



Optimization and Evaluation of KL Identification Performance

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Belle II Summer School Duke University

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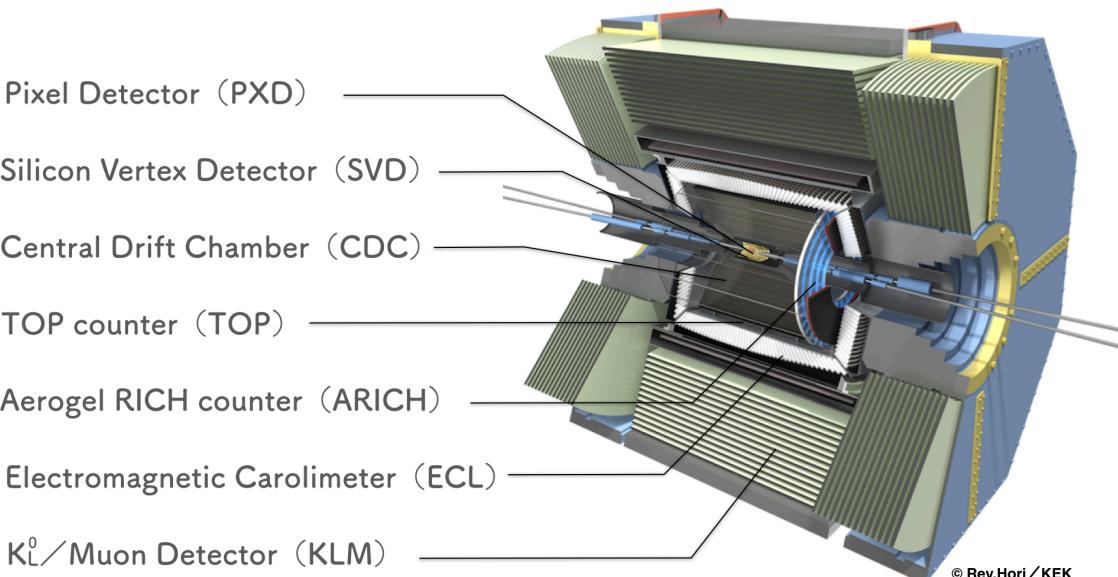
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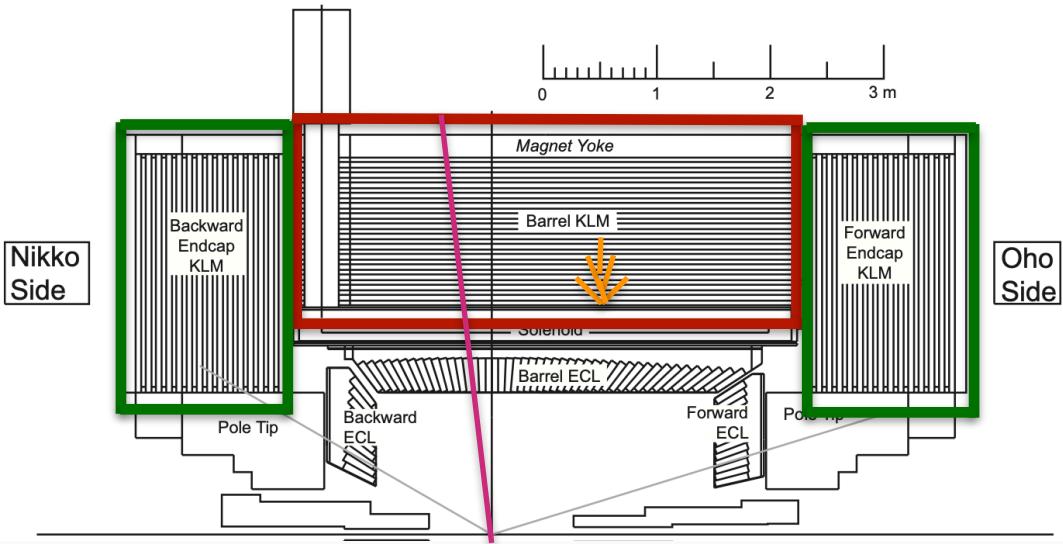
Outline of my activities

- Develop improved K_L identification (ID) using a Boosted Decision Tree (BDT)
- Identify KLM clusters from true K_L 's in experimental data using $\phi \rightarrow K_L K_S$ events
- Identify KLM clusters from true K_L 's in experimental data using $B \rightarrow D^* \pi$ events
- Goal: identify K_L with a higher identification efficiency and *lower fake-rate*



The K-Long Muon Detector (KLM)

- Consists of **barrel** and **forward** and **backward endcap**
- KLM polar angle acceptance:
 $20^\circ < \theta < 155^\circ$
- **Barrel** setup: Alternating resistive plate chambers (RPCs) and iron plates
- **Endcap** setup: plastic scintillators with silicon photomultipliers
- Detect **muons** by hit along their path and **K_L** by hadronic shower



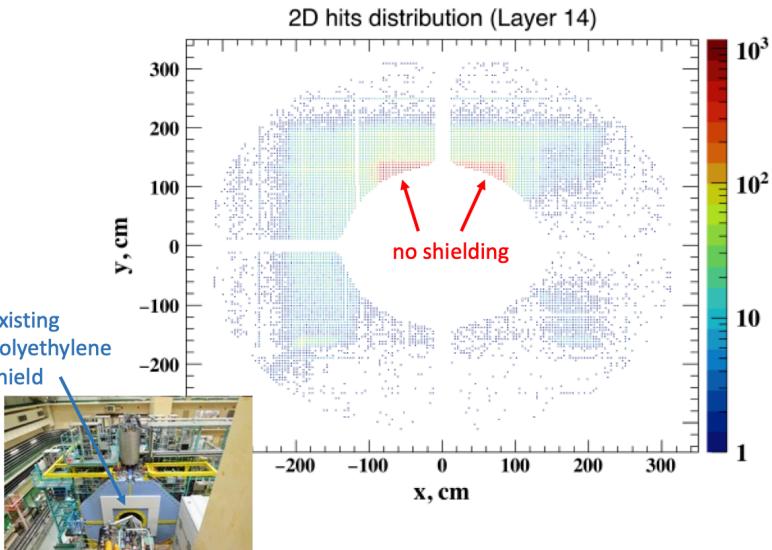
[T. Abe et al., Belle II Technical Design Report, 2010, ArXiv:<https://arxiv.org/pdf/1011.0352.pdf>]

Beam induced neutrons as background

[Leo Piilonen, KLM Work Plan for Summer 2022, 2010, [indicohttps://indico.belle2.org/event/3781/contributions/18728/attachments/9438/14494/KLM_Summer2022Plans.pdf](https://indico.belle2.org/event/3781/contributions/18728/attachments/9438/14494/KLM_Summer2022Plans.pdf)]

- Important beam background sources are:
 - Beam-Gas interaction
 - Touschek effect
 - Radiative Bhabha scattering
- Fast neutrons are created outside the detector region
- Neutrons interact hadronically with detector material —> **Causes clusters in KLM that can produce fake K_L candidates**

Neutron illumination is not uniform across FWD endcap face



What do we need, do and want?

We need:

Good K_L candidate sample

Bad K_L candidate sample

We do:

BDT training on KLM
variables

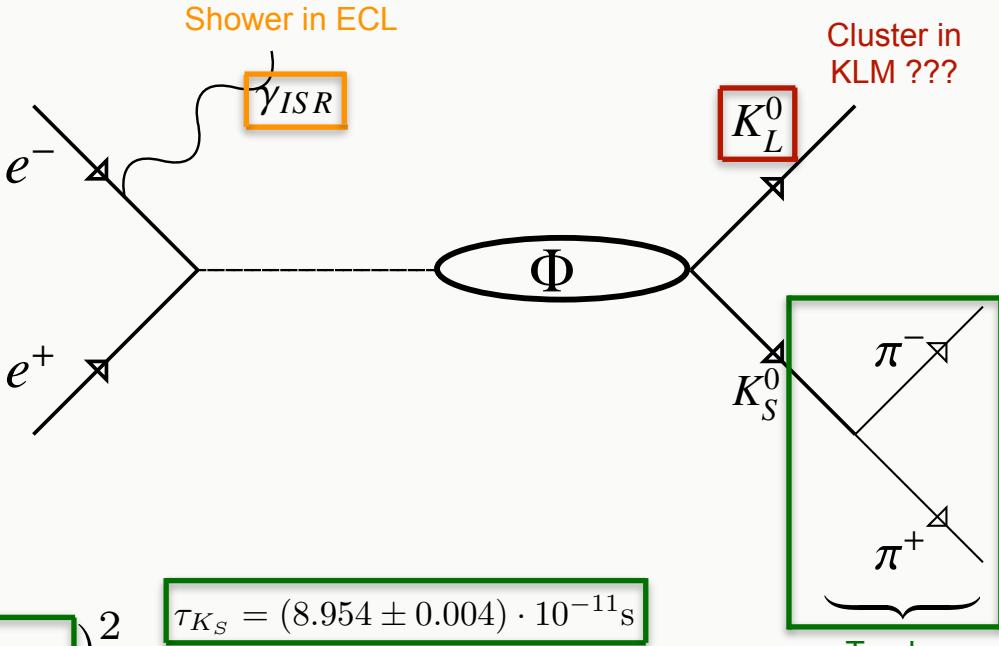
We want:

Classification for
each KLM cluster
whether to be a K_L
or not

What to do First?

- Find good K_L clusters and bad K_L clusters in the KLM
 - Use a very clean decay:
- $e^+e^- \rightarrow \gamma_{ISR}\Phi \rightarrow K_L K_S$
- with $K_S \rightarrow \pi^+\pi^-$
- γ_{ISR} and K_S is easy to reconstruct
 - Do not reconstruct K_L , but predict where the K_L should be in an event

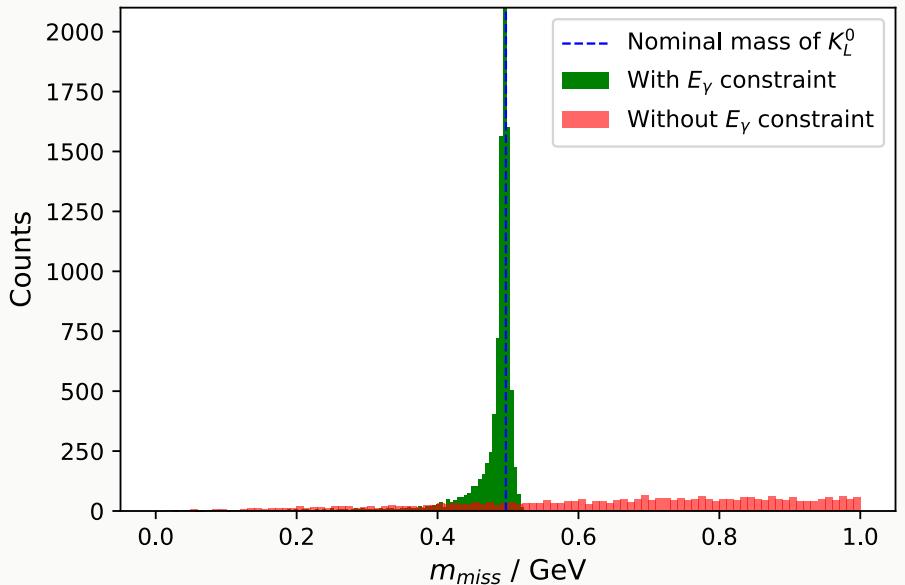
$$m_{miss}^2 = p_{miss}^2 = (p_{beam} - p_\gamma - p_{K_S})^2$$



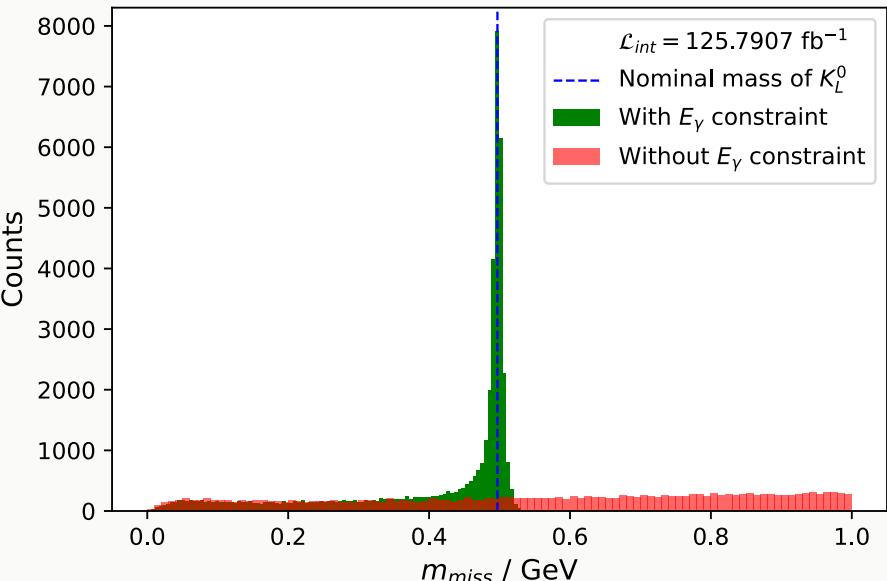
$$\tau_{K_S} = (8.954 \pm 0.004) \cdot 10^{-11} \text{ s}$$

$$\tau_{K_L} = (5.116 \pm 0.021) \cdot 10^{-8} \text{ s}$$

Missing Mass with/without Photon Energy Constraint

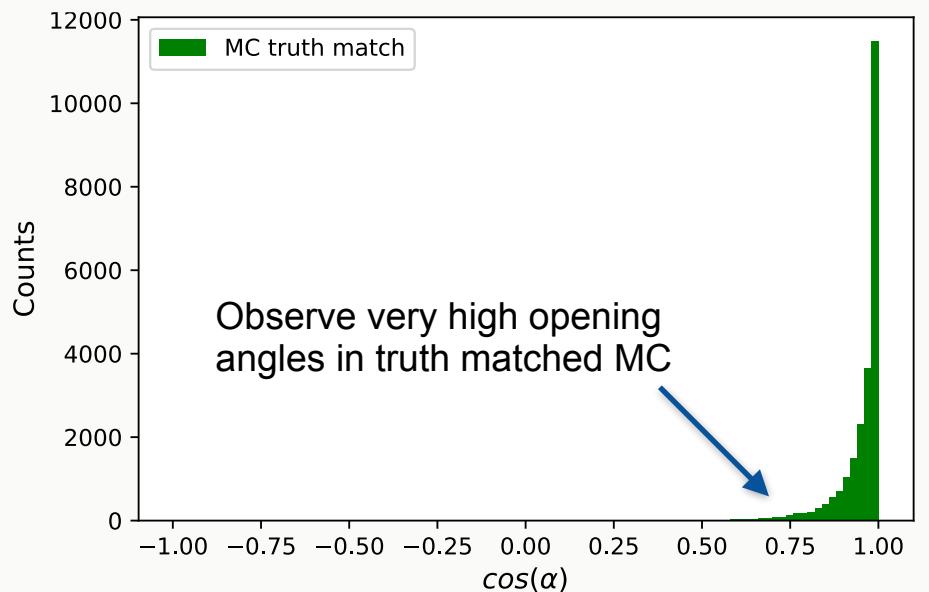


Signal MC

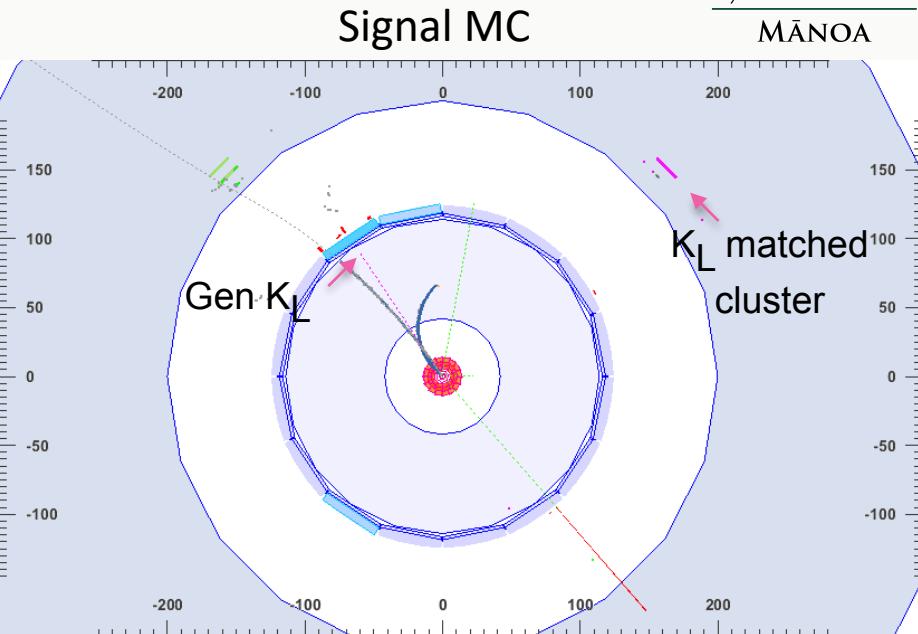


Data

Cluster truth matching is failing?

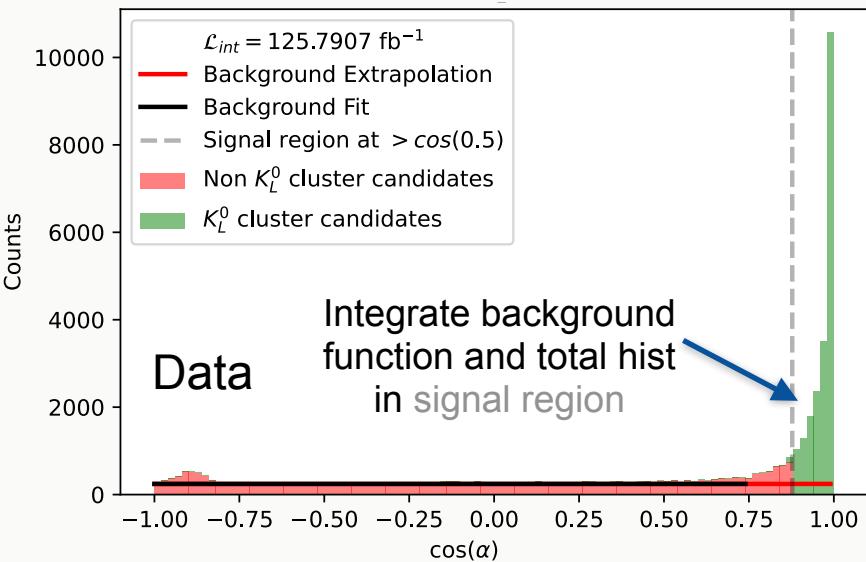


- KLM Cluster-Truth matching is broken



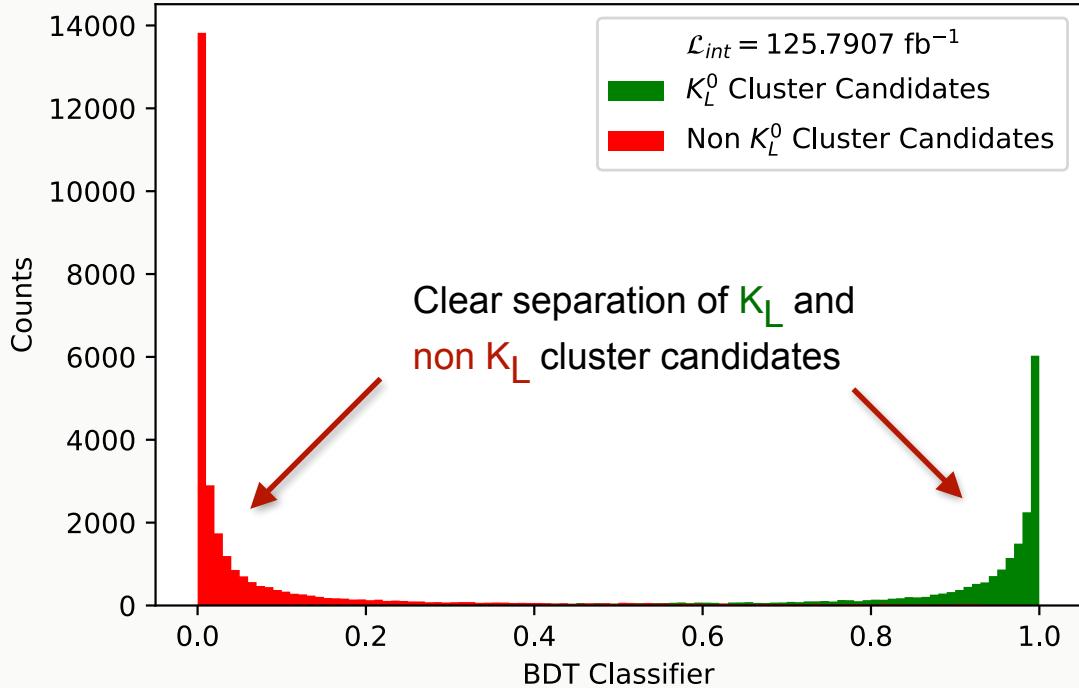
Preliminary definition of K-Long Cluster Candidates

- Preliminary definition of K_L cluster candidates by the opening angle between missing momentum and **KLM cluster** vector
- Good K_L cluster candidates defined by $\alpha < 0.5$ rad
- Identification efficiency $\approx 0.733 \pm 0.007$, fake-rate $\approx 1.225 \pm 0.008$ average fake cluster per event
- This efficiency **does not include the detection efficiency** but only the identification of a cluster as a K_L

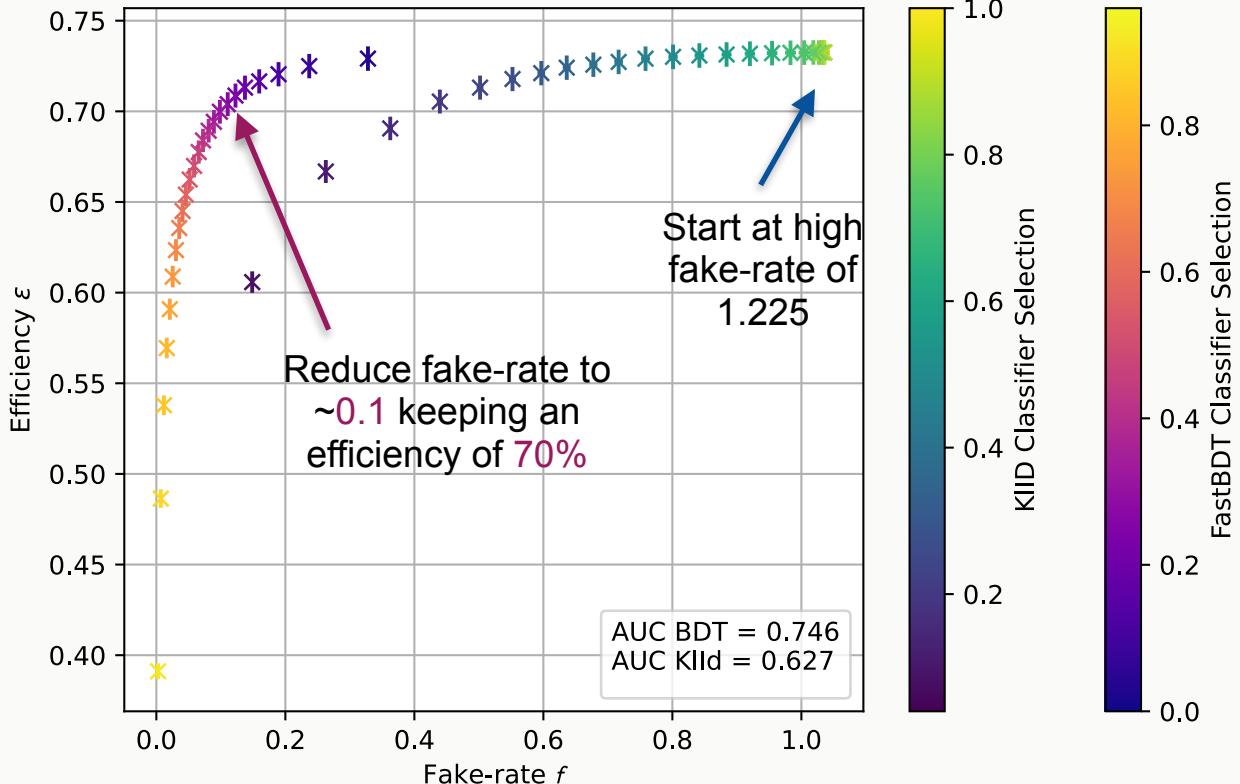


Start the BDT Training

- Start training BDT on a large number of KLM variables of experimental data
- In the end use 12 out of the 23 KLM variables
- BDT clearly distinguishes between K_L^0 cluster candidates and expected fast neutron cluster candidates plus other background clusters



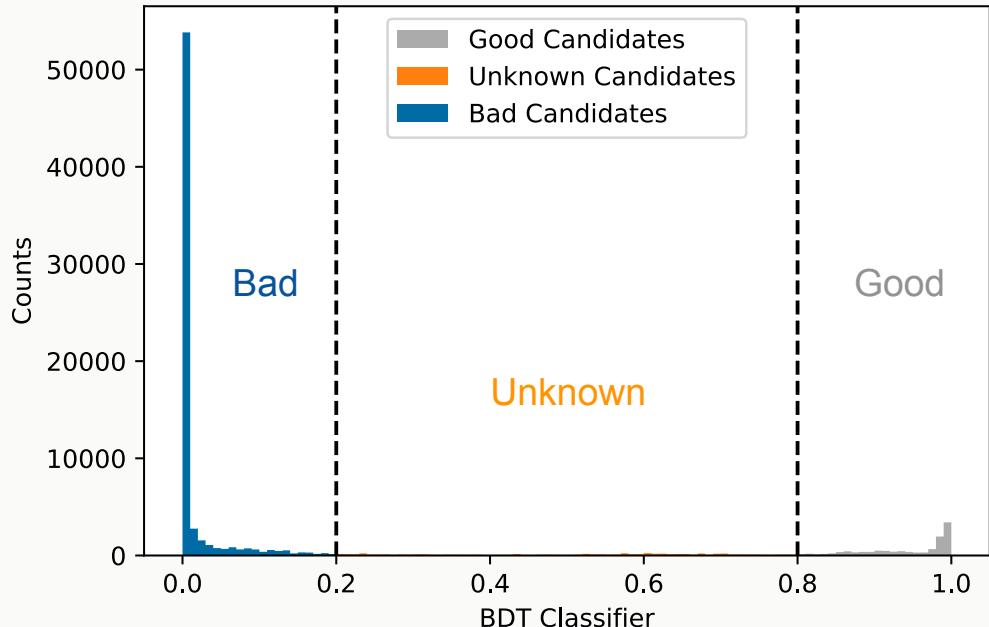
BDT Identification Efficiency and Fake-Rate



Apply BDT to a Data sample with low momentum K_L

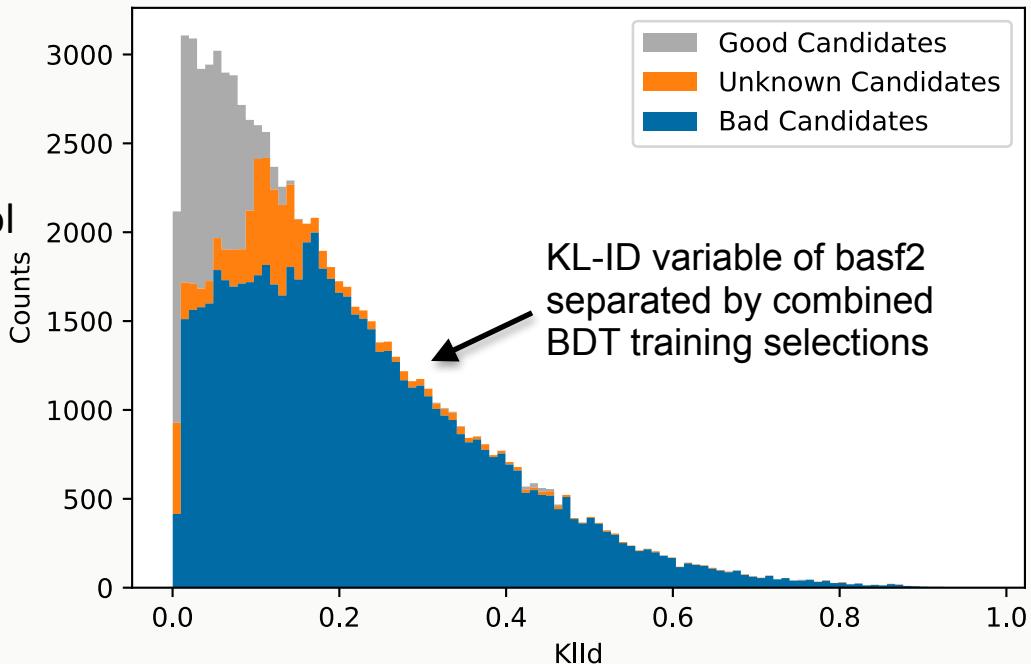
- Use custom GEANT4 simulated signal events of generated K_L 's
- Train on:
 - klmClusterInnermostLayer
 - klmClusterEnergy
 - klmClusterPhi
 - klmClusterPositionZ
 - klmClusterKId
- Apply FastBDT training to hadronic skimmed Data
- Only reconstruct KLM clusters with no matched tracks
- Cut at $<0.2 \rightarrow$ fake-rate ~ 0.25 average fake clusters per event

$$f_{\text{comb}} = \frac{f_\phi \cdot N_{\text{obs}} - N_{\text{removed}}}{N_{\text{obs}}}$$



Compare FastBDT to current tools

- Overlap of bad, **unknown** and good clusters is observed
- In current classifier ($K\text{Ild}$) not distinguishable
- FastBDT performs better than current tool for K_L identification —> above 0.15 we observe only potential bad candidate clusters
- Need validation that the potential **good** clusters are indeed good K_L clusters



Validation of new K_L identification

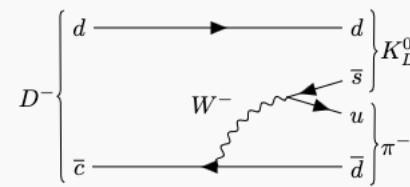
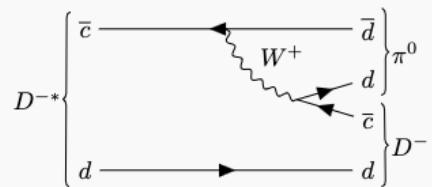
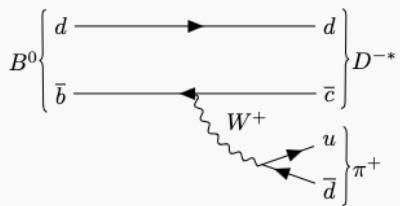
- Generate 25k signal
MC events of $B \rightarrow \pi^+ [D^{-*} \rightarrow \pi^0 [D^- \rightarrow K_L^0 \pi^-]]$
- Use constraints on the
 B , D^- and D^{-*} to solve
for missing K_L energy
and momentum
components

$$E_{K_L} = E_B - E_{\pi^-} - E_{\pi^0} - E_{\pi^+}$$

$$|\vec{p}_B|^2 = (\vec{p}_{K_L} + \vec{p}_{\pi^-} + \vec{p}_{\pi^0} + \vec{p}_{\pi^+})^2$$

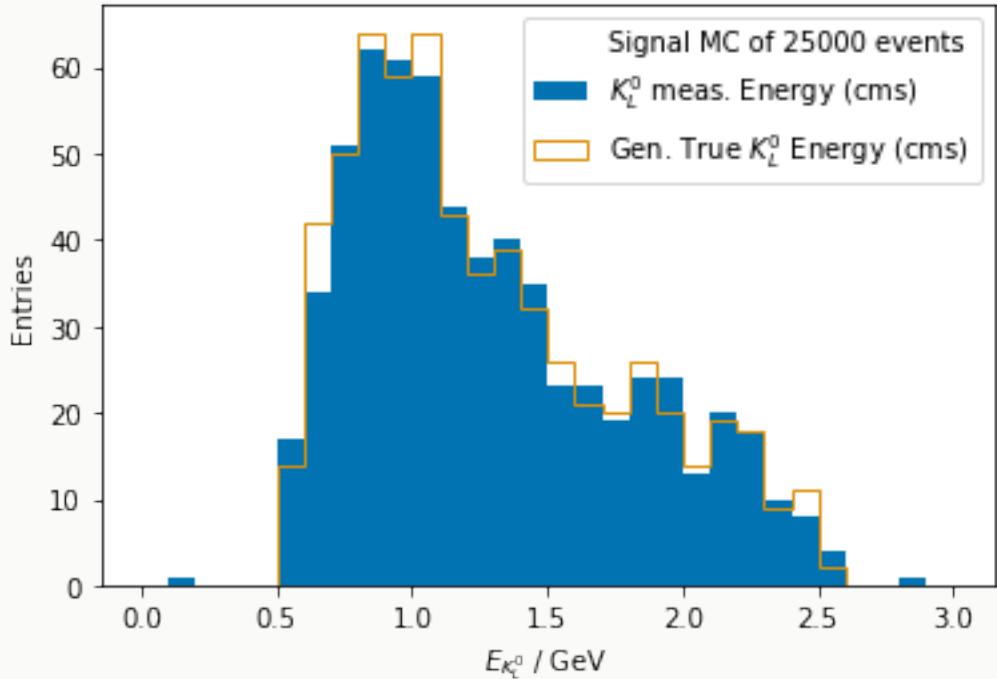
$$|\vec{p}_{D^{-*}}|^2 = (\vec{p}_{K_L} + \vec{p}_{\pi^-} + \vec{p}_{\pi^0})^2 \quad \longrightarrow \quad |\vec{p}_{D^{*-}}|^2 = E_{D^{*-}}^2 - m_{D^{*-}}^2$$

$$|\vec{p}_{D^-}|^2 = (\vec{p}_{K_L} + \vec{p}_{\pi^-})^2 \quad \longrightarrow \quad |\vec{p}_{D^-}|^2 = E_{D^-}^2 - m_{D^-}^2$$

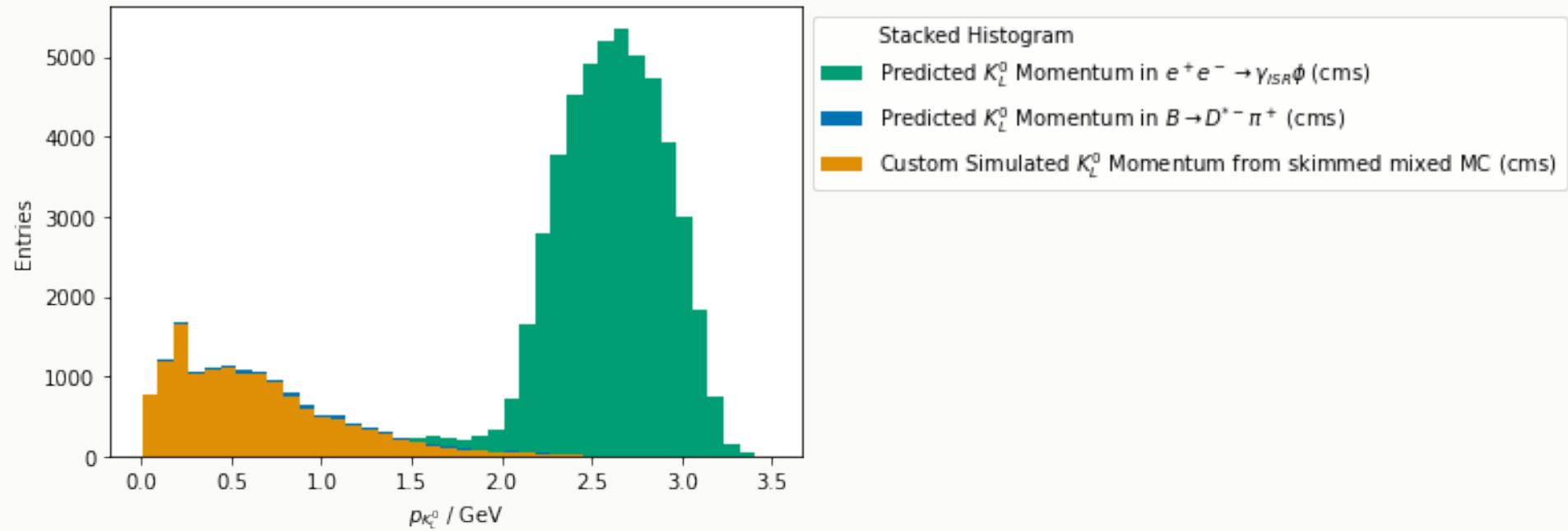


Predicted KL energy

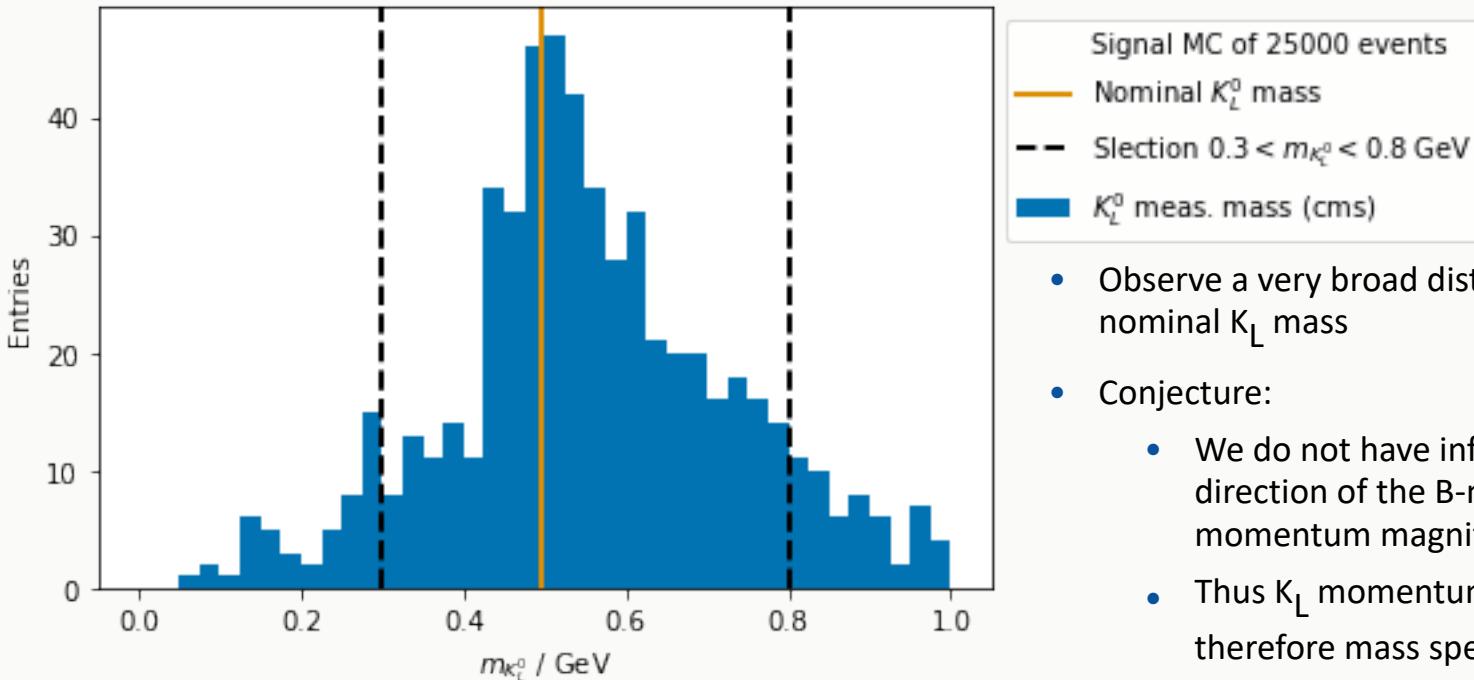
- Observe good agreement between generated true and predicted K_L energy
- Difference comes through resolution effects of pion reconstruction



Momentum comparison of all studies



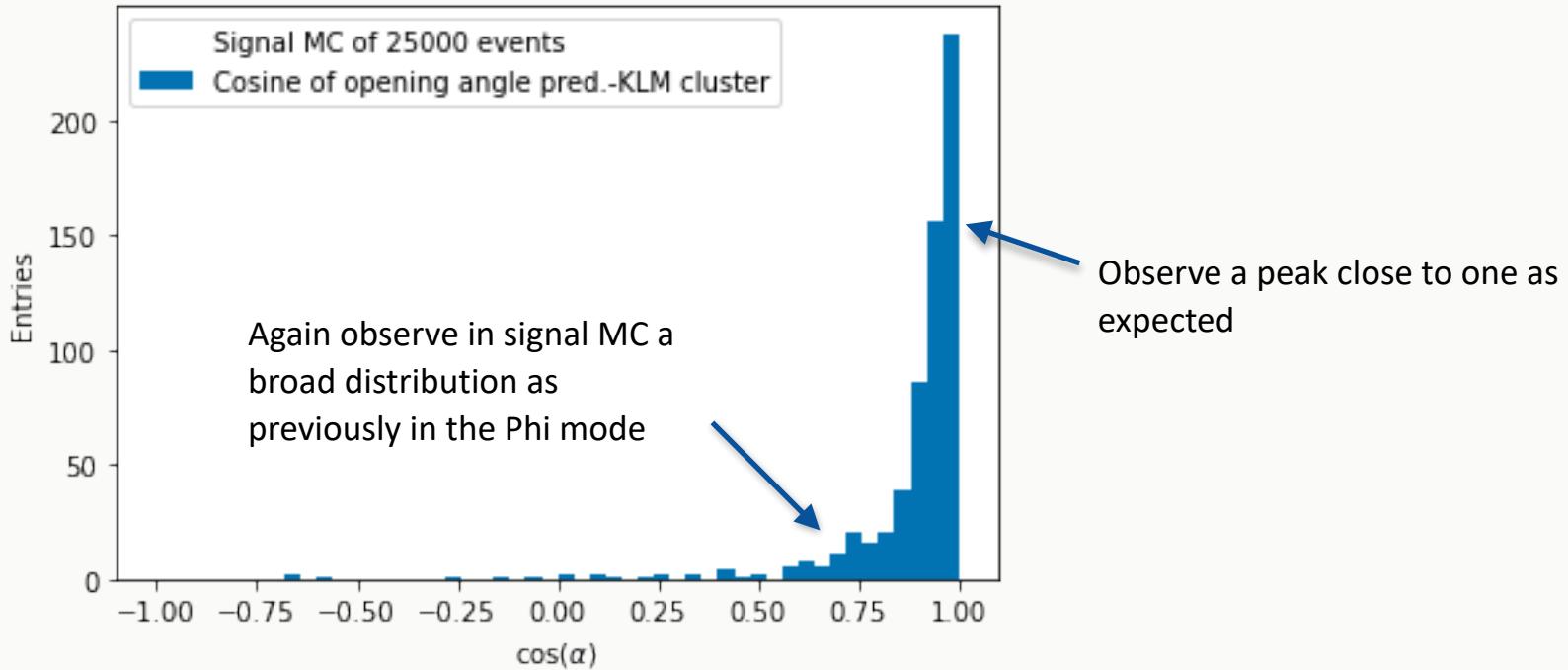
Predicted missing mass



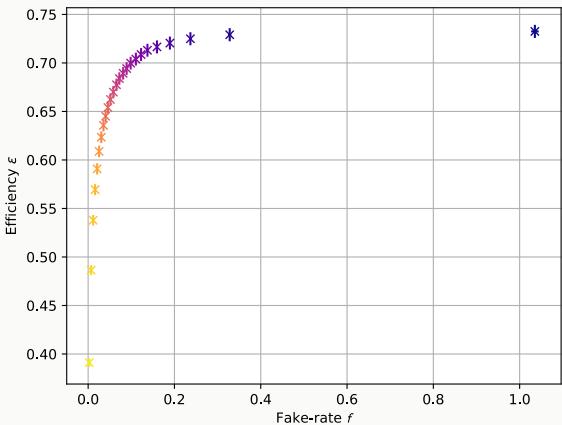
- Observe a very broad distribution around the nominal K_L mass
- Conjecture:
 - We do not have information about the direction of the B-meson but only its momentum magnitude
 - Thus K_L momentum shows smearing and therefore mass spectrum as well



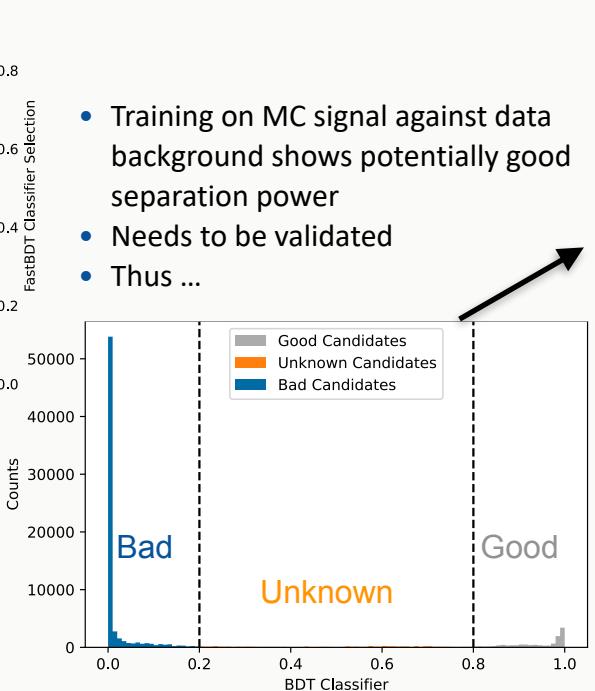
Opening angle between predicted vector and cluster in KLM



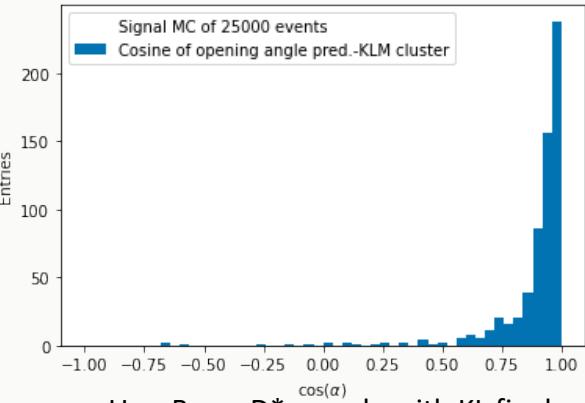
Summary & Outlook



- In the Φ mode we are able to reduce the fake-rate while keeping a high identification efficiency
- But only high momentum KL
- Thus ...



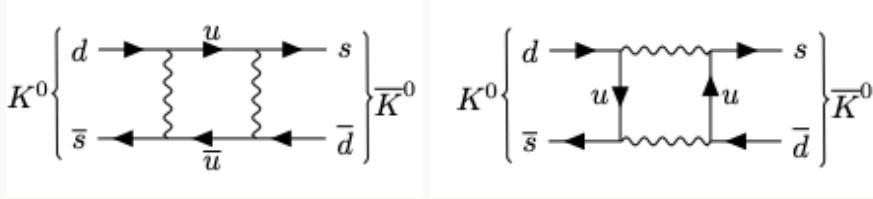
Thank you for your attention!



- Use $B \rightarrow D^* \pi$ mode with KL final state as validation mode
- Could predict the KL energy/momentum
- Observe same behavior of opening angle as in Φ signal MC
- Next step repeat for mixed MC and experimental data

Backup: Neutral long living Kaons?

- Neutral Kaons mix via box diagrams —> no CP eigenstates by itself but linear combination K_1 and K_2
- Found physical state of a short living and long living neutral Kaon
- If CP conserved
 $|K_S\rangle \approx |K_1\rangle$, $|K_L\rangle \approx |K_2\rangle$
- Cronin and Fitch found $K_L \rightarrow \pi\pi$ decays which was the first evidence of direct CP violation
- K_S and K_L are linear combinations of K_1 and K_2 with a correction factor ϵ



$$\tau_{K_S} = (8.954 \pm 0.004) \cdot 10^{-11} \text{ s}$$

$$\tau_{K_L} = (5.116 \pm 0.021) \cdot 10^{-8} \text{ s}$$

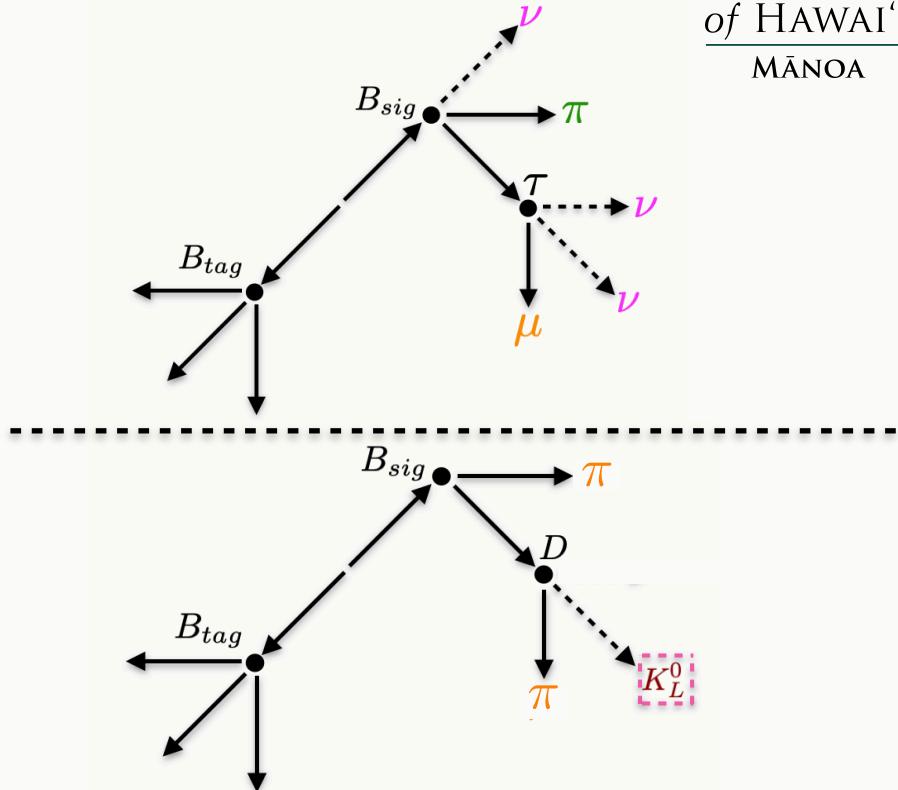
$$|K_S\rangle = \frac{1}{\sqrt{1 + |\epsilon|^2}} (|K_1\rangle + \epsilon |K_2\rangle) e^{-i\lambda_{st}}$$

$$|K_L\rangle = \frac{1}{\sqrt{1 + |\epsilon|^2}} (|K_2\rangle + \epsilon |K_1\rangle) e^{-i\lambda_{Lt}}$$



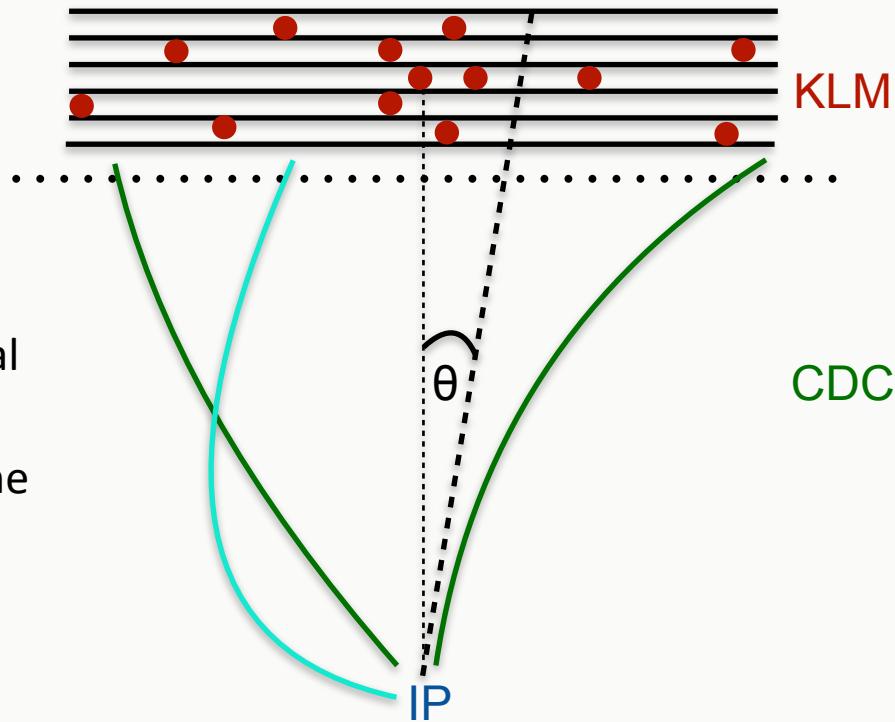
Backup: Who ordered this background?

- In $B \rightarrow \pi\tau\nu$ followed by $\tau \rightarrow \mu\nu\nu$, events with K_L 's mirror the signature of this decay process
- Decays like $B \rightarrow D\pi$ and $D \rightarrow [K_L^0]\pi$ are possible background sources
- Vetoing these events decreases the efficiency



Backup: K-Long cluster building

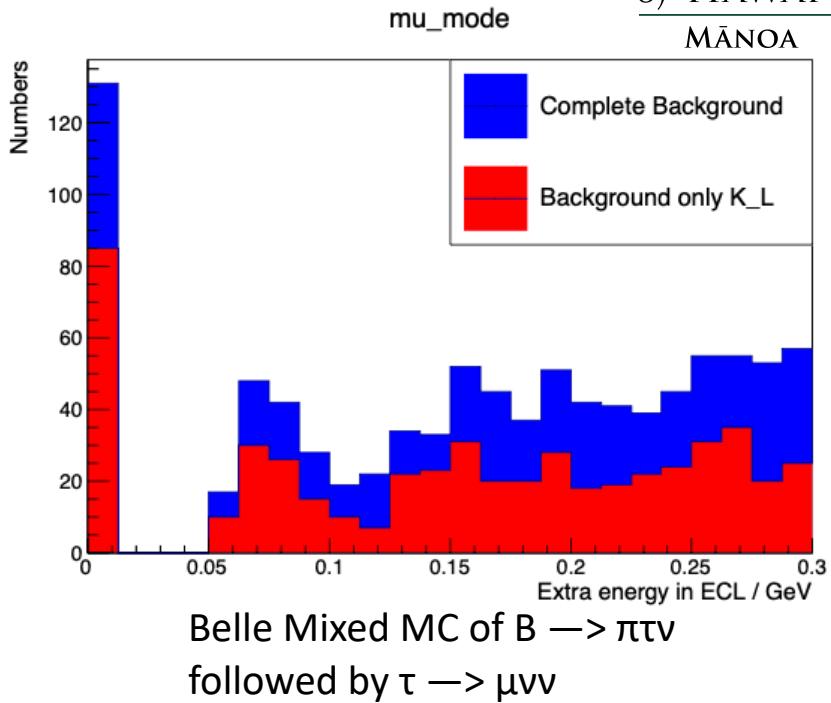
- In **KLM**, hits within a $\theta=5^\circ$ cone drawn from the interaction point (IP) are formed to a cluster
- K_L identification:
 - Only considered to be K_L cluster candidate if no charged track from central drift chamber (**CDC**) can be extrapolated into the KLM and lies within **150 cm** to the cluster





Backup: Why are we doing this?

- In semitauoninc B decays we observe deviations from the standard model
- Studies of $B \rightarrow \pi\tau\nu$ can help to understand this deviation, however those decays come with a lot of background
- One of the major background sources are events with missing K_L 's, especially low momentum K_L 's
- We see, in mixed MC of Belle $B \rightarrow \pi\tau\nu$ followed by $\tau \rightarrow \mu\nu\nu$, approximately in 55.1% of the events a K_L is found
- In Belle a K_L veto led to a 5% increase of $B \rightarrow \tau\nu$ sensitivity [1]



Backup: Fast Neutrons in e^+e^- collision?

Beam-Gas Interaction:



- Electron scatters on nuclei or atomic electron of the gas
- Creates secondary particles
- Detected as background in the Detector

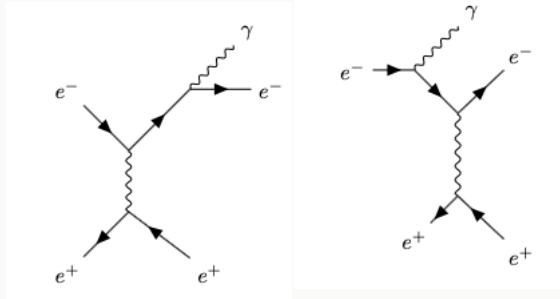
Touscheck Effect:



- Large **momentum transfer**
- Transfer from transverse to longitudinal
- Longitudinal momentum higher than energy acceptance of the ring electron is lost

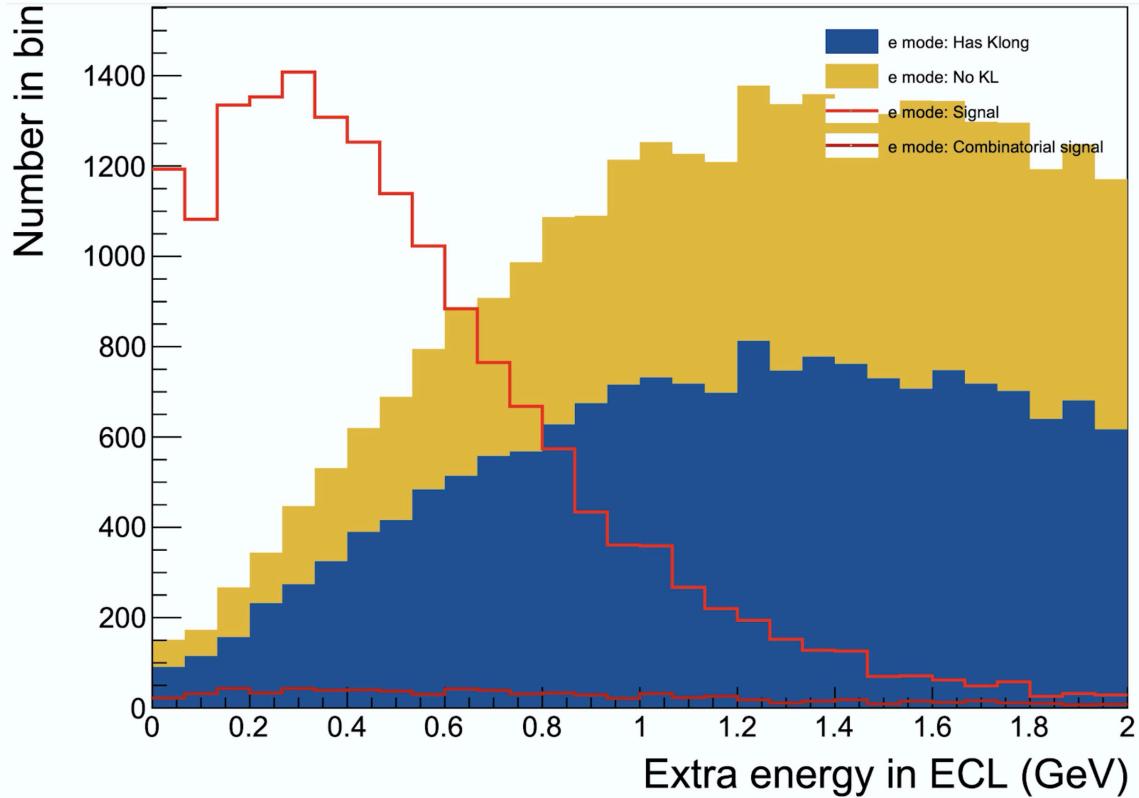
- Shower from off-orbit beam particles or photons interact with beam pipe material
- The created secondaries excite nuclei via giant dipole resonance —> producing neutrons

Radiative Bhabha scattering:



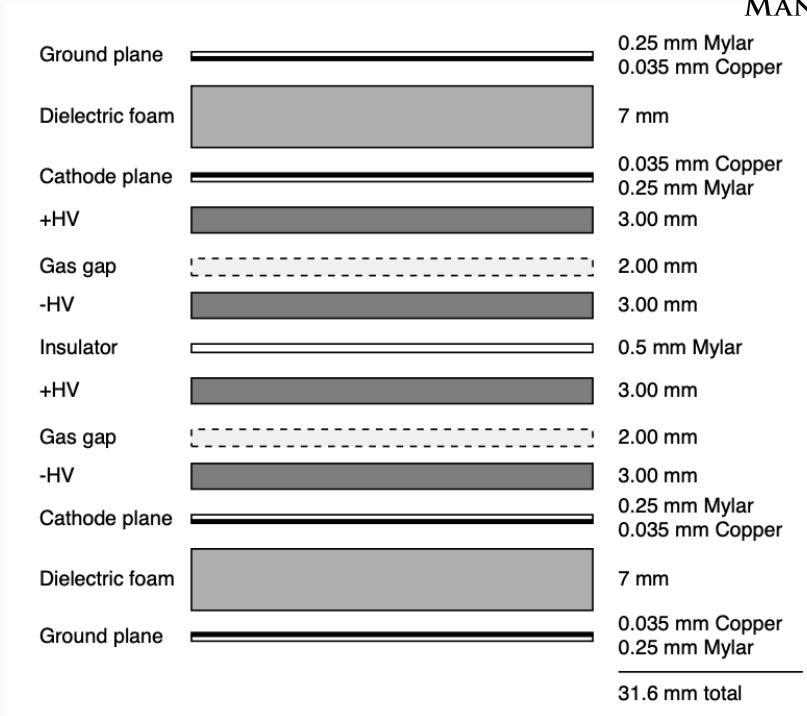
- ISR or FSR of a photon in e^+e^- scattering

Backup: Who ordered this background?

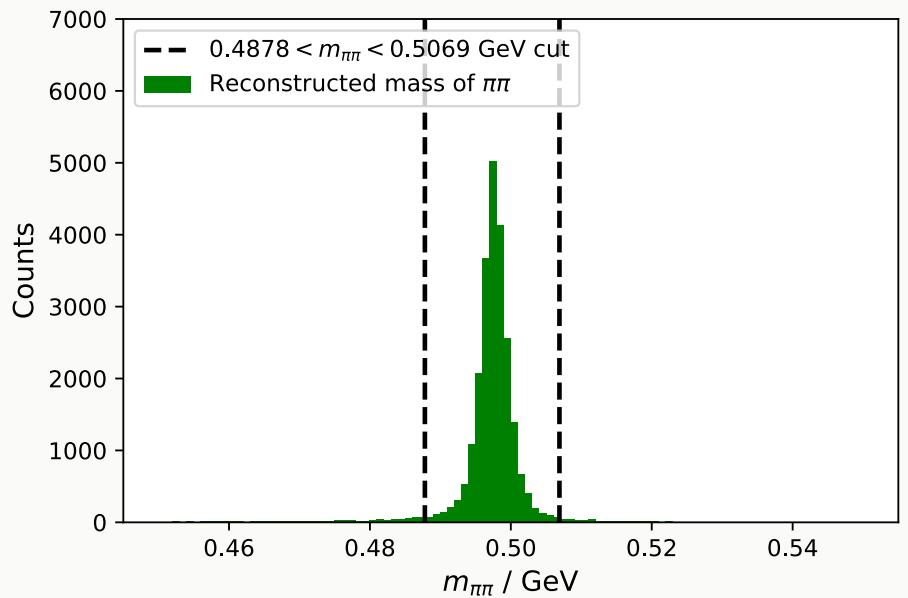


Backup: Resistive Plate Chambers (RPC's)

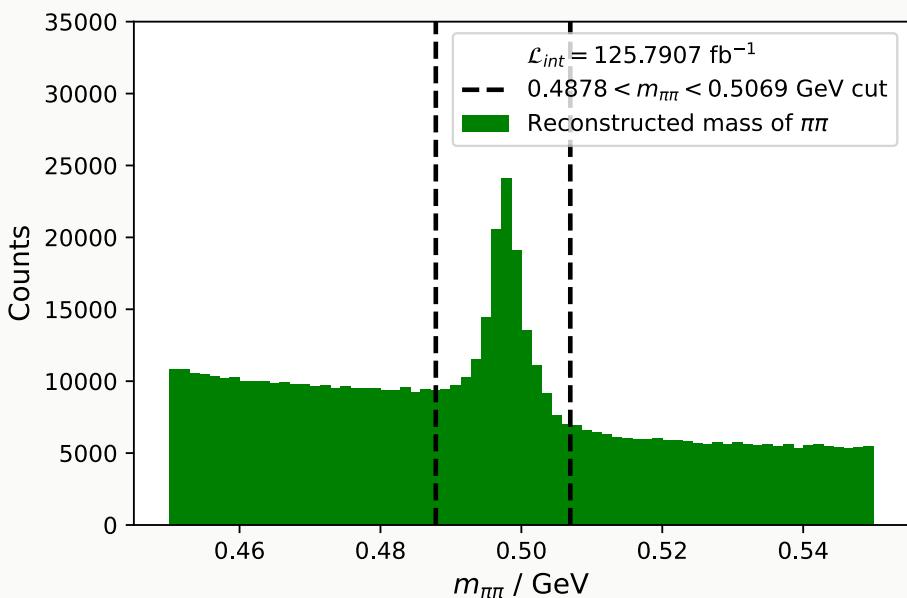
- A gas volume is enclosed by two glass electrodes supplied with a high voltage
- In Belle II use two chambers to form a superlayer —> Resulting in 99% detection efficiency
 - Advantage: If one chamber fails, detection efficiency still up to 90 - 95%
- Orthogonal readout stripes are placed behind an insulator on both ends
- Use 48 readout stripes for θ and 36 (48) stripes in layers 0 to 6 (7 to 14) for ϕ measurement in one module



Backup: Reconstructed K-Short Mass

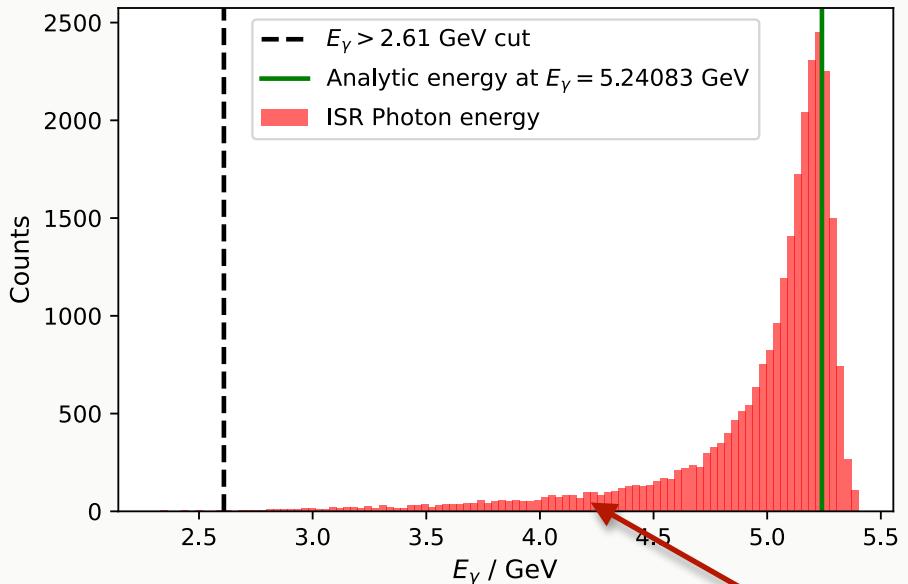


Signal MC

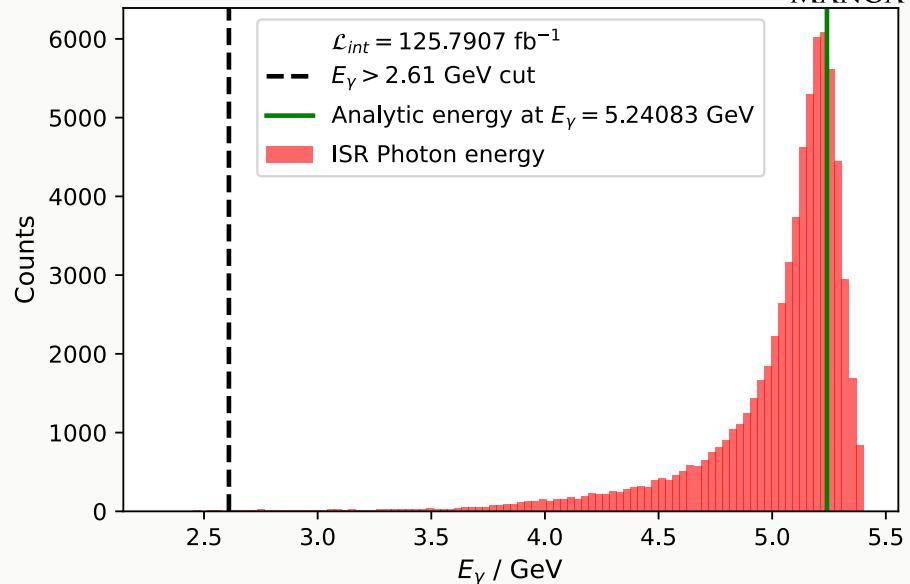


Data

Backup: Photon Energy Signal MC and Data



Signal MC



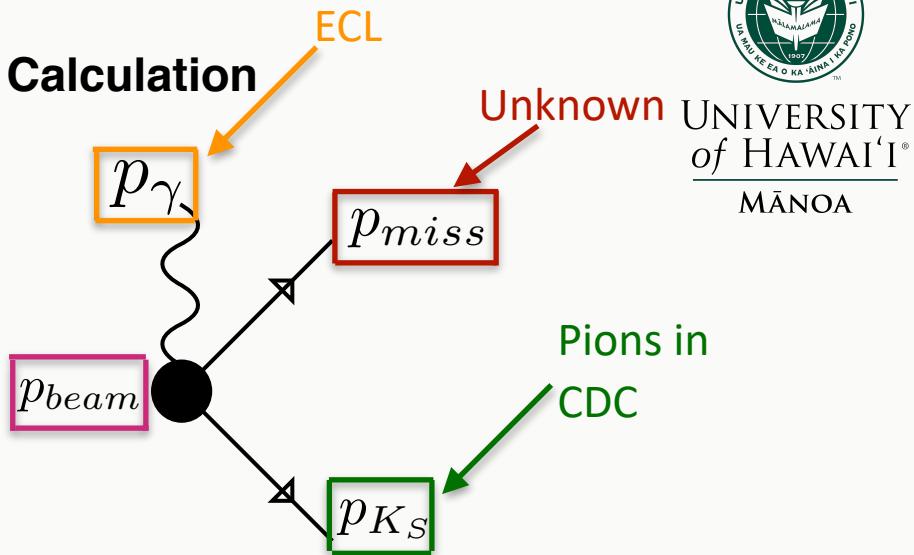
Data

Long tail, due to **ECL**
energy leakage for high
energy photons

Backup: Missing Mass Calculation

- Do not use any KLM information
- Use four-momentum vector of K_S , γ_{ISR} and beam
- Thus get missing four-momentum vector and missing mass
- Use constraint on γ_{ISR} energy and correct momentum components

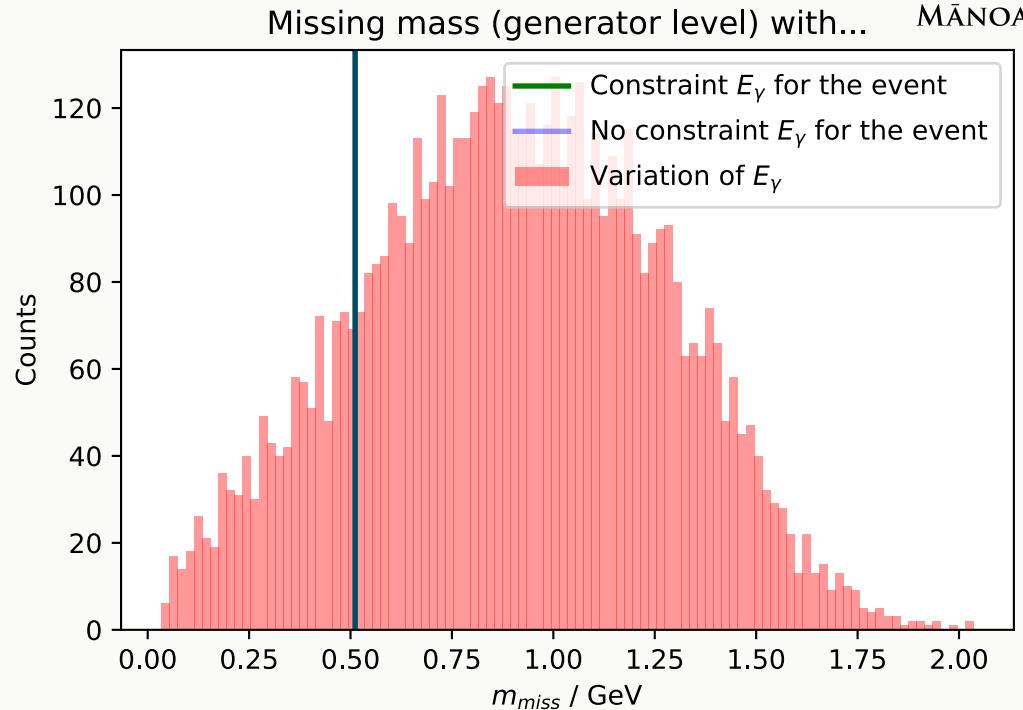
$$m_{miss}^2 = p_{miss}^2 = (p_{beam} - p_\gamma - p_{K_S})^2$$



$$E_\gamma^{con} \equiv E_\gamma = |\vec{p}_\gamma| = \frac{s - m_\phi^2}{2\sqrt{s}}$$

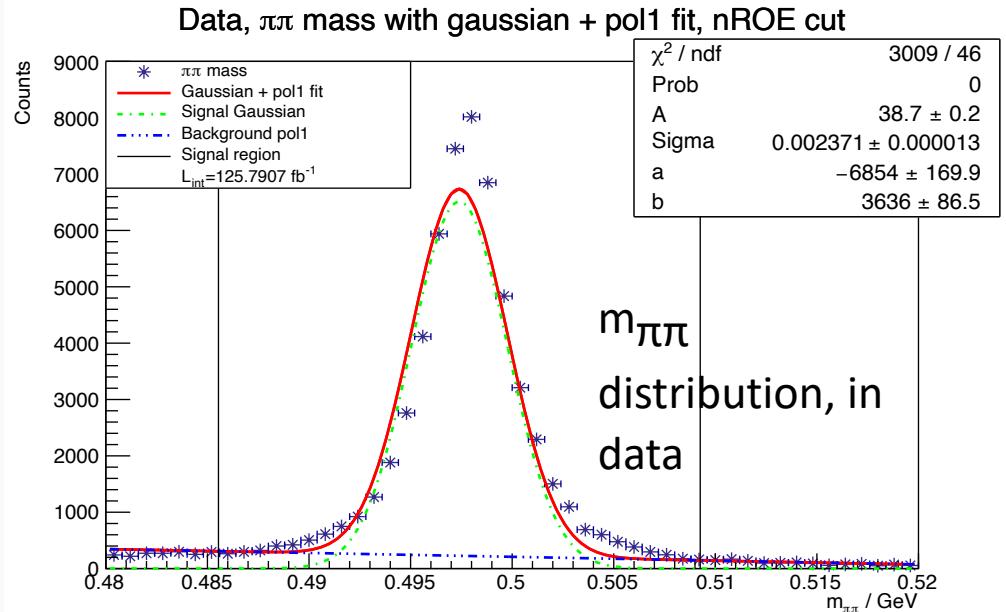
$$p_{\gamma,i}^{con} = p_{\gamma,i}^{meas} \cdot \frac{E_\gamma^{con}}{E_\gamma^{meas}}$$

- Study the influence of a small variation on the photon energy
- Use MC generator information and add a variation in form of a gaussian random variable with $\mu=0$ and $\sigma=0.1$ GeV
- We can observe a broadening, of the same level as in signal MC and data



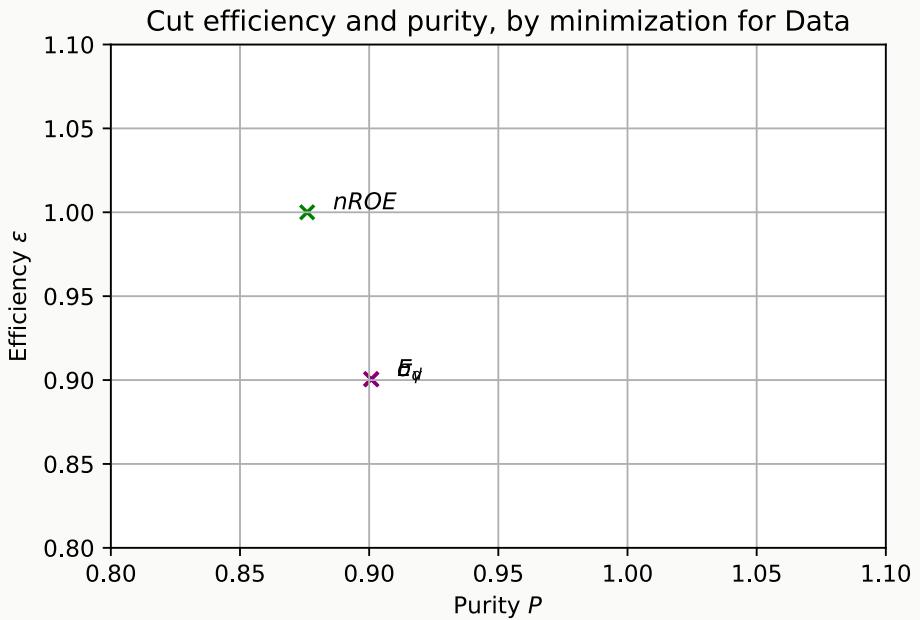
Backup: Purity and Efficiency of our Selection

- Determine the purity looking at the $m_{\pi\pi}$ distribution using background subtraction
- Fit Gaussian (**sig**) + pol 1st order (**back**)
- Define signal region by mean of fit $\pm 5\sigma$
- Integrate **signal** and **background** function over signal region
- End up with a purity and efficiency of 90%



Backup: Purity and Efficiency for Data BDT Training

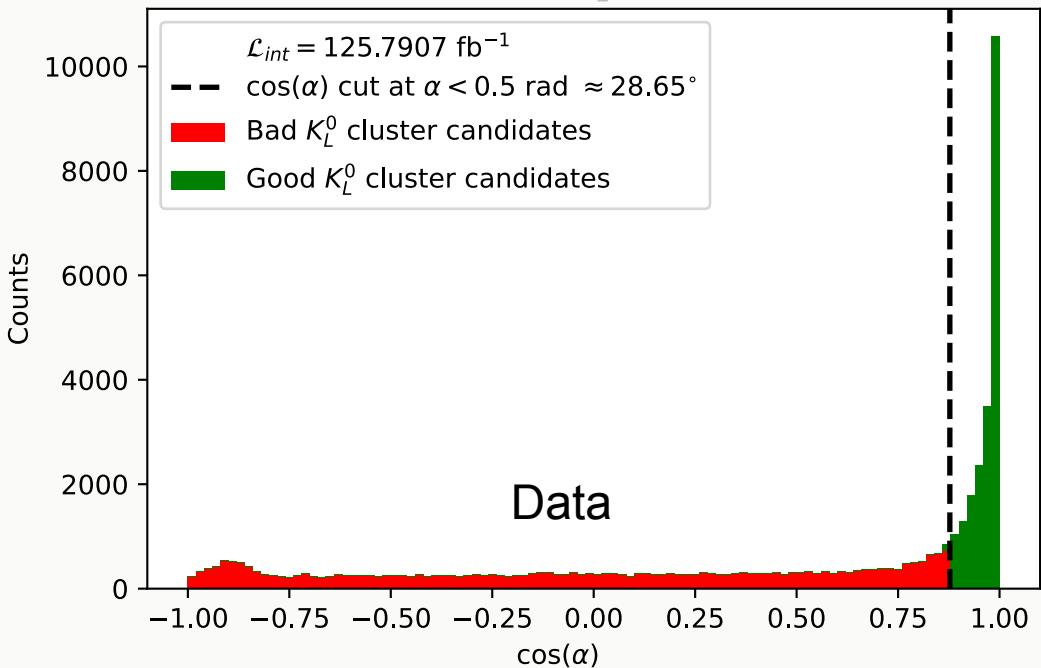
- For BDT Training create more Data
- Reiterate minimisation of cut purity and efficiency
- New cuts give $p=90\%$ and $\varepsilon=90\%$



Backup: Preliminary definition of K-Long Cluster Candidates

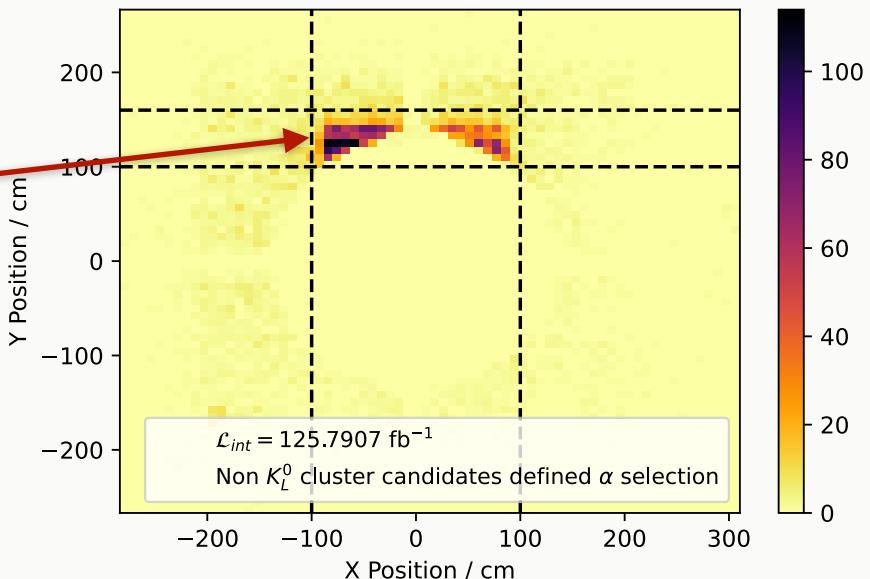
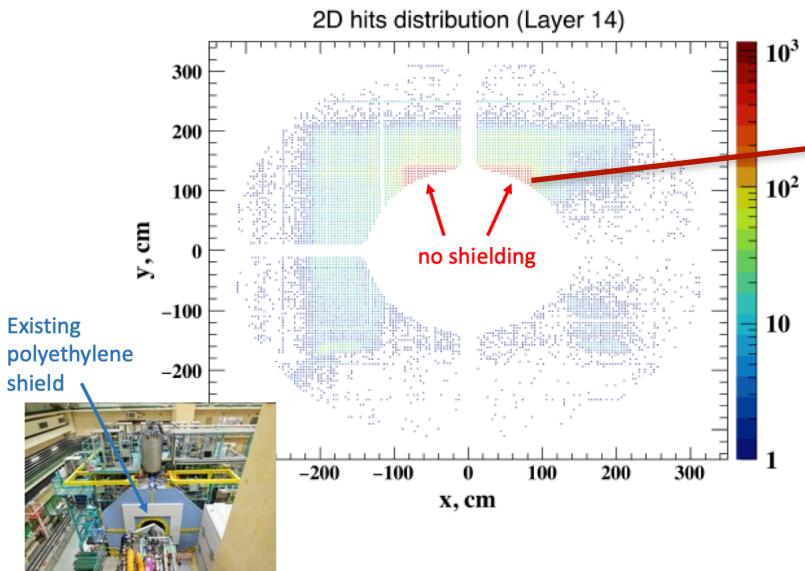


- Preliminary definition of K_L cluster candidates by the opening angle between missing momentum and **KLM cluster** vector
- Good K_L cluster candidates defined by $\alpha < 0.5$ rad
- What are these **bad K_L cluster candidates**?



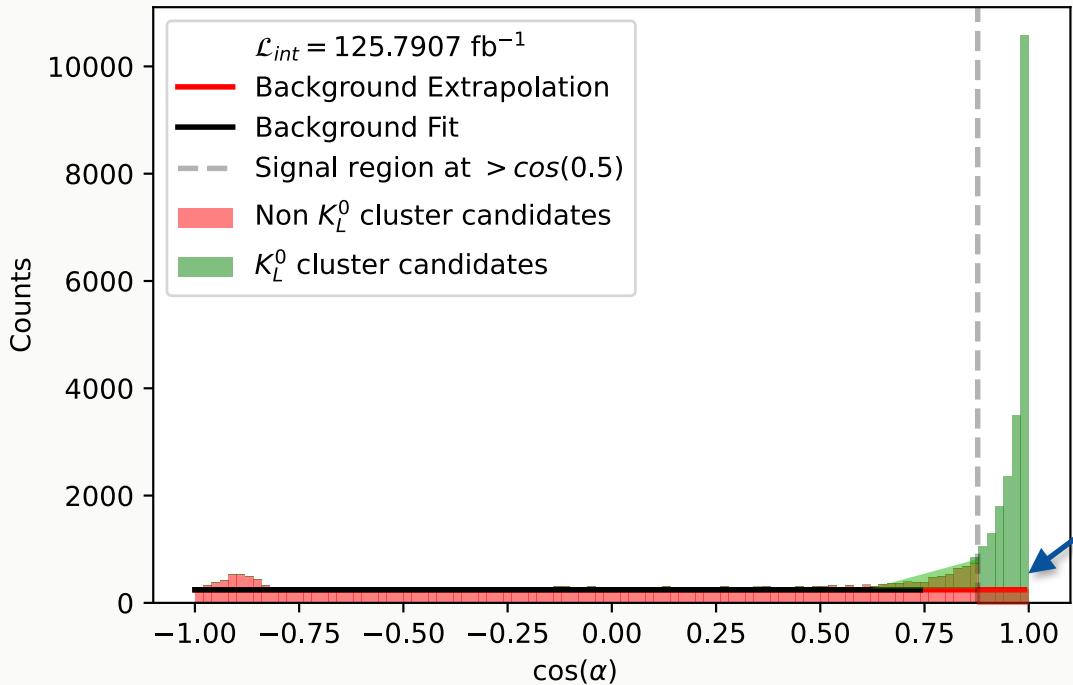
Backup: Even More Background

Neutron illumination is not uniform across FWD endcap face



- Apply selection and thereby neglect 4557 background clusters from beam induced fast neutrons

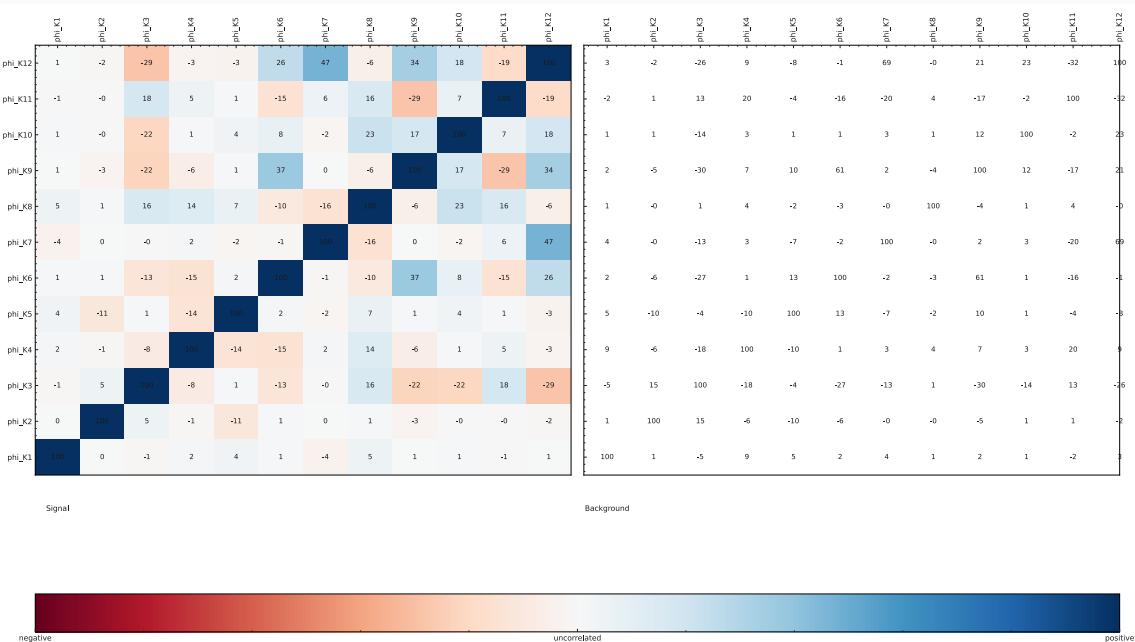
Backup: Background subtraction for Efficiency and Fake-Rate



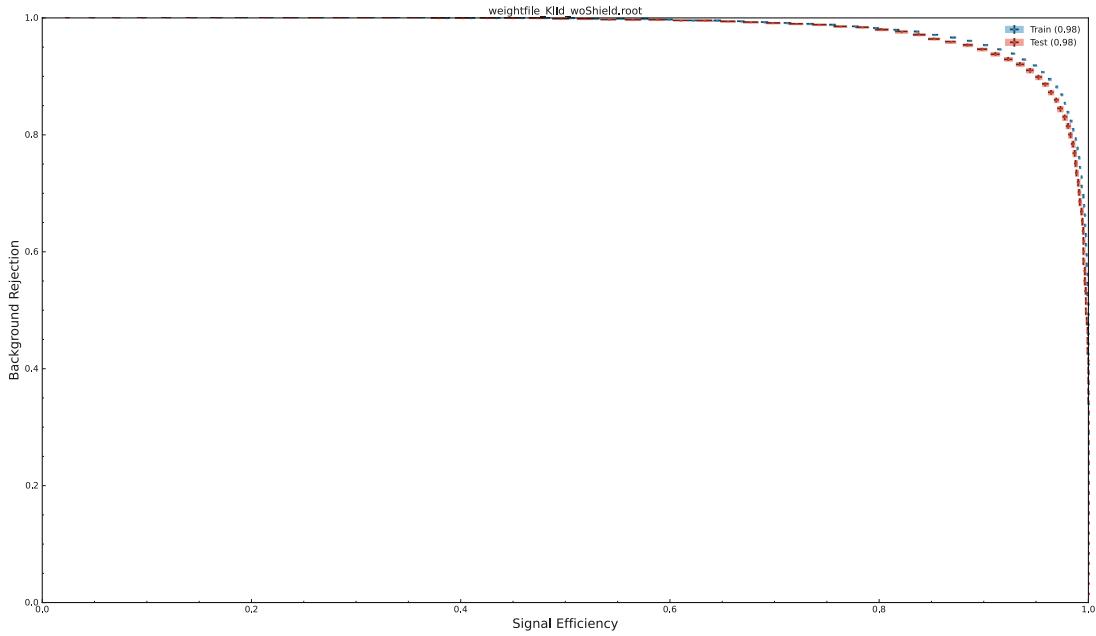
Integrate background function and total hist in signal region

- Identification efficiency $\approx 0.733 \pm 0.007$, fake-rate $\approx 1.225 \pm 0.008$ average fake cluster per event

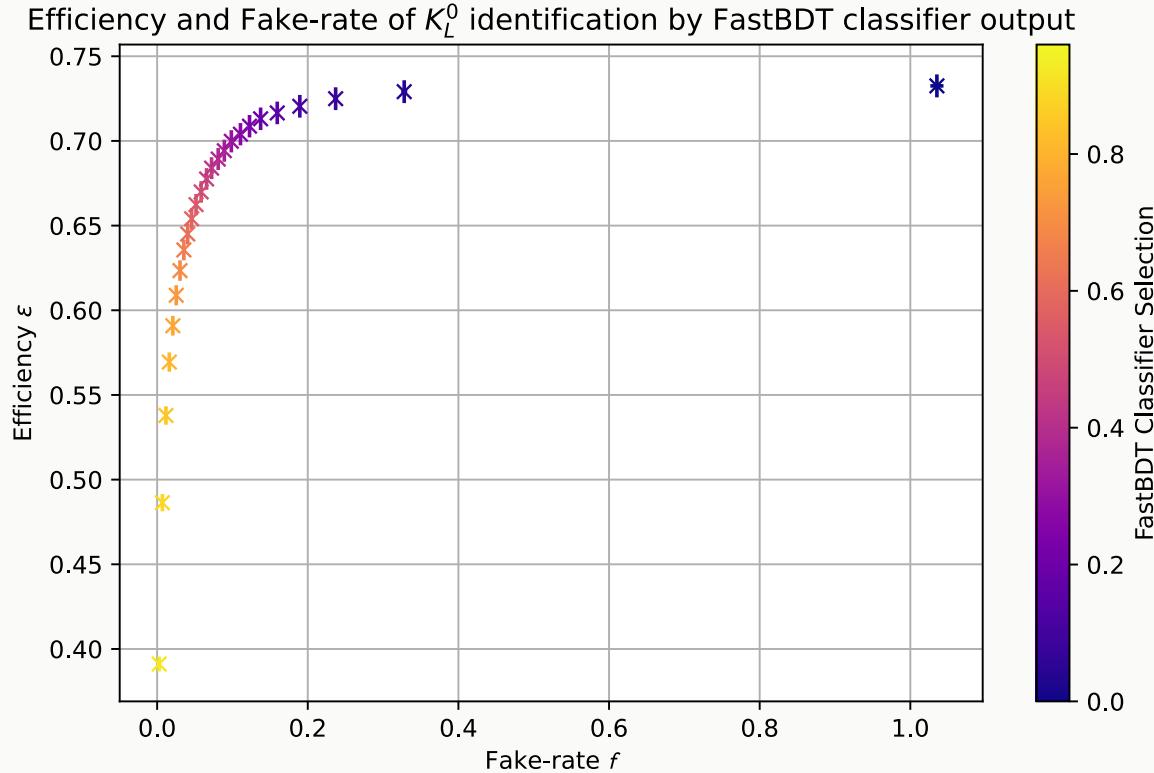
- phi_K1: KLM Cluster x Position
 - phi_K2: KLM Cluster z Position
 - phi_K3: KLM Cluster Inner Most Layer
 - phi_K4: KLM Cluster Theta
 - phi_K5: KLM Cluster Max Angle in CMS
 - phi_K6: KLM Cluster Matches nECL Cluster
 - phi_K7: KLM Cluster Track Distance
 - phi_K8: KLM Cluster Timing
 - phi_K9: KLM Cluster Belle ECL Flag
 - phi_K10: KLM Cluster Layers
 - phi_K11: KLM Cluster KlId
 - phi_K12: KLM Cluster Matches nTracks



Backup: BDT ROC Curve



Backup: Compare ID's of BDT and current KL-ID variable



Backup: If one channel closes another opens

- In order to predict low momentum K_L

use a different decay channel

- Use: $e^+e^- \rightarrow \gamma_{ISR} [J/\psi \rightarrow \pi^+\pi^- K_S^0 K_L^0]$

- Find high energy photon and K_S from

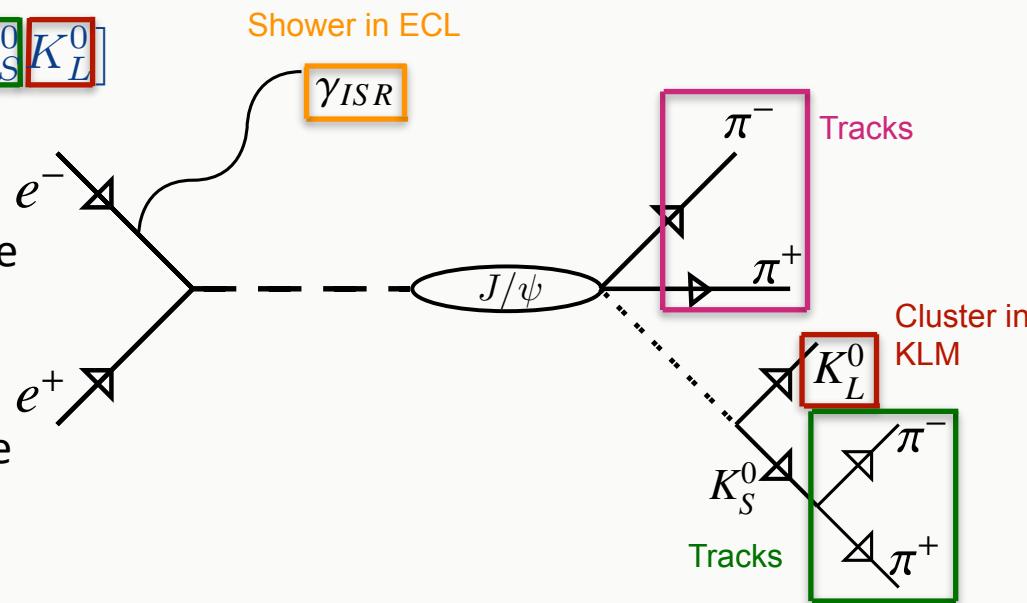
two pions, plus two additional pions

- Problem are the pions in the final state and the pions from the K_S

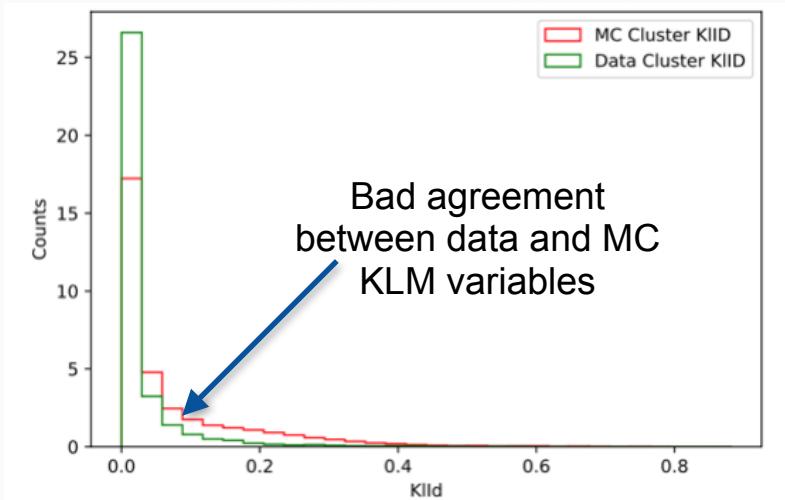
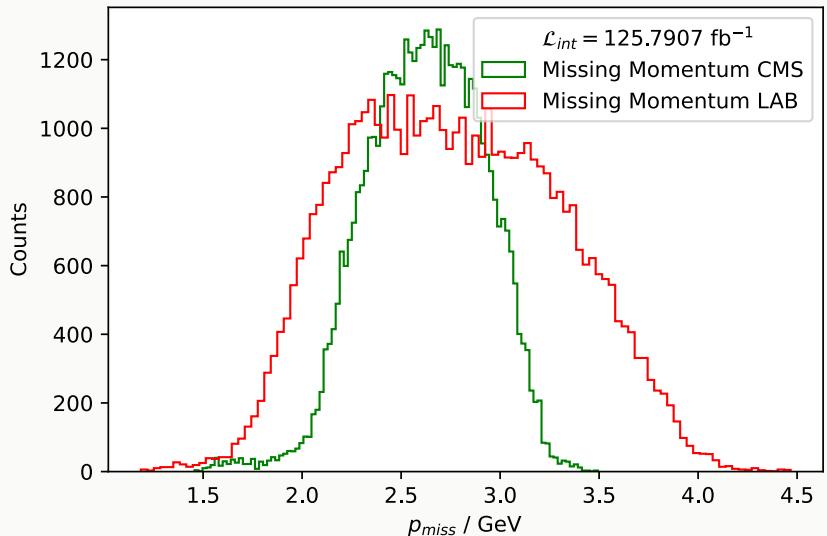
- Through different combinations multiple candidates per event possible

- Need a Best K_S Selection

- Use same procedure as in ϕ study



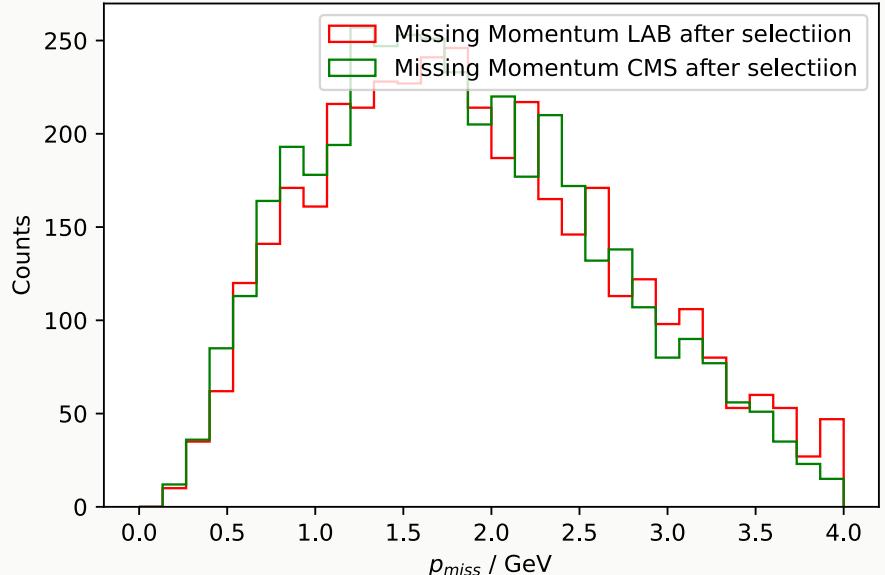
Backup: The momentum problem



- Studies of: $e^+e^- \rightarrow \gamma_{\text{ISR}} [J/\psi \rightarrow \pi^+\pi^- K_S^0 K_L^0]$ showed no evidence for low momentum candidates
- Idea: use MC to train on low momentum K_L candidates

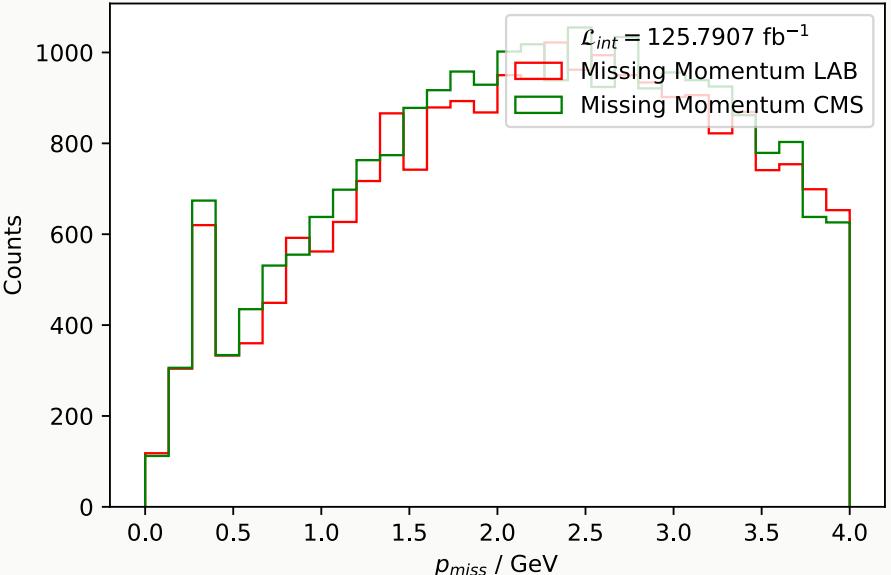
Backup: Missing Momentum in ISR J/ ψ Decay

Signal MC, Missing momentum after selections



Signal MC

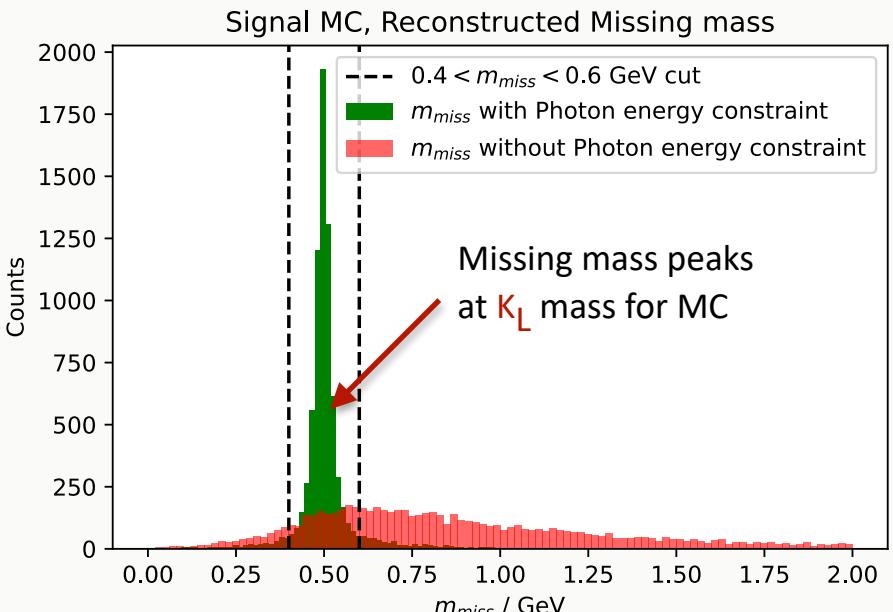
Data, Missing Momentum in LAB and CMS Frame



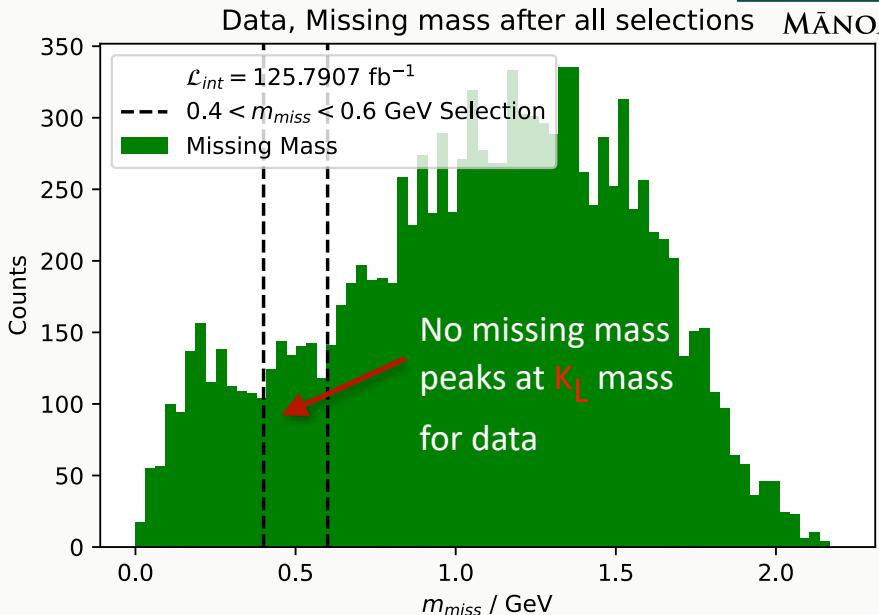
Data



Backup: Missing Mass with/without Photon Energy Constraint



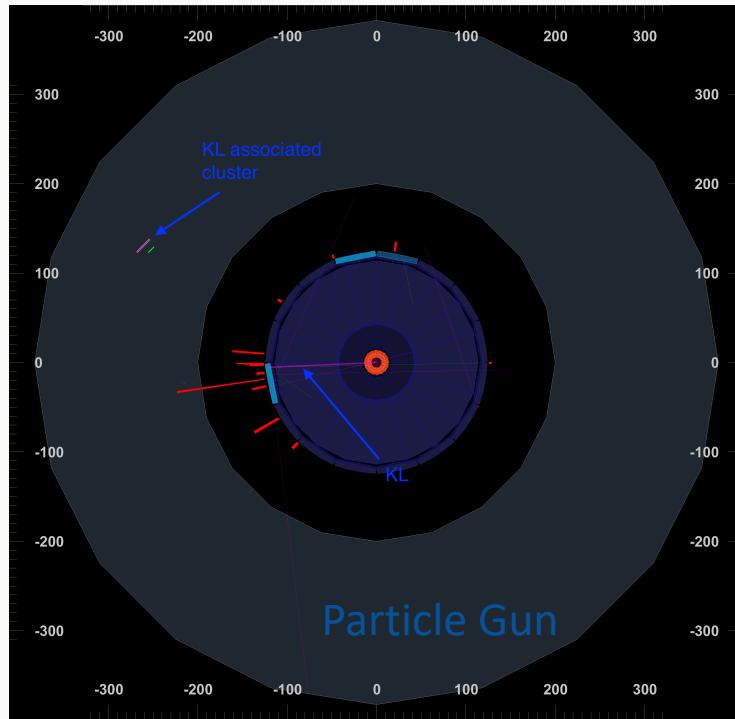
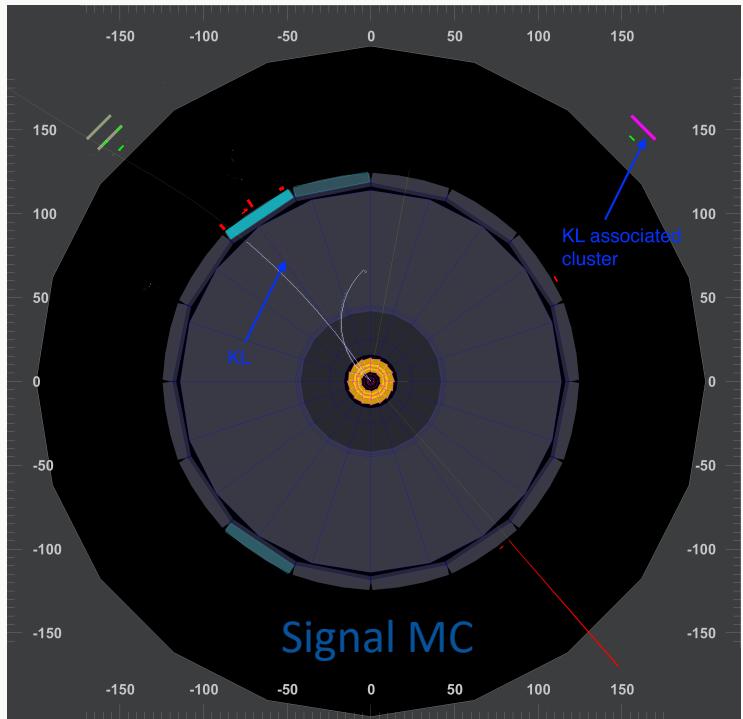
Signal MC



Data

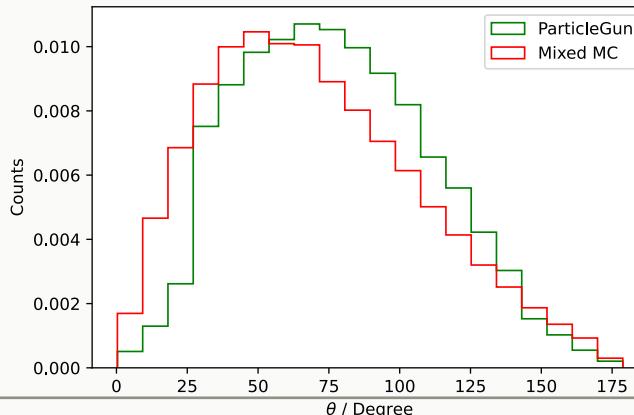
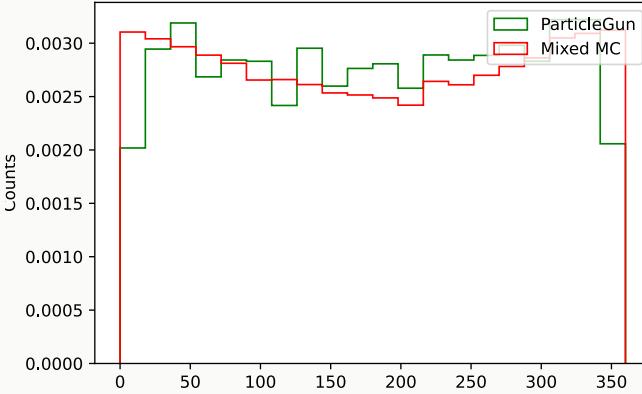
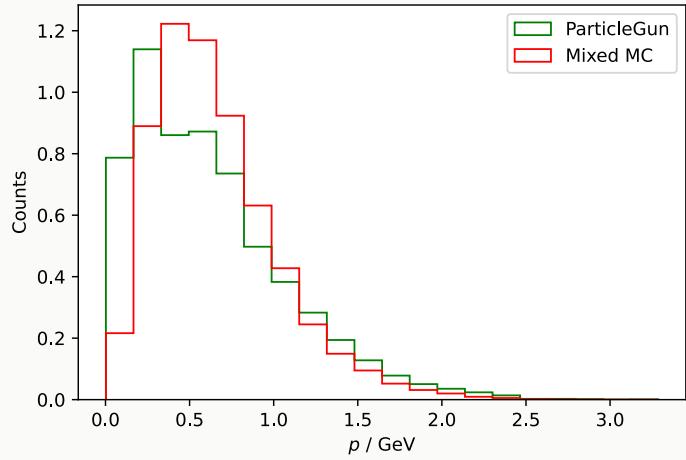
- No evidence for good K_L candidates due to massive background overlap in signal region

Backup: Width of $\cos(\alpha)$ for signal MC and a particle gun



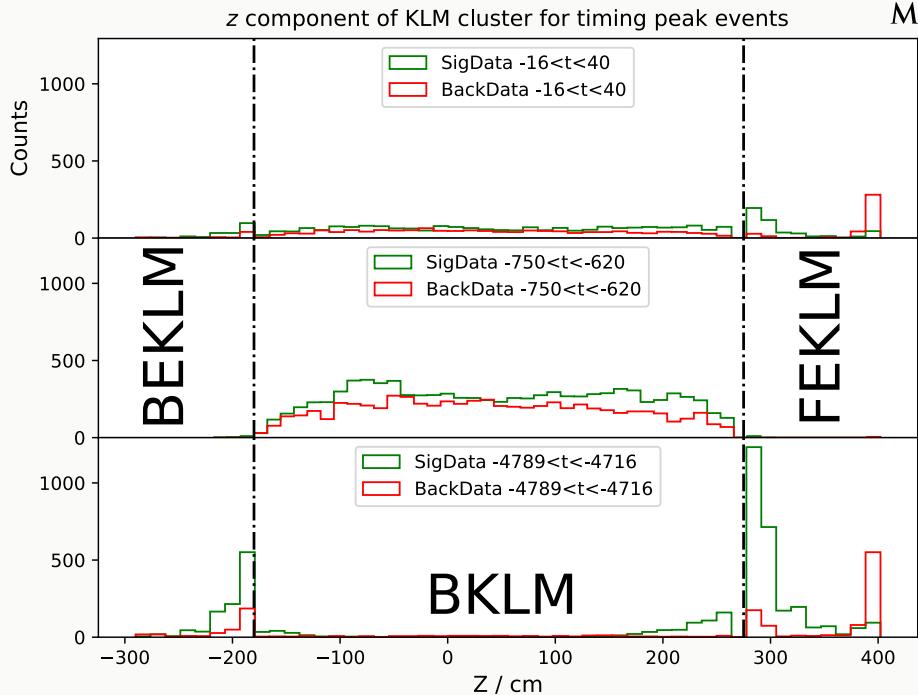
Backup: Training custom GEANT4 simulated signal against Data background events

- Model K_L momentum, phi and theta distribution based on MC generated K_L particles
- Differences due to assuming the variables are 1dim and not correlated



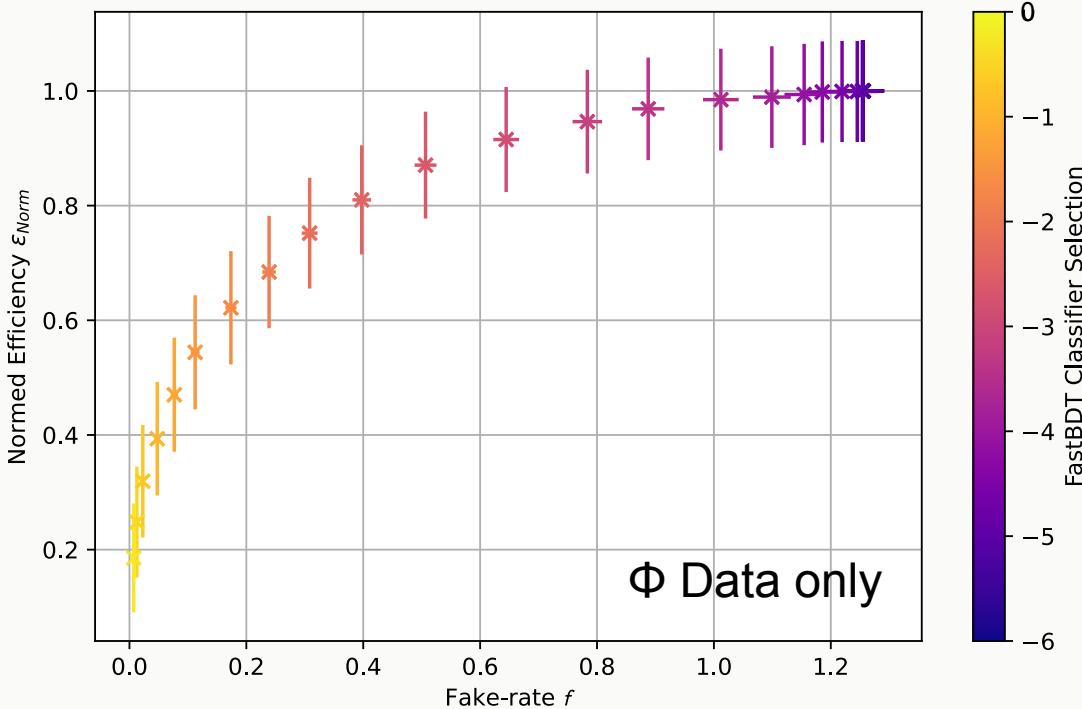
Backup: Selections for Combined Training

- Use Timing of KLM although no time calibration
- Neglect clusters in the back of the forward endcap
- Neglect events with matched tracks

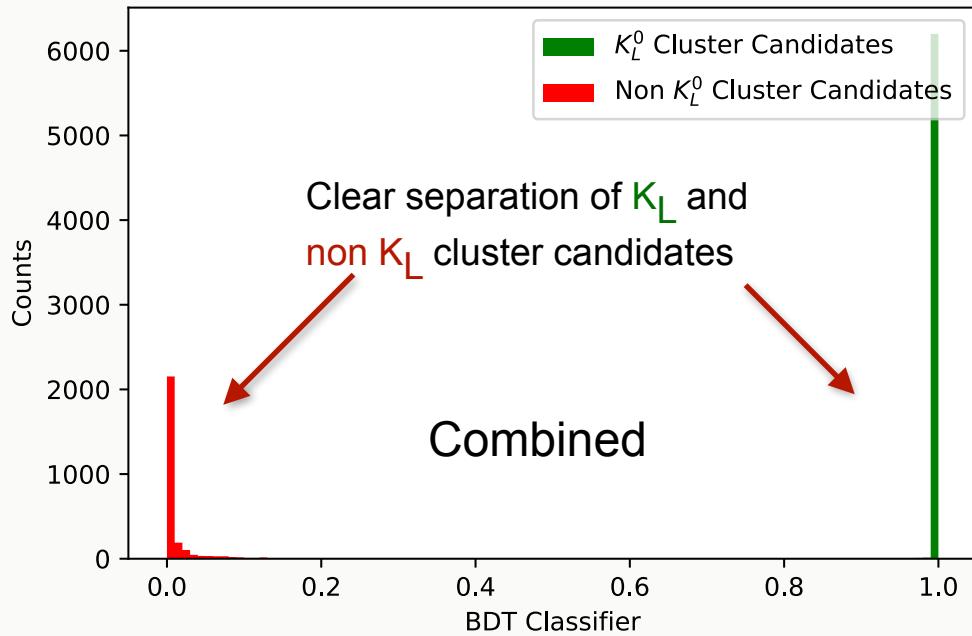


Backup: BDT Identification Efficiency and Fake-Rate

- We norm the efficiency in the data only sample by its initial value (without applying a cut)
- Achieve $\sim (68.4 \pm 9.8)\%$ identification efficiency of K_L and a fake-rate of 0.23 average fake K_L clusters per event
- Thus provided a tool to reduce the fake-rate of K_L clusters with a good efficiency (regarding the overall KLM efficiency)

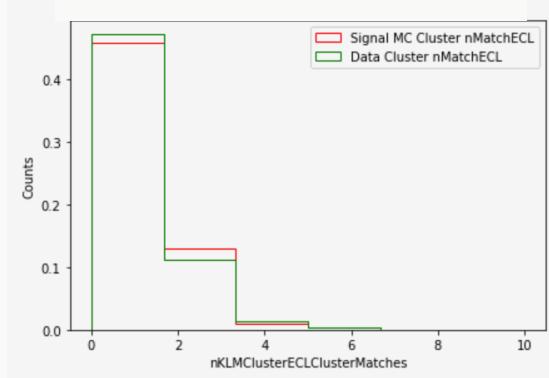
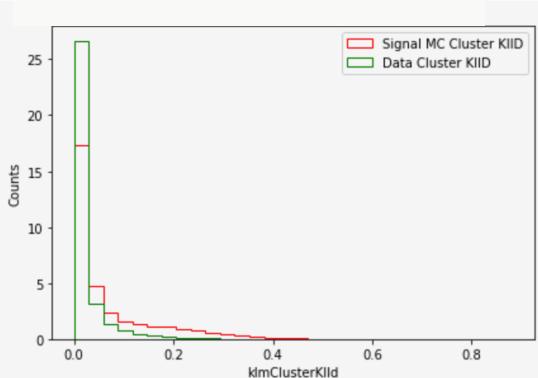
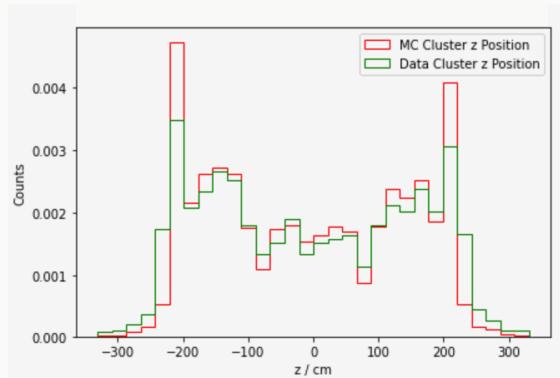
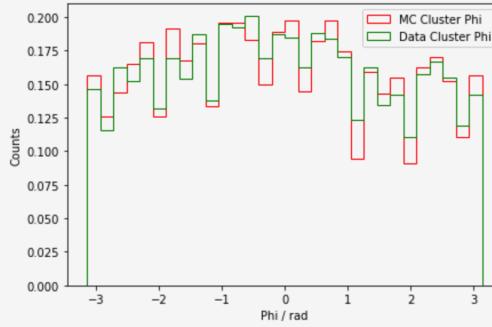
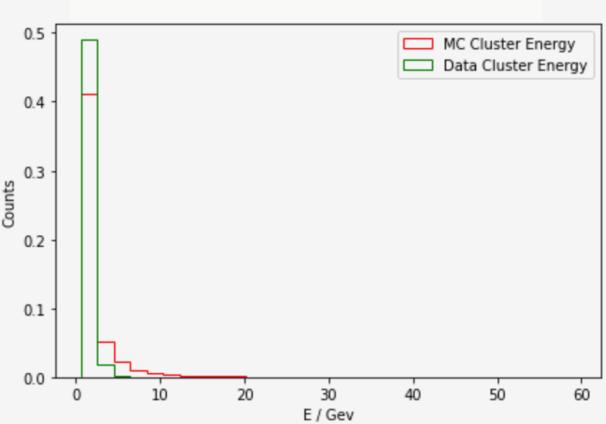
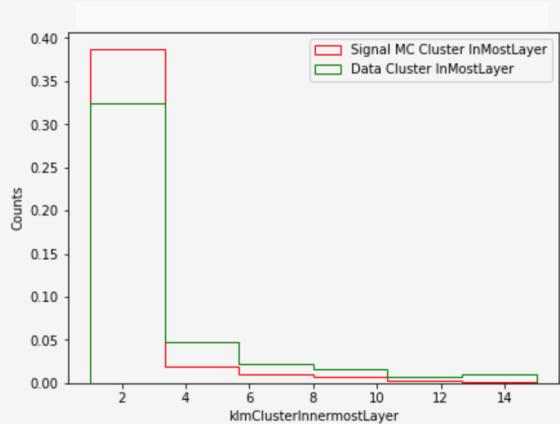


Backup: Start the BDT Training



- Apply FastBDT to combined sample of MC signal and data background
- BDT show good separation power in both cases

Backup: Data - MC agreement Phi study



Backup: Mass broadening

