

Data Preservation:

$B \rightarrow X_u \ell \nu$ Differential Branching Fractions

Lu Cao

Belle II Data Preservation Workshop, 7 Oct 2022

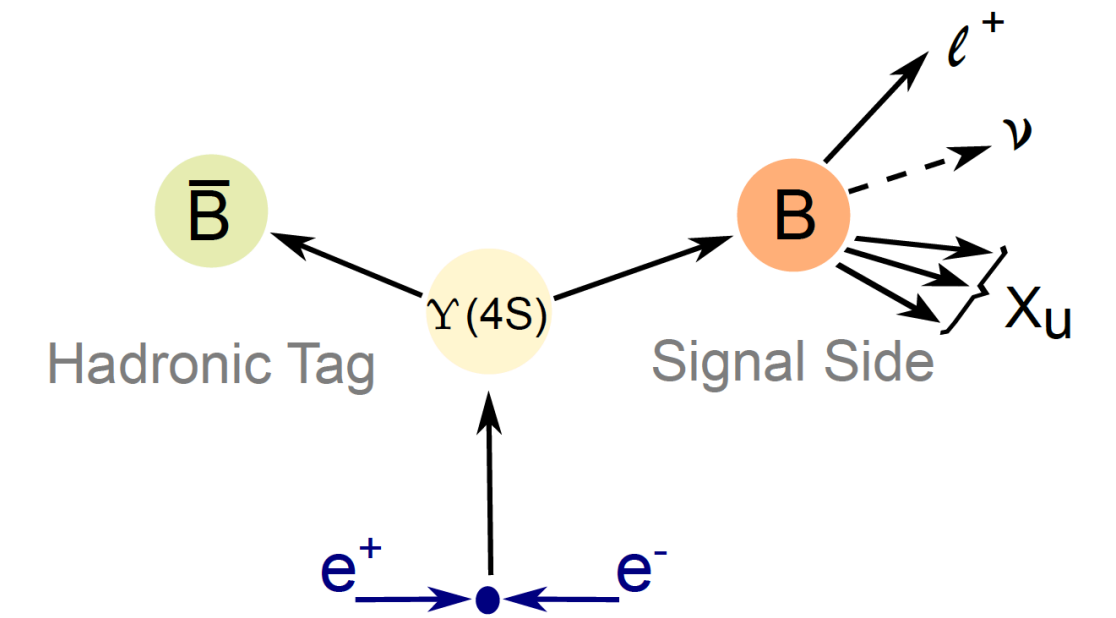


Measurement of Differential Branching Fractions of Inclusive $B \rightarrow X_u \ell \nu$ Decays

Belle: Phys. Rev. Lett. 127 (2021) 26, 261801

- Using **full Belle** dataset of **711 fb⁻¹**
- **Hadronic tagging** with Neural Networks ($\sim 0.2\text{-}0.3\%$ efficiency)
- Based on **machine learning (BDT)** to suppress backgrounds with 11 training features, e.g. $MM^2, \#K^\pm, \#K_S$.
- Measure differential spectra of 6 kinematic variables in the phase space of $E_{|B} > 1$ GeV:

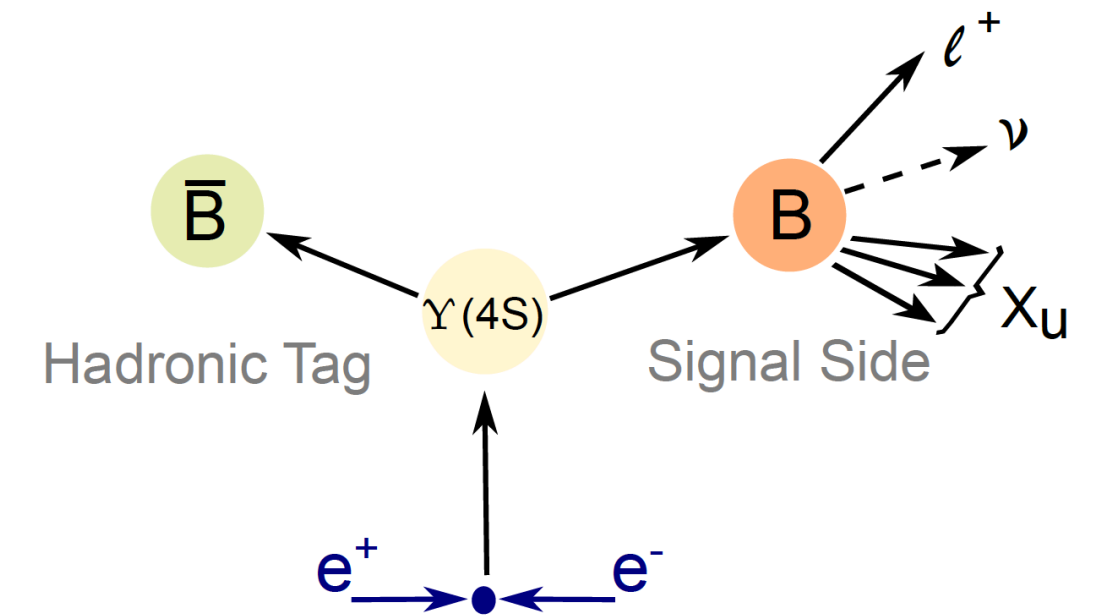
$q^2, E_{|B}, M_X, M_X^2, P_+, P_-$ (light-cone momenta: $P_\pm = E_X \mp |p_X|$)



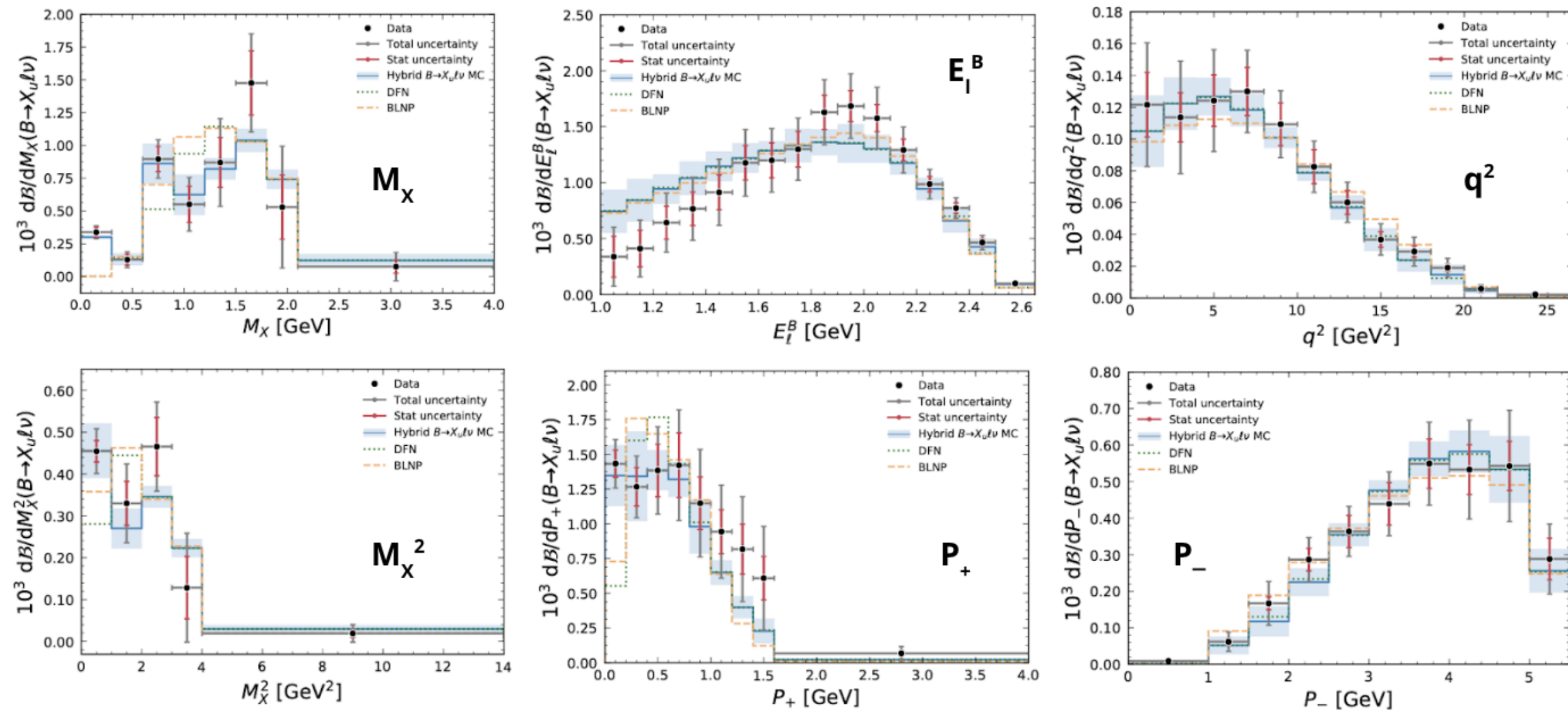
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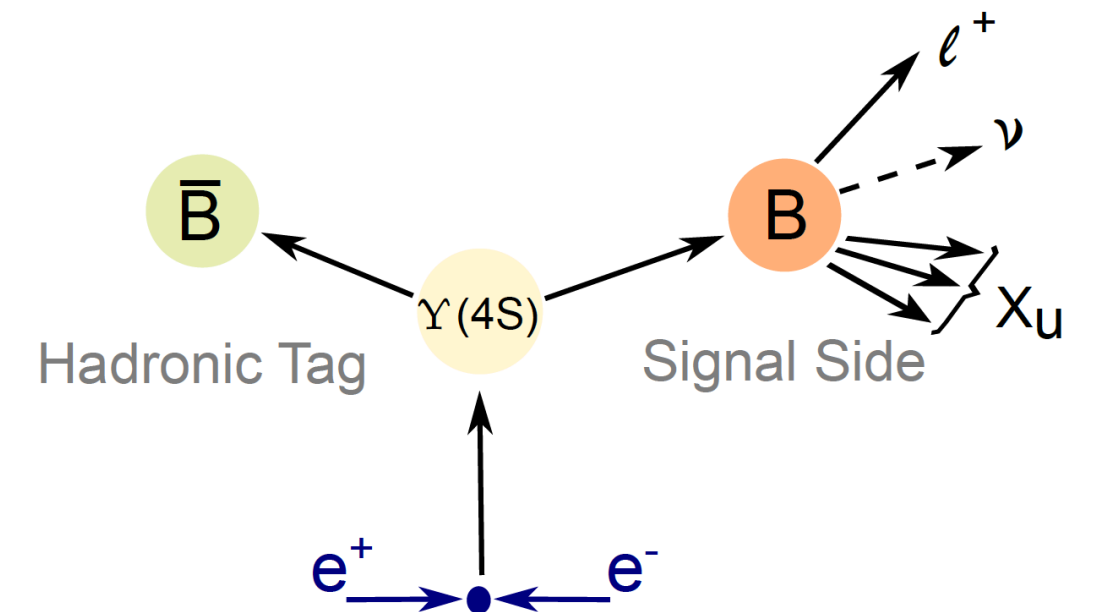


All MC shapes are normalised to 1.59×10^{-3} [Belle, PRD 104, 012008 (2021)]

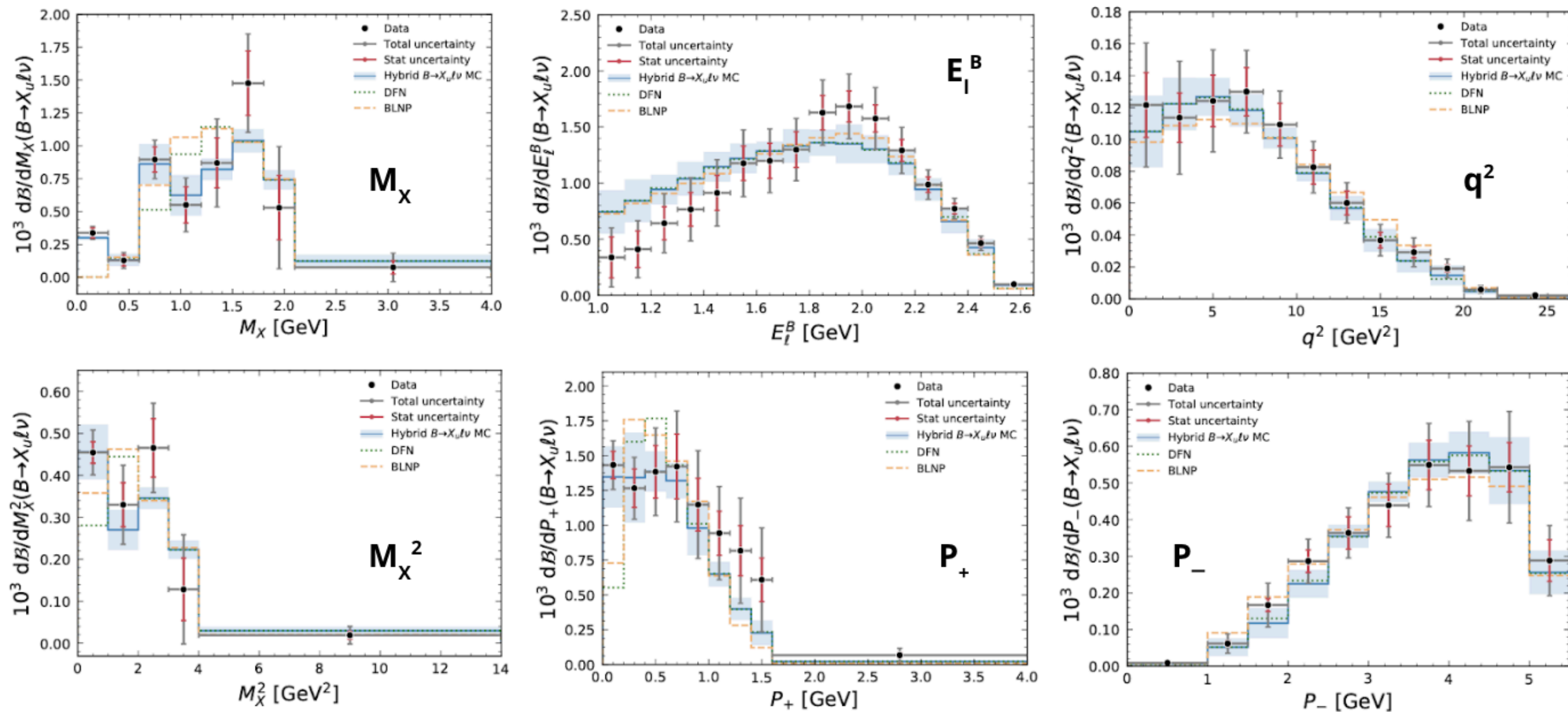
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+ 16 pages supplement and 50 tables on HepData

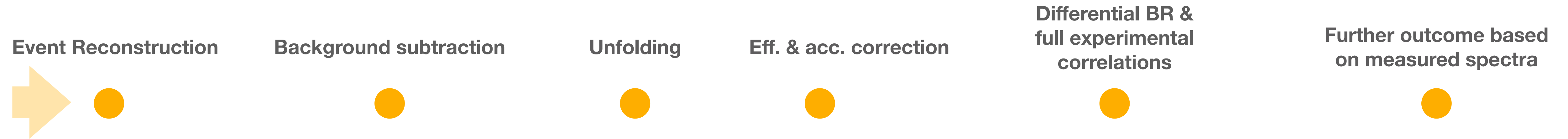
SUPPLEMENT TO THE PUBLICATION: MEASUREMENT OF DIFFERENTIAL BRANCHING FRACTIONS OF INCLUSIVE $B \rightarrow X_u \ell^+ \nu_\ell$ DECAYS

HEPDATA and Forward-Folding

The results will be made fully available in HEPData (<https://www.hepdata.net>), including the background-subtracted yields, migration matrices, and efficiency curves. This will allow interested parties to also forward-fold $B \rightarrow X_u \ell^+ \nu_\ell$ theory predictions and directly compare such with the background-subtracted Belle data. In addition, the first to third moments of each differential spectrum are provided.

Analysis Workflow

Brief Recap



Shortly on analysis details, focus on **which** data is preserved and **why**

Analysis Workflow

Brief Recap

Event Reconstruction

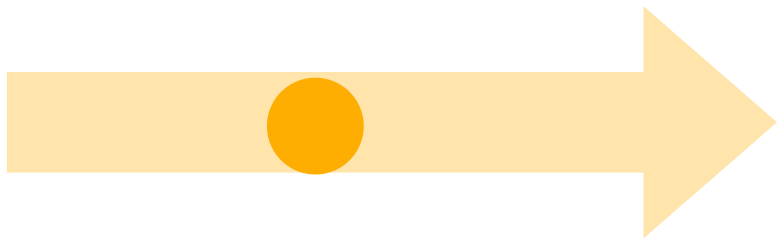
Background subtraction

Unfolding

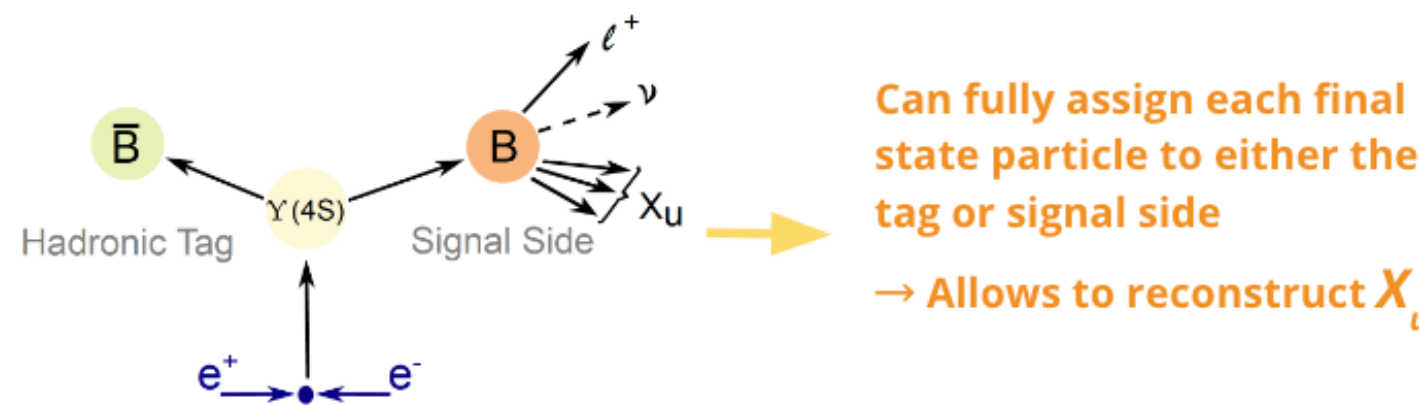
Eff. & acc. correction

Differential BR & full experimental correlations

Further outcome based on measured spectra



- Reconstruct $B \rightarrow X\ell\nu$ decays and key kin. variables
- Apply all necessary selections to enhance signal significance (e.g. BDT score)
- Strategy inherited from the partial BR measurement [Belle: *Phys. Rev. D* 104 (2021) 1, 012008]



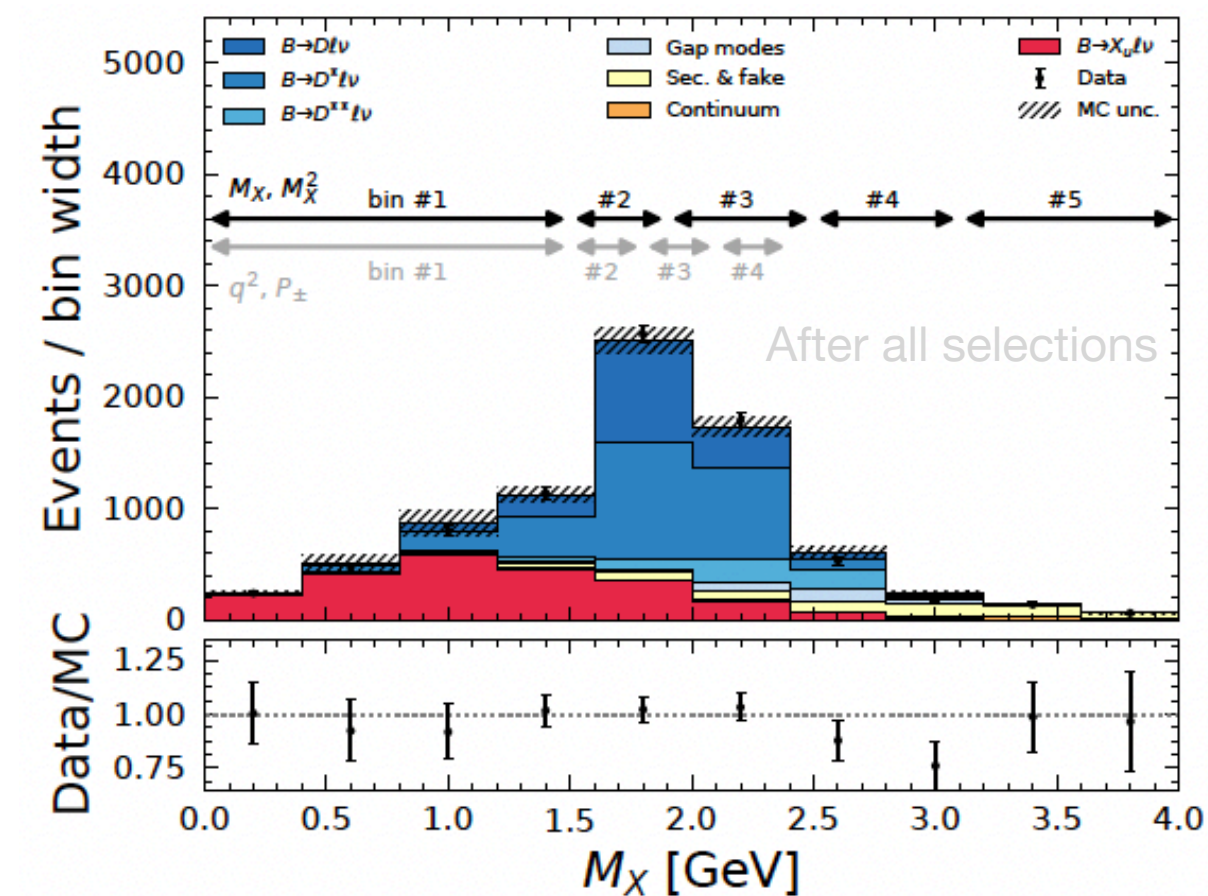
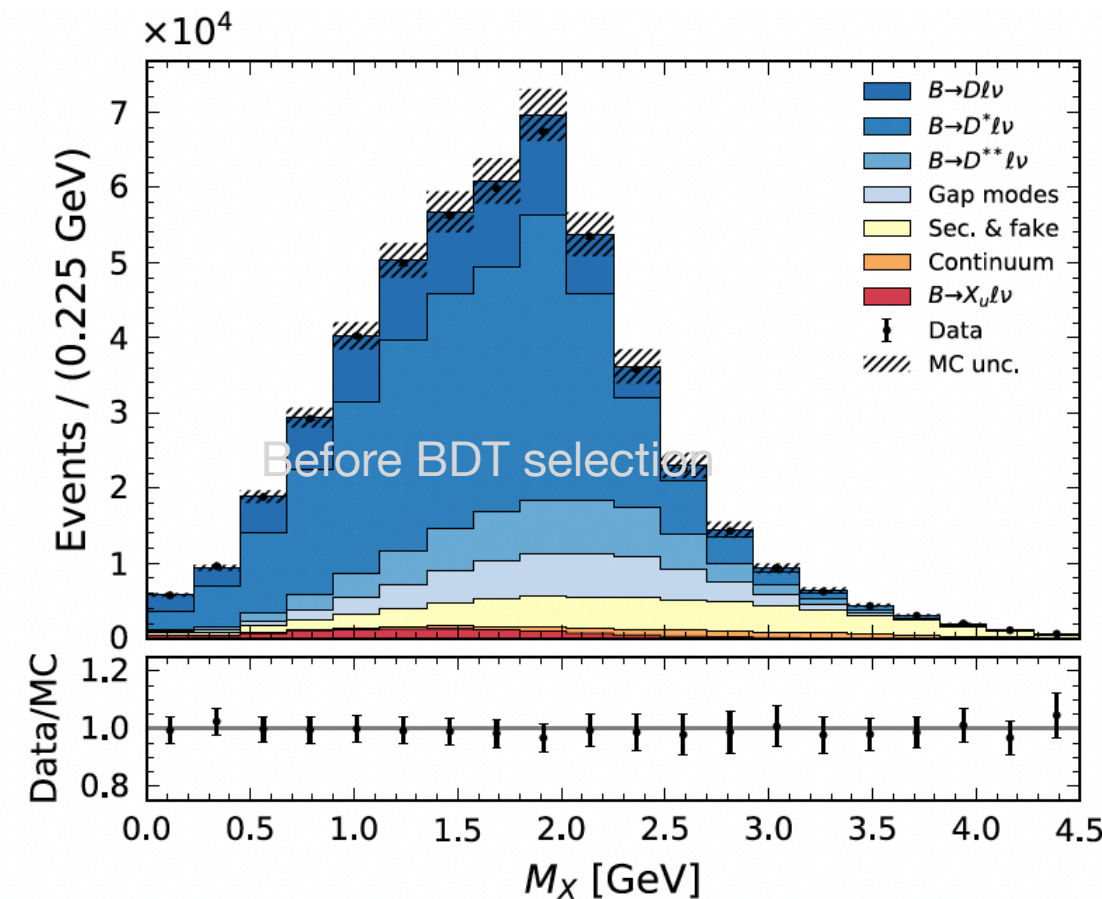
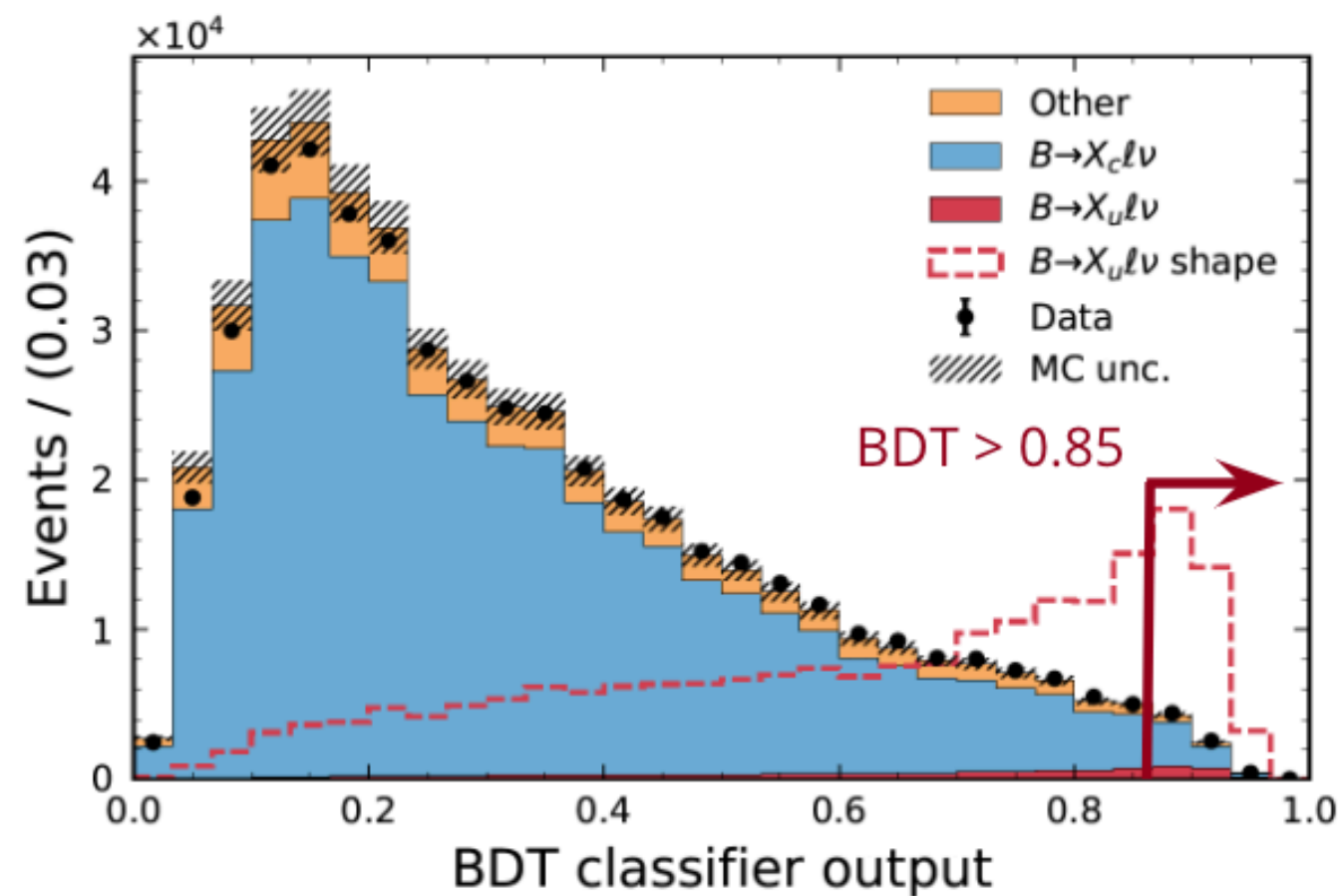
Reconstructed kinematic variables

- Hadronic system X:

$$p_X = \sum_i (\sqrt{m_\pi^2 + |\mathbf{p}_i|^2}, \mathbf{p}_i) + \sum_i (E_i, \mathbf{k}_i)$$
- Missing mass squared:

$$MM^2 = (P_{Y(4S)} - P_{\text{tag}} - P_X - P_\ell)^2$$
- Leptonic system:

$$q^2 = (P_B - P_X)^2 = (P_\ell + P_\nu)^2$$



Analysis Workflow

Brief Recap

Event Reconstruction

Background subtraction

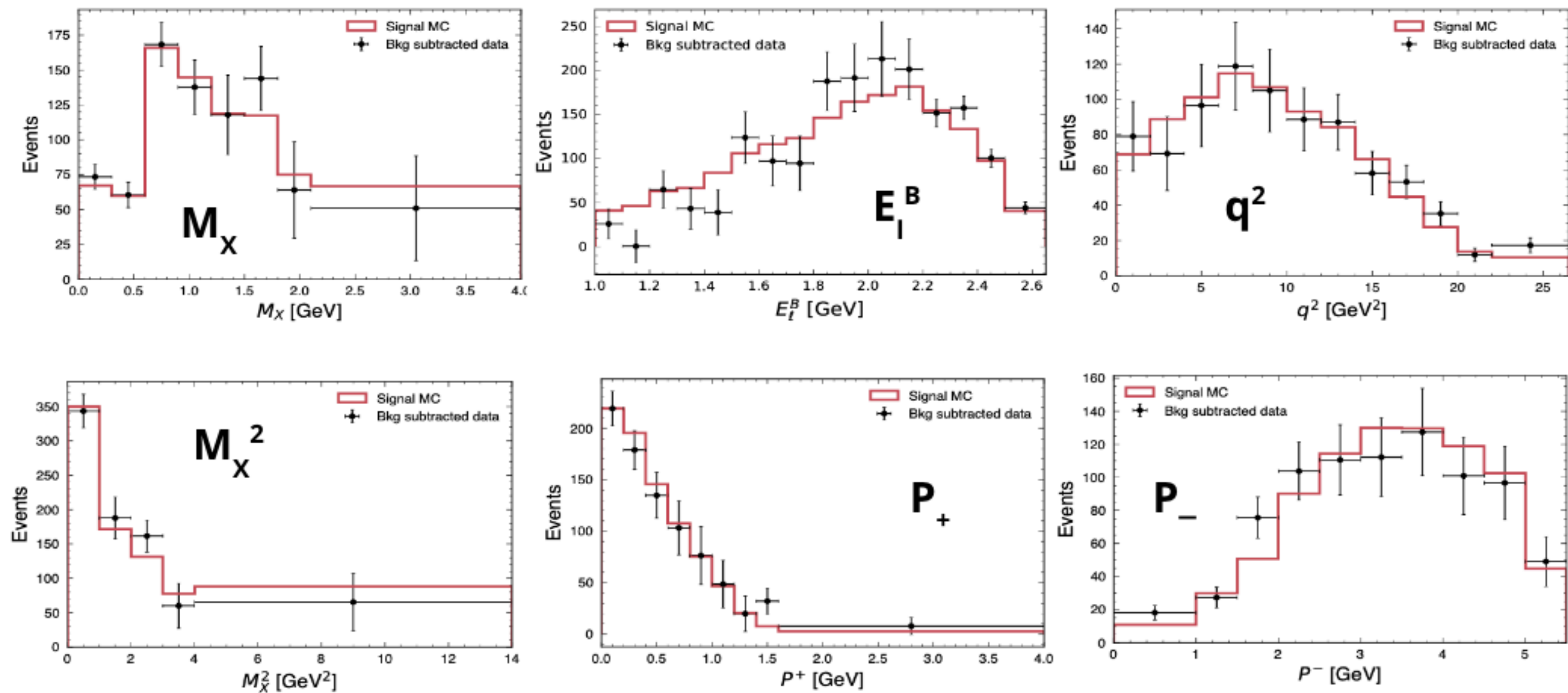
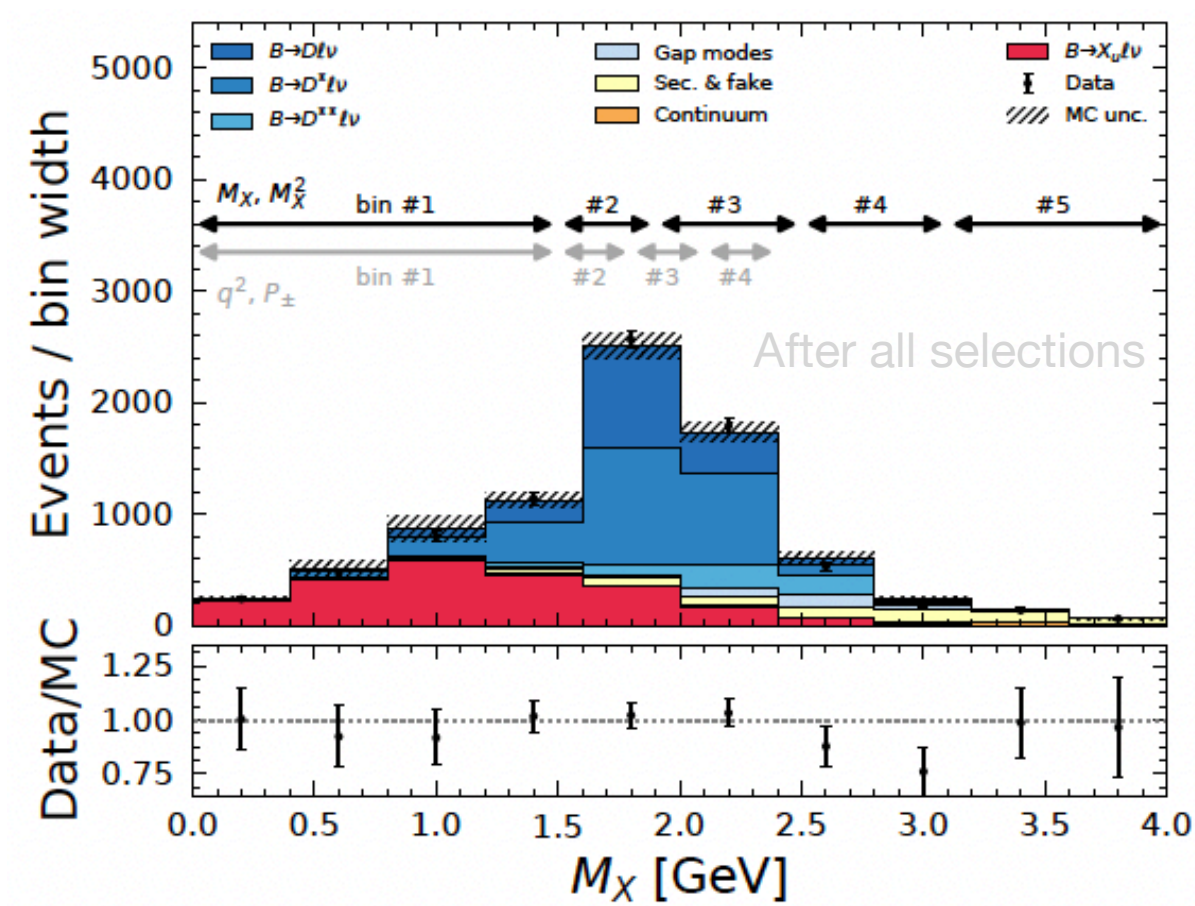
Unfolding

Eff. & acc. correction

Differential BR & full experimental correlations

Further outcome based on measured spectra

- Fit M_X distribution and subtract background events from data
- Fit uncertainty and correlations fully propagated into bkg-subtracted spectra



Analysis Workflow

Brief Recap

Event Reconstruction

Background subtraction

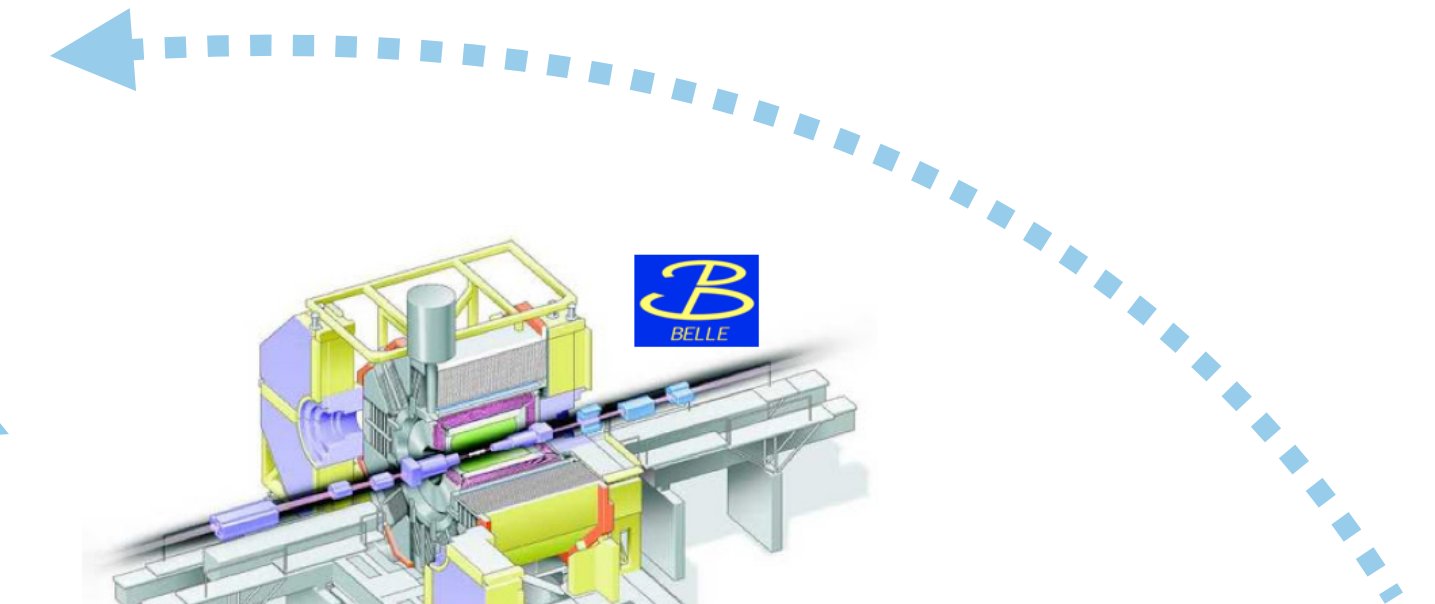
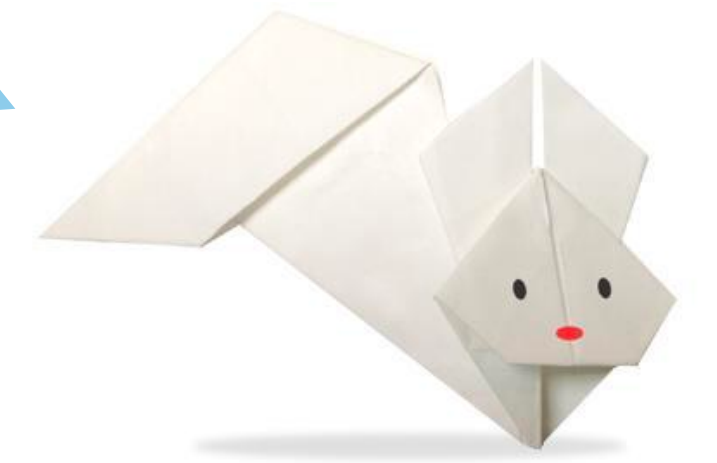
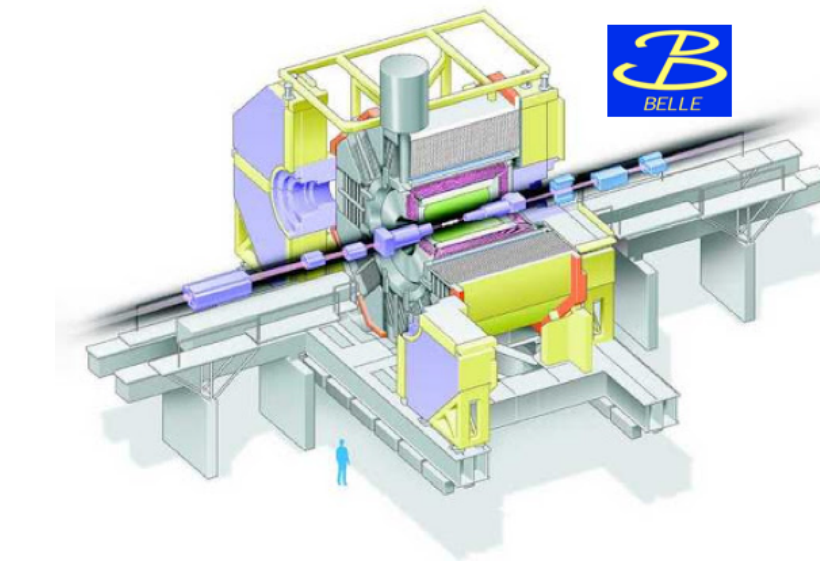
Unfolding

Eff. & acc. correction

Differential BR &
full experimental
correlations

Further outcome based
on measured spectra

- Measured spectra are usually distorted and transformed by various detector effects (resolution, acceptance, etc.) ==> **Need unfolding**
- Singular-Value-Decomposition (SVD) [NIMA 372:469(1996)] is used in this analysis



Analysis Workflow

Brief Recap

Event Reconstruction

Background subtraction

Unfolding

Eff. & acc. correction

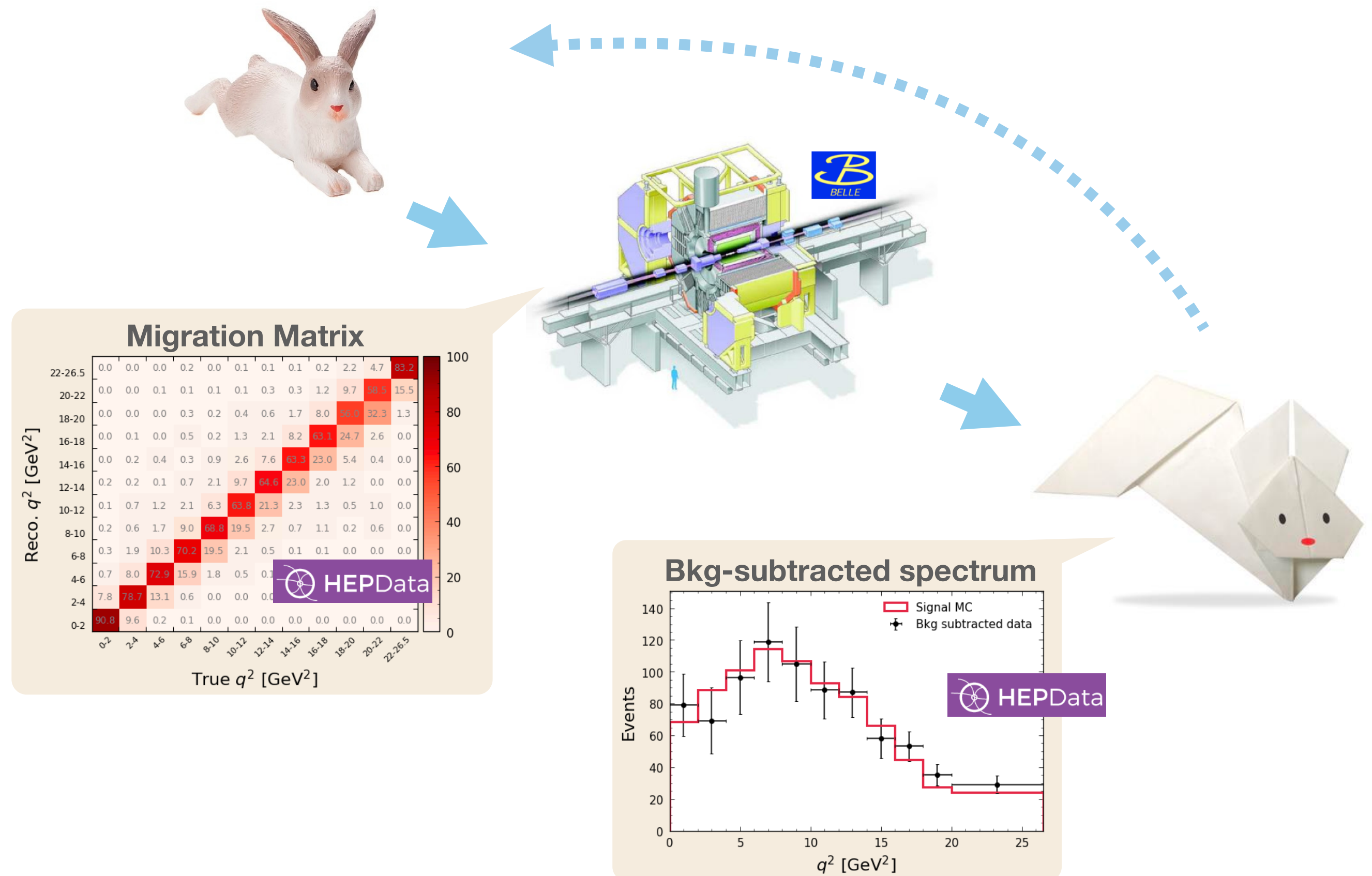
Differential BR & full experimental correlations

Further outcome based on measured spectra

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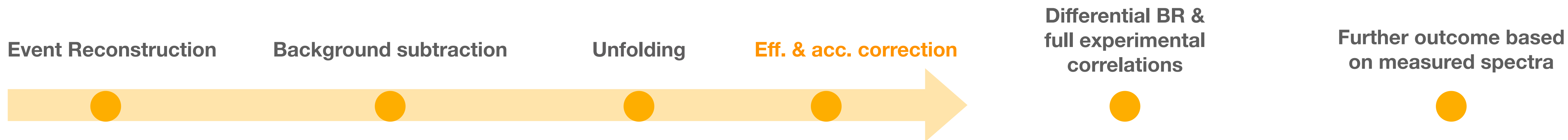
Ingredients provided on HepData allow:

- **EXP:** utilise another unfolding method
- **TH:** forward-fold to smear theoretical predictions (can be used to compare with observed spectra w/o unfolding)



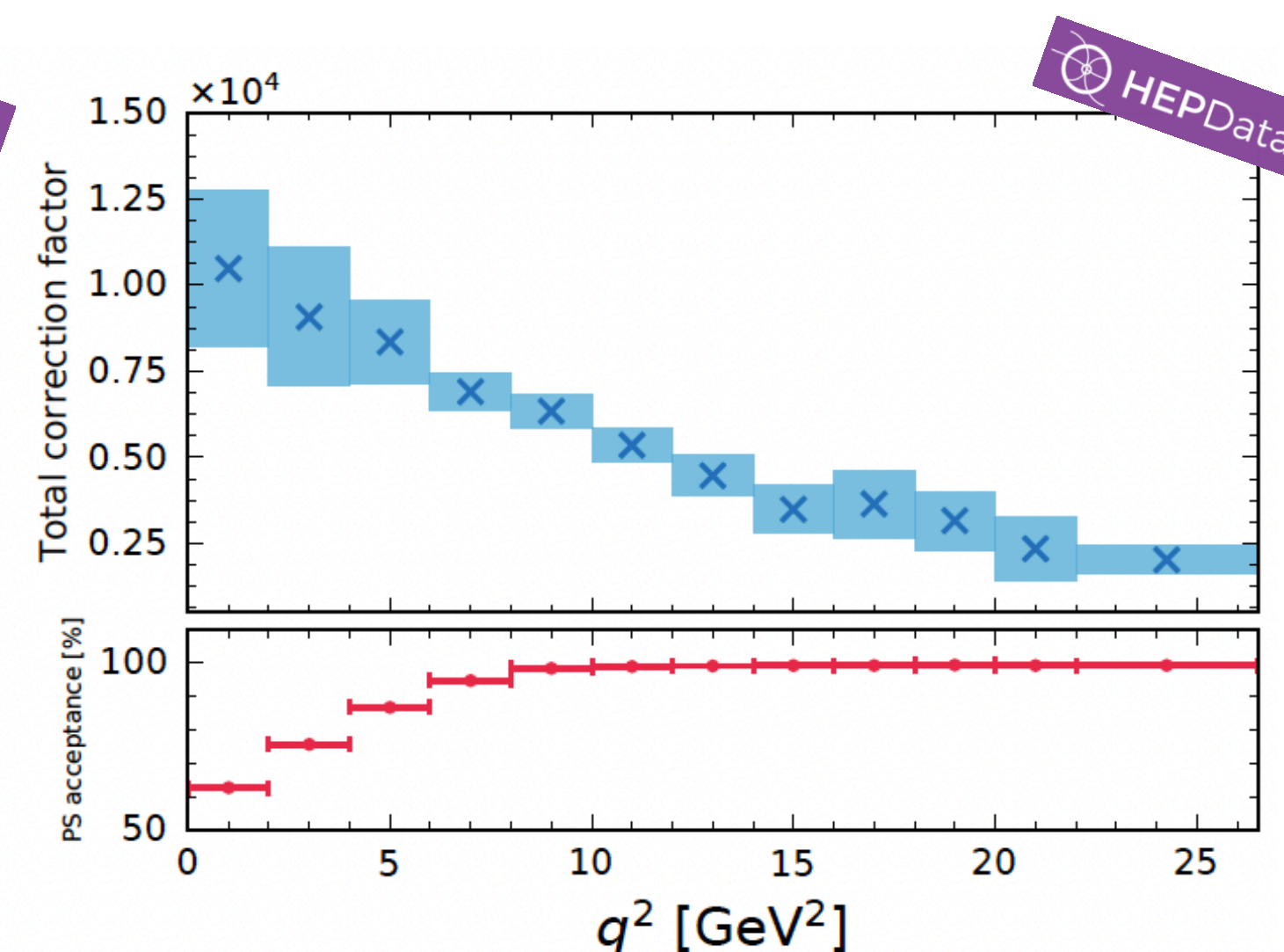
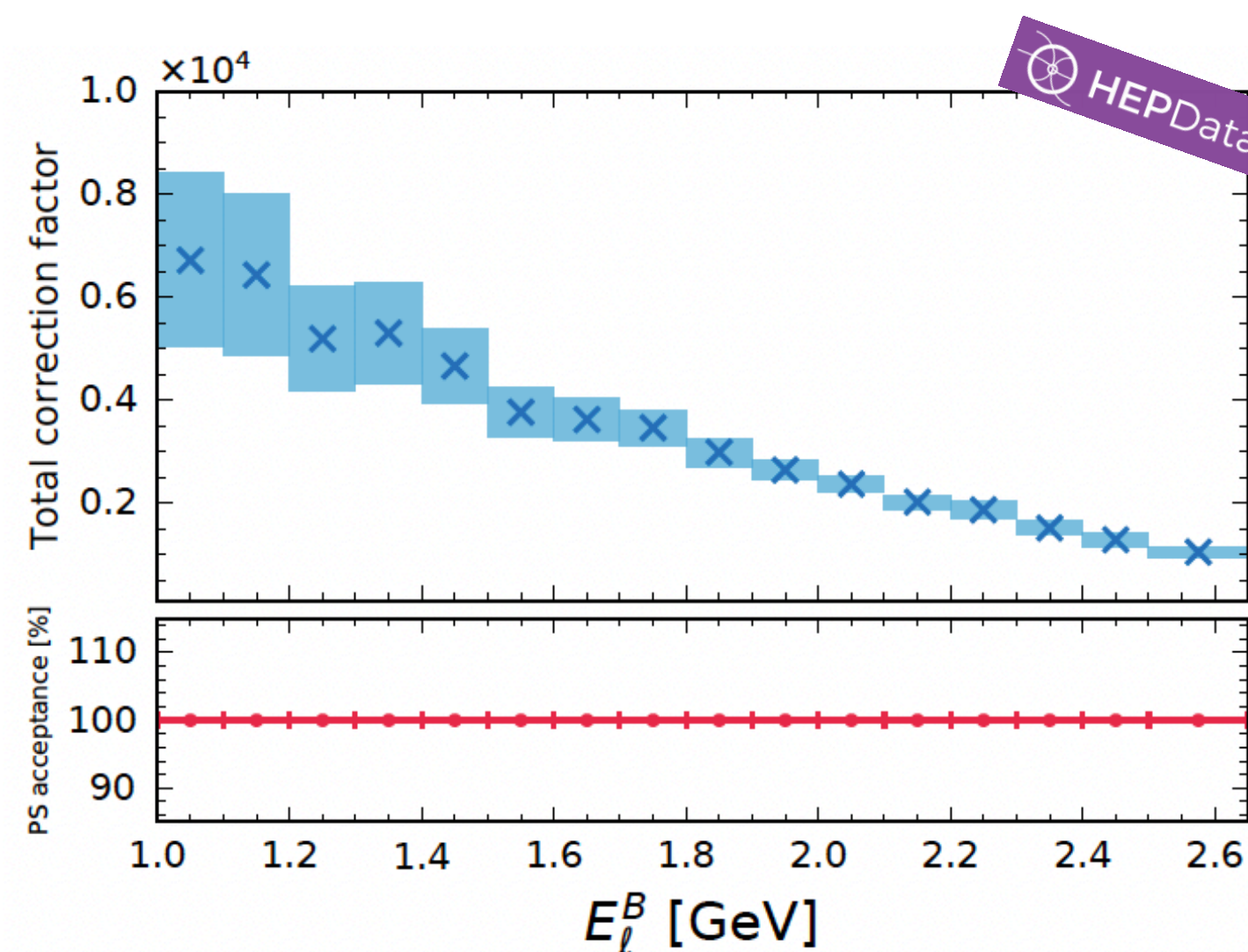
Analysis Workflow

Brief Recap



$$\Delta^i \mathcal{B} (B \rightarrow X_u \ell^+ \nu_\ell; \text{PS}) = \frac{\hat{\eta}_{\text{unfolded}}^i \cdot \left(\epsilon_{\text{tag}}^i \cdot \epsilon_{\text{sel}}^i \right)^{-1} \cdot \epsilon_{\Delta \mathcal{B}}^i (\text{PS})}{4 \cdot N_{B\bar{B}}}$$

- Measured phase space (PS): $E_l^B > 1 \text{ GeV}$
- Correction factors for selection efficiency and PS acceptance are provided for all kin. variables



Analysis Workflow

Brief Recap

Event Reconstruction

Background subtraction

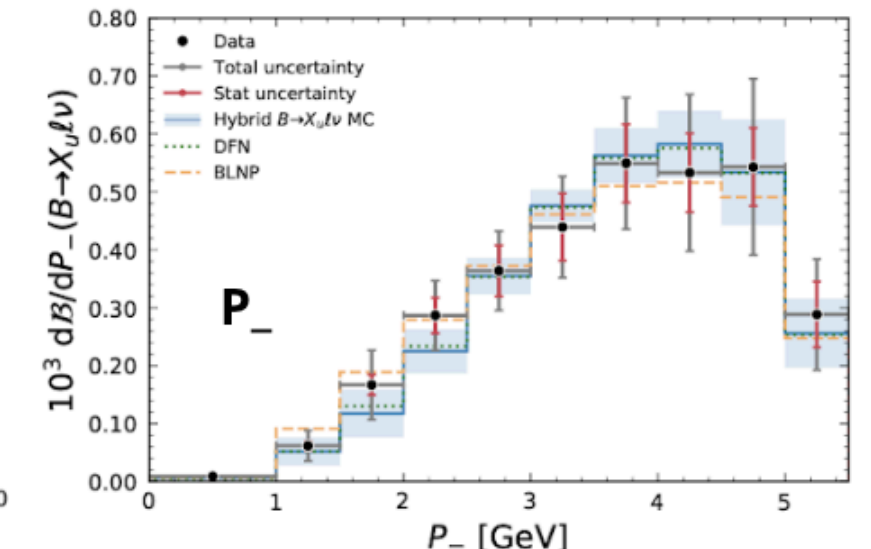
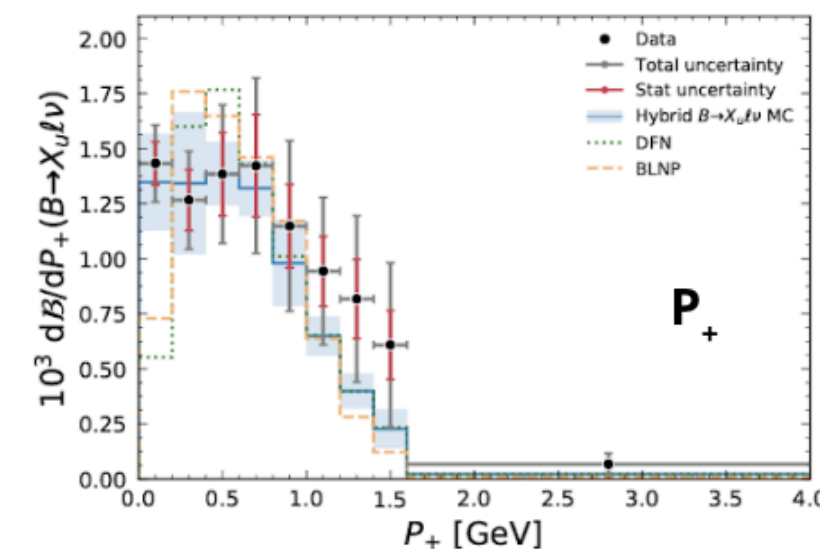
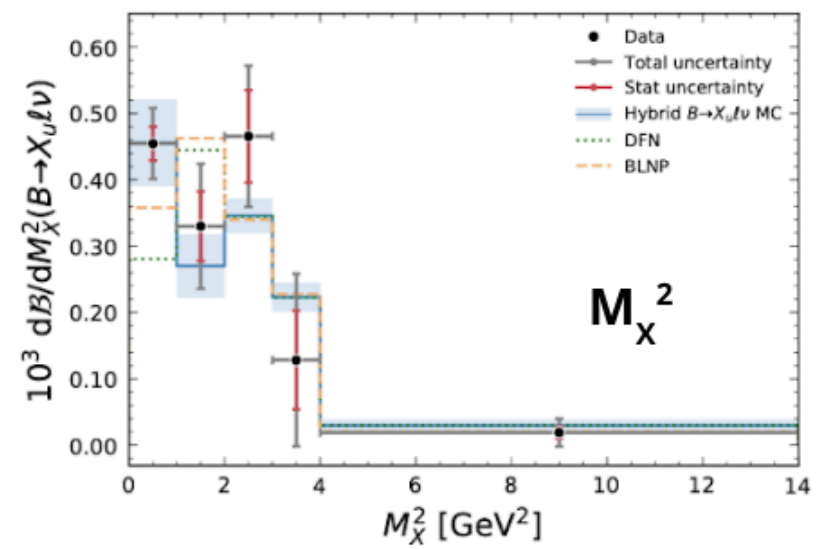
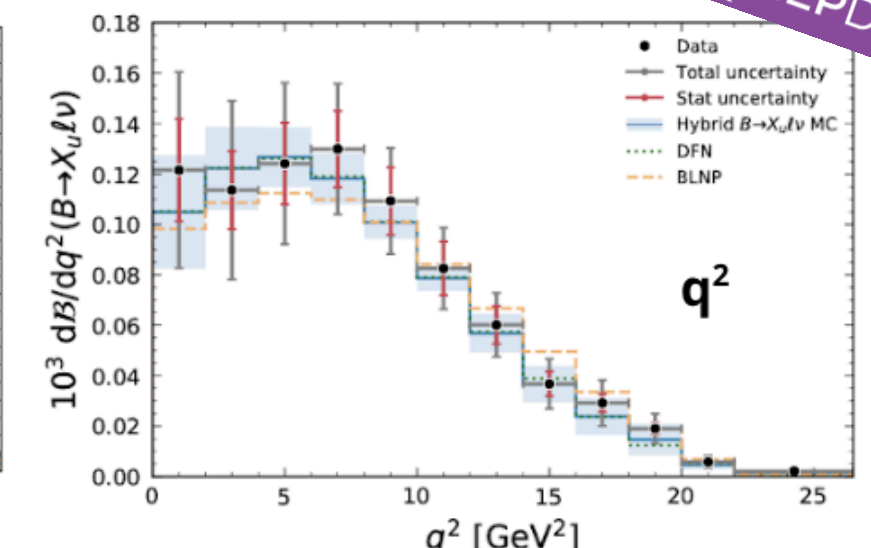
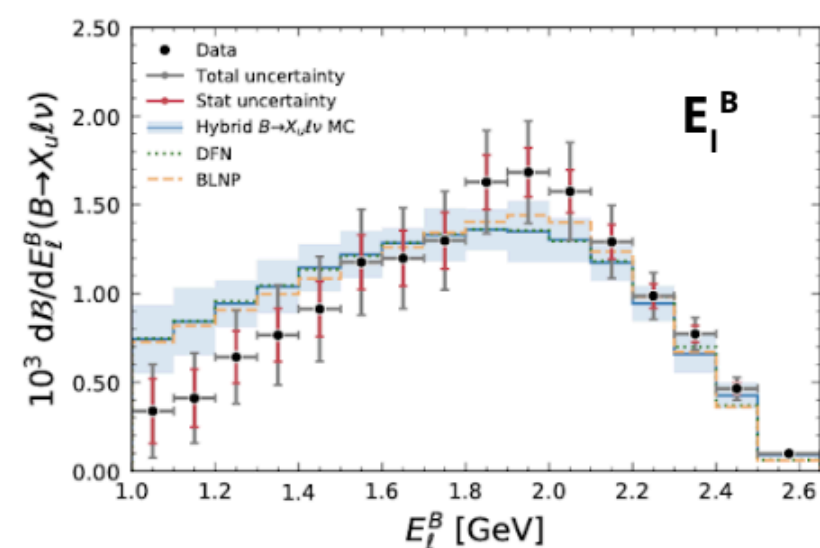
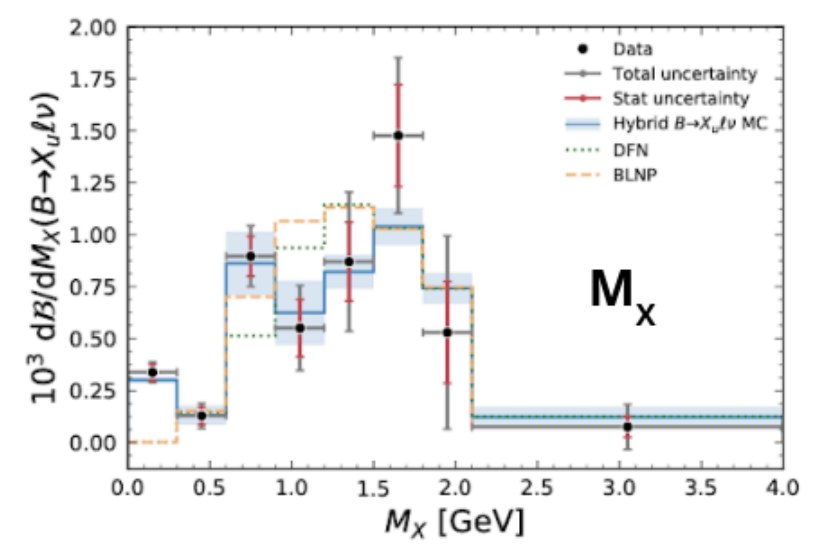
Unfolding

Eff. & acc. correction

Differential BR & full experimental correlations

Further outcome based on measured spectra

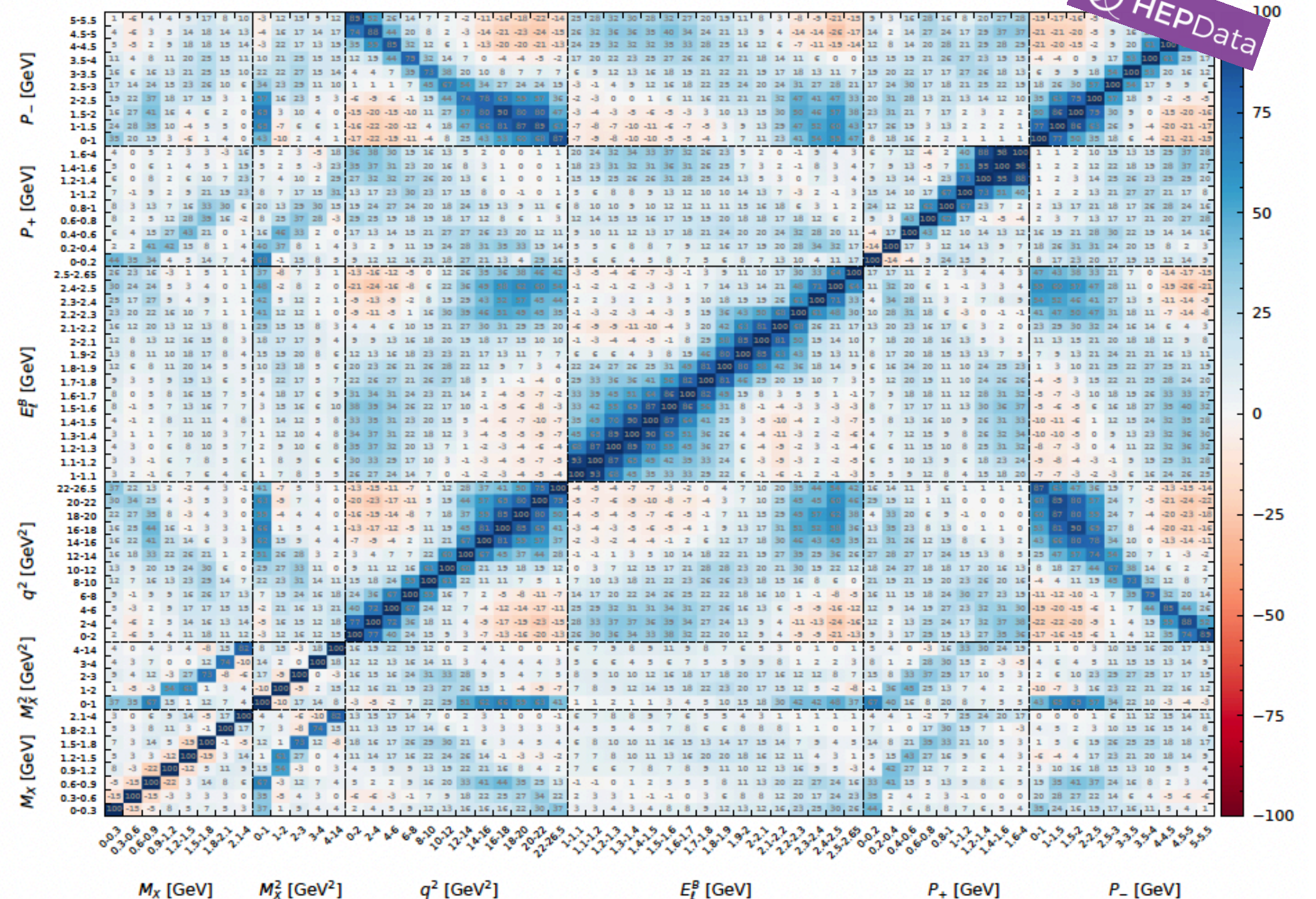
$$\Delta^i \mathcal{B}(B \rightarrow X_u \ell^+ \nu_\ell; \text{PS}) = \frac{\hat{\eta}_{\text{unfolded}}^i \cdot (\epsilon_{\text{tag}}^i \cdot \epsilon_{\text{sel}}^i)^{-1} \cdot \epsilon_{\Delta \mathcal{B}}^i(\text{PS})}{4 \cdot N_{B\bar{B}}}$$



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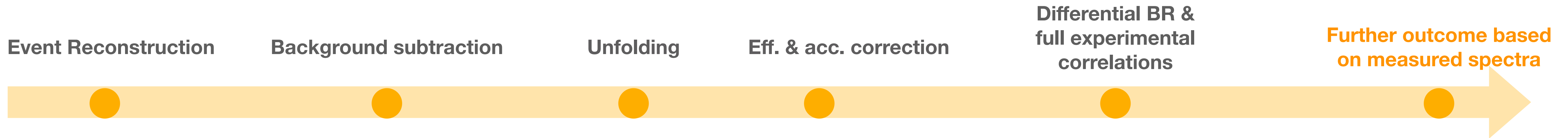
Necessary input for a global fit

Full experimental correlation matrix

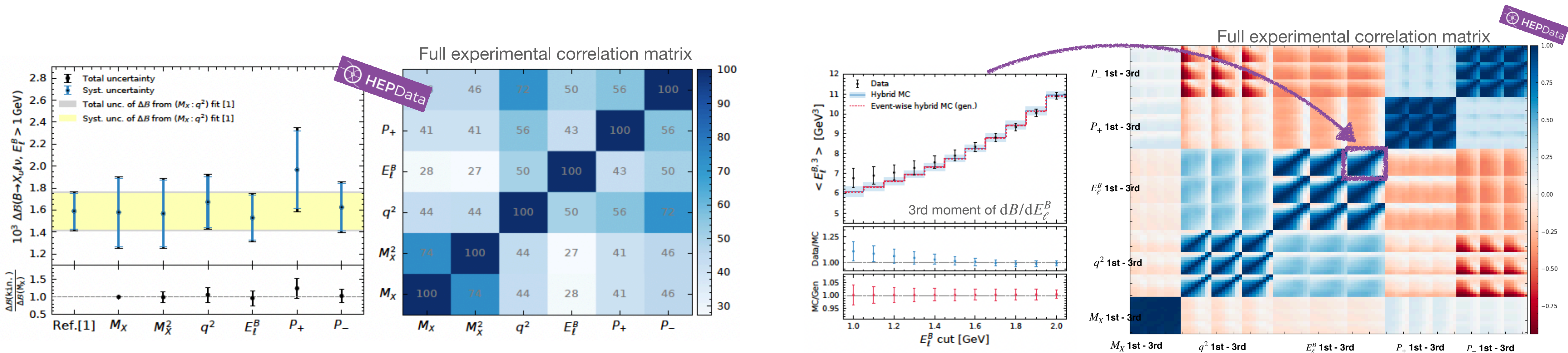


Analysis Workflow

Brief Recap



- Provide **direct** input for theory community:
 - Summed differential BRs & full correlations
 - 1st-3rd moments of each measured differential spectrum & full correlations



Crucial input for theoretical extraction of non-perturbative shape function & incl. $|V_{ub}|$

HepData Resources



HepData Resources

Event Reconstruction

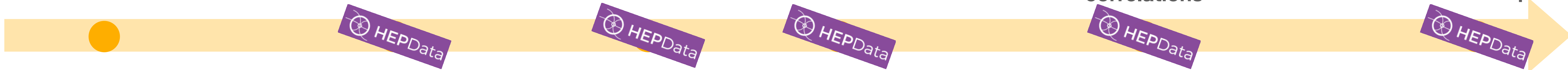
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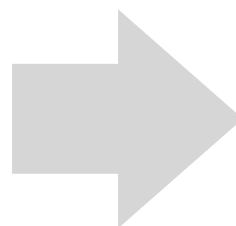
Measurement of Differential Branching Fractions of Inclusive $B \rightarrow X_u \ell^+ \nu_\ell$ Decays

Belle Collaboration • L. Cao (Bonn U., HISKP and DESY) [Show All\(201\)](#)
Jul 29, 2021

8 pages
Published in: *Phys.Rev.Lett.* 127 (2021) 26, 261801
Published: Dec 22, 2021
e-Print: [2107.13855](https://arxiv.org/abs/2107.13855) [hep-ex]
DOI: [10.1103/PhysRevLett.127.261801](https://doi.org/10.1103/PhysRevLett.127.261801) (publication)
Report number: Belle Preprint 2021-15, KEK Preprint 2021-13
Experiments: KEK-BF-BELLE
View in: [HAL Archives Ouvertes](#), [ADS Abstract Service](#)

[pdf](#) [cite](#) [claim](#)

[datasets](#)

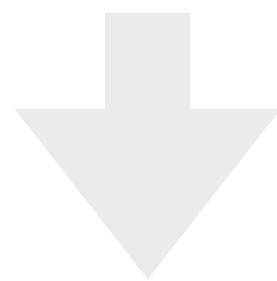


E_ℓ^B [GeV]	$DSIG/D E_\ell^B$
1.0 - 1.1	$0.00033783 \pm 0.00018357 \text{ stat} \pm 0.00018818 \text{ syst}$
1.1 - 1.2	$0.00041072 \pm 0.00016211 \text{ stat} \pm 0.00019656 \text{ syst}$
1.2 - 1.3	$0.00064222 \pm 0.00014802 \text{ stat} \pm 0.0002179 \text{ syst}$
1.3 - 1.4	$0.00076557 \pm 0.00015075 \text{ stat} \pm 0.0002393 \text{ syst}$
1.4 - 1.5	$0.00091303 \pm 0.00015576 \text{ stat} \pm 0.00025088 \text{ syst}$
1.5 - 1.6	$0.0011769 \pm 0.00015388 \text{ stat} \pm 0.00025575 \text{ syst}$
1.6 - 1.7	$0.0011987 \pm 0.00015629 \text{ stat} \pm 0.00023759 \text{ syst}$
1.7 - 1.8	$0.0012986 \pm 0.00015855 \text{ stat} \pm 0.00024699 \text{ syst}$
1.8 - 1.9	$0.0016281 \pm 0.00015298 \text{ stat} \pm 0.00024659 \text{ syst}$
1.9 - 2.0	$0.0016831 \pm 0.00013761 \text{ stat} \pm 0.00025329 \text{ syst}$

Hands-on Example

1D, 2D, binned, unbinned

- **1D**: yields, efficiency, differential branching fractions, moments, etc.
- **2D**: all matrices, i.e. covariance, correlation, migration
- **Binned**: differential branching fractions, efficiency, migration, etc.
- **Unbinned**: moments (as function of threshold), matrix given with elements' index, etc.



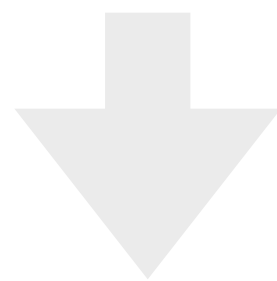
ALL filled & provided as flat tables



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ALL filled & provided as flat tables



HepData tutorial: https://github.com/HEPData/hepdata_lib/tree/master/examples

1. Define table title, location, etc.

2. Define axis
(independent variable)

3. Fill values
(dependent variable)

X axis	Y axis (if 2D)	Value

Hands-on Example

1D binned: dB/dq^2

```
import hepdata_lib
from hepdata_lib import Submission, Table, Variable, Uncertainty

submission = Submission()

submission.read_abstract("./B1_BtoXulnu_PRL/abstract_hepdata.txt")
submission.add_link("Publication website", "https://journals.aps.org/prl")
submission.add_link("arXiv", "https://arxiv.org/abs/2107.13855")
submission.add_record_id(1895149, "inspire")
```

```
## define table title, location, etc.
table_fig3b = Table("Fig. 3 (top right)")
table_fig3b.description = "The measured differential branching fractions as a function of t."
table_fig3b.location = "Top right panel of Fig. 3"
table_fig3b.keywords["observables"] = ["DSIG/DQ**2"]
table_fig3b.keywords["reactions"] = ["B --> X_u l+ nu_l"]

# define 1D axis
x_fig3b = Variable("$q^{2}$", is_independent=True, is_binned=True, units="GeV$^2$")
x_fig3b.values = list(zip(q2_unfold_bin[:-1], q2_unfold_bin[1:]))
table_fig3b.add_variable(x_fig3b)

# fill central result
data_fig3b = Variable("DSIG/D$q^{2}$", is_independent=False, is_binned=False, units="")
data_fig3b.values = dBF_q2['dBF_cen']/get_bin_widths(q2_unfold_bin)

# fill stat. uncertainty
unc_data_fig3b_stat = Uncertainty("stat", is_symmetric=True)
unc_data_fig3b_stat.values = dBF_q2['dBF_err_stat']/get_bin_widths(q2_unfold_bin)
data_fig3b.add_uncertainty(unc_data_fig3b_stat)

# fill syst. uncertainty
unc_data_fig3b_syst = Uncertainty("syst", is_symmetric=True)
unc_data_fig3b_syst.values = dBF_q2['dBF_err_sys']/get_bin_widths(q2_unfold_bin)
data_fig3b.add_uncertainty(unc_data_fig3b_syst)
table_fig3b.add_variable(data_fig3b)
```

Fig. 3 (top right) [10.17182/hepdata.131599.v1/t2](https://www.hepdata.net/record/10.17182/hepdata.131599.v1/t2)

Top right panel of Fig. 3

The measured differential branching fractions as a function of the four-momentum-transfer squared of the B to the X_u system q^2 .

observables

DSIG/DQ**2

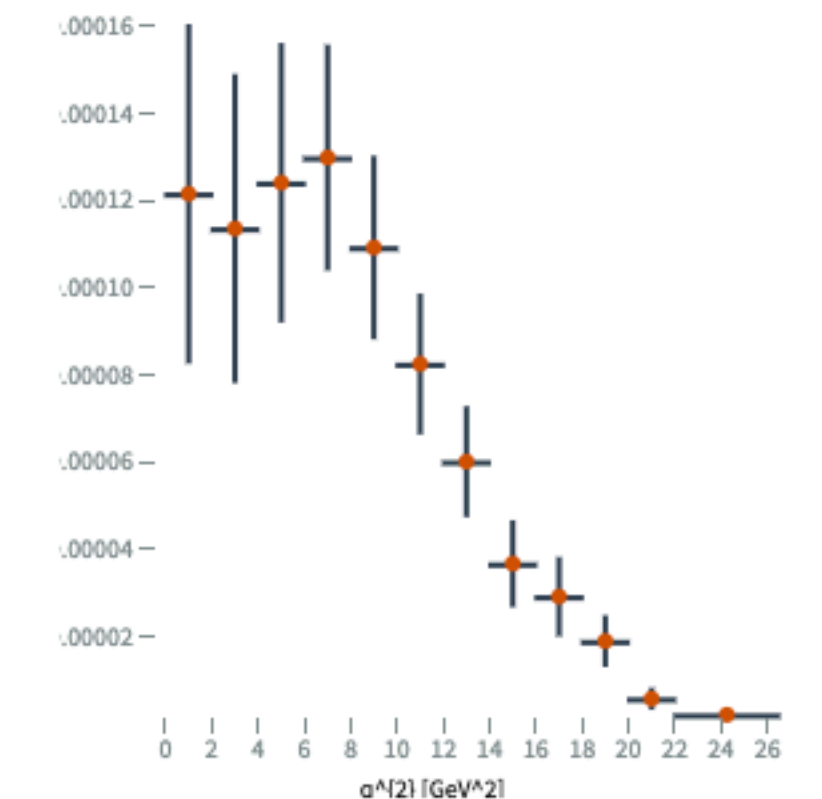
reactions

B --> X_u l+ nu_l

q^2 [GeV ²]	DSIG/D q^2
0.0 - 2.0	0.00012158 $\pm 2.0314e-05$ stat $\pm 3.3209e-05$ syst
2.0 - 4.0	0.00011361 $\pm 1.5535e-05$ stat $\pm 3.1849e-05$ syst
4.0 - 6.0	0.00012413 $\pm 1.6196e-05$ stat $\pm 2.7661e-05$ syst
6.0 - 8.0	0.00012988 $\pm 1.5083e-05$ stat $\pm 2.1042e-05$ syst
8.0 - 10.0	0.00010926 $\pm 1.3397e-05$ stat $\pm 1.6234e-05$ syst
10.0 - 12.0	8.2558e-05 $\pm 1.0624e-05$ stat $\pm 1.2165e-05$ syst
12.0 - 14.0	6.0146e-05 $\pm 7.4884e-06$ stat $\pm 1.0255e-05$ syst
14.0 - 16.0	3.6742e-05 $\pm 4.8875e-06$ stat $\pm 8.6703e-06$ syst
16.0 - 18.0	2.9185e-05 $\pm 3.4902e-06$ stat $\pm 8.378e-06$ syst
18.0 - 20.0	1.8975e-05 $\pm 2.2995e-06$ stat $\pm 5.4628e-06$ syst
20.0 - 22.0	5.7594e-06 $\pm 9.0366e-07$ stat $\pm 2.3605e-06$ syst
22.0 - 26.5	2.0731e-06 $\pm 4.1392e-07$ stat $\pm 5.2062e-07$ syst

<https://www.hepdata.net>   

Visualize



Sum errors Log Scale (X) Log Scale (Y)

Deselect variables or hide different error bars by clicking on them.

Hands-on Example

2D unbinned: full experimental correlations of differential spectra

- Giant correlations among all kin. variables
- In this case, matrix element is given with bin index instead of bin range (due to numerical overlap for various variables)

```
# define table title, location, etc.
table_fig8 = Table("Fig. 8")
table_fig8.description = "The full experimental (statistical and systematic) correlations of the
table_fig8.keywords["reactions"] = ["B --> X_u l+ nu_l"]

# define 2D X-axis
x = Variable("Element index (X)", is_independent=True, is_binned=False)
x.values = get_2Dbinedges(np.linspace(0,59,60), "X", binindex=True)

# define 2D Y-axis
y = Variable("Element index (Y)", is_independent=True, is_binned=False)
y.values = get_2Dbinedges(np.linspace(0,59,60), "Y", binindex=True)

# fill matrix elements
correlation_full = Variable("Correlation coefficient", is_independent=False, is_binned=False)
correlation_full.values = giant_cor_tot.transpose().reshape(len(giant_cor_tot)**2)

table_fig8.add_variable(x)
table_fig8.add_variable(y)
table_fig8.add_variable(correlation_full)

submission.add_table(table_fig8)
```

Fig. 8 [10.17182/hepdata.131599.v1/t32](https://www.hepdata.net/record/10.17182/hepdata.131599.v1/t32)

Example location

The full experimental (statistical and systematic) correlations of the differential branching fractions are shown. The matrix elements are ordered for $M_X, M_X^2, q^2, E_\ell^B, P_+$ and P_- .

reactions

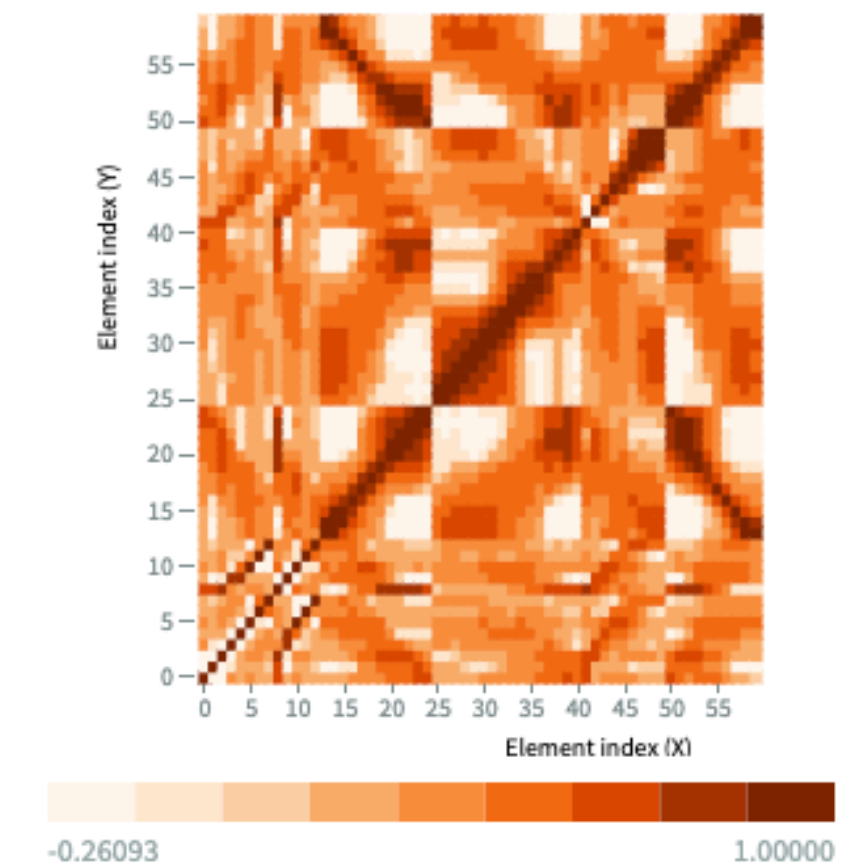
B --> X_u l+ nu_l

Showing 50 of 3600 values

Show All 3600 values

Element index (X)	Element index (Y)	Correlation coefficient
0.0	0.0	1.0
0.0	1.0	-0.15023
0.0	2.0	-0.046279
0.0	3.0	0.078509
0.0	4.0	0.050481
0.0	5.0	0.067942
0.0	6.0	0.053793
0.0	7.0	0.029232
0.0	8.0	0.36972
0.0	9.0	0.013695
0.0	10.0	0.090197
0.0	11.0	0.036792
0.0	12.0	0.03691

Visualize



Brushing Enabled?

X Axis

Y Axis

Hands-on Example

2D binned: migration matrix

```
# define table title, location, etc.
table_mig_q2 = Table("Fig. 5 (middle right)")
table_mig_q2.description = "Migration matrix of $q^2$ [in %]."
table_mig_q2.location = "Middle right panel of Fig. 5"
table_mig_q2.keywords["reactions"] = ["B --> X_u l+ nu_l"]

# define 2D X-axis
x_mig_q2 = Variable("True $q^2$ bin", is_independent=True, is_binned=True, units="GeV$^2$")
x_mig_q2.values = get_2Dbinedges(q2_unfold_bin, "X")

# define 2D Y-axis
y_mig_q2 = Variable("Reco. $q^2$ bin", is_independent=True, is_binned=True, units="GeV$^2$")
y_mig_q2.values = get_2Dbinedges(q2_unfold_bin, "Y")

# fill matrix elements
data_mig_q2 = Variable("Migration matrix", is_independent=False, is_binned=False, units="%")
data_mig_q2.values = 100*mig_q2['nominal_migration_matrix'].transpose().reshape(len(mig_q2['nominal_migration_matrix']))

table_mig_q2.add_variable(x_mig_q2)
table_mig_q2.add_variable(y_mig_q2)
table_mig_q2.add_variable(data_mig_q2)
```

Tutorial notebook: https://stash.desy.de/users/lcaocn/repos/hepdata_example/browse

Example: convert results into yaml for HepData submission

```
In [1]: import numpy as np
import pickle

import hepdata_lib
from hepdata_lib import Submission, Table, Variable, Uncertainty

Welcome to Jupyter 6.24/06
```

1. Initialise submission with details on related publication

```
In [2]: submission = Submission()

submission.read_abstract("./abstract.txt")
submission.add_link("Publication website", "https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.127.261801")
submission.add_link("arXiv", "https://arxiv.org/abs/2107.13855")
submission.add_record_id(1895149, "inspire")
```

Some useful functions

```
In [3]: def get_bin_widths(bins):
widths = [b-a for a, b in zip(bins[0:-1], bins[1:])]
return widths

def get_2Dbinedges(bins, axis="X", binindex=False):
# prepare 2D binning array for hepdata matrix

if binindex==False:
a=list(zip(bins[0:-1], bins[1:]))
b=[]
if axis=="X":
```

Fig. 5 (middle right) [10.17182/hepdata.131599.v1/t20](https://www.hepdata.net/record/10.17182/hepdata.131599.v1/t20)

Middle right panel of Fig. 5

Migration matrix of q^2 [in %].

reactions

B --> X_u l+ nu_l

Showing 50 of 144 values

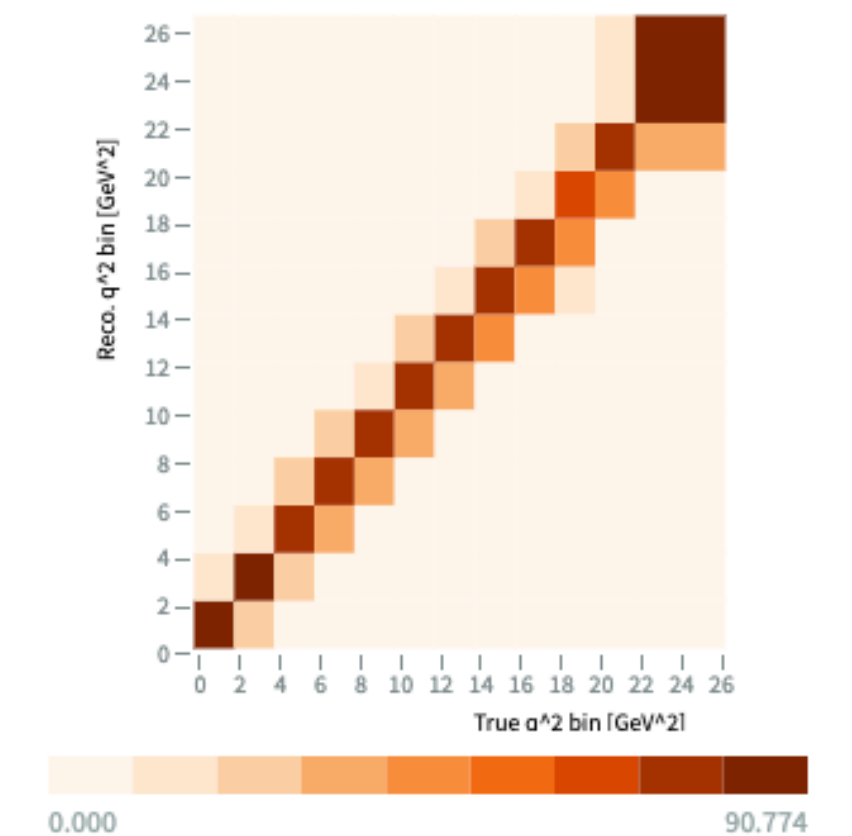
[Show All 144 values](#)

True q^2 bin [GeV ²]	Reco. q^2 bin [GeV ²]	Migration matrix [%]
0.0 - 2.0	0.0 - 2.0	90.774
0.0 - 2.0	2.0 - 4.0	7.7856
0.0 - 2.0	4.0 - 6.0	0.7107
0.0 - 2.0	6.0 - 8.0	0.27675
0.0 - 2.0	8.0 - 10.0	0.15665
0.0 - 2.0	10.0 - 12.0	0.070682
0.0 - 2.0	12.0 - 14.0	0.22555
0.0 - 2.0	14.0 - 16.0	0.0
0.0 - 2.0	16.0 - 18.0	0.0
0.0 - 2.0	18.0 - 20.0	0.0
0.0 - 2.0	20.0 - 22.0	0.0
0.0 - 2.0	22.0 - 26.5	0.0
2.0 - 4.0	0.0 - 2.0	9.5878

<https://www.hepdata.net>



Visualize



Brushing Enabled?

X Axis True q^2 bin [GeV²]

Y Axis Reco. q^2 bin [GeV²]