

Dark matter search at Belle



3rd DMNet 2023 - Padova

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TOKYO METROPOLITAN UNIVERSITY

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Experiment and Theory Tension

Extra Leptophilic $U(1)$ gauge boson, Z'

KEKB and Belle

Z' searches in Belle

The invisible Z' search

Punzi Loss Neural Net

The leptophilic scalar search @ Belle

Summary

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$(g - 2)_\mu$ 2021 and 2023 measurements

$(g - 2)_\mu$ 2021 measurement [PRL 126, 141801 - 2021](#)

$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (251 \pm 59) \times 10^{-11} \text{ corresponding to } 4.2\sigma$$

$(g - 2)_\mu$ 2023 measurement [2308.06230](#)

$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (249 \pm 48) \times 10^{-11} \text{ corresponding to } 5.1\sigma$$

2 options

1. The gap between SM and the Experimental result can be bridged with an improved calculation of a_{μ}^{SM}
2. **New Physics is the reason for the gap**

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$L_{e,\mu,\tau}$ are the lepton numbers

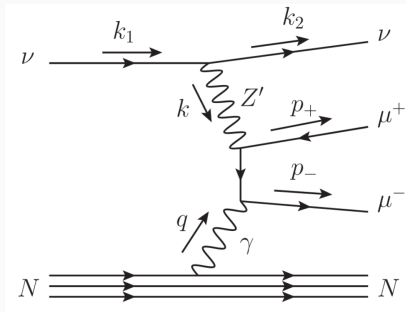
$$L_1 = L_e - L_\mu, L_2 = L_e - L_\tau \text{ and } L_3 = L_\mu - L_\tau$$

Three different new gauge groups

so that $G_{\text{SM}} \otimes U(1)_{L_{1,2,3}}$

allows for an additional neutral gauge boson (Z'_1, Z'_2 , and Z'_3)

Z'_1 and Z'_2 mediate $L_1 = L_e - L_\mu$ and $L_2 = L_e - L_\tau$



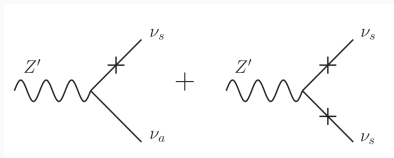
$$\mathcal{L}_{Z'} = -\frac{1}{4}(Z')_{\alpha\beta}(Z')^{\alpha\beta} + \frac{1}{2}m_{Z'}^2 Z'_\alpha Z'^\alpha + \underbrace{g' Z'_\alpha (\bar{\ell}_2 \gamma^\alpha \ell_2 - \bar{\ell}_3 \gamma^\alpha \ell_3 + \bar{\mu}_R \gamma^\alpha \mu_R - \bar{\tau}_R \gamma^\alpha \tau_R)}_{\text{coupling to electroweak doublets and right-handed leptons}}$$

$$\mathcal{L}_{\text{int}} = -g' \bar{\mu} \gamma^\mu Z'_\mu \mu + g' \bar{\tau} \gamma^\mu Z'_\mu \tau - g' \bar{\nu}_{\mu,L} \gamma^\mu Z'_\mu \nu_{\mu,L} + g' \bar{\nu}_{\tau,L} \gamma^\mu Z'_\mu \nu_{\tau,L}$$

where the g' is the $U(1)$ gauge coupling, $(Z')_{\alpha\beta} = \partial_\alpha Z'_\beta - \partial_\beta Z'_\alpha$ is the field strength, $\ell_2 = (\nu_\mu, \mu_L)$ and $\ell_3 = (\nu_\tau, \tau_L)$ are the electroweak doublets. The g' coupling the new gauge boson Z' to the electroweak doublets and the that enhances the rate of neutrino trident production in the $\nu_\mu N \rightarrow N \nu \mu^+ \mu^-$ process.

Neutrino trident production has not been observed so far!

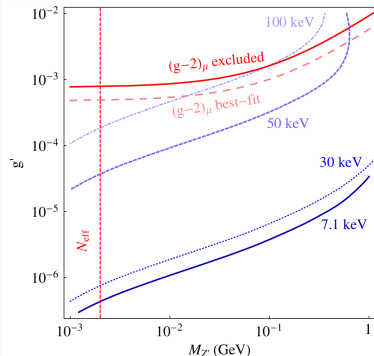
Assuming that a sterile neutrino ν_s , that mixes weakly with the active $\nu_{a(\mu,\tau)}$ states, is added to the SM.



$$\begin{pmatrix} \nu_a \\ \nu_s \end{pmatrix} \equiv \begin{pmatrix} \cos \theta_0 & \sin \theta_0 \\ -\sin \theta_0 & \cos \theta_0 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

$$\Gamma_{Z' \rightarrow \nu_s} = \frac{g'^2 M_{Z'}}{12\pi} \frac{\sin^2 2\theta_m}{4} (1 + \tan^2 \theta_m)$$

A massive Z' with $\text{MeV} < m_{Z'} < \text{GeV}$ with coupling $10^{-2} < g' < 10^{-6}$ results in the correct relic abundance of sterile neutrinos DM



- $M_{Z'} - g'$ plane
- Magnetic moment of the muon anomaly favored region
- $N_{\text{eff}} \rightarrow M_{Z'} \gtrsim 2.0 \text{ MeV}$ from Planck measurement constraint 1303.5076
- Sterile neutrino candidates

- $m_s = 7.1 \text{ keV} \sin 2\theta_0 = 8 \times 10^{-6}$
- $m_s = 30 \text{ keV} \sin 2\theta_0 = 2.2 \times 10^{-6}$
- $m_s = 50 \text{ keV} \sin 2\theta_0 = 3.5 \times 10^{-8}$
- $m_s = 100 \text{ keV} \sin 2\theta_0 = 5 \times 10^{-9}$
- $(Y_{\text{DM}} = 4.7 \times 10^{-4} \text{ keV}/m_s)$

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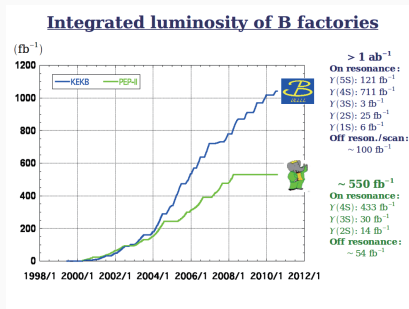
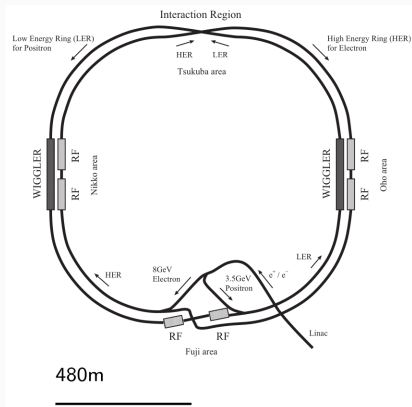
The leptophilic scalar search @ Belle

Summary

The **KEKB** Accelerator

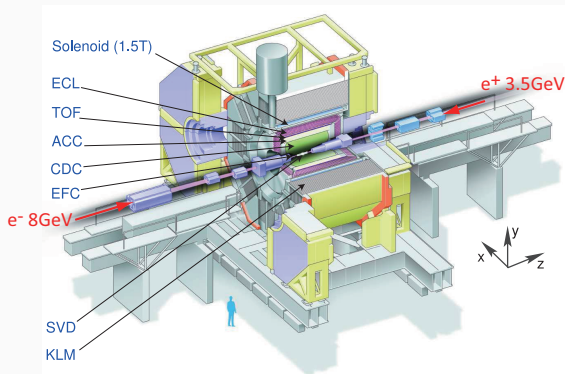
KEKB is an e^+e^- collider made up of two rings, a High Energy Ring, HER and a Low Energy Ring, LER.

Located in Tsukuba and has achieved a record Luminosity of 1 ab^{-1}



KEKB together with the Belle detector were responsible for confirming the CPV formalism in the quark sector, the 2008 Nobel Prize of Physics.

The Belle Detector



- SVD (Silicon Vertex Detector)
- EFC (Extreme Forward Calorimeter)
- ACC (Aerogel Cherenkov Counter)
- TOF (Time Of Flight)
- CDC (Central Drift Chamber)
- ECL (Electromagnetic Calorimeter)
- KLM ($K_L^0 - \mu$)

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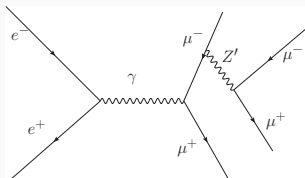
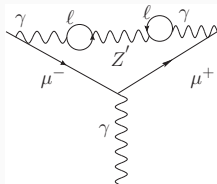
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Punzi Loss Neural Net

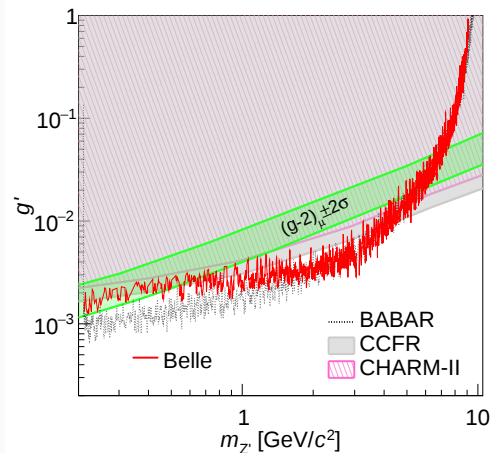
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Summary

Z' search modes in B-factories



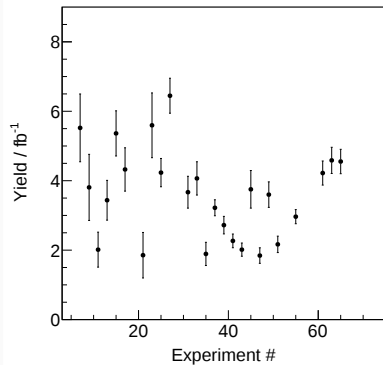
- Motivated by:
 - the $(g - 2)_\mu$
 - connection to **sterile neutrinos** as a dark matter candidate
- $Z' \rightarrow \mu^+ \mu^-$
 - [Martina's talk on Belle II results](#)
- $Z' \rightarrow \text{invisible}$
 - $Z' \rightarrow \nu \nu$
 - $Z' \rightarrow \chi \bar{\chi}$
 - $Z' \rightarrow e^- \mu^+$ (LFV)
- $\phi_L \rightarrow \ell^+ \ell^-$
- $A' \rightarrow \ell^+ \ell^-$



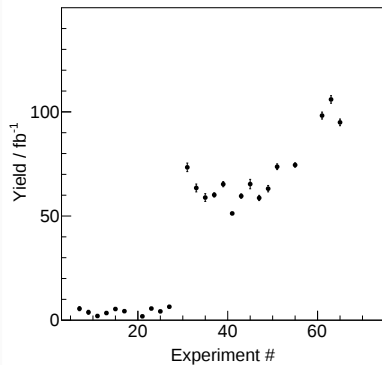
- No Z' signal was found
- Limit set for $0.212(\text{dimuon mass}) \sim 10 \text{ GeV}/c^2$
- Z' contribution for the $(g-2)_\mu$ almost excluded

What did we learn in the Z' visible search?

HadronB skim



tauskimA



Definitions of **tauskimA(B)**

tauskimA

1. $2 \leq \# \text{ q tracks} \leq 8$
2. $|\text{charge sum}| \leq 2$
3. $\sum P^{\text{CM}} < 10 \text{ GeV}/c$
4. $\sum E(ECL) < 10 \text{ GeV}/c$
5. $P_{t\text{max}} > 0.5 \text{ GeV}/c$
6. Evt vtx $|r| < 0.5 \text{ cm}$, $|z| < 3 \text{ cm}$
7. for 2 tracks events
 - 7.1 Sum of $P^{\text{CM}} < 9 \text{ GeV}/c$
 - 7.2 Sum of $E(ECL) < 9 \text{ GeV}$
 - 7.3 $5 < \theta_{\text{missing momentum}} < 175^\circ$
8. $E_{\text{rec}} > 3 \text{ GeV}$ or $P_{t\text{max}} > 1.0 \text{ GeV}/c$
9. for 2 ~ 4 charged tracks
 - 9.1 $E_{\text{tot}} < 9 \text{ GeV}$ or max opening angle $< 175^\circ$
 - 9.2 $N_{\text{barrel}} \geq 2$ or $E(ECL)_{\text{trk}} < 5.3 \text{ GeV}$

Too tight for the visible Z'

tauskimB

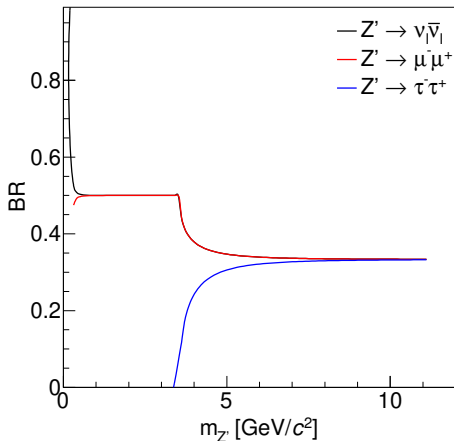
1. $2 \leq \# \text{ q tracks} \leq 8$
2. $|\text{charge sum}| \leq 2$
3. ~~$\sum P^{\text{CM}} < 10 \text{ GeV}/e$~~
4. ~~$\sum E(ECL) < 10 \text{ GeV}/e$~~
5. $P_{t\text{max}} > 0.5 \text{ GeV}/c$
6. Evt vtx $|r| < 1.0 \text{ cm}$, $|z| < 3 \text{ cm}$
7. for 2 tracks events
 - 7.1 ~~Sum of $P^{\text{CM}} < 9 \text{ GeV}/e$~~
 - 7.2 Sum of $E(ECL) < 11 \text{ GeV}$
 - 7.3 $5 < \theta_{\text{missing momentum}} < 175^\circ$
8. $E_{\text{rec}} > 3 \text{ GeV}$ or $P_{t\text{max}} > 1.0 \text{ GeV}/c$
9. for 2 ~ 4 charged tracks
 - 9.1 $E_{\text{tot}} < 9 \text{ GeV}$ or max opening angle $< 175^\circ$ or $2 < \sum E(ECL) < 9 \text{ GeV}$
 - 9.2 $N_{\text{barrel}} \geq 2$ or $E(ECL)_{\text{trk}} < 5.3 \text{ GeV}$

Too loose for the invisible Z'

Z' decay width and Branching Ratio (BR)

$$\bullet \Gamma(Z' \rightarrow \ell^+ \ell^-) = \frac{(g')^2 m_{Z'}}{12\pi} \left(1 + \frac{2m_\ell^2}{m_{Z'}^2} \right) \sqrt{1 - \frac{4m_\ell^2}{m_{Z'}^2}} \theta(m_{Z'} - 2m_\ell)$$

$$\bullet \Gamma(Z' \rightarrow \nu_\ell \bar{\nu}_\ell) = \frac{(g')^2 m_{Z'}}{24\pi}$$



The invisible Z' search

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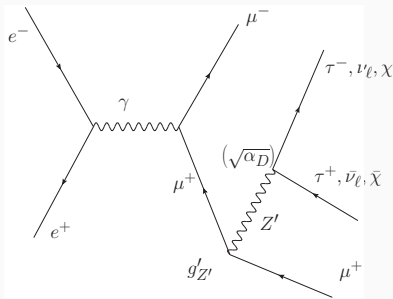
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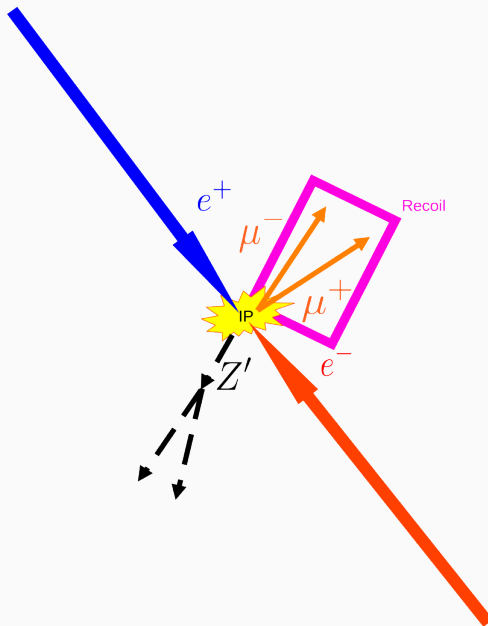
Summary

Z' → invisible or not fully visible

- ~~$Z' \rightarrow \tau^+ \tau^-$~~
 - Recent [Belle II publication](#) renders Belle analysis not competitive
- $Z' \rightarrow \chi \bar{\chi}$
- $Z' \rightarrow \nu_\ell \nu_\ell$



What does it look like?



How were the cuts elaborated?

- 2D histogram $x : M_{Z'}^2$
- Signal resolution σ is obtained under the studied cut
- ε detection efficiency at fixed Z' mass under cuts
- B is the integration of backgrounds around $(\pm 3\sigma)$ Z' mass
- $\frac{\varepsilon}{\sqrt{B}}$ maximized

Background sources

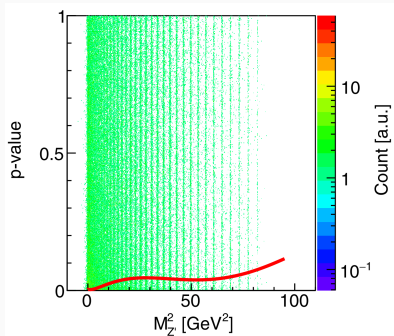
gen	channel	survives
KKMC	$e^+e^- \rightarrow e\bar{e}$	no
	$e^+e^- \rightarrow d\bar{d}$	no
	$e^+e^- \rightarrow s\bar{s}$	no
	$e^+e^- \rightarrow \tau^+\tau^-$	YES
	$e^+e^- \rightarrow \mu^+\mu^-$	YES
BBBREM	$e^+e^- \rightarrow e^+e^-\gamma$	no
AAFH(Diag36)	$e^+e^- \rightarrow e^+e^-e^+e^-$	no
	$e^+e^- \rightarrow e^+e^-\tau^+\tau^-$	no
	$e^+e^- \rightarrow e^+e^-\mu^+\mu^-$	YES
	$e^+e^- \rightarrow \mu^+\mu^-\mu^+\mu^-$	YES
	$e^+e^- \rightarrow \mu^+\mu^-\tau^+\tau^-$	YES
PHOKHARA	$e^+e^- \rightarrow \mu^+\mu^-\gamma_{ISR}$	no
	$e^+e^- \rightarrow n\bar{n}\gamma_{ISR}$	no
	$e^+e^- \rightarrow \pi^+\pi^-\pi^0\gamma_{ISR}$	no
	$e^+e^- \rightarrow p\bar{p}\gamma_{ISR}$	no
	$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0\gamma_{ISR}$	no
	$e^+e^- \rightarrow \pi^+\pi^-\gamma_{ISR}$	no
	$e^+e^- \rightarrow \Lambda\bar{\Lambda}\gamma_{ISR}$	no
	$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\gamma_{ISR}$	no
	$e^+e^- \rightarrow K^+K^-\gamma_{ISR}$	no
	$e^+e^- \rightarrow K^0\bar{K}^0\gamma_{ISR}$	no
BABA	$e^+e^- \rightarrow \mu^+\mu^-$	no
	$e^+e^- \rightarrow \gamma\gamma$	no
	$e^+e^- \rightarrow e^+e^-$	no

Z' invisible selection criteria list

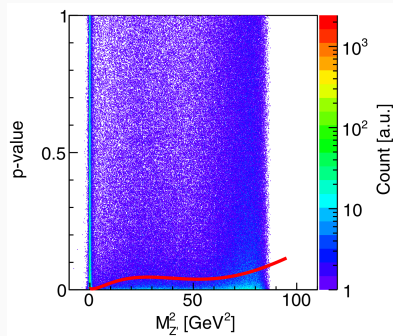
1. 2 tracks of opposite charge only, 2 μ ID
2. Vertex fit of the the 2 tracks, CL cut
3. Energy conservation dependent on $M_{Z'}^2 = s + m_{\mu\mu}^2 - 2E_{\mu\mu}^* \sqrt{s}$
4. Energy sum of neutral cluster, ECL
5. p_t of the two tracks sum dependent on $M_{Z'}$
6. 6.1 Mass conservation on $M_{Z'}$
6.2 Opening angle between tracks
7. Recoil muon pair polar angle
8. Azimuthal angle difference between final state 4-vector and neutral clusters
9. Z' missing angle cut
10. **tauskimB replaced by tauskimA**
11. $p_t^{*Z'}$ projection on $p_{\max}^{*\mu}$ and $p_{\min}^{*\mu}$

Cut example: p-value

Track quality, **p-value**, based on Vertex Fitter

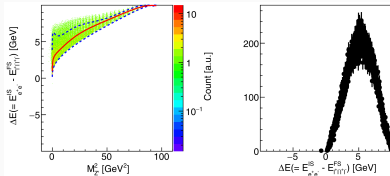


Selection curve for all Z' mass hypotheses signal MC.

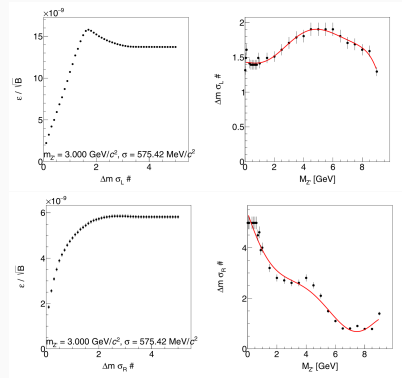


Selection curve for **exp65** data.

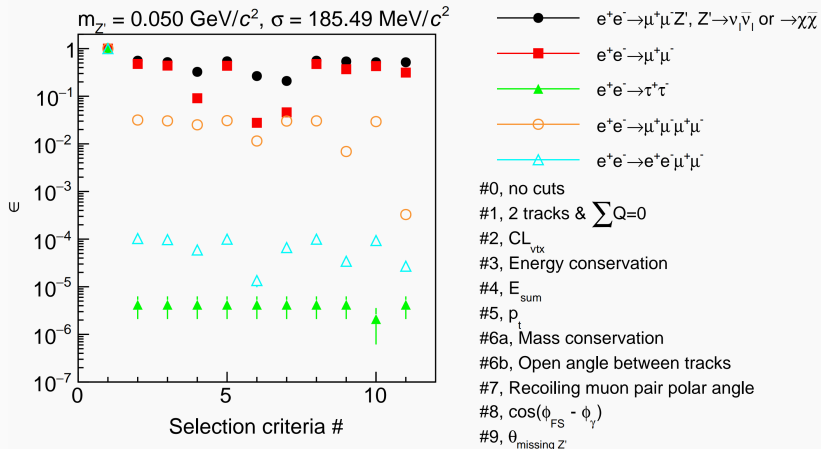
Cut example: ΔE



- How many σ should be taken to maximize FOM?
- On the left
- and on the right



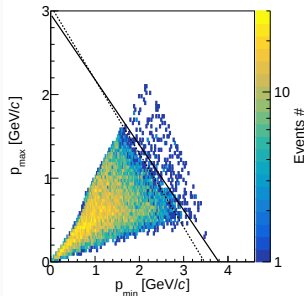
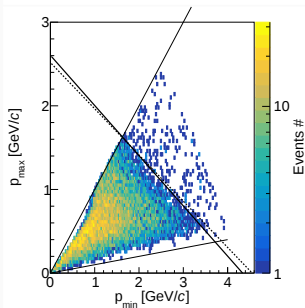
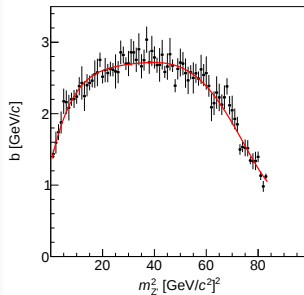
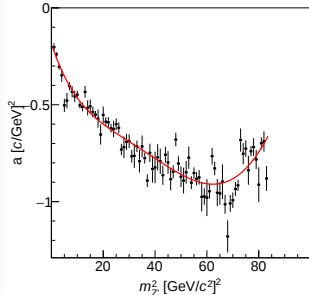
Cut effects on $m_{Z'} = 50 \text{ MeV}/c^2$ $\sigma = 185.5 \text{ MeV}/c^2$



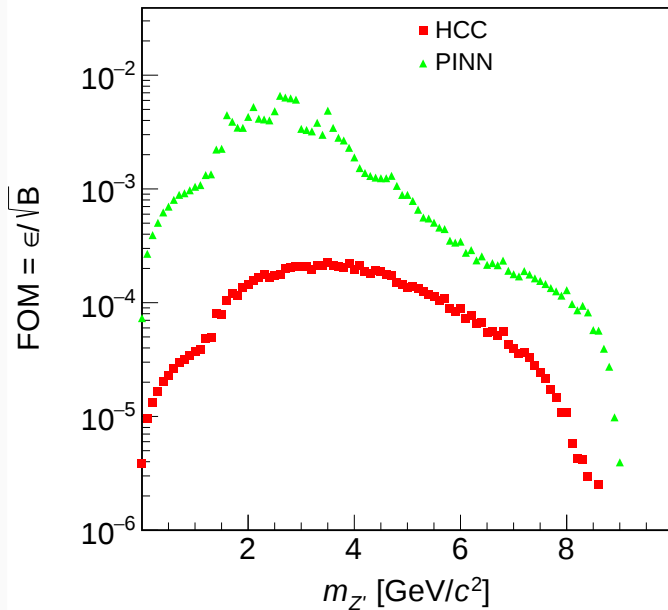
- Missing transverse momentum in cms: $p_t^{*Z'}$
- Maximum momentum muon in cms: $p_{\max}^{*\mu}$
- Minimum momentum muon in cms: $p_{\min}^{*\mu}$
- $\angle \mathbf{p}_t^{*Z'} \mathbf{p}_{\max}^{*\mu} \equiv \alpha_M$
- $\angle \mathbf{p}_t^{*Z'} \mathbf{p}_{\min}^{*\mu} \equiv \alpha_m$
- Projection: $p_t^{*Z'} \sin \alpha_M \equiv p_{\max}$
- Projection: $p_t^{*Z'} \sin \alpha_m \equiv p_{\min}$

Diagonal cut

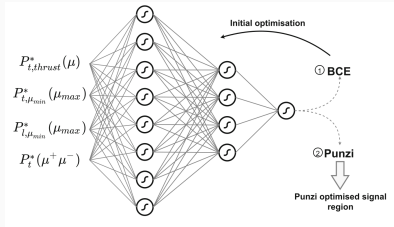
$$e^+e^- \rightarrow \tau^+\tau^-$$



FOM comparison



The Punzi Loss Neural Net selection

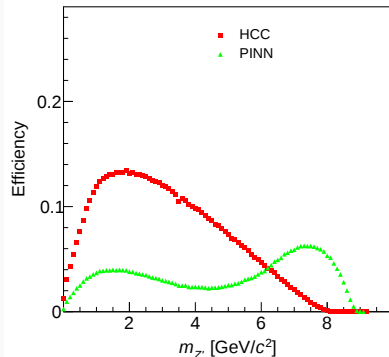
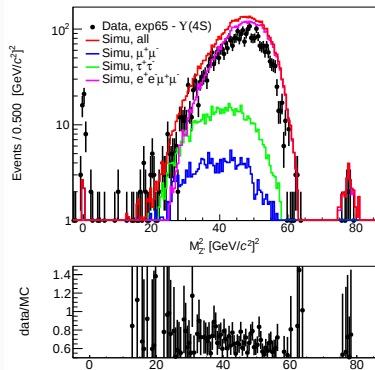


• Layers:

1. input (32 nodes)
2. hidden (64 nodes)
3. hidden (64 nodes)
4. hidden (32 nodes)
5. hidden (16 nodes)
6. hidden (8 nodes)
7. output (1 node)

- $E_{\mu\mu}^*$
- $\cos \theta_{\text{rec}}^*$
- E_{sum}
- $p - \text{value}$
- ΔM
- ΔM_g
- $p_l \min^\mu$
- $p_l \max^\mu$
- p_{thrust}
- $p_l \min^\mu$
- $p_l \max^\mu$
- $p_t^{*Z'} \sin \alpha_M$
- $p_t^{*Z'} \sin \alpha_m$
- $p_t^{\mu\mu}$
- $\angle p_t^{\mu-} p_{\text{thrust}}$
- $\angle p_t^{\mu+} p_{\text{thrust}}$

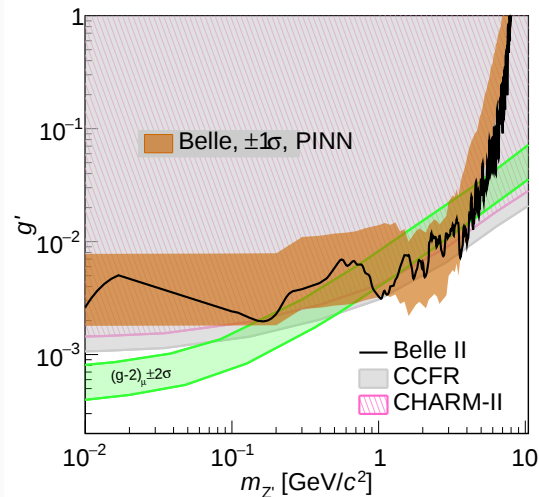
Background sources and detection efficiency



Hand Crafted Cuts (HCC)

Physical Informed Neural Network
(PINN)

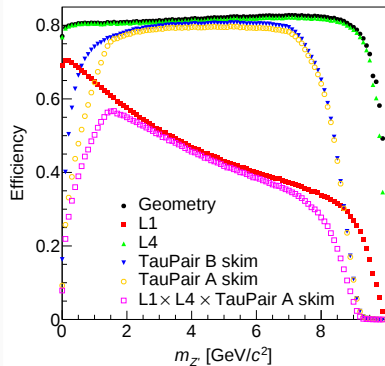
Preliminary Limit in Comparison with Belle II 79.1 fb^{-1}



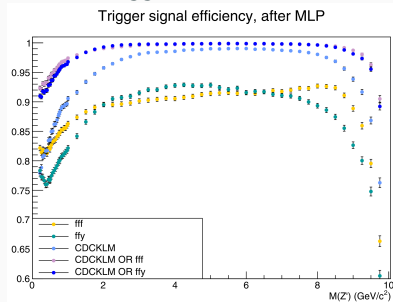
- PINN trained with 60 ab^{-1} MC samples
- Extrapolation on 3% of the total Belle data (exp 65)

Trigger Efficiency (Signal)

Belle Trigger



Belle II Trigger



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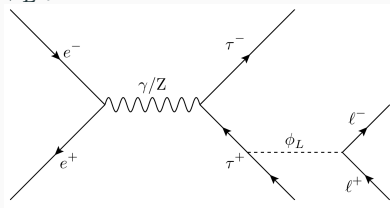
The leptophilic scalar search @ Belle

Summary

What if instead of the vector boson mediator (Z' , A') a leptophilic dark Higgs (ϕ_L) is responsible for $(g - 2)_\mu$?

$$\mathcal{L} = -\xi \sum_\ell \frac{m_\ell}{v} \bar{\ell} \phi_L \ell$$

ϕ_L production



- ℓ are all leptons, and m_ℓ their masses
- ξ is the coupling strength
- $v = 246$ GeV is the vacuum expectation value of the Higgs Field

Signal decay modes (MadGraph 5)

- $e^+e^- \rightarrow \tau^+\tau^-\phi_L$
- 1. $\phi_L \rightarrow e^+e^-$ for $m_{\phi_L} \leq 2m_\mu$
- 2. $\phi_L \rightarrow \mu^+\mu^-$ for $m_{\phi_L} > 2m_\mu(\tau)$

Data sample and backgrounds

- $626 \text{ fb}^{-1} = 562(\Upsilon(4S)) + 64(\Upsilon(4S) - 60 \text{ MeV})$
- 1. $e^+e^- \rightarrow q\bar{q}, q = u, d, s, c$
- 2. $e^+e^- \rightarrow \ell^+\ell^-, \ell = e, \mu, \tau$
- 3. unsimulated $e^+e^- \rightarrow \tau^+\tau^-e(\mu)^+e(\mu)^-$

1. events with 4 tracks
2. transverse distance from IP < 1 cm
3. longitudinal distance from IP < 5 cm
4. net charge of the event is zero
5. at least one track ID is μ or e

Reconstruction

1. ϕ_L from ee or $\mu\mu$ common vertex
2. remaining 2 tracks are daughters from τ

Major background

- $e^+e^- \rightarrow \tau\tau$
- to remove radiative Bhabha ($\mu\mu$) a rectangular cut
 1. $M_{\text{miss}} \in [2, 6] \text{ GeV}/c^2$
 2. $\theta_{\text{miss}}^{\text{CM}} \in [30^\circ, 150^\circ]$

To suppress the surviving background a boosted decision tree (BDT), `GradientBoostingClassifier` from `scikit-learn` assigns 5 BDT scores

SR (Signal Region) Signal Score > 0.5

1. $\phi_L \rightarrow e^+e^-(\mu^+\mu^-)$

GCR (General Control Region)

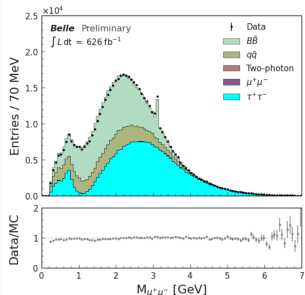
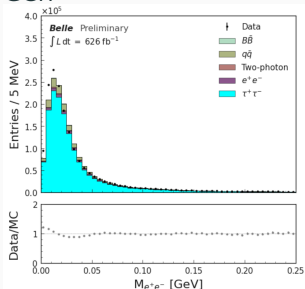
2. $\tau^+\tau^-$

3. $e^+e^-(\mu^+\mu^-)$

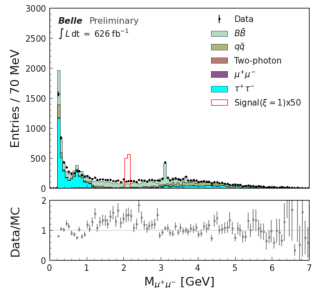
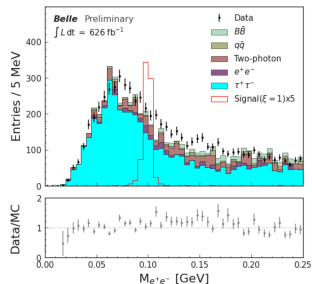
4. $q\bar{q}$

5. $B\bar{B}$

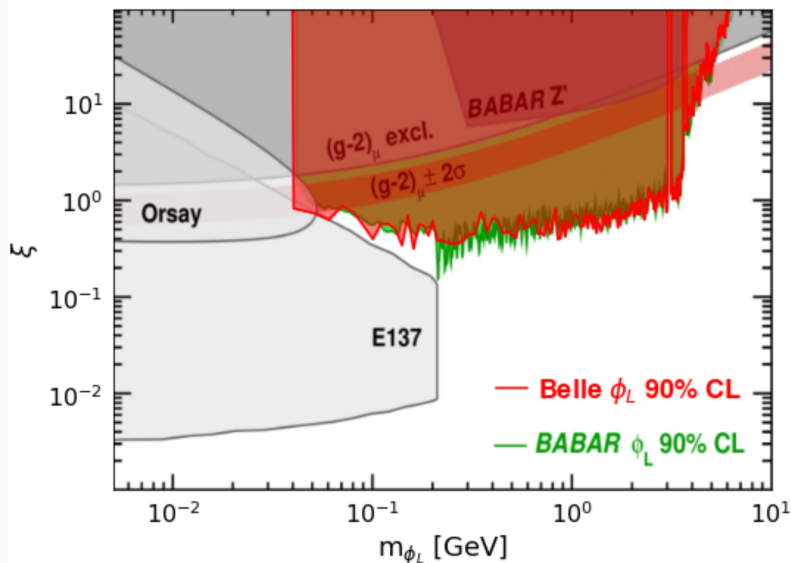
GCR



SR



Results: ξ coupling limit 2207.07476



Experiment and Theory Tension

Extra Leptophilic $U(1)$ gauge boson, Z'

KEKB and Belle

Z' searches in Belle

The invisible Z' search

Punzi Loss Neural Net

The leptophilic scalar search @ Belle

Summary

Leptophilic Z' and ϕ_L outlook

- Finally touching very low mass parameter spaces in Belle
- Belle full data ($\sim 1 \text{ ab}^{-1}$) analysis of the Z' invisible hopefully before winter
 - Currently using Belle II machinery tuned to the Belle background and efficiency