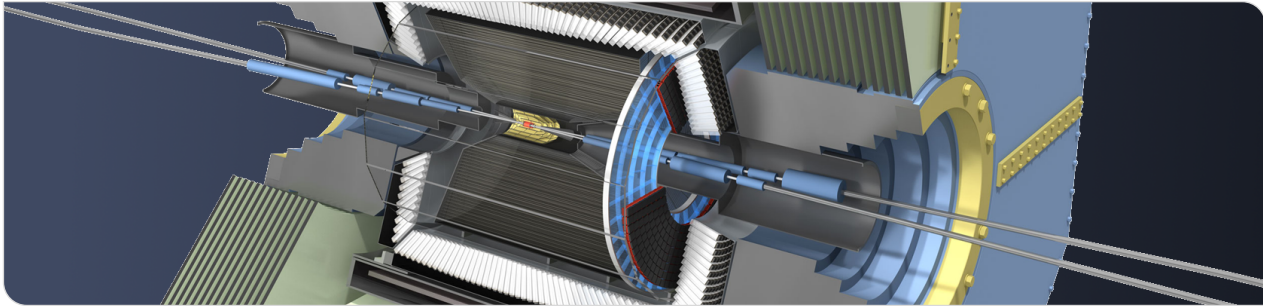


# GNN-based Track and Vertex Finding

B2GM TRG

Lea Reuter, Philipp Dorwarth, Slavomira Stefkova, Torben Ferber | 7th October 2022



# Project members: Machine Learning for Trigger



## KIT (ETP)

L. Reuter, I. Haide, P. Dorwarth,  
P. Ecker, S. Stefkova, T. Ferber



## KIT (ITIV)

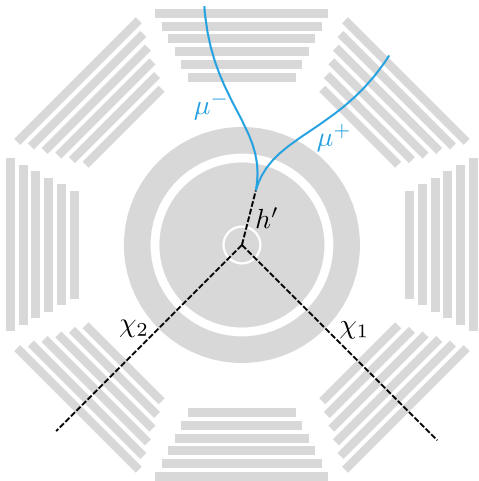
M. Neu, K. Unger, J. Becker



## MPI (MPP)

E. Schmidt, F. Meggendorfer, C. Kiesling





## Searches for displaced vertices <sup>a</sup>

- Displaced vertices important signature in searches for new physics

- Example signal decay with dark photon  $A'$  and dark higgs  $h'$

$$e^+e^- \rightarrow A'h',$$

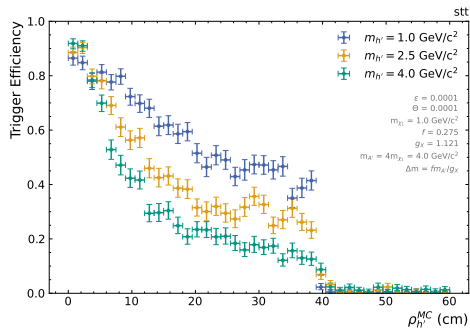
$$h' \rightarrow \mu^+\mu^-,$$

$$A' \rightarrow \chi_1\chi_2,$$

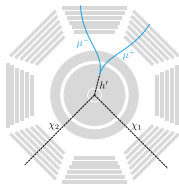
$$\chi_2 \rightarrow \chi_1 e^+e^-$$

---

<sup>a</sup>Patrick Ecker : [Search for Inelastic Dark Matter](#)



Credit: Patrick Ecker



## Searches for displaced vertices

- Displaced vertices important signature in searches for new physics
- Example signal decay with dark photon  $A'$  and dark higgs  $h'$ 

$$e^+ e^- \rightarrow A' h',$$

$$h' \rightarrow \mu^+ \mu^-,$$

$$A' \rightarrow \chi_1 \chi_2,$$

$$\chi_2 \rightarrow \chi_1 e^+ e^-$$

## Problem:

- Tracks with displacement larger than 40 cm are currently not triggered by **Single Track Trigger (stt)**
- stt reconstruction efficiency decreases depending on displacement



- **Improve Track and Develop Vertex Finding using Graph Neural Networks (GNNs):**

- Find events with displaced vertices (develop vertex finding)
- Need to improve online L1 Trigger reconstruction

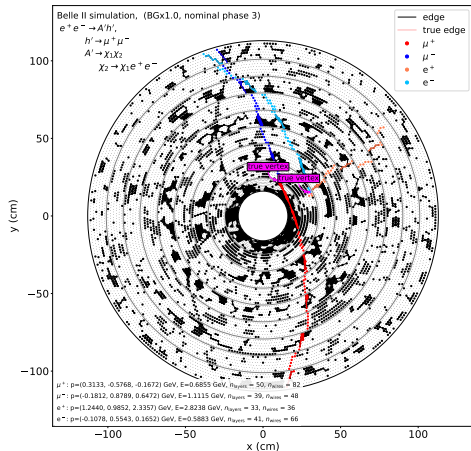
# Project Goal

## ■ Improve Track and Develop Vertex Finding using Graph Neural Networks (GNNs):

- Find events with displaced vertices (develop vertex finding)
- Need to improve online L1 Trigger reconstruction

## ■ Challenge:

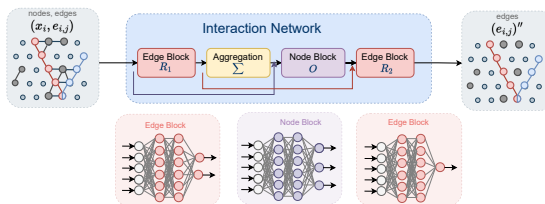
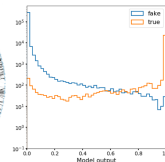
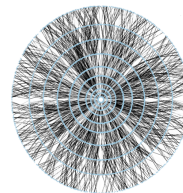
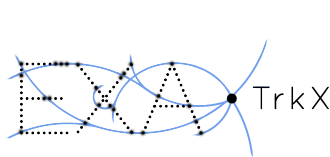
- Tracks with low  $p_t$  (tracks curve)
- Large occupancy due to beam-background hits (nominal phase 3)
- Beam-background tracks (look like signal tracks)
- Displaced vertices that are not pointing back to the interaction point



/group/belle2/dataproduct/BG0overlay/nominal\_phase3/  
prerelease-05-00-00a/overlay/phase3/BGx1/

# Related Work: GNN Models for Real-Time Tracking

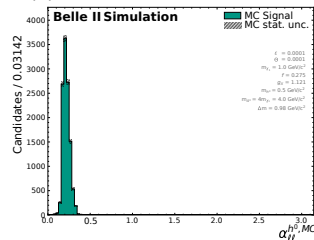
- Project [Exa.TrkX](#): ATLAS, CMS, and DUNE experiments: Tracking with GNN models on FPGA-based real-time processing systems
- Graph Neural Networks for Charged Particle Tracking on FPGAs ([arxiv:2112.02048](#))
- Greta Heine (ETP, IPE): Trackfinding on FPGAs for the PANDA Experiment



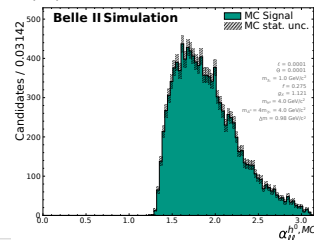
# MC Simulated Samples

- Release:  
feature/BII-9379-store-cdchit-relations-to-all-particle
- Globaltags: main\_2022-01-27 and patch\_main\_release-07
- Starting with BGx0 and early-phase 3 BGx1  
/group/belle2/dataproduct/BG0overlay/early\_phase3/  
release-05-01-15/overlay/phase31/BGx1/set0/
- Signal samples:
  - Single displaced vertex samples
  - $e^+e^- \rightarrow A'h'$ ,  
 $h' \rightarrow \mu^+\mu^-$ ,  
 $A' \rightarrow \chi_1\chi_2$ ,  
 $\chi_2 \rightarrow \chi_1 e^+e^-$  (outside of CDC)
  - on-shell (two-body)
  - $m(h)$  (0.5-4.0 GeV) in 0.1 GeV steps
- Background samples:
  - $e^+e^- \rightarrow e^+e^-$
  - $e^+e^- \rightarrow \mu^+\mu^-$

Distribution of opening angle  $\alpha_{\ell\ell}^{h'}$   
 $m(h) = 0.5 \text{ GeV}$

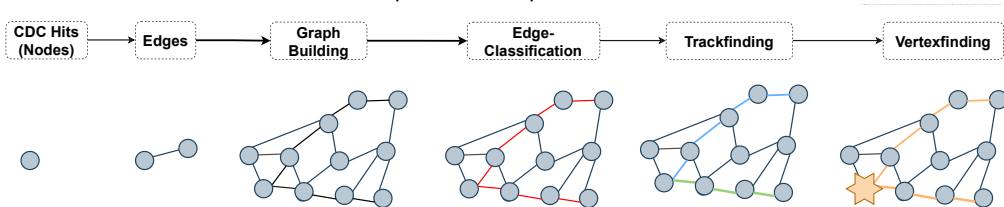


$m(h') = 4.0 \text{ GeV}$



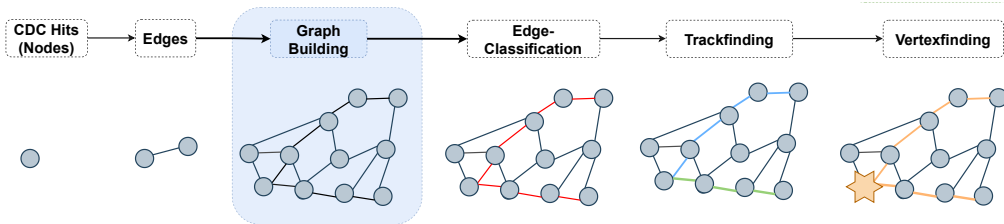
# Approach with Graph Neural Networks

Variable number of CDC hits → utilize Graphs and Graph Neural Networks

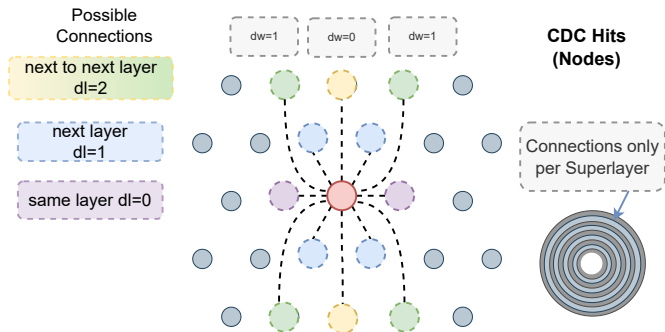


# Approach with Graph Neural Networks: Graph Building

Variable number of CDC hits → utilize Graphs and Graph Neural Networks



# Graph-Segment Building

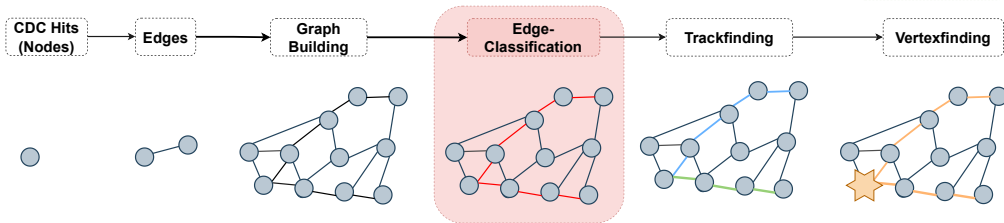


- Find trade-offs between purity, efficiency, graph size and timing
- Choice of graph building dependent on subsequent tasks
- Working together with [ITIV \(Department of Electrical Engineering Information Technology\)](#) at KIT for L1 Trigger graph building

→ Philipp Dorwarth is working on this and will show studies and results in upcoming trigger meetings

# Approach with Graph Neural Networks: Edge Classification

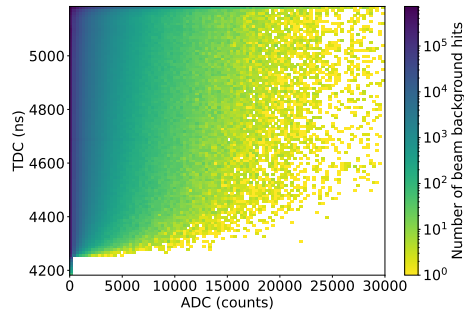
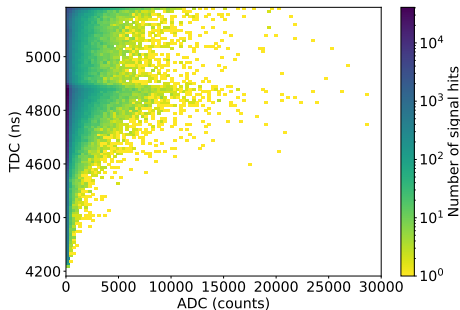
Classify True and False edges of the graph



**Interaction Network:** Graph Neural Networks for Charged Particle Tracking on FPGAs  
([arxiv:2112.02048](https://arxiv.org/abs/2112.02048))



# GNN Input Feature Studies



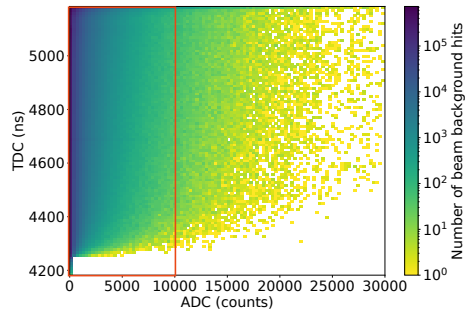
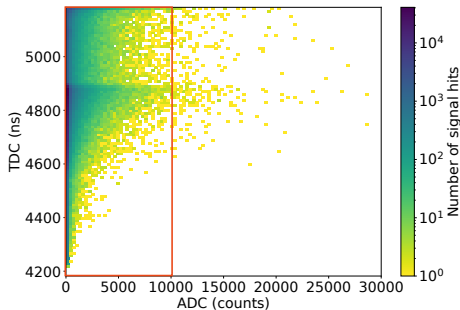
Testing discriminating input features:

- Edges:  $\Delta\rho$ ,  $\Delta\phi$
- Nodes:  $\rho$ ,  $\phi$ , TDC, ADC

Additional inputs

- digitized timing information **TDC**  
(online available after LS1)
- digitized signal information **ADC**  
(online perhaps available for 2025)

# GNN Input Feature Studies



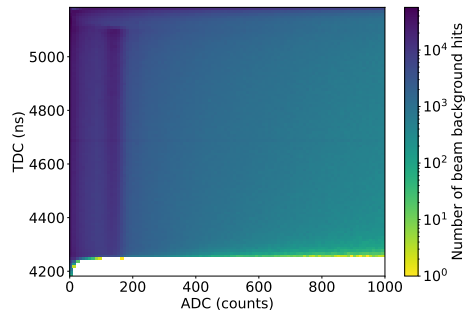
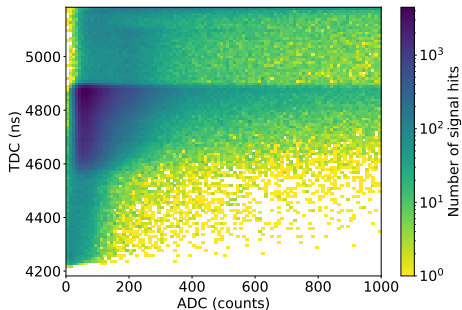
Testing discriminating input features:

- Edges:  $\Delta\rho$ ,  $\Delta\phi$
- Nodes:  $\rho$ ,  $\phi$ , TDC, ADC

Additional inputs

- digitized timing information **TDC**  
(online available after LS1)
- digitized signal information **ADC**  
(online perhaps available for 2025)

# GNN Input Feature Studies



Testing discriminating input features:

- Edges:  $\Delta\rho$ ,  $\Delta\phi$
- Nodes:  $\rho$ ,  $\phi$ , TDC, ADC

Additional inputs

- digitized timing information **TDC**  
(online available after LS1)
- digitized signal information **ADC**  
(online perhaps available for 2025)

→ **Currently working on data to MC comparison for ADC and TDC (see backup for initial comparison)!**

# Edge Classification GNN Evaluation

Determine binary threshold using maximal  $F_1$  score:

- $purity = \frac{TP}{TP+FP}$

- $efficiency = \frac{TP}{TP+FN}$

- $F_1 = 2 \cdot \frac{purity \cdot efficiency}{purity + efficiency} = \frac{TP}{TP + (FP + FN)/2}$

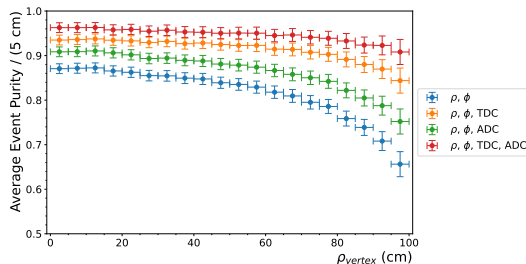
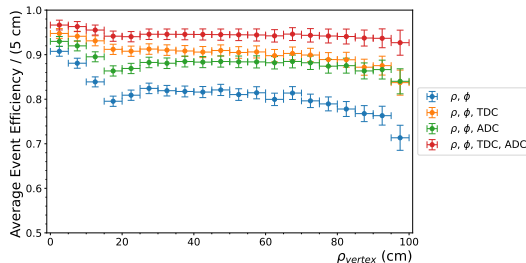
Using both TDC and ADC results in a

- Event classification efficiency of 94% and

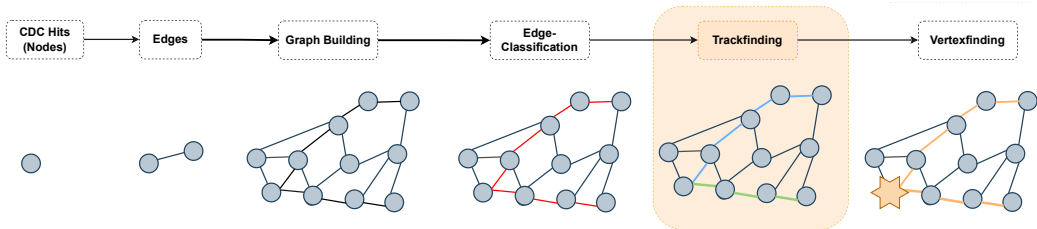
- Event classification purity of 93%

on signal with early-phase 3  
beam-background

evaluated on 1000 samples per mass



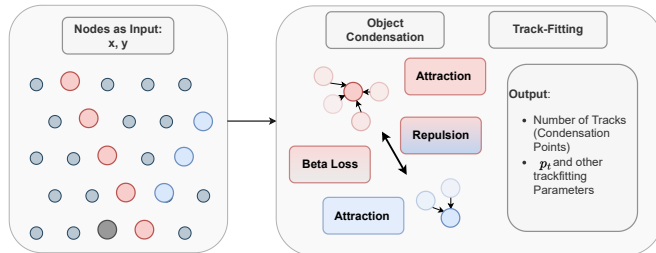
# Approach with Graph Neural Networks: Trackfinding



Use **Object Condensation** ([arXiv:2002.03605](https://arxiv.org/abs/2002.03605))

→ Based on Isabel Haide: [Improving ECL Clustering with Object Condensation](#)

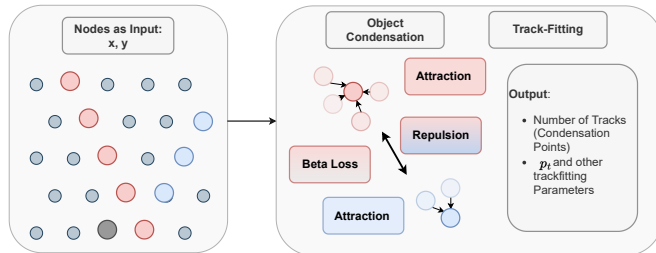
# Object Condensation Trackfinding Approach



→ Use nodes as input to Object Condensation ([arXiv:2002.03605](https://arxiv.org/abs/2002.03605))

→ **Goal:** predict track fitting parameters and find condensation points

# Object Condensation Trackfinding Approach

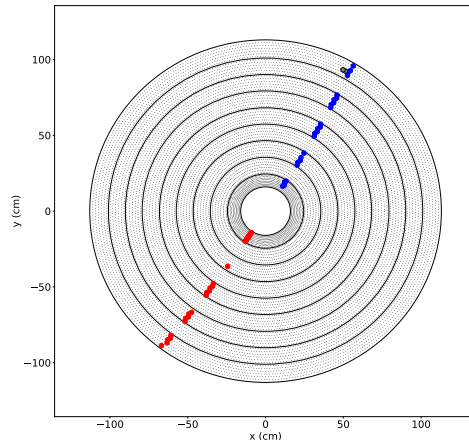


→ Use nodes as input to Object Condensation ([arXiv:2002.03605](https://arxiv.org/abs/2002.03605))  
→ **Goal:** predict track fitting parameters and find condensation points

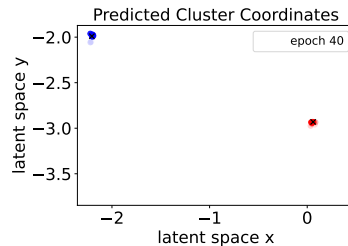
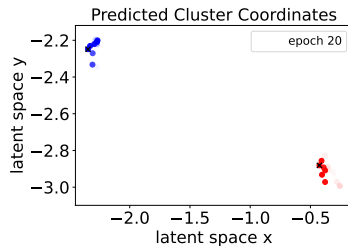
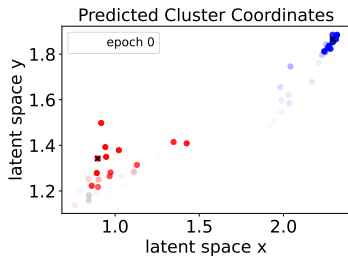
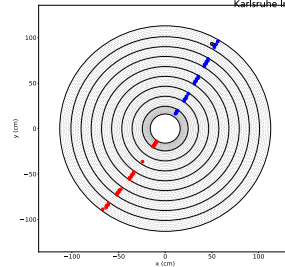
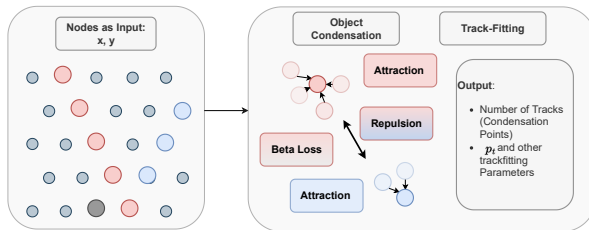
Start with very simple case:

$$e^+e^- \rightarrow \mu^+\mu^-$$

no beam-background



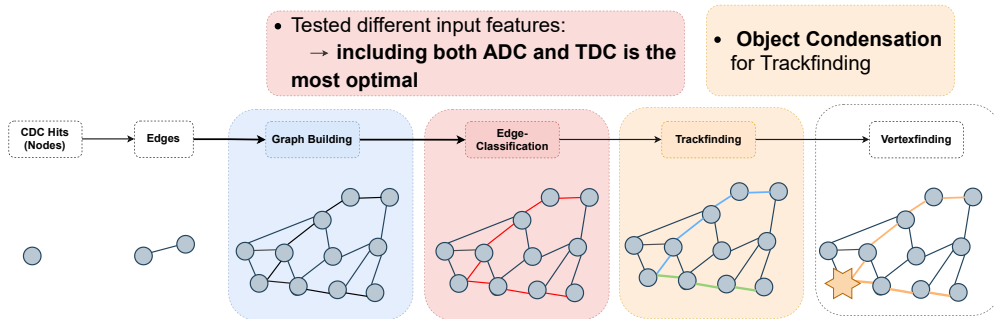
# Object Condensation Trackfinding Approach





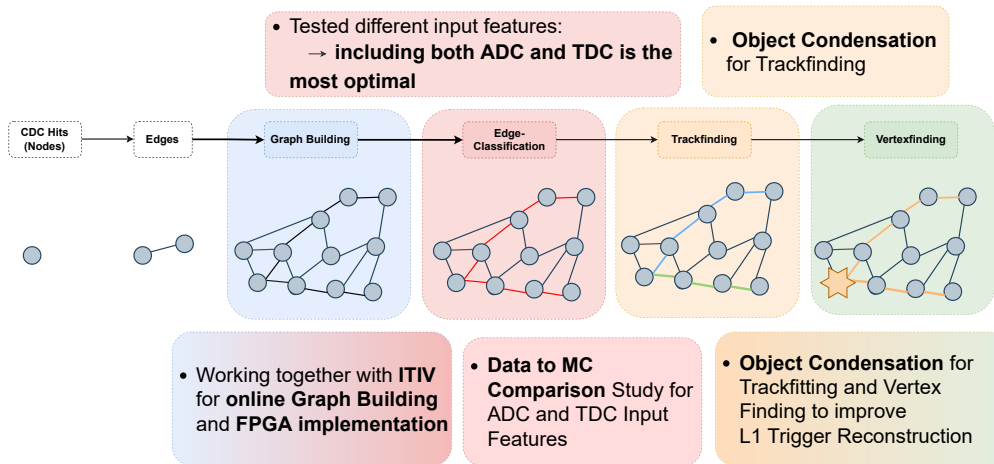
# Summary and Outlook

- **Displaced vertices** relevant for new physics searches
- **L1 Trigger reconstruction** needs to be improved

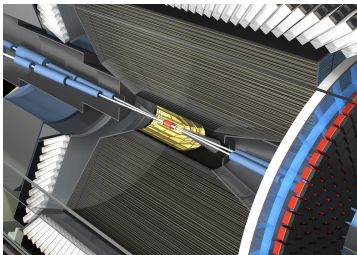


# Summary and Outlook

- **Displaced vertices** relevant for new physics searches
- **L1 Trigger reconstruction** needs to be improved



# Central Drift Chamber (CDC)



- Sense wires are arranged around the beamline (z-axis) to measure charged particles
- z Information gathered from stereo layers
- Events with displacement  $\rho > 16.0$  cm start within the CDC

→ Focus on track reconstruction using the CDC information

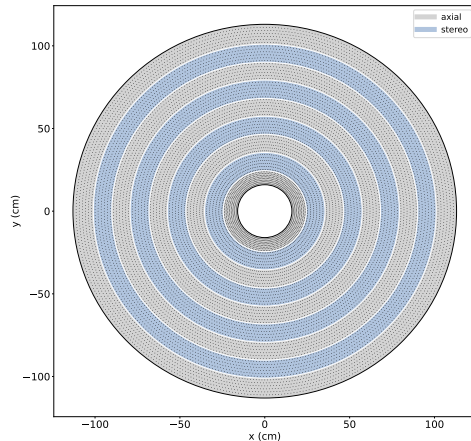


(a) An axial wire layer - sense wires are parallel to the beamline



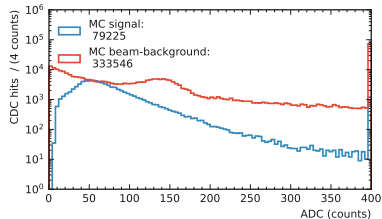
(b) A stereo wire layer - sense wires are skewed to the beamline (exaggerated)

CDC x-y view

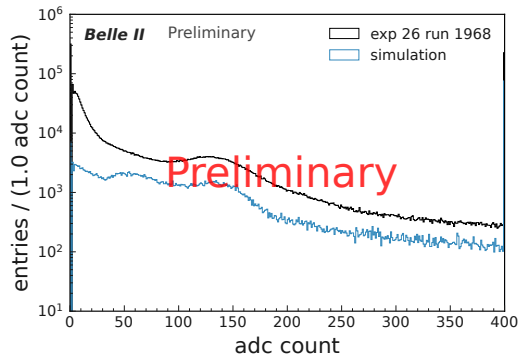
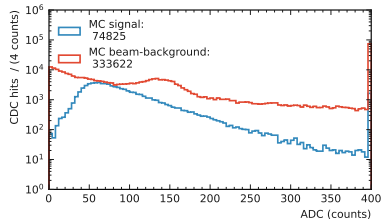


# Preliminary Data to MC ADC Overlay

$e^+e^- \rightarrow A'h', h' \rightarrow \mu^+\mu^-, m(h')=2.0\text{ GeV}$   
(run-independent early-phase 3)



$e^+e^- \rightarrow \mu^+\mu^-$  (run-independent early-phase 3)



Credit: Philipp Dorwarth, Work in Progress:

- MC ( $e^+e^- \rightarrow \mu^+\mu^-$ , run-independent early-phase 3) not skimmed (hlt\_mumu\_tight\_or\_highm\_calibskim) and not calibrated
- Data (hlt\_mumu\_tight\_or\_highm\_calibskim) only contains exp 26 run 1968

# GNN Evaluation: $F_1$ : Input Feature Studies

Determine binary threshold using maximal  $F_1$  score:  $F_1 = 2 \cdot \frac{\text{precision} \cdot \text{recall}}{\text{precision} + \text{recall}} = \frac{TP}{TP + (FP + FN)/2}$

input features:

$[\rho, \phi]$

Confusion matrix

|            |       | True                                | False                               | Row Sum                              |
|------------|-------|-------------------------------------|-------------------------------------|--------------------------------------|
| Actual     | True  | 36784<br>TP: 14.68%                 | 7465<br>FN: 2.98%                   | 44249<br>TPR: 83.13%<br>FNR: 16.87%  |
|            | False | 9826<br>FP: 3.92%                   | 196459<br>TN: 78.42%                | 206285<br>TNR: 95.24%<br>FPR: 4.76%  |
| Column Sum |       | 46610<br>PPV: 78.92%<br>FDR: 21.08% | 203924<br>NPV: 96.34%<br>FOR: 3.66% | 250534<br>ACC: 93.10%<br>MISS: 6.90% |
|            |       | Predicted                           |                                     |                                      |

$F_1 = 0.81$

input features:

$[\rho, \phi, TDC]$

Confusion matrix

|            |       | True                                | False                               | Row Sum                              |
|------------|-------|-------------------------------------|-------------------------------------|--------------------------------------|
| Actual     | True  | 41499<br>TP: 16.56%                 | 3414<br>FN: 1.36%                   | 44913<br>TPR: 92.40%<br>FNR: 7.60%   |
|            | False | 5111<br>FP: 2.04%                   | 200510<br>TN: 80.03%                | 205621<br>TNR: 97.51%<br>FPR: 2.49%  |
| Column Sum |       | 46610<br>PPV: 89.03%<br>FDR: 10.97% | 203924<br>NPV: 98.33%<br>FOR: 1.67% | 250534<br>ACC: 96.60%<br>MISS: 3.40% |
|            |       | Predicted                           |                                     |                                      |

$F_1 = 0.91$

input features:

$[\rho, \phi, ADC]$

Confusion matrix

|            |       | True                                | False                               | Row Sum                              |
|------------|-------|-------------------------------------|-------------------------------------|--------------------------------------|
| Actual     | True  | 40465<br>TP: 16.15%                 | 5993<br>FN: 2.39%                   | 46458<br>TPR: 87.10%<br>FNR: 12.90%  |
|            | False | 6145<br>FP: 2.45%                   | 197931<br>TN: 79.00%                | 204076<br>TNR: 96.99%<br>FPR: 3.01%  |
| Column Sum |       | 46610<br>PPV: 86.82%<br>FDR: 13.18% | 203924<br>NPV: 97.06%<br>FOR: 2.94% | 250534<br>ACC: 95.16%<br>MISS: 4.84% |
|            |       | Predicted                           |                                     |                                      |

$F_1 = 0.87$

input features:

$[\rho, \phi, TDC, ADC]$

Confusion matrix

|            |       | True                               | False                               | Row Sum                              |
|------------|-------|------------------------------------|-------------------------------------|--------------------------------------|
| Actual     | True  | 43741<br>TP: 17.46%                | 2760<br>FN: 1.10%                   | 46501<br>TPR: 94.06%<br>FNR: 5.94%   |
|            | False | 2869<br>FP: 1.15%                  | 201164<br>TN: 80.29%                | 204033<br>TNR: 98.59%<br>FPR: 1.41%  |
| Column Sum |       | 46610<br>PPV: 93.84%<br>FDR: 6.16% | 203924<br>NPV: 98.65%<br>FOR: 1.35% | 250534<br>ACC: 97.75%<br>MISS: 2.25% |
|            |       | Predicted                          |                                     |                                      |

$F_1 = 0.94$

# GNN Evaluation per Mass

