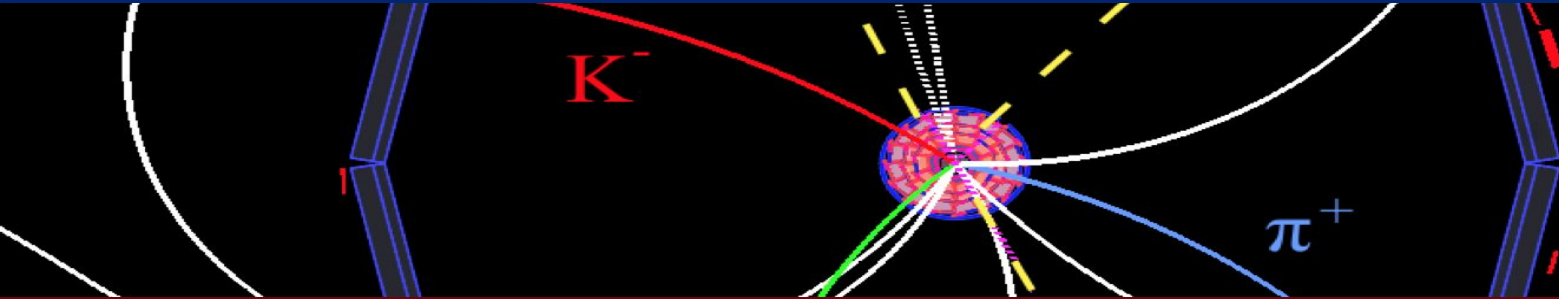


# FEI Brainstorm



**Belle II Physics Week**

December 1st, 2022

**William Sutcliffe**

University of Bonn

# Program

- FEI Task Force, performance and calibrations - Will
- B  $\rightarrow$  D pi calibration and more immediate potential improvements - Vidya
- More on potential FEI improvements for the longer term - Will
- A couple of slides on the FEI training - Will

10 mins discussion after each subsection, feel free to ask questions through out.

# FEI Task Force, FEI Performance, Calibrations

# FEI Task Force

- Confluence: <https://confluence.desy.de/display/BI/FEI+Task+Force>
- Mailing List: [task-fei@belle2.org](mailto:task-fei@belle2.org)
- First meeting: [Indico 16 Nov](#) and in a person meeting here.
- **Aims:**
  - **Immediate: Robust calibration factors for the LS dataset and MC15ri**
  - Key improvements to be discussed later.
- Time frame
  - next 1-2 months for Moriond 2023, 5-6 months for EPS 2023

FEI skims: currently FEI skims exist for  $0.8\alpha b^{-1}$  of generic MC15ri\_b,  $1\alpha b^{-1}$  of continuum MC15ri\_b + the LS1 dataset.

FEI modes	Skim Code
Hadronic B0/B+	11180500
Semileptonic B0/B+	11180600

- Samples:
  - FEI skims MC15ri\_b
- Future aims (3-9 months)
  - Improved MC15 (rd) training with improved simulation.
  - Tuning of particle selections and BDTs
  - Extra B modes.
  - Improved vertex fitting (decay tree fitting)

# FEI Task Force

<https://confluence.desy.de/display/BI/FEI+Task+Force>

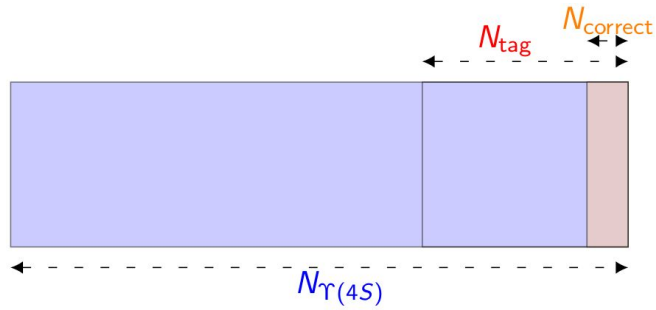
## Calibration and FEI performance efforts

The table below gives a list of people expressed their interest to actively participate in sub-group's activities. Please feel free to modify or add information if needed.

Responsible / interested parties	Tag-side modes	Calibration channel / Performance study	Reference
<a href="#">@William Sutcliffe</a>	Hadronic FEI (B+, B0)	B→Xlnu (inclusive, pl fit)	<a href="#">BELLE2-NOTE-PH-2019-031</a>
<a href="#">@Taichiro Koga</a> <a href="#">@Qidong Zhou</a> <a href="#">@Michele Aversano</a> <a href="#">@William Sutcliffe</a>	Hadronic FEI (B+, B0)	B→D(*)lnu	
<a href="#">@Niharika Rout</a> <a href="#">@Vidya Vobbilisetti</a> <a href="#">@Trabelsi Karim</a>	Hadronic FEI (B+)	B+ → D(*)pi+ (partial reco)	<a href="#">BELLE2-NOTE-PH-2022-002</a>
<a href="#">@Meihong Liu</a> <a href="#">@Trabelsi Karim</a> <a href="#">@Vidya Sagar Vobbilisetti</a>	Hadronic FEI (B0)	B0 → D(*)pi+ (partial reco)	<a href="#">BELLE2-NOTE-PH-2022-046</a>
<a href="#">@William Sutcliffe</a>	Hadronic FEI (B+, B0)	Mbc fitting in Data (ROC curves)	
<a href="#">@Andre Hao Yuan Huang</a> <a href="#">@Kevin Varvell</a>	Semileptonic FEI (B+, B0)	B→D(*) l nu	
	Semileptonic FEI (B+, B0)	B → X l nu (inclusive)	
	Semileptonic FEI (B+, B0)	cos theta BY fits in Data (ROC curves)	

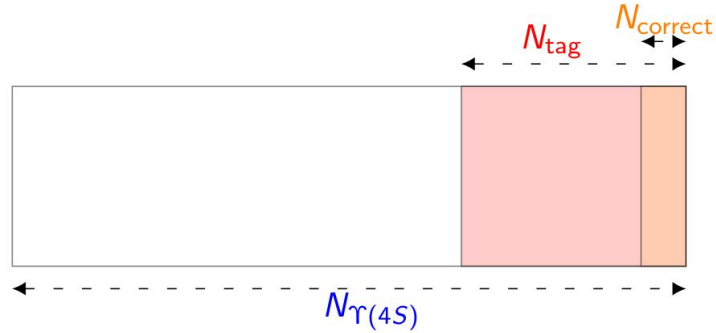
Lacking still some person power for the SL FEI - especially we need cos theta BY fits perhaps also Sydney group (Andre, Kevin et al.) or Markus Roerken

# FEI Performance



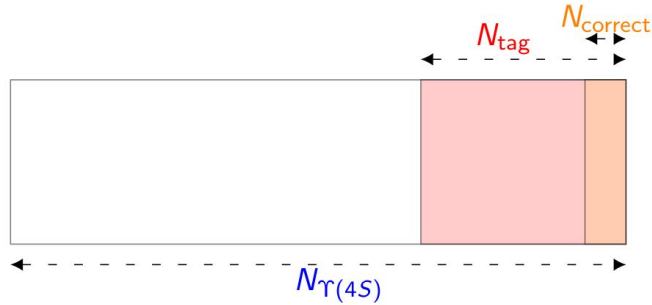
- tagging efficiency =  $N_{tag}/N_{\Upsilon(4S)}$
- tag-side efficiency =  $N_{correct}/N_{\Upsilon(4S)}$

# FEI Performance metrics

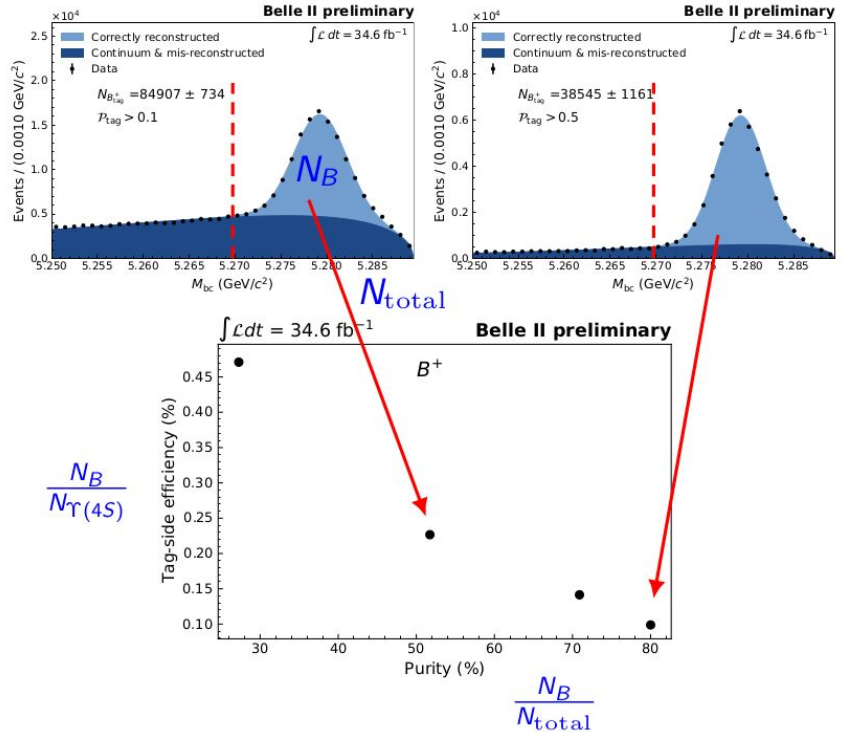


- tagging efficiency =  $N_{tag}/N_{\Upsilon(4S)}$
- tag-side efficiency =  $N_{correct}/N_{\Upsilon(4S)}$
- purity =  $N_{correct}/N_{tag}$

# FEI Performance metrics



- tagging efficiency =  $N_{\text{tag}}/N_{\Upsilon(4S)}$
- tag-side efficiency =  $N_{\text{correct}}/N_{\Upsilon(4S)}$
- purity =  $N_{\text{correct}}/N_{\text{tag}}$

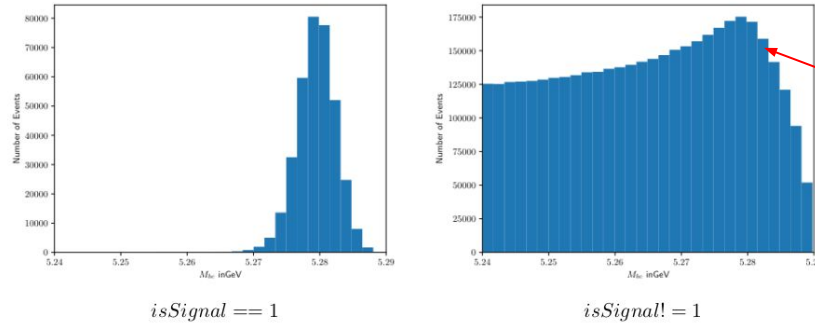


- Aim: Tag-side efficiency vs purity for both hadronic and semileptonic tag-sides.
- High priority of Moriond 2023 and EPS 2023 but not critical like calibrations.



# Big Issue: How is a correct tag-side defined?

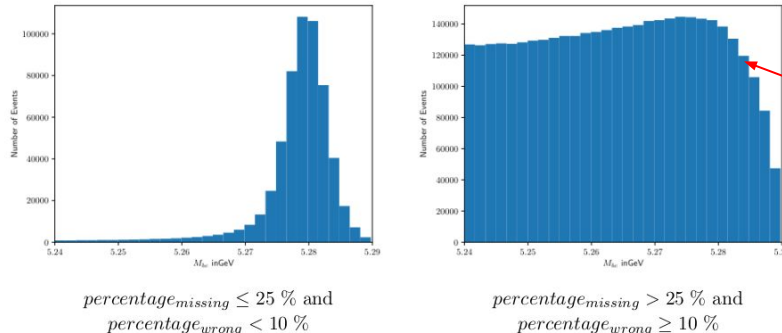
- Issues arise regarding the definition of a correct tag.
- Good example of this from Noreen Rauls below.
- She implemented basf2 variables for the % of wrong and missing tag-sides.



“Bad tags” peak

Note: Noreen, Ariane, Racha and Will  
[BELLE2-NOTE-TE-2021-026](#)

FIG. 13:  $M_{bc}$  distribution for all  $B^0$  FEI decay modes by applying the provided cut.

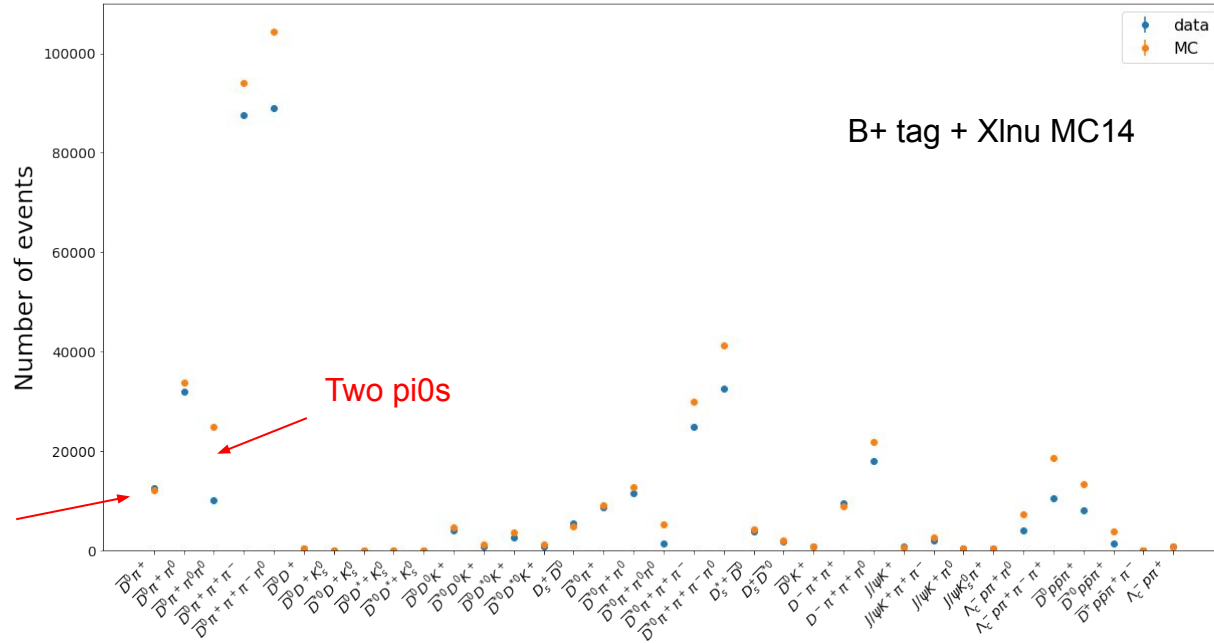


“Bad tags” peak better using new variables:  
 $percentage_{MissingParticlesBTag}$   
 $percentage_{WrongParticlesBTag}$

One can also use mcErrors as done for Xs  
gamma [BELLE2-NOTE-PH-2022-021](#)

FIG. 17:  $M_{bc}$  distribution for all  $B^0$  FEI decay modes by applying the provided cut.

# The need for calibrations

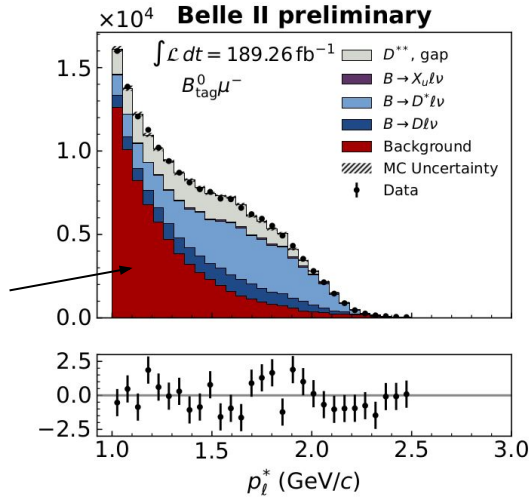
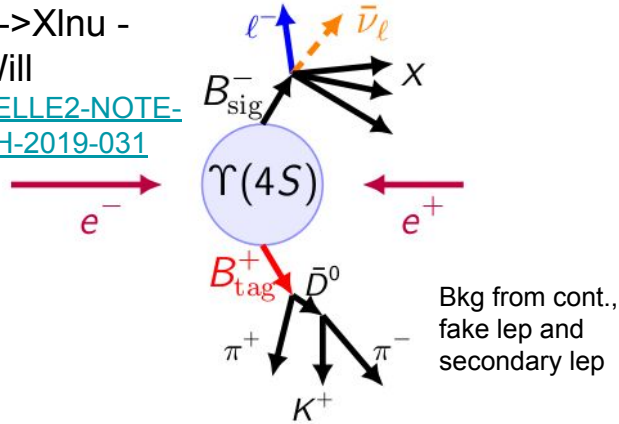


- The algorithm requires independent calibrations for SL and hadronic tag-sides due to the data-MC efficiency mismatch.
- $\varepsilon = \frac{N^{\text{Data}}_{\text{cal channel}}(\text{sig prob bin, tag decay mode})}{N^{\text{MC}}_{\text{cal channel}}(\text{sig prob bin, tag decay mode})}$
- Several calibration channels -> need for combination and application framework eventually.

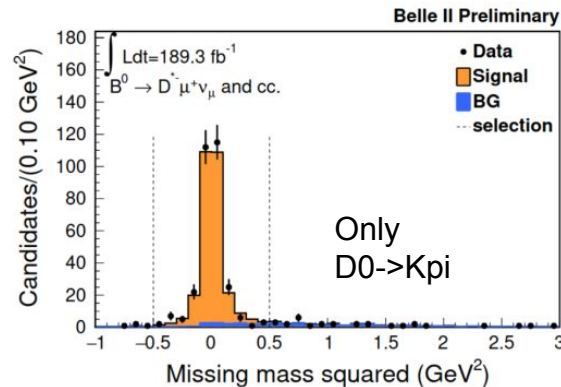
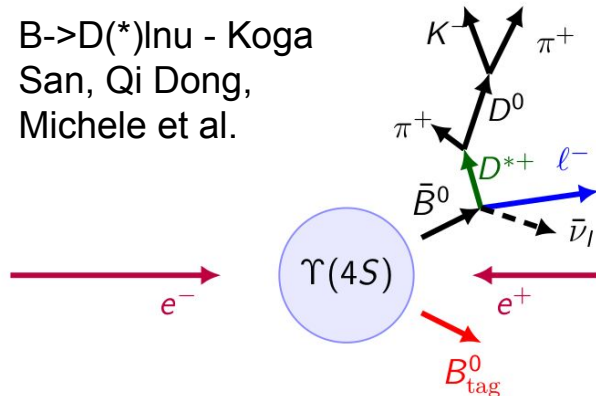
# Current Calibration Channels

B->Xlnu - Will

[BELLE2-NOTE-PH-2019-031](#)



B->D(\*)lnu - Koga San, Qi Dong, Michele et al.

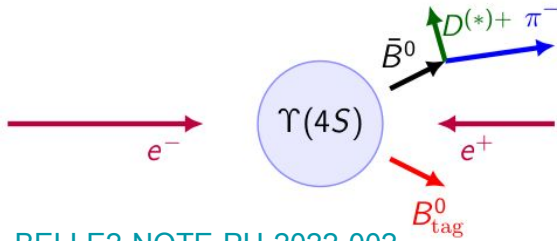


- High BF (~20%) + single lepton -> lots of Stats
- Only a single lepton so B0 / B+ cross feed issues
- Dominating systematic from the B-> Xlnu BF 3%
- Discrepancy seen between e and mu

- Very pure but lower stats due to D BF coverage.
- Reconstructed D\*+ l nu constrains B+ / B0
- Discrepancy seen between e and mu
- slow pions for D\*

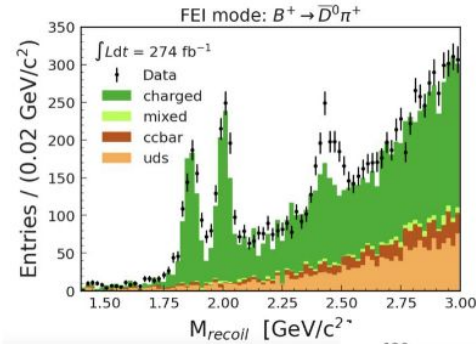
# Current Calibration Channels

Partial reco D pi / D\* pi - Vidya, Niharika, Karim et al.



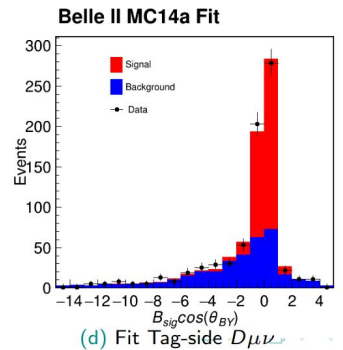
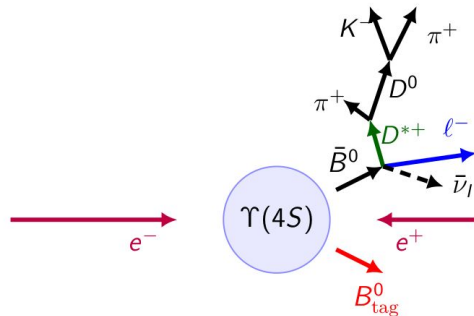
[BELLE2-NOTE-PH-2022-002](#)

[BELLE2-NOTE-PH-2022-046](#)



- Lower had. branching fraction however partial reconstruction helps boost efficiency -> Moderate stats
- Orthogonal dominating systematic effects (e.g no LID)
- Potential cross feedfeed between tag-side and the signal side. E.g swapped pi+
- B+ (B0)->D pi BF uncertainty ~ 3% (5%) similar for D\* pi

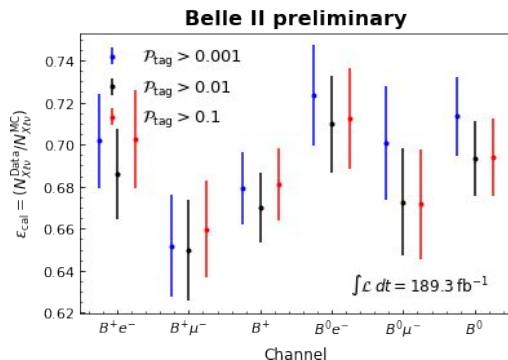
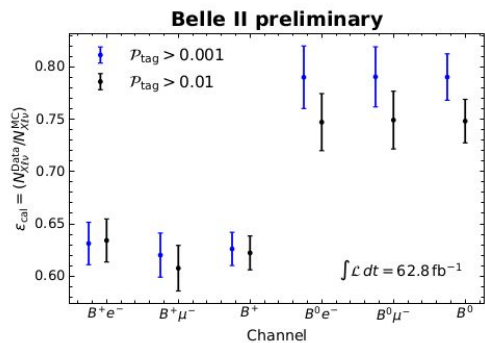
SL Tagging + B->D(\*) l nu- Andre, Chia-Ling and Kevin



- Low - moderate stats
- Issues with peaking background however reasonable purity.
- Could be signal - calibration correlations as both are semileptonic.

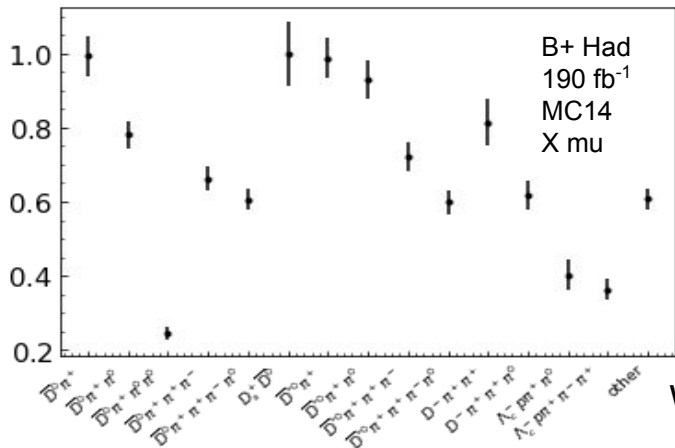
# Example of hadronic tag-side cal. factors

Old format: average cal. factor across tag-side modes

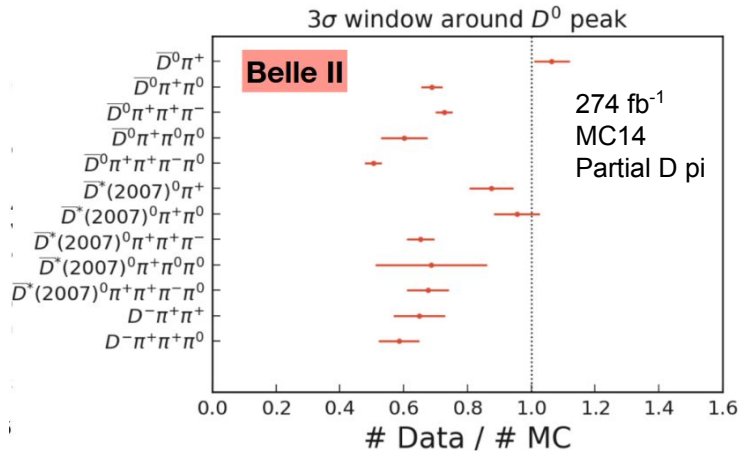


Will

Future format: calibration factors for decay modes, some grouping required



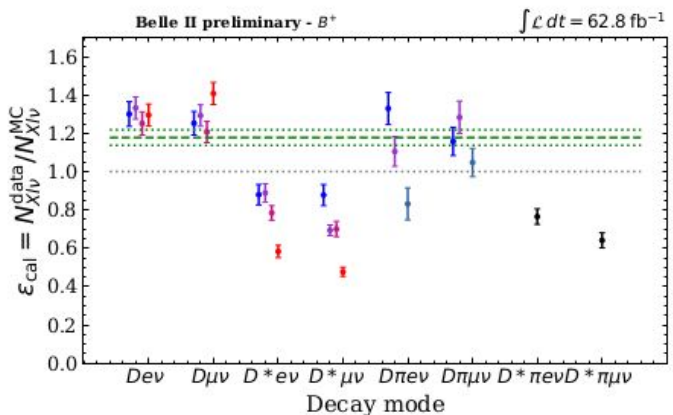
Will



Vidya,  
Niharika,  
Karim et al.

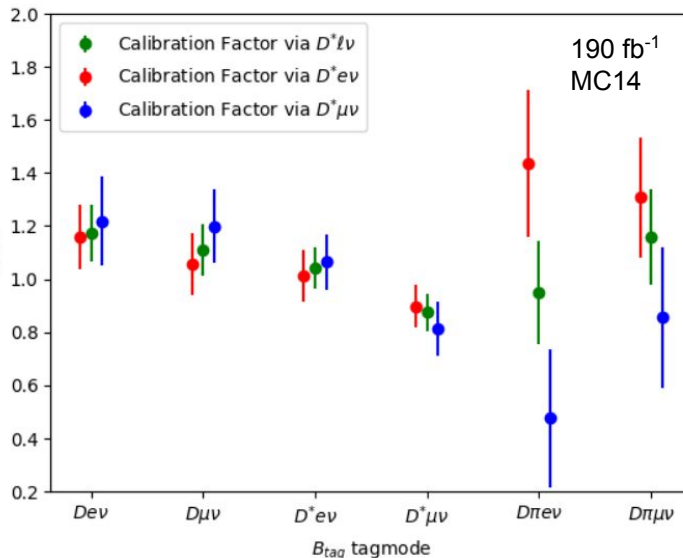
# Example of SL tag-side cal. factors

Old format: split by SL tag-side decay mode



Alina Mantei, Will, Peter et al.

- no more person power



Andre, Kevin and Chia-Ling

**New format:** split by SL tag-side decay mode, Sig prob cuts 0.001, 0.01, 0.1

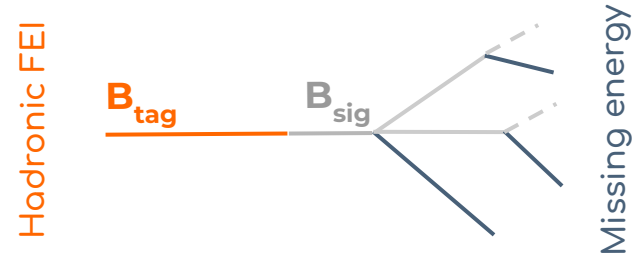
# Key Calibration questions

As Peter said users must follow the same key tag-side selection choices of calibrations

- **Which tag-side cuts ?**
  - Had:  $M_{bc} > 5.27$ ,  $-0.15 < \Delta E < 0.1$
  - SL:  $p_1^* > 1 \text{ GeV}/c$ ,  $X < \cos \theta_{BY} < Y$
- **Tag-side Best Candidate selection**
  - Highest sig prob. (Caveats which will be explained later)
- **Continuum suppression?**
  - $\cos \theta_{TBO} < 0.9$  (in the past Fox Wolfram R2 however this is poorly modelled)
- **Granularity of the calibration?**
  - In bins of decay mode for high stat. Modes.
  - Various sig. Prob cuts or bins? At least 0.001, 0.01 and 0.1. (Again caveats later)
- **Other Ideas?**
  - Simultaneous fitting of good and bad tags in the calibration.
  - Double tagging, SL + had. Signal side

**Break for discussion (~10 mins)**

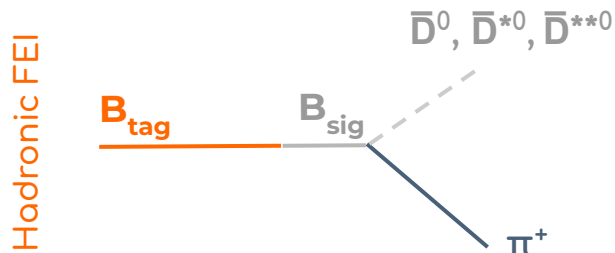
# Calibration and first round of improvements with $B \rightarrow D \pi$ samples



Gaetano de Marino, Meihong Liu (Fudan), Niharika Rout (Trieste),  
Karim Trabelsi, Vidya Sagar Vobbiliseti

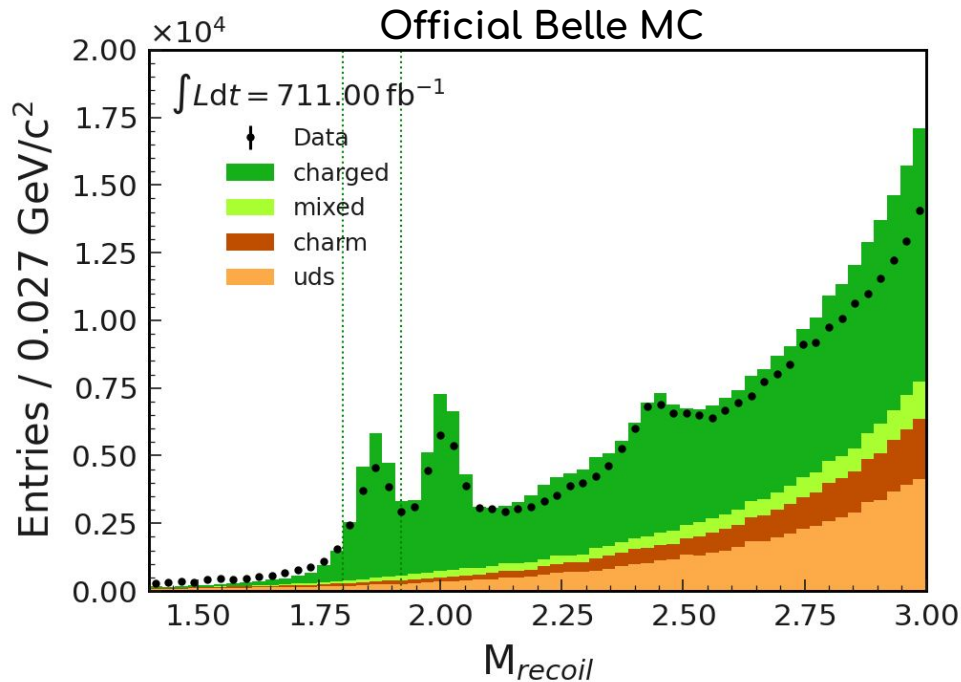


# Partial reconstruction for more statistics!



We can look for  $D^0, D^{*0}$  and even  $D^{**0}$  in the recoil mass of a fully reconstructed B and a  $\pi^\pm$

Within a narrow region around the peak, we know that one B decays to  $D^0\pi^+$  and we can study the other B (decaying hadronically)



~16k events in a  $3\sigma$  window around each peak in data.  
 Roughly  $\frac{1}{3}$  statistics of  $X_c \text{ lv}$  sample, but much smaller systematic.  
[\[BELLE2-NOTE-PH-2021-029, Belle note bn1615\]](#)

# Calibration factors per mode

with PDG uncertainties

$3\sigma$  window around  $D^0$  peak

Overall calibration factor:  
 $(82.6 \pm 0.9)\%$

$$\int L dt = 711 \text{ fb}^{-1}$$

— PDG uncertainty

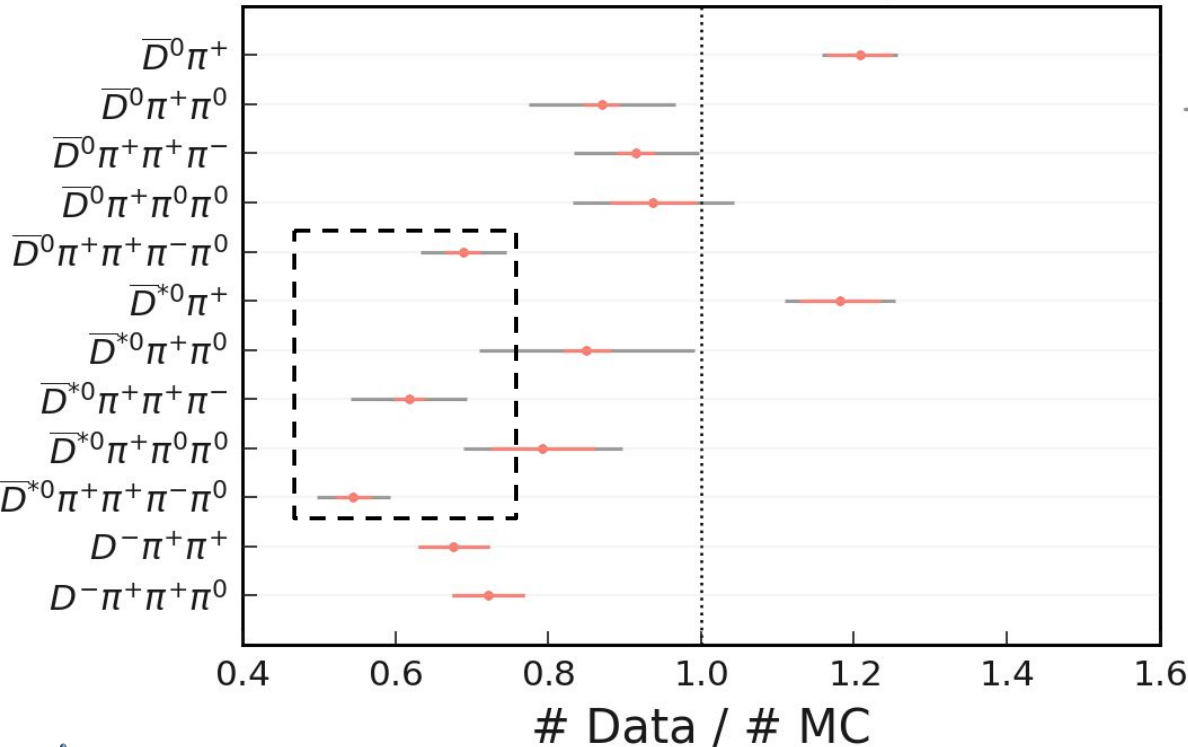
— Official MC

Modes with high multiplicity have large calibration factors! Even ~50%!

Even after considering PDG uncert, MC is clearly overestimating.

But the issue is not just in scaling, but also in the intermediate resonances to get to these final states.

⇒ We need a model for Hadronic B decays ! (a well educated and coherent update of DECAY table)<sup>18</sup>



# Case study: $B^+ \rightarrow \bar{D}^0 \pi^+ \pi^+ \pi^-$

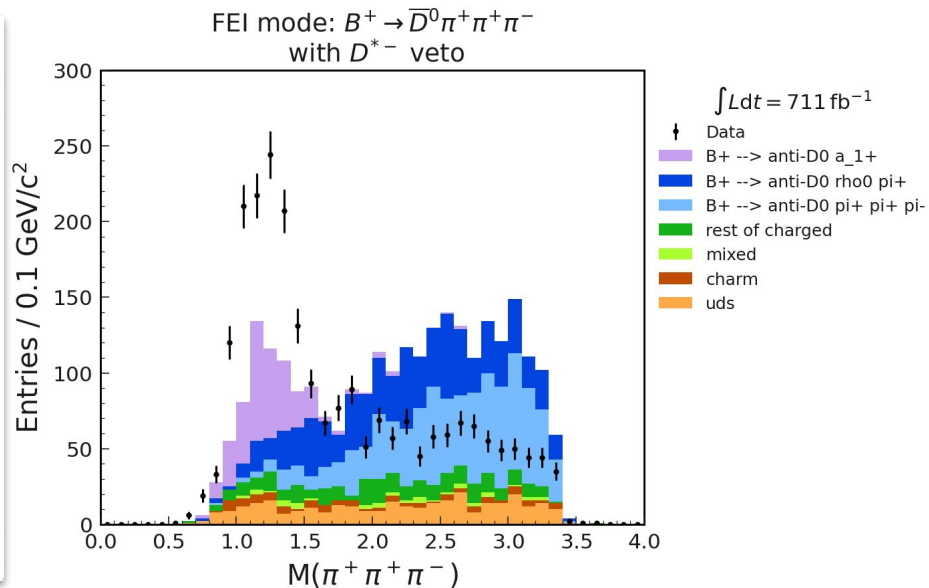
Improving calibration factors is not our primary target, instead improving the invariant masses (of intermediate particles), which are used as training variables in FEI will impact efficiency and purity

TABLE VI: Contents of the DECAY file concerning the  $B^+ \rightarrow \bar{D}^0 \pi^+ \pi^+ \pi^-$  final state and corresponding measurements in PDG [in %].

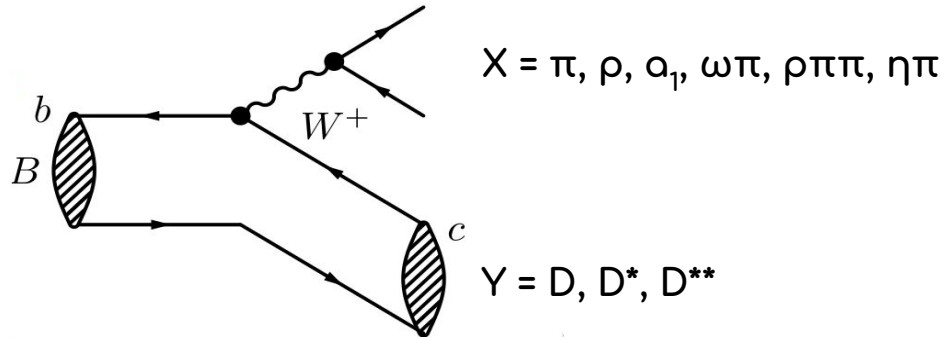
Decay	Belle	Belle II	Marker	Ref
$B^+ \rightarrow \bar{D}^0 \pi^- \pi^+ \pi^+$	0.46	0.51	■	[8]
$B^+ \rightarrow \bar{D}^0 \rho(770)^0 \pi^+; \rho(770)^0 \rightarrow \pi^+ \pi^-$	0.39	0.42	★	[8]
$B^+ \rightarrow \bar{D}^0 a_1(1260)^+; a_1(1260)^+ \rightarrow \rho(770)^0 \pi^+; \rho(770)^0 \rightarrow \pi^+ \pi^-$	0.13	0.14	★	[8]
$B^+ \rightarrow \bar{D}^0 a_1(1260)^+; a_1(1260)^+ \rightarrow f_0(500) \pi^+; f_0(500) \rightarrow \pi^+ \pi^-$	0.05	0.05	★	[8]
$B^+ \rightarrow \bar{D}_1(2420)^0 \pi^+; \bar{D}_1(2420)^0 \rightarrow D^*(2010)^- \pi^+; D^*(2010)^- \rightarrow \bar{D}^0 \pi^-$	0.04	0.02		[10], [9]
$B^+ \rightarrow \bar{D}_1(2430)^0 \pi^+; \bar{D}_1(2430)^0 \rightarrow D^*(2010)^- \pi^+; D^*(2010)^- \rightarrow \bar{D}^0 \pi^-$	0.03	0.02		[10], [9]
$B^+ \rightarrow \bar{D}_2^*(2460)^0 \pi^+; \bar{D}_2^*(2460)^0 \rightarrow D^*(2010)^- \pi^+; D^*(2010)^- \rightarrow \bar{D}^0 \pi^-$	0.01	0.01		[10], [9]
$B^+ \rightarrow D^*(2010)^- \pi^+ \pi^+; D^*(2010)^- \rightarrow \bar{D}^0 \pi^-$	-	0.09	■	[10]
$B^+ \rightarrow \bar{D}^0 a_1(1260)^+; a_1(1260)^+ \rightarrow \pi^+ \pi^+ \pi^-$	-	0.07	★	[8]
$B^+ \rightarrow \bar{D}_1(2420)^0 \pi^+; \bar{D}_1(2420)^0 \rightarrow \bar{D}^0 \pi^- \pi^+$	-	0.02		[10], [9]
$B^+ \rightarrow \bar{D}^0 K^*(892)^+; K^*(892)^+ \rightarrow K^0 \pi^+; K^0 \rightarrow K_S^0; K_S^0 \rightarrow \pi^+ \pi^-$	-	0.01		
Rest of Exclusive	0.03	0.03		
Sum of Exclusive	1.12	1.38		
Sum of PYTHIA	0	0		
Total Sum	1.12	1.38		

[\[BELLE2-NOTE-PH-2022-002\]](#)

By restudying the CLEO and LHCb measurements for this mode, we realized that the NR and  $\rho$  components should be almost 0 and should be dominated by  $a_1^+$



# Model for $B \rightarrow D^{(*,**)} \eta\pi \rho\pi^0$ decays



Happens through 2 channels, one with spectator quarks (call Y) and one from the W (call X).

We want to modify the DECAY table to latest PDG/paper interpretations and this model to see the impact.

2 primary rules:

- $D^0 X : D^{*0} X : D^{**0} X \sim 1 : 1 : 1$   
(based on observation from  $D \pi^- : D^* \pi^- : D^{**} \pi^-$  and  $D \rho^- : D^* \rho^-$ )
- $Y \pi^- : Y \rho^- : Y a_1^- \sim 1 : 2.5 : 2.5$   
(based on predictions and confirmed with  $\tau \rightarrow h \nu$  decays)

Essentially validation, we do not want to fine-tune (except set 0 there is no signal\*).

Additional information:

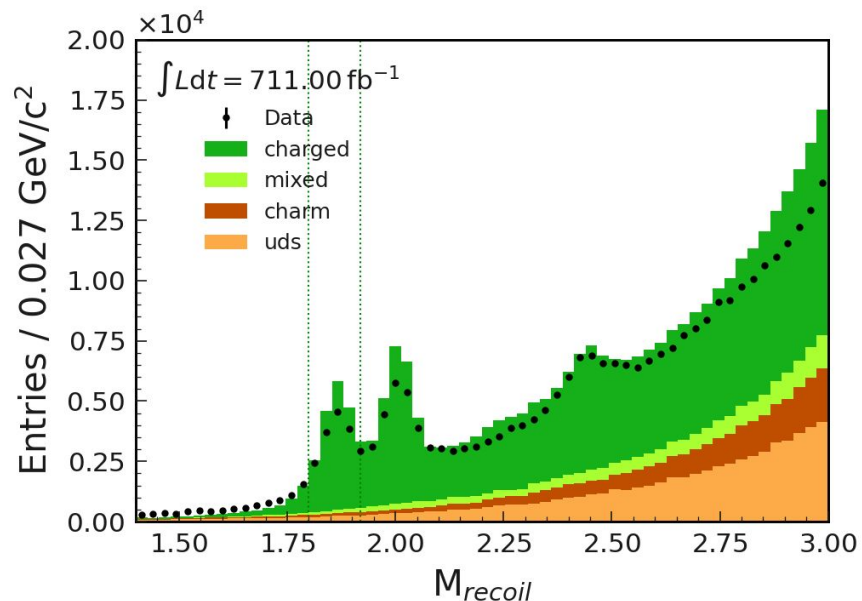
- $3\pi \pi^0$  is hard to model without some sort of  $\rho'$  resonance
  - For  $\omega\pi$  we fix from measurements.
  - For  $\rho\pi\pi$  and  $\eta\pi$ , we let PYTHIA generate it.
- Decays of  $D^{**}$  particles is synchronized with Belle II
- The fraction of 4 different  $D^{**}$  is fixed based on observations.

\*See backup

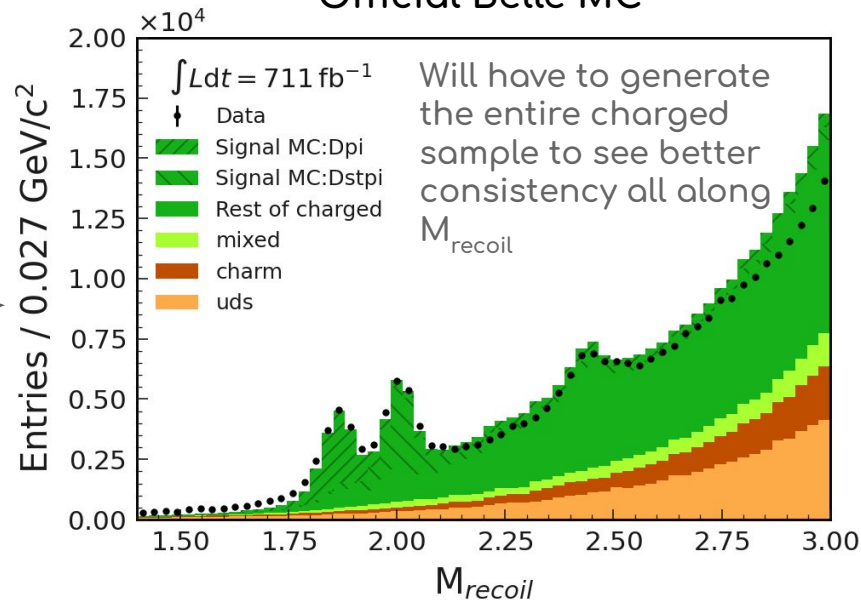
# Validation by embedding signal MC

To quickly study the impact of the modified DECA.Y.DEC file, generated Signal MC of  $B \rightarrow D^{(*)}\pi$  (other B decays updated) and replaced corresponding events in the generic Charged MC:

Official Belle MC



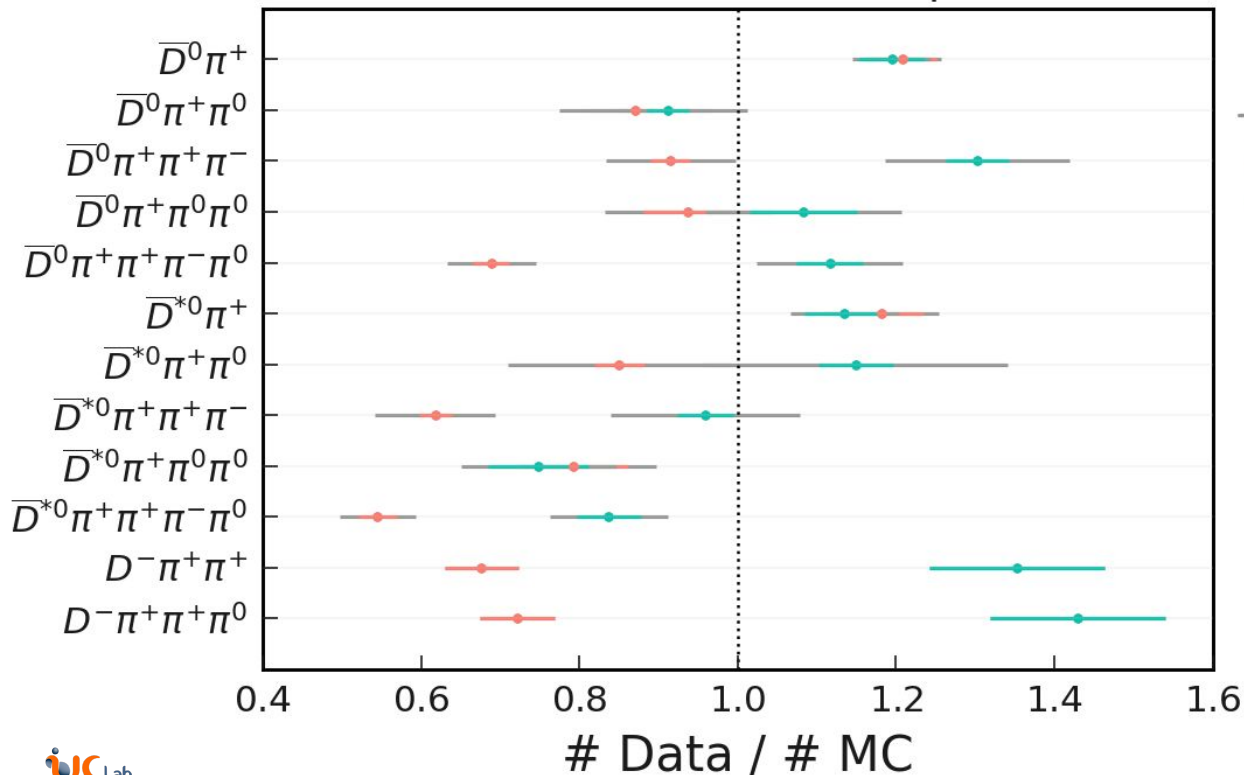
Modified Signal MC embedded in Official Belle MC



# Updated calibration factors

per mode

$3\sigma$  window around  $D^0$  peak



$\int L dt = 711 \text{ fb}^{-1}$

- PDG uncertainty
- Official MC
- Proposed MC

Overall calibration factor:

$(82.6 \pm 0.9)\%$

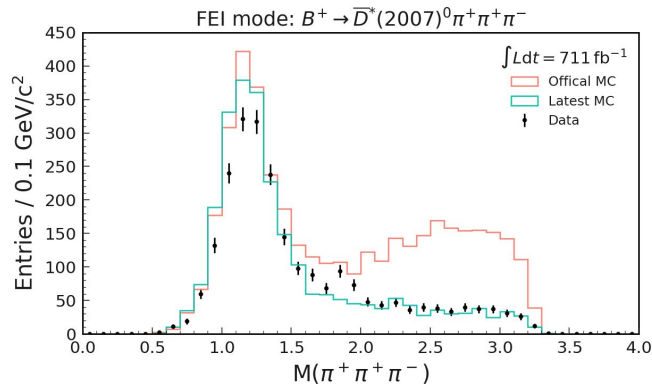
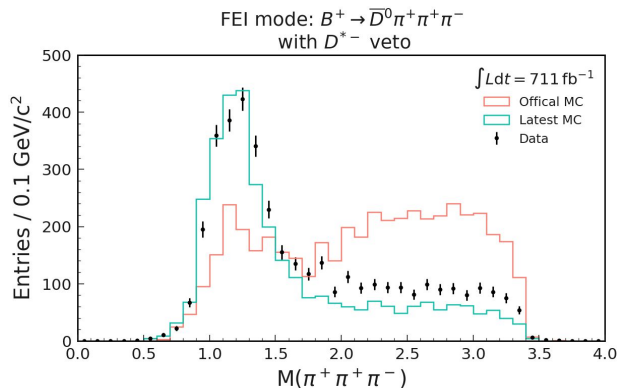


$(104.2 \pm 1.2)\%$

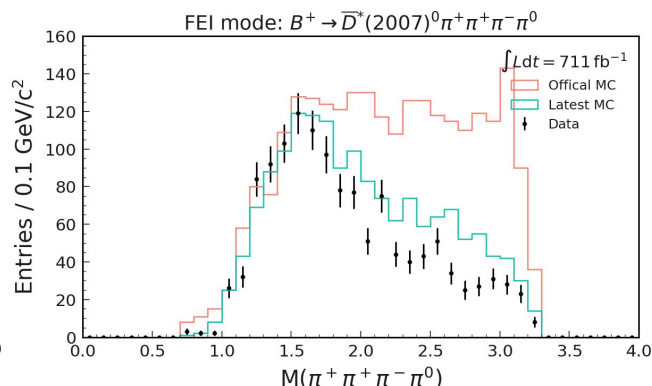
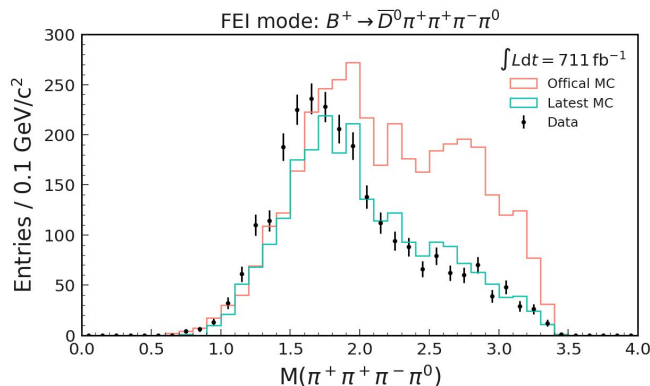
# Decay description is improved!

The improvement is not limited to calibration factors, but more importantly in the invariant masses (of intermediate particles), which are used as training variables in FEI

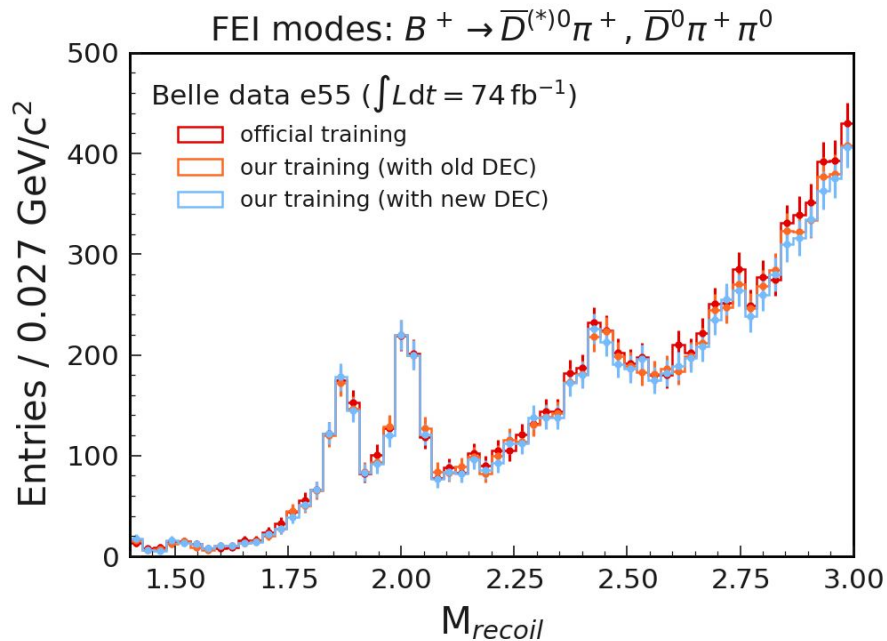
$3\pi^\pm$  case:



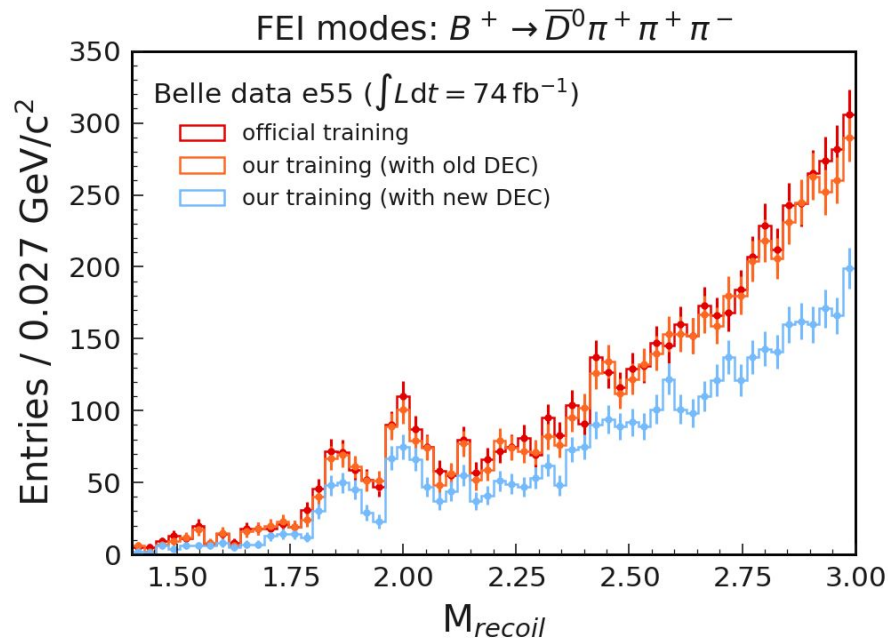
$3\pi^\pm \pi^0$  case:



# Retraining FEI: Validation



Nothing changes in the FEI modes where we did not change anything.

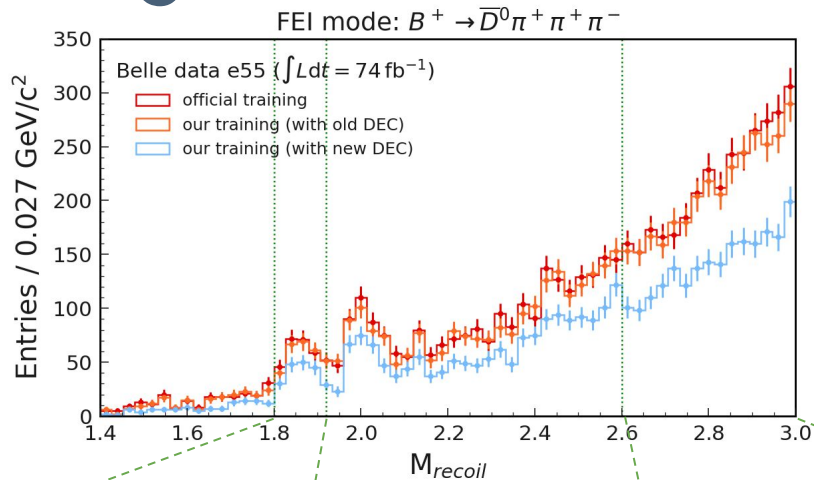


There is a significant background reduction in FEI modes where MC model is improved.

Our training has some issues while reconstructing modes with  $\pi^0$ , under investigation... (see backup) 14



# Retraining FEI: Effective cuts

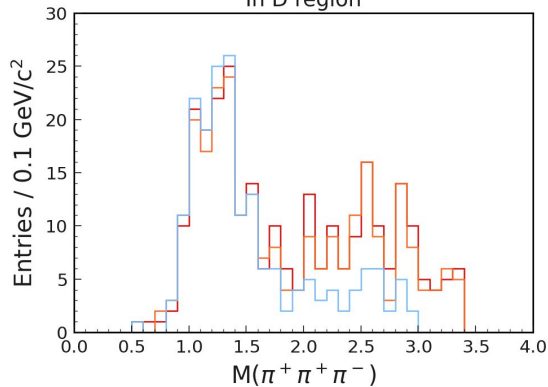


The new training is effectively applying a  $a_1^+$  cut!

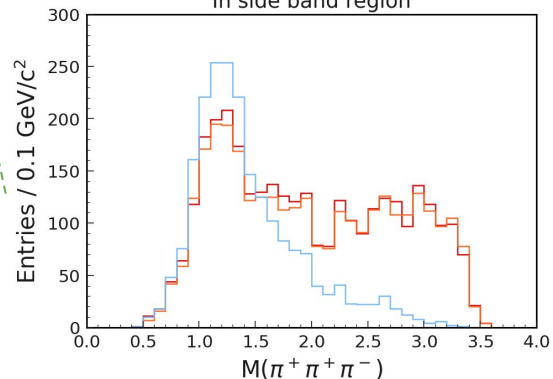
Can we apply this cut manually?  
Is that enough?

Can we have a fully cut-based B-tagging? i.e., no training?

In D region

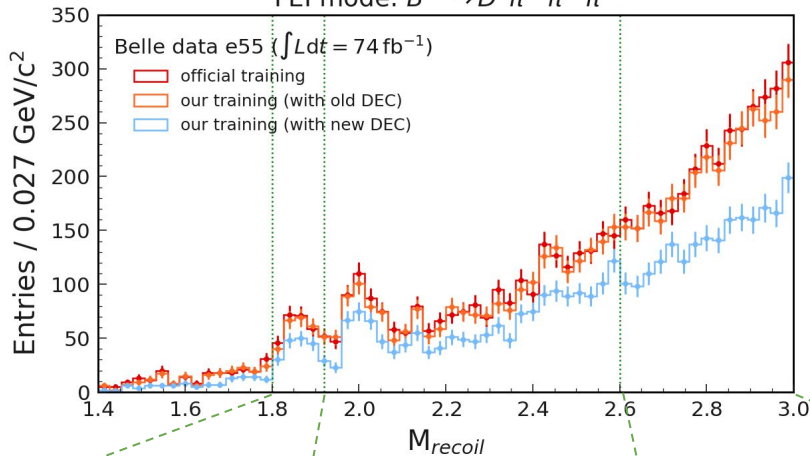


In side band region

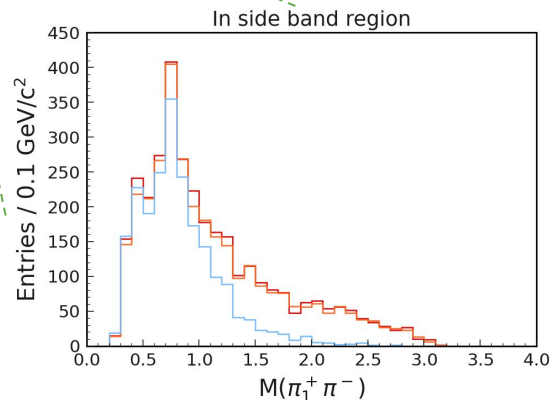
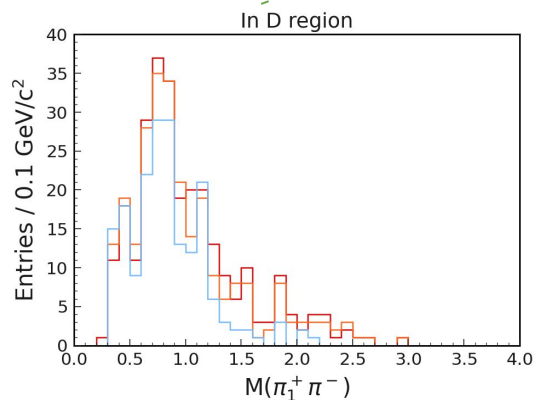


# Retraining FEI: Effective cuts

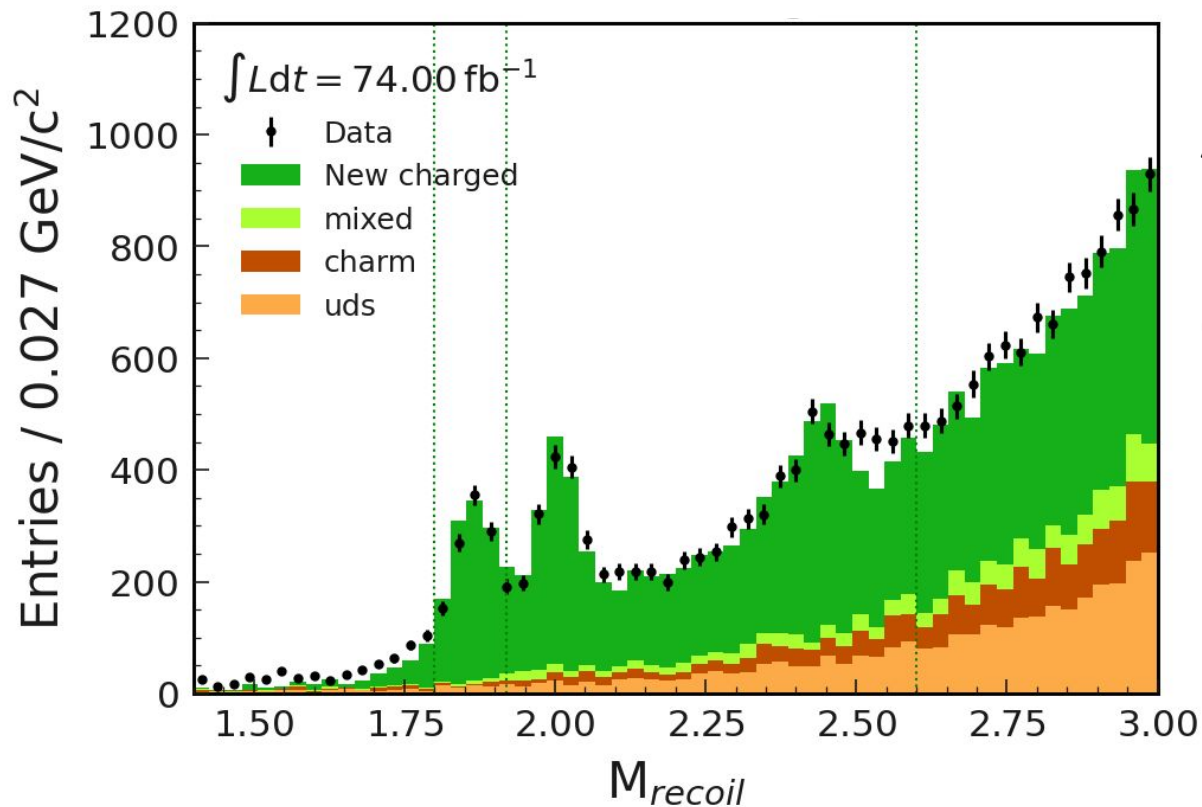
FEI mode:  $B^+ \rightarrow \bar{D}^0 \pi^+ \pi^+ \pi^-$



$M(3\pi)$  is the dimension we usually look at, but the changed kinematics is visible in other dimensions like  $M(2\pi)$  also.



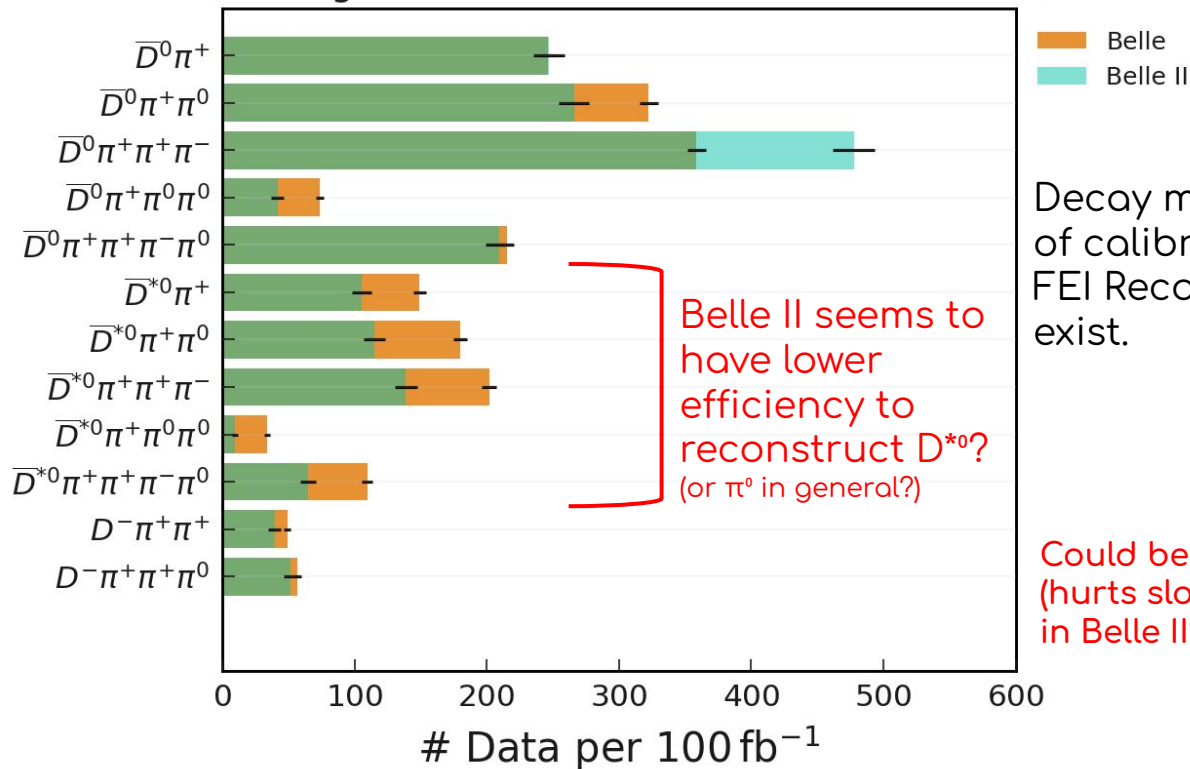
# Retraining FEI: Data-MC agreement



After reconstructing all MC and data with the training based on new DEC, the Data - MC agreement improves too! (even at higher  $M_{recoil}$  !)

# What can we learn by comparing Belle and Belle II?

Counting in  $3\sigma$  window around  $D^0$  in recoil side



Decay model may not be the only source of calibration factor?  
FEI Reconstruction effects certainly also exist.

Could be because of tighter  $\gamma$  cuts (hurts slow  $\pi^0$ ) in Belle II?

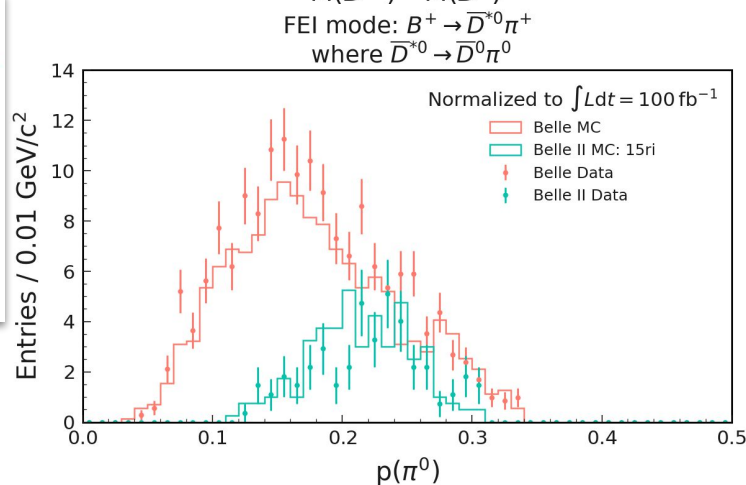
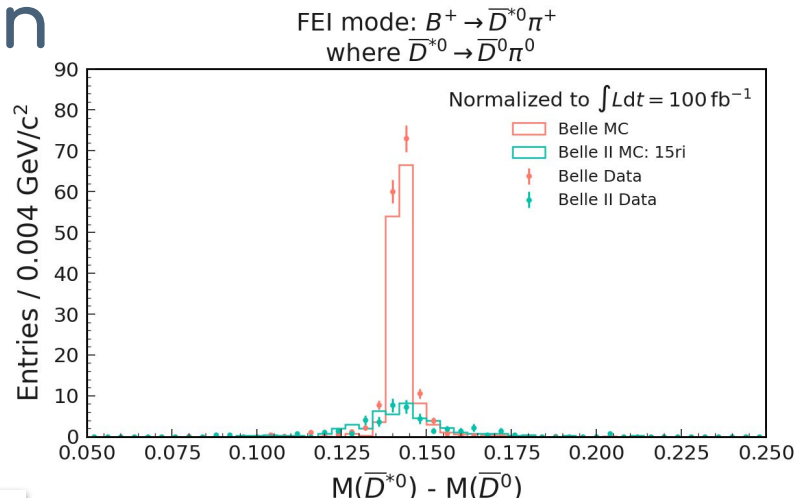
# $D^{*0} \rightarrow D^0 \pi^0$ reconstruction

In Belle II, the yield of  $D^{*0} \rightarrow D^0 \pi^0$  is much worse than Belle.

$E > 0.09$  GeV cut for  $\gamma$  is too tight for slow  $\pi^0$   
Should be loosened.

```
if convertedFromBelle:
    gamma_cut = 'goodBelleGamma == 1 and clusterBelleQuality == 0'
else:
    gamma_cut = '[[clusterReg == 1 and E > 0.10] or [clusterReg == 2 and E > 0.09] or [clusterReg == 3 and E > 0.16]]'
if specific:
    gamma_cut += ' and isInRestOfEvent > 0.5'

gamma = Particle('gamma',
    MVAConfiguration(variables=['clusterReg', 'clusterNHits', 'clusterTiming', 'extraInfo(preCut_rank)',
                               'clusterE9E25', 'pt', 'E', 'pz'],
                     target='isPrimarySignal'),
    PreCutConfiguration(userCut=gamma_cut,
                       bestCandidateMode='highest',
                       bestCandidateVariable='E',
                       bestCandidateCut=40),
    PostCutConfiguration(bestCandidateCut=20, value=0.01))
gamma.addChannel(['gamma:FSP'])
```



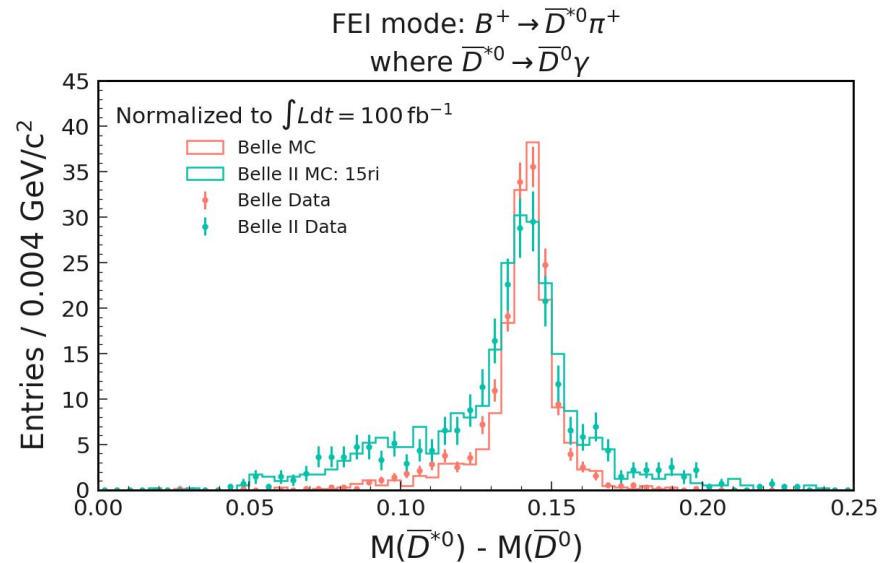
# $D^{*0} \rightarrow D^0 \gamma$ reconstruction

In Belle II, the yield of  $D^{*0} \rightarrow D^0 \pi^0$  is much worse than Belle, because the tighter pre-cuts on  $\gamma$  hurts slow  $\pi^0$  reconstruction.

A part of it is recovered in the tail of  $D^{*0} \rightarrow D^0 \gamma$ , but not ideal.

This also shows that a tight  $\Delta M$  constraint, which could bring high purity is not effectively utilized.

Should tighten the  $\Delta M$  pre-BDT cut?



# “Light” plans before summer

- Provide calibration factors for Moriond: Fitting, systematics and ROC with  $D\pi$  sample
- First round of improvements:
  - Retraining with updated MC model (DEC files):
    - Generate (2 streams of) run-dependant charged MC with proposed DEC file for:
      - for Belle and,
      - MC15rd with rel-06 for Belle II.
    - Debug slow- $\pi^0$  reconstruction to fix  $D^{*0}$  yield in Belle II
    - Remove  $\Delta E$  from Hadronic B-training, which is being sculpted by BDTs (This is essential to recover some broken Bs from shifted  $\Delta E$  bin.)

Other potential FEI algorithm  
improvements in the longer term



# Improving the FEI - Particle selections, features

- The bases selections of the FEI could do with tuning
  - Charged tracks:  $[dr < 2]$  and  $[abs(dz) < 4]$
  - Gammas:  $[[clusterReg == 1 \text{ and } E > 0.10]$  or  $[clusterReg == 2 \text{ and } E > 0.09]$  or  $[clusterReg == 3 \text{ and } E > 0.16]$
  - Pi0s:  $0.08 < InvM < 0.18$
  - Jpsi:  $2.6 < M < 3.7$
  - Kshorts:  $0.4 < M < 0.6$ , Lamdas:  $0.9 < M < 1.3$
  - D and D+:  $1.7 < M < 1.95$ , Ds+  $1.68 < M < 2.1$  , Lc:  $2.2 < M < 2.4$
  - D\*0, D\*+, Ds\* :  $0 < Q < 0.3$
  - B+ and B0:  $M_{bc} > 5.2$  and  $abs(deltaE) < 0.5$
- Possible improvements could be:
  - Tuning the simple gamma preselection
  - Multiple types of particles e.g new fei lists for charged and neutral slow pions including gammas for slow pi0s

**Q. Do the various particle experts have recommendations?**

# Improving the FEI - Particle selections, features

- Charged particles:

```
chargedVariables = ['electronID', 'kaonID', 'protonID', 'muonID',  
                  'p', 'pt', 'pz', 'dr', 'dz', 'chiProb', 'extraInfo(preCut_rank)']
```

- Gammas

Introduction of new lepton / hadron ID MVAs ?

```
variables=['clusterReg', 'clusterNHits', 'clusterTiming', 'extraInfo(preCut_rank)',  
          'clusterE9E25', 'pt', 'E', 'pz'],
```

- Pi0s

Here we should we consider adding beam background and hadronic splitoff MVAs ?

```
variables=['InvM', 'extraInfo(preCut_rank)', 'chiProb', 'abs(BellePi0SigM)',  
          'daughterAngle(0,1)', 'pt', 'pz', 'E'],
```

- Ks0 and Lambdas

Separate BDT for slow pions

```
variables=['dr', 'dz', 'distance', 'significanceOfDistance', 'chiProb', 'M', 'abs(dM)',  
          'useCMSFrame(E)', 'daughterAngle(0,1)',  
          'cosAngleBetweenMomentumAndVertexVector',  
          'extraInfo(preCut_rank)', 'extraInfo(goodKs)', 'extraInfo(ksnbVLike)',  
          'extraInfo(ksnbNoLam)', 'extraInfo(ksnbStandard)'],
```

# Improving the FEI - Particle selections, features

- Intermediates:

```
# variables for D mesons and J/Psi
```

```
intermediate_vars = ['daughterProductOf(extraInfo(SignalProbability))', 'daughter({},extraInfo(SignalProbability))',  
                    'chiProb', 'daughter({}, chiProb)', 'extraInfo(preCut_rank)', 'abs(dM)',  
                    'useRestFrame(daughter({}, p))',  
                    'useRestFrame(daughter({}, distance))',  
                    'decayAngle({})', 'daughterAngle({},{})', 'cosAngleBetweenMomentumAndVertexVector',  
                    'daughterInvariantMass({},{})', 'daughterInvariantMass({}, {}, {})', 'daughterInvariantMass({}, {}, {}, {})',  
                    'daughterInvariantMass({}, {}, {}, {}, {})', 'dQ', 'Q', 'dM', 'daughter({},extraInfo(decayModeID))']
```

- Had Bs:

```
# note: these should not be correlated to Mbc (weak correlation of deltaE is OK)
```

```
B_vars = ['daughterProductOf(extraInfo(SignalProbability))', 'daughter({},extraInfo(SignalProbability))',  
          'chiProb', 'daughter({}, chiProb)', 'extraInfo(preCut_rank)',  
          'useRestFrame(daughter({}, p))',  
          'useRestFrame(daughter({}, distance))',  
          'decayAngle({})', 'daughterAngle({},{})', 'cosAngleBetweenMomentumAndVertexVector',  
          'dr', 'dz', 'dx', 'dy', 'distance', 'significanceOfDistance', 'deltaE', 'daughter({},extraInfo(decayModeID))']
```

As Vidya mentioned immediate plan to remove deltaE as loosely correlated to sig. prob.

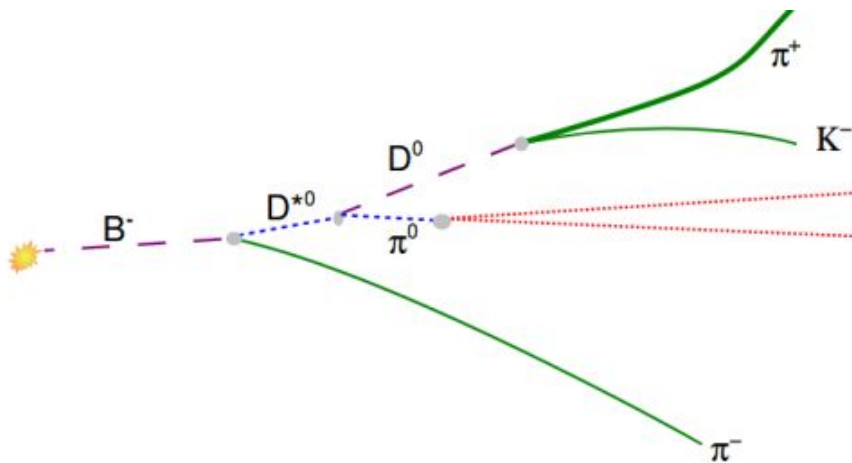
- SL Bs

```
#MR20210301 B_vars_SL original (remove DeltaE, decayAngle and daughterAngle)  
B_vars_SL = ['daughterProductOf(extraInfo(SignalProbability))', 'daughter({},extraInfo(SignalProbability))',  
            'chiProb', 'daughter({}, chiProb)', 'extraInfo(preCut_rank)',  
            'useRestFrame(daughter({}, p))',  
            'useRestFrame(daughter({}, distance))',  
            'cosAngleBetweenMomentumAndVertexVector',  
            'dr', 'dz', 'dx', 'dy', 'distance', 'significanceOfDistance', 'daughter({},extraInfo(decayModeID))']
```

Markus Roerken already removed some biasing variables already for the SL case.

# Vertex Fitting

- Vertex fitting dominates reconstruction time of FEI decay chains.
- Decay tree fitting with suitable constraints could help better reconstruct decay chains with neutrals.
- Current kFit does not work when two pi0s are present.



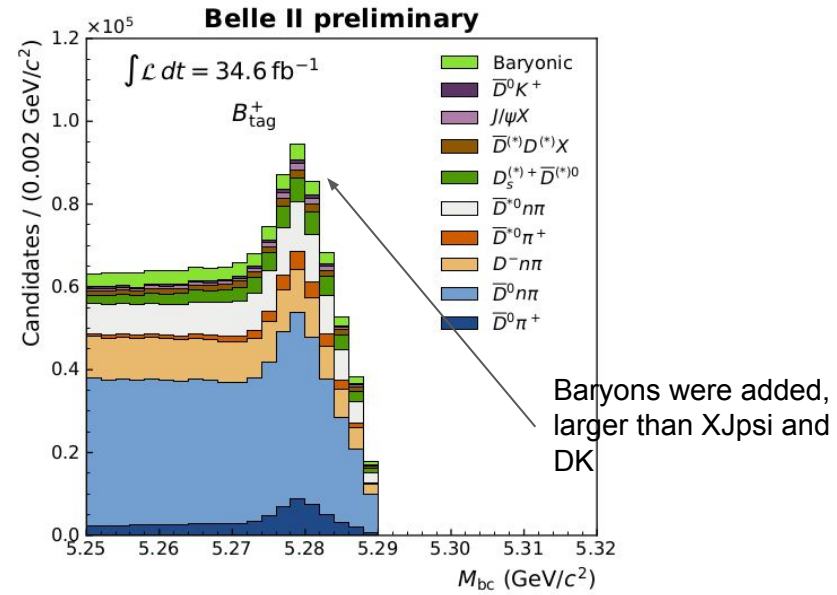
Task	Training	Application
read/write DataStore	30	0
vertex fitting	26	38
particle combination	19	27
classifier inference	11	15
training data & monitoring	6	0
best candidate selection	3	6
other	5	14

Dominate time on  
vertex fitting in  
application (during  
skims)

# Adding more decay modes

- Naturally the higher the branching fraction covered the higher the tag-side efficiency.
- An example of this was adding B decay modes with Baryons.
- Suggested by Vidya et al.: -  $B^+ \rightarrow D^{*-} (4\pi)^{++}$ ,  $B^+ \rightarrow D^{*0} (5\pi)^+$ ,  $B^+ \rightarrow D^{(*)0} K^+ K^0(*)$  (an easy change)

$B^0$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Confidence
$f^+ \nu_i$ anything	[ttt] (10.33 ± 0.28) %	
$e^+ \nu_e X_c$	[ttt] (10.1 ± 0.4) %	
$D^{*+} \nu_i$ anything	[ttt] (2.19 ± 0.12) %	
$D^- f^+ \nu_i$	[ttt] (1.03 ± 0.11) %	
$D^- f^+ \nu_i$	[ttt] (4.93 ± 0.17) %	
$D^{*+}(2010)^- f^+ \nu_i$	(1.78 ± 0.17) %	
<b>Inclusive modes</b>		
$\kappa^+$ anything	(79 ± 8) %	
$D^0 X$	(81 ± 15) %	
$D^+ X$	(47.4 ± 2.8) %	
$D^+ X$	< 3.9	
$D^+ X$	(96.9 ± 3.3) %	
$D^+ X$	(10.3 ± 2.1) %	
$D^+ X$	< 2.6	
$D^+ X$	< 3.1	
$D^+ X$	(5.0 ± 2.1) %	
$D^+ X$	(95 ± 5) %	
$D^+ X$	(24.6 ± 3.1) %	
$D^+ X$	(119 ± 6) %	
<b><math>D, D^*</math> or <math>D_s</math> modes</b>		
$D^{*+}$	(7.5 ± 0.13) × 10 <sup>-3</sup>	
$D^{*+}$	(2.92 ± 0.12) × 10 <sup>-3</sup>	
$D^{*+}$	(4.9 ± 0.9) × 10 <sup>-3</sup>	
$D^{*+}$	(4.5 ± 0.7) × 10 <sup>-3</sup>	
$D^{*+}$	(2.8 ± 0.8) × 10 <sup>-3</sup>	
$D^{*+}$	(1.96 ± 0.20) × 10 <sup>-3</sup>	
$D^{*+}$	(3.3 ± 0.8) × 10 <sup>-3</sup>	
$D^{*+}$	(8.8 ± 1.9) × 10 <sup>-3</sup>	
$D^{*+}$	(8.8 ± 0.5) × 10 <sup>-3</sup>	
$D^{*+}$	(3.4 ± 0.1) × 10 <sup>-3</sup>	
$D^{*+}$	(4.9 ± 1.1) × 10 <sup>-3</sup>	
$D^{*+}$	(6.0 ± 0) × 10 <sup>-3</sup>	
$D^{*+}$	(3.9 ± 0.3) × 10 <sup>-3</sup>	
$D^{*+}$	(1.1 ± 0.3) × 10 <sup>-3</sup>	
$D^{*+}$	(6.0 ± 0) × 10 <sup>-3</sup>	
$D^{*+}$	(1.5 ± 0.3) × 10 <sup>-3</sup>	
$D^{*+}$	(2.2 ± 0.5) × 10 <sup>-3</sup>	
<b>Charmonium modes</b>		
$D^{*+}$	(8.0 ± 2) × 10 <sup>-3</sup>	



# An aside on an earlier caveat: FEI confusion matrix

- Noreen also looked into a FEI confusion matrix

Here Best cand. Selection on Sig Prob > 0.001 (?)

Perhaps alternative classifiers / BCSs could improve this

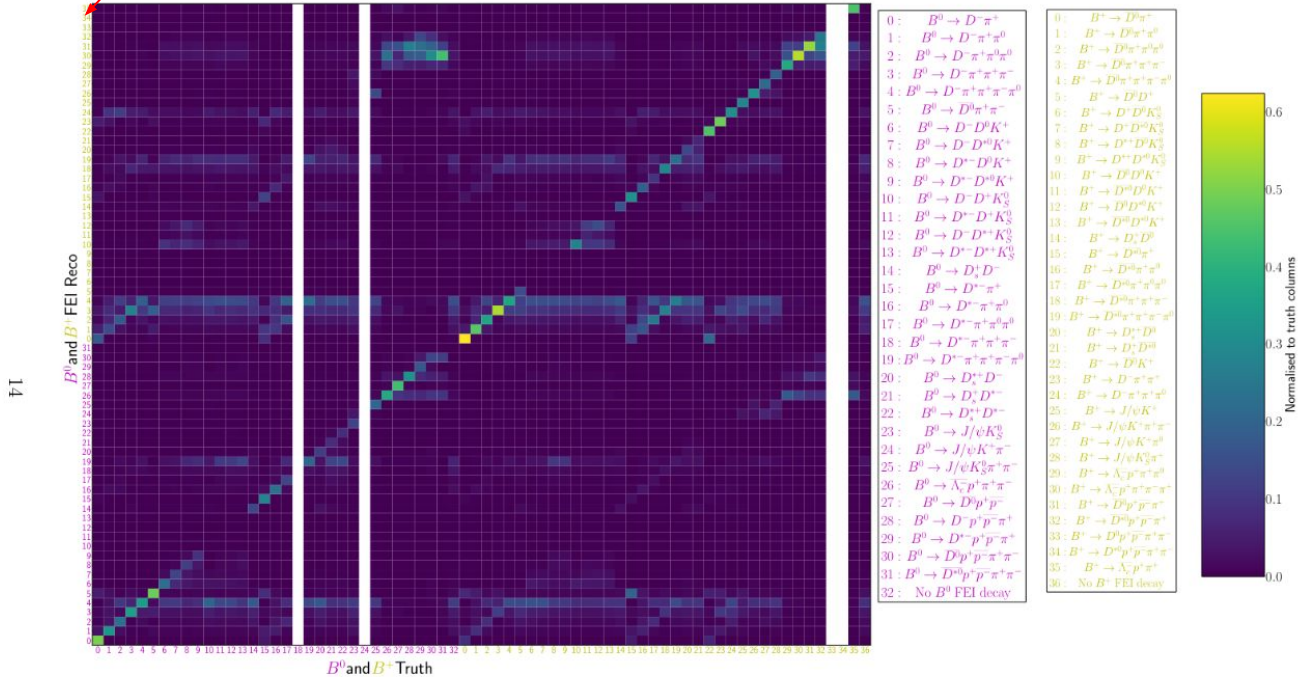


FIG. 22: Correlation between the hadronic  $B^0$  and  $B^+$  FEI. On the x axis the truth decays are given by TopoAna. On the y axis the reconstructed mode used by the FEI is provided. All  $B^0$  decays are coloured in purple and the charged decays are greenish. All the decay modes are also written out in the boxes next to the plot on the right hand side. The plot is normalised to the truth columns, thus to the x axis.

- People forget that the FEI has a unique BDT for each B mode. A single overall BCS + global cut is not optimal.
- BCS per mode? Different cuts for each mode. Applies also to delta E and Mbc

# Classifiers of the FEI

- One could also aim to improve the classifier (ROC curve + confusion matrix) of the FEI (new architectures)
- This can not increase the maximum tag-side efficiency. However it can improve the ROC curve (a better background rejection for a given tag-side efficiency).
- Here one can explore hyperparameter optimizations or more sophisticated architectures such as graph convolutional networks for graph classifications.

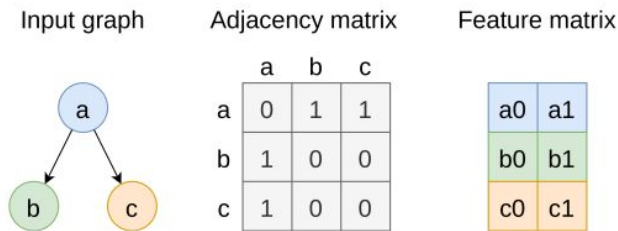
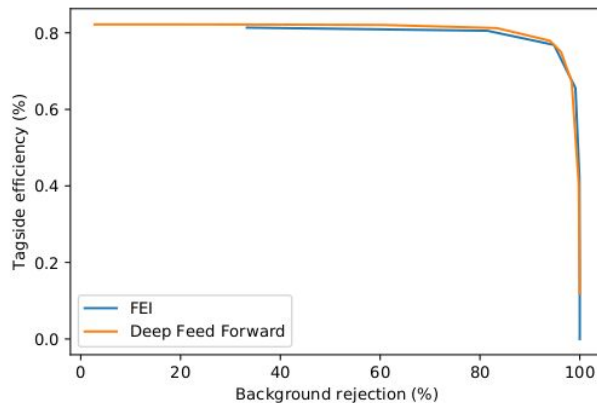
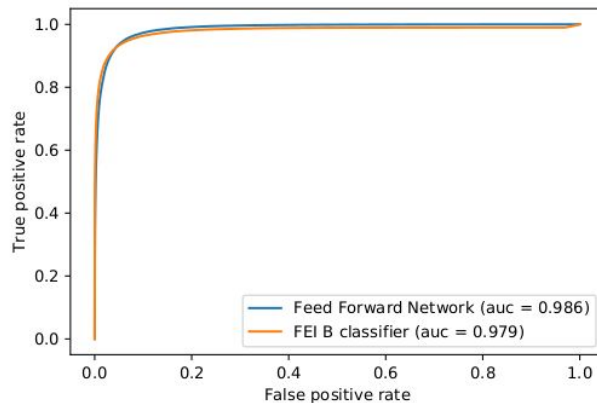
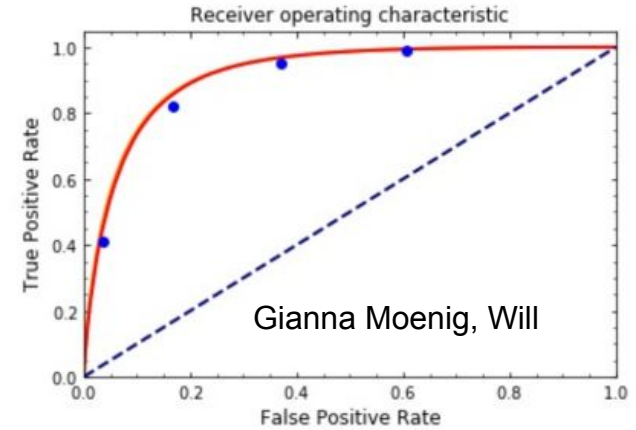


Figure: Example of matrices fully defining a graph.



# Other possible developments

- A built in continuum classifier trained specifically on the ROEs of FEI candidates.
- Investigating training with  $K_L$ s (already implemented but not run in trainings)
- No one uses semileptonic D decays (tag-side efficiency small  $\sim 0.1\%$ )
- **Other ideas?**

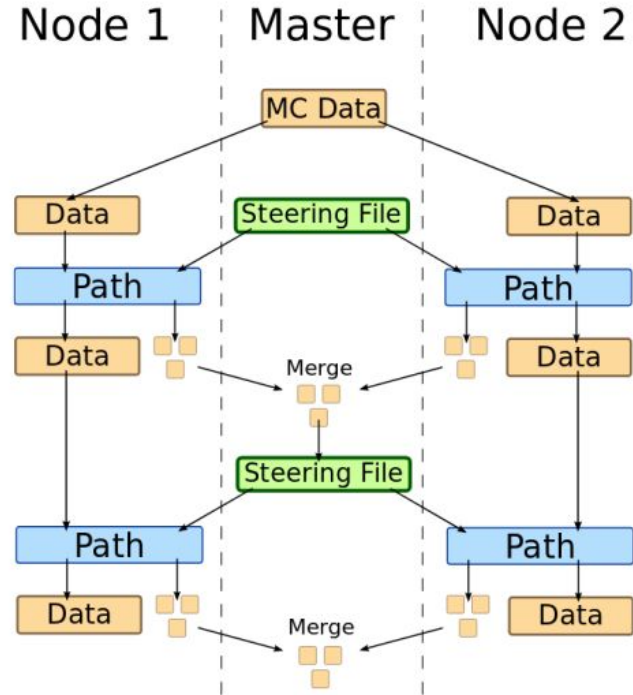




# Improving FEI Trainings

# FEI - Training

- Both training and application phases can be distributed via a map reduce approach.
- For training:
  - ▶  $O(100M)$  simulated  $\Upsilon(4S) \rightarrow B\bar{B}$  events
  - ▶ Monte carlo is partitioned and processed at different nodes.
  - ▶ At each of the reconstruction phases training data is generated.
  - ▶ Training data of each stage is subsequently merged and classifiers trained.



Training is offline in between each distributed reconstruction stage

# FEI - Training

- Locally:
  - 100 fb<sup>-1</sup> MC required.
  - Space requirements large O(10TB)
- Technically FEI can be trained on the grid (Artur Gottman, sphinx) but it is error prone and longer than local trainings.
  - All prior reconstruction stages must be rerun at each stage of training -> 2x training time without failed jobs
- However the GRID would allow for greater automation and a training + skimming workflow
- As discussed training assistance would be welcome. Many hurdles to overcome for better automation.

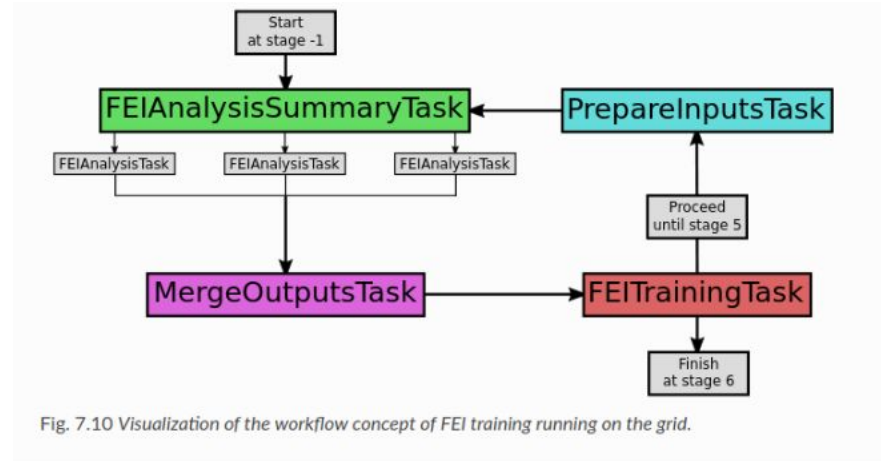
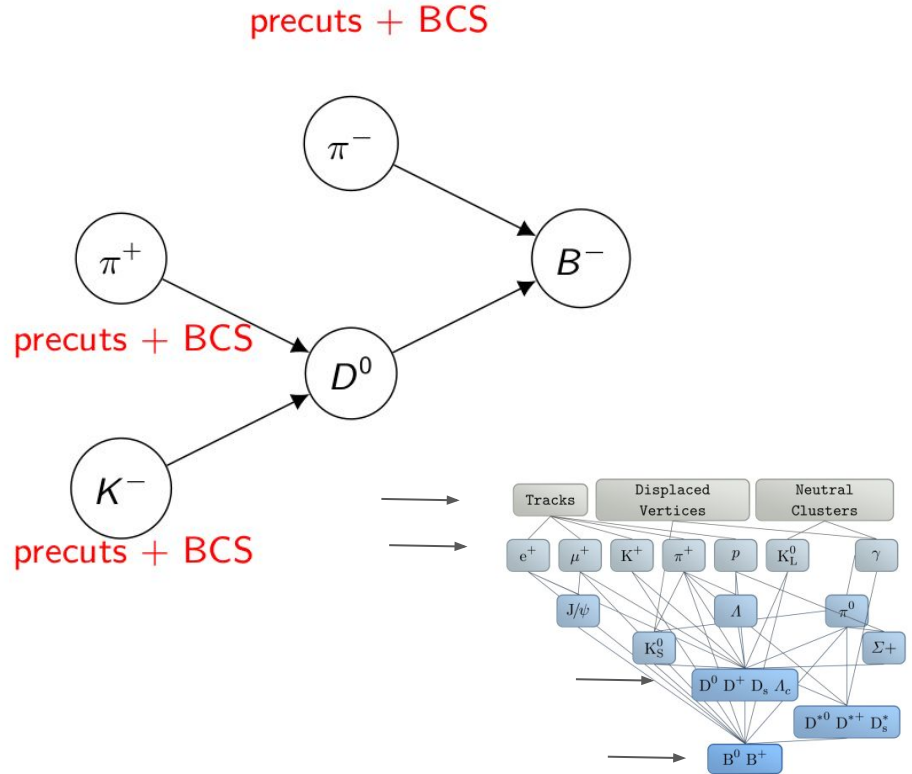


Fig. 7.10 Visualization of the workflow concept of FEI training running on the grid.

# Backup

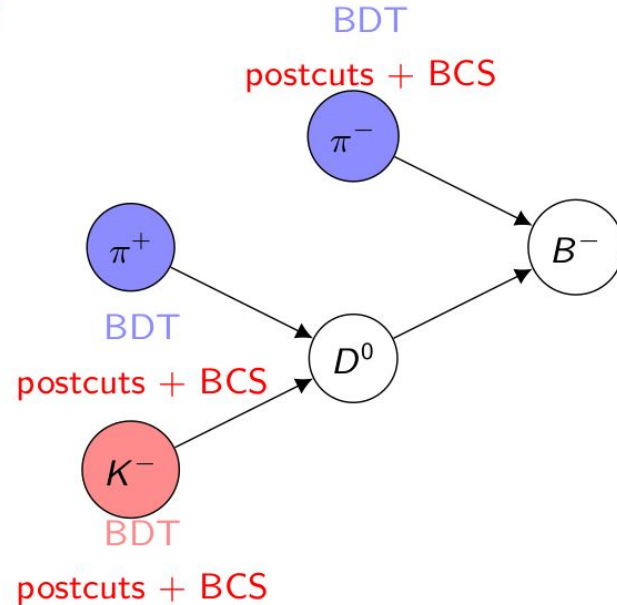
# FEI - Algorithm in greater depth

- Particle candidates assigned from tracks and clusters after a **precuts + Best Candidate Selection (BCS)**.



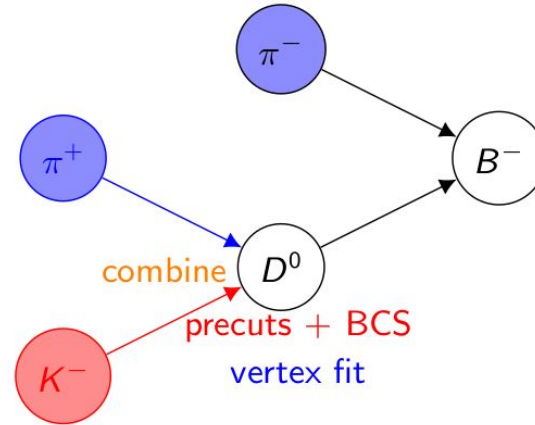
# FEI - Algorithm in greater depth

- Particle candidates assigned from tracks and clusters after a **precuts + Best Candidate Selection (BCS)**.
- For each particle a pre-trained BDT is applied and **post cuts + BCS** are made.



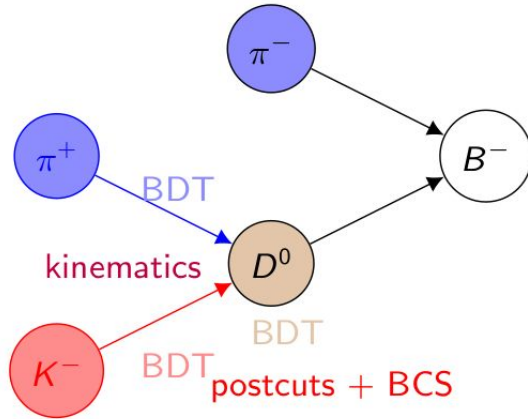
# FEI - Algorithm in greater depth

- Particle candidates assigned from tracks and clusters after a **precuts + Best Candidate Selection (BCS)**.
- For each particle a pre-trained BDT is applied and **post cuts + BCS** are made.
- Stable particles are **combined** to reconstruct decays of intermediate particles. After **precuts + BCS** a **vertex fit** is performed.



# FEI - Algorithm in greater depth

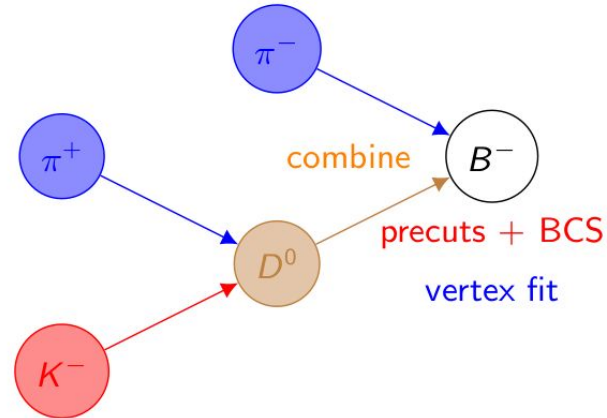
- Particle candidates assigned from tracks and clusters after a **precuts + Best Candidate Selection (BCS)**.
- For each particle a pre-trained BDT is applied and **post cuts + BCS** are made.
- Stable particles are **combined** to reconstruct decays of intermediate particles. After **precuts + BCS** a **vertex fit** is performed.
- Intermediate classifiers use daughter **kinematics** and classifiers.



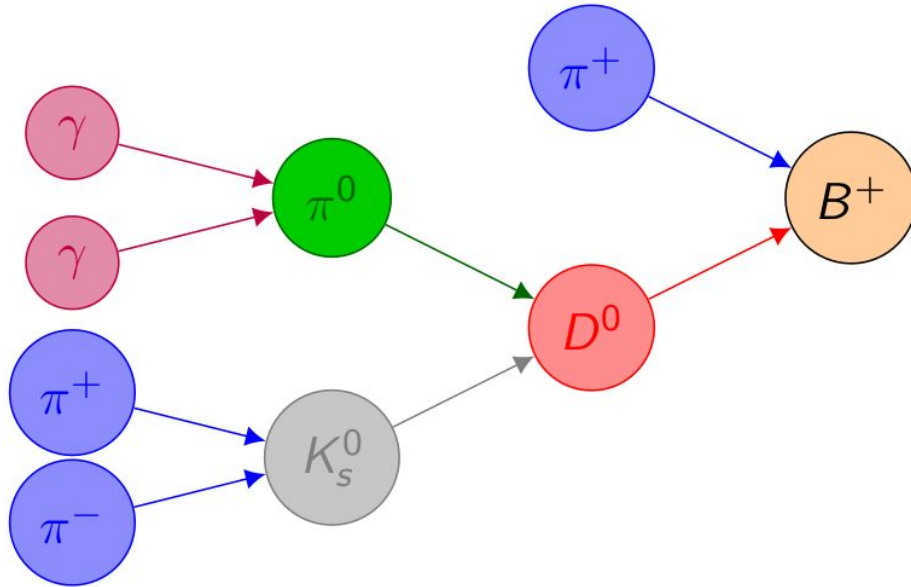


# FEI - Algorithm in greater depth

- Particle candidates assigned from tracks and clusters after a **precuts + Best Candidate Selection (BCS)**.
- For each particle a pre-trained BDT is applied and **post cuts + BCS** are made.
- Stable particles are **combined** to reconstruct decays of intermediate particles. After **precuts + BCS** a **vertex fit** is performed.
- Intermediate classifiers use daughter **kinematics** and classifiers.
- Intermediates and stable particles are **combined** into a  $B$  candidate.



# FEI - Algorithm in greater depth - another decay



- Same  $B^+ \rightarrow D^0 \pi^+$  classifier.
- Different decay chain as  $D^0 \rightarrow K_s^0 \pi^0$ .
- $D^0 \rightarrow K_s^0 \pi^0$  has its own classifier.

# Improving the FEI - Best Candidate Selections

- Major challenge of the FEI is to reduce combinatorics
- Therefore there are best candidate selections
  - Generally 20 candidates kept for precuts and 10 for postcuts
  - Exceptions e and mu (10 pre. 5 post), Gammas (40 pre. 20 post), Bs (20 pre., 20 post)
  - Precuts based on particle ID for charged particles (electronID, pionID etc), E for gammas, Mreco - Mtrue for most intermediate particles, abs(dQ) for D\*s, Sig Prob. for Bs
- Here we could explore retuning these hyperparameters

# Backup

# $B^+ \rightarrow D\pi$ selection procedure

These cuts could be further optimized, but seem good enough for preliminary studies.

We start by reconstructing a FEI-Hadronic B with cuts:

- $M_{bc} > 5.27 \text{ GeV}/c^2$
- $|\Delta E| < 0.05 \text{ GeV}$
- FEI Signal Probability  $> 0.01$

Select a  $\pi$  with:

- $|d0| < 1$  and  $|z0| < 3$
- $L_{K/\pi} < 0.9$  and  $\mu\text{-id} < 0.9$  and  $e\text{-id} < 0.9$

Simple continuum suppression:

- Event sphericity  $> 0.2$
- $B_{\text{tag}}$ 's  $\cos\text{TBTO} < 0.9$

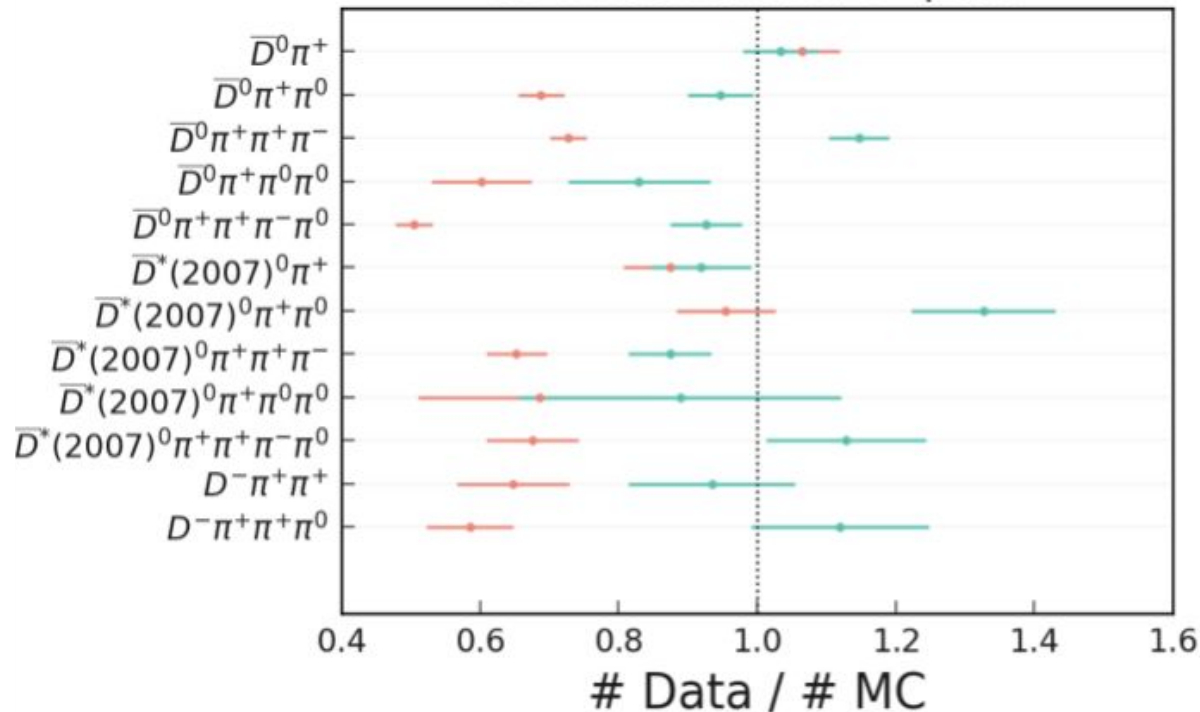
After all this, if there are multiple candidates, we select the one with highest FEI signal probability and highest  $\pi$  momentum in CMS

The code is present [\[here\]](#)

# Similarly, in Belle II with MC14rd + rel5

[Niharika Rout]

$3\sigma$  window around  $D^0$  peak



$\int L dt = 189.2 \text{ fb}^{-1}$

Official MC  
Proposed MC

Even lower than Belle!

Overall:

$(70 \pm 1)\%$



$(98 \pm 2)\%$

MC15rd looks essentially the same.

Except for  $\pi^0 \pi^0$  modes, where official MC is very low, still investigating...(see backup)

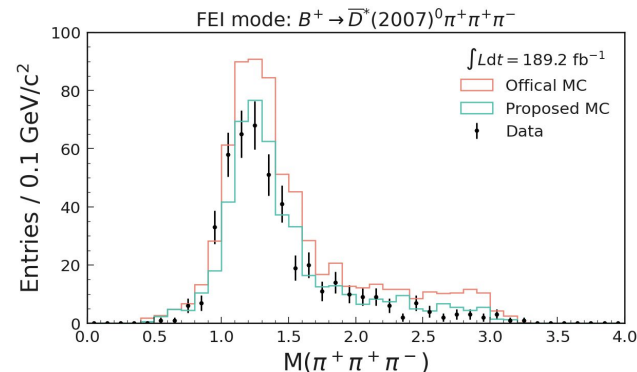
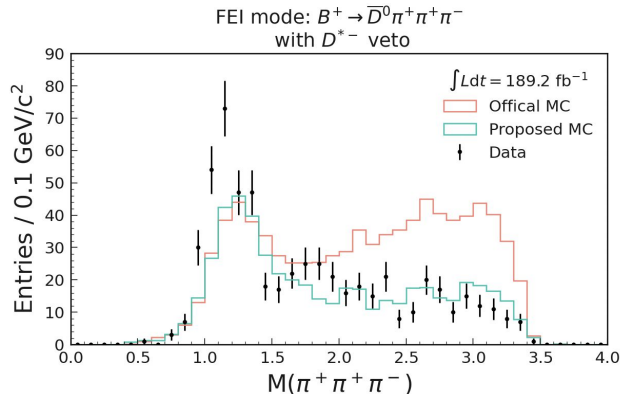
# Belle II: Decay description is improved!

with MC14rd + rel5

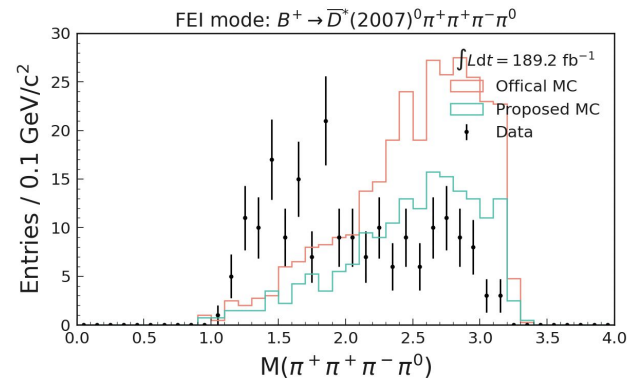
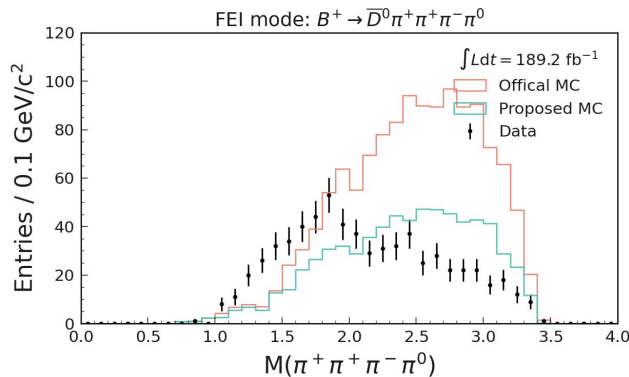
[Niharika Rout]

The improvement is not limited to calibration factors, but more importantly in the invariant masses (of intermediate particles):

$3\pi^\pm$  case:



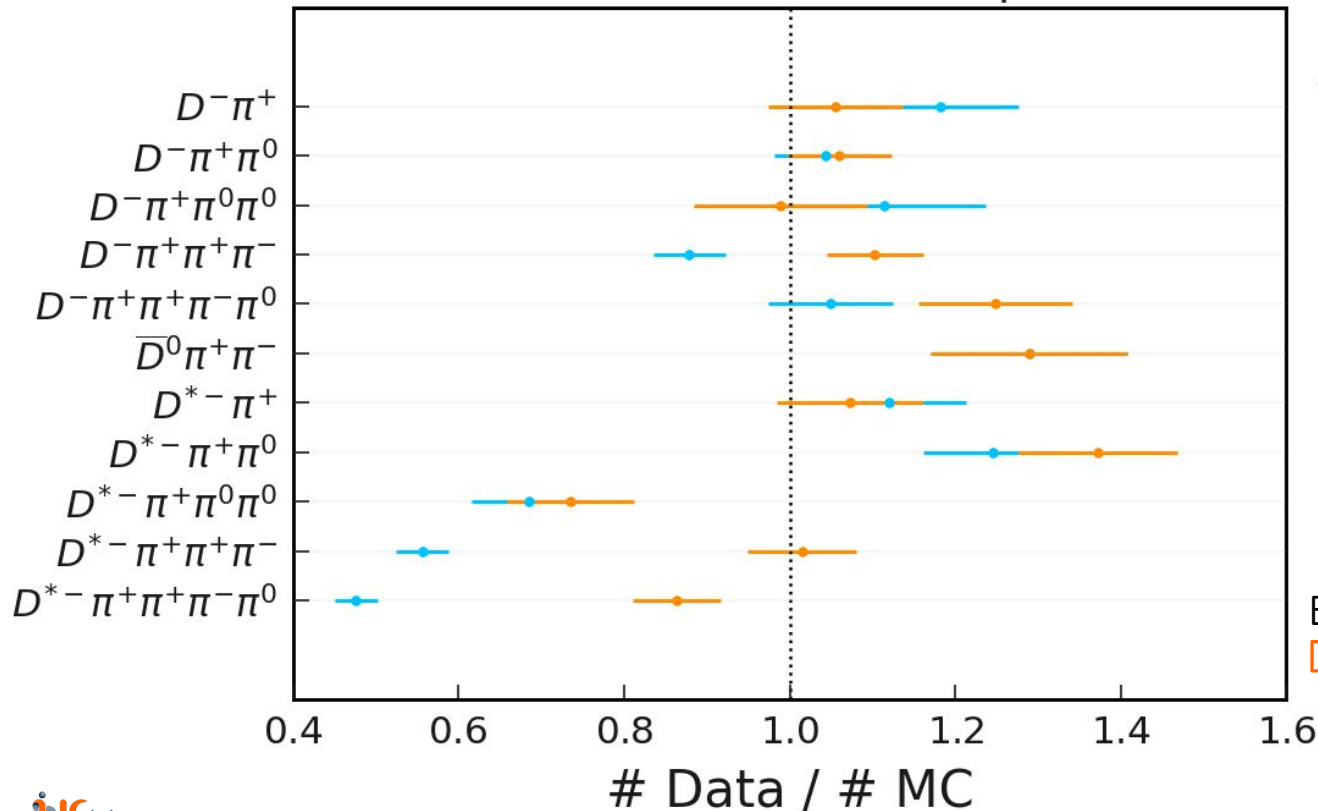
$3\pi^\pm \pi^0$  case:



# Similarly, with $B^0 \rightarrow D^- \pi^+$ in recoil @ Belle

$3\sigma$  window around  $D^-$  peak

[Meihong Liu]



$\int L dt = 711 \text{ fb}^{-1}$

- Official MC
- Latest MC

Overall calibration factor:

$(84.8 \pm 1.6)\%$



$(103.7 \pm 2.0)\%$

Belle II note in progress:

[\[BELLE2-NOTE-PH-2022-046\]](#)

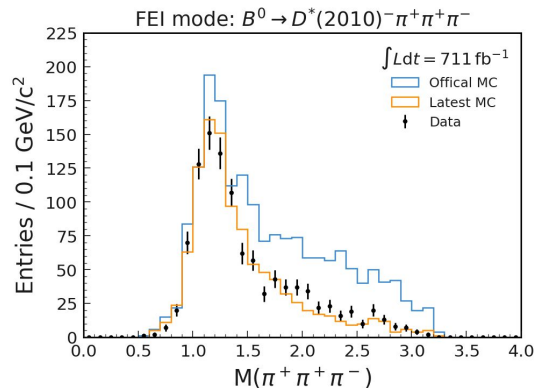
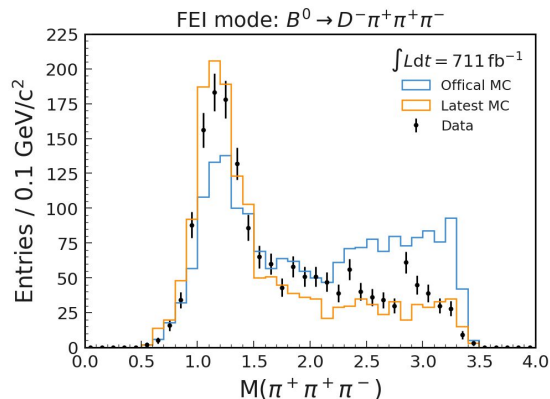


# Decay description is improved in $B^0$

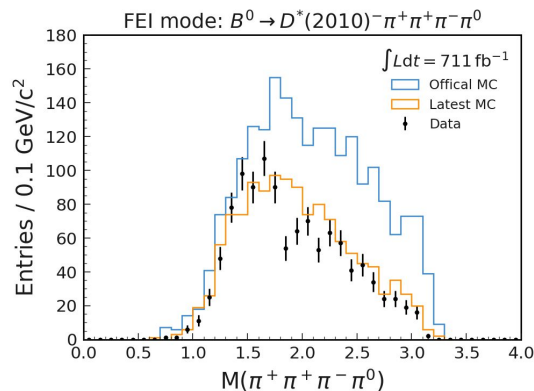
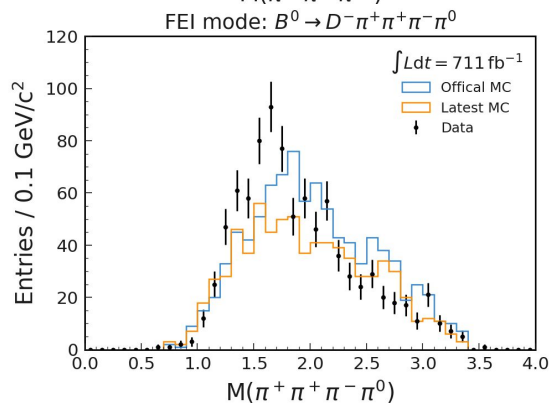
[Meihong Liu]

The improvement is not limited to calibration factors, but more importantly in the invariant masses (of intermediate particles), which are used as training variables in FEI

$3\pi^\pm$  case:



$3\pi^\pm \pi^0$  case:



# Plans (for the task-force?)

- **Calibration and modeling efforts:**
  - Study the issue in MC for modes with  $\pi^0\pi^0$  in MC15rd
  - Fitting, systematics and ROC with  $D\pi$  sample
  - Monitor the changes in  $B \rightarrow D n\pi$  modes decay tables over time. Promote (re-)measurement of these modes (including intermediate states)?
- **Retraining efforts:**
  - Understand the impact of retraining on  $\pi^0$
  - Generate (2 streams of) run-dependant charged MC with proposed DEC file for retraining:
    - for Belle and,
    - MC15rd with rel-06 for Belle II.
- **Modifying FEI reconstruction:**
  - Reconsider the pre-BDT cuts: like loosen the E cut on  $\gamma$ ; tighten the  $\Delta M$  cut for  $D^{*0}$
  - Apply cuts on  $n\pi$ -system invariant masses as pre-cuts or add as intermediate particles?
  - Reconsider variables used for BDT: Like removing  $\Delta E$  (in Hadronic FEI also) which is being sculpted by BDTs? (This is essential to recover some broken Bs from shifted  $\Delta E$  bin.)
  - Applying the right kind of fit among (mass constrained, mass-vertex constrained or vertex) for different intermediate states instead of vertex fit for all.  
[Roman Mizuk: BELLE2-NOTE-PH-2022-015]
  - Add a couple of B modes?

# Alternative FEI algorithm

Alternatively, using FEI  
particle list of  $\bar{D}^0$ ,  
we want to reconstruct  $B^+$   
particle list manually

in orders of  $\bar{D}^0$  ( $m \pi^+$ ) ( $n \pi^0$ ):

$(m, n) = (1, 0)$



$(m, n) = (1, 1)$



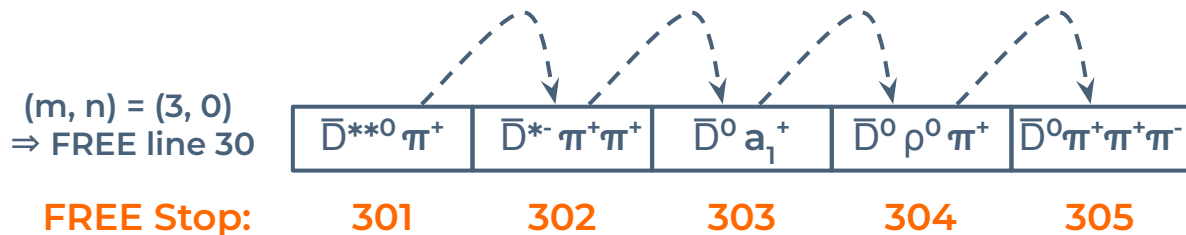
$(m, n) = (3, 0)$



⋮  
⋮

Reconstructing in this order,  
going to the next step only if it fails,  $\Rightarrow$  **Simpler best candidate selection**  
using the constraints of intermediate resonances when possible  $\Rightarrow$  **Higher purity**

# Multiplicity in FREE: BCS



- Level 1 (among FREE lines):
  - Like an event having a  $\bar{D}^0 \pi^+$  candidate and a  $\bar{D}^0 \pi^+ \pi^0$  candidate
  - Tight tag-side selection (Mbc and deltaE cuts) should make this negligible.
- Level 2 (among FREE stops):
  - Like a 301 candidate and a 303 candidate.
  - Lowest stop is the best.
- Level 3 (among the same FREE stop):
  - Like 2 candidates in 303.
  - Not worrying about this right now and see how many survive till the end.