

# Precision Measurement on $R(D^{(*)})$ with Inclusive Tagging Methods at Belle II

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#### **Results and Predictions**

- The standard model predicts all leptons have the same coupling  $(g_{\ell=e,\mu,\tau})$  to electroweak bosons  $(W^{\pm}, Z^0)$
- HFLAV average tension of  $3.3\sigma$
- OUR GOAL: Increase precision of  $R(D^{(*)})$ measurement with *inclusive tagging* to further test lepton flavor universality...

$$R(D^{(*)}) = \frac{N(D^{(*)}\tau\nu)}{N(D^{(*)}\ell\nu)} \frac{\varepsilon(D^{(*)}\ell\nu)}{\varepsilon(D^{(*)}\tau\nu)} \frac{1}{B(\tau)}$$
Removes most systematic uncertainties

$$\Gamma(B^- \to D^0 \ell^- \bar{\nu}_\ell) \propto \frac{g_\ell^2}{M_W^2} \frac{g^2}{M_W^2} m_B^5$$
$$R(D) = \frac{\Gamma(B^- \to D^0 \tau^- \bar{\nu}_\tau)}{\Gamma(B^- \to D^0 \ell^- \bar{\nu}_\ell)} \propto \frac{g_\tau^2}{g_\ell^2}$$

#### Belle II Results





First lepton flavor universality (LFU) results from Belle II!

Shifts difference (exceeding) standard model (SM) predictions from  $3.2\sigma$  to  $3.3\sigma$ 

 $R(D^*) = 0.267 + 0.041 - 0.039$ (stat.) + 0.028 (syst.)

Standard Model (SM) predictions:  $R(D) = 0.298 \pm 0.004$  $R(D^*) = 0.254 \pm 0.005$ 

# Inclusive Tagging Method

- With good ROE, exploit Belle II high resolution tracking, impact parameter, and small beam spot
- Exact topology of tag side is not important, but simple masks placed to ensure "good"  $B_{tag}$ 
  - Apply lepton veto to ROE to ensure there is no missing energy on the tag side → increase signal fit resolution

Signal

 $D^0$ 

- ADVANTAGE: Maximize sensitivity by increasing signal efficiency
- DISADVANTAGE: Yields lower purity compared to FEI tagging

FEI Thomas Keck Inclusive Tag  $\varepsilon = \mathcal{O}(100)\%$  (2) Consistency of B<sub>tag</sub> Semileptonic Tag  $\varepsilon = \mathcal{O}(1)\%$  (1) Knowledge of B<sub>tag</sub> Hadronic Tag  $\varepsilon = \mathcal{O}(0.1)\%$  (2) Exact knowledge of B<sub>tag</sub>

ω

Efficiency

γ

ROE

 $K^{\pm}$ 

 $B^+$ 

 $B^{-}$ 

 $\bar{\nu}_{\tau}$ 

 $\nu_{\tau}$ 

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Signal Simulta reconst normal	Reconstruct aneously ruct signatization mo	uction l and odes.
Variable	$B \rightarrow De\nu$	$B \to D\tau\nu$
binary K-ID	>	0.1
binary $\pi$ -ID	>	0.1
$e^{\pm}$ -p [GeV/c]	>	0.2
MVA e-ID	>	0.9
$0^0$ InvM [GeV/c <sup>2</sup> ]	$1.85 < \mathrm{In}$	vM < 1.88
	(07.1 + 0.1)07	$(99.9 \pm 0.1)\%$

			DODICI		
		Track	$\frac{\text{ROE Mask}}{\text{thotaInCDCAcceptance, pValue > 0.001}}$		
<b>Signa</b> Simul recons	<b>I Reconstruction</b> taneously struct signal and	Track Energy Cluster	thetaInCDCAcceptance, pValue > 0.001, $\left[pt < 0.15 \text{ and } \left(\frac{dr^2}{3} + \frac{dz^2}{6}\right) < 1\right]$ or $\left[0.15 < pt < 0.25 \text{ and } \left(\frac{dr^2}{2} + \frac{dz^2}{3}\right) < 1\right]$ or $\left[0.25 < pt < 0.5 \text{ and } \left(\frac{dr^2}{2} + \frac{dz^2}{3}\right) < 1\right]$ or $\left[0.5 < pt < 1.0 \text{ and } \left(\frac{dr^2}{2} + \frac{dz^2}{3}\right) < 1\right]$ or $\left[1.0 < pt \text{ and } \left(dr^2 + dz^2\right) < 1\right]$ beamBackgroundSuppression > 0.15, fakePhotonSuppression > 0.15,		
norma	lization modes.		(FWD Endcap, clusterE > 0.075), or (BRL, clusterE > 0.05), or (BWD Endcap, clusterE > 0.1)		
Variable	$B \to De\nu \qquad B \to D$	$\tau \nu$			
binary K-ID	> 0.1	-			
binary $\pi$ -ID	> 0.1	J	Rest Of Event		
$e^{\pm}$ -p [GeV/c]	> 0.2		Select only good $B_{tag}$		
MVA e-ID	> 0.9	(	candidates via minimizing		
$\rm D^0~InvM~[GeV/c^2]$	$1.85 < \mathrm{InvM} < 1.88$	Ì	$Mbc_{ROE}$ and $\Delta E_{ROE}$ widths		
ε	$(27.1 \pm 0.1)\%$ $(22.2 \pm 0.1)\%$	0.1)%	-		
		]	Lepton Veto		
		]	Ensure no missing mass for		

better resolution of signal fit

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# Signal Efficiency $B^{\pm} \rightarrow (D^0 \rightarrow K\pi) \ell^{\pm} \nu$

With hadronic and semileptonic tagging, the efficiency is  $O(\leq 0.5\%)$ 

${f B}  o {f D}^0 \ {f e} \  u$			${f B}  ightarrow {f D}^0 \;  au( ightarrow {f e}  u  u) \;  u$	
	Kpi	Ī		Kpi
Reconstruction	$0.271 \pm 0.001$		Reconstruction	$0.222\pm0.001$
Rest of Event			Rest of Event	
$\ell \text{ Veto}2$	$0.253\pm0.001$		$\ell \text{ Veto}2$	$0.207 \pm 0.001$
5.2 <mbc< td=""><td><math display="block">0.191\pm 0.001</math></td><td></td><td>5.2<mbc< td=""><td><math>0.158 \pm 0.001</math></td></mbc<></td></mbc<>	$0.191\pm 0.001$		5.2 <mbc< td=""><td><math>0.158 \pm 0.001</math></td></mbc<>	$0.158 \pm 0.001$
-4 <deltae<2< td=""><td><math display="block">0.190\pm 0.001</math></td><td></td><td>-4<deltae<2< td=""><td><math>0.157 \pm 0.001</math></td></deltae<2<></td></deltae<2<>	$0.190\pm 0.001$		-4 <deltae<2< td=""><td><math>0.157 \pm 0.001</math></td></deltae<2<>	$0.157 \pm 0.001$
Background Suppression			Background Suppression	
SignalProb>0.7	$0.077\pm0.002$		SignalProb>0.7	$0.126 \pm 0.002$
Best Candidate Selection			Best Candidate Selection	
B vertex chiProb	$0.077\pm0.002$		B vertex chiProb	$0.126 \pm 0.002$
		With <i>inclusive tag</i> efficiency of C	<i>rging</i> we get 0(10%)	

#### MC Truth



#### Kernel Density Estimation

- Non-parametric method of constructing a continuous PDF based on dataset
- Each data point is assigned a multi-dimensional kernel (Gaussian)



#### Kernel Density Estimation

- Non-parametric method of constructing a continuous PDF based on dataset
- Each data point is assigned a multi-dimensional kernel (Gaussian)
- User defines bandwidth (# datapoints associated with kernel) which controls the tradeoff between smoothness and fine-scale fluctuations

ADVANTAGE: Avoid bias of binning associated with a histogram (binned) PDF  $\rightarrow$  increase sensitivity

DISADVANTAGE: Unbinned fit requires extended processing time

 $B \rightarrow (D^0 \rightarrow K\pi)\tau\nu$  Template Bandwidth = 2 Any smaller leads to *overfitting* (PDF fits each data point and microscopic fluctuations present) Any larger leads to *underfitting* (greatly worsen  $\chi^2/ndf$ and unable to extract macroscopic properties, ie amplitude)



Statistics			
Signal Component	Events Used for Template Construction		
$B \to D^0 \tau \nu$	93438		
$B \rightarrow D^0 e \nu$	64741		
$B \to D^* \tau \nu$	1468		
$B \rightarrow D^* e \nu$	30278		





#### Concluding Remarks

- A test of lepton flavor universality via a precision measurement on  $R(D^{(*)}) \rightarrow \underline{deviation from the SM}$ prediction could be signs of new physics!
- *Inclusive tagging* permits high efficiency  $\rightarrow$  increased sensitivity
- Simultaneous reconstruction of signal and normalization modes
- Most errors cancel out in  $R(D^{(*)})$  as we are taking the ratio
- KDE is employed to construct signal templates



 $\nu_{\tau}$ 

# Backup Slides

#### MetaData

D <sup>0</sup> Signal Metadata			
Release	release-06-00-08		
Generated Signal Events	20M Events		
$K\pi + K2\pi$ File	13.5e6		
$\rightarrow K\pi \ (0.0395)$	2905995		
$\rightarrow K2\pi \ (0.144)$	10594005		
$K3\pi$ File	6.5e6		

$\mathbf{D}^{*0}$ Signal Metadata			
Release	release-06-00-08		
Generated Signal Events	5M Events		
$K\pi + K2\pi$ File	3.4e6		
$\rightarrow K\pi$ (0.0395)	731880		
$\rightarrow K2\pi \ (0.144)$	2668120		
$K3\pi$ File	1.6e6		

Reconstruction Release: light-2303-iriomote MC15ri\_b Samples

D <sup>*+</sup> Signal Metadata			
Release	release-06-00-08		
Generated Signal Events	<u>5M Events</u>		
$K\pi + K2\pi$ File	3.4e6		
$\rightarrow K\pi \ (0.0395)$	731880		
$\rightarrow K2\pi$ (0.144)	2668120		
$K3\pi$ File	1.6e6		

# Signal Selection



Composite State Selection: electron					
Крі	K2pi	КЗрі			
1.85386 < InvM < 1.87562	1.83637 < InvM < 1.88824	1.85342 < InvM < 1.8756			
D0 vertex fit (conf_level=0.001)	D0 vertex fit (conf_level=0.001, pi0 mass constraint)	D0 vertex fit (conf_level=0.001)			
B vertex fit (conf_level=0.001)	B vertex fit (conf_level=0.001)	B vertex fit (conf_level=0.001)			

# Signal Definition

The signal is defined through...

- 1. The intermediate resonance structure for the respective decay branch (TopoAna)
  - nSigIncCascDcyBr\_(decay branch) and B\_mcPDG=-521
  - $\bullet\,$  nCcSigIncCascDcyBr\_(decay branch) and B\_mcPDG=521
- 2.  $(B_mcPDG^*D_mcPDG) = -521^*421$  or  $(B_mcPDG^*D_mcPDG) = -511^*421$ 
  - The multiplication of the mcPDGs ensures the mode is properly reconstructed (i.e. proper D associated with the proper B)
- 3. (D\_mcPDG\*l\_mcPDG)=lrec\*421
  - $lrec \in \{11, 13\}$
- 4. B\_mcErrors  $< \{16, 32, 64, 152\}.$ 
  - $D^0$ :
    - electron/muon: B\_mcErrors < 16
    - tauon: B<sub>-</sub>mcErrors < 32
  - $D^{*0}$  and  $D^{**0}$ : B\_mcErrors < 64
  - $D^{*+}$  and  $D^{**+}$ : B\_mcErrors < 521
- 5. (l\_mcPDG\*l\_genMotherPDG)=lrec\*lmother
  - $lrec \in \{11, 13\}$
  - $\operatorname{Imother} \in \{521, 511, 15\}$

Signal Efficiency  $B \rightarrow (D^{*0} \rightarrow K\pi) \ell \nu$ 

${f B}  ightarrow {f D}^{*0}   {f e}    u$		
	Kpi	
Reconstruction	$0.227 \pm 0.002$	
Rest of Event		
$\ell \text{ Veto}2$	$0.212 \pm 0.002$	
5.2 <mbc< th=""><th><math>0.158 \pm 0.003</math></th></mbc<>	$0.158 \pm 0.003$	
-4 <deltae<2< th=""><th><math>0.157 \pm 0.003</math></th></deltae<2<>	$0.157 \pm 0.003$	
Background Suppression		
MVA Output>0.7	$0.067 \pm 0.004$	
Best Candidate Selection		
B vertex chiProb	$0.067 \pm 0.004$	

$\mathbf{B} \rightarrow \mathbf{D}^{*\circ} \ \tau (\rightarrow \mathbf{e} \nu \nu) \ \nu$			
	Kpi		
Reconstruction	$0.182 \pm 0.002$		
Rest of Event			
$\ell  { m Veto2}$	$0.170 \pm 0.002$		
5.2 < Mbc	$0.129\pm0.003$		
-4 < delta E < 2	$0.128 \pm 0.003$		
Background Suppression			
MVA Output>0.7	$0.088 \pm 0.004$		
Best Candidate Selection			
B vertex chiProb	$0.088 \pm 0.004$		

D

n \* 0

Signal Efficiency  $B \rightarrow (D^{*+} \rightarrow K\pi) \ell \nu$ 

${f B}  ightarrow {f D}^{*+}  {f e}   u$			
	Kpi		
Reconstruction	$0.273 \pm 0.002$		
Rest of Event			
$\ell \text{ Veto}2$	$0.254 \pm 0.002$		
5.2 <mbc< td=""><td><math>0.188 \pm 0.003</math></td></mbc<>	$0.188 \pm 0.003$		
-4 <deltae<2< td=""><td><math>0.150 \pm 0.003</math></td></deltae<2<>	$0.150 \pm 0.003$		
<b>Background Suppression</b>			
MVA Output>0.7	$0.077\pm0.004$		
Best Candidate Selection			
B vertex chiProb	$0.077\pm0.004$		

$\mathbf{B}  ightarrow \mathbf{D}^{*+} \  au( ightarrow \mathbf{e} \  u  u) \  u$			
	Kpi		
Reconstruction	$0.216 \pm 0.002$		
Rest of Event			
$\ell \text{ Veto}2$	$0.201 \pm 0.002$		
5.2 <mbc< td=""><td><math>0.151 \pm 0.003</math></td></mbc<>	$0.151 \pm 0.003$		
-4 < delta E < 2	$0.187 \pm 0.003$		
<b>Background Suppression</b>			
MVA Output>0.7	$0.102 \pm 0.004$		
Best Candidate Selection			
B vertex chiProb	$0.102 \pm 0.004$		

#### MVA and BCS Statistics

	Efficiency (SigProb>0.7)	Figure of Merit: $\frac{S}{\sqrt{S+B}}$	Candidates Before	Candidates After				
<b>Relative Sample Signal</b>	0.7343	3.2958						
Fake D	0.1158	56.2299						
Fake B	0.3347	57.3869						
qqbar	0.0772	1.9459						
TOTAL			965644	414869				
MVA Background Suppression								
	Mean # Candidates Before	# Candidates Before	Mean # Candidates After	# Candidates After				
TOTAL	1.005	414869	1.003	414256				
Best Candidate Selection								

# MVA Output





# MVA Output



# MVA Output



### **Dominant Generated Signals**

		Number B- case	er of es	Number of B+ cases	Total cases (B- and B+)	Cumulative cases
rowNo	cascade decay branch of $B^-$	iCascDcyBrP	nCase	nCcCase	nAllCase	nCCase
1	$B^- \to e^- \bar{\nu}_e D^{*0}, D^{*0} \to \pi^0 D^0, D^0 \to \pi^+ K^-$	4	12151	12431	24582	24582
2	$B^- \rightarrow e^- \bar{\nu}_e D^0, D^0 \rightarrow \pi^+ K^-$	0	7663	7765	15428	40010
3	$B^- \rightarrow e^- \bar{\nu}_e D^{*0}, D^{*0} \rightarrow D^0 \gamma, D^0 \rightarrow \pi^+ K^-$	28	6681	6701	13382	53392
4	$B^- \to \tau^- \bar{\nu}_\tau D^0, \tau^- \to e^- \bar{\nu}_e \nu_\tau, D^0 \to \pi^+ K^-$	32	612	603	1215	54607
5	$B^- \to \tau^- \bar{\nu}_\tau D^{*0}, \tau^- \to e^- \bar{\nu}_e \nu_\tau, D^{*0} \to \pi^0 D^0, D^0 \to \pi^+ K^-$	16	503	544	1047	55654
6	$B^- \to e^- \bar{\nu}_e D^0_1, D^0_1 \to \pi^- D^{*+}, D^{*+} \to \pi^+ D^0, D^0 \to \pi^+ K^-$	44	324	304	628	56282
7	$B^- \to \tau^- \bar{\nu}_\tau D^{*0}, \tau^- \to e^- \bar{\nu}_e \nu_\tau, D^{*0} \to D^0 \gamma, D^0 \to \pi^+ K^-$	7	308	316	624	56906
8	$B^- \to e^- \bar{\nu}_e D_1^{\prime 0}, D_1^{\prime 0} \to \pi^- D^{*+}, D^{*+} \to \pi^+ D^0, D^0 \to \pi^+ K^-$	38	269	237	506	57412
9	$B^- \to e^- \bar{\nu}_e D^0_1, D^0_1 \to \pi^+ \pi^- D^0, D^0 \to \pi^+ K^-$	36	223	206	429	57841
10	$B^- \to e^- \bar{\nu}_e D_0^{*0}, D_0^{*0} \to \pi^0 D^0, D^0 \to \pi^+ K^-$	119	205	221	426	58267

#### $B \rightarrow (D^0 \rightarrow K\pi) e\nu$ Train-Test Template



USED IN PRESENTATION: 50% of signal samples for PDF construction, 50% for composite fit and validation

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# $\begin{array}{c} B \to (D^0 \to K\pi)\tau\nu \text{ Train-Test} \\ \text{Template} \end{array}$



#### $B \rightarrow (D^* \rightarrow K\pi) e\nu$ Train-Test Template



# $\begin{array}{c} B \to (D^* \to K\pi)\tau\nu \text{ Train-Test} \\ \text{Template} \end{array}$





# $B \rightarrow (D^0 \rightarrow K\pi)\tau\nu$ Template









## Fake D Template



# Fake B Template



# $q\bar{q}$ Template





# Previous $R(D^{(*)})$ Results

A test of lepton flavor universality...



 $R(D^*)$ 

0.4

HFLAV average

**HFLAV** 

 $\Delta \chi^2 = 1.0$  contours

# Previous $R(D^{(*)})$ Results

A test of lepton flavor universality...



 $R(D^*)$ 

0.4

HFLAV

2021

LHCb15

**HFLAV** 

 $\Delta \chi^2 = 1.0$  contours





