



***Measuring A_{LR} with polarization
at Belle II via $c\bar{c}$ production***

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The problem (my understanding)

$$\begin{aligned}
 A_{LR} &= \frac{\sigma(e^+e_L^- \rightarrow \bar{c}c) - \sigma(e^+e_R^- \rightarrow \bar{c}c)}{\sigma(e^+e_L^- \rightarrow \bar{c}c) + \sigma(e^+e_R^- \rightarrow \bar{c}c)} \equiv \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} \\
 &= \frac{N(\bar{c}c)_L/\mathcal{L}_L - N(\bar{c}c)_R/\mathcal{L}_R}{N(\bar{c}c)_L/\mathcal{L}_L + N(\bar{c}c)_R/\mathcal{L}_R} \\
 &\equiv \frac{N_L/\mathcal{L}_L - N_R/\mathcal{L}_R}{N_L/\mathcal{L}_L + N_R/\mathcal{L}_R}
 \end{aligned}$$

[NOTE: for $N = D^0$ decays, the fragmentation factor divides out. For N_L, N_R being the yield of a single decay mode, the efficiency divides out]

$$\Rightarrow \delta A_{LR} = \frac{2(N_L/\mathcal{L}_L)(N_R/\mathcal{L}_R)}{(N_L/\mathcal{L}_L + N_R/\mathcal{L}_R)^2} \sqrt{\left(\frac{\delta N_L}{N_L}\right)^2 + \left(\frac{\delta N_R}{N_R}\right)^2 + \left(\frac{\delta \mathcal{L}_L}{\mathcal{L}_L}\right)^2 + \left(\frac{\delta \mathcal{L}_R}{\mathcal{L}_R}\right)^2}$$

$$\approx \frac{1}{2} \sqrt{\left(\frac{\delta N_L}{N_L}\right)^2 + \left(\frac{\delta N_R}{N_R}\right)^2 + \left(\frac{\delta \mathcal{L}_L}{\mathcal{L}_L}\right)^2 + \left(\frac{\delta \mathcal{L}_R}{\mathcal{L}_R}\right)^2} \quad [\text{if } N_L/\mathcal{L}_L \approx N_R/\mathcal{L}_R]$$

$$\Rightarrow \frac{\delta A_{LR}}{A_{LR}} = \frac{2(N_L/\mathcal{L}_L)(N_R/\mathcal{L}_R)}{(N_L/\mathcal{L}_L)^2 - (N_R/\mathcal{L}_R)^2} \sqrt{\left(\frac{\delta N_L}{N_L}\right)^2 + \left(\frac{\delta N_R}{N_R}\right)^2 + \left(\frac{\delta \mathcal{L}_L}{\mathcal{L}_L}\right)^2 + \left(\frac{\delta \mathcal{L}_R}{\mathcal{L}_R}\right)^2}$$

What are these factors?

Assumptions

$$\delta A_{LR} = \frac{2(N_L/\mathcal{L}_L)(N_R/\mathcal{L}_R)}{(N_L/\mathcal{L}_L + N_R/\mathcal{L}_R)^2} \sqrt{\left(\frac{\delta N_L}{N_L}\right)^2 + \left(\frac{\delta N_R}{N_R}\right)^2 + \left(\frac{\delta \mathcal{L}_L}{\mathcal{L}_L}\right)^2 + \left(\frac{\delta \mathcal{L}_R}{\mathcal{L}_R}\right)^2}$$

Take $\mathcal{L}_L = \mathcal{L}_R = 40 \text{ ab}^{-1}$ (from p.14 of M. Roney's TAU 2021 talk, September 2021)

Note that $(\delta \mathcal{L}_L/\mathcal{L}_L) = (\delta \mathcal{L}_R/\mathcal{L}_R) \approx 1.4\%$ (Belle) or 1.1% (BaBar); Belle II would need to do much better

For negligible background, take $(\delta N_L/N_L) \approx 1/\sqrt{N_L}$, $(\delta N_R/N_R) \approx 1/\sqrt{N_R}$

But: what are N_L , N_R ?



Strategy I

- To minimize backgrounds, we need to use $D^{*+} \rightarrow D^0 \pi^+$ decays
- To maximize statistics, we need to use Cabibbo-favored (CF) D^0 decays, i.e.,

$$D^0 \rightarrow K^- \pi^+ \quad (\text{branching fraction} = 4.0 \%)$$

$$D^0 \rightarrow K^- \pi^+ \pi^0 \quad (\text{branching fraction} = 14.4 \%, \text{ but notable backgrounds due to } \pi^0)$$

$$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^- \quad (\text{branching fraction} = 8.2 \%)$$

What are the yields of these decays at Belle II?

only one charm paper published so far:

72 fb⁻¹

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Precise Measurement of the D^0 and D^+ Lifetimes at Belle II

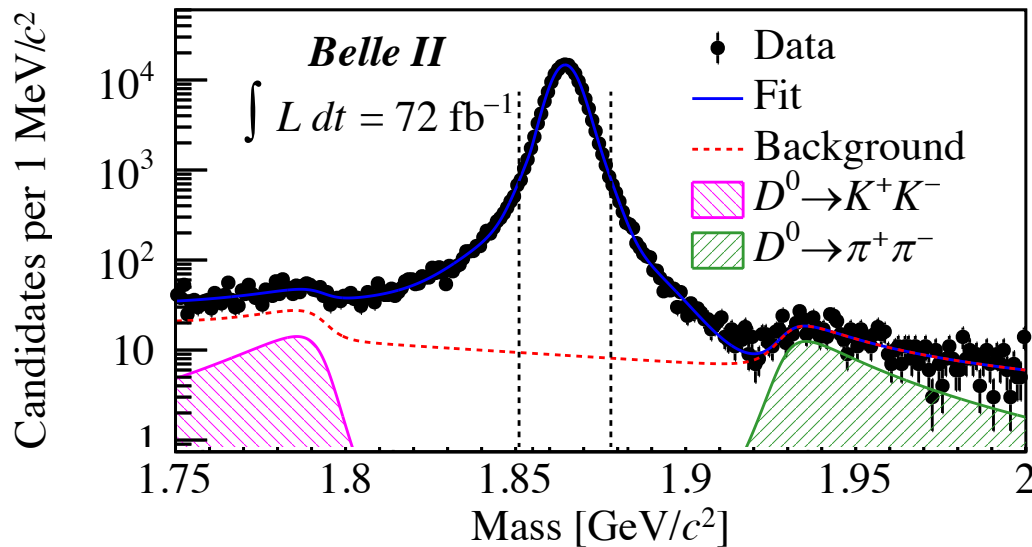
F. Abudinén,³¹ I. Adachi,^{21,18} K. Adamczyk,⁶⁶ L. Aggarwal,⁷³ H. Ahmed,⁷⁶ H. Aihara,¹¹² N. Akopov,² A. Aloisio,^{88,25} N. Anh Ky,^{40,13} D. M. Asner,³ H. Atmacan,⁹⁹ V. Aushev,⁸¹ V. Babu,¹¹ S. Bacher,⁶⁶ H. Bae,¹¹² S. Baehr,⁴⁶ S. Bahinipati,³³ P. Bambade,⁹⁵ Sw. Banerjee,¹⁰³ S. Bansal,⁷³ M. Barrett,²¹ J. Baudot,⁹⁶ M. Bauer,⁴⁶ A. Baur,¹¹ J. Becker,⁴⁶ P. K. Behera,³⁵ J. V. Bennett,¹⁰⁶ E. Bernieri,²⁹ F. U. Bernlochner,⁹⁷ M. Bertemes,³⁸ E. Bertholet,⁸⁴ M. Bessner,¹⁰¹ S. Bettarini,^{91,28} V. Bhardwaj,³² F. Bianchi,^{93,30} T. Bilka,⁷ S. Bilokin,⁵⁴ D. Biswas,¹⁰³ A. Bobrov,^{4,68} D. Bodrov,^{64,52} A. Bolz,¹¹ A. Bozek,⁶⁶ M. Bračko,^{104,80} P. Branchini,²⁹ N. Braun,⁴⁶ R. A. Briere,⁵ T. E. Browder,¹⁰¹ A. Budano,²⁹ S. Bussino,^{92,29} M. Campajola,^{88,25} L. Cao,¹¹ G. Casarosa,^{91,28} C. Cecchi,^{90,27} D. Červenkov,⁷ M.-C. Chang,¹⁵ P. Chang,⁶⁵ R. Cheaib,¹¹ V. Chekelian,⁵⁷ C. Chen,⁴² Y.-T. Chen,⁶⁵ B. G. Cheon,²⁰ K. Chilikin,⁵² K. Chirapatpimol,⁸ H.-E. Cho,²⁰ K. Cho,⁴⁸ S.-J. Cho,¹¹⁸ S.-K. Choi,¹⁹ S. Choudhury,³⁴ D. Cinabro,¹¹⁶ L. Corona,^{91,28} L. M. Cremaldi,¹⁰⁶ S. Cunliffe,¹¹ T. Czank,¹¹³ F. Dattola,¹¹ E. De La Cruz-Burelo,⁶ G. de Marino,⁹⁵ G. De Nardo,^{88,25} G. De Pietro,²⁹ R. de Sangro,²⁴ M. Destefanis,^{93,30} S. Dey,⁸⁴ A. De Yta-Hernandez,⁶ A. Di Canto,³ F. Di Capua,^{88,25} J. Dingfelder,⁹⁷ Z. Doležal,⁷ I. Domínguez Jiménez,⁸⁷ T. V. Dong,¹³ M. Dorigo,³¹ K. Dort,⁴⁵ D. Dossett,¹⁰⁵ S. Dubey,¹⁰¹ S. Duell,⁹⁷ G. Dujany,⁹⁶ P. Ecker,⁴⁶ D. Epifanov,^{4,68} T. Ferber,¹¹ D. Ferlewicz,¹⁰⁵ G. Finocchiaro,²⁴ K. Flood,¹⁰¹ A. Fodor,⁵⁸ F. Forti,^{91,28} B. G. Fulsom,⁷² A. Gabrielli,^{94,31} N. Gabyshev,^{4,68} A. Gaz,^{89,26} A. Gellrich,¹¹ G. Giakoustidis,⁹⁷ R. Giordano,^{88,25} A. Giri,³⁴ A. Glazov,¹¹ B. Gobbo,³¹ R. Godang,¹¹⁰ P. Goldenzweig,⁴⁶ B. Golob,^{102,80} W. Gradl,⁴⁴ E. Graziani,²⁹ D. Greenwald,⁸³ T. Gu,¹⁰⁸ Y. Guan,⁹⁹ K. Gudkova,^{4,68} J. Guilliams,¹⁰⁶ C. Hadjivasiliou,⁷² S. Halder,⁸² K. Hara,^{21,18} T. Hara,^{21,18} O. Hartbrich,¹⁰¹ K. Hayasaka,⁶⁷ H. Hayashii,⁶³ S. Hazra,⁸² C. Hearty,^{98,39} I. Heredia de la Cruz,^{6,10} M. Hernández Villanueva,¹¹ A. Hershenhorn,⁹⁸ T. Higuchi,¹¹³ E. C. Hill,⁹⁸ H. Hirata,⁶⁰ M. Hoek,⁴⁴ M. Hohmann,¹⁰⁵ C.-L. Hsu,¹¹¹ T. Humair,⁵⁷ T. Iijima,^{60,62} K. Inami,⁶⁰

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$$D^{*+} \rightarrow D^0 \pi^+, D^0 \rightarrow K^- \pi^+$$



From this analysis, we have:

- $\mathcal{L} = 72 \text{ fb}^{-1}$
- $N_{\text{signal}} = 171 \times 10^3$
- Purity = 0.998

\Rightarrow in 40 ab^{-1} , we would reconstruct $(171000)(40/0.072) = 95 \times 10^6$ decays

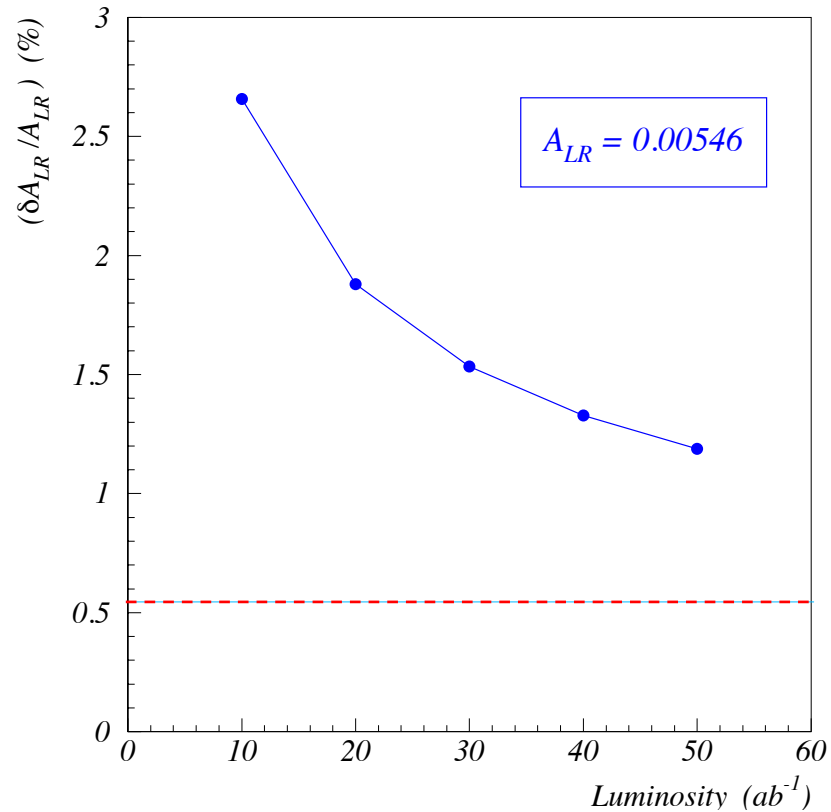
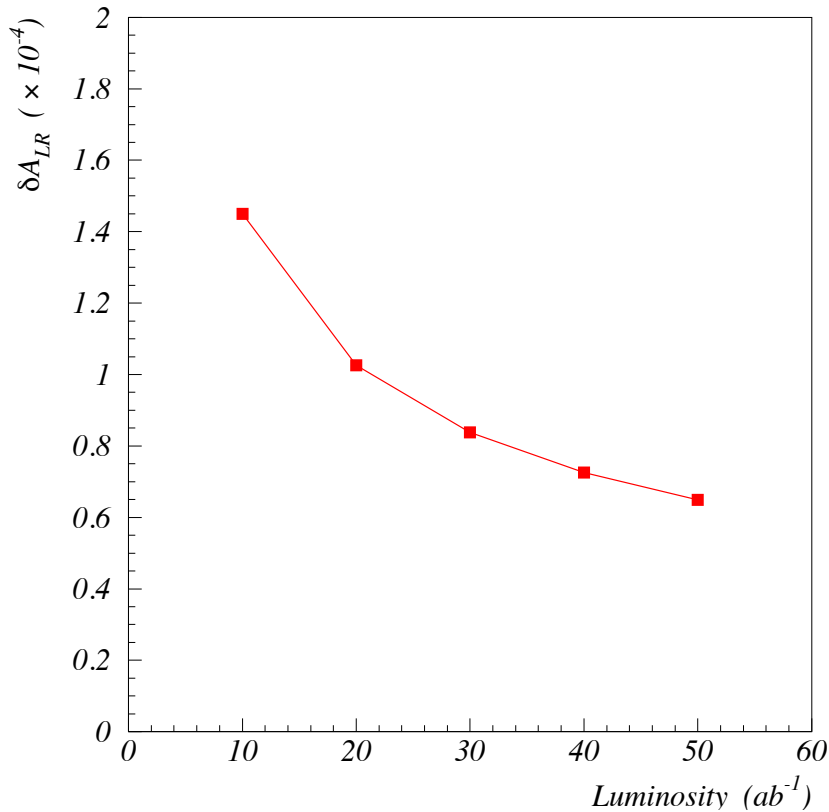
$\Rightarrow (\delta N_L / N_L) = 1.0 \times 10^{-4}$

Note that $\delta \mathcal{L} / \mathcal{L} = 0.011$ (Belle/Babar precision) would dominate

$$D^{*+} \rightarrow D^0 \pi^+, D^0 \rightarrow K^- \pi^+$$

(take to be 0 for now)

$$\delta A_{LR} = \frac{2(N_L/\mathcal{L}_L)(N_R/\mathcal{L}_R)}{(N_L/\mathcal{L}_L + N_R/\mathcal{L}_R)^2} \sqrt{\left(\frac{\delta N_L}{N_L}\right)^2 + \left(\frac{\delta N_R}{N_R}\right)^2 + \left(\frac{\delta \mathcal{L}_L}{\mathcal{L}_L}\right)^2 + \left(\frac{\delta \mathcal{L}_R}{\mathcal{L}_R}\right)^2}$$



(from p.14 of M. Roney's TAU 2021 talk)

Add another mode: $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$

Belle:

- $\mathcal{L} = 281 \text{ fb}^{-1}$
- $N_{\text{sig}} = 525900$
- Purity = very good

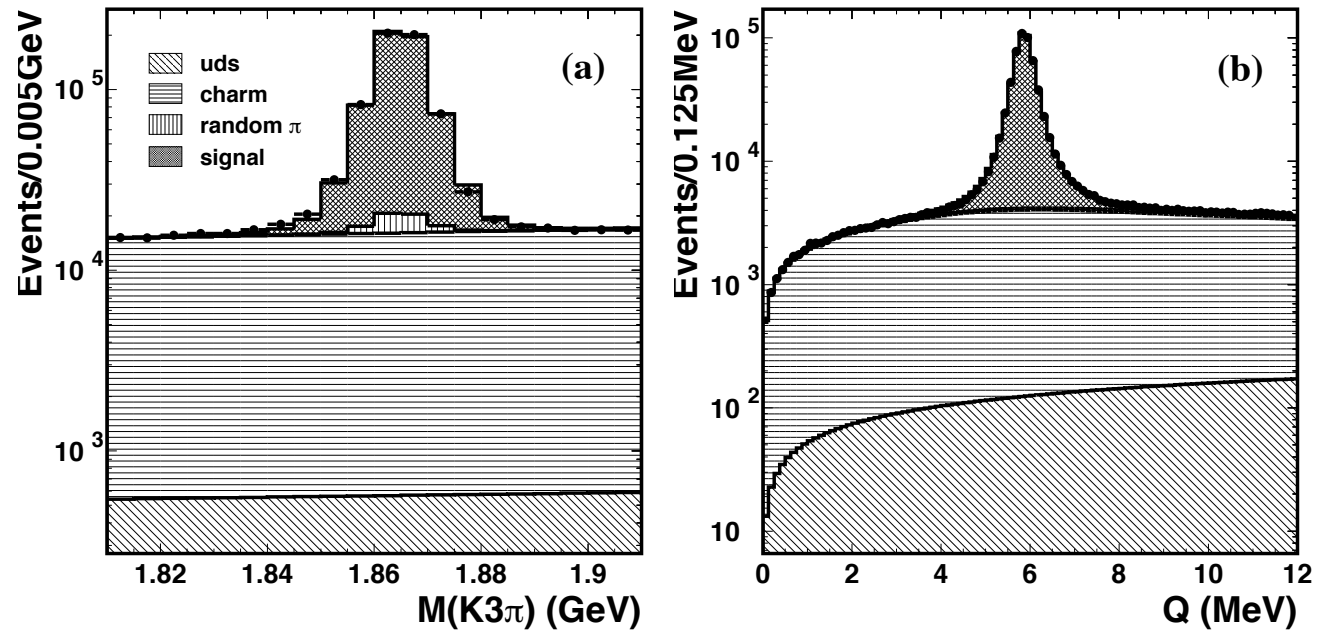
\Rightarrow in 40 ab^{-1} , we would reconstruct
 $(525900)(40/0.281) = 74.9 \times 10^6$ decays

$\Rightarrow (\delta N_L / N_L) = 1.2 \times 10^{-4}$

This would almost double the statistics

\Rightarrow reduce statistical error on δA_{LR} by $\sim 30\%$, but a systematic from the ratio of efficiencies $\varepsilon_{K\pi} / \varepsilon_{K\pi\pi\pi}$ would enter

X.C.Tian et al. (Belle), PRL 95, 231801 (2005)





Summary

- *Measurement is feasible: there will be large, ~background-free charm samples. Most promising modes are $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow K^- \pi^+$, $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$. The $K^- \pi^+$ final state is expected to provide somewhat better sensitivity.*
- *But uncertainty on integrated luminosity could dominate the measurement (?)*
- *Assuming it does not, the first charm result from Belle II indicates that the precision ($\delta A_{LR}/A_{LR}$) would be perhaps a factor of 2 worse than initial (rough) estimates*