

Probing NP with rare charm decays @ Belle II

Héctor Gisbert

TU Dortmund



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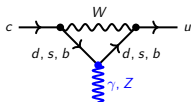
Rare charm decays are special!

1 Window to test FCNCs in the up-sector!

2 Strong non-perturbative dynamics \rightarrow "Null tests" $\mathcal{O} \pm \delta \mathcal{O}$

- Use SM symmetries: $\mathcal{O}_{\text{SM}} = 0$,
- Small uncertainties: $\mathcal{O}_{\text{SM}} \gg \delta \mathcal{O}_{\text{SM}}$,
- Use large hadronic effects to enhance NP contributions,
- Construct \mathcal{O} sensitive to specific NP,
- Use $SU(3)_F$ -flavor symmetry, ...

3 Very efficient GIM mechanism: $\sum_i \lambda_i = 0$ with $\lambda_i \equiv V_{ci}^* V_{ui}$.



$$= \sum_{i=d,s,b} \lambda_i f_i = \lambda_s \left[(f_s - f_d) + \frac{\lambda_b}{\lambda_s} (f_b - f_d) \right]$$

$$f_i \sim \frac{m_i^2}{(4\pi)^2 M_W^2}, \quad \text{Im}(\lambda_b/\lambda_s) \sim 10^{-3}$$

BRs (A_{CP}) are loop-(CKM-) suppressed!

Excellent place to search for BSM physics!

Rare charm decays are well-suited for Belle II

- $N(c\bar{c})_{\text{Belle II}} = 65 \cdot 10^9!$ (Abada:2019lih)

- How many charm hadrons h_c ?

★ $N(h_c) = 2 f(c \rightarrow h_c) N(c\bar{c})$

- ★ Fragmentation fractions (1509.01061)

$$N(h_c) \sim 10^{10}!$$

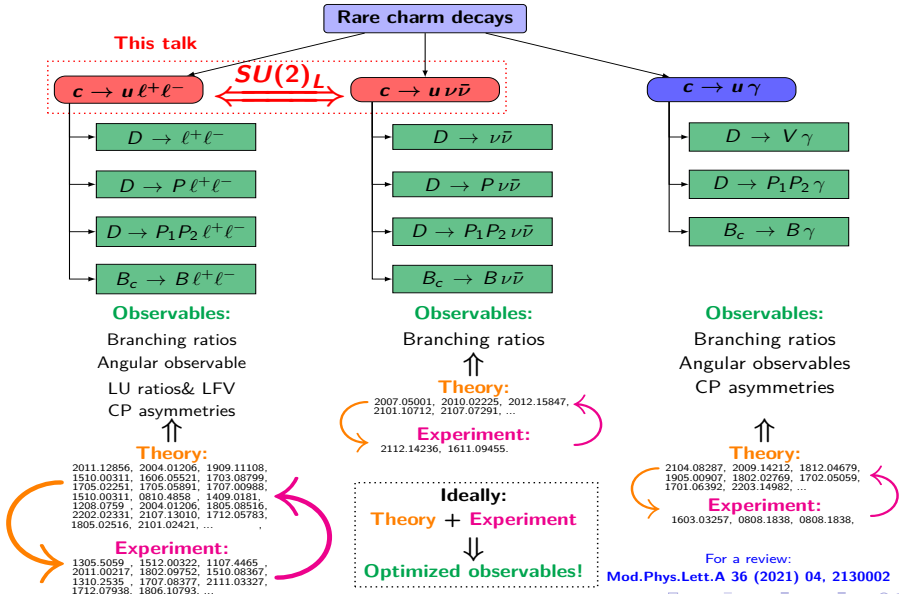
h_c	$f(c \rightarrow h_c)$	$N(h_c)_{\text{Belle II}}$
D^0	0.59	$8 \cdot 10^{10}$
D^+	0.24	$3 \cdot 10^{10}$
D_s^+	0.10	$1 \cdot 10^{10}$
Λ_c^+	0.06	$8 \cdot 10^9$

- And translated to branching ratios?

Relative statistical uncertainty: $\delta\mathcal{B}(h_c) = 1/\sqrt{N^{\text{exp}}}$ with $N^{\text{exp}} = \eta_{\text{eff}} N(h_c) \mathcal{B}(h_c)$

$$\eta_{\text{eff}} \mathcal{B}(h_c) \sim 10^{-9} \text{ for } \delta\mathcal{B}(h_c) = \frac{1}{5}$$

A sketch of the playground



EFT approach to charm physics (1)

- 1 **Dynamical fields ϕ_i at μ_{EW} : $\phi_i^{SM} = q_i, \ell_i, A_\mu, \dots$**
- 2 **Symmetries to build all $O_j(\phi_i)$ up to desired dimension ($D = 6$):**

$$\mathcal{H}_{\text{eff}} \sim \frac{4 G_F}{\sqrt{2}} \frac{\alpha_e}{4\pi} \sum_i C_i O_i$$

$$O_1^q = (\bar{u}_L \gamma_\mu T^a q_L)(\bar{q}_L \gamma^\mu T^a c_L), \quad O_2^q = (\bar{u}_L \gamma_\mu q_L)(\bar{q}_L \gamma^\mu c_L), \quad q = d, s,$$

$$O_7^{(\prime)} = \frac{m_c}{e} (\bar{u}_{L(R)} \sigma_{\mu\nu} c_{R(L)}) F^{\mu\nu}, \quad O_{9(10)}^{(\prime)} = (\bar{u}_{L(R)} \gamma_\mu c_{L(R)})(\bar{\ell} \gamma^\mu (\gamma_5) \ell),$$

$$O_{S(P)}^{(\prime)} = (\bar{u}_{L(R)} c_{R(L)})(\bar{\ell} (\gamma_5) \ell), \quad O_T(T_5) = \frac{1}{2} (\bar{u} \sigma_{\mu\nu} c)(\bar{\ell} \sigma^{\mu\nu} (\gamma_5) \ell).$$

- 3 **Compute $C_i(\mu_{EW})$ to avoid large $\alpha_s(\mu_{\text{low}}) \log(\mu_{\text{low}}^2/\mu_{EW}^2)$.**

$$m_{q_{\text{light}}} = 0 + \text{GIM mechanism} \implies C_{7,9,10}^{SM}(\mu_{EW}) = 0!$$

EFT approach to charm physics (2)

- ④ RGEs to go down $\mu_{\text{low}} \approx m_c$ (2-step matching at μ_{EW} and m_b).

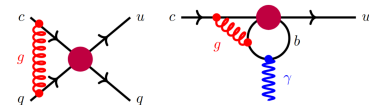
- Penguins generated at $\mu = m_b$

- $O_{7,9}$ mix with $O_{1,2}$:

$$|C_7^{\text{eff}}(\mu_c)| \lesssim 0.004 \ \& \ |C_9^{\text{eff}}(\mu_c)| \lesssim 0.01$$

- **BUT NOT** all other SM WCs:

$$C_i^{\prime \text{SM}} = C_S^{\text{SM}} = C_T^{\text{SM}} = C_{T5}^{\text{SM}} = C_{10}^{\text{SM}} = 0$$



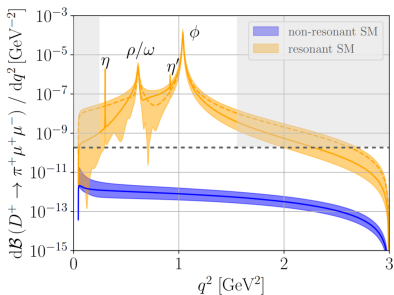
Rock stars of charm physics!

Any observable proportional to these WCs is a null test!

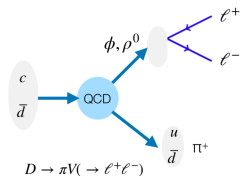
- ⑤ $\langle O_i(\mu_{\text{low}}) \rangle$ from non-perturbative techniques (Lattice, LCSR, ...)

- ⑥ **Include resonances:** Breit–Wigner distributions + **exp. data.**

Rare semileptonic charm $c \rightarrow u \ell^+ \ell^-$ decays



Dominated by resonances!



$$\mathcal{B}(D \rightarrow \pi \ell^+ \ell^-)_{\text{SM}} \approx \mathcal{B}(D \rightarrow \pi V(\rightarrow \ell^+ \ell^-))$$

- Current data still allows for large NP effects at large q^2

$$\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-) < 6.7 \cdot 10^{-8} \text{ (90\% C.L.)}$$

- Allowing to get bounds on WCs ($\mathcal{B}(D^+ \rightarrow \mu^+ \mu^-) < 2.9 \cdot 10^{-9}$ (90% C.L.))

$$|C_7| \lesssim 0.3, |C_9^{(\prime)}| \lesssim 0.9, |C_{10}^{(\prime)}| \lesssim 0.6, |C_{S,P}^{(\prime)}| \lesssim 0.06, |C_{T,T5}| \lesssim 1.6$$

- NP searches in BRs are difficult, and clearly are not the way to go!
- Can we extract something positive from BRs? **YES**, with more data model parameters (a_j, δ_j) can be constrained and the model can be improved!

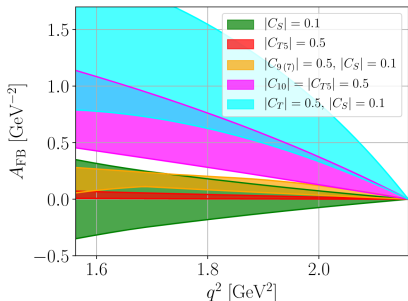
Null tests the way to go! Angular observables

- Lepton forward-backward asymmetry (**many more ...**)

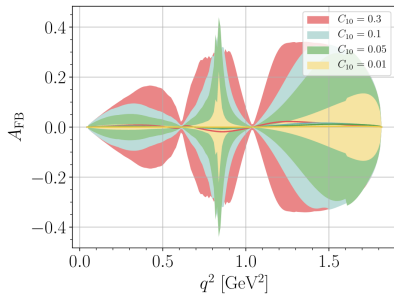
$$A_{\text{FB}}(q^2) \propto \left[\int_0^1 - \int_{-1}^0 \right] \frac{d^2\Gamma}{dq^2 d\theta_{\ell P}}$$

- Linear dependence with $C'_i, C_{S,T,T5,10} \rightarrow A_{\text{FB}}^{\text{SM}}(q^2) \approx 0$

$D_s^+ \rightarrow K^+ \mu^+ \mu^-$ (1909.11108)



$\Lambda_c \rightarrow p \mu^+ \mu^-$ (2107.13010)



Any signal is NP!

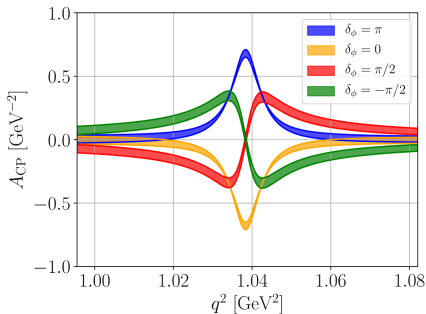
Next step, CP-asymmetries!

$$A_{CP}(q^2) \propto \frac{d\Gamma}{dq^2} - \frac{d\bar{\Gamma}}{dq^2}$$

Let's get benefit from resonances! (1208.0759)

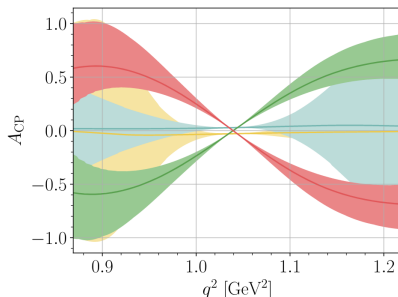
- Linear dependence with $\text{Im}[C_i^{\text{NP}}] \times \text{Im}[C_{9,\rho}^R] \rightarrow A_{CP}^{\text{SM}}(q^2) \approx 0$

$D_s^+ \rightarrow K^+ \mu^+ \mu^-$ (1909.11108)



$C_9 = 0.1 \exp(i\pi/4)$, $q^2 \in [(m_\phi - 5\Gamma_\phi)^2, (m_\phi + 5\Gamma_\phi)^2]$

$\Lambda_c \rightarrow p \mu^+ \mu^-$ (2107.13010)



$C_9 = 0.5 \exp(i\pi/4)$, $q^2 \in [(m_\phi - 5\Gamma_\phi)^2, (m_\phi + 5\Gamma_\phi)^2]$

Any signal is CP-violating NP!

LU ratios

- **LU can be probed in $c \rightarrow u \ell^+ \ell^-$ (same as B decays)**

$$R_P^D = \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(D \rightarrow P\mu^+\mu^-)}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(D \rightarrow Pe^+e^-)}{dq^2} dq^2}$$

- **Same kinematical limits \rightarrow Cancellation of had. uncertainties!**

- **Well control of SM prediction:** $R_P^D|_{\text{SM}} \approx 1$

- **e.g. $D^+ \rightarrow \pi^+ \ell^+ \ell^-$ 1909.11108, see 1805.08516 ($D \rightarrow P_1 P_2 \ell^+ \ell^-$)**
 - **full q^2 :** insensitive to NP.
 - **low q^2 :** poor knowledge of resonances \rightarrow sizable uncertainties.
 - **high q^2 :** induce significant NP effects.

	SM	$ C_9 = 0.5$	$ C_{10} = 0.5$	$ C_9 = \pm C_{10} = 0.5$	$ C_{S(P)} = 0.1$	$ C_T = 0.5$	$ C_{T5} = 0.5$
full q^2	$1.00 \pm \mathcal{O}(10^{-2})$	SM-like	SM-like	SM-like	SM-like	SM-like	SM-like
low q^2	$0.95 \pm \mathcal{O}(10^{-2})$	$\mathcal{O}(100)$	$\mathcal{O}(100)$	$\mathcal{O}(100)$	0.9...1.4	$\mathcal{O}(10)$	1.0...5.9
high q^2	$1.00 \pm \mathcal{O}(10^{-2})$	0.2...11	3...7	2...17	1...2	1...5	2...4

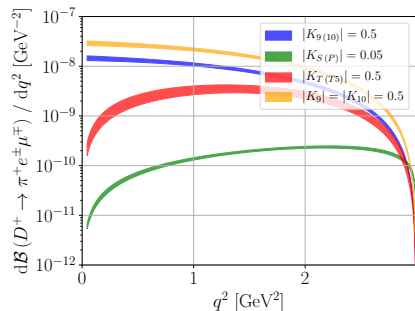
Testing LFV with $c \rightarrow u \ell^+ \ell'^-$ decays

- **Forbidden in SM! Any signal is LFV NP!**
- **Experimental limits (90% C.L.)** (2011.00217, 1107.4465)

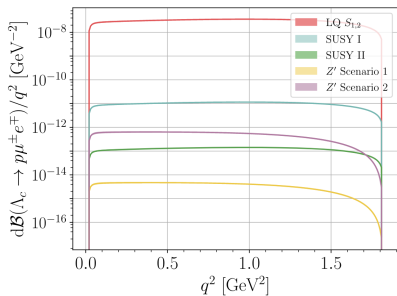
$$\mathcal{B}(D^+ \rightarrow \pi^+ e^{+(-)} \mu^{-(+)})_{\text{LHCb}} < 2.1(2.2) \cdot 10^{-7}$$

$$\mathcal{B}(\Lambda_c \rightarrow p e^{+(-)} \mu^{-(+)})_{\text{Babar}} < 9.9(19) \cdot 10^{-6}$$

1909.11108



2107.13010



Dineutrino modes $c \rightarrow u \nu \bar{\nu}$

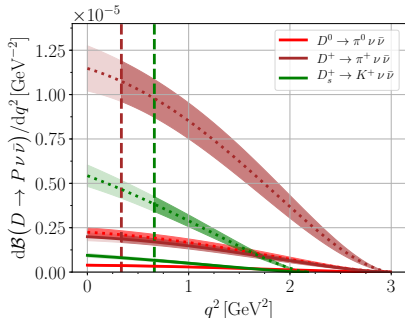
- Extremely GIM-suppressed in the SM (hep-ph/0112235, 0908.1174)

$$\mathcal{B}(D \rightarrow \pi \nu \bar{\nu})_{\text{SM}} \sim 10^{-16}!$$

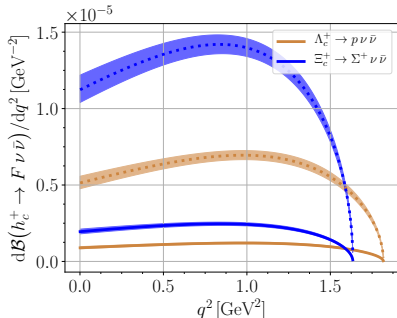
- Only experimental information on (90% C.L.) (1611.09455, 2112.14236)

$$\mathcal{B}(D^0 \rightarrow \nu \bar{\nu}) < 9.4 \cdot 10^{-5}, \quad \mathcal{B}(D^0 \rightarrow \pi^0 \nu \bar{\nu}) < 2.1 \cdot 10^{-4}$$

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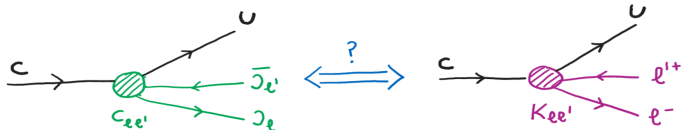


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Can we get complementary information on LFV from dineutrino modes?

ℓ and ν_ℓ (with $\ell = e, \mu, \tau$) belong to same $SU(2)_L$ doublet in the SM.



$$\begin{pmatrix} c_{ee} & c_{e\mu} & c_{e\tau} \\ c_{\mu e} & c_{\mu\mu} & c_{\mu\tau} \\ c_{\tau e} & c_{\tau\mu} & c_{\tau\tau} \end{pmatrix}$$

Neutrino flavor not tagged!

$$\mathcal{B}(c \rightarrow u \nu \bar{\nu}) = \sum_{\ell, \ell'} \mathcal{B}(c \rightarrow u \nu_\ell \bar{\nu}_{\ell'})$$

LU, cLFC or general:

$$\mathcal{B}(c \rightarrow u \nu \bar{\nu}) \sim \frac{1}{3} \sum_{\ell, \ell'} c_{\ell\ell'}$$

$$\begin{pmatrix} k_{ee} & k_{e\mu} & k_{e\tau} \\ k_{\mu e} & k_{\mu\mu} & k_{\mu\tau} \\ k_{\tau e} & k_{\tau\mu} & k_{\tau\tau} \end{pmatrix}$$

Charged leptons tagged!

LU: $R_H \sim \frac{\mathcal{B}(c \rightarrow u \mu^+ \mu^-)}{\mathcal{B}(c \rightarrow u e^+ e^-)} \sim 1 + k_{\mu\mu} - k_{ee}$

cLFC or general: $\mathcal{B}(c \rightarrow u \ell'^+ \ell^-) \sim k_{\ell\ell'}$

Is there a link between $c_{\ell\ell'}$ and $k_{\ell\ell'}$?

Low-energy $|\Delta c| = |\Delta u| = 1$ EFT description

$$\boxed{c \rightarrow u \nu_{\ell} \bar{\nu}_{\ell'}}$$

$$\longleftrightarrow ?$$

$$\boxed{c \rightarrow u \ell^{-} \ell'^{+}}$$

$$\mathcal{H}_{\text{eff}}^{\nu_{\ell} \bar{\nu}_{\ell'}} = -\frac{4 G_F}{\sqrt{2}} \frac{\alpha}{4\pi} \sum_k C_k^{U\ell\ell'} Q_k^{U\ell\ell'} \quad \mathcal{H}_{\text{eff}}^{\ell^{-} \ell'^{+}} = -\frac{4 G_F}{\sqrt{2}} \frac{\alpha}{4\pi} \sum_k \mathcal{K}_k^{U\ell\ell'} O_k^{D\ell\ell'}$$

Only two operators (no RH neutrinos like SM) Further operators non-connected

$$Q_{L(R)}^{U\ell\ell'} = (\bar{u}_{L(R)} \gamma_{\mu} c_{L(R)}) (\bar{\nu}_{\ell'} \gamma^{\mu} \nu_{\ell}) \quad O_{L(R)}^{U\ell\ell'} = (\bar{u}_{L(R)} \gamma_{\mu} c_{L(R)}) (\bar{\ell}'_L \gamma^{\mu} \ell_L)$$

...

Dineutrino BR is obtained via an incoherent neutrino flavor sum:

$$\mathcal{B}(c \rightarrow u \nu \bar{\nu}) = \sum_{\ell, \ell'} \mathcal{B}(c \rightarrow u \nu_{\ell} \bar{\nu}_{\ell'}) \sim \sum_{\ell, \ell'} \left| C_L^{U\ell\ell'} \pm C_R^{U\ell\ell'} \right|^2$$

C^P and \mathcal{K}^P in the mass basis. $P = D$ ($P = U$) \rightarrow down-quark sector (up-quark sector).

Correlate neutrinos and charged leptons with $SU(2)_L$

Lowest order $SU(2)_L \times U(1)_Y$ -invariant effective theory [1008.4884](#)

$$\mathcal{L}_{\text{SMEFT}}^{\text{LO}} \supset \frac{C_{\ell q}^{(1)}}{v^2} \bar{Q} \gamma_\mu Q \bar{L} \gamma^\mu L + \frac{C_{\ell q}^{(3)}}{v^2} \bar{Q} \gamma_\mu \tau^a Q \bar{L} \gamma^\mu \tau^a L + \frac{C_{\ell u}}{v^2} \bar{U} \gamma_\mu U \bar{L} \gamma^\mu L + \frac{C_{\ell d}}{v^2} \bar{D} \gamma_\mu D \bar{L} \gamma^\mu L$$

- ① **Writing in $SU(2)_L$ -components:** ($C \rightarrow$ dineutrinos and $K \rightarrow$ dileptons in the gauge basis)

$$C_L^U = K_L^D = \frac{2\pi}{\alpha} \left(C_{\ell q}^{(1)} + C_{\ell q}^{(3)} \right), \quad C_R^U = K_R^U = \frac{2\pi}{\alpha} C_{\ell U}.$$

② **Mass basis:** $C_L^U = W^\dagger \mathcal{K}_L^D W + \mathcal{O}(\lambda), \quad C_R^U = W^\dagger \mathcal{K}_R^U W$

- ③ **BR is independent of PMNS matrix!**

$$\begin{aligned} \mathcal{B}(c \rightarrow u \nu \bar{\nu}) &\sim \sum_{\ell, \ell'} |C_L^{U\ell\ell'} \pm C_R^{U\ell\ell'}|^2 = \text{Tr}[(C_L^U \pm C_R^U)(C_L^U \pm C_R^U)^\dagger] \\ &= \text{Tr}[W^\dagger (\mathcal{K}_L^D \pm \mathcal{K}_R^U) W W^\dagger (\mathcal{K}_L^D \pm \mathcal{K}_R^U)^\dagger W] = \sum_{\ell, \ell'} |\mathcal{K}_L^{D\ell\ell'} \pm \mathcal{K}_R^{U\ell\ell'}|^2 + \mathcal{O}(\lambda) \end{aligned}$$

Prediction of dineutrino rates for different leptonic flavor structures

$\mathcal{K}_{L,R}^{\ell\ell'}$ can be probed with lepton-specific measurements!

Possible leptonic flavor structures for $\mathcal{K}_{L,R}^{\ell\ell'}$

$$\mathcal{B}(c \rightarrow u \nu \bar{\nu}) \sim \sum_{\ell, \ell'} |\mathcal{K}_L^{D\ell\ell'} \pm \mathcal{K}_R^{U\ell\ell'}|^2$$

i) **Lepton-universality (LU).**

$$\begin{pmatrix} k & 0 & 0 \\ 0 & k & 0 \\ 0 & 0 & k \end{pmatrix}$$

ii) **Charged lepton flavor conservation (cLFC).**

$$\begin{pmatrix} k_{ee} & 0 & 0 \\ 0 & k_{\mu\mu} & 0 \\ 0 & 0 & k_{\tau\tau} \end{pmatrix}$$

iii) $\mathcal{K}_{L,R}^{\ell\ell'}$ arbitrary.

$$\begin{pmatrix} k_{ee} & k_{e\mu} & k_{e\tau} \\ k_{\mu e} & k_{\mu\mu} & k_{\mu\tau} \\ k_{\tau e} & k_{\tau\mu} & k_{\tau\tau} \end{pmatrix}$$

Dineutrino branching ratios

$$\mathcal{B} = A_+ x^+ + A_- x^-, \quad x^\pm = \sum_{\ell, \ell'} \left| c_L^{U\ell\ell'} \pm c_R^{U\ell\ell'} \right|^2$$

→ Long-distance dyn. & kinematics A_\pm : LCSR (low q^2) + Lattice (high q^2)

→ Short-distance dynamics x^\pm : WCs (BSM)

→ Excellent complementarity \mathcal{B} :

- $A_- = 0$ in $D \rightarrow P \nu \bar{\nu}$ decays.
- $A_- > A_+$ in $D \rightarrow P_1 P_2 \nu \bar{\nu}$ decays.
- $A_- = A_+$ in inclusive D decays.

$D \rightarrow F$	A_+ [10^{-8}]	A_- [10^{-8}]
$D^0 \rightarrow \pi^0$	0.9	0
$D^+ \rightarrow \pi^+$	3.6	0
$D^0 \rightarrow \pi^0 \pi^0$	0	0.2
$D^0 \rightarrow \pi^+ \pi^-$	0	0.4
$D^0 \rightarrow X$	2.2	2.2
$D^+ \rightarrow X$	5.6	5.6

Upper limits on dineutrino modes can probe LU!

- Limits from high- p_T & charged dilepton D and K-decays (†):¹

	$ \mathcal{K}_A^{P\ell\ell'} $	ee	$\mu\mu$	$\tau\tau$	$e\mu$	$e\tau$	$\mu\tau$
sd	$ \mathcal{K}_L^{D\ell\ell'} $	$5 \cdot 10^{-2\dagger}$	$1.6 \cdot 10^{-2\dagger}$	6.7	$6.6 \cdot 10^{-4\dagger}$	6.1	6.6
$c u$	$ \mathcal{K}_R^{U\ell\ell'} $	2.9	0.9^\dagger	5.6	1.6	4.7	5.1

- $x^\pm < 2x$, $x = \sum_{\ell, \ell'} (|\mathcal{K}_L^{D\ell\ell'}|^2 + |\mathcal{K}_R^{U\ell\ell'}|^2) + \mathcal{O}(\lambda) = \sum_{\ell, \ell'} R^{\ell\ell'} + \mathcal{O}(\lambda)$

$$x = 3 R^{\mu\mu} \lesssim 2.6, \quad (\text{Lepton Universality}) \text{ LU is fixed by muons.}$$

$$x = R^{ee} + R^{\mu\mu} + R^{\tau\tau} \lesssim 156, \quad (\text{charged Lepton Flavor Conservation})$$

$$x = R^{ee} + R^{\mu\mu} + R^{\tau\tau} + 2(R^{e\mu} + R^{e\tau} + R^{\mu\tau}) \lesssim 655.$$

¹2002.05684, 2003.12421 & 2007.05001 (†)

Dineutrino branching ratios upper limits

$h_c \rightarrow F$	\mathcal{B}_{LU}^{\max} [10^{-7}]	$\mathcal{B}_{cLFC}^{\max}$ [10^{-6}]	\mathcal{B}^{\max} [10^{-6}]
$D^0 \rightarrow \pi^0$	0.5	2.8	12
$D^+ \rightarrow \pi^+$	1.9	11	47
$D^0 \rightarrow \pi^0 \pi^0$	0.1	0.7	2.8
$D^0 \rightarrow \pi^+ \pi^-$	0.2	1.3	5.4
$\Lambda_c^+ \rightarrow p^+$	1.4	8.4	35
$\Xi_c^+ \rightarrow \Sigma^+$	2.7	17	70

$\mathcal{B}(D^0 \rightarrow \pi^0 \nu \bar{\nu}) < 2.1 \cdot 10^{-4}$ from BES III is about one order of magnitude away from our predictions [2112.14236](#)

Outlook

- ★ Window to explore FCNCs in the up-sector.
- ★ Unique phenomenology (strong GIM suppression).
- ★ Clean null test observables can probe NP.
- ★ Plenty of opportunities:
 - Angular observables
 - CP-asymmetries
 - LU ratios
 - LFV
 - Dineutrino modes
- ★ Well-suited for Belle II.

Thank you for your attention!

$\delta\mathcal{B}$ vs \mathcal{B} : exp. projections and theo. predictions

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