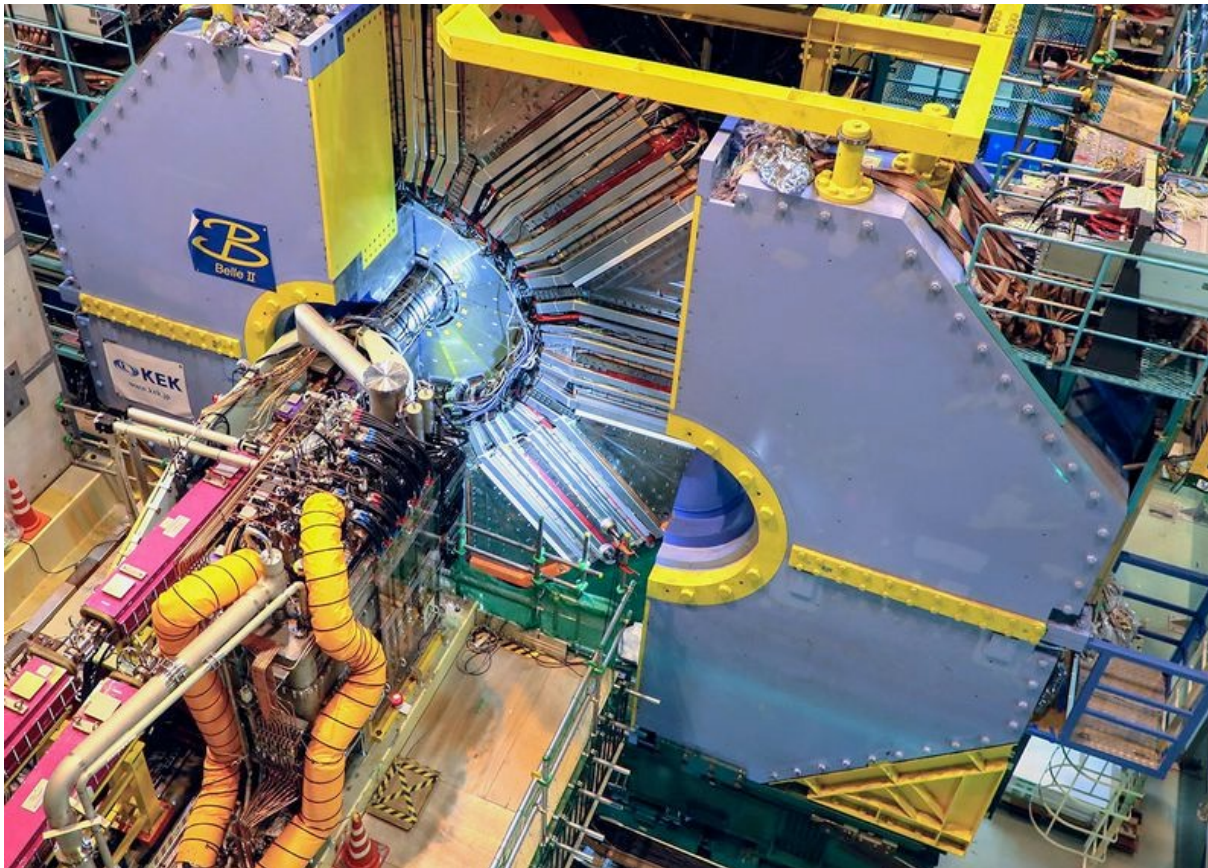




Charm lifetimes at Belle II: recent results

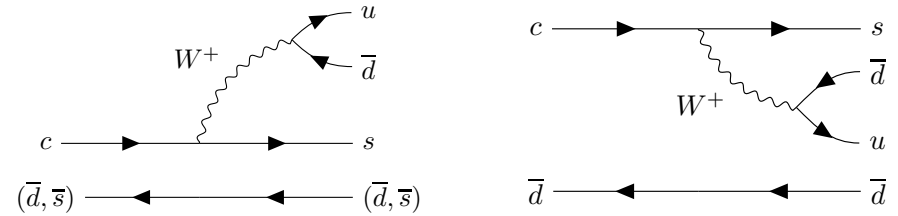
Alan Schwartz
University of Cincinnati, USA
11th International Workshop
on Charm Physics
(CHARM 2023)
University of Siegen
Siegen, Germany
17 July 2023



- Overview of Belle II
- Recent measurements:
Mesons: D^0 , D^+ , D_s^+
Baryons: Λ_c , Ω_c
- Comparison with theory

Charm particle lifetimes:

- qualitatively understood in terms of simple diagrams,**
e.g., $c \rightarrow s$ u anti- d gives ubiquitous $G_F^2 m_c^5 |V_{cs}|^2 / (192\pi^3)$ dependence. Long D^+ lifetime can be understood as arising from destructive interference between spectator and color-suppressed amplitudes.



- quantitatively calculated using the Heavy Quark Expansion:**

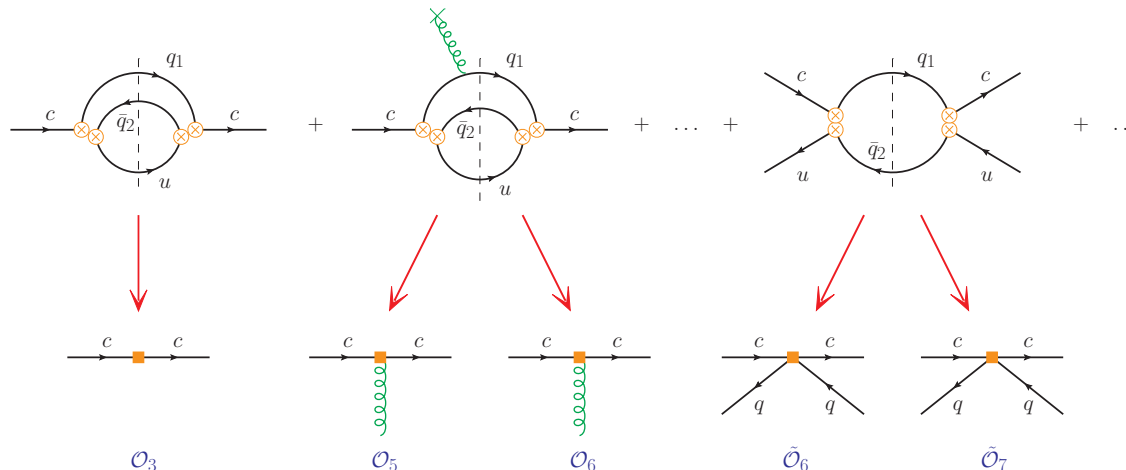
$$\begin{aligned}\Gamma(D) &= \frac{1}{2m_D} \sum_X \int_{\text{PS}} (2\pi)^4 \delta^{(4)}(p_D - p_X) |\langle X(p_X) | \mathcal{H}_{\text{eff}} | D(p_D) \rangle|^2, \\ &\rightarrow \frac{1}{2m_D} \text{Im} \langle D | \mathcal{T} | D \rangle \quad \text{where} \quad \mathcal{T} = i \int d^4x \mathcal{T} \{ \mathcal{H}_{\text{eff}}(x), \mathcal{H}_{\text{eff}}(0) \} \\ &\rightarrow \Gamma_3 + \Gamma_5 \frac{\langle \mathcal{O}_5 \rangle}{m_c^2} + \Gamma_6 \frac{\langle \mathcal{O}_6 \rangle}{m_c^3} + \dots + 16\pi^2 \left(\tilde{\Gamma}_6 \frac{\langle \tilde{\mathcal{O}}_6 \rangle}{m_c^3} + \tilde{\Gamma}_7 \frac{\langle \tilde{\mathcal{O}}_7 \rangle}{m_c^4} + \dots \right)\end{aligned}$$

ΣX is sum over final states

via optical theorem

via Heavy Quark Expansion

Wilson coefficients Γ_i are expanded in powers of α_s and calculated perturbatively



Lenz, IJMP A30 (2015)
Lenz et al., JHEP 12 (2020) 199
King, Lenz et al., JHEP 08 (2022) 241
Gratrex et al., JHEP 07 (2022) 058



Major accelerator upgrade (KEKB $\rightarrow$ SuperKEKB)

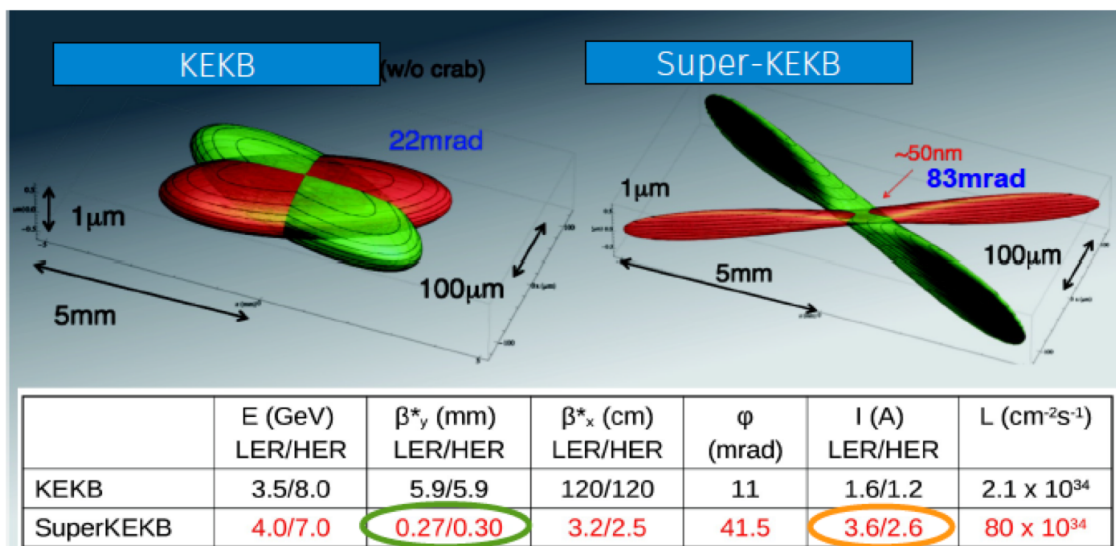
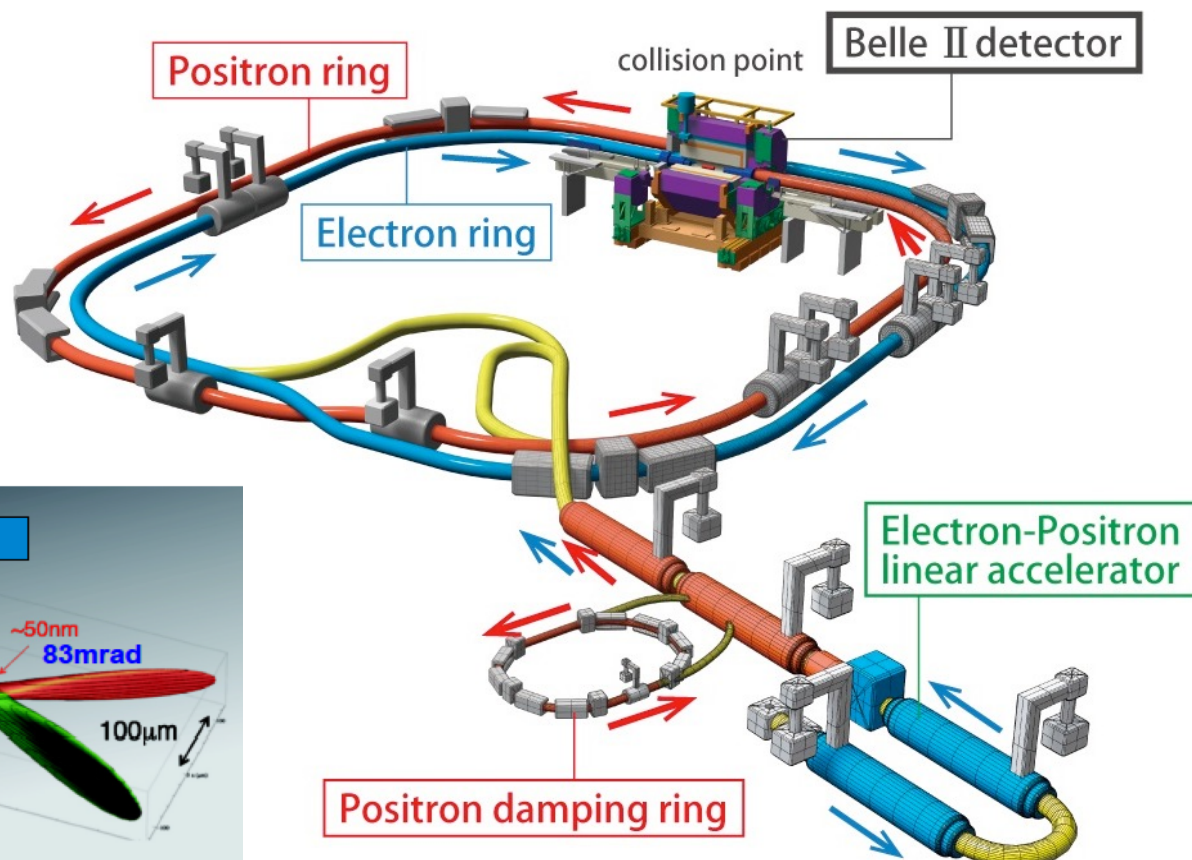
e^+e^- collider running at the Upsilon(4S) [and Upsilon(5S)] resonances with 7 GeV (e^-) on 4 GeV(e^+) beams.
New e^+ damping ring, new e^+ storage ring, new IR optics, Superconducting FF, new RF

beam size:

100 μm (H) x 2 μm (V)
 $\rightarrow$ 10 μm (H) x 59 nm(V)

Belle-II Goal:

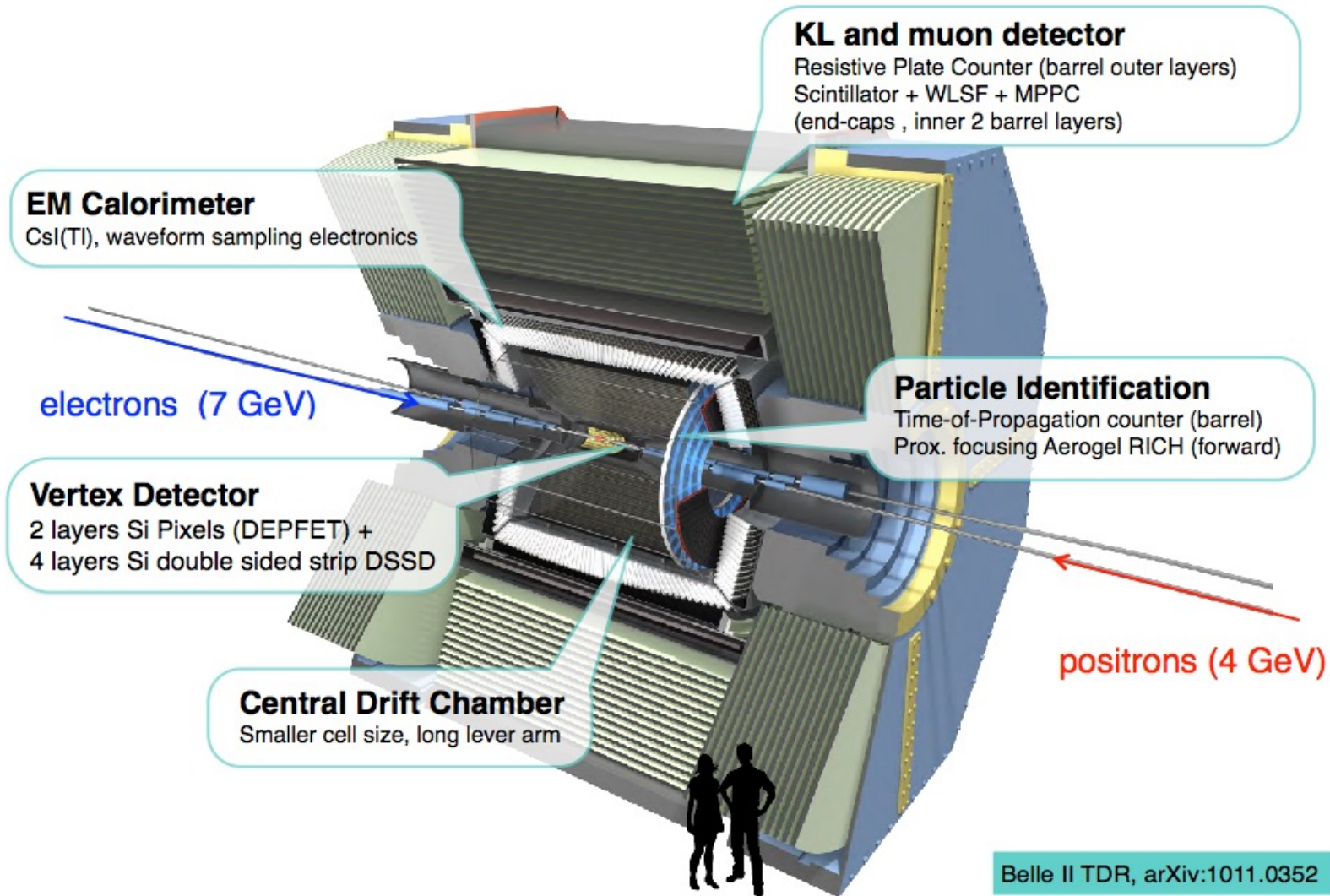
30 x Belle = $\sim 6 \times 10^{35}$



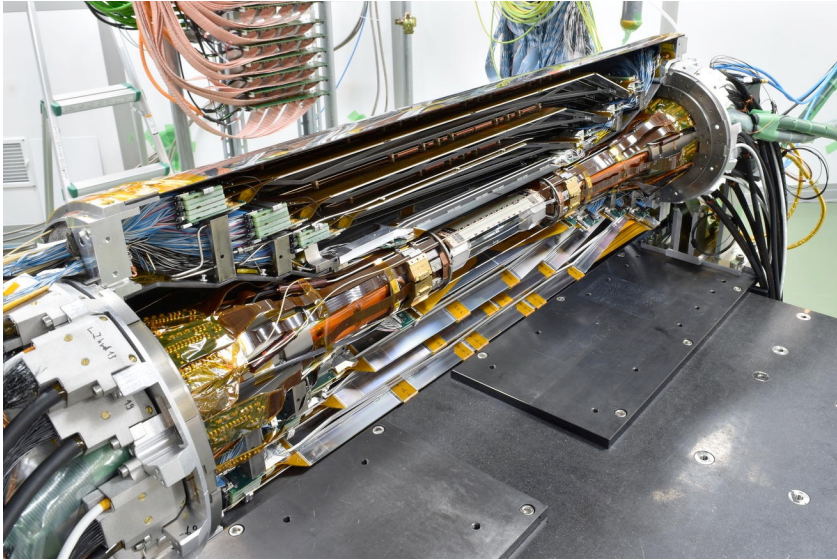
factor 20

factor 2-3

The Belle II Experiment



Charm lifetimes: measurement @ Belle II



Six-layer silicon vertex detector:

(beampipe $r = 10$ mm)

DEPFET silicon pixels:

Layer 1 $r = 14$ mm

Layer 2 $r = 22$ mm

Double-sided silicon strips:

Layer 3 $r = 38$ mm

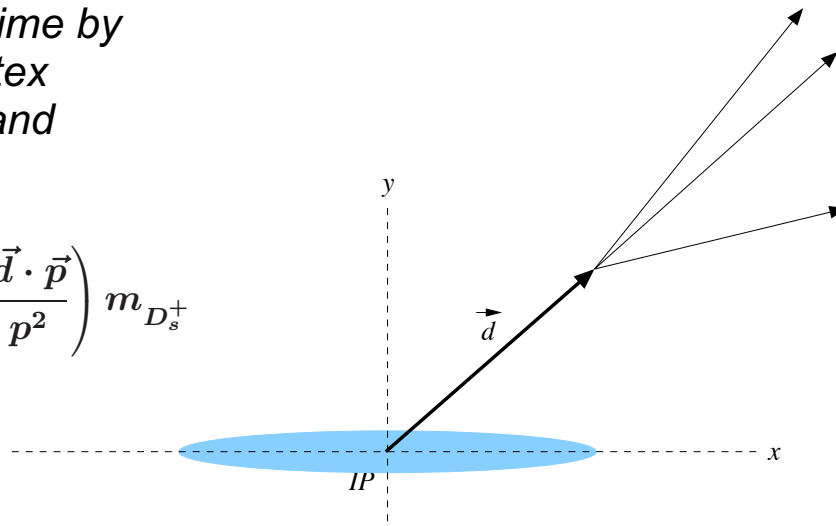
Layer 4 $r = 80$ mm

Layer 5 $r = 115$ mm

Layer 6 $r = 140$ mm

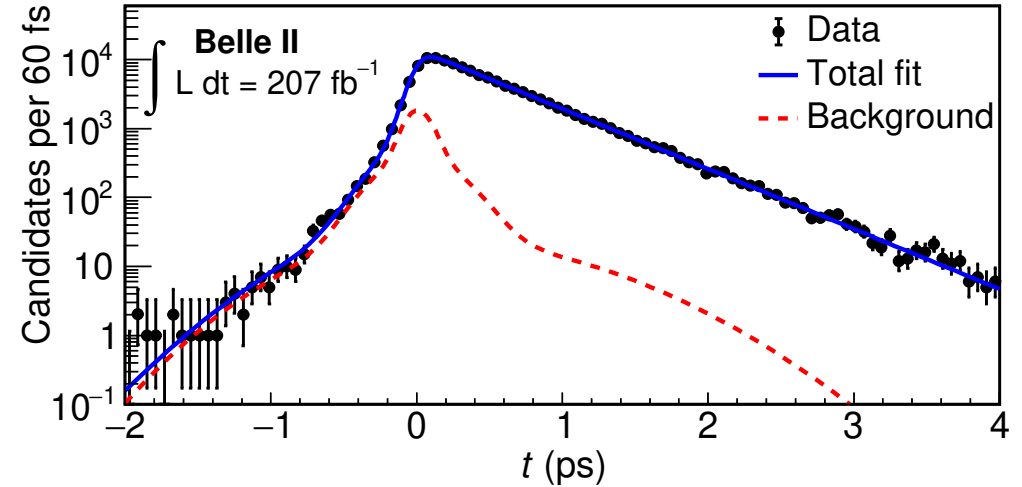
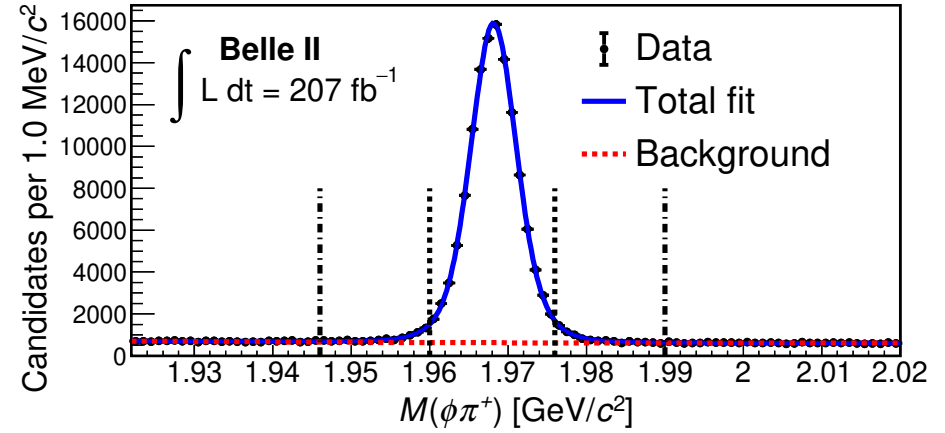
Determine lifetime by measuring vertex displacement and momentum:

$$t = \left(\frac{\vec{d} \cdot \vec{p}}{p^2} \right) m_{D_s^+}$$



- IP is measured at regular intervals using $e^+e^- \rightarrow \mu^+\mu^-$ events
- Uncertainty on t (σ_t) is calculated event-by-event by propagating uncertainties $\delta d_x, \delta d_y, \delta d_z, \delta p_x, \delta p_y, \delta p_z$ and their correlations. The quantity σ_t is used as the width of a Gaussian resolution function for the PDF used to fit the t distribution; this improves the resolution on lifetime.

- Select $D_s^+ \rightarrow \phi \pi^+$ ($\phi \rightarrow K^+ K^-$) decays (low background)
- $p_{\text{CM}}(D_s^+) > 2.5 \text{ GeV}/c$ to eliminate $B \rightarrow D_s^+ X$ decays (preserves 2/3 of $e^+ e^- \rightarrow cc$ events)
- small background remaining from random combinations of real ϕ and π^+
- require $1.960 < M(\phi\pi^+) < 1.976 \text{ GeV}/c^2$; unbinned ML fit give 116k signal, 92% purity
- lifetime determined from unbinned ML fit to t :
- likelihood function for event i :



$$\mathcal{L}(\tau|t^i, \sigma_t^i) = f_{\text{sig}} P_{\text{sig}}(t^i|\tau, \sigma_t^i) P_{\text{sig}}(\sigma_t^i) + (1 - f_{\text{sig}}) P_{\text{bkg}}(t^i|\tau, \sigma_t^i) P_{\text{bkg}}(\sigma_t^i)$$

(to avoid bias:
Punzi, arXiv:physics/0401045)

- PDF for signal D_s^+ decays:

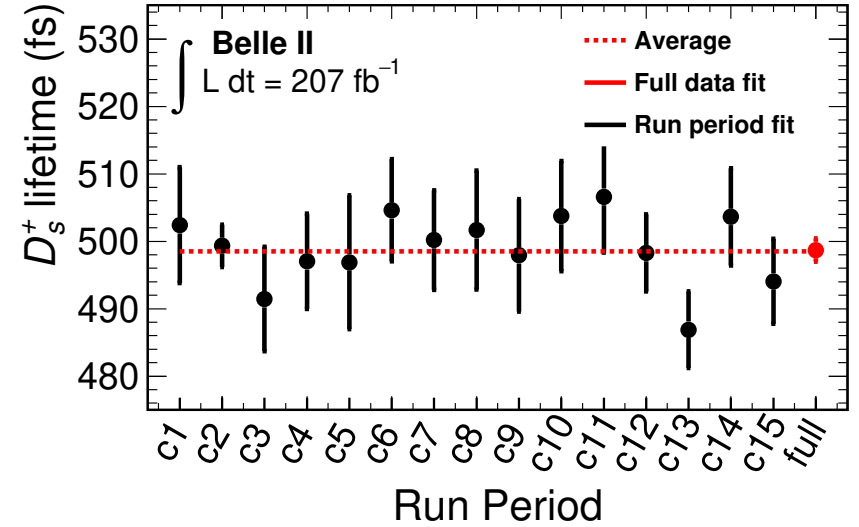
$$P_{\text{sig}}(t^i | \tau, \sigma_t^i) = \frac{1}{\tau} \int e^{-t'/\tau} R(t^i - t'; \mu, s, \sigma_t^i) dt'$$

- resolution function R is a single Gaussian with mean μ and per-candidate standard deviation $s \times \sigma_t^i$; μ and scaling parameter s are floated
- PDF for background is taken from fitting $M(\phi\pi^+)$ upper sideband $[1.990, 2.020] \text{ GeV}/c^2$

- Result: $\tau_{D_s^+} = (498.7 \pm 1.7^{+1.1}_{-0.8}) \text{ fs}$

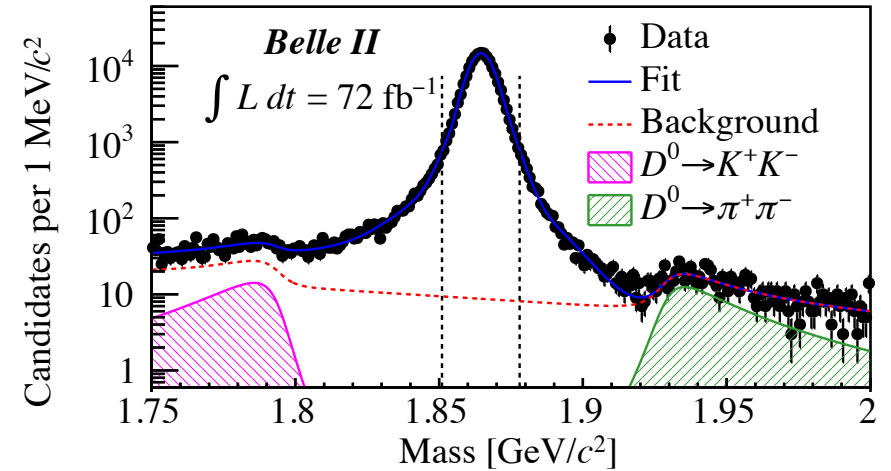
- Systematic uncertainties:

Source	Uncertainty (fs)
Resolution function	+0.85
Background (t, σ_t) distribution	± 0.40
Binning of σ_t histogram PDF	± 0.10
Imperfect detector alignment	± 0.56
Sample purity	± 0.09
Momentum scale factor	± 0.28
D_s^+ mass	± 0.02
Total	$+1.14$ -0.76



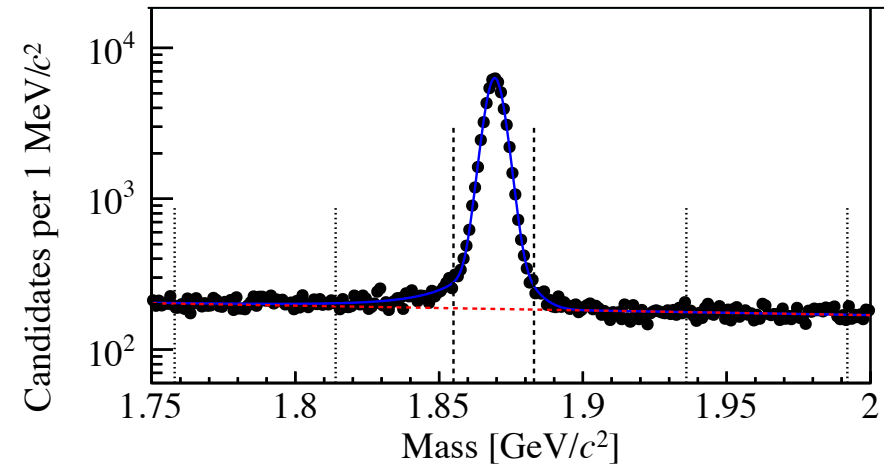
- Select $D^{*+} \rightarrow D^0 \pi_s^+$ ($D^0 \rightarrow K^- \pi^+$) decays (~no background)
- $p_{\text{CM}}(D^{*+}) > 2.5 \text{ GeV}/c$ to eliminate $B \rightarrow D^{*+} X$ decays
- require $1.851 < M(K^- \pi^+) < 1.878 \text{ GeV}/c^2$ and $144.94 < M(K^- \pi^+ \pi_s^+) - M(K^- \pi^+) < 145.90 \text{ MeV}/c^2$; binned χ^2 fit give 171k signal, 99.8% purity

171k $D^0 \rightarrow K^- \pi^+$



- Select $D^{*+} \rightarrow D^+ \pi^0$ ($D^+ \rightarrow K^- \pi^+ \pi^+$) decays (low background), where $\pi^0 \rightarrow \gamma\gamma$ and $m(\gamma\gamma) \in [120, 145] \text{ MeV}/c^2$
- $p_{\text{CM}}(D^{*+}) > 2.6 \text{ GeV}/c$ to eliminate $B \rightarrow D^{*+} X$ decays
- require $1.855 < M(K^- \pi^+) < 1.883 \text{ GeV}/c^2$ and $138 < \Delta M < 143 \text{ MeV}/c^2$; binned χ^2 fit give 59k signal, 91% purity

59k $D^+ \rightarrow K^- \pi^+ \pi^+$



- lifetime determined from unbinned ML fit to (t, σ_t)

- PDF for signal decays:

$$P_{\text{sig}}(t^i | \tau, \sigma_t^i) = \frac{1}{\tau} \int e^{-t'/\tau} R(t^i - t'; \mu, s, \sigma_t^i) dt'$$

- resolution function R is a double Gaussian for D^0 (single Gaussian for D^+) with mean μ and per-candidate standard deviation $s \times \sigma_t^i$; μ and scaling parameter s are floated

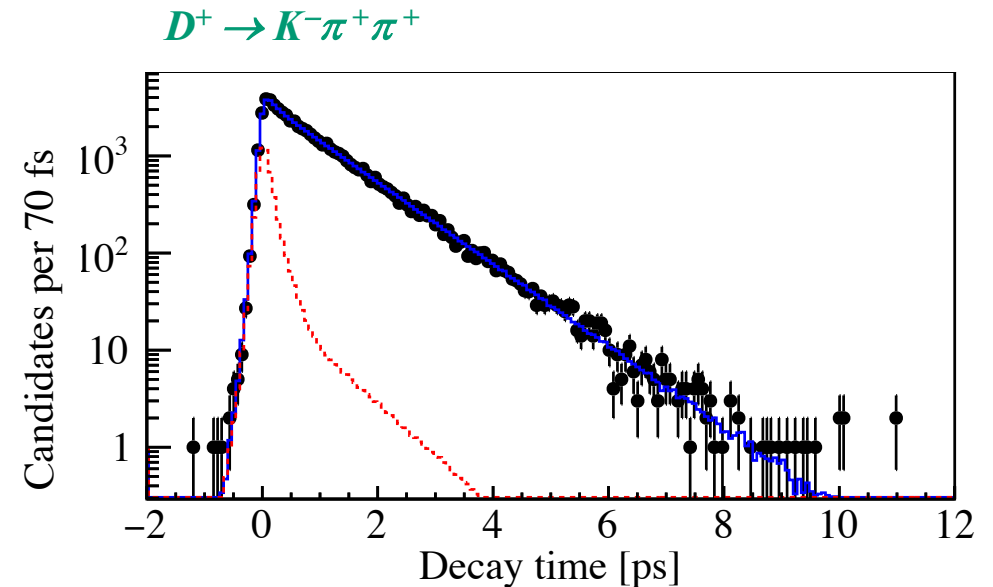
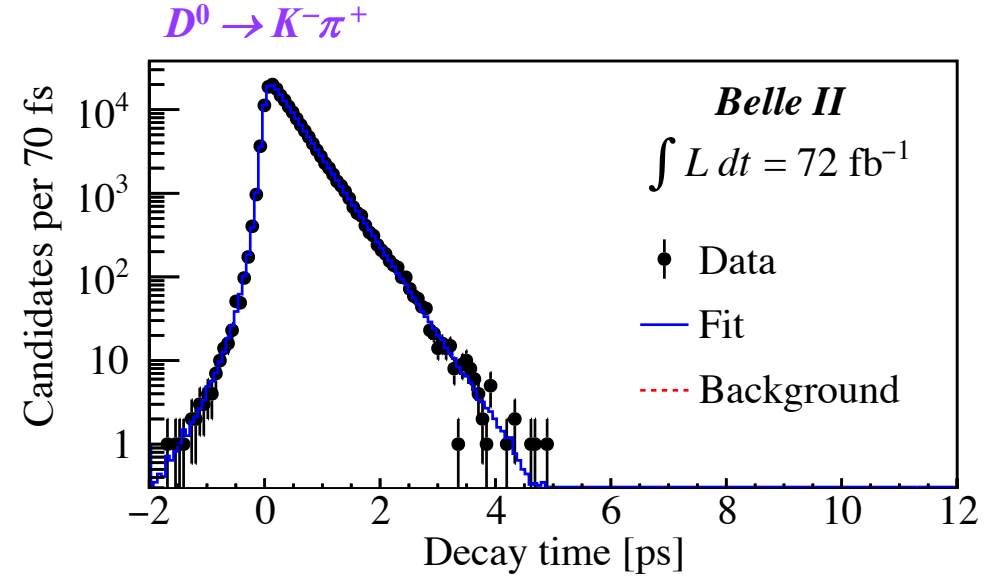
- PDF for D^+ background is taken from fitting $M(K^-\pi^+\pi^+)$ sidebands $[1.758, 1.814]$ and $[1.936, 1.992] \text{ GeV}/c^2$. D^0 background is neglected, with a systematic included

- Results:

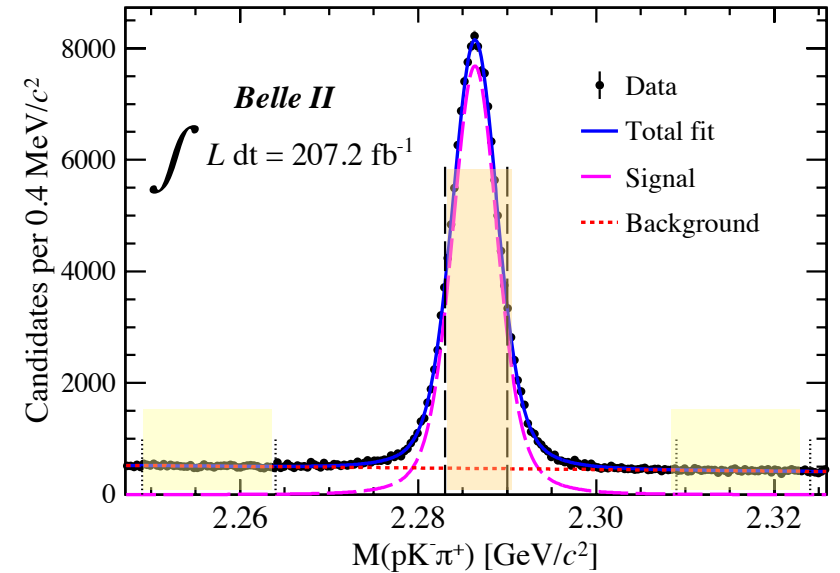
$$\begin{aligned} \tau_{D^0} &= (410.5 \pm 1.1 \pm 0.8) \text{ fs} \\ \tau_{D^+} &= (1030.4 \pm 4.7 \pm 3.1) \text{ fs} \end{aligned}$$

- Systematic uncertainties:

Source	$\tau(D^0)$ (fs)	$\tau(D^+)$ (fs)
Resolution model	0.16	0.39
Backgrounds	0.24	2.52
Detector alignment	0.72	1.70
Momentum scale	0.19	0.48
Total	0.80	3.10



- Select $\Lambda_c^+ \rightarrow pK^-\pi^+$ decays (low background)
- $p_{\text{CM}}(\Lambda_c^+) > 2.5 \text{ GeV}/c$ to eliminate $B \rightarrow \Lambda_c^+ X$ decays
- require $M(pK^-\pi^+) \in [2.283, 2.290] \text{ GeV}/c^2$; binned χ^2 fit gives 116k signal, 93% purity
- lifetime determined from unbinned ML fit to (t, σ_t) . Background (t, σ_t) distribution is determined from sidebands $M(pK^-\pi^+) \in [2.249, 2.264] \text{ GeV}/c^2$ or $[2.309, 2.324] \text{ GeV}/c^2$
- Resolution function $R(t, \sigma_t)$ is a single Gaussian with mean μ and standard deviation $s \propto \sigma_t$, where μ and s are floated
- problematic background from $\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-$, $\Xi_c^+ \rightarrow \Lambda_c^+ \pi^0$ decays: $\tau(\Xi_c^0) = 153 \text{ fs}$, $\tau(\Xi_c^+) = 456 \text{ fs}$.
 - Ξ contamination in Λ_c^+ sample is estimated by fitting distribution of Λ_c^+ vertex displacement in plane transverse to the beam. Result: 374 events (0.003% of Λ_c^+ candidates).
 - To reduce, impose vetos:
 $M(pK^-\pi^+\pi^-) - M(pK^-\pi^+) \notin [183.4, 186.4] \text{ MeV}/c^2$
 $M(pK^-\pi^+\pi^0) - M(pK^-\pi^+) \notin [175.3, 187.3] \text{ MeV}/c^2$
 This reduces Ξ decays by 40%.
 - Effect of remaining decays is estimated via MC simulation; bias of 0.34 fs is subtracted from fitted $\tau(\Lambda_c^+)$



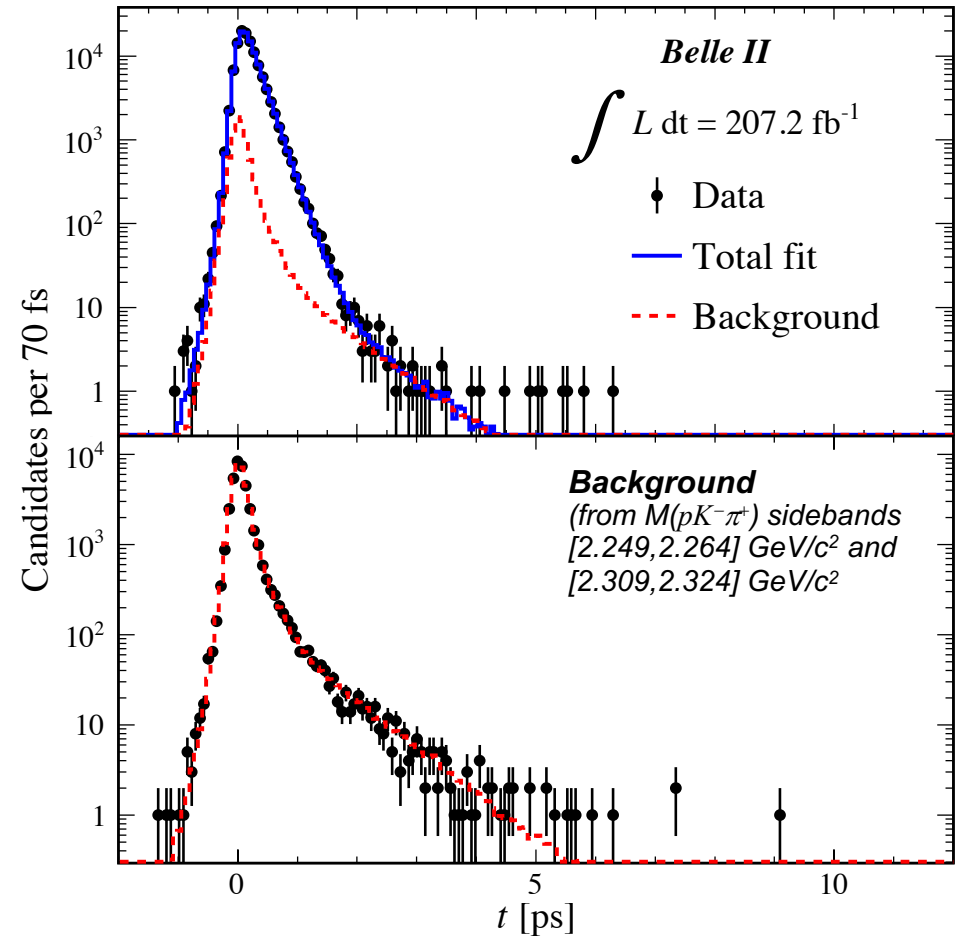
- PDF for background is sum of two exponentials and a δ function, all convolved with resolution functions having floated parameters μ_b , s_b

- Result:

$$\tau_{\Lambda_c^+} = (203.20 \pm 0.89 \pm 0.77) \text{ fs}$$

- Systematic uncertainties:

Source	Uncertainty [fs]
Ξ_c contamination	0.34
Resolution model	0.46
Non- Ξ_c backgrounds	0.20
Detector alignment	0.46
Momentum scale	0.09
Total	0.77



Theory expectation:
(& E687, WA89)

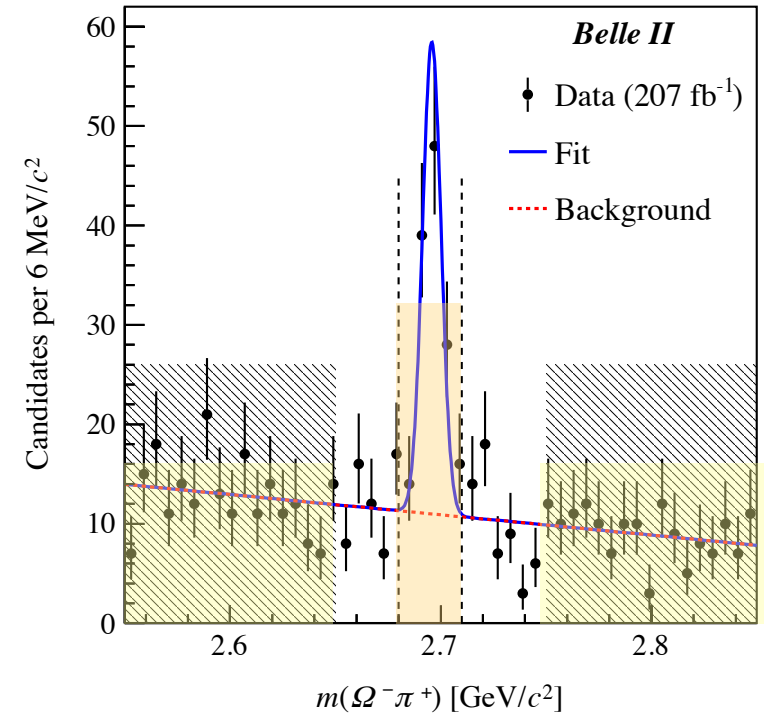
$$\tau(\Omega_c) < \tau(\Xi_c^0) < \tau(\Lambda_c^+) < \tau(\Xi_c^+)$$

LHCb measurement:
(2018, 2022)

$$\tau(\Xi_c^0) < \tau(\Lambda_c^+) < \tau(\Omega_c) < \tau(\Xi_c^+)$$

$\Rightarrow$ Belle II can resolve this

- Select $\Omega_c \rightarrow \Omega \pi^+$, $\Omega^- \rightarrow \Lambda K^-$, $\Lambda \rightarrow p \pi^-$ decays (large CF branching fractions)
- $p_{\text{CM}}(\Omega_c)/p_{\text{max}} > 0.6$ to eliminate $B \rightarrow \Omega_c X$ decays, where $p_{\text{max}} = \sqrt{[(E_{\text{beam}}^{\text{CM}})^2 - m(\Omega \pi)^2]}$
- require $M(\Omega^- \pi^+) \in [2.68, 2.71] \text{ GeV}/c^2$; unbinned ML fit gives 132 signal decays, 67% purity
- lifetime determined from unbinned ML fit to (t, σ_t) . Background (t, σ_t) distribution is determined from sidebands $M(\Omega^- \pi^+) \in [2.55, 2.65] \text{ GeV}/c^2$ and $[2.75, 2.85] \text{ GeV}/c^2$
- Resolution function $R(t, \sigma_t)$ is a single Gaussian with mean μ and standard deviation s $X \sigma_t$, where μ and s are floated



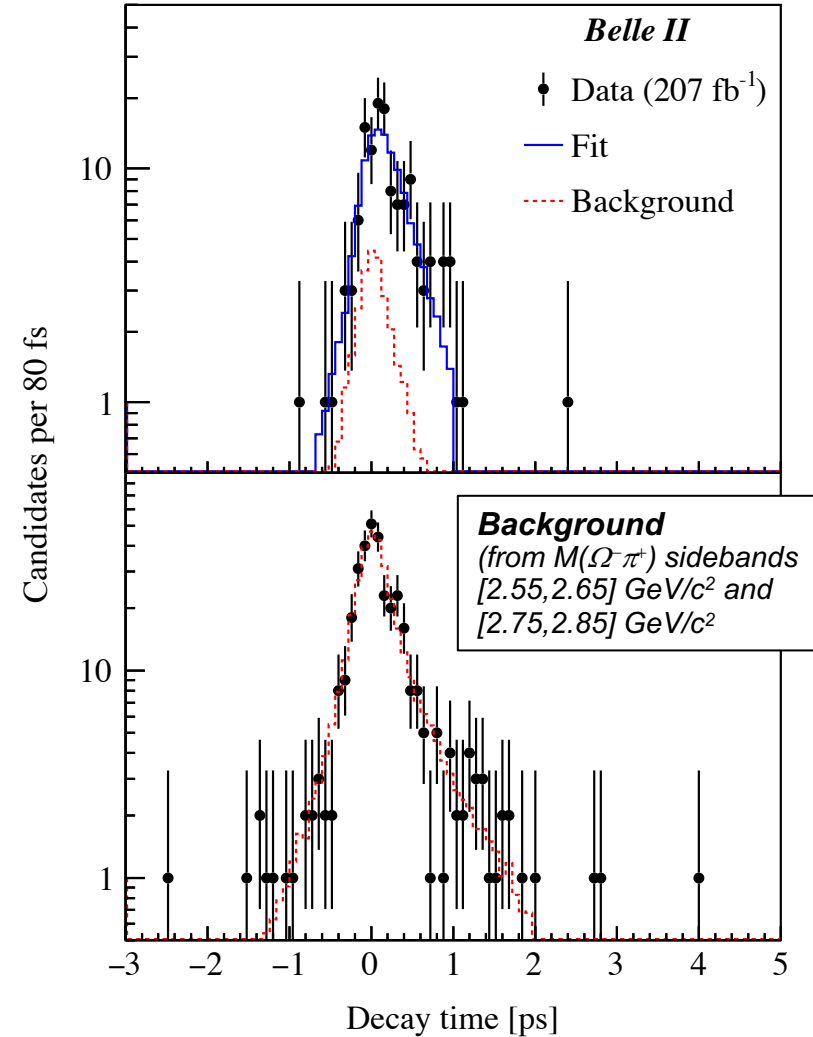
- PDF for background is sum of an exponential and a δ function, both convolved with a Gaussian resolution function having floated parameters μ_b and s_b

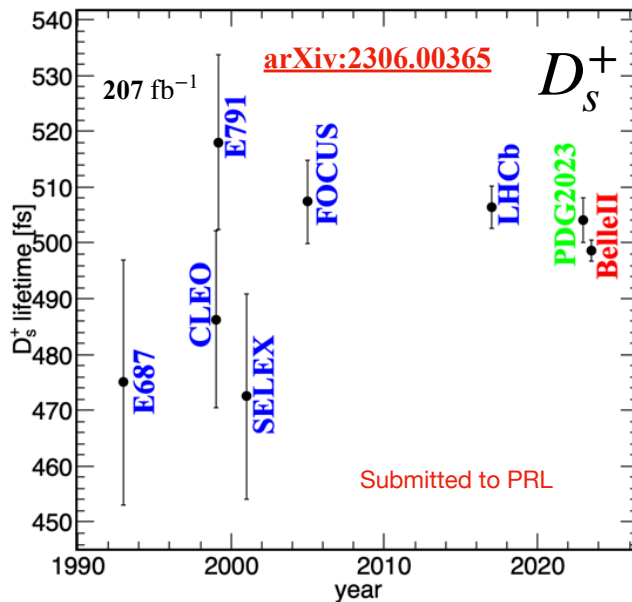
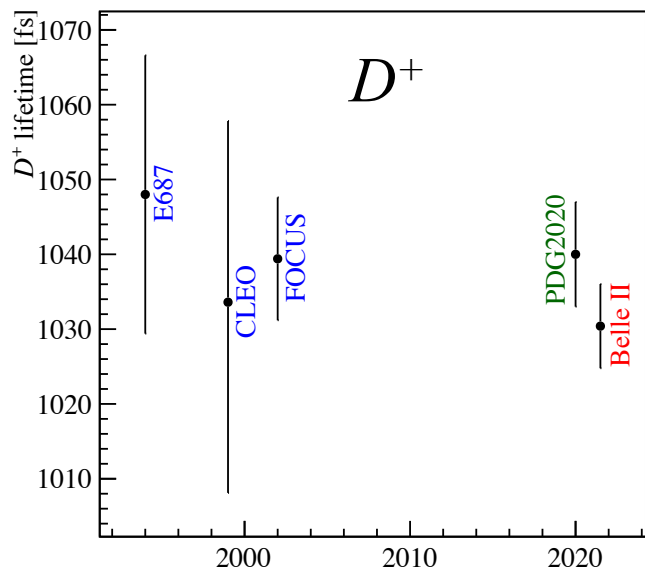
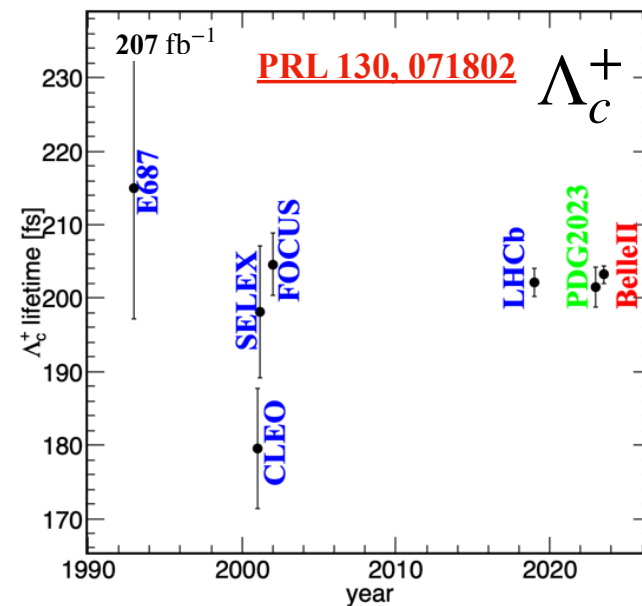
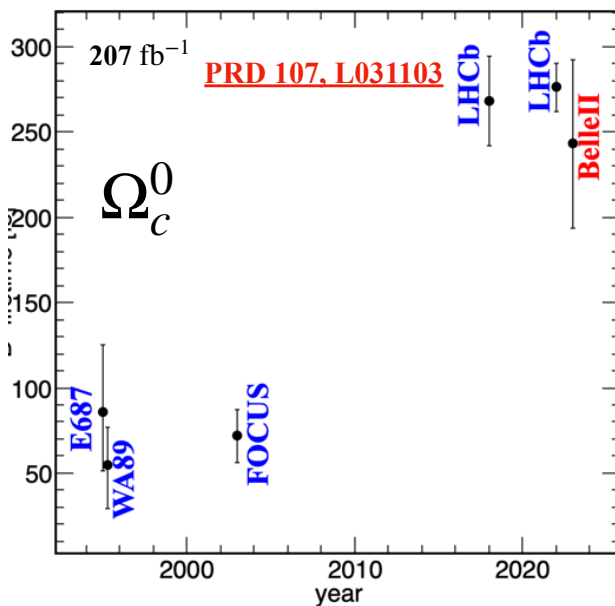
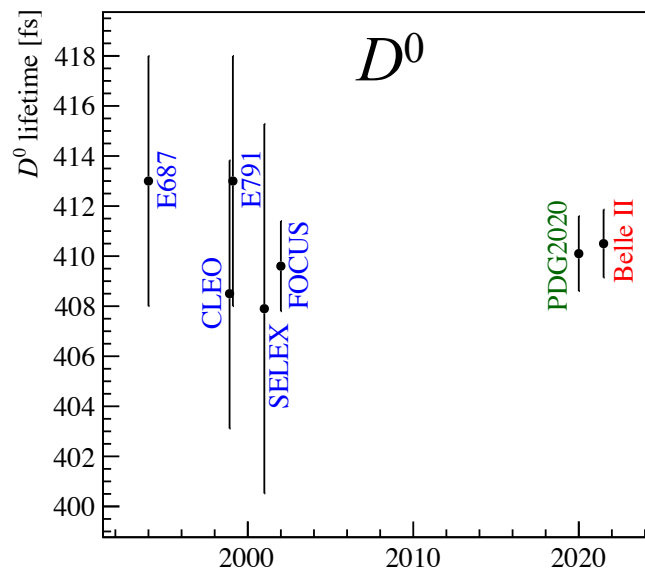
- Result:

$$\tau_{\Omega_c^0} = (243 \pm 48 \pm 11) \text{ fs}$$

- Systematic uncertainties:

Source	Uncertainty (fs)
Fit bias	3.4
Resolution model	6.2
Background model	8.3
Detector alignment	1.6
Momentum scale	0.2
Input Ω_c^0 mass	0.2
Total	11.0





- In all cases except for Ω_c^0 , Belle II has made the world's highest precision measurement (in some cases after 20 years)*
- For Ω_c^0 , the Belle II measurement resolves the discrepancy between LHCb and all previous measurements (LHCb's long lifetime looks correct)*

King, Lenz et al., JHEP 08 (2022) 241; arXiv:2109.13219
 Gratrex et al., JHEP 07 (2022) 058; arXiv:2204.11935

Some comparisons with theory:

Quantity	 Belle II	King et al. JHEP 08 (2022) 241	Gratrex et al. JHEP 07 (2022) 058
$\tau(D^0)$	$410.5 \pm 1.1 \pm 0.8$		
$\tau(D^+)$	$1030.4 \pm 4.7 \pm 3.1$		
$\tau(D_s^+)$	$498.7 \pm 1.7^{+1.1}_{-0.8}$		
$\tau(D^+)/\tau(D^0)$	2.510		
$\tau(D_s^+)/\tau(D^0)$	1.215		
$\tau(\Lambda_c^+)$	$203.20 \pm 0.89 \pm 0.77$		
$\tau(\Omega_c^0)$	$243 \pm 48 \pm 11$		
$\tau(\Omega_c^0)/\tau(\Lambda_c^+)$	1.20		

All measurements and predictions in reasonable agreement, some tension...

