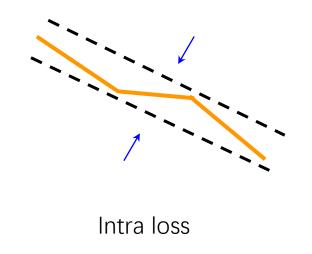


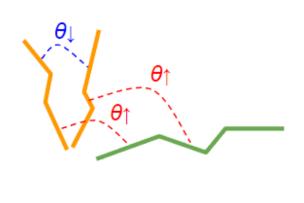
#### Practice

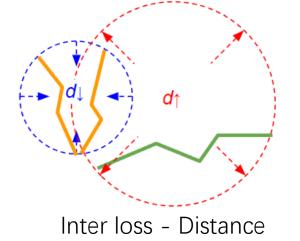


# **Sample Level Embedding –** Losses:

- Intra loss: align the samples from the same decay event, separate otherwise
- Inter loss:
  - Angle loss: minimize the angles between pairs from similar decays (same channel for toy MC), maximize otherwise
  - Distance loss: minimize the hyperbolic distance between pairs from similar decays, maximize otherwise







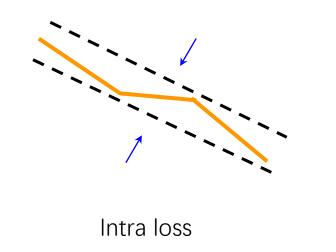


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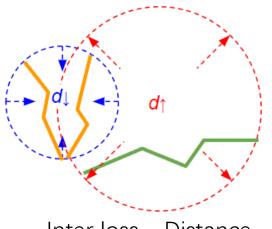


#### **Sample Level Embedding –** Losses:

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  - Angle loss: minimize the angles between pairs from similar decays (same channel for toy MC), maximize otherwise
  - Distance loss: minimize the hyperbolic distance between pairs from similar decays, maximize otherwise
- Radius loss: encourage the radius of embedded samples to be certain values according to their depths will be replaced by fix radius calculated from  $E_{ROE}$  in the future



 $\theta \uparrow$ 



Inter loss - Distance

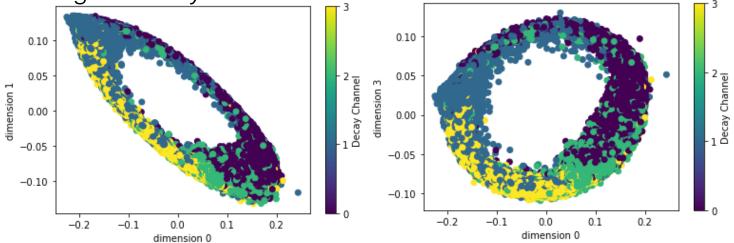


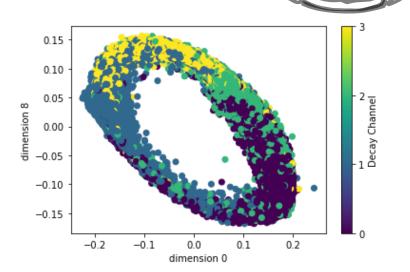
Practice

# Sample Level Embedding:

Visualisation with 16 dimensional hyperbolic embedding

Clustering vs. Decay channels



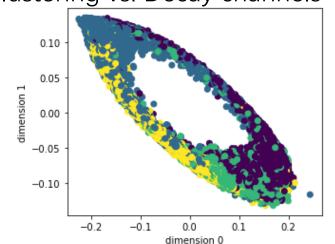


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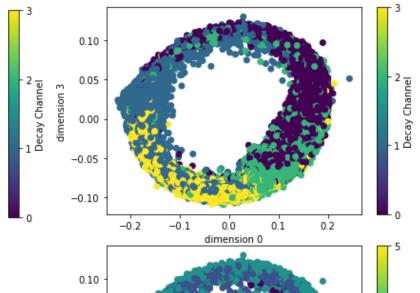
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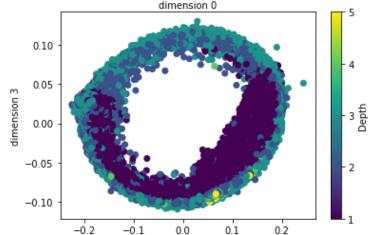
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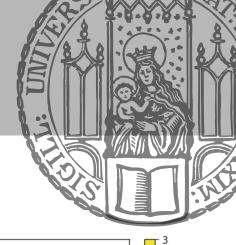


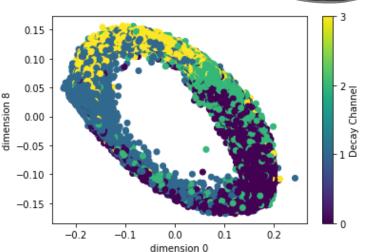






dimension 0







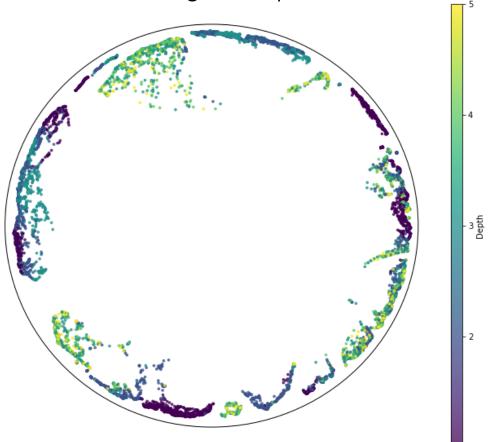
Practice

# Sample Level Embedding:

Visualisation with UMAP\* for 16 dimensional hyperbolic embedding

Clustering vs. Decay channels

Clustering vs. Depth





#### Summary



# **Capacities:**

Particle Level Embedding

• 12K Parameters

Sample Level Embedding

- 900K Parameters
- 16-D hyperbolic space



#### Summary



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#### In Comparison – Famous Networks using Transformer

- Vision Transformer (small): 85M Parameters
- BERT (small): 110M Parameters
- GPT-3: 175B Parameters
- Hyperbolic Vision Transformer: 22M Parameters, 384-D hyperbolic space



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#### -> Great potential for improvement



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- Finished the prediction of decay channels from final state particles for toy MC
- Hyperbolic embedding works for the representation of decays



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#### To do:

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- Study the necessity of using hyperbolic embedding, i.e. improvement against Euclidean space
- Try with real dataset with general channels
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#### **Outlook:**

- Once well trained with large dataset, can be used for the reconstruction of any decay channels
- The workflow / well trained networks can also be invested on other HEP projects



# Thank You for your Attention

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LMU München

Belle II Germany Meeting, 20 Sep 2022





#### Reference:

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- 2. T. Keck, "The Full Event Interpretation for Belle II", IEKP-KA-2014-18
- 3. W. Peng et al. "Hyperbolic Deep Neural Networks: A Survey", arXiv:2101.04562
- 4. A. Vaswani et al. "Attention Is All You Need", arXiv:1706.03762
- 5. W. Song et al. "AutoInt: Automatic Feature Interaction Learning via Self-Attentive Neural Networks", arXiv:1810.11921
- 6. K. Stelzner et al. "Generative Adversarial Set Transformers", Workshop on Object-Oriented Learning at ICML 2020
- 7. L. McInnes et al. "UMAP: Uniform Manifold Approximation and Projection for Dimension Reduction", arXiv:1802.03426
- 8. A. Ermolov et al. "Hyperbolic Vision Transformers: Combining Improvements in Metric Learning", arXiv:2203.10833



# Backup





#### Backup



#### **Hyperbolic metrics**

Addition: 
$$\mathbf{x} \oplus_c \mathbf{y} = \frac{(1 + 2c\langle \mathbf{x}, \mathbf{y} \rangle + c \|\mathbf{y}\|^2)\mathbf{x} + (1 - c \|\mathbf{x}\|^2)\mathbf{y}}{1 + 2c\langle \mathbf{x}, \mathbf{y} \rangle + c^2 \|\mathbf{x}\|^2 \|\mathbf{y}\|^2}$$

Distance: 
$$D_{hyp}(\mathbf{x}, \mathbf{y}) = \frac{2}{\sqrt{c}} \operatorname{arctanh}(\sqrt{c} \| -\mathbf{x} \oplus_{c} \mathbf{y} \|)$$

Exponential: 
$$\exp_{\mathbf{x}}^{c}(\mathbf{v}) = \mathbf{x} \oplus_{c} \left( \tanh \left( \sqrt{c} \frac{\lambda_{\mathbf{x}}^{c} || \mathbf{v} ||}{2} \right) \frac{\mathbf{v}}{\sqrt{c} || \mathbf{v} ||} \right)$$

with x the base point, usually set to 0



#### Backup



#### **Pairwise Cross-Entropy Loss**

Pairwisely calculate hyperbolic distance and euclidical cosine similarity

$$D_{hyp}(\mathbf{x}, \mathbf{y}) = \frac{2}{\sqrt{c}}\operatorname{arctanh}(\sqrt{c}\| - \mathbf{x} \oplus_{c} \mathbf{y}\|)$$

$$D_{cos}(\mathbf{z}_{i}, \mathbf{z}_{j}) = \left\| \frac{\mathbf{z}_{i}}{\|\mathbf{z}_{i}\|_{2}} - \frac{\mathbf{z}_{j}}{\|\mathbf{z}_{j}\|_{2}} \right\|_{2}^{2} = 2 - 2 \frac{\langle \mathbf{z}_{i}, \mathbf{z}_{j} \rangle}{\|\mathbf{z}_{i}\|_{2} \cdot \|\mathbf{z}_{j}\|_{2}}$$

• Calculate the cross entropy losses w.r.t the two metrics for positive pairs (i,j)

$$l_{i,j} = -\log \frac{\exp(-D(\mathbf{z}_i, \mathbf{z}_j)/\tau)}{\sum_{k=1, k \neq i}^K \exp(-D(\mathbf{z}_i, \mathbf{z}_k)/\tau)}$$

#### Backup



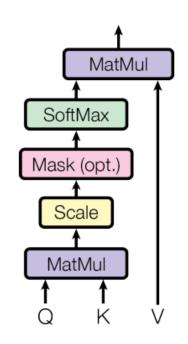
# **Building Block: Multihead Attention**

- Inputs and outputs are all vectors
  - *Q*: Query
  - *K*: Keys
  - V: Values
- Weights represent the similarity of Q and K
- Attention is reweighted V

$$\operatorname{Attention}(Q,K,V) = \operatorname{softmax}(\frac{QK^T}{\sqrt{d_k}})V$$

 Multi-Head enables different combinations of the subspaces of the inputs through linear projections

#### Scaled Dot-Product Attention

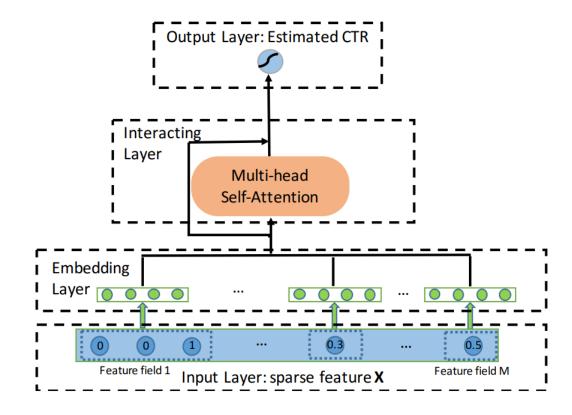


# Multi-Head Attention Linear Concat Scaled Dot-Product Attention Linear Linear

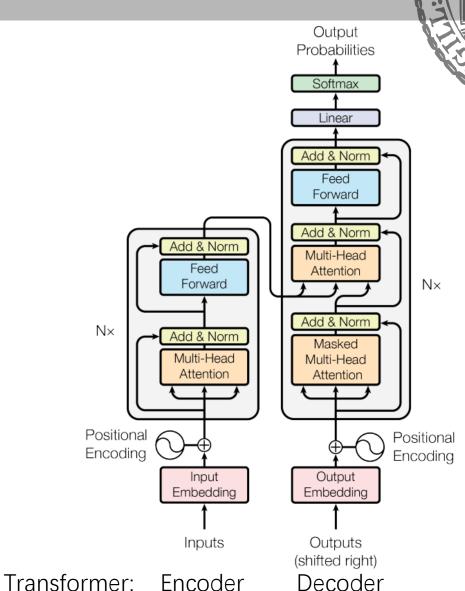


Backup

# **Building Block: Interactor and Transformer**



AutoInt: Interactor





Backup

### **Reconstruction:** Generative Adversarial Set Transformers + Knowledge Transfer

