

Determination of CKM angle ϕ_3 using $B^- \rightarrow D^{*0}(D^0(K_s^0 h^+ h^-)\pi^0/\gamma)h^-$.

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The CKM Matrix

SM accounts for CP violation through Kobayashi-Maskawa mechanism.

- The weak interactions of quarks are described in terms of the unitary Cabibbo-Kobayashi-Maskawa (CKM) matrix.

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} \equiv \hat{V}_{\text{CKM}} \begin{pmatrix} d \\ s \\ b \end{pmatrix} \quad (1)$$

Wolfenstein parametrisation:

$$V_{\text{Wolf}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2, & \lambda, & A\lambda^3(\rho - i\eta) \\ -\lambda, & 1 - \frac{1}{2}\lambda^2, & A\lambda^2(1 + i\lambda^2\eta) \\ A\lambda^3(1 - \rho - i\eta), & -A\lambda^2, & 1 \end{pmatrix} \quad (2)$$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \quad (3)$$

The unitarity triangle

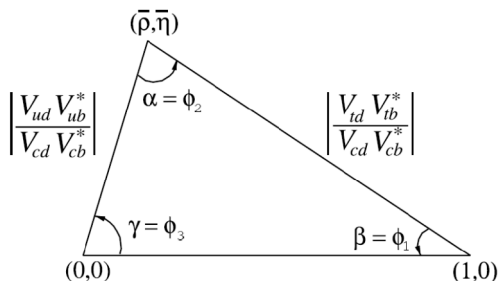


Figure: Unitarity Triangle

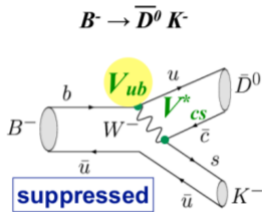
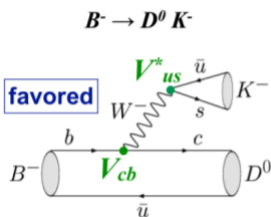
- We are interested in angle ϕ_3 (also denoted as γ) defined as,

$$\phi_3 = \gamma \equiv \arg \left[-V_{ud} V_{ub}^* / V_{cd} V_{cb}^* \right] \quad (4)$$

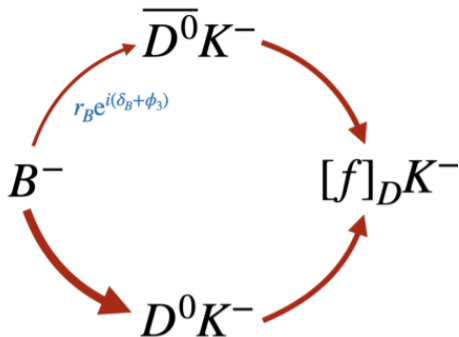
- ϕ_3 is least well known parameter in CKM triangle.
- Precise measurement will lead to a better understanding of SM description of CP violation.

Extraction of CKM angle ϕ_3

- $B \rightarrow D^{(*)0} h$, $h = \pi, K$ are sensitive to ϕ_3
- The tree-level nature of amplitudes involved allows theoretically clean extraction of ϕ_3 .
- The $B \rightarrow D^* h$ decay, where $D^* \rightarrow D\pi^0$ or $D\gamma$ exhibits CP-violating effects when B decays accessible to both D^0 and \bar{D}^0 mesons are studied.
- ϕ_3 is the phase between $b \rightarrow u\bar{c}s$ and $b \rightarrow c\bar{u}s$ transition.
- $b \rightarrow u\bar{c}s$: favored transition
- $b \rightarrow c\bar{u}s$: CKM and colour suppressed



Extraction of CKM angle ϕ_3



- Common final states allow interference between the two paths
- Interference gives access to the phase
- We can measure ϕ_3 by exploiting the interference between $B^- \rightarrow D^{(*)0} h^-$ and $B^- \rightarrow \bar{D}^{(*)0} h^-$ where the D^0 and \bar{D}^0 decay to self-conjugate multi-body final states $K_s h h$: GGSZ method.

$$\frac{\mathcal{A}^{\text{suppr.}}(B^- \rightarrow \bar{D}^{(*)0} K^-)}{\mathcal{A}^{\text{favor.}}(B^- \rightarrow D^{(*)0} K^-)} = r_B e^{i(\delta_B + \phi_3)} \quad (5)$$

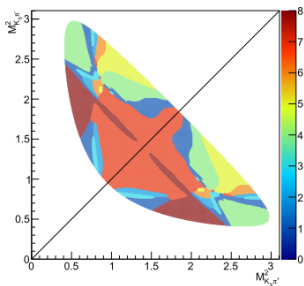
We use the final states D^0/\bar{D}^0 decaying to $K_S h^+ h^-$, $h = \pi, K$

BPGGSZ method

- Uses self-conjugate multi-body $D(K_S^0 h^- h^+)$ final states
- Sensitivity to ϕ_3 by comparing D Dalitz distributions of B^+ and B^-
- Fit D Dalitz plot with full amplitude model.

$$A_{B^+} = A_{\bar{D}}(m_-^2, m_+^2) + r_B e^{i(\delta_B - \phi_3)} A_D(m_-^2, m_+^2) \quad (6)$$

- $A_{\bar{D}}(m_-^2, m_+^2)$ [$A_D(m_-^2, m_+^2)$] is the $\bar{D}^0 \rightarrow K_S^0 h^+ h^-$ [$D^0 \rightarrow K_S^0 h^+ h^-$] decay amplitude
- $m_{\pm}^2 =$ squared invariant masses of $K_S^0 h^+$: D Dalitz plot variables



- In presence of **CP Violation** expect differences between $B^{(+)}$ and $B^{(-)}$ distributions
- The magnitude and position of the differences are driven by the values of r_B, δ_B, ϕ_3 and the physics of the D decay

- But model-independent analysis have model uncertainty upto $3^\circ - 9^\circ$

BPGGSZ : Binned model-independent approach

- Optimal (non-uniform) binning of the D Dalitz plot which gives the maximum sensitivity to ϕ_3
- Observed yields in each bin can be related to physics parameters of interest and D^0 decay information

$$\mathbf{N}_i^\pm = \mathbf{h}_B \pm \left[\mathbf{F}_i + r_B^2 \bar{\mathbf{F}}_i + 2\sqrt{\mathbf{F}_i \bar{\mathbf{F}}_i} (c_i \mathbf{x}_\pm + s_i \mathbf{y}_\pm) \right] \quad (7)$$

- h_{B^\pm} : Normalization constant
- Physics parameters of interest : $(x_\pm, y_\pm) = r_B (\cos(\phi_3 + \delta_B), \sin(\phi_3 + \delta_B))$
- Amplitude averaged strong phase differences between \bar{D}^0 and D^0 over i^{th} bin are obtained from external charm factories like CLEO and BESIII
- Fraction of pure D^0 decay to bin i taking into account the reconstruction and selection efficiency

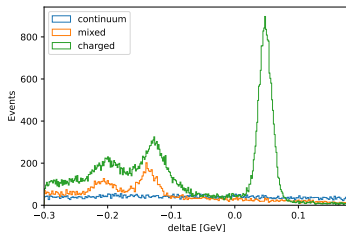
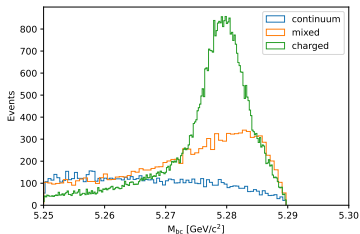
Selection :

- The small $D^* - D$ mass difference and conservation of angular momentum in $D^* \rightarrow D\pi^0$ and $D\gamma$ results in distinctive signatures for $B \rightarrow D^* h$ signal in the Dh invariant mass.
- $B \rightarrow D^* h$ yields obtained with a partial reconstruction technique.
- transverse impact parameter $|dr| < 0.2$ cm
- longitudinal impact parameter $|dz| < 1$ cm
- $\cos\theta \geq -0.6$ for prompt tracks
- binary likelihood-ratio kaonID > 0.2 for D daughters
- $1.85 < M_{D^0} < 1.88$ GeV/ c^2 \rightarrow massKFit() has been applied
- $M_{bc} > 5.25$ GeV/ c^2
- $-0.13 < \Delta E < 0.18$ GeV
- $0.487 < M_{K_s} < 0.508$ \rightarrow massKFit() has been applied
- FBDBTKs selection
- MC: $1 ab^{-1}$ MC14ri

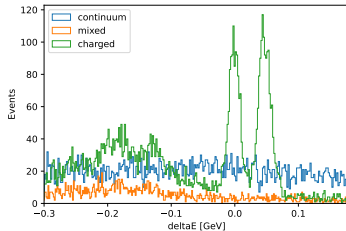
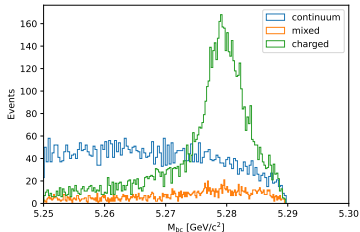
Continuum Suppression

- Training variables: KSWF moments (hoo0,hso02,hso12)
- $\cos\theta_B$: The absolute value of the cosine of the angle between the B candidate and the beam axis in the e^+e^- center-of-mass frame
- $\cos\theta_B^{ROE}$: Cosine of the angle between the thrust axis of the signal B and the thrust axis of ROE
- B_{thrust} : Magnitude of the signal B thrust axis
- ΔZ : $Z(\text{Brec}) - Z(\text{Btag})$
- $|qr|$: Flavor-tagger output

Pion Enhanced(binary KaonID < 0.6)

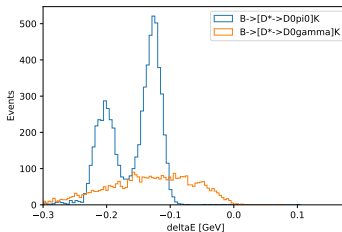
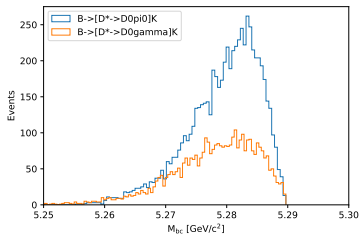


Kaon enhanced (binary KaonID > 0.6)

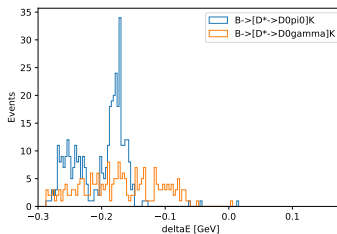
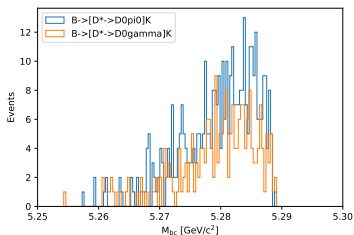


Truth-matched sample:

$$B \rightarrow D^{*0}(\pi^0/\gamma)\pi$$



$$B \rightarrow D^{*0}(\pi^0/\gamma)K$$



- Aim of this analysis is the model-independent measurement of the CKM angle ϕ_3 using $B \rightarrow D^* h$.
- $B \rightarrow DK$ channel is reconstructed in 1 ab^{-1} of generic MC.
- Since the π^0 or γ from the D^* decay is not reconstructed, fully reconstructed $B^- \rightarrow Dh^-$ and partially reconstructed $B^- \rightarrow D^* h^-$ candidates contain the same reconstructed particles and thus appear in the same sample.
- The next immediate step would be to identify the background beneath the signal using truth-matching information and topology analysis.