

# The role of $|V_{cb}|$ : global UT fits & constraining $|DF|=2$ NP



VNIVERSITAT  
DE VALÈNCIA



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**Luiz VALE SILVA (IFIC, UV – CSIC)**

**[CKMfitter 2023 update: see CKM 2023 @ Santiago]**

**[Charles, Descotes-Genon, Ligeti, Monteil, Papucci, Trabelsi, LVS,  
PRD 102, 056023 (2020), arXiv:2006.04824]**

2023 Belle II Physics Week, 30/10/2023

# Flavor in the quark sector

(Gauge couplings to fermions)

$$\mathcal{L}_{SM(NP)} \sim -\frac{1}{4}(F_{\mu\nu})^2 + i\bar{\psi}\not{D}\psi$$

(Higgs self-interaction)

$$+ |D_\mu H|^2 - V(H)$$

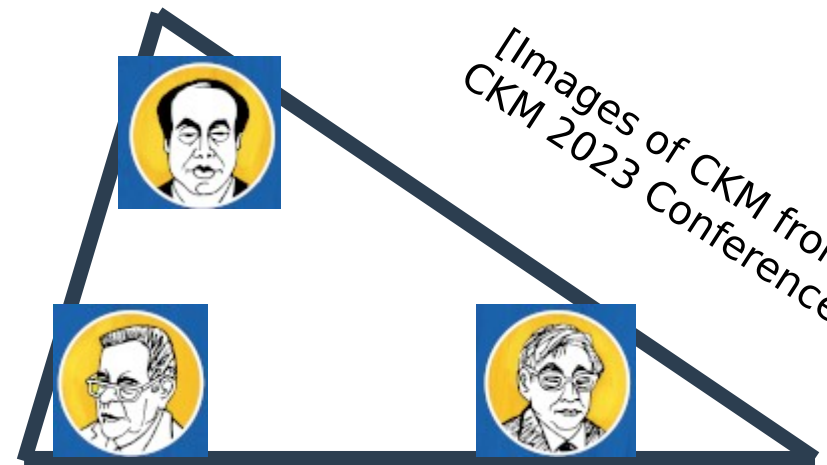
(short-range weak interactions)

$$+ YH\bar{\psi}\psi + \text{h.c.}$$

(spectrum of fermion masses, CKM matrix)

$$\left( + \sum_{d>4} \frac{1}{\Lambda_{heavy}^{d-4}} C_k O_k^d \right)$$

**Particle physics framework**



**Experimental data**

**Theoretical inputs**

- Flavor transitions pattern is likely to change in the presence of NP
- Goal is **testing the SM**, and **possibly point out tensions**
- Many flavour observables enjoy the status of **precision physics**, thanks to progress in **different fronts** (e.g. QCD inputs)

# The Cabibbo-Kobayashi-Maskawa matrix

15 JUNE 1963

UNITARY SYMMETRY AND LEPTONIC DECAYS

Nicola Cabibbo  
CERN, Geneva, Switzerland  
(Received 29 April 1963)

Universality of  $\Delta S=0,1$  weak transitions;  
Cabibbo introduces a  
phenomenological mixing angle

$$\begin{pmatrix} \cos \theta_1 & -\sin \theta_1 \cos \theta_3 & -\sin \theta_1 \sin \theta_3 \\ \sin \theta_1 \cos \theta_2 & \cos \theta_1 \cos \theta_2 \cos \theta_3 - \sin \theta_2 \sin \theta_3 e^{i\delta} & \cos \theta_1 \cos \theta_2 \sin \theta_3 + \sin \theta_2 \cos \theta_3 e^{i\delta} \\ \sin \theta_1 \sin \theta_2 & \cos \theta_1 \sin \theta_2 \cos \theta_3 + \cos \theta_2 \sin \theta_3 e^{i\delta} & \cos \theta_1 \sin \theta_2 \sin \theta_3 - \cos \theta_2 \sin \theta_3 e^{i\delta} \end{pmatrix} \quad \text{first } V_{cb}$$

No CPV with 2 generations;  
KM consider a 3<sup>rd</sup> one,  
1<sup>st</sup> CKM matrix in the literature

Progress of Theoretical Physics, Vol. 49, No. 2, February 1973

**CP-Violation in the Renormalizable Theory  
of Weak Interaction**

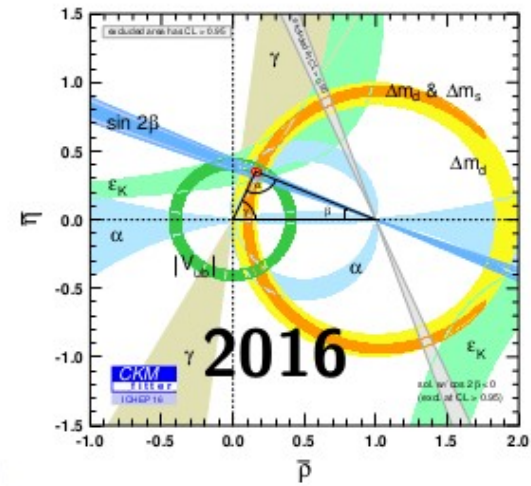
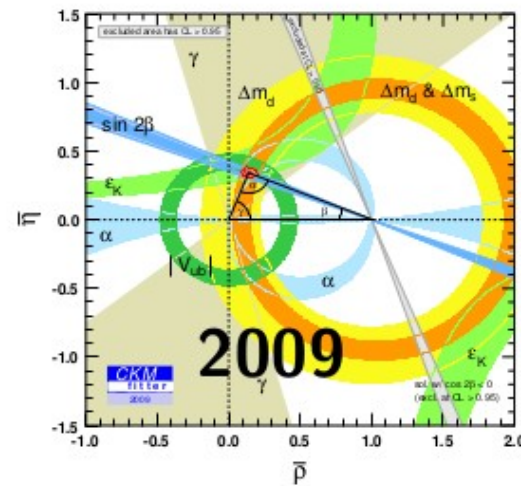
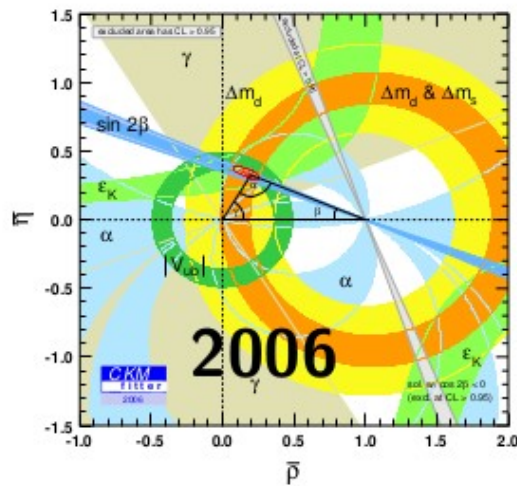
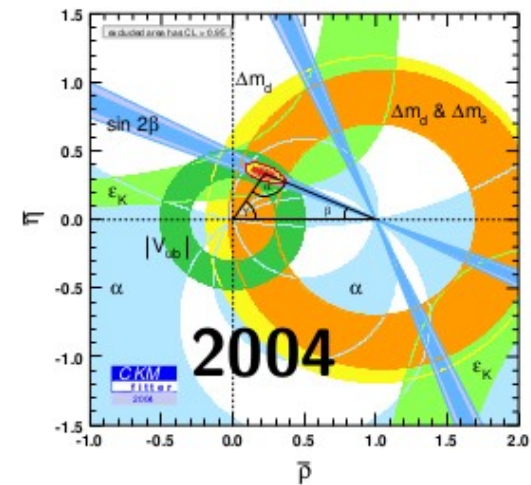
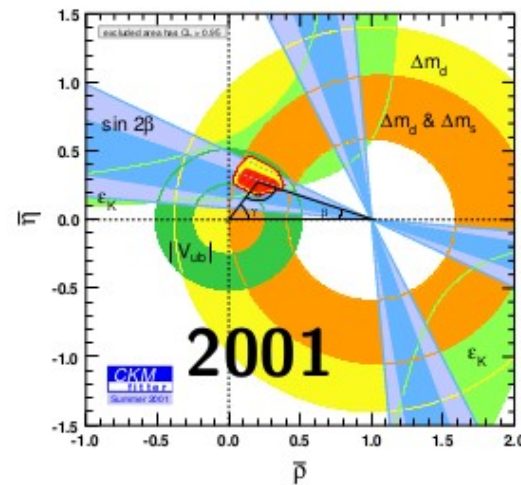
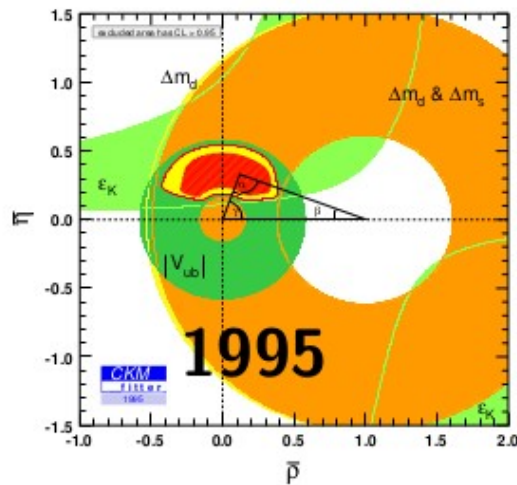
Makoto KOBAYASHI and Toshihide MASKAWA  
Department of Physics, Kyoto University, Kyoto

(Received September 1, 1972)

(13)

# Progress over the years

→ Long road for a better theoretical control (e.g., Lattice QCD), and more accurate data (LEP, KTeV, NA48, BaBar, Belle, CDF, DØ, LHCb, CMS, ...)



# Current status of flavour

- A **single** phase must be responsible for CP violation across distinct flavour sectors
- Observables of very different natures are available

$$A = 0.8215^{+0.0047}_{-0.0082} \text{ (0.8\% unc.)}$$

$$\lambda = 0.22498^{+0.00023}_{-0.00021} \text{ (0.1\% unc.)}$$

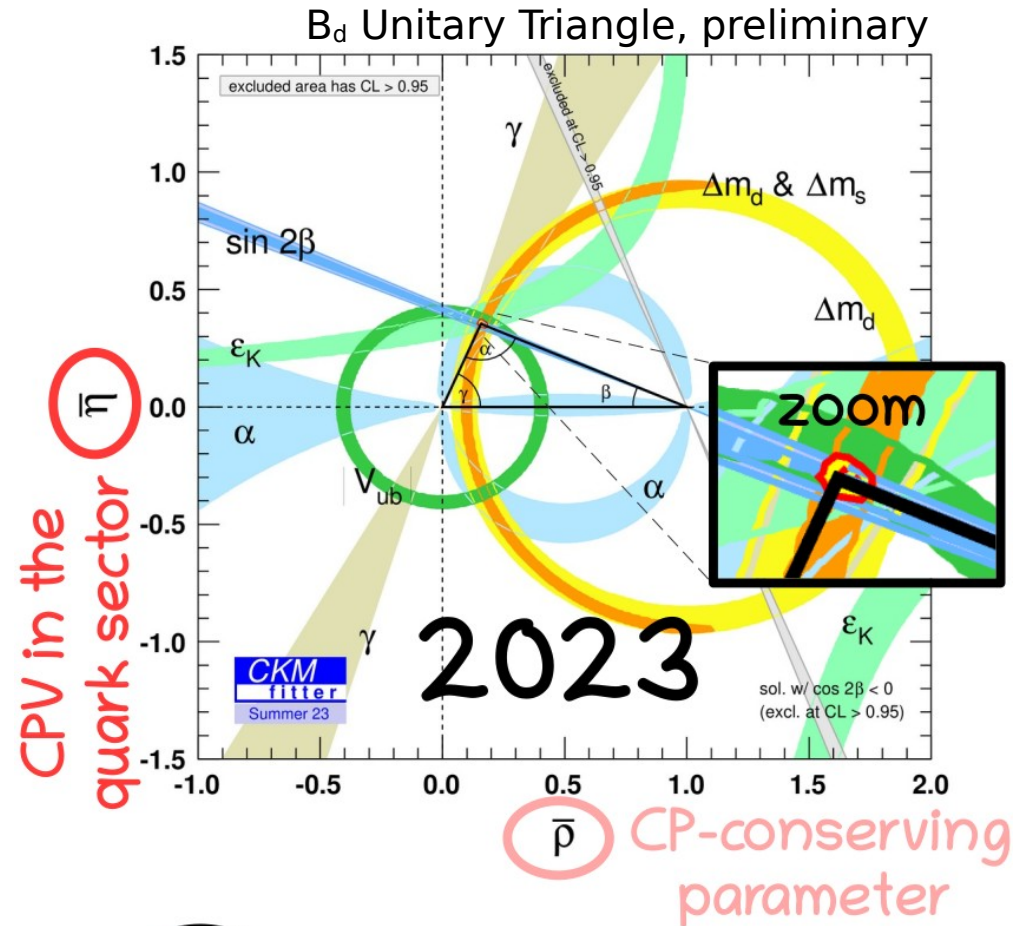
$$\bar{\rho} = 0.1562^{+0.0112}_{-0.0040} \text{ (4.9\% unc.)}$$

$$\bar{\eta} = 0.3551^{+0.0051}_{-0.0057} \text{ (1.5\% unc.)}$$

68% C.L. intervals

Rephasing invariant:

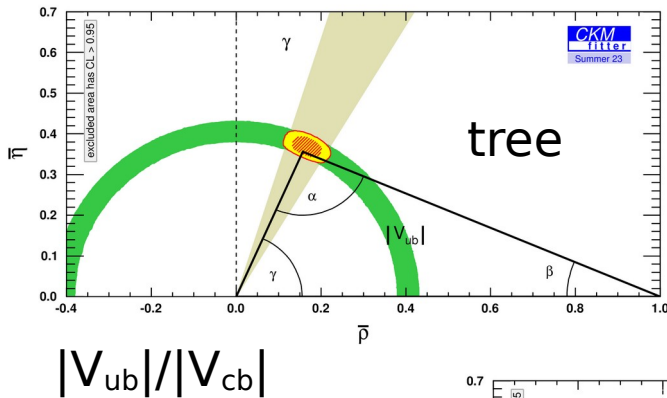
$$\frac{|V_{us}|}{(|V_{ud}|^2 + |V_{us}|^2)^{1/2}} = \lambda, \quad \frac{|V_{cb}|}{(|V_{ud}|^2 + |V_{us}|^2)^{1/2}} = A\lambda^2, \quad -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} = \bar{\rho} + i\bar{\eta}$$



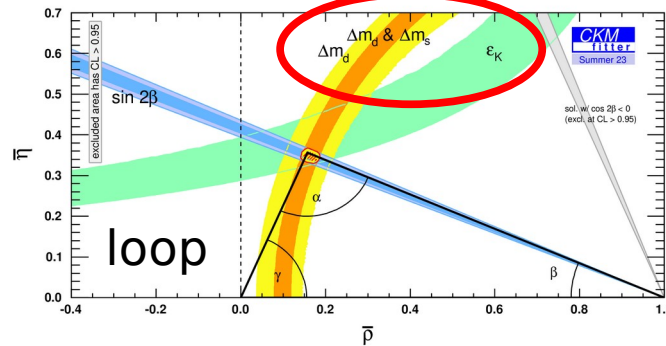
**b** :  $|V_{xb}|, \alpha, \beta, \gamma, \Delta m_d, \Delta m_s$

**s** :  $\epsilon_K$

# Consistency among observables



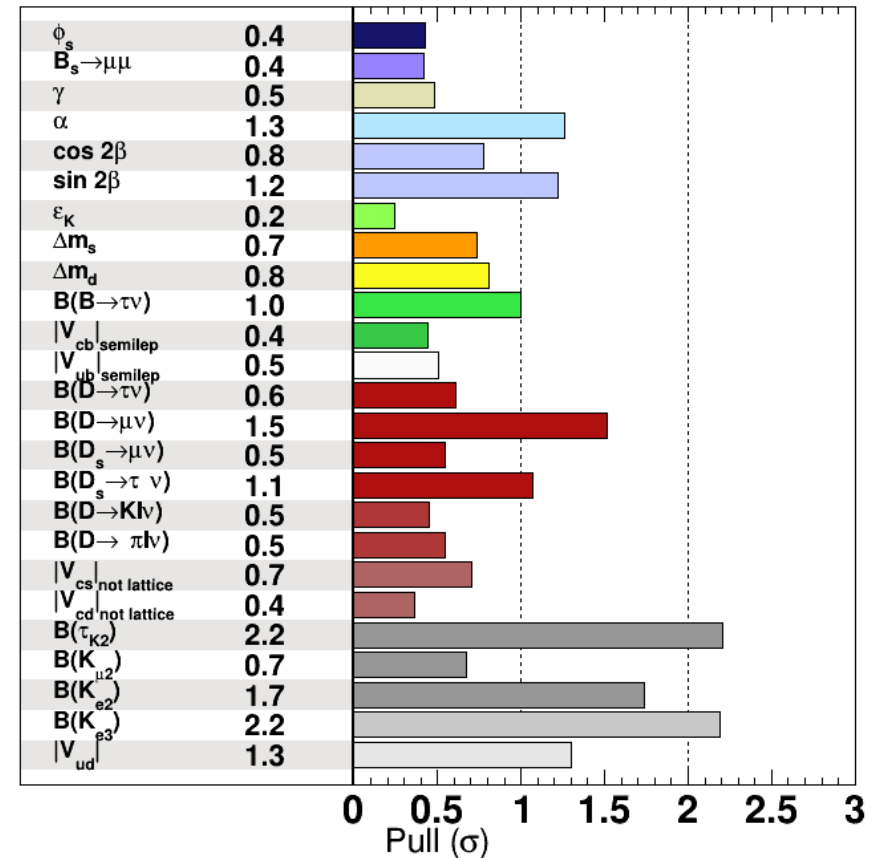
meson-mixing,  
with  $|V_{cb}|$



- Overall agreement w/ the SM, but some existing tensions (e.g., incl. vs excl.  $|V_{xb}|$ )

$$\text{pull}_{\mathcal{O}_{exp}} = \sqrt{\chi_{min}^2 - \chi_{min,! \mathcal{O}_{exp}}^2}$$

!  $\mathcal{O}_{exp}$ :  $\chi_{min}^2$  w/o  $\mathcal{O}_{exp}$



# $|V_{cb}|$ : excl. & incl. B-meson decays

→ Excl. and incl. have similar error budgets

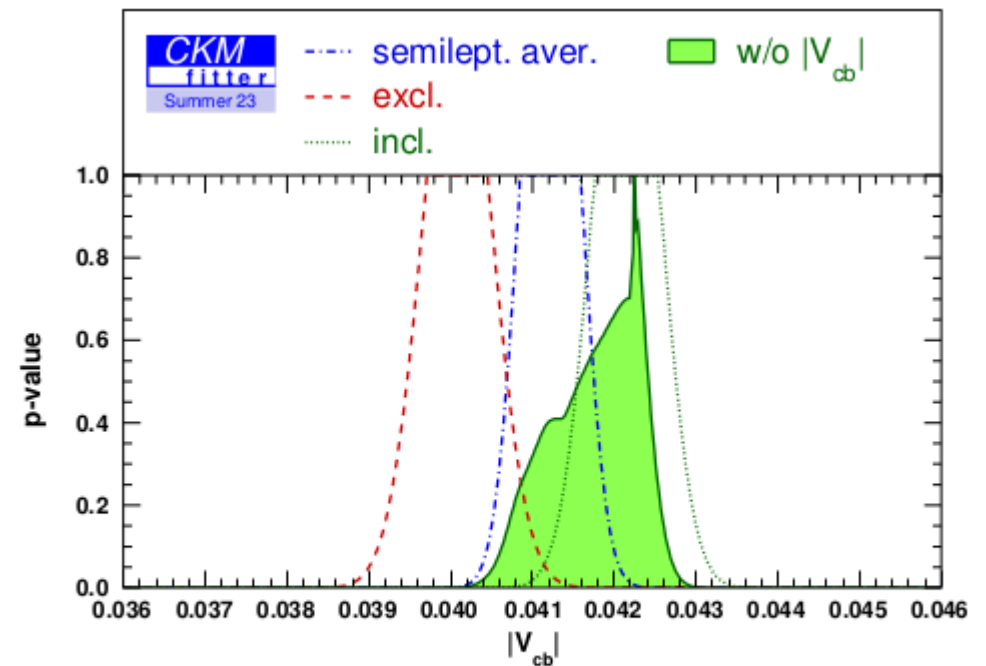
→ Our inputs for excl. and incl. differ by about  $2\sigma$

→ Similar averages:

$$'21, |V_{cb}|_{SL} = (41.15 \pm 0.34 \pm 0.45) \times 10^{-3}$$

$$'23, |V_{cb}|_{SL} = (41.22 \pm 0.24 \pm 0.37) \times 10^{-3}$$

(individual inputs given in back up; see discussion in “SL b-Hadron Decays” PDG 2023 review)

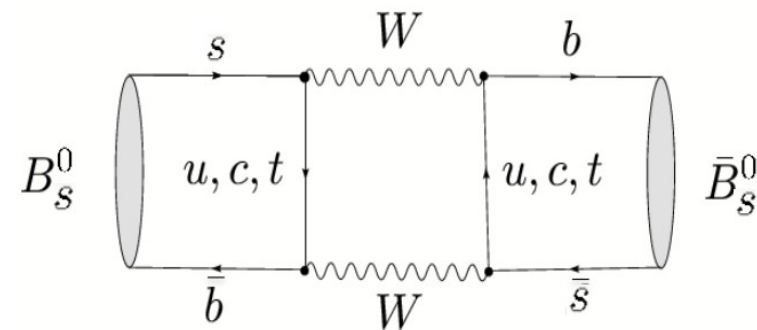


$$|V_{cb}|: \pm 1.7\% [\text{ind.}], \pm 0.9\% [\text{comb.}]$$

# NP in B meson mixing

- Address present and future bounds on NP in  $|\Delta B|=2$ , and discuss future limitations

- $|\Delta B|=2$ : NP competes with  **suppressions in the SM (GIM/CKM)**, and enjoys the status of  **precision physics**



$$V_{tb} V_{ts}^* \sim -V_{cb}$$

- Not discussing D meson mixing

[K meson mixing: PRD 89, 033016 (2014), [arxiv:1309.2293](#)]

- **Combine projections for future data**: need global fit including “tree” and “loop” observables

[see e.g. [CKMfitter](#)]



# NP in B meson mixing

- **NP in  $|\Delta B|=2$ :**

**$h_d$  and  $h_s$  set sizes**

- **Assumptions:**

- No NP in  $|\Delta F|=1$ :

tree level in SM ( $\gamma$ ,  $|V_{ub}|$ ,  $|V_{cb}|$ , ...) free of NP

- NP is short-distance

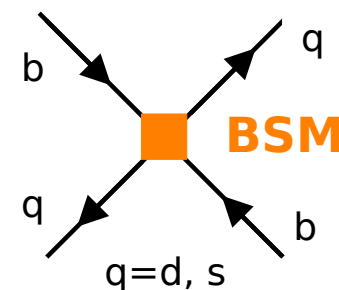
- Unitarity of the CKM 3x3 matrix

- Unrelated NP in  $B_d$  and  $B_s$  systems

CKM (in presence of NP),  
bag parameters,  
↓ decay constants

$$M_{12} = M_{12}^{\text{SM}} \times (1 + h e^{2i\sigma})$$

NP parameters



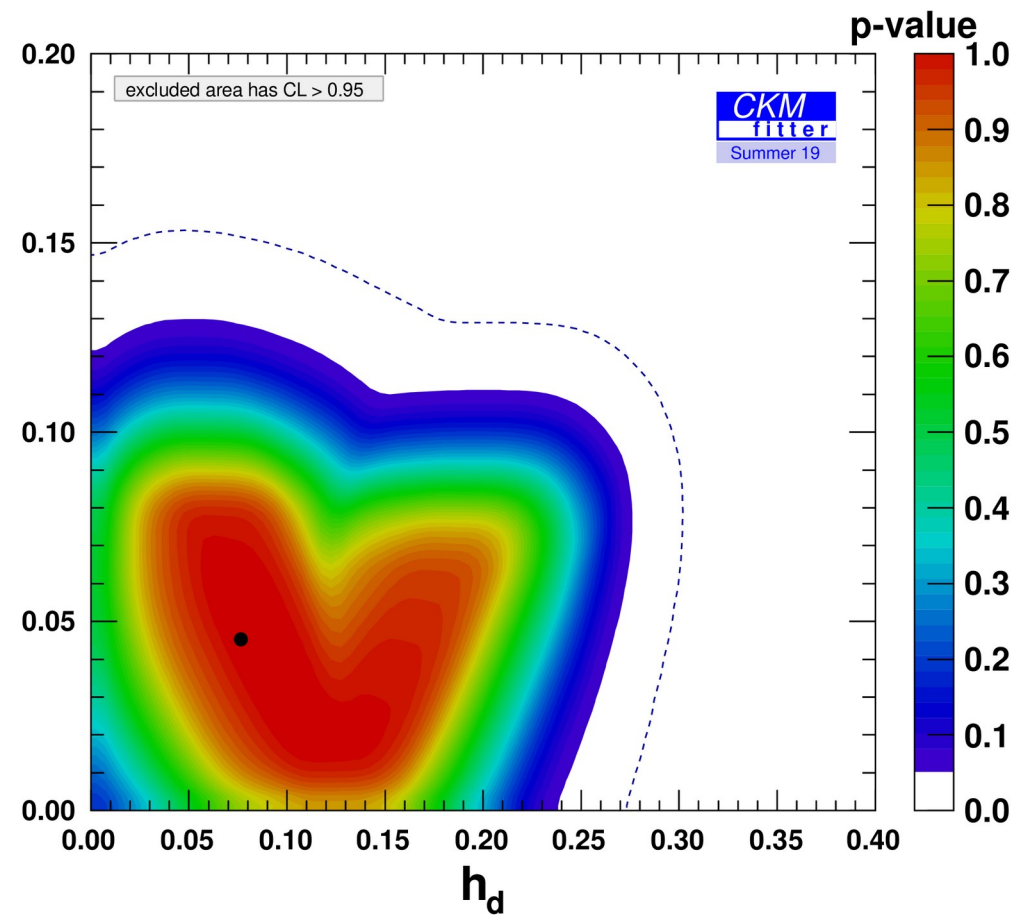
[See: PRD 89, 033016 (2014),  
[arxiv:1309.2293](https://arxiv.org/abs/1309.2293)]

- SMEFT: **four-quark operators** of different chiral structures

# Present status of NP in B meson mixing

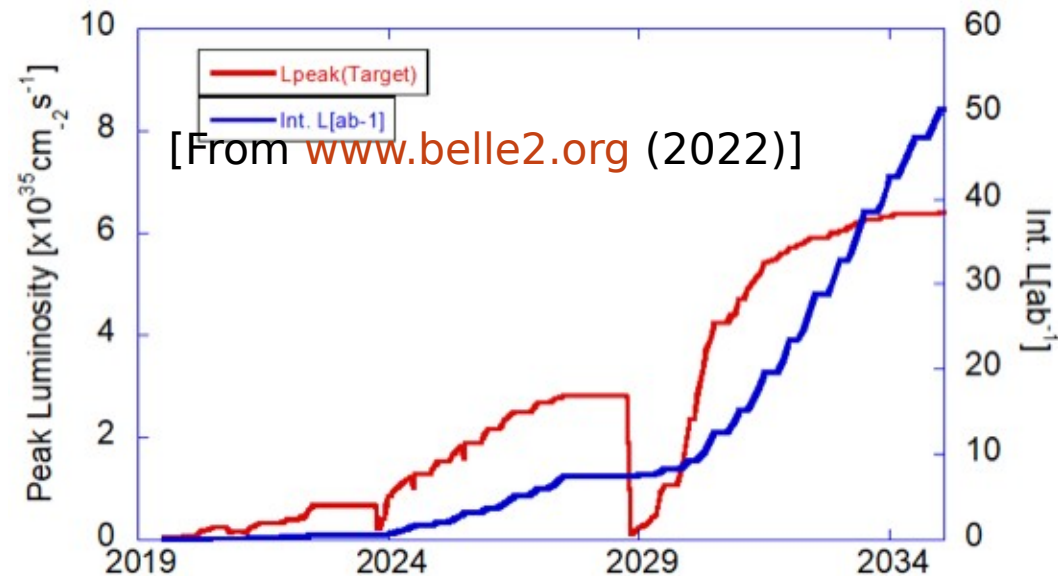
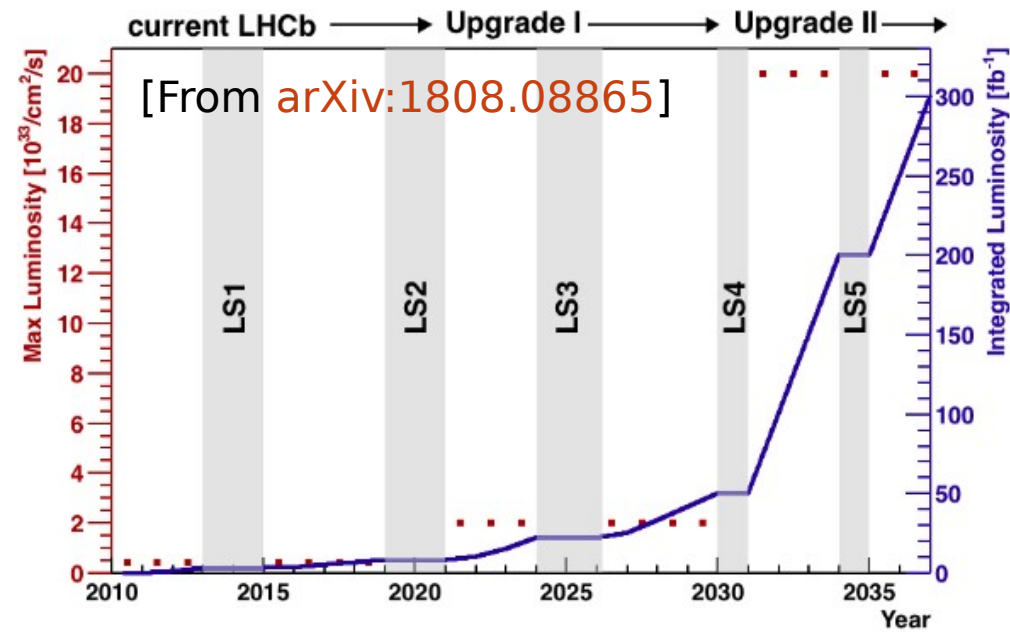
- **Agreement with the SM ( $h_d=h_s=0$ ) at  $\sim 1\sigma$**
- **Allowed size for NP at the level of  $O(20\%)!$**
- **Extractions of  $\rho$  and  $\eta$**  (Wolfenstein parm.) degrade by factor  $\sim 3$

Status as of Summer '19



**Black dot:** best fit point;  
 $\sigma_d$  and  $\sigma_s$  are unconstrained

# New era of flavour ahead



## Benchmarks for the future:

- **Phase I: LHCb-upgrade I** 50/fb, & **Belle II** 50/ab
- **Phase II: LHCb-upgrade II** 300/fb, & **Belle II upgrade** 250/ab

# Experimental and theoretical inputs

[For projections, see e.g. [Belle II Physics Book](#), 1808.10567]

[Full list of projections given in back up]

- $|V_{ub}|_{SL}$  &  $|V_{cb}|_{SL}$ : respectively 0.9% & 1.0% @ Phase II (Belle II U.)

[incl. vs excl. inputs and impact on extraction of NP in  $|\Delta F|=2$ :  
[De Bruyn, Fleischer, Malami, van Vliet](#)]

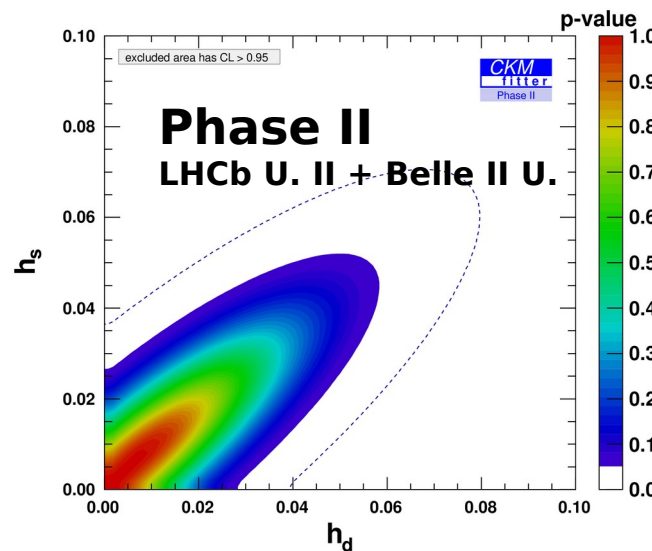
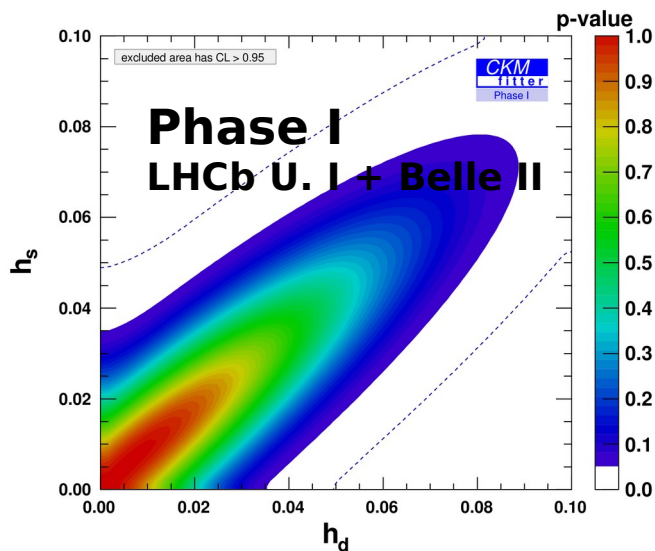
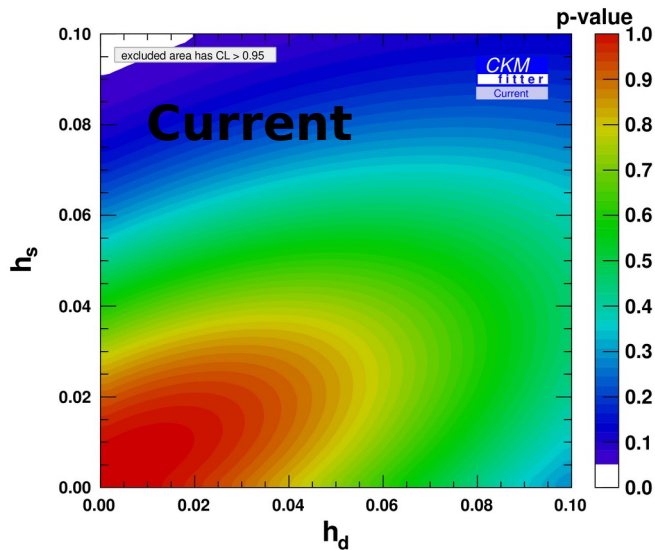
- Phases I and II uncs. for **Lattice QCD** (decay constants, bag parameters) < 1%

Literature discusses Lattice QCD projections up to Phase II (QED effects included)

# Future improvements

- SM reference: shift the central values
- Compared to Current, **improvement by factor >3 (5) at Phase I (II)**

Sensitivities	Summer 2019	Phase I	Phase II
$h_d$	0.26	0.073	0.049
$h_s$	0.12	0.065	0.044

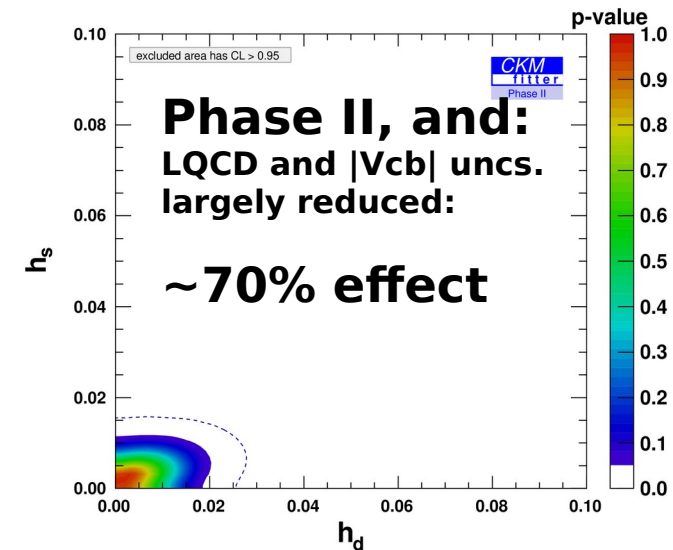
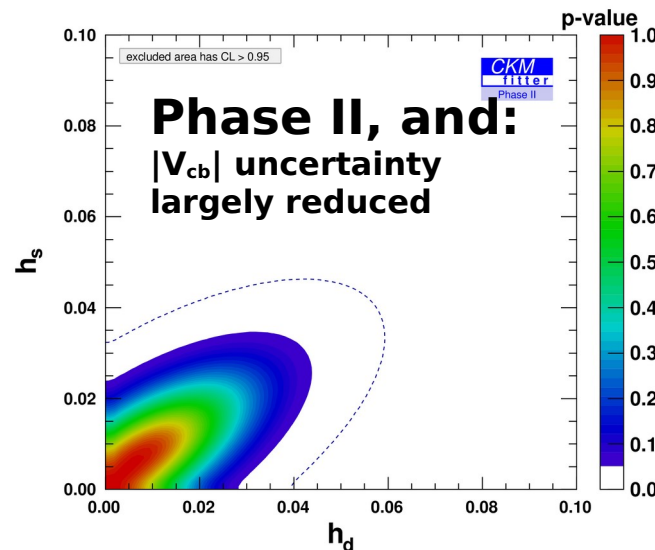
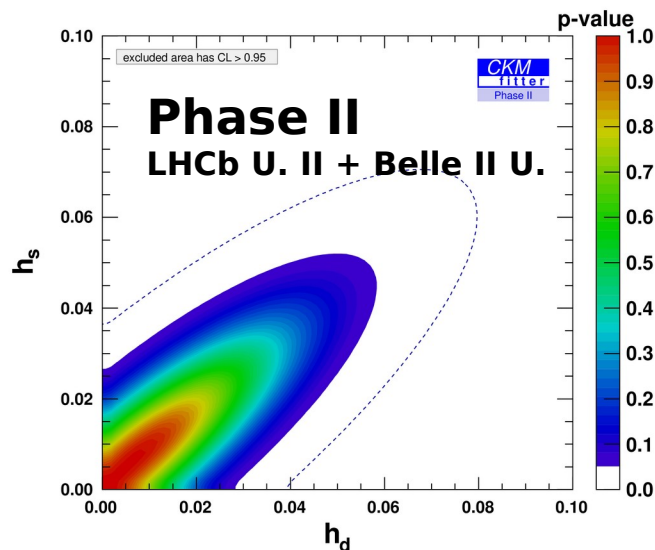


# Bottlenecks

**Necessary improvements** beyond current expectations **for enhancing sensitivity to NP**:

[SD: Brod, Gorbahn, Stamou et al., in progress]

- **Lattice QCD** (also short-distance QCD corrections)
- $|V_{cb}|$ , overall normalization (Wolfenstein parameter A)
- **Individual impacts on  $h_d$  and  $h_s$** : improvements by O(20-30)%



# Future reach to NP in B meson mixing

$$\frac{C_{ij}^2}{\Lambda^2} (\bar{q}_{i,L} \gamma_\mu q_{j,L})^2, \quad \longrightarrow \quad h \simeq 1.5 \frac{|C_{ij}|^2 (4\pi)^2}{|\lambda_{ij}^t|^2 G_F \Lambda^2} \simeq \frac{|C_{ij}|^2}{|\lambda_{ij}^t|^2} \left( \frac{4.5 \text{ TeV}}{\Lambda} \right)^2,$$

$$\sigma = \arg(C_{ij} \lambda_{ij}^{t*}),$$

- In the absence of suppressions: **NP scale >> TeV**
- Possible flavour and loop suppressions: **alleviate bounds on NP**

Couplings	NP loop order	Sensitivity for Summer 2019 [TeV]		Phase I Sensitivity [TeV]		Phase II Sensitivity [TeV]	
		$B_d$ mixing	$B_s$ mixing	$B_d$ mixing	$B_s$ mixing	$B_d$ mixing	$B_s$ mixing
$ C_{ij}  =  V_{ti} V_{tj}^* $ (CKM-like)	Tree level	9	13	17	18	20	21
	One loop	0.7	1.0	1.3	1.4	1.6	1.7
$ C_{ij}  = 1$ (No hierarchy)	Tree level	$1 \times 10^3$	$3 \times 10^2$	$2 \times 10^3$	$4 \times 10^2$	$2 \times 10^3$	$5 \times 10^2$
	One loop	80	20	$2 \times 10^2$	30	$2 \times 10^2$	40

# Conclusions

- Flavour physics: crucial in **shaping the SM**, but also in looking for **candidates of NP**
- **$V_{cb}$ : tests of CKM unitarity**
- **$|\Delta B|=2$ : only one flavour aspect** of future experimental and theoretical progress
- Allowed NP in B meson mixing **still large**: bounds will largely improve
- Identified future limitations in Phase II:  
**LQCD and  $|V_{cb}|$  → bounds on NP at 1-2% of SM**

**THANKS!**



# CKMfitter Collaboration

## MORE DETAILS @ [CKMfitter](#)

Jérôme Charles, Theory  
Olivier Deschamps, LHCb  
Sébastien Descotes-Genon, Theory  
Stéphane Monteil, LHCb  
Jean Orloff, Theory  
Wenbin Qian, LHCb/BESIII  
Vincent Tisserand, LHCb/BABAR  
Karim Trabelsi, Belle/Belle II  
Philip Urquijo, Belle/Belle II  
Luiz Vale Silva, Theory

The screenshot shows the CKMfitter website homepage. The header features the 'CKMfitter' logo and a navigation menu with links to Home, Plots & Results, Specific Studies, Talks & Writeups, Publications, and CKMfitter Group. The main content area is titled 'The CKMfitter group provides:' and lists three main areas: Plots & Results, Talks, and Tools. Each area has a corresponding colored box with a brief description and a link to more information.

**CKMfitter**

Home  
Plots & Results  
Specific Studies  
Talks & Writeups  
Publications  
CKMfitter Group  
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The CKMfitter group provides:

- A global analysis of measurements determining the CKM matrix parameters in the framework of the Standard Model and some of its extensions.
- Graphical and numerical constraints on CKM matrix elements, predictions on rare K and B meson decays, theoretical parameters, etc.
- The statistical treatment is based on Frequentist statistics and **Rfit** (Range fit) for the theoretical uncertainties.

**Plots & Results**  
Preliminary results as of Moriond 2021  
(updated Jan 2022)

**Talks**  
Workshop on High Energy Physics Phenomenology (WHEPP) XVI  
Dec 1-10, Guwahati, India  
"Beyond 1st and 3rd generation unitarity triangle: what can we learn from the others?" [\(pdf\)](#)

**Tools**  
Perform your own flavour analyses online  
with **CKMlive**

**Specific Studies**  
Prospective studies for  
Opportunities in Flavour Physics at the HL-LHC and HE-LHC

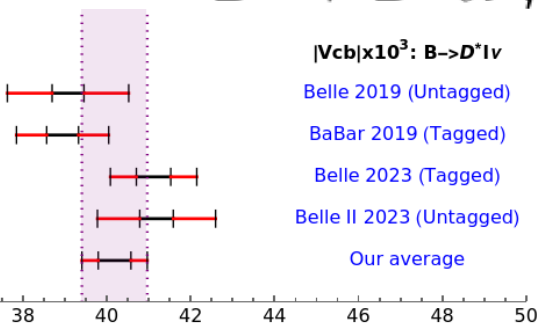
**BACK UP!**

# CKMfitter 2023 inputs for $|V_{cb}|$

→ Exclusive  $|V_{cb}|$ :

[Belle II untagged: 2310.01170]

●  $B \rightarrow D^* \ell \nu$ , BGL:  $|V_{cb}|_{B \rightarrow D^*} = (40.17 \pm 0.39 \pm 0.39) \times 10^{-3}$

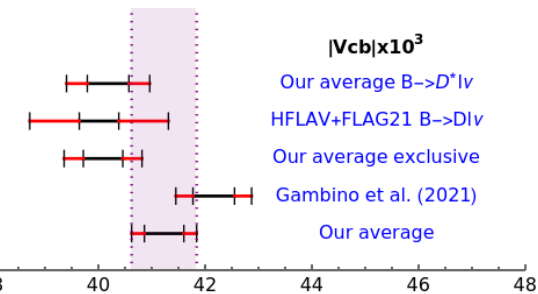


[Belle '19 (untagged), BaBar '19 (untagged); preliminary Belle (tagged) & Belle II (untagged)]

[preliminary combination of lattice inputs]

[See M. Prim & R. Cheaib @ EPS-HEP; C. Schwanda on Tue @ 17h15]

●  $B \rightarrow D \ell \nu$ , BCL:  $|V_{cb}|_{B \rightarrow D} = (40.00 \pm 0.93 \pm 0.37) \times 10^{-3}$

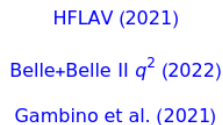


[HFLAV+FLAG 2021 combination]

$|V_{cb}|_{excl.} = (40.08 \pm 0.36 \pm 0.37) \times 10^{-3}$

→ Inclusive:  $|V_{cb}|_{incl.} = (42.16 \pm 0.32 \pm 0.39) \times 10^{-3} (m_b^{kin})$

$|V_{cb}| \times 10^3: B \rightarrow X \ell \nu$



[Fael, Schönwald, Steinhauser '20 '20 '20; Bordone, Capdevila, Gambino '21]

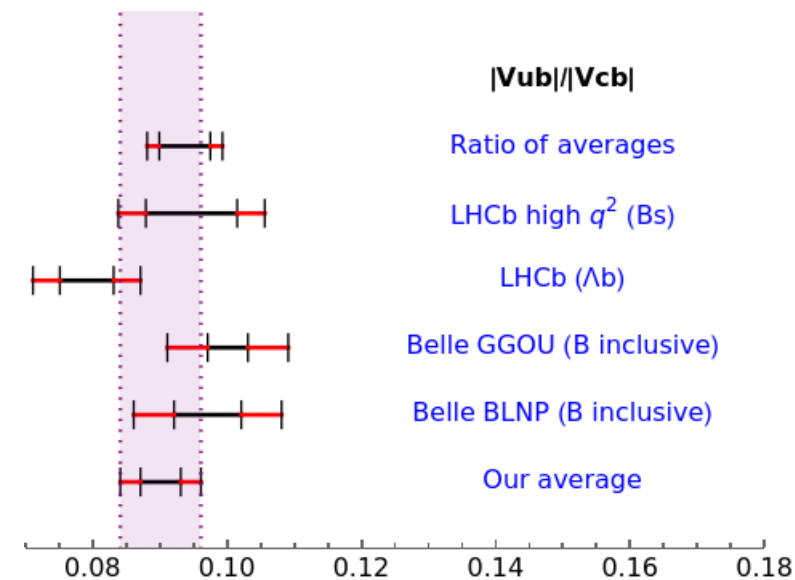
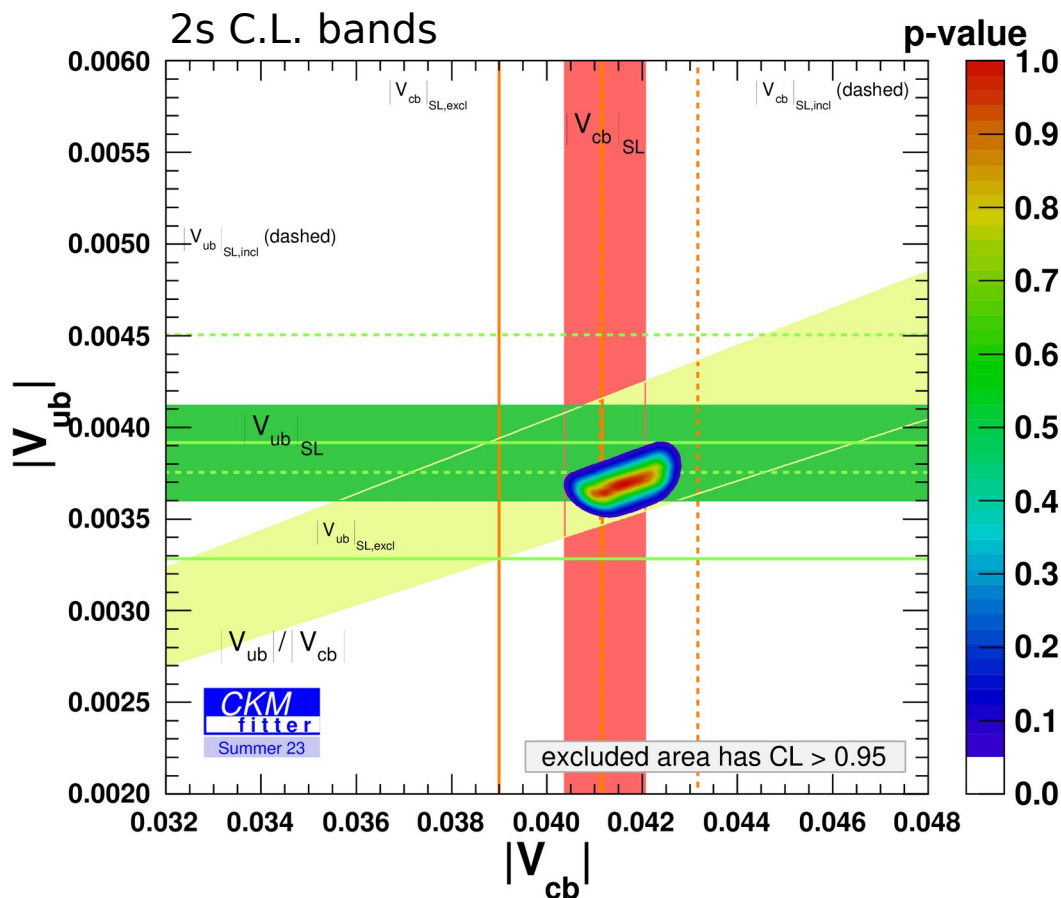
# $|V_{ub}|$ and $|V_{cb}|$ plane

→  $|V_{ub}|/|V_{cb}|_{incl} = 0.100 \pm 0.006 \pm 0.003$  (GGOU)

[preliminary Belle '23 (tagged)]

[See L. Cao @ EPS-HEP; M. Prim on Tue @ 13h00]

→  $|V_{cb}|_{incl.}$  and  $|V_{ub}|_{excl.}$  are preferred by their indirect extractions



# Experimental quantities vs. theoretical ones

Observables considered in the fit that are modified by NP in  $|\Delta B|=2$ :

$$\Delta_q = |\Delta_q| e^{i2\Phi_q^{\text{NP}}}$$

parameter	prediction in the presence of NP
$\Delta m_q$	$ \Delta_q^{\text{NP}}  \times \Delta m_q^{\text{SM}}$
$2\beta$	$2\beta^{\text{SM}} + \Phi_d^{\text{NP}}$
$2\beta_s$	$2\beta_s^{\text{SM}} - \Phi_s^{\text{NP}}$
$2\alpha$	$2(\pi - \beta^{\text{SM}} - \gamma) - \Phi_d^{\text{NP}}$
$\Phi_{12,q} = \text{Arg}\left[-\frac{M_{12,q}}{\Gamma_{12,q}}\right]$	$\Phi_{12,q}^{\text{SM}} + \Phi_q^{\text{NP}}$
$A_{SL}^q$	$\frac{\Gamma_{12,q}}{M_{12,q}^{\text{SM}}} \times \frac{\sin(\Phi_{12,q}^{\text{SM}} + \Phi_q^{\text{NP}})}{ \Delta_q^{\text{NP}} }$
$\Delta\Gamma_q$	$2 \Gamma_{12,q}  \times \cos(\Phi_{12,q}^{\text{SM}} + \Phi_q^{\text{NP}})$

# Experimental and theoretical inputs

	Central values	Uncertainties				Reference Phases I–III
		Current [28]	Phase I	Phase II	Phase III	
$ V_{ud} $	0.97437	$\pm 0.00021$	id	id	id	[28]
$ V_{us}  f_+^{K \rightarrow \pi}(0)$	0.2177	$\pm 0.0004$	id	id	id	[28]
$ V_{cd} $	0.2248	$\pm 0.0043$	$\pm 0.003$	id	id	[40,41]
$ V_{cs} $	0.9735	$\pm 0.0094$	id	id	id	[28,40,41]
$\Delta m_d$ [ps <sup>-1</sup> ]	0.5065	$\pm 0.0019$	id	id	id	[17]
$\Delta m_s$ [ps <sup>-1</sup> ]	17.757	$\pm 0.021$	id	id	id	[17]
$ V_{cb} _{\text{SL}} \times 10^3$	42.26	$\pm 0.58$	$\pm 0.60$	$\pm 0.44$	id	[29]
$ V_{cb} _{W \rightarrow cb} \times 10^3$	...	...	...	...	$\pm 0.17$	[34–36]
$ V_{ub} _{\text{SL}} \times 10^3$	3.56	$\pm 0.22$	$\pm 0.042$	$\pm 0.032$	id	[29]
$ V_{ub} / V_{cb} $ (from $\Lambda_b$ )	0.0842	$\pm 0.0050$	$\pm 0.0025$	$\pm 0.0008$	id	[30]
$\mathcal{B}(B \rightarrow \tau \nu) \times 10^4$	0.83	$\pm 0.24$	$\pm 0.04$	$\pm 0.02$	$\pm 0.009$	[29,34]
$\mathcal{B}(B \rightarrow \mu \nu) \times 10^6$	0.37	...	$\pm 0.03$	$\pm 0.02$	id	[29]
$\sin 2\beta$	0.680	$\pm 0.017$	$\pm 0.005$	$\pm 0.002$	$\pm 0.0008$	[29,30,34]
$\alpha$ [°] (mod 180°)	91.9	$\pm 4.4$	$\pm 0.6$	id	id	[29]
$\gamma$ [°] (mod 180°)	66.7	$\pm 5.6$	$\pm 1$	$\pm 0.25$	$\pm 0.20$	[29,30,34]
$\beta_s$ [rad]	-0.035	$\pm 0.021$	$\pm 0.014$	$\pm 0.004$	$\pm 0.002$	[30,34]
$A_{\text{SL}}^d \times 10^4$	-6	$\pm 19$	$\pm 5$	$\pm 2$	$\pm 0.25$	[14,17,34,37]
$A_{\text{SL}}^s \times 10^5$	3	$\pm 300$	$\pm 70$	$\pm 30$	$\pm 2.5$	[14,17,34,37]
$\bar{m}_t$ [GeV]	165.30	$\pm 0.32$	id	id	$\pm 0.020$	[28,34]
$\alpha_s(m_Z)$	0.1185	$\pm 0.0011$	id	id	$\pm 0.00003$	[28,34]
$f_+^{K \rightarrow \pi}(0)$	0.9681	$\pm 0.0026$	$\pm 0.0012$	id	id	[30]
$f_K$ [GeV]	0.1552	$\pm 0.0006$	$\pm 0.0005$	id	id	[30]
$f_{B_s}$ [GeV]	0.2315	$\pm 0.0020$	$\pm 0.0011$	id	id	[30]
$B_{B_s}$	1.219	$\pm 0.034$	$\pm 0.010$	$\pm 0.007$	id	[30]
$f_{B_s}/f_{B_d}$	1.204	$\pm 0.007$	$\pm 0.005$	id	id	[30]
$B_{B_s}/B_{B_d}$	1.054	$\pm 0.019$	$\pm 0.005$	$\pm 0.003$	id	[30]
$\tilde{B}_{B_s}/\tilde{B}_{B_d}$	1.02	$\pm 0.05$	$\pm 0.013$	id	id	[30,42,43]
$\tilde{B}_{B_s}$	0.98	$\pm 0.12$	$\pm 0.035$	id	id	[30,42,43]
$\eta_B$	0.5522	$\pm 0.0022$	id	id	id	[44]

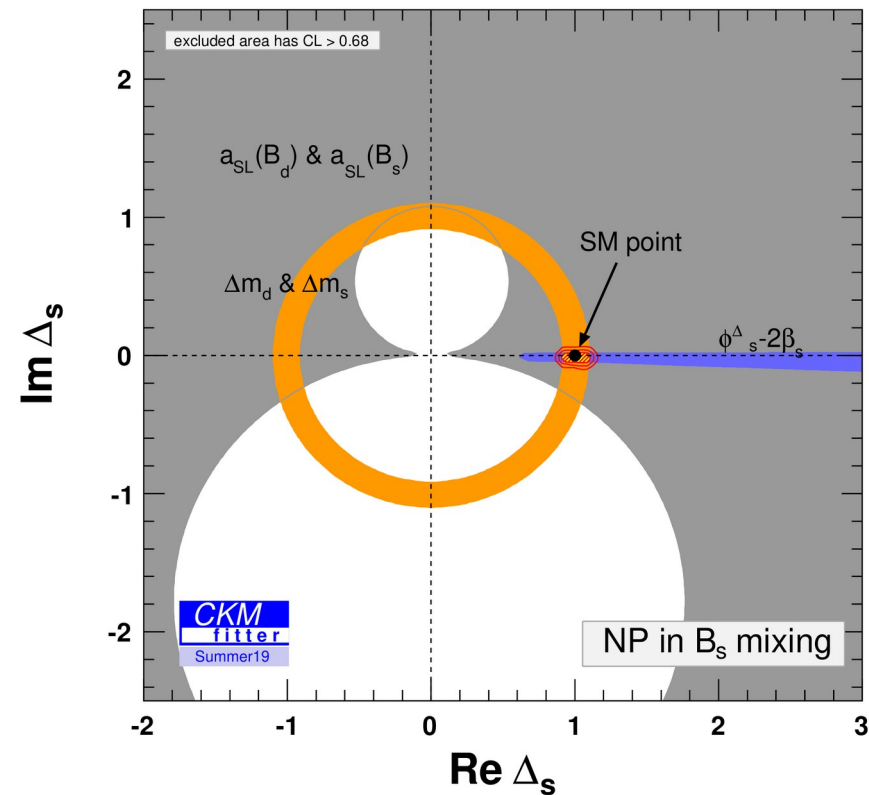
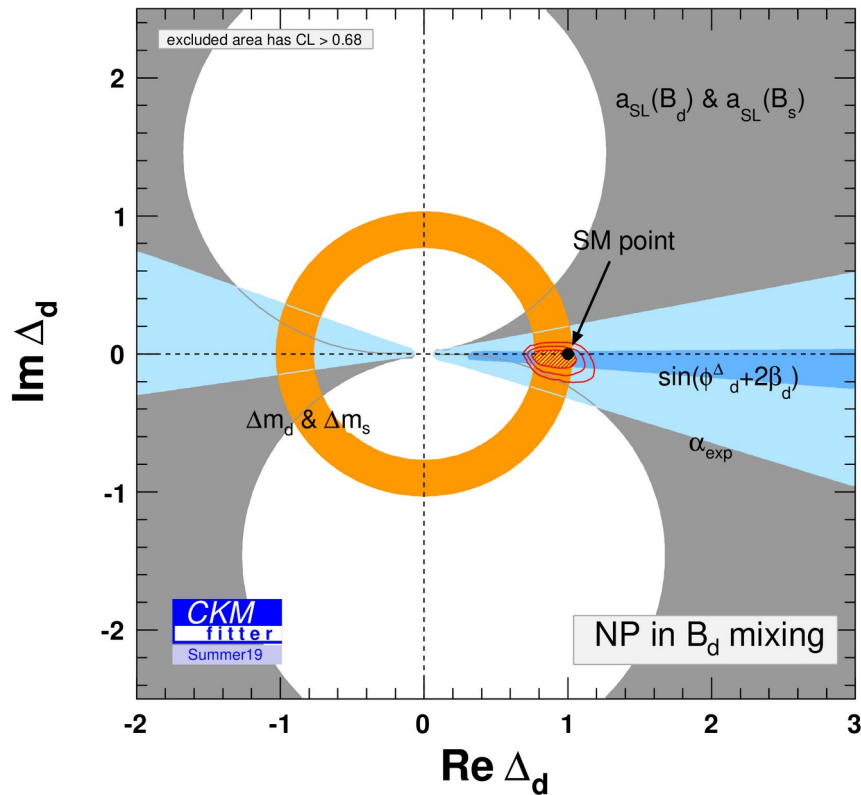
[See for refs.: PRD 102, 056023 (2020), arXiv:2006.04824  
and also EPJPlus 136, 837 arXiv:2106.01259,  
and EPJPlus 136, 912 arXiv:2106.12168]

# Different representation

$$\langle B_q | \mathcal{H}_{\Delta B=2}^{\text{SM+NP}} | \bar{B}_q \rangle \equiv \langle B_q | \mathcal{H}_{\Delta B=2}^{\text{SM}} | \bar{B}_q \rangle \times (\text{Re}(\Delta_q) + i \text{Im}(\Delta_q))$$

$$\text{Re}(\Delta_q) + i \text{Im}(\Delta_q) = r_q^2 e^{i2\theta_q} = 1 + h_q e^{i\sigma_q}$$

Soares & Wolfenstein, PRD 47, 1021 (1993)  
 Deshpande, Dutta & Oh, PRL77, 4499 (1996)  
 Silva & Wolfenstein, PRD 55, 5331 (1997)  
 Cohen et al., PRL78, 2300 (1997)  
 Grossman, Nir & Worah, PLB 407, 307 (1997)



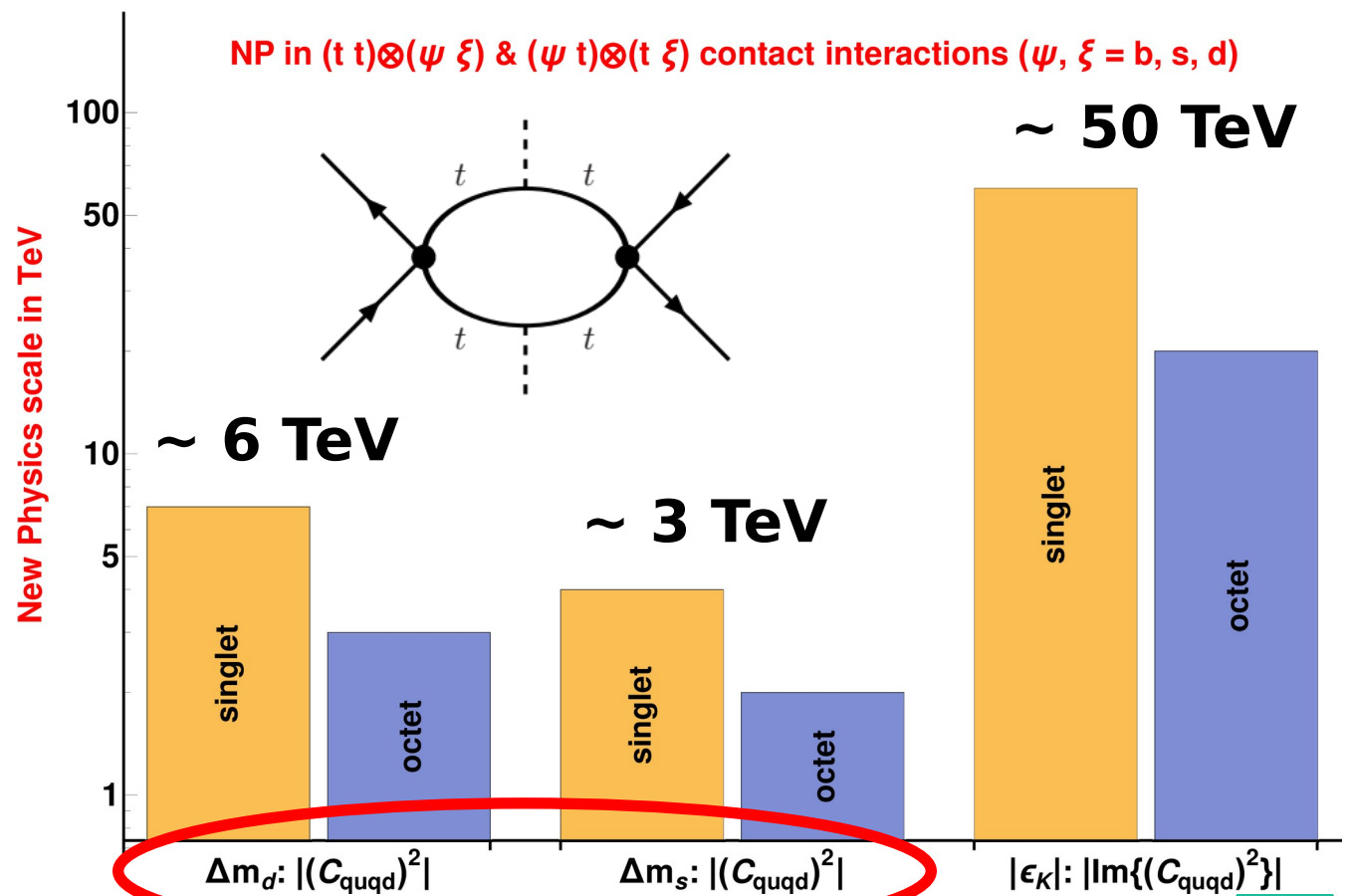
# Current sensitivity to SMEFT dim.-8

## $|\Delta F|=2$ dim.-8: sensitivity to multi-TeV NP effects

- $|\Delta F|=2$  dim.-6 operators: previous slide set bounds for (V-A)x(V-A)
- $(|\Delta F|=1 \text{ dim.-6})^2 = (|\Delta F|=2 \text{ dim.-8 operators})$
- $|\Delta F|=1$  quqd-operator does not change global fit analysis

NP bag parameters:  
[ETM '15, HPQCD '19]

[LVS, arXiv:2201.03038]





# Discovery prospects

**B meson mixing** observables also provide potential **discovery for NP**

