



Measurement of D_s^+ lifetime at Belle II

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Why measure D_s^+ lifetime ?

- **What is D_s^+ lifetime ?**
 - Massive unstable particles decays to more stable particles (respecting different conservation laws), has a lifetime.
 - Lifetime depends on dominant decay modes and the underlying interaction.
 - D_s^+ lifetime world average value is $(5.04 \pm 0.04) \times 10^{-13} \text{ s}$ [PDG 2022]
- **Why measure D_s^+ lifetime ?**
 - Using fraction of current Belle II data, we can achieve world's best precision.
 - Will add one more measurement to the list of charm lifetime measurements from Belle II.
 - A precision measurement of D_s^+ lifetime adds to the demonstration of:
 - Good Belle II detector performance
 - Excellent vertexing capabilities.

Proper decay time t :

• Proper decay time: $t = \frac{(\Delta\vec{r} \cdot \hat{p})}{(|\vec{p}|/m)c}$

distance
velocity

- $\Delta\vec{r}$ is vector from D_s^+ production point (IP) to the decay vertex.
- \vec{p} is the reconstructed D_s^+ momentum vector.
- m is the D_s^+ invariant mass.
- D_s^+ production vertex is constrained at IP (only considering D_s^+ from $e^+e^- \rightarrow c\bar{c}$)

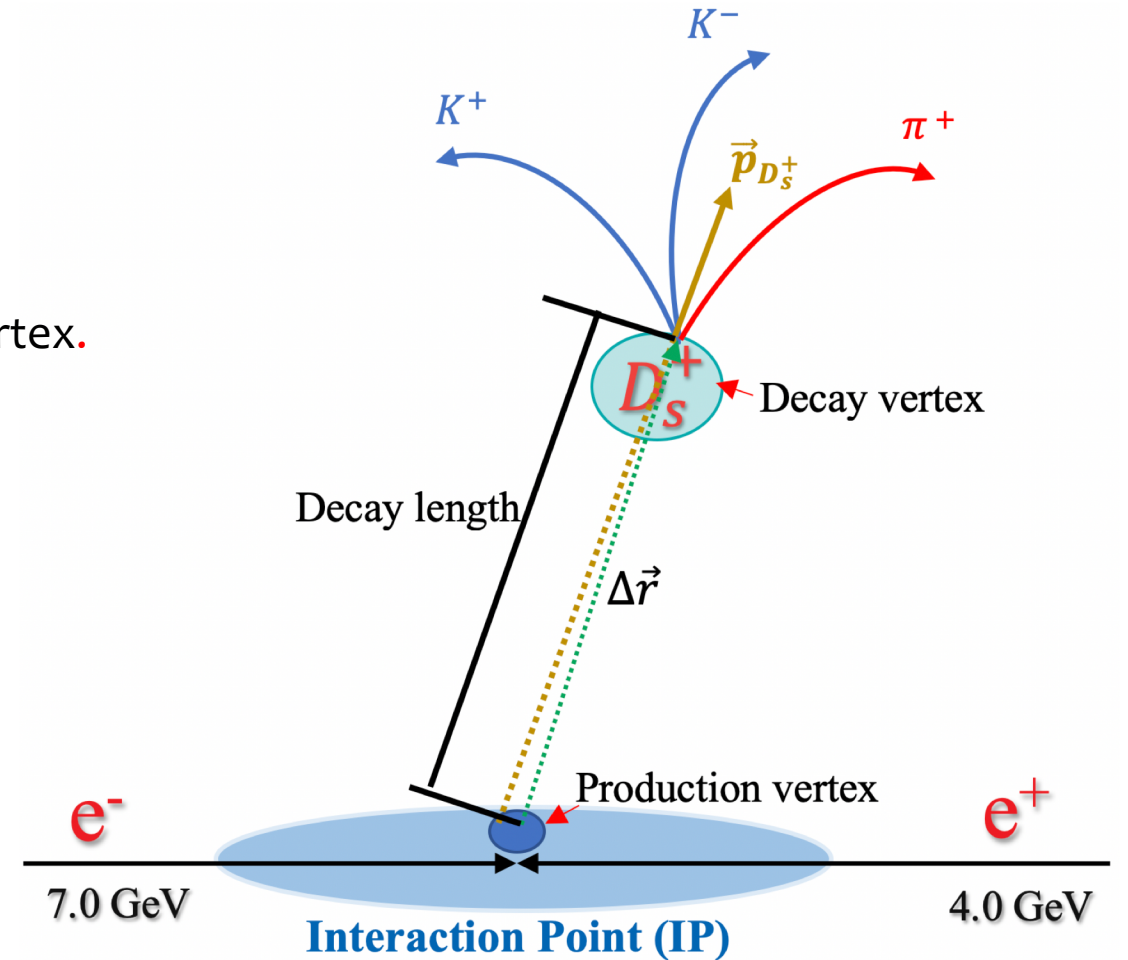


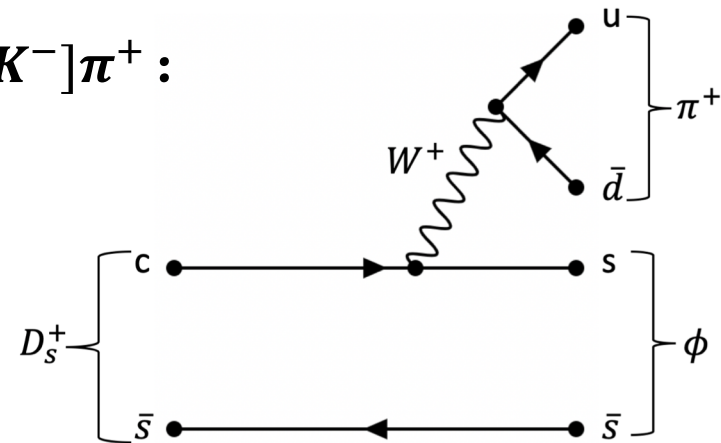
Fig. not to scale

Choice of decay mode for the D_s^+ lifetime measurement?

- We have to pick a D_s^+ decay mode with:
 - Large branching fraction. (*higher statistics for precision measurement*)
 - All charged tracks in the final state. (*very good momentum resolution and decay vertex reconstruction is crucial for lifetime precision*)
 - High sample purity i.e. ratio of signal with signal plus background.

• For lifetime measurement we chose decay mode: $D_s^+ \rightarrow \phi [K^+ K^-] \pi^+$:

- Large branching fraction : $2.24 \pm 0.08 \%$ [PDG 2021]
- Three charged tracks, $K^+ K^-$ and π^+ in the final state.
- High sample purity of $\sim 94 \%$ in the signal region.



Data and MC sample used for measurement:

- **MC sample:**
 - Run independent MC sample
 - MC 14ri_d (200 fb⁻¹)
 - Processed 3 independent 200 fb⁻¹ samples for MC studies (*always a good idea to have different independent MC samples to separate statistical and systematic effects*)
- **Data:**
 - All data until Exp. 18 bucket 25
 - **Total: ~ 207 fb⁻¹**

Check out for latest data production updates:



<https://confluence.desy.de/display/BI/Data+Production+Status>

Reconstruction of $D_s^+ \rightarrow \phi [K^+ K^-] \pi^+$

Variable	Selection criterion
Charged tracks	
dr	$ dr < 0.5 \text{ cm}$ } $ dz < 2.0 \text{ cm}$ } Selecting tracks originating near IP
dz	
#PXD hits	≥ 1 } ≥ 4 } ≥ 30 } Selecting tracks with momentum measured with better precision. Identification of charged tracks as pion or kaon.
# SVD hits	
# CDC hits	
PID (binary, $\frac{L_K}{L_K + L_\pi}$)	> 0.6 for K and < 0.55 for π }
Vertex chi prob	> 0.001 (Tree fitter, beam spot constraint) }
Helicity	$ \cos(\theta_{hel}) > 0.45$ }
$P_{D_s^+}^*$	$> 2.5 \text{ GeV}/c$ (remove D_s^+ from B decays)
M_ϕ	$(1.01 < M_\phi < 1.03) \text{ GeV}/c^2$
$M_{D_s^+}$	$(1.922 < M_{D_s^+} < 2.02) \text{ GeV}/c^2$

- Beam spot constraint requires D_s^+ to originate from IP.
- This improves the *decay time resolution* by a factor of 3

To suppress the background

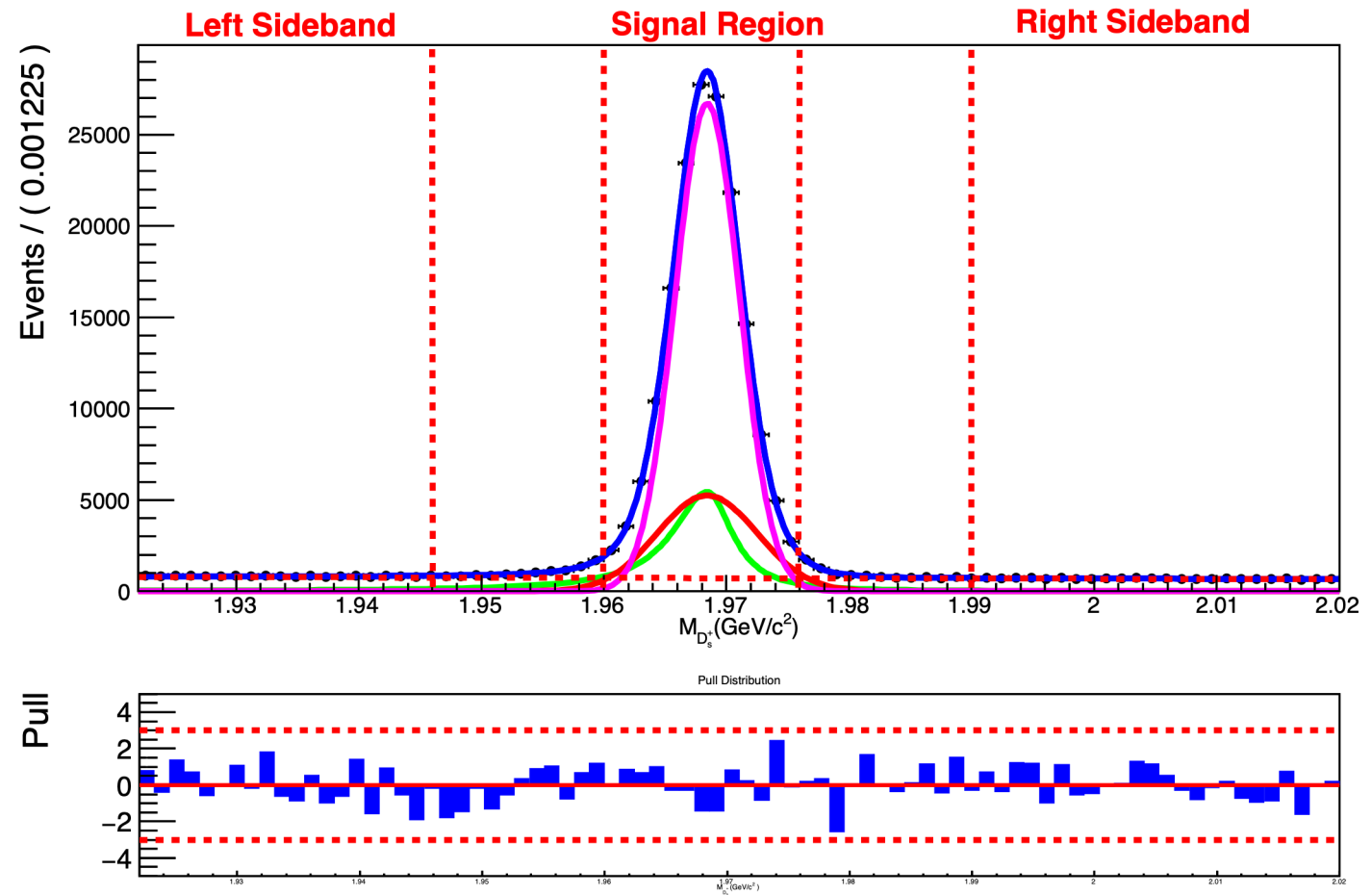
B mesons have a finite lifetime

Results from MC studies

- 200 fb⁻¹ run independent MC sample is used for results in following slides.

D_s^+ mass distributions after reconstruction:

- We fit for lifetime in a Signal region (SR) of (1.96, 1.976) GeV/c^2
- To study the background we use left and right sidebands
- For 200 fb^{-1} MC sample we have **$\sim 160\text{k}$ D_s^+ decays in the SR**
- **Sample purity $[S/(S + B)] = \sim 94.3\%$ in the SR** where S and B are the number of signal and background events in the signal region



Lifetime PDF:

- **Signal Events:** Real D_s^+ decays to $K^+ K^- \pi^+$ final state:
 - Probability of an event to decay at time t :

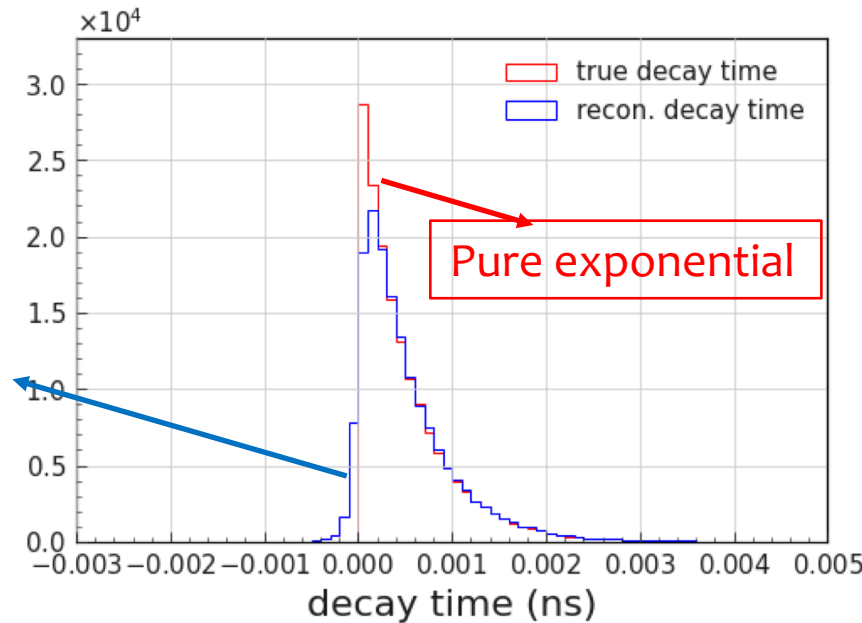
$$F_{\text{sig}}(t) = \int \frac{1}{\tau} \exp\left(\frac{-t'}{\tau}\right) R(t - t' : \text{mean}, s, \sigma_t^i) dt'$$

Convolution of natural decay law and experimental resolution function

Natural decay law
No experimental effects

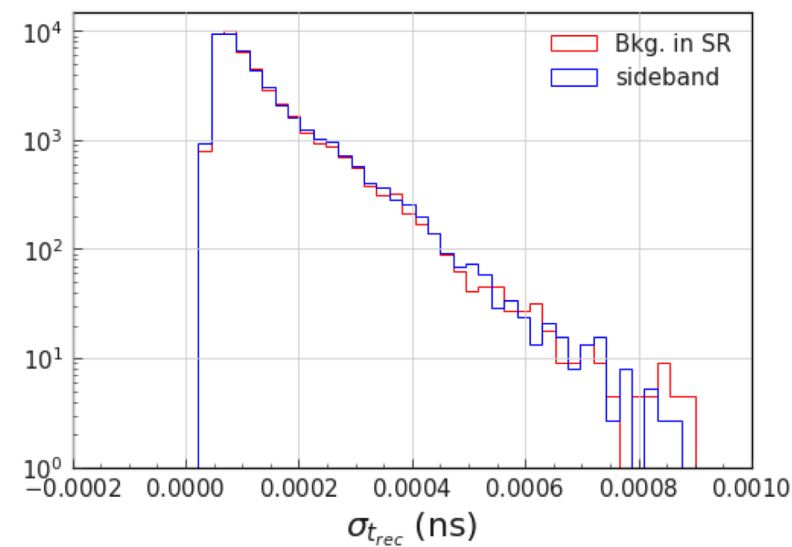
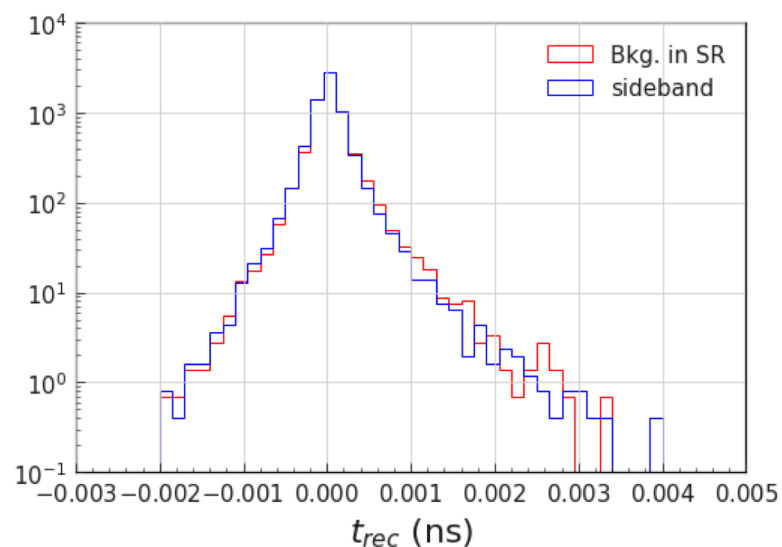
Detector resolution effect

- **Event level resolution function:** $R(t - t' : \text{mean}, s, \sigma_t^i)$
 - A single gaussian is used as resolution function.
 - Resolution function has different width for each event.
 - We use the σ_t^i , error in decay time t for event i as the width of resolution function for that event.
 - σ_t^i could be “over” or “under” estimated.
 - To correct for that, we use a **scaling factor** s common for all events.



Lifetime pdf:

- **Background Events:** non D_s decays, majority random combination of final state particles:
 - Distribution of decay time t for background events, $F_{\text{bkg}}(t)$ is modelled using sum of 3 asymmetric gaussian with common mean.
 - $F_{\text{bkg}}(t)$ is obtained using events in $M_{D_s^+}$ sidebands.
 - We fit for background events in signal region using pdf shape obtained from sideband events assuming the distribution are same. (*assumption verified in MC using truth matching*)



Lifetime pdf:

- Total decay time t pdf:

- We use a 2d pdf, $f(t, \sigma_t)$ in fit variables: decay time (t), error in decay time (σ_t) *

- $f(t, \sigma_t, M_{D_s^+}) = f_{\text{sig}} \times F_{\text{sig}}(\sigma_t) \times F_{\text{sig}}(t) + (1 - f_{\text{sig}}) \times F_{\text{bkg}}(\sigma_t) \times F_{\text{bkg}}(t)$

- Ratio of # signal with # signal plus background.
- Obtained using 1d $M_{D_s^+}$ fit (**fixed**)

- Model decay time t for signal events
- $F_{\text{sig}}(\sigma_t)$: background subtracted histogram PDF

- **Fixed** from results of 1d $M_{D_s^+}$ fit.

- Model decay time t for background events.
- $F_{\text{bkg}}(\sigma_t)$: histogram PDF
- **Fixed** to shapes obtained using sideband events.

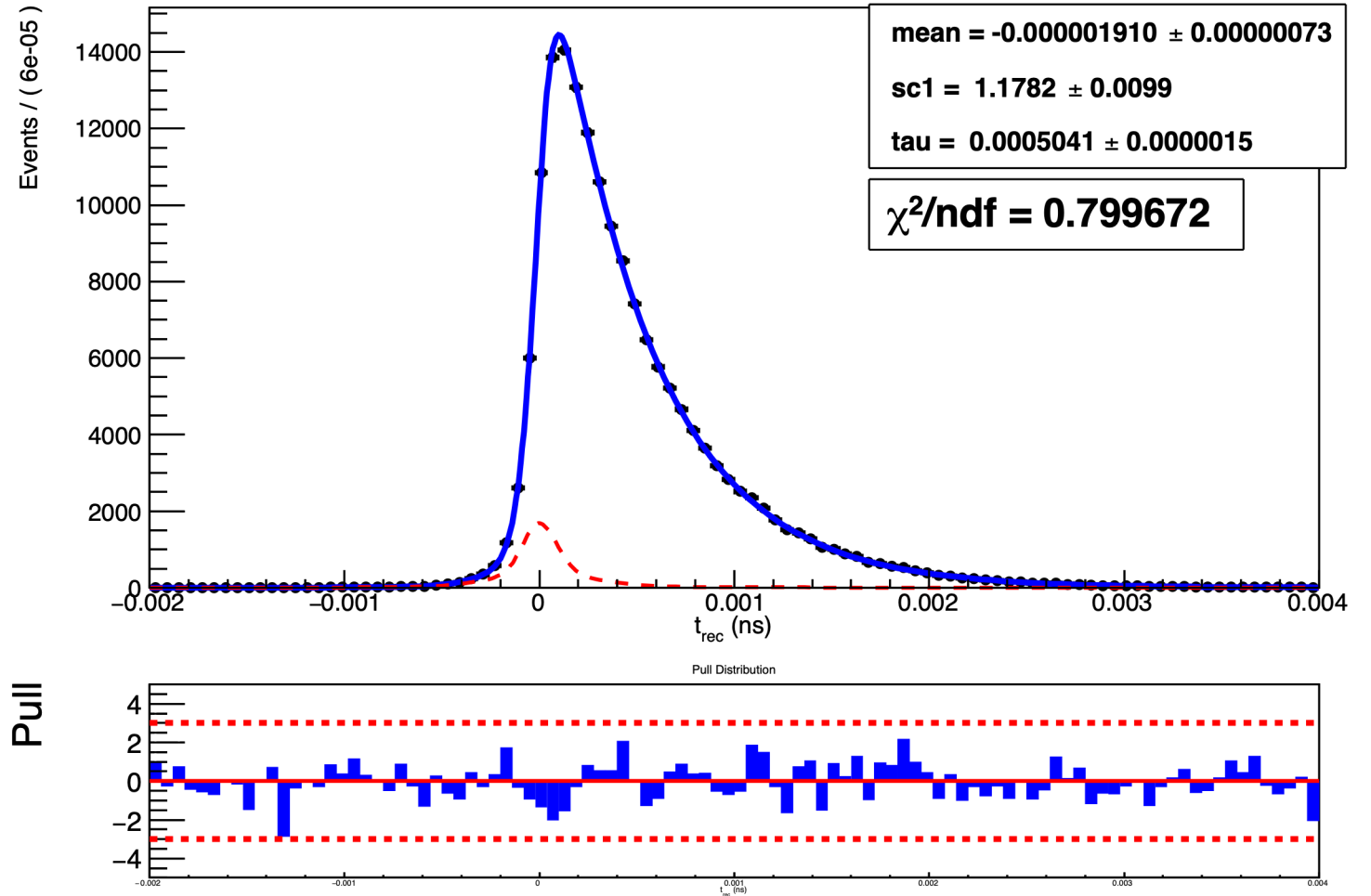
- **For fit to data, no input (pdf shape parameters) are used from simulation.**

* Previously used 3d fit in $t, \sigma_t, .$ Found bias in lifetime due to mass PDF

Final fit results (MC):

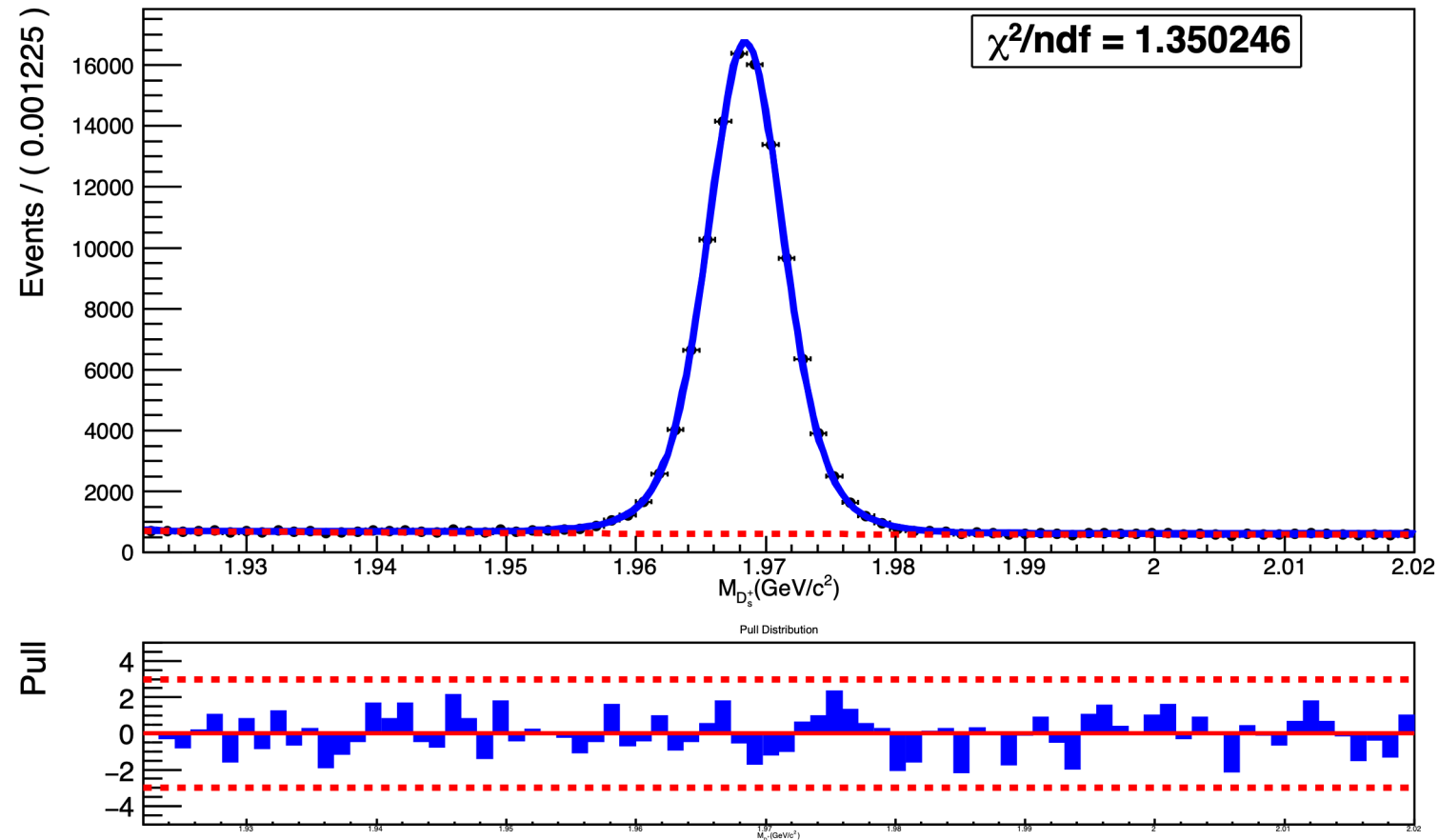
Results from 200 fb^{-1} MC sample:

- Lifetime value from fit is:
 - $\tau = (504.10 \pm 1.47) fs$
- Result consistent with lifetime value used in Belle II simulation $\tau = 504.00 fs$
- Lifetime measured on other independent MC stream $505.22 \pm 1.47 fs$ (also consistent within 1 sigma)



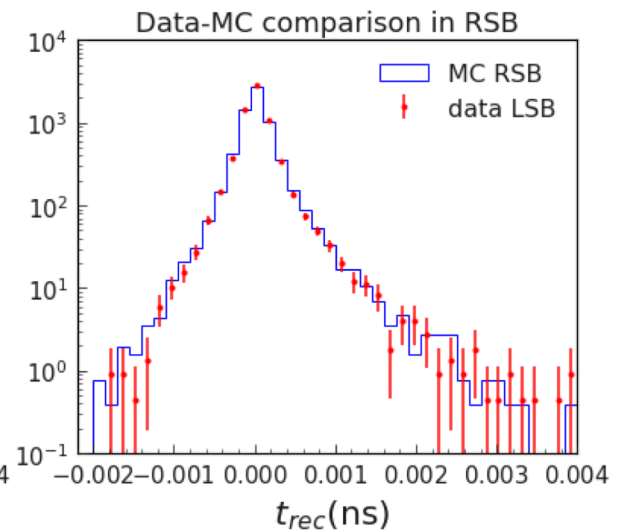
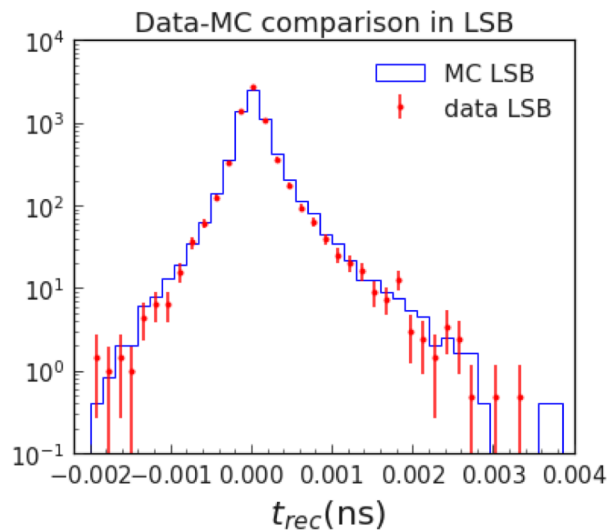
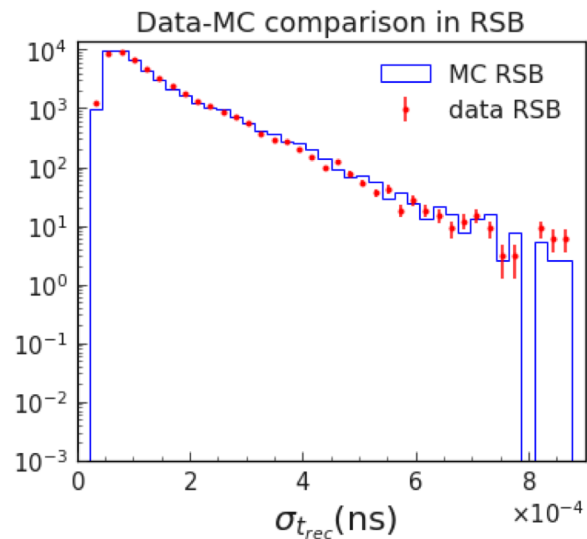
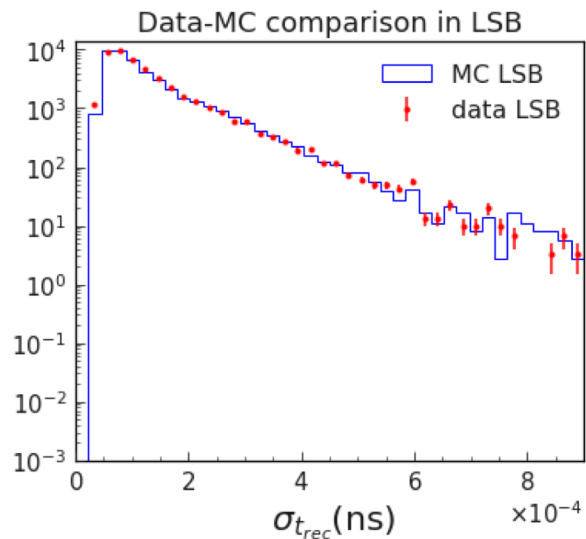
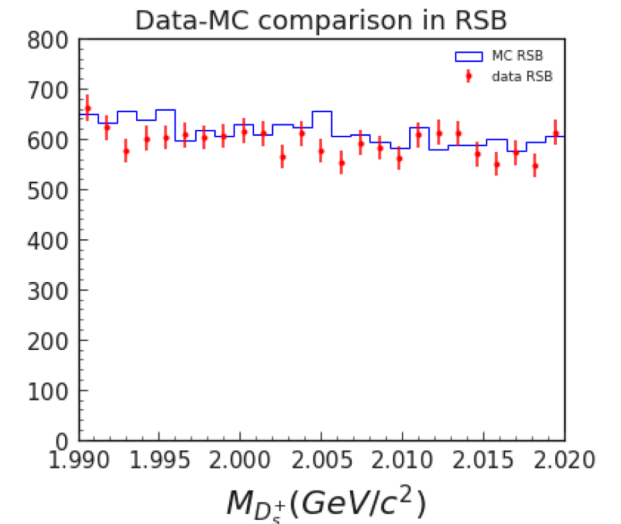
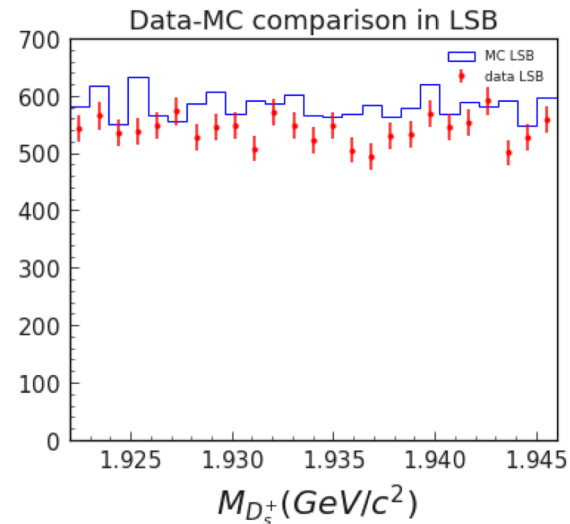
D_s^+ mass fit in data:

- The plot on right shows D_s^+ mass fit on data sample using same functional form as used for MC
- **Purity of data = 92.61 %**
 - Lower compared to MC (94.3%)
 - $N_{\text{sig}}(\text{data})/N_{\text{sig}}(\text{MC}) \sim 70\%$
 - $N_{\text{bkg}}(\text{data})/N_{\text{bkg}}(\text{MC}) \sim 95\%$



Comparing data-MC sidebands (t, σ_t)

- MC is scaled to match data luminosity.
- In the sideband, the data-MC shapes are consistent for $(M_{D_s^+}, t, \sigma_t)$



Summary:

- Presented a basic overview of D_s^+ lifetime measurement using $\sim 207 \text{ fb}^{-1}$ Belle II data.
- Discussion is applicable in general to other lifetime measurements as well
- If interested in lifetime measurements, check Belle II notes for recent charm lifetime results ($\Lambda_c, \Omega_c, D^0, D^+$)
- Lifetime measurement results obtained using MC sample:
 - Results from MC sample I : $\tau = (504.10 \pm 1.47) \text{ fs}$
 - Results from MC sample II: $\tau = (505.22 \pm 1.47) \text{ fs}$
 - Both are consistent with generated MC value of 504.00 fs.
- Looked at data (lifetime blinded)
 - Fit the D_s^+ mass distribution in data
 - The t, σ_t shapes in sideband are consistent between data and MC
- Analysis got delayed due to commitments to Belle analysis
- Plan to release first draft of Belle II note soon.

Backup

Selection variables:

Cut on helicity angle:

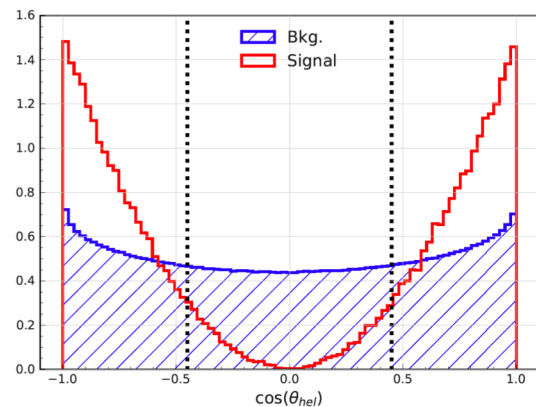
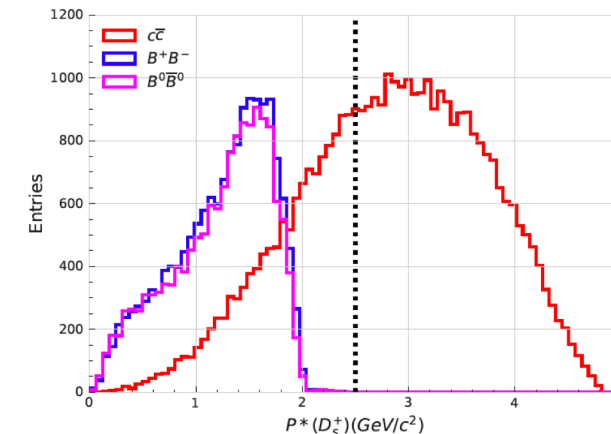
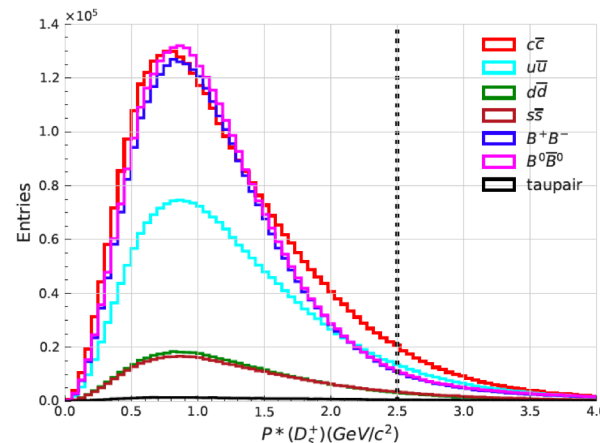


FIG. 6: Distribution of $\cos(\theta_{hel})$ for truth matched signal (red) and background (blue) events. To suppress the maximum amount of background and retain maximum amount of signal we require $|\cos(\theta_{hel})| > 0.45$

Cut on D_s^+ momentum in e^+e^- COM frame:



(a) $P_{D_s^+}^*$ distribution for truth matched background events (b) $P_{D_s^+}^*$ distribution for truth matched signal events

FIG. 5: $P_{D_s^+}^*$ distribution for truth matched signal (5a) and background events (5b) from different production type. We require $P_{D_s^+}^* > 2.5$ to get rid of D_s^+ coming from B meson decays.